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Nucleation and twinning in tin droplet solidification on single crystal intermetallic compounds

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#### Abstract

$\beta$ Sn nucleation is a key step in the formation of microstructure in electronic solder joints. Here, the heterogeneous nucleation of $\beta S n$ is studied in undercooled tin droplets spread on the facets of various intermetallic compounds (IMCs). Nucleation undercoolings are measured in solidifying droplets and are linked to orientation relationships (ORs) measured by electron backscatter diffraction (EBSD). Preferred ORs developed on all IMCs studied. For the more potent nucleants $\left(\alpha \operatorname{CoSn}_{3}, \operatorname{IrSn}_{4}, \mathrm{PtSn}_{4}, \mathrm{PdSn}_{4}\right)$ the ORs represent relatively simple atomic matches. ORs with lower potency nucleants $\left(\mathrm{Cu}_{6} \mathrm{Sn}_{5}, \mathrm{Ag}_{3} \mathrm{Sn}_{1}, \mathrm{Ni}_{3} \mathrm{Sn}_{4}\right)$ had more complex atomic matches that are explored based on matching of the closest packed atomic rows. $\beta$ Sn solidification twinning is shown to be more complex than has been reported previously: both nucleation on an IMC facet and cyclic twinning of that grain occurred in many droplets on $\mathrm{Cu}_{6} \mathrm{Sn}_{5}, \mathrm{Ag}_{3} \mathrm{Sn}, \mathrm{Ni}_{3} \mathrm{Sn}_{4}$; in all twinned droplets the $\left.<100\right\rangle_{\text {Sn }}$ twinning axis occurred along a direction on the IMC with the lowest linear atomic disregistry; and interrelated cyclic twins formed consisting of up to five rings of cyclic twins all related by shared $\langle 100\rangle_{\text {sn }}$ axes.


## 1 INTRODUCTION

The solidification of electronic solder joints typically occurs from a single $\beta$ Sn nucleation event in a small volume of undercooled liquid. This commonly generates $\beta$ Sn cyclic twins involving $\{101\}$ or $\{301\}$ type twins with $57.2^{\circ}$ and $62.8^{\circ}$ rotations around $<100>$ respectively [1]. In the case of $\mathrm{Sn}-\mathrm{Ag}$ and $\mathrm{Sn}-\mathrm{Ag}-\mathrm{Cu}$, solidification twinning creates beachball and interlaced $\beta$ Sn microstructures [1-5] whereas, in $\mathrm{Sn}-\mathrm{Cu}$ and $\mathrm{Sn}-\mathrm{Cu}-\mathrm{Ni}$, twinning usually creates $\beta$ Sn plate structures [1, 3, 6-9]. Similar twinning also occurs in Sn - Zn solders [10]. It has been shown that twinned solder joints perform differently in service than single-grain joints [11] and that interlaced twinned microstructures can improve creep performance [12] Since these twinned microstructures appear to be related with $\beta$ Sn nucleation and/or the early stages of growth, a deeper understanding of solidification twinning requires fundamental studies on the $\beta$ Sn nucleation process.

Catalysing $\beta$ Sn nucleation has been intensively studied in recent years $[9,10,13-18]$ in order to prevent large and variable nucleation undercoolings $[2,4,19,20]$, excessive dissolution of Cu substrates [21, 22], and large primary intermetallic compounds (IMCs) such as $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$ rods and $\mathrm{Ag}_{3} \mathrm{Sn}$ plates in solder joints [23-27]. This body of work has identified a range of additions that reduce the $\beta$ Sn nucleation undercooling (e.g. $\mathrm{Zn}, \mathrm{Al}, \mathrm{Ti}, \mathrm{Mn}, \mathrm{Co}, \mathrm{Ir}, \mathrm{Pd}, \mathrm{Pt}$ ), and heterogeneous nucleants for $\beta$ Sn have been identified such as the family of transition metal stannides that includes $\alpha \operatorname{CoSn}_{3}, \mathrm{PtSn}_{4}, \mathrm{PdSn}_{4}$, and $\beta 1 r \mathrm{Sn}_{4}$ which are a relatively good lattice match to $\beta$ Sn and can be used to control $\beta$ Sn nucleation and orientation(s) in joints [28].

Furthermore, various researchers have suggested that the common solder $\mathrm{IMCs} \mathrm{Cu}_{6} \mathrm{Sn}_{5}[6$, $29,30], \mathrm{Ag}_{3} \mathrm{Sn}[24,31]$, and $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$ [32] can catalyse $\beta$ Sn nucleation, although there is limited information on the heterogeneous nucleation mechanisms in these cases. Since $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$,
$\mathrm{Ag}_{3} \mathrm{Sn}$, and/or $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$ form prior to $\beta \mathrm{Sn}$ nucleation as primary phases and interfacial reaction layers in most joints, it is important to understand how they influence $\beta S n$ nucleation and twinning.

In this paper, a recently developed experimental approach to studying heterogeneous nucleation [28] is used to gain insights into the nucleation and twinning of $\beta S n$ in electronic soldering. The approach involves solidifying $5-100 \mu \mathrm{~m}$ droplets of Sn on the fluxed facets of IMC single crystals, measuring the nucleation undercooling by DSC and investigating ORs by EBSD without any mounting/grinding/polishing. The key advantages of this technique are that nucleation ORs can be measured directly by EBSD, and the relative simplicity allows hundreds of droplets to be studied and statistically significant datasets to be collected.

This work was conducted to (i) directly test whether $\beta$ Sn can nucleate heterogeneously on a range of intermetallic compounds including the common solder $\mathrm{IMCs}: \mathrm{Cu}_{6} \mathrm{Sn}_{5}, \mathrm{Ni}_{3} \mathrm{Sn}_{4}$, and $\mathrm{Ag}_{3} \mathrm{Sn}$, (ii) compare nucleation on $\mathrm{Cu}_{6} \mathrm{Sn}_{5}, \mathrm{Ni}_{3} \mathrm{Sn}_{4}$, and $\mathrm{Ag}_{3} \mathrm{Sn}$ with that on relatively potent IMC nucleants: $\mathrm{PdSn}_{4}, \mathrm{PtSn}_{4}, \beta \mathrm{IrSn}_{4}$ and $\alpha \mathrm{CoSn}_{3}$, (iii) explore whether preferred nucleation ORs exist between $\beta$ Sn and each of the IMCs, and (iv) gain deeper insights into the link between $\beta$ Sn nucleation and solidification twinning.

## 2 METHODS

$\alpha \operatorname{CoSn}_{3}, \mathrm{PtSn}_{4}, \mathrm{PdSn}_{4}, \mathrm{BlrSn}_{4}, \mathrm{Cu}_{6} \mathrm{Sn}_{5}, \mathrm{Ag}_{3} \mathrm{Sn}$ and $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$ were grown in Sn -rich binary alloy melts and were then extracted as single crystals by selective dissolution of the $\beta$ Sn after solidification. Hypereutectic $\mathrm{Sn}-\mathrm{X}(\mathrm{X}=0.1 \mathrm{Co}, 0.2 \mathrm{Pt}, 0.5 \mathrm{Pd}, 1 \mathrm{Ir}, 1.1 \mathrm{Cu}, 0.5 \mathrm{Ni}, 4 \mathrm{Ag}$ all in wt\%) alloys were used, prepared by holding the specified amounts of $99.9 \%$ purity tin and $99.9 \%$ X in evacuated quartz ampoules for 168 h at $1200^{\circ} \mathrm{C}$. Alloys were reheated to $400{ }^{\circ} \mathrm{C}$ and cooled at $0.004 \mathrm{~K} / \mathrm{s}$ to grow the desired IMCs. Finally, to dissolve $\beta \mathrm{Sn}$ and release the single crystal IMCs, a solution of $5 \% \mathrm{NaOH}$ and $3.5 \%$ ortho-nitrophenol in distilled water was used.

To wet and spread liquid tin droplets on the facets of the IMCs, particles of $99.9 \% \mathrm{Sn}$ powder with size $\sim 5-100 \mu$ mere placed on the single crystal IMCs covered with a $\mathrm{ZnCl}_{2}$ $\mathrm{NH}_{4} \mathrm{Cl}$ based soldering flux (Stay-Clean ${ }^{\circledR}$, HARRIS), and reflowed in a forced air convection reflow oven with thermal profile of heating rate $1 \mathrm{~K} / \mathrm{s}$, peak temperature $240^{\circ} \mathrm{C}$, liquid time ~80 s, and cooling rate ${ }^{\sim} 3 \mathrm{~K} / \mathrm{s}$. Flux residues were cleaned off in ethanol in an ultrasonic bath and then samples were reflowed again in a Mettler Toledo DSC under a $\mathrm{N}_{2}$ atmosphere. The heating rate was $0.17 \mathrm{~K} / \mathrm{s}$, the maximum temperature was $240^{\circ} \mathrm{C}$ and the cooling rate was $0.33 \mathrm{~K} / \mathrm{s}$. To measure $\beta \mathrm{Sn}$ nucleation undercoolings, a sample (a single Sn droplet of size ${ }^{\sim} 40-75 \mu \mathrm{~m}$ on an IMC facet) was cycled $5-20$ times in the DSC. The $\beta$ Sn nucleation undercooling was defined as the eutectic melting onset on heating minus the solidification onset on cooling. Typical DSC heating and cooling curves for single $\sim 40 \mu \mathrm{~m}$ Sn droplets are shown in Supplementary Information Figure 1. 4-9 samples were measured separately for each IMC phase resulting in at least 50 undercooling values for each IMC. In separate experiments, numerous $S n$ droplets were solidified on IMC facets using the same DSC thermal profile to generate multiple droplets on IMC facets for EBSD studies.

Figure 1 overviews the droplet technique used here. Figure $1(A)$ is a schematic $\mathrm{Sn}-\mathrm{X}(\mathrm{X}=\mathrm{Co}$, $\mathrm{Pt}, \mathrm{Pd}, \mathrm{Ir}, \mathrm{Cu}, \mathrm{Ni})$ phase diagram at the Sn -rich corner; the phase at the right side is the IMC studied for each Sn-X system. Note that, in all cases, the IMCs studied are the most Sn-rich compounds in the binary $\mathrm{Sn}-\mathrm{X}$ system. When a Sn droplet wets and spreads on a single crystal IMC at the peak temperature of $240^{\circ} \mathrm{C}$, the liquid must dissolve some of the IMC to increase the concentration of X in the liquid to the equilibrium value of $C_{L}{ }^{240}$. During subsequent solidification, the possible mechanisms for $\beta$ Sn nucleation are summarised in Figure $1(B)$ as: 1) homogeneous nucleation; 2) heterogeneous nucleation on the IMC, which can be 2a) heterogeneous nucleation on the flat facet or $2 b$ ) heterogeneous nucleation on growth ledges or other surface defects of the IMC [33, 34]; and/or 3) heterogeneous nucleation on other phases such as primary IMCs, impurity phases, or oxides.

To explore the active mechanisms and resulting growth microstructures, analytical scanning electron microscopy (SEM) was performed in a Zeiss AURIGA field-emission gun-SEM (Carl Zeiss, Oberkochen, Germany) equipped with an Oxford Instruments INCA x-sight energy dispersive x-ray (EDX) detector (Oxford Instruments, Oxfordshire, UK) and an e-Flash Bruker electron backscatter diffraction (EBSD) detector (Bruker AXS Inc., Fitchburg, WI). Each IMC has been identified by detailed XRD studies previously [35-42] and were confirmed here by combining EDX with EBSD. The crystal structures used for EBSD indexing are summarised in Table 1. Note that $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$ has multiple polymorphs [43-46] which could all be fit to the EBSD patterns and that the high-temperature hexagonal $\eta \mathrm{Cu}_{6} \mathrm{Sn}_{5}$ [40] was used for EBSD indexing because it is the stable phase at the $\beta$ Sn nucleation temperatures. The microstructures and orientation relationships (ORs) between the $\beta$ Sn droplets and IMC facets were measured by EBSD directly on the IMCs and $\beta$ Sn droplets without further sample preparation.

To study the surface of the partially-dissolved IMC (Figure 1 (B)), some Sn droplets on IMCs were etched in $5 \% \mathrm{NaOH}$ and $3.5 \%$ orthonitrophenol in $\mathrm{H}_{2} \mathrm{O}$ to remove all $\beta$ Sn. The IMC surface was then studied by SEM imaging. 3D tomographs of some droplets were obtained by slice \& view using a focused ion beam (FIB) of 2.8 nA and a slice distance of 200 nm in a FEI Helios Nanolab (FEI, Hillsboro, Oregon). Raw images were processed using ImageJ and Matlab, and then Avizo 7 was used for 3D reconstruction and analysis of the droplet and IMC.

## 3 RESULTS AND DISCUSSION

### 3.1 Nucleation of $\beta \mathbf{S n}$ on $\mathrm{PdSn}_{4}, \alpha \operatorname{CoSn}_{3}, \mathrm{PtSn}_{4}$, and $\beta 1 r \mathrm{Sn}_{4}$

SE-SEM images of typical single crystals of $\alpha \mathrm{CoSn}_{3}, \mathrm{PtSn}_{4}, \mathrm{PdSn}_{4}$, and $\beta \mathrm{IrSn}_{4}$ are shown in Figure 2 (A). All have a similar morphology of near-square plates which has been described as tile-like previously [4, 28, 47]. The largest facet of these orthorhombic or tetragonal single crystal IMCs are identified as $(100)_{\alpha \operatorname{CoSn3}},(010)_{p t S n 4},(010)_{\text {PaSn4 }}$, and $(001)_{\beta 1 r S n 4}$, by EBSD as shown in Figure 2 (A) where the unit cell orientations have been plotted from the measured Euler angles. Note that these phases have been assigned different space groups by different authors and the indexing in this work refers to the crystallographic descriptions in Table 1.

A typical Sn droplet solidified on a facet is shown in Figure 2 (B) using $\alpha \mathrm{CoSn}_{3}$ as an example. It can be seen that the liquid Sn wet and spread into a hemispherical cap before solidification. Figure $2(\mathrm{C})$ shows 5 typical Sn droplets on a $\mathrm{PdSn}_{4}(\mathrm{O} 010)$ facet. Orientations of the $\beta S n$ and $\mathrm{PdSn}_{4}$ were measured by EBSD and are shown as wireframe unit cells in Figure 2 (C) and by the EBSD IPF-Y map in Figure 2 (D). All $\beta$ Sn grains contain a single orientation that can be classified into two types: the orientation shown by green unit cell wireframes and that shown by the orange wireframe. The $\mathrm{PdSn}_{4}$ wireframe unit cell is plotted in black in Figure 2 (C). The two $\beta$ Sn orientations correspond to two ORs with $\mathrm{PdSn}_{4}$ respectively:

$$
\begin{array}{ll}
(010)_{P d S n 4}| |(100)_{S n} \text { with }[100]_{P d S n 4} \|[001]_{S_{n}} & \text { Eq. } 1 \\
(010)_{P d S n 4} \|(100)_{S_{n}} \text { with }[001]_{P d S n 4} \|[001]_{S n} & \text { Eq. } 2
\end{array}
$$

These two ORs are plotted in pole figures in Figure $2(\mathrm{E})$ and are indicated by the common circles, squares, and triangles of the same colour as the $\beta$ Sn unit cell wireframes in Figure 2 (C) and IPF-Y map in Figure 2 (D).

The $\beta$ Sn orientations of 117 droplets on $\mathrm{PdSn}_{4}$ crystals are summarized into a stereographic projection in Figure 2 (F) with the IMC facet-normal at the centre. Each droplet solidified into a single $\beta S n$ orientation and all measured $\beta$ Sn orientations have been rotated towards one representative orientation by exploiting symmetry. The mean $\pm$ standard deviation (measured from all EBSD points of different droplets/grains) of three pairs of parallel planes are given. In all cases, the $\beta$ Sn had one of the ORs with $\mathrm{PdSn}_{4}$ in Eq. 1 and 2 with angular deviations $<4^{\circ}$.

Similar investigations were performed on Sn droplets on $\alpha \mathrm{CoSn}_{3}, \mathrm{PtSn}_{4}$, and $\beta 1 r \mathrm{Sn}_{4}$ plates in reference [28]. The $\mathrm{PdSn}_{4}$ data and the data from reference [28] are combined into a single dataset in Table 2 which summarises the EBSD-measured ORs and the statistics of occurrence of each OR. As shown in Table 2, all droplets had highly reproducible ORs on these IMCs.

The mean nucleation undercooling of $\sim 40-75 \mu \mathrm{~m}$ Sn droplets on $\alpha \mathrm{CoSn}_{3}, \mathrm{PtSn}_{4}, \mathrm{PdSn}_{4}$, and $\beta \mathrm{IrSn}_{4}$ is shown by the 'grey' bars in Figure 3. There are at least 50 measurements for each case. Note that this data comes from droplets with a range of diameters of $\sim 35 \mu \mathrm{~m}$ ( $\sim 40-75$ $\mu \mathrm{m}$ ) which is likely to influence the nucleation undercooling values. However, the size distribution of the droplets in each case (freestanding or on IMCs) are the same since droplets are selected from the same powder. Therefore, the nucleation undercoolings of different cases are comparable. It is clear that droplets on these four IMCs show substantially suppressed nucleation undercooling when comparing with $\sim 40-75 \mu \mathrm{~m}$ freestanding Sn droplets (labelled ' Sn ball'). Combining the suppressed undercooling and the reproducible OR(s), it can be inferred that $\beta S n$ nucleated heterogeneously on the IMC facet in every droplet by mechanism 2a or 2 b in Figure $1(\mathrm{~B})$. At the same time, it is striking in

Figure 3 that the undercoolings are large relative to most studies of potent heterogeneous nucleants. In large part, this is due to the small size of the Sn droplets since previous studies on large ( 60 g ) samples measured nucleation undercoolings of less than 1 K for alloys containing $\alpha \operatorname{CoSn}_{3}, \beta 1 \mathrm{HSn}_{4}, \mathrm{PdSn}_{4}$ or $\mathrm{PtSn}_{4}$ [10]. This size effect can be seen further in Figure 3 where undercooling data are also shown for $\sim 550 \mu \mathrm{~m}$ balls made from the $7 \mathrm{Sn}-\mathrm{X}$ hypereutectic alloys.

### 3.2 Nucleation of $\beta \mathrm{Sn}$ on $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$

A typical $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$ single crystal is shown in Figure $4(\mathrm{~A})$ and (B). It has a hexagonal rod-like morphology. EBSD analysis showed that its main facets and the direction along the rod are $\{10 \overline{10}\}_{C u 65 n 5}$ and $[0001]_{c u 65 n 5}$ respectively as shown by the wireframe unit cell and Euler angles on Figure 4 (A) and labels on Figure 4 (B). This morphology is consistent with past work [48-51].

Figure 4 (C) shows 8 typical Sn droplets on a ( $10 \overline{10})_{\text {Cu6Sn5 }}$ facet with unit cell wireframes superimposed. As shown in Figure 4 (C) and the EBSD IPF-X map in Figure 4 (D), these $\beta$ Sn droplets are either single-grain (droplets 2 and 6) or contain multiple grains (droplets 1, 3, 4, 5, 7 and 8 ).

EBSD revealed that all multiple-grain Sn droplets contain all or some $\beta$ Sn grains that are solidification twins (i.e. $\sim 60^{\circ}$ rotations about a shared <100> as discussed in [1]) as indicated by the same coloured $<100>$ axes on the $\beta$ Sn unit cells in Figure 4 (C). Some of the multiplegrain Sn droplets (droplets $3,4,5$ and 8 ) have $\beta$ Sn grains that are all interrelated with each other by twinning (e.g. droplet 3), while others do not (e.g. droplet 1 contains two grains related by twinning and a third independent grain).

Droplet 3 is shown in more detail in Figure 5 as a typical example of multiple interrelated cyclic twins. This Sn droplet contains grains that are twinned about three different <100> axes, indicated by red-twins i, green-twins ii, and blue-twins iii. Cyclic twins i and ii share a common grain ' 1 ' and cyclic twins $i$ and iii share a common grain ' 3 ', as shown in Figure 5 (A). This can also be seen in the $<100>$ pole figure of $\beta S n$ in Figure $5(B)$, in which $<100>$ poles of different grains are numbered and dashed lines indicate the trace of the common $\{100\}$.

Note that the common axes (dashed circles) of cyclic twins ii and iii are in the common plane of cyclic twins i (Figure 5 (B)). These interrelated twins are further shown in Figure 5 (C) by plotting the unit cells of the 5 orientations from the measured Euler angles and translating the unit cells to make clear the cyclic twinning. The common $\{100\}$ and $<100>$ of each cyclic twins are shaded red, green and blue for cyclic twins i, ii and iii respectively. The dashed unit cell in green-twins ii was not measured experimentally but is shown for clarity. Each cyclic twin is shown twice, first arranged as $\{101\}$ cyclic twins and then translated into $\{301\}$ cyclic twins to depict the different spatial relationships.

Figure 5 (D) quantifies the angular deviation between the <100> twinning axes $\left(\delta_{i j}\right)$, the misorientation between the other $\langle 100\rangle\left(\omega_{i j}\right)$, and the in-grain misorientation $\left(m_{i}\right)$ for each of grains 1, 2, and 3 in twins i (Figure 5 (A)). $\delta$ and $\omega$ are defined schematically in Figure 5 (C). The angles in Figure 5 (D) are the mean $\pm$ the standard deviation using the Euler angles from all points in grains 1, 2, and 3 in the EBSD map. For a perfect $\mathrm{twin}, \delta_{\mathrm{ij}}=0, \mathrm{~m}_{\mathrm{ij}}=0$, and $\omega_{\mathrm{ij}}=57.2^{\circ}$ for $\{101\}$ twins and $62.8^{\circ}$ for $\{301\}$ twins. For grains 1,2 , and $3, \delta_{\mathrm{ij}}$ and $\mathrm{m}_{\mathrm{ij}}$ are $<3^{\circ}$ in all cases and the standard deviations in $\omega_{\mathrm{ij}}$ are $\leq 1^{\circ}$ (Figure 5 (D)). These values are significantly smaller than in BGA-scale balls/joints [1, 4, 8], where typical values are $\delta_{\mathrm{ij}}=4^{\circ}$, $m_{\mathrm{ii}}=6^{\circ}$, and the typical standard deviation in $\omega_{\mathrm{ij}}$ is $6^{\circ}$ [4]. This is an advantage of the technique used here where (i) the small droplet size gives little growth distance in which angular deviations can develop and (ii) the absence of grinding/polishing prevents $\beta$ Sn deformation. By comparing the values of $\omega_{\mathrm{ij}}$ in Figure 5 (D) and the histograms of misorientation angle in Figure 5 (E), it can be seen that the misorientation distribution between grains 1, 2, and 3 can be distinctly separated with two peaks consistent with \{101\} twinning ( $57.2^{\circ}$ ) and one peak close to $\{301\}$ twinning ( $62.8^{\circ}$ ) [1]. Examination of multiple
droplets on $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$ showed a similar result: two grain pairs are misorientated close to one twinning angle and the other is misoriented close to the other twinning angle. Despite this, for simplicity, in Figure 5 and subsequent Figures cyclic twinning is plotted as all \{101\} twinning and/or all $\{301\}$ twinning.

Some $\beta$ Sn grains (labelled with red unit cell wireframes in droplets in Figure 4 (C)) had a preferred OR with $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$. Typical examples are shown for droplets 4 and 6 in Figure 4 (C) whose pole figures and that of $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$ are shown in Figure $4(\mathrm{E})$. The OR is indicated by common circles, triangles, diamonds, and squares in the $\beta \mathrm{Sn}$ and $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$ pole figures. There are multiple near-parallel pairs of planes for both droplets 4 and 6 and, in both cases, the OR with $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$ can be written as Eq. 3:

$$
\begin{equation*}
(10 \overline{1} 0)_{C u 6 S n 5}| |(111)_{S_{n}} \text { and }[0001]_{C u 6 S n 5}| |[11 \overline{2}]_{\mathrm{Sn}} \tag{Eq. 3}
\end{equation*}
$$

Among 60 EBSD measured Sn droplets, 37 featured $\beta$ Sn grains with the above measured OR (Table 2 and 3) and the orientations of these grains with respect to $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$ are summarised into the stereographic projection of 10 near-parallel planes and 16 near-parallel directions in Figure $4(F)$ and (G). The mean misorientation for each pair of near-parallel planes is $<\sim 3^{\circ}$.

Note by comparing the pole figures of $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$ in Figure $4(\mathrm{E})$, that $\beta \mathrm{Sn}$ grains in droplet 6 and droplet 4 have a different plane parallel with the $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$ facet (indicated by the triangles in Figure $4(\mathrm{E})$ ); one is $\{241\}_{\mathrm{sn}}$, the other is $\{111\}_{\mathrm{sn}}$. These planes are indicated by bold font in Figure 4 (F). Table 2 shows that 5 out of 37 Sn droplets had $\{111\}_{S_{n}}$ parallel with the $\{10 \overline{1} 0\}_{C u 6 S n 5}$ facet and the remaining 32 had $\{241\}_{S_{n}}$. The atomic matching associated with this OR and interface planes are discussed in our previous paper [6] and, therefore, are not discussed further here.

Table 3 summarises the $\beta \mathrm{Sn}$ microstructures and ORs in all 60 droplets on $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$. It can be inferred that there was one $\beta$ Sn nucleation event in each single-grain and twinned droplet (45 out of 60 droplets), and multiple $\beta S n$ nucleation events in each droplet with multiple independent grains (15 out of 60). The presence or absence of an OR with $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$ provides insights into the nucleation mechanisms: $\beta$ Sn most likely nucleated heterogeneously only on $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$ in the $28 / 60$ single-grain and twinned droplets with the OR in Eq. 3 by mechanism 2a or 2 b in Figure 1 (B); in the 9/60 multiple-independent-grain droplets with the OR in Eq. 3 $\beta$ Sn nucleated by both mechanisms $2 a / 2 b$ and 3 in Figure $1(B)$; and the remaining 23/60 droplets with no reproducible OR most likely nucleated on other phases (or geometrically catalytic sites such as grooves and ridges in the oxide layer) that are more potent than $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$ by mechanism 3 in Figure 1 (B).

The different nucleation mechanisms in droplets on $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$ indicate that there was competition among nucleation sites (i.e. between mechanism 2 and 3 in Figure 1 (B)). Examining the nucleation undercooling for $\beta \mathrm{Sn}$ on $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$ in Figure 3, it can be seen that the mean undercooling on $\mathrm{Cu}_{6} \mathrm{Sn}_{5}(53 \mathrm{~K})$ is only slightly less than with no IMC substrate ( 58 K ) and that there is overlap over a wide range of undercooling values. From this, it can be seen that the $\{10 \overline{1} 0\}$ facet of $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$ is only weakly catalytic to $\beta \mathrm{Sn}$ nucleation and, in some droplets, other sites that are naturally present in the droplet were more potent than $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$.

### 3.3 Nucleation of $\beta \mathrm{Sn}$ on $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$

A typical $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$ single crystal is shown in Figure $6(\mathrm{~A})$ and (B). EBSD measurements showed that there are three main facets: $(100)_{\mathrm{NiSSn4} 4}(\overline{2} 01)_{\mathrm{Ni3Sn} 4}$, and $(001)_{\mathrm{Ni3Sn} 4}$ and the direction along the rod is $[010]_{\text {Ni3Sn4 }}$. These are consistent with ref. [52].

Typical examples of Sn droplets on a (100) facet of $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$ are shown in Figure $6(\mathrm{C})$ and the measured EBSD IPF-X map of these droplets is shown in Figure 6 (D). Similar to the Sn droplets on $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$, single-grain (e.g. droplets 1, 5, and 6), simple-twins (droplets 2 and 3), interrelated-twins (e.g. droplets 4 and 7), and multiple-independent-grain microstructures were all found in droplets on the different facets of $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$. Unit cell wireframes are superimposed in Figure 6 (C) to show grain orientations, and green, pink, and yellow are used to indicate the twinning axes. The interrelated twins had similar features to those shown in Figure 5 for droplets on $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$. Twinning angles could be clearly separated with one/two close to $\{101\}$ twinning and the other(s) close to $\{301\}$ twinning.

Some $\beta$ Sn grains in droplets on the different facets of $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$ had reproducible ORs with the $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$. In Figure $6(\mathrm{C})$, those grains with the OR are indicated by red unit cell wireframes. The OR between a typical red-wireframe $\beta$ Sn grain (droplet 1) and the $\{100\}$ facet of $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$ is shown in the pole figures in Figure 6 (E) where near-parallel planes are indicated by common circles, triangles, and squares. The $\beta$ Sn plane parallel to the $\{100\}_{\mathrm{Ni} 3 \mathrm{~S}_{n} 4}$ facet is \{241\}, as shown by the superimposed triangles. This OR can be written as Eq. 4:

$$
\begin{equation*}
(100)_{\mathrm{Ni3Sn} 4}| |(\overline{2} \overline{4} \overline{1})_{\mathrm{sn}} \text { and }[0 \overline{1} 0]_{\mathrm{Ni3Sn} 4}| |[10 \overline{2}]_{\mathrm{S}_{\mathrm{n}}} \tag{Eq. 4}
\end{equation*}
$$

The same OR was measured in Sn droplets on $\{\overline{2} 01\}_{\mathrm{Ni} 3 S_{n 4}}$ and $\{001\}_{\mathrm{Ni} 35 n 4}$ facets, indicating that the OR is independent of the facet plane of $\mathrm{Ni}_{3} \mathrm{Sn}_{4} . \beta \mathrm{Sn}$ grains showing the above OR
were found in 112 out of 179 droplets (Table 2), and their orientations are summarised into a pole figure with respect to $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$ in Figure 6 (F). 12 pairs of near-parallel planes are plotted, and the scalar misorientation angle between the planes (mean $\pm$ standard deviation from all EBSD points) is shown for each. The three $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$ facets and their parallel planes in $\beta$ Sn are indicated by bold font. Figure $6(\mathrm{G})$ is a similar stereographic projection plotting 8 pairs of near-parallel directions.

Figure 7 (A) is a plot of the OR in Eq. 4 and the interfaces on the three facets. The red shaded planes are the closest packed $\{100\}_{\text {Sn }}$ (Table 4) which is parallel with $\{\overline{4} 01\}_{\text {Ni3Sn } 4}$ and the d -spacing mismatch of them is $\sim 1 \%$. The three facets share a common parallel direction, $\left.\langle 010\rangle_{\text {Ni3sn } 4}| |<102\right\rangle_{\text {sn }}$. The planar atomic matches of the interfaces on the three facets are shown in Figure 7 (B). Red atoms represent Sn in $\beta \mathrm{Sn}$, gray atoms are Sn in $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$, and transparent atoms have been projected into the plane. It can be seen that there is reasonable matching on some sites but the planar matches are not excellent and all the interface planes have at least one phase with zig-zag character as indicated by transparent atoms. The percentage occurrence of the OR (Eq. 4) on each facet is shown on Figure 7 (B), which is calculated from Table 2. Based on this, it might be expected that the $\beta \mathrm{Sn}-\mathrm{Ni}_{3} \mathrm{Sn}_{4}$ interfacial energy on these facets for this OR follows the order (001)>( $\overline{2} 01)>(100)$.

At the same time, note that the nucleation plane does not need to be the macroscopic facet plane and could be another surface plane created by ledges etc. on the facet surface, as shown schematically in Figure 1 (B). To explore the lattice match further, we consider Zhang and Kelly's Edge-to-Edge theory [53, 54] which predicts that the lowest energy heterointerface should involve the closest or nearly closest packed planes in the two crystals meeting edge-to-edge at the interface with a good atomic match and that these planes
need not be parallel. With this configuration, some of the closest or nearly closest packed atomic rows (i.e. directions) should be parallel and arranged so as to minimise the linear disregistry along these rows. Table 4 shows a rank ordered list of (i) the planar atomic density and (ii) the interatomic distances along atomic rows in $\beta \mathrm{Sn}$ and $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$. Note that many planes and directions have zig-zag character in these phases and, therefore, densities and spacings have been calculated by projecting atoms into the planes or rows. Comparing Table 4 and Figure $6(F)$ and (G) it can be seen that the two closest packed rows in $\beta S n[0 \overline{1} 0]$, [100] are parallel with the $2^{\text {nd }}$ and $3^{\text {rd }}$ closest packed rows in $\mathrm{Ni}_{3} \mathrm{Sn}_{4}[10 \overline{1}],[\overline{1} \overline{5} \overline{4}]$ and, in each case, the linear disregistry is $\sim 1 \%$. These pairs of directions lie in the planes $(1 \overline{1} 1)_{\text {ni3Sn4 }}| |$ $(00 \overline{1})_{\text {Sn }}$. Similarly, $[0 \overline{1} 0]_{\text {Ni3Sn4 }}| |[10 \overline{2}]_{\text {Sn }}\left(5^{\text {th }}\right.$ II $4^{\text {th }}$ with $6 \%$ linear disregistry $)$ and $[10 \overline{1}]_{\text {Ni3Sn } 4}$ || $[0 \overline{1} 0]_{S n}\left(2^{\text {nd }}| | 1^{\text {st }}\right.$ with $\sim 1 \%$ disregistry $)$ and lie in the planes $(101)_{\text {Ni3Sn4 }}| |(\overline{2} 0 \overline{1})_{\text {Sn }}$. However, these planes are complex zig-zag planes so the planar lattice match is not as good as it appears from an analysis of rows. From this analysis of parallel rows and planes, it can be seen that the Edge-to-Edge theory [53,54] is in reasonable agreement with our measured OR although the optimum interface plane is unclear.

Figure 3 shows that the nucleation undercooling for $\beta \mathrm{Sn}$ in droplets on $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$ is significantly smaller than on $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$ and $\mathrm{Ag}_{3} \mathrm{Sn}$, indicating that $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$ is more catalytic. This is consistent with the atomic matches of $\mathrm{Sn} / \mathrm{Cu}_{6} \mathrm{Sn}_{5}$ as shown in ref. [6] and in Figure 7 (B), i.e. the atomic matches on the (100) and ( 201 ) $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$ facets are significantly better than those of $(1 \overline{1} 00)_{C u 65 n 5} \|(\overline{2} 41)_{S_{n}}$ and $(10 \overline{1} 0)_{C u 6 S n 5} \|(111)_{S n}$, where the planar densities are quite different for $\beta \mathrm{Sn}$ and $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$ as shown in Ref. [6]. At the same time, the relatively high undercooling in droplets on $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$ (compared with the $\alpha \mathrm{CoSn}_{3}, \mathrm{PtSn}_{4}, \mathrm{PdSn}_{4}$, and $\beta 1 \mathrm{ISn}_{4}$ ) is
likely to be due to the lack of a simple match in an interfacial plane (Figure 7 (B)) and their zig-zag features.

Table 3 and 2 summarise the $\beta$ Sn microstructures and ORs in all 179 droplets on $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$. It can be inferred that there was a single $\beta$ Sn nucleation event in the single-grain and twinned droplets (159 out of 179) on the three facets of $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$, and multiple $\beta \mathrm{Sn}$ nucleation events in the droplets with multiple independent grains (20 out of 179). 104 out of 179 single-grain and twinned droplets had the $O R$ in Eq. 4 which indicates that $\beta S n$ nucleated heterogeneously only on $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$ in these droplets by mechanism 2a or 2b in Figure 1 (B). 8/179 multiple-independent-grains droplets had both a grain with the OR (Eq. 4) and independent grains, showing that nucleation occurred on both the $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$ and on other phases/sites in the same droplet (i.e. by both mechanisms 2 and 3 in Figure 1 (B)). In the remaining 67/179 droplets with no reproducible OR, it is likely that $\beta$ Sn nucleation happened on other phases/sites by mechanism 3 in Figure 1 (B). Thus, while $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$ is more catalytic to $\beta \mathrm{Sn}$ nucleation than $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$ (Figure 3), there was competition between nucleation sites on $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$ and $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$ did not always act as a heterogeneous nucleant in the small droplets of this study. Table 2 highlights a stark contrast between $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$ and $\mathrm{PtSn}_{4}$, where the latter caused only a slightly smaller nucleation undercooling but always acted as a heterogeneous nucleant.

### 3.4 Nucleation of $\boldsymbol{\beta S n}$ on $\mathrm{Ag}_{3} \mathrm{Sn}$

A typical $\mathrm{Ag}_{3} \mathrm{Sn}$ single crystal is shown in Figure $8(\mathrm{~A})$ and (B). It has a thin plate morphology and EBSD analysis identified the main facet to be $(001)_{\mathrm{Ag} 35 \mathrm{n}}$ and the edge directions to be $[100]_{A B 3 S n}$ and $[010]_{A g 3 S n}$. The measurements here are consistent with ref.[52, 55].

Figure 8 (C) shows 13 typical Sn droplets on a ( 001$)_{\mathrm{Ag} 3 \mathrm{Sn}}$ facet, and $\beta$ Sn orientations in these droplets are shown in the IPF-Z map in Figure 8 (D). Unit cell wireframes are superimposed to show the grain orientations, and green and yellow axes indicate different <100> twinning axes. Single-grain (e.g. droplets 9 and 11), simple-twins (e.g. droplet 13), interlaced-twins (e.g. droplets 1-8), interrelated-twins (e.g. droplet 10), and multiple-independent-grains (e.g. droplet 12) all formed in Sn droplets on $\mathrm{Ag}_{3} \mathrm{Sn}$. Interrelated twins in droplets on $\mathrm{Ag}_{3} \mathrm{Sn}$ are similar to those in droplets on $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$ (Figure 5) and $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$. Interlaced twins (droplets 1 to 8 in Figure $8(\mathrm{C})$ ) were relatively common in droplets on $\mathrm{Ag}_{3} \mathrm{Sn}$. A typical example is shown in Figure 9 (A), in which the $\beta$ Sn grains exhibit an interlaced grain structure rather than distinct separate twin grains. In Figure 9 (D), the measured in-grain misorienation $\left(m_{i}\right)$ and the deviation angles between the twinning axis $\left(\delta_{\mathrm{ij}}\right)$ in these typical interlaced twins are slightly larger than the corresponding ones in twin i in the droplet on $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$ shown in Figure 5 (D). The rotation angles $\omega_{\mathrm{ij}}$ also have relatively large standard deviations, and the misorientation angles in Figure 9 (E) show substantially overlapping distributions with mean values close to $60^{\circ}$. Therefore, we cannot clarify whether they are $\{101\} /\{301\}$ twinning [1]. This uncertainty occurred in most twinned droplets on $\mathrm{Ag}_{3} \mathrm{Sn}$ and is significantly different to twinned droplets on $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$ and $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$ which were typically similar to Figure 5 (E).

EBSD measurements indicate that some $\beta$ Sn grains had a reproducible OR with the $\mathrm{Ag}_{3} \mathrm{Sn}$. Examples of such grains are denoted by red wireframes in Figure 8 (C). Pole figures of the 'red' $\beta$ Sn grain in droplet 8 and $\mathrm{Ag}_{3} \mathrm{Sn}$ are shown in Figure 8 (E). This OR is:

$$
(001)_{\mathrm{Ag} 3 \mathrm{~S}}| |(001)_{\mathrm{Sn}} \text { and }[010]_{\mathrm{Ag} 3 \mathrm{Sn}}| |[010]_{\mathrm{Sn}}
$$

The red-wireframe grains were commonly related with another one or two grains by $\sim 60^{\circ}$ twins (e.g. grains with blue wireframes in Figure 8 (C)), where the $\langle 010\rangle_{\text {sn }}$ twinning axis was always parallel with $[010]_{\mathrm{Ag} 35 \mathrm{n}}$. Therefore, these blue-wireframe grains also have a reproducible OR with the $\mathrm{Ag}_{3} \mathrm{Sn}$ as shown by the ' 8 All $\beta \mathrm{Sn}^{\prime}$ ' pole figures in Figure 8 (E). The OR between the twinned $\beta \mathrm{Sn}$ grains and $\mathrm{Ag}_{3} \mathrm{Sn}$ is:

$$
(001)_{\mathrm{Ag}_{\mathrm{g}} 3 \mathrm{n}}| |(301)_{\mathrm{s}_{n}} \text { and }[010]_{\mathrm{Ag} 35 \mathrm{Sn}| |[010]_{\mathrm{sn}}}
$$

To clarify these ORs, Figure 9 (C) exhibits the relative orientations of the three $\beta$ Sn grains and the $\mathrm{Ag}_{3} \mathrm{Sn}$ crystal by plotting the unit cell orientations from the Euler angles and applying the same $90^{\circ}$ rotation along $X$ to all to aid visualisation (compare the coordinate systems in Figure 9 (A) and (C)). As shown in Figure 9 (C), $\beta$ Sn grains are cyclic twinned (the \{101\} type twinning arrangement is plotted here) and red-wireframe grains and bluewireframe grains have $\{001\}$ and $\{301\}$ respectively parallel with the $\{001\}_{\mathrm{Ag} 3 \mathrm{Sn}}$ as indicated by the common black shaded planes in Figure 9 (C).

While the ORs in Eq. 5 and Eq. 6 were measured almost exactly in some droplets, many droplets had substantial rotations away from these ORs. The orientations of $\beta \mathrm{Sn}$ grains from 145 out of 188 droplets are summarised into stereographic projections in Figure 8 (F) with respect to $\mathrm{Ag}_{3} \mathrm{Sn}$. The pole figures with red datapoints and blue datapoints indicate $\beta \mathrm{Sn}$ orientations that have the same or similar ORs as Eq. 5 and Eq. 6 respectively. It can be seen
that, in both cases, the common $\{010\}_{\mathrm{Ag} 3 \mathrm{Sn} \|} \mid\{010\}_{\mathrm{Sn}_{\mathrm{n}}}$ (in both Eq. 5 and Eq. 6) has a relatively small mean misorientation angle of $\sim 4^{\circ}$, while the other two pairs of planes exhibit much larger misorientation angles $\left(>^{\sim} 10^{\circ}\right)$. This large angular misorientation was found to be specific to $\mathrm{Ag}_{3} \mathrm{Sn}$ and all other IMCs studied in this work had all near-parallel planes reproducibly within $\sim 4^{\circ}$ (e.g. Figure $2(F)$, Figure $4(F)$, and Figure $\left.6(F)\right)$.

The fixed common direction $[010]_{A_{g} 3 n}| |[010]_{s_{n}}$ but variable common plane can possibly be understood by examination of the $\beta \mathrm{Sn}-\mathrm{Ag}_{3} \mathrm{Sn}$ atomic lattice match in Figure 10. In Figure 10 (A) and (C), which represent ORs in Eq. 5 and Eq. 6 respectively, the closest packed $\{100\}_{\text {Ag3Sn }}$ meets with the closest packed $\{100\}_{S_{n}}$ either parallel on an $\{001\}_{\mathrm{AB} 3 \mathrm{Sn}}| |\{001\}_{\mathrm{Sn}}$ interface or obliquely on an $\{001\}_{\mathrm{Ag} 3 S_{n}}| |\{301\}_{\mathrm{Sn}}$ interface and there are large d -spacing mismatches ( $>14 \%$ ) in both cases. However, there is a good atomic match ( $\sim 2.7 \%$ ) along $\left.\langle 010\rangle_{\text {Ag3sn }_{n}}| |<010\right\rangle_{\text {sn }}$ which are the closest packed rows in each crystal (Table 4). Since there is good atomic match along only one direction, it is likely that the lowest energy interface is achieved by aligning the well-matched common direction, and the lack of other wellmatched rows means that there is no strong preference for the common plane. This is in contrast to the other six IMCs in this study where there are multiple reasonably-well matched directions and a fixed OR.

The good matching along $[010]_{\mathrm{Ag} 35 n}| |[010]_{\mathrm{sn}}$ is probably also the origin of the $\langle 100\rangle_{\mathrm{s}_{\mathrm{s}}}$ twinning axis always being parallel to $[010]_{\mathrm{Ag} 3 \mathrm{~S}}$, since this allows the good row matching between $\beta \mathrm{Sn}$ and $\mathrm{Ag}_{3} \mathrm{Sn}$ to be maintained in the twinned grains (Figure 9 (C)). The best matching direction(s) was also the twinning axis in twinned droplets on $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$ and $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$; on $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$ (Figure $6(\mathrm{G})$ ), the twinning axis was either $[100]_{\mathrm{Sn}}| |[\overline{1} \overline{5} \overline{4}]_{\mathrm{Ni} 3 \mathrm{Sn} 4}$ or $[0 \overline{1} 0]_{s_{n}}| |[10 \overline{1}]_{N i 3 S n 4}$ and both exhibit the lowest atomic mismatch in the $\mathrm{Ni}_{3} \mathrm{Sn}_{4}-\beta \mathrm{Sn}$ OR of
$0.7 \%$; on $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$ (Figure $4(\mathrm{G})$ ), the two $<100>$ of $\beta \mathrm{Sn}$ are parallel to two symmetrically equivalent $\left\langle 10 \overline{1} 1>\right.$ in $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$ and have the same lowest atomic mismatch in the $\mathrm{Cu}_{6} \mathrm{Sn}_{5}-\beta \mathrm{Sn}$ OR of 1.4\%.

All microstructures in droplets on $\mathrm{Ag}_{3} \mathrm{Sn}$ are summarised in Table 3 along with their frequency of occurrence. Similar to $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$ and $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$, the microstructure types indicate the $\beta$ Sn nucleation mechanisms are: i) heterogeneous nucleation on $\mathrm{Ag}_{3} \mathrm{Sn}$ by mechanism 2 in Figure $1(B)$ in single-grain and twinned droplets (97 out of 188) that have the ORs in Eq. 5 and/or Eq. 6; ii) heterogeneous nucleation on other phases by mechanism 3 in Figure 1 (B) in droplets that show 'other' ORs with $\mathrm{Ag}_{3} \mathrm{Sn}$ (43 out of 188); and iii) a mixture of heterogeneous nucleation on $\mathrm{Ag}_{3} \mathrm{Sn}$ and heterogeneous nucleation on other phases in multiple-independent-grain droplets (48/188) that have a grain with the ORs in Eq. 5 and/or Eq. 6.

In Figure 3, it can be seen that the nucleation undercooling of single Sn droplets on $\mathrm{Ag}_{3} \mathrm{Sn}$ is high compared with $\alpha \operatorname{CoSn}_{3}, \mathrm{PtSn}_{4}, \mathrm{PdSn}_{4}, \mathrm{\beta lrSn}_{4}$, and $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$, and only slightly more catalytic than no IMC facet (i.e. freestanding Sn droplets). This shows that $\mathrm{Ag}_{3} \mathrm{Sn}$ is a low potency nucleant for $\beta$ Sn which is consistent with the relatively poor lattice match in Figure 10 with good matching along only a single direction. This is also consistent with better atomic matches on $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$ facets (Figure 7 (B)).

### 3.5 IMC surface reconstruction

Figure 11 (A)-(G) shows typical surfaces of the IMCs after dissolving all $\beta$ Sn. The prior location of the droplets is visible for each IMC and each surface is partially-dissolved and/or reconstructed to some extent. It is clear that the dissolved IMC is much thicker (deeper) for $\mathrm{PdSn}_{4}($ Figure $11(\mathrm{~B})), \mathrm{Cu}_{6} \mathrm{Sn}_{5}($ Figure $11(\mathrm{E}))$, and $\mathrm{Ag}_{3} \mathrm{Sn}$ (Figure $\left.11(\mathrm{G})\right)$ compared with those of $\mathrm{Ni}_{3} \mathrm{Sn}_{4}, \alpha \mathrm{CoSn}_{3}, \mathrm{PtSn}_{4}$, and $\beta \mathrm{IrSn}_{4}$, in agreement with the calculated dissolved thickness $\Delta h$ shown in Table 5 (details of the calculations can be found in the Supplementary Information). It can also be seen that primary $\mathrm{PdSn}_{4}$ plates exist on the $\mathrm{PdSn}_{4}$ facet (Figure 11 (B)), and no primary IMC was observed on the facets of other IMCs. Their absence in $\alpha \operatorname{CoSn}_{3}, \mathrm{PtSn}_{4}, \beta 1 r \mathrm{Sn}_{4}$, and $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$ is mainly due to their low volume fractions $\left(f_{I M C}^{p r i}\right)$ as indicated in Table 5. Relatively large volume fractions of primary IMCs are predicted in droplets on $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$ and $\mathrm{Ag}_{3} \mathrm{Sn}$ (Table 5) but are not present in Figure $11(\mathrm{E})$ and (G). To test further for primary IMCs in $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$ and $\mathrm{Ag}_{3} \mathrm{Sn}$, some of their droplets were studied by FIBtomography. A 3D reconstructed droplet on $\mathrm{Ag}_{3} \mathrm{Sn}$ is shown in Figure $11(\mathrm{H})-(\mathrm{K})$. Figure 11 (K) shows that there are numerous eutectic $\mathrm{Ag}_{3} \mathrm{Sn}$ particles $(<\sim 1 \mu \mathrm{~m})$ in the bulk but no primary $\mathrm{Ag}_{3} \mathrm{Sn}$. Therefore, the predicted primary $\mathrm{Ag}_{3} \mathrm{Sn}$ is likely to have deposited on the $\mathrm{Ag}_{3} \mathrm{Sn}$ facet during cooling from the peak temperature. This interpretation is corroborated by the average thickness of the final dissolved $\mathrm{Ag}_{3} \mathrm{Sn}$ of ${ }^{\sim} 0.05 \mu \mathrm{~m}$ (Figure $11(\mathrm{~K})$ ), which is close to the calculated result $(0.04 \mu \mathrm{~m})$ assuming that all primary $\mathrm{Ag}_{3} \mathrm{Sn}$ is deposited on the main $\mathrm{Ag}_{3} \mathrm{Sn}$ plate during cooling from the peak temperature (see the Supplementary Information for further detail on this calculation).

Primary IMCs were only found in $\mathrm{PdSn}_{4} / \mathrm{Sn}$ droplets and thus, on $\mathrm{PdSn}_{4}$, there will have been competition between nucleation on the main $\mathrm{PdSn}_{4}$ plate and the primary $\mathrm{PdSn}_{4}$. However,

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in Figure 11 ( $B$ ), it can be seen that the primary $\mathrm{PdSn}_{4}$ has the same orientation as the main plate and, therefore, nucleation competition will not affect the OR.

The micrographs in Figure 11 (A)-(G) and the FIB-tomography in Figure 11 (I)-(K) show that many IMCs have grooves and ledges on the main facet after partial dissolution and surface reconstruction. Thus, the interfacial plane at the nucleation site need not be the macroscopic facet plane and nucleation could have occurred by mechanism 2b in Figure 1 (B) in at least some of the droplets, particularly for lower potency $\mathrm{Cu}_{6} \mathrm{Sn}_{5}, \mathrm{Ag}_{3} \mathrm{Sn}$, and $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$ where the extra catalysis from the grooves and ledges $[6,33,34]$ may be important. It is also likely that surface grooves, ledges etc. affected the undercooling measurements in Figure 3 so that the undercooling is not a simple reflection of the lattice match but also a function of the geometrically catalytic features on the facet.

### 3.6 Insights into $\beta$ Sn nucleation and twinning in solder joints

The $\beta \mathrm{Sn}$ microstructure in Sn droplets on $\alpha \mathrm{CoSn}_{3}, \mathrm{PtSn}_{4}, \mathrm{PdSn}_{4}$ and $\beta \mathrm{IrSn}_{4}$ was always a single grain without twinning (Table 3, Figure 2, and ref.[28]). Our previous studies on $550 \mu \mathrm{~m} \mathrm{Sn}-0.07 \mathrm{Pt}$ balls (containing $\mathrm{PtSn}_{4}$ ) also measured single-grain or multiple independent-grain structures at both low and high cooling rate, with no solidification twinning [10]. However, Pd- [10] and Co- [4] microalloyed Sn-3.0Ag-0.5Cu-X balls/joints containing $\mathrm{PdSn}_{4}$ and $\alpha \mathrm{CoSn}_{3}$ particles often have cyclic-twinned (beach-ball like) microstructures, and cyclic-twinning has also been demonstrated in $\beta S n$ that nucleates on the $\alpha \mathrm{CoSn}_{3}$ layer when $\mathrm{Sn}-3 \mathrm{Ag}-0.5 \mathrm{Cu}$ is soldered on cobalt substrates [5]. This indicates that cyclic twinning of $\beta S n$ that nucleates on $\alpha \operatorname{CoSn}_{3}$ and $\mathrm{PdSn}_{4}[4,5,10]$ depends on the presence of Ag and/or Cu solute. To test this, $\sim 5-100 \mu \mathrm{~m}$ droplets of $\mathrm{Sn}-3 \mathrm{Ag}-0.5 \mathrm{Cu}$ were solidified on the (100) facet of $\alpha \mathrm{CoSn}_{3}$ crystals. Typical results are shown in Figure 12 (A) where the droplet consists of three cyclically-twinned $\beta$ Sn orientations and one of the twinned grains (marked with an asterisk) has the OR in Table 2 with the $\alpha \mathrm{CoSn}_{3}$. Combining this result with the 299/299 Sn droplets with no twinning on $\alpha \mathrm{CoSn}_{3}, \mathrm{PtSn}_{4}, \mathrm{PdSn}_{4}$ and $\beta \mathrm{IrSn}_{4}$ (Table 3), indicates that $\beta$ Sn nucleated heterogeneously on the $\alpha \mathrm{CoSn}_{3}$ facet and the Ag and/or Cu solute promoted the development of cyclic-twins. However, solute may not be the only factor inducing solidification twinning, sample size (which affects the nucleation undercooling) and the concentration of Ag and/or Cu solute (which influences the solidification path) may also play important roles. For example, in ref.[28], where SAC305 solidified on Cu pads with added $\alpha \mathrm{CoSn}_{3}, \mathrm{PtSn}_{4}$, and $\beta \mathrm{IrSn}_{4}$ seed crystals, all joints solidified with a single $\beta \mathrm{Sn}$ orientation, though both Ag and Cu solute were present. In these specific cases, the joint sizes are much bigger than the Sn droplets used here and the Ag and Cu
concentrations are changed due to the dissolution of the Cu substrate. Further studies are needed to investigate these other factors that promote twinning of $\beta$ Sn.

It has been found here that $\mathrm{Cu}_{6} \mathrm{Sn}_{5}, \mathrm{Ni}_{3} \mathrm{Sn}_{4}$, and $\mathrm{Ag}_{3} \mathrm{Sn}$ can act as heterogeneous nucleation sites for $\beta$ Sn (Figure 4, Figure 6, and Figure 8) with preferred ORs (Table 2) unless more catalytic sites are available (Table 3). Many of the droplets on these IMCs formed microstructures that are analogous to those widely reported in $\mathrm{Sn}-\mathrm{Ag}$ and $\mathrm{Sn}-\mathrm{Ag}-\mathrm{Cu}$ solder joints on Cu or Ni substrates [1, 3-8, 56-61]. For example, the single-grain, cyclically-twinned and interlaced-twinned structures in the droplets in Figure 4, Figure 6, and Figure 8. This confirms that the droplet technique used here recreates phenomena that occur in solder joints. In these twinned droplets, it was common for one of the $\beta$ Sn grains to have the OR in Eq. 3, 4, 5 or 6 with the IMC facet. For example, in Figure 5 (A) grain 1 (marked with an asterisk) has the OR in Eq. 3 with $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$, indicating that $\beta \mathrm{Sn}$ both nucleated heterogeneously on the $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$ facet, and developed into cyclic-twins.

Some droplets developed twinned structures that were complex, with heterogeneous nucleation on an IMC facet and multiple $\beta$ Sn orientations all linked by multiple rings of interrelated cyclic twins; For example, Figure 12 (B) shows five interrelated rings of cyclictwins in a droplet on $\mathrm{Ag}_{3} \mathrm{Sn}$. The $\beta \mathrm{Sn}$ grain labelled 1* has the OR in Eq. 5 and grains 2* and 3* have the OR in Eq. 6 indicating heterogeneous nucleation on the $\mathrm{Ag}_{3} \mathrm{Sn}$ facet and grains 1, $2,3,4,5,6,7$ and 8 all have twin relationships indicated by the arrows and rings. Since all grains are interrelated by $\sim 60^{\circ}$ rotations around shared $\sim<100>$ axes, they almost certainly all come from a single nucleation event. These interrelated twinned structures are significantly more complex than those that form from the proposed twinned-nucleus model in ref. [1].


## 4 CONCLUSIONS

A droplet solidification technique has been applied to study the heterogeneous nucleation of $\beta S n$ on single crystal intermetallic compounds and to extract new insights into cyclic twinning in solder solidification. The following conclusions can be drawn:

1. In Sn droplets on relatively potent $\mathrm{IMCs}\left(\alpha \operatorname{CoSn}_{3}, \beta \mathrm{IrSn}_{4}, \mathrm{PdSn}_{4}\right.$, and $\left.\mathrm{PtSn}_{4}\right), \beta \mathrm{Sn}$ nucleated on the IMC facet with a simple orientation relationship (OR) in every droplet even when the undercooling was relatively high. Crystallographically similar ORs formed on $\alpha \operatorname{CoSn}_{3}, \beta_{1 r S n}^{4}, \mathrm{PdSn}_{4}$, and $\mathrm{PtSn}_{4}$. In the case of $\mathrm{PdSn}_{4}$, the OR can be written:

$$
(010)_{P d S n 4}| |(100)_{S_{n}} \text { and }[100]_{P d S n 4}| |[001]_{S_{n}} \text { or }[001]_{P d S n 4}| |[001]_{S_{n}}
$$

2. In Sn droplets on lower potency $\mathrm{IMCs}\left(\mathrm{Cu}_{6} \mathrm{Sn}_{5}, \mathrm{Ni}_{3} \mathrm{Sn}_{4}\right.$, and $\left.\mathrm{Ag}_{3} \mathrm{Sn}\right)$, $\beta \mathrm{Sn}$ nucleated on the IMC facet in some droplets and not in others, indicating a competition between different low potency nucleation sites such as the IMC facet, impurity particles, and the oxide. When $\beta$ Sn nucleated on the IMC facet, the following preferred ORs were measured:

$$
\begin{aligned}
& (10 \overline{1} 0)_{C_{\text {cu6sn5 }}}| |(111)_{\text {sn }} \text { and }[0001]_{C_{\text {u6Sn5 }}}| |[11 \overline{2}]_{s_{n}} \\
& (100)_{\text {Ni3Sn4 }}| |(\overline{2} \overline{4} \overline{1})_{\text {sn }} \text { and }[0 \overline{1} 0]_{\text {Ni3Sn4 }}| |[10 \overline{2}]_{\text {sn }} \\
& (001)_{\mathrm{Ag} 3 \mathrm{~S}}| |(001)_{\mathrm{Sn}} \text { or }(001)_{\mathrm{Ag} 3 \mathrm{~S}}| |(301)_{\mathrm{Sn}} \text { both with }[010]_{\mathrm{Ag} 3 \mathrm{~S}}| |[010]_{\mathrm{Sn}}
\end{aligned}
$$

All ORs formed with misorientations in the parallel planes/directions within $\sim 4^{\circ}$ except for $\mathrm{Ag}_{3} \mathrm{Sn}$ which had misorientations $>10^{\circ}$ in the parallel planes.
3. Cyclic twinning occurred in some Sn droplets solidified on the facets of $\mathrm{Cu}_{6} \mathrm{Sn}_{5}, \mathrm{Ni}_{3} \mathrm{Sn}_{4}$ or $\mathrm{Ag}_{3} \mathrm{Sn}$, with microstructures similar to those reported in electronic solder joints. In many cases there was both heterogeneous nucleation on the IMC facet (with a reproducible OR) and cyclic twinning. In the case of $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$ and $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$, only one of the twinned $\beta$ Sn grains had a simple OR with the IMC. For $\mathrm{Ag}_{3} \mathrm{Sn}$, all three cyclically twinned grains had one of two ORs all with a similar lattice match to the $\mathrm{Ag}_{3} \mathrm{Sn}$ facet.
4. For twinned Sn droplets on $\mathrm{Cu}_{6} \mathrm{Sn}_{5}, \mathrm{Ni}_{3} \mathrm{Sn}_{4}$ or $\mathrm{Ag}_{3} \mathrm{Sn}$, the $<100>_{\text {sn }}$ twinning axis always corresponded to the lowest linear disregistry on the IMC facet.
5. In twinned $\beta \mathrm{Sn}$ droplets on $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$ and $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$, it was common for the twinning angles to be distinctly separable with one /two grains close to $\{101\}$ twinning ( $57.2^{\circ}$ ) and the other(s) close to $\{301\}$ twinning $\left(62.8^{\circ}\right)$.
6. While past work has reported single cyclic twins in solder joints, this work often measured both (i) an OR with the IMC particle and (ii) multiple interrelated cyclic twins in droplets, that have multiple shared <100> axes with cyclic twinning around each shared <100> axis. Up to 5 interrelated twinning axes were measured in a single droplet.

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## Figure titles:

Figure 1 (A) A schematic phase diagram showing the Sn rich side of $\mathrm{Sn}-\mathrm{X}$ systems ( $\mathrm{X}=\mathrm{Co}, \mathrm{Pt}, \mathrm{Pd}, \mathrm{Ir}, \mathrm{Cu}$, $\mathrm{Ni}, \mathrm{Ag}$ ). The peak temperature for reflow is $240^{\circ} \mathrm{C}$. (B) A schematic showing the possible nucleation mechanisms in the Sn droplet on the IMC.

Figure 2 (A) Single crystals of $\alpha \mathrm{CoSn}_{3}, \mathrm{PtSn}_{4}, \mathrm{PdSn}_{4}$, and $\beta \mathrm{IrSn}_{4}$ with facets indexed by EBSD. (B) A Sn droplet solidified on the (100) facet of $\alpha \mathrm{CoSn}_{3}$. (C) 5 typical Sn droplets solidified on the (010) facet of a $\mathrm{PdSn}_{4}$. (D) IPF-Y map. (E) Pole figures. $\beta$ Sn unit cell wireframes have the same colour as the EBSD maps. Triangles, circles, and squares indicate ORs between the $\beta S n$ and the $P d S n_{4}$. (F) The summarised pole figure of $\beta S n$ orientations in Sn droplets on $\mathrm{PdSn}_{4}$ (see reference coordinate systems).

Figure 3 Nucleation undercoolings of $\sim 40-75 \mu \mathrm{~m}$ (Sn droplet size) single Sn droplets on IMCs (grey bars) and the ${ }^{\sim} 550 \mu \mathrm{~m}$ Sn-X alloy balls (red bars). For simplicity, only IMC names are shown to represent both droplets and alloys.

Figure 4 (A) $\mathrm{A} \mathrm{Cu}_{6} \mathrm{Sn}_{5}$ crystal indexed as hexagonal $\eta \mathrm{Cu}_{6} \mathrm{Sn}_{5}$ [40] by EBSD. (B) The same crystal $70^{\circ}$ tilted to the electron beam direction. (C) Typical Sn droplets on a $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$ crystal, and grain orientations are shown individually using unit cell wireframes and dash lines. (D) EBSD IPF-X map region in (C). (E) Pole figures of droplet 4, droplet 6, and the $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$ crystal. Parallel planes and directions are indicated by the same symbols, triangles indicate the facet of the $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$ and parallel plane in $\beta$ Sn. Orientations of $37 \beta$ Sn grains with the OR with $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$ in Eq. 3 summarised into pole figures of ( $F$ ) planes and (G) directions with respect to the orientation of the $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$ (see the reference coordinate system). Blue text in (G) are selected linear disregistries.

Figure 5 (A) A Sn droplet on $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$ (droplet 3 in Figure 4) showing 3 interrelated cyclic twins. All grains are labelled by numbers. The asterisked number indicates the grain that has the OR in Eq. 3 with $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$. (B) The <100>Sn pole figure of the Sn droplet showing how the 3 cyclic twins are related. (C) Translated $\beta$ Sn unit cell wireframes of 3 cyclic twins arranged in either $\{101\}$ or $\{301\}$ cyclic twinning type. Dashed unit cells were not measured but are shown for clarity. Red, green and blue are used to indicate twinning axes and shared common planes. (D) The misorientations $\delta_{\mathrm{ij}}$ between twinning axes, the in-grain misorientation $\mathrm{m}_{\mathrm{i}}$, and the misorientation $\omega_{\mathrm{ij}}$ between the other <100> axes of grains in twins i. (E) Angular distributions of misorientation between grains in twins i.

Figure 6 (A) $\mathrm{A} \mathrm{Ni}_{3} \mathrm{Sn}_{4}$ crystal indexed as $m S 14-\mathrm{Ni}_{3} \mathrm{Sn}_{4}[41]$ by EBSD. (B) The same crystal $70^{\circ}$ tilted to the electron beam direction. (C) Typical Sn droplets on $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$. Grain orientations are shown on each Sn droplet as unit cell wireframes. (D) EBSD IPF-X map. (E) Pole figures of droplet 1 and the $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$ crystal. Parallel planes and directions in $\beta \mathrm{Sn}$ and $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$ are indicated by the same symbols. Triangles indicate the facet of $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$ and parallel plane in $\beta S n$. ( $F, G$ ) $\beta$ Sn grains with the OR in Eq. 4 summarised into a pole figure with respect to $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$ (see the reference coordinate system). (F) Planes. (G) Directions. Blue text in (G) are selected linear disregistries.

Figure 7 (A) Atomic matching between $\beta \mathrm{Sn}$ and $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$ on different facets. (B) Planar atomic matching of interfaces on the three facets. All near-interface atoms are projected into the plane. Transparent atoms are out of plane.

Figure $8(\mathrm{~A})$ A typical $\mathrm{Ag}_{3} \mathrm{Sn}$ single crystal indexed as oP8- $\mathrm{Ag}_{3} \mathrm{Sn}$ [42] by EBSD. (B) The same crystal that is $54^{\circ}$ tilted to the electron beam direction. (C) Typical Sn droplets on $\mathrm{Ag}_{3} \mathrm{Sn}$, with $\beta n$ orientations shown with unit cell wireframes. (D) EBSD IPF-Z map. (E) Pole figures of droplet 8 and the $\mathrm{Ag}_{3} \mathrm{Sn}$ crystal. To represent the OR, parallel planes and directions in the $\beta \mathrm{Sn}$ and the $\mathrm{Ag}_{3} \mathrm{Sn}$ are indicated by the same symbols. Triangles indicate the facet of the $\mathrm{Ag}_{3} \mathrm{Sn}$ and corresponding parallel
plane in $\beta S n$. (F) Orientations of $\beta$ Sn grains that have the ORs in Eq. 5 and Eq. 6 with $\mathrm{Ag}_{3} \mathrm{Sn}$ summarised into pole figures with respect to $\mathrm{Ag}_{3} \mathrm{Sn}$ (see the reference coordinate system).

Figure 9 (A) A typical droplet on $\mathrm{Ag}_{3} \mathrm{Sn}$ with interlaced-twinned $\beta$ Sn structure with an EBSD IPF-Z map and unit cell wireframes superimposed. (B) Corresponding pole figures with parallel planes and directions labelled using the same symbols. (C) The OR between cyclic twinned $\beta \mathrm{Sn}$ grains and $\mathrm{Ag}_{3} \mathrm{Sn}$ created by translating the unit cells and rotating all orientations in (A) $90^{\circ}$ upwards (see their coordinate systems). Parallel planes in $\beta \mathrm{Sn}$ and $\mathrm{Ag}_{3} \mathrm{Sn}$ are indicated by black shaded planes. Red planes indicate the common plane of cyclic twinned $\beta$ Sn grains. (D) Misorientations $\delta_{\mathrm{ij}}$ between twinning axes, in-grain misorientation $\mathrm{m}_{\mathrm{i}}$, and the misorientation $\omega_{\mathrm{ij}}$ between the other <100> axes of grains. (E) Angular distributions of misorientation between grains in the interlaced twins.

Figure 10 (A) Atomic matching between $\beta$ Sn and $\mathrm{Ag}_{3} \mathrm{Sn}$ in (A) OR in Eq. 5 and (C) OR in Eq. 6. (B) and (D) The corresponding interfacial atomic match shown by projecting all near-interface atoms into the plane. Transparent atoms are out of plane.

Figure 11 Interfaces of Sn droplets on IMCs after dissolving all $\beta \mathrm{Sn}$ : (A) $\alpha \operatorname{CoSn}_{3}$, (B) $\mathrm{PdSn}_{4}$, (C) $\beta I r \mathrm{Sn}_{4}$, (D) $\mathrm{PtSn}_{4},(\mathrm{E}) \mathrm{Cu}_{6} \mathrm{Sn}_{5}$, (F) $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$, and (G) $\mathrm{Ag}_{3} \mathrm{Sn}$. (H)-(K) FIB-tomography of the Sn droplet on $\mathrm{Ag}_{3} \mathrm{Sn}$ in Figure 9: $(\mathrm{H})$ the secondary electron image, (I) reconstructed tin droplet, (J) the interface on $\mathrm{Ag}_{3} \mathrm{Sn}$, and $(K)$ a semi-transparent side view showing the wetting angle and the average dissolved thickness of the $\mathrm{Ag}_{3} \mathrm{Sn}$ single crystal.

Figure 12 (A) A Sn-3.0Ag-0.5Cu droplet on a (100) $\alpha \mathrm{CoSn}_{3}$ facet and the EBSD IPF-Z map of $\beta$ Sn in this droplet. The orientations of the cyclic twinned $\beta S n$ grains are shown in the $\{101\}$ type twinning configuration. (B) A Sn droplet on a (001) $\mathrm{Ag}_{3} \mathrm{Sn}$ facet showing 5 interrelated twins as indicated by the superimposed $\beta S n$ unit cell wireframes and coloured twinning axes. Arrows show orientations that are shared between two rings of cyclic twins.

## Tables:

Table 1 Crystal structures and lattice parameters used for indexing EBSD patterns (fractional coordinates are in the references).

| Phase | Space group | Pearson symbol | Lattice parameters |  |  |  |  |  | Ref. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | $\mathrm{a}(\mathrm{nm})$ | $\mathrm{b}(\mathrm{nm})$ | $\mathrm{c}(\mathrm{nm})$ | $\alpha\left({ }^{\circ}\right)$ | $\beta\left({ }^{\circ}\right)$ | $\gamma\left({ }^{\circ}\right)$ |  |
| $\beta$ Sn | 141/amd | t/4 | 0.5831 | 0.5831 | 0.3182 | 90 | 90 | 90 | [35] |
| PtSn 4 | Ccca | oS20 | 0.6418 | 1.1366 | 0.6384 | 90 | 90 | 90 | [36] |
| $\mathrm{PdSn}_{4}$ | Ccca | oS20 | 0.6442 | 1.1445 | 0.6389 | 90 | 90 | 90 | [37] |
| $\alpha \mathrm{CoSn}_{3}$ | Cmica | oS32 | 1.6864 | 0.6268 | 0.6270 | 90 | 90 | 90 | [38] |
| $\mathrm{BlrSn}_{4}$ | $14_{1} /$ acd | t/40 | 0.6310 | 0.6310 | 2.2770 | 90 | 90 | 90 | [39] |
| $\eta^{+} \mathrm{Cu}_{6} \mathrm{Sn}_{5}$ | $\mathrm{Pb}_{3} / \mathrm{mmc}$ | hP4 | 0.4206 | 0.4206 | 0.5097 | 90 | 90 | 120 | [40] |
| $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$ | C2/m | mS14 | 1.2214 | 0.4060 | 0.5219 | 90 | 105 | 90 | [41] |
| $\mathrm{Ag}_{3} \mathrm{Sn}$ | Pmmn | oP8 | 0.4782 | 0.5998 | 0.5164 | 90 | 90 | 90 | [42] |

Table 2 Summary of main IMC facets, measured parallel planes in $\beta$ Sn, common directions on planes, the frequency of occurrence of each OR, and the nucleation undercooling of single Sn droplets on the IMC. The $\alpha \operatorname{CoSn}_{3}, \mathrm{PtSn}_{4}$, and $\mathrm{IrSn}_{4}$ data are from ref. [28].

| IMC | IMC facets | Parallel plane in $\beta S n$ | Common directions on planes | Frequency of occurrence | $\Delta \mathrm{T}_{\text {nuc }}$ <br> (K) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\alpha \mathrm{CoSn}_{3}$ | (100) | (100) | [010]CoSn $\mid$ \|[001]Sn [001]CoSn ${ }^{\|l\|[001] S n}$ | 16 out of 41 <br> 25 out of 41 | $14 \pm 4$ |
| $\mathrm{PtSn}_{4}$ | (010) | (100) | [100]PtSn ${ }_{4} \mid$ [001]Sn [001]PtSn \||[001]Sn | 93 out of 105 <br> 12 out of 105 | $29 \pm 8$ |
| $\mathrm{PdSn}_{4}$ | (010) | (100) | [100]PdSn ${ }_{4} \mid$ [001]Sn [001]PdSn ${ }_{4} \mid$ [001]Sn | 73 out of 117 <br> 44 out of 117 | $21 \pm 6$ |
| $\beta 1 r \mathrm{Sn}_{4}$ | (001) | (100) | [100] $\mathrm{IrSn}_{4}\| \|[001] \mathrm{Sn}$ | 36 out of 36 | $19 \pm 3$ |
| $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$ | \{10 10$\}$ | $\begin{aligned} & (241) \\ & (\overline{1} 11) \end{aligned}$ | $\begin{aligned} & {[0001] \mathrm{Cu}_{6} \mathrm{Sn}_{5}\| \|[1 \overline{1} 2] \mathrm{Sn}} \\ & {[0001] \mathrm{Cu}_{6} \mathrm{Sn}_{5}\| \|[1 \overline{1} 2] \mathrm{Sn}} \end{aligned}$ | 32 out of 60 <br> 5 out of 60 | $53 \pm 11$ |
| $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$ | (100) | ${ }^{\text {a }}$ (241) | [010] $\mathrm{Ni}_{3} \mathrm{Sn}_{4}\| \|[\overline{1} 02] \mathrm{Sn}$ | 82 out of 111 | $35 \pm 5$ |
|  | (001) | ${ }^{\text {a }}$ (211) | [010] $\mathrm{Ni}_{3} \mathrm{Sn}_{4} \mid$ \| [ 102$] \mathrm{Sn}$ | 16 out of 47 |  |
|  | (201) | ${ }^{\text {a }}$ (261) | $[010] \mathrm{Ni}_{3} \mathrm{Sn}_{4} \mid$ \| [ 102$] \mathrm{Sn}$ | 14 out of 21 |  |
| $\mathrm{Ag}_{3} \mathrm{Sn}$ | (001) | $\begin{aligned} & (001) \\ & (301) \end{aligned}$ | [010]Ag ${ }_{3} \mathrm{Sn}\| \|[010] \mathrm{Sn}$ [010] $\mathrm{Ag}_{3} \mathrm{Sn}\| \|[010] \mathrm{Sn}$ | $\begin{aligned} & b^{b}+140 \text { out of } 188 \\ & b^{b} 2+140 \text { out of } 188 \end{aligned}$ | $39 \pm 8$ |

a. The parallel $\beta$ Sn planes with $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$ facets are different, but represent the same OR (see Eq. 4)
b. $A+B$ means that there are $A$ droplets that show single grain and only have this $O R$, and $B$ droplets that contain grains with both (001) $\mathrm{Ag}_{3} \mathrm{Sn}| |(001) \mathrm{Sn}$ and (001) $\mathrm{Ag}_{3} \mathrm{Sn}| |(301) \mathrm{Sn}$.

Table 3 Summary of $\beta$ Sn microstructures in Sn droplets on IMC facets. Gs=grains, Ts=twins, IGs= independent grains.

| IMC | Facet | Parallel plane in $\beta S n$ | Sum | Sn droplet microstructure and frequency of occurrence |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | Single | Simple twins |  | Interlaced twins |  | Interrelated twins |  |  |  | Multiple |
|  |  |  |  | grain | 2 Gs | 3 Gs | 2 Gs | 3 Gs | 2 Ts | 3 Ts | 4 Ts | >4 Ts | IGs |
| $\alpha \mathrm{CoSn}_{3}$ | (100) | (100) | 41 | 41 | -- | -- | -- | -- | -- | -- | -- | -- | -- |
| $\mathrm{PtSn}{ }_{4}$ | (010) | (100) | 105 | 105 | -- | -- | -- | -- | -- | -- | -- | -- | -- |
| $\mathrm{PdSn}_{4}$ | (010) | (100) | 117 | 117 | -- | -- | -- | -- | -- | -- | -- | -- | -- |
| $\beta 1 r \mathrm{Sn}_{4}$ | (001) | (100) | 36 | 36 | -- | -- | -- | -- | -- | -- | -- | -- | -- |
| $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$ | \{1010 0 | (241) | 32 | 11 | -- | 3 | -- | -- | 4 | 3 | 2 | 2 | 7 |
|  |  | (111) | 5 | -- | -- | 1 | -- | -- | 2 | -- | -- | -- | 2 |
|  |  | Others | 23 | 13 | 1 | 3 | -- | -- | -- | -- |  | -- | 6 |
| $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$ | (100) | (241) | 82 | 54 | 9 | 9 | 1 | -- | 6 | -- | -- | -- | 3 |
|  |  | Others | 29 | 21 | 1 | 2 | -- | -- | 1 | -- | -- | -- | 4 |
|  | (001) | (211) | 16 | 10 | 1 | 1 | -- | -- | -- | -- | -- | -- | 4 |
|  |  | Others | 31 | 20 | 1 | -- | -- | -- | 2 | -- | -- | -- | 8 |
|  | (201) | (261) | 14 | 10 | 2 | 1 | -- | -- | -- | -- | -- | -- | 1 |
|  |  | Others | 7 | 7 | -- | -- | -- | -- | -- | -- | -- | -- | -- |
| $\mathrm{Ag}_{3} \mathrm{Sn}$ | (001) | (001) | 143 | 3 | 6 | 3 | 8 | 50 | 17 | 1 | 3 | 4 | 48 |
|  |  | (301) | 142 | 2 | 6 | 3 | 8 | 50 | 17 | 1 | 3 | 4 | 48 |
|  |  | Others | 43 | 15 | 7 | 2 | -- | -- | -- | -- | -- | -- | 19 |

Table 4 Planes and atomic rows ranked by atomic density ( $\mathrm{nm}^{-2}$ ) and interatomic distance ( nm ) for $\beta \mathrm{Sn}, \mathrm{Cu}_{6} \mathrm{Sn}_{5}, \mathrm{Ni}_{3} \mathrm{Sn}_{4}$, and $\mathrm{Ag}_{3} \mathrm{Sn}$. N.B. some planes and directions are zig-zag and calculations have projected all atoms into the planes/directions.

| Rank | $\beta$ Sn (tetragonal) |  | $\eta \mathrm{Cu}_{6} \mathrm{Sn}_{5}$ (hexagonal) |  | $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$ (monoclinic) |  | $\mathrm{Ag}_{3} \mathrm{Sn}$ (orthorhombic) |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Plane, ${ }^{\text {a }}$ PD | Direction, ${ }^{\text {b }} \mathrm{AD}$ | Plane, ${ }^{\text {a }}$ PD | Direction, ${ }^{\text {b }} \mathrm{AD}$ | Plane, ${ }^{\text {a }}$ PD | Direction, ${ }^{\text {b }} \mathrm{AD}$ | Plane, ${ }^{\text {a }}$ PD | Direction, ${ }^{\text {b }} \mathrm{AD}$ |
| 1 | \{100\}, 10.78 | <100>, 0.292 | \{02̄22\}, 11.87 | <0001>, 0.255 | \{111\}, 12.32 | <001>, 0.261 | \{100\}, 12.91 | <010>, 0.300 |
| 2 | \{110\}, 7.62 | <001>, 0.318 | \{2̄110\}, 11.85 | <22 $201>, 0.257$ | $\{3 \overline{1} \overline{2}\}, 11.66$ | <101]>, 0.290 | \{121\}, 12.52 | <101>, 0.352 |
| 3 | \{211\}, 7.46 | <101>, 0.332 | \{1010 $0,9.34$ | <1101>, 0.296 | \{ 401 \}, 11.57 | <154>, 0.294 | \{102\}, 12.27 | <100>, 0.478 |
| 4 | \{241\}, 5.45 | <102>, 0.432 | \{0004\}, 7.83 | <1010>, 0.364 | \{010\}, 11.37 | <203>, 0.362 | \{010\}, 8.10 | <001>, 0.516 |
| 5 | \{111\}, 4.66 | <111>, 0.442 | -- | <2 $\overline{1} 10\rangle, 0.421$ | \{001\}, 8.07 | <010>, 0.406 | \{001\}, 6.97 | <201>, 0.544 |
| 6 | \{201\}, 3.97 | <103>, 0.559 | -- | <2 $\overline{1} \overline{1} 3>, 0.661$ | \{201\}, 7.11 | <130>, 0.862 |  |  |
| 7 | \{261\}, 3.27 | <104>, 0.700 | -- |  | \{100\}, 4.72 | <100>, 1.221 | -- | -- |
| 8 | \{221\}, 3.20 | <112>, 1.042 | -- | - | -- | -- | -- | -- |
| 9 | \{001\}, 2.94 | <412>, 1.244 | -- | -- | -- | -- | -- | -- |

a Planar atomic density, $\mathrm{nm}^{-2}$. The ranking goes down when the density decreases.
b Atomic distance, nm. The ranking goes down when the distance increases (i.e. less close packed).

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Table 5 Changes in liquid composition, volume fractions of primary and eutectic IMC, and dissolved thickness of the main IMC crystal for the situation in Figure 1. Calculation details are given in the Supplementary Information.

| $\mathrm{Sn} / \mathrm{IMC}$ | ${ }^{\mathrm{a}} C_{E}$ <br> $(\mathrm{wt} \%)$ | ${ }^{\mathrm{a}} C_{L}(240)$ <br> $(\mathrm{wt} \%)$ | ${ }^{\mathrm{b}} C_{I M C}$ <br> $(\mathrm{wt} \%)$ | ${ }^{\mathrm{c}}$ Density <br> $\left(\mathrm{g} \cdot \mathrm{cm}^{-3}\right)$ | ${ }^{\mathrm{d}} f_{I M C}^{p r i}$ <br> $(\mathrm{vol} \%)$ | ${ }^{\mathrm{e}} f_{I M C}^{\text {eut }}$ <br> $(\mathrm{vol} \%)$ | ${ }^{\mathrm{f}} \Delta h$ <br> $(\mathrm{~nm})$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\beta \mathrm{Sn}$ | -- | -- | -- | 7.26 | -- | -- | -- |
| $\alpha \mathrm{CoSn}_{3}$ | 0.02 Co | 0.02 Co | 14.2 Co | 8.32 | 0.03 | 0.09 | 3 |
| $\mathrm{PtSn}_{4}$ | 0.03 Pt | 0.03 Pt | 29.1 Pt | 9.55 | 0.08 | 0.002 | 2 |
| $\mathrm{PdSn}_{4}$ | 0.40 Pd | 0.52 Pd | 18.3 Pd | 8.20 | 1.45 | 1.07 | 57 |
| $\mathrm{IrSn}_{4}$ | -- | -- | 28.8 lr | 9.79 | -- | -- | -- |
| $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$ | 0.89 Cu | 1.08 Cu | 39.1 Cu | 8.31 | 1.63 | 0.42 | 55 |
| $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$ | 0.04 Ni | 0.04 Ni | 27.1 Ni | 8.65 | 0.06 | 0.07 | 3 |
| $\mathrm{Ag}_{3} \mathrm{Sn}^{2}$ | 3.73 Ag | 4.70 Ag | 73.2 Ag | 9.92 | 2.89 | 2.52 | 110 |

a $C_{E}$ (the eutectic composition of $\mathrm{Sn}-\mathrm{IMC}$ ) and $C_{L}$ data are from ref. [62], except $C_{E}$ of Pt - Sn from [47].
$\mathrm{b} C_{I M C}$ is the composition of the IMC, assuming stoichiometric compounds.
c Densities are theoretical values for the crystals in Table 1.
d Volume \% of primary IMC, assuming the nucleation undercooling in Table 2.
e Volume \% of eutectic IMC, assuming the nucleation undercooling in Table 2.
f Thickness dissolved in Figure $1(\mathrm{~B})$, assuming a droplet diameter $d=20 \mu \mathrm{~m}$, wetting angle $\theta=20^{\circ}$.

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Figure 1 (A) A schematic phase diagram showing the Sn rich side of $\mathrm{Sn}-\mathrm{X}$ systems (X=Co, Pt, Pd, Ir, Cu, Ni, Ag ). The peak temperature for reflow is $240^{\circ} \mathrm{C}$. (B) A schematic showing the possible nucleation mechanisms in the Sn droplet on the IMC.


Figure 2 (A) Single crystals of $\alpha \operatorname{CoSn}_{3}, \mathrm{PtSn}_{4}, \mathrm{PdSn}_{4}$, and $\beta \mathrm{IrSn}_{4}$ with facets indexed by EBSD. (B) A Sn droplet solidified on the (100) facet of $\alpha \operatorname{CoSn}_{3}$. (C) 5 typical Sn droplets solidified on the (010) facet of a $\mathrm{PdSn}_{4}$. (D) IPF-Y map. (E) Pole figures. $\beta S n$ unit cell wireframes have the same colour as the EBSD maps. Triangles, circles, and squares indicate ORs between the $\beta S n$ and the $\mathrm{PdSn}_{4}$. (F) The summarised pole figures of $\beta$ Sn orientations in Sn droplets on $\mathrm{PdSn}_{4}$ (see reference coordinate systems).


Figure 3 Nucleation undercoolings of $\sim 40-75 \mu \mathrm{~m}$ (Sn droplet size) single Sn droplets on IMCs (grey bars) and the $\sim 550 \mu \mathrm{~m}$ Sn-X alloy balls (red bars). For simplicity, only IMC names are shown to represent both droplets and alloys


Figure 4 (A) $\mathrm{A} \mathrm{Cu}_{6} \mathrm{Sn}_{5}$ crystal indexed as hexagonal $\eta \mathrm{Cu}_{6} \mathrm{Sn}_{5}$ [40] by EBSD. (B) The same crystal $70^{\circ}$ tilted to the electron beam direction. (C) Typical Sn droplets on a $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$ crystal, and grain orientations are shown individually using unit cell wireframes and dash lines. (D) EBSD IPF-X map region in (C). (E) Pole figures of droplet 4, droplet 6, and the $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$ crystal. Parallel planes and directions are indicated by the same symbols, triangles indicate the facet of the $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$ and parallel plane in $\beta$ Sn. Orientations of $37 \beta$ Sn grains with the OR with $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$ in Eq . 3 summarised into pole figures of ( F ) planes and (G) directions with respect to the orientation of the $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$ (see the reference coordinate system). Blue text in ( $G$ ) are selected linear disregistries.

Twins iii

(D)
$\left[\begin{array}{ccc}m_{1} & \omega 12 & \omega 13 \\ \delta_{12} & m 2 & \omega 23 \\ \delta_{13} & \delta 23 & m 3\end{array}\right]$
$\left[\begin{array}{ccc}1.5 \pm 0.5^{\circ} & 57 \pm 1^{\circ} & 65 \pm 1^{\circ} \\ 1.8 \pm 0.8^{\circ} & 0.1 \pm 0.7^{\circ} & 58 \pm 1^{\circ} \\ 2.5 \pm 0.6^{\circ} & 1.4 \pm 0.7^{\circ} & 0.7 \pm 0.3^{\circ}\end{array}\right]$


Figure 5 (A) A Sn droplet on $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$ (droplet 3 in Figure 4) showing 3 interrelated cyclic twins. All grains are labelled by numbers. The asterisked number indicates the grain that has the OR in Eq. 3 with $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$. (B) The <100>Sn pole figure of the Sn droplet showing how the 3 cyclic twins are related. (C) Translated $\beta$ Sn unit cell wireframes of 3 cyclic twins arranged in either \{101\} or $\{301\}$ cyclic twinning type. Dashed unit cells were not measured but are shown for clarity. Red, green and blue are used to indicate twinning axes and shared common planes. (D) The misorientations $\delta_{\mathrm{ij}}$ between twinning axes, the in-grain misorientation $\mathrm{m}_{\mathrm{i}}$, and the misorientation $\omega_{\mathrm{ij}}$ between the other <100> axes of grains in twins i. (E) Angular distributions of misorientation between grains in twins $i$.


Figure 6 (A) $\mathrm{A} \mathrm{Ni}_{3} \mathrm{Sn}_{4}$ crystal indexed as $m S 14-\mathrm{Ni}_{3} \mathrm{Sn}_{4}[41]$ by EBSD. (B) The same crystal $70^{\circ}$ tilted to the electron beam direction. (C) Typical Sn droplets on $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$. Grain orientations are shown on each Sn droplet as unit cell wireframes. (D) EBSD IPF-X map. (E) Pole figures of droplet 1 and the $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$ crystal. Parallel planes and directions in $\beta \mathrm{Sn}$ and $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$ are indicated by the same symbols. Triangles indicate the facet of $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$ and parallel plane in $\beta \mathrm{Sn}$. $(\mathrm{F}, \mathrm{G}) \beta$ Sn grains with the OR in Eq. 4 summarised into a pole figure with respect to $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$ (see the reference coordinate system). (F) Planes. (G) Directions. Blue text in (G) are selected linear disregistries.


Figure 7 (A) Atomic matching between $\beta \mathrm{Sn}$ and $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$ on different facets. (B) Planar atomic matching of interfaces on the three facets. All near-interface atoms are projected into the plane. Transparent atoms are out of plane.


Figure 8 (A) A typical $\mathrm{Ag}_{3} \mathrm{Sn}$ single crystal indexed as $o \mathrm{P} 8-\mathrm{Ag}_{3} \mathrm{Sn}$ [42] by EBSD. (B) The same crystal that is $54^{\circ}$ tilted to the electron beam direction. (C) Typical Sn droplets on $\mathrm{Ag}_{3} \mathrm{Sn}$, with $\beta \mathrm{n}$ orientations shown with unit cell wireframes. (D) EBSD IPF-Z map. (E) Pole figures of droplet 8 and the $\mathrm{Ag}_{3} \mathrm{Sn}$ crystal. To represent the OR, parallel planes and directions in the $\beta \mathrm{Sn}$ and the $\mathrm{Ag}_{3} \mathrm{Sn}$ are indicated by the same symbols. Triangles indicate the facet of the $\mathrm{Ag}_{3} \mathrm{Sn}$ and corresponding parallel plane in $\beta \mathrm{Sn}$. (F) Orientations of $\beta$ Sn grains that have the ORs in Eq. 5 and Eq. 6 with $\mathrm{Ag}_{3} \mathrm{Sn}$ summarised into pole figures with respect to $\mathrm{Ag}_{3} \mathrm{Sn}$ (see the reference coordinate system).


Figure 9 (A) A typical droplet on $\mathrm{Ag}_{3} \mathrm{Sn}$ with interlaced-twinned $\beta \mathrm{Sn}$ structure with an EBSD IPF-Z map and unit cell wireframes superimposed. (B) Corresponding pole figures with parallel planes and directions labelled using the same symbols. (C) The OR between cyclic twinned $\beta$ Sn grains and $\mathrm{Ag}_{3} \mathrm{Sn}$ created by translating the unit cells and rotating all orientations in (A) $90^{\circ}$ upwards (see their coordinate systems). Parallel planes in $\beta \mathrm{Sn}$ and $\mathrm{Ag}_{3} \mathrm{Sn}$ are indicated by black shaded planes. Red planes indicate the common plane of cyclic twinned $\beta S n$ grains. (D) Misorientations $\delta_{\mathrm{ij}}$ between twinning axes, in-grain misorientation $\mathrm{m}_{\mathrm{i}}$, and the misorientation $\omega_{\mathrm{ij}}$ between the other <100> axes of grains. (E) Angular distributions of misorientation between grains in the interlaced twins.


Figure 10 (A) Atomic matching between $\beta \mathrm{Sn}$ and $\mathrm{Ag}_{3} \mathrm{Sn}$ in (A) OR in Eq. 5 and (C) OR in Eq. 6. (B) and (D) The corresponding interfacial atomic match shown by projecting all near-interface atoms into the plane. Transparent atoms are out of plane.


Figure 11 Interfaces of Sn droplets on IMCs after dissolving all $\beta \mathrm{Sn}$ : (A) $\alpha \mathrm{CoSn}_{3}$, (B) $\mathrm{PdSn}_{4}$, (C) $\beta 1 \mathrm{rSn}_{4}$, (D) $\mathrm{PtSn}_{4}$, (E) $\mathrm{Cu}_{6} \mathrm{Sn}_{5}$, (F) $\mathrm{Ni}_{3} \mathrm{Sn}_{4}$, and (G) $\mathrm{Ag}_{3} \mathrm{Sn}$. (H)-(K) FIB-tomography of the Sn droplet on $\mathrm{Ag}_{3} \mathrm{Sn}$ in Figure 9: (H) the secondary electron image, (I) reconstructed tin droplet, (J) the interface on $\mathrm{Ag}_{3} \mathrm{Sn}$, and ( K ) a semi-transparent side view showing the wetting angle and the average dissolved thickness of the $\mathrm{Ag}_{3} \mathrm{Sn}$ single crystal.


Figure 12 (A) A Sn-3.0Ag-0.5Cu droplet on a (100) $\alpha^{(0) S n} n_{3}$ facet and the EBSD IPF-Z map of $\beta$ Sn in this droplet. The orientations of the cyclic twinned $\beta S n$ grains are shown in the \{101\} type twinning configuration. (B) A Sn droplet on a (001) $\mathrm{Ag}_{3} \mathrm{Sn}$ facet showing 5 interrelated twins as indicated by the superimposed $\beta$ Sn unit cell wireframes and coloured twinning axes. Arrows show orientations that are shared between two rings of cyclic twins.



## ACCEPTED MANUSCRIPT








Twins iii

(D)

$$
\begin{aligned}
& {\left[\begin{array}{ccc}
m 1 & \omega 12 & \omega 13 \\
\delta_{12} & m 2 & \omega 23 \\
\delta_{13} & \delta_{23} & m 3
\end{array}\right]} \\
& {\left[\begin{array}{ccc}
1.5 \pm 0.5^{\circ} & 57 \pm 1^{\circ} & 65 \pm 1^{\circ} \\
1.8 \pm 0.8^{\circ} & 0.1 \pm 0.7^{\circ} & 58 \pm 1^{\circ} \\
2.5 \pm 0.6^{\circ} & 1.4 \pm 0.7^{\circ} & 0.7 \pm 0.3^{\circ}
\end{array}\right]}
\end{aligned}
$$







(D)
(E)
$\left[\begin{array}{ccc}m_{1} & \omega 12 & \omega 13 \\ \delta_{12} & m_{2} & \omega_{23} \\ \delta_{13} & \delta_{23} & m_{3}\end{array}\right]$
$\left[\begin{array}{crr}2 \pm 2^{\circ} & 60 \pm 3^{\circ} & 60 \pm 3^{\circ} \\ 1.7 \pm 0.6^{\circ} & 2.9 \pm 1.4^{\circ} & 61.3 \pm 3.0^{\circ} \\ 1.5 \pm 0.6^{\circ} & 1.5 \pm 0.8^{\circ} & 2.4 \pm 1.4^{\circ}\end{array}\right]$


