

1 Fast and Non-destructive Pore Structure Analysis using
2 Terahertz Time-Domain Spectroscopy

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15 **Abstract**

16 Pharmaceutical tablets are typically manufactured by the uni-axial compaction of
17 powder that is confined radially by a rigid die. The directional nature of the compaction
18 process yields not only anisotropic mechanical properties (e.g. tensile strength) but
19 also directional properties of the pore structure in the porous compact. This study
20 derives a new quantitative parameter, S_a , to describe the anisotropy in pore structure
21 of pharmaceutical tablets based on terahertz time-domain spectroscopy measurements.
22 The S_a parameter analysis was applied to three different data sets including tablets
23 with only one excipient (functionalised calcium carbonate), samples with one excipient
24 (microcrystalline cellulose) and one drug (indomethacin), and a complex formulation
25 (granulated product comprising several excipients and one drug). The overall porosity,
26 tablet thickness, initial particle size distribution as well as the granule density were all
27 found to affect the significant structural anisotropies that were observed in all investigated
28 tablets. The S_a parameter provides new insights into the microstructure of a tablet and
29 its potential was particularly demonstrated for the analysis of formulations comprising
30 several components. The results clearly indicate that material attributes, such as particle
31 size and granule density, cause a change of the pore structure, which, therefore, directly
32 impacts the liquid imbibition that is part of the disintegration process. We show, for the
33 first time, how the granule density impacts the pore structure, which will also affect the

34 performance of the tablet. It is thus of great importance to gain a better understanding
35 of the relationship of the physical properties of material attributes (e.g. intragranular
36 porosity, particle shape), the compaction process and the microstructure of the finished
37 product.

38 *Keywords:* Pharmaceutical tablet, terahertz, pore structure, microstructure,
39 anisotropy, disintegration

40 **1. Introduction**

41 Powder compaction is a central process in pharmaceutical tablet manufacturing. Dur-
42 ing compaction, force is applied on an aggregate of mixed particles of excipient and active
43 pharmaceutical ingredient (API) to transform the powder bed into a porous compact of
44 a well-defined shape. The compaction process involves the rearrangement, plastic and
45 elastic deformation, as well as fragmentation of particles. As a result, individual par-
46 ticles come into sufficiently close proximity with one other to establish interparticulate
47 attractive forces or bonds (Nyström et al., 2008). The magnitude of the particle-particle
48 bonding forces depends on the underlying physical mechanism of bonding between the
49 individual particles as well as on the surface areas of interparticulate contacts. The
50 resulting interparticulate bonds do not only govern the tensile strength of the powder
51 compact, but they play a key role in the tablet disintegration process. A tablet only
52 disintegrates when sufficiently many interparticulate bonds are broken. This process
53 is typically achieved or facilitated by the stress that is generated from the swelling of
54 specifically designated excipient particles (Markl and Zeitler, 2017). A wide range of
55 pharmaceutical excipient particles begin to swell when they come in contact with water
56 or physiological fluids in the body. The swelling and subsequent disintegration of the
57 powder compact is thus driven by the rate at which liquid penetrates into the porous
58 tablet. The liquid uptake rate is directly affected by the pore space in the tablet, which
59 is formed during powder compaction (Yassin et al., 2015a,b). It is well-established in
60 other fields that the liquid imbibition process is quite complex and cannot be described
61 accurately only by the overall total porosity (Berg, 2014) but that it is considerably

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62 impacted by other characteristic properties of the pore structure, such as their pore con-
63 nectivity, constrictivity and tortuosity as well as pore wall roughness Schoelkopf (2000);
64 Liu et al. (2014). It is these properties that are particularly affected by anisotropy in
65 pore structure as they are defined by the compaction process.

66 Powder compaction is inherently anisotropic in nature as the powder particles are
67 confined radially by a rigid die whilst they are compressed axially by the moving punch
68 (Moe and Rippie, 1997). Unsurprisingly, this yields directionally dependent mechanical
69 properties of the finished tablet. It is well-known that the tensile strength varies signifi-
70 cantly between the axial and radial direction (Mullarney and Hancock, 2006) as well as
71 that the punch geometry affects the density distribution within a tablet Eiliazadeh et al.
72 (2003, 2004). Such anisotropic mechanical properties explain common failure modes
73 that are encountered during tablet manufacturing such as capping and delamination.
74 Besides the impact on the mechanical properties, uni-axial compression also affects the
75 pore structure within a tablet. Thus far there is a much better understanding of the
76 directional mechanical properties in tablets and much less is known with regard to the
77 anisotropy of the void space. This is not too surprising given that it is much harder
78 to measure and quantify. The most common methods for pore characterisation, namely
79 mercury porosimetry and helium pycnometry, cannot resolve the directionality of the
80 pores.

81 One method that can provide such information is X-ray computed microtomography
82 ($X\mu$ CT). It was recently demonstrated that $X\mu$ CT can be used to analyse the orientation
83 of pores by representing individual pores by their eigenvectors (Markl et al., 2017b). The
84 first eigenvector is defined in the direction of the main axis of a pore and its angle relative
85 to the global coordinate system of the macroscopic tablet provides a measure of the
86 orientation of the pore. Another very promising method to study the pore structure of
87 pharmaceutical tablets is terahertz time-domain spectroscopy (THz-TDS). THz-TDS can
88 be employed to measure the effective refractive index of a sample in a non-destructive
89 manner (Bawuah et al., 2016b; Markl et al., 2017a,b). The effective refractive index
90 is a function of the fill fractions of each constituent as well as of the total porosity.
91 It can therefore be used to determine the porosity of a tablet within seconds. The
92 measurement speed is clearly an advantage of THz-TDS (seconds) compared to $X\mu$ CT

93 (hours). Although the terahertz method cannot provide information about individual
94 pores, by using polarised terahertz radiation, it is possible to analyse the directional
95 properties of the pore structure as introduced recently (Bawuah et al., 2016a).

96 This study presents a rigorous development of a new structural parameter, S_a , to
97 characterise anisotropic pore structures using THz-TDS based on the method originally
98 developed by Bawuah et al. (2016a). The S_a parameter is derived for a two-phase
99 system (air filled pores and one solid material) and then extended to multi-phase porous
100 media (air filled pores and several different components). This parameter is applied
101 to characterise a simple formulation, a three-phase system and eventually a complex
102 commercial formulation.

103 2. Theory

104 Using THz-TDS it is possible to measure the effective refractive index, n_{eff} , of a porous
105 medium, which is related to the effective permittivity by $\varepsilon_{\text{eff}} = n_{\text{eff}}^2$. Effective medium
106 theory or zero-porosity approximation (ZPA) can be applied to calculate the porosity
107 from ε_{eff} or n_{eff} (Markl et al., 2017b). Besides determining the total porosity, it is
108 possible to gain insight into the directionality of the pores by exploiting the polarisation
109 of the terahertz wave. The terahertz plane wave's electric field vector, \mathbf{E} , is in the
110 direction perpendicular to the propagation direction, \mathbf{k} , of the terahertz pulse. The
111 specific direction of the terahertz electric field can thus be used to analyse anisotropic
112 characteristics of the pores or the material of the probed medium. We begin with deriving
113 the lower and upper limits of ε_{eff} on the basis of a theoretical model of the porous
114 medium that was first introduced by Wiener (1912). This model is then combined with
115 the experimental terahertz data to define a new characteristic parameter, S_a , that is a
116 measure of the degree of anisotropy of a pore structure. Initially, this concept is derived
117 for a two-phase system (one solid material and air voids) and then generalised for multi-
118 phase systems. Throughout this study we assume that scattering and dispersion effects
119 are negligible as well as that the fill fraction(s), i.e. porosity and fractions of each
120 constituent, are known.

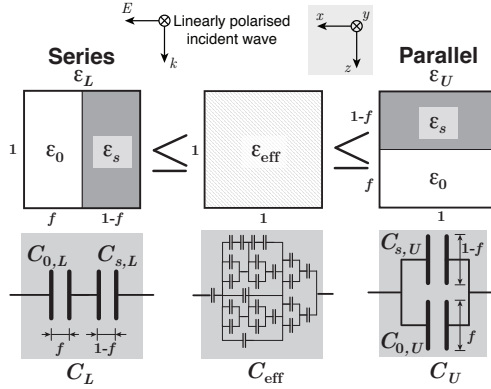


Figure 1: Schematic of the equivalent electric circuits for the propagation of a terahertz pulse in the z -direction through a two-phase porous compact composed of air and solid phase. The extreme cases are represented by the arrangement in series (left, lower Wiener bound) and in parallel (right, upper Wiener bound). The permittivity of air is $\varepsilon_0 = 1$ and that of the solid material is ε_s . The effective permittivity, ε_{eff} , for an actual sample always falls between the lower, ε_L , and the upper, ε_U , limits defined by the Wiener bounds. Its equivalent circuit is a combination of series and parallel capacitors. The dimensions of the capacitors, which are not provided in the schematic, are all set to unity.

121 2.1. Extreme Cases of the Pore Structure: Wiener Bounds

122 The permittivity of a porous medium can be calculated by considering a unit cell
 123 in which a repeating layered structure is used to reflect the pore structure. In this
 124 representation the pore space is described as air layers that are separated by solid matrix
 125 layers. The dimensions of the layers are much smaller than the wavelength of the terahertz
 126 waves, which are propagating parallel to the plane of the unit cell. Two extreme cases
 127 define the minimum and maximum of ε_{eff} : a serial and a parallel arrangement of the
 128 solid material, ε_s , and the air, ε_0 , respectively (Figure 1). The direction of the terahertz
 129 electric field defines the type of arrangement (e.g. the material and air are in series
 130 when they are arranged along \mathbf{E}). The description of ε_{eff} can be performed analogous
 131 to electrical circuitry using capacitors to represent the material and air (Kadlec et al.,
 132 2008).

The relative capacitance of the serial (C_L) and parallel (C_U) configuration can thus

be calculated by

$$\frac{1}{C_L} = \frac{1}{C_{0,L}} + \frac{1}{C_{S,L}}$$

$$C_L = \frac{C_{0,L}C_{S,L}}{C_{0,L} + C_{S,L}} \quad (1)$$

$$C_U = C_{0,U} + C_{S,U}. \quad (2)$$

In general a capacitance is defined as $C = \varepsilon \frac{A}{w}$ with ε , A , w as the permittivity of the dielectric medium between the two plates, the area of the conductive plates and the distance between the two plates, respectively. Figure 1 depicts only the dimensions that deviate from unity and therefore either the area of the conductive plates or the distance between the two plates is assumed to be unity. A unit length represents the amplitude of the \mathbf{E} vector. Furthermore, the influence of the $x - y$ geometry of the tablet on the terahertz measurement is negligible as the cross-section of the beam is much smaller than the dimensions of the tablet (i.e. the diameter of the tablet). In other words, the electric field decays in a distance much less than the radius of the tablet so that the dependence on the lateral geometry is negligible. The capacitance in the Eqs. 1 and 2 as well as in Figure 1 can thus be defined as $C_{0,L} = \varepsilon_0 \frac{1}{f}$, $C_{s,L} = \varepsilon_s \frac{1}{(1-f)}$, $C_{0,U} = \varepsilon_0 f$ and $C_{s,U} = \varepsilon_s (1 - f)$. The intrinsic permittivity ε_s is a material property and it refers to the skeletal material of the particle, i.e. the permittivity of the material in the absence of any intraparticle pores. $\varepsilon_0 = 1$ is taken to approximate the permittivity of ambient air ($\varepsilon = 1.0006$). The extreme cases, Eqs. 1 and 2, can now be expressed in terms of their permittivities as

$$\varepsilon_L = \frac{\varepsilon_s}{f(\varepsilon_s - 1) + 1} \quad (3)$$

$$\varepsilon_U = f + (1 - f)\varepsilon_s = f(1 - \varepsilon_s) + \varepsilon_s. \quad (4)$$

133 with $\varepsilon_L = C_L$ and $\varepsilon_U = C_U$. Eqs. 3 and 4 are well known as the lower and upper limits
 134 of the Wiener bounds for a two-phase porous medium (Tuononen et al., 2010; Bawuah
 135 et al., 2016a). The true value of the effective permittivity must always fall within the
 136 Wiener bounds ($\varepsilon_L \leq \varepsilon_{\text{eff}} \leq \varepsilon_U$) for arbitrary shapes of the pores and the solid material.

As outlined above, the Wiener bounds represent the extreme cases of either a fully parallel or in series arrangement of the solid material and the pores. However, in reality

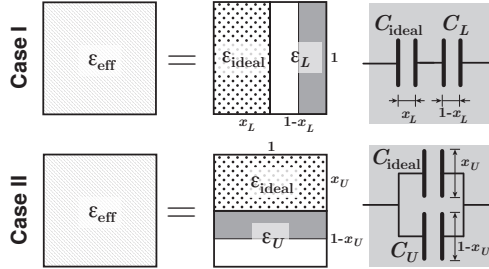


Figure 2: Representation of the two cases as electric circuits. The ideal permittivity, ϵ_{ideal} , is given by the underlying model (e.g. effective medium theory, ZPA) used to relate n_{eff} from the terahertz measurements to the porosity. x_L and x_U are fractional dimensions to express C_{ideal} , C_L and C_U as a function of their respective permittivities.

the pore architecture in a pharmaceutical tablet forms a complex structure that can be approximated by a combination of parallel and serial circuits (Figure 1). Bawuah et al. (2016a) used the concept of Wiener bounds and adapted a model from effective heat conductivity (Krischer and Kast, 1978) to study the structure of pharmaceutical tablets. The effective permittivity was used in conjunction with both the upper and the lower bound permittivities of the Wiener limits model to derive a structure parameter (S) for porous pharmaceutical tablets:

$$\frac{1}{\epsilon_{\text{eff}}} = \frac{S}{\epsilon_L} + \frac{1-S}{\epsilon_U}$$

$$S = \frac{1}{\epsilon_U - \epsilon_L} \left(\frac{\epsilon_U \epsilon_L}{\epsilon_{\text{eff}}} - \epsilon_L \right). \quad (5)$$

137 2.2. Alternative Definition of Structural Parameter

138 The S parameter as defined in Eq. 5 strongly depends on the porosity and it is thus
 139 limited to study structural changes of samples of the same porosity. We therefore propose
 140 an alternative definition, the S_a parameter, which enables the comparison of structural
 141 changes for samples with different porosities.

142 This reused structural parameter S_a is defined to be 0.5 for the case of a completely
 143 random arrangement of solid material and pores. This means that the measured ϵ_{eff} is
 144 equal to the theoretical/ideal permittivity, ϵ_{ideal} . ϵ_{ideal} can be calculated from the known
 145 porosity, f , and the intrinsic permittivity, ϵ_s , of the material using either an effective

146 medium approximate (EMA) or ZPA. The proposed S_a model considers two cases: i)
 147 $\varepsilon_{\text{eff}} < \varepsilon_{\text{ideal}}$, and ii) $\varepsilon_{\text{eff}} \geq \varepsilon_{\text{ideal}}$ (Figure 2).

The effective permittivity is represented by the ideal permittivity in conjunction with either a serial (Case I) or a parallel (Case II) arrangement as the boundary of each extreme case (Figure 1). In Case I this leads to

$$\begin{aligned} \frac{1}{\varepsilon_{\text{eff}}} &= \frac{x_L}{\varepsilon_L} + \frac{1-x_L}{\varepsilon_{\text{ideal}}} \\ x_L &= \frac{\varepsilon_L(\varepsilon_{\text{ideal}} - \varepsilon_{\text{eff}})}{\varepsilon_{\text{eff}}(\varepsilon_{\text{ideal}} - \varepsilon_L)}. \end{aligned} \quad (6)$$

Case II can be expressed as

$$\begin{aligned} \varepsilon_{\text{eff}} &= x_U \varepsilon_U + (1-x_U) \varepsilon_{\text{ideal}} \\ x_U &= \frac{\varepsilon_{\text{eff}} - \varepsilon_{\text{ideal}}}{\varepsilon_U - \varepsilon_{\text{ideal}}}. \end{aligned} \quad (7)$$

x_L and x_U are the fractional dimension of the representative capacitors. These fractional dimensions range from 0 to 1, where 0 yields $\varepsilon_{\text{eff}} = \varepsilon_{\text{ideal}}$ and 1 corresponds to the extreme case. The S_a parameter combines these two cases by

$$S_a = \begin{cases} 0.5(1-x_L) & \text{for } \varepsilon_{\text{eff}} < \varepsilon_{\text{ideal}} \\ 0.5(1+x_U) & \text{for } \varepsilon_{\text{eff}} \geq \varepsilon_{\text{ideal}} \end{cases}. \quad (8)$$

148 Consequently, S_a ranges from 0 to 1 and it indicates the degree of parallel and serial
 149 arrangements of pore/solid material structures in a sample.

150 Rather than in transmission, the S_a as well as the S parameter can also be applied to
 151 study the tablet structure on the basis of terahertz reflection measurements. A reflection
 152 setting could be beneficial for imaging applications or in-process control of the tablet
 153 quality where a transmission setup is not feasible. The change of the measurement
 154 configuration only affects the calculation of n_{eff} from the reflected terahertz waveform
 155 (Jepsen et al., 2007), but it does not require a modification of the definitions of the
 156 structural parameters or the Wiener bounds.

157 2.3. Multi-Phase Systems

The S_a and S parameters, as defined above, can be applied to reflect the arrangement of the pores in more complex tablet matrices. For a formulation of J constituents in the

powder compact, J solid materials are considered in the calculation of the Wiener bounds using the general definition:

$$\varepsilon_L = \frac{1}{f + \sum_{j=1}^J \frac{x_j}{\varepsilon_j}} \quad (9)$$

$$\varepsilon_U = f + \sum_{j=1}^J x_j \varepsilon_j \quad (10)$$

158 with x_j as the fill fraction of component j . Using Eqs. 9 and 10 to determine the S_a pa-
 159 rameter allows to study the arrangement and structure of all components including pores.
 160 This, however, does not enable the dissociation of the pore/solid material arrangement
 161 from that of the different components to each other and to the pores.

In order to study only the arrangement of the pores with respect to the solid phase, we propose to consider all solid constituents as one solid material, which is described by the lumped intrinsic permittivity, $\varepsilon_{s,\text{lumped}}$. The lower and upper bounds are thus defined as

$$\begin{aligned} \varepsilon_L &= \frac{1}{f + \sum_{j=1}^J \frac{x_j}{\varepsilon_j}} \\ &= \frac{1}{f + \frac{x_{\text{rest}}}{\varepsilon_{s,\text{lumped}}}} = \frac{1}{f + \frac{1-f}{\varepsilon_{s,\text{lumped}}}} \end{aligned} \quad (11)$$

$$\begin{aligned} \varepsilon_U &= f + \sum_{j=1}^J x_j \varepsilon_j \\ &= f + x_{\text{rest}} \varepsilon_{s,\text{lumped}} = f + (1-f) \varepsilon_{s,\text{lumped}} \end{aligned} \quad (12)$$

162 with $x_{\text{rest}} = 1 - f$. The multi-phase system can now be treated like a two-phase sys-
 163 tem where the pores are embedded in an effective medium. The theories developed for
 164 two-phase systems, such as the S_a parameter (Eq. 8), can be applied to porous media
 165 consisting of several components using Eqs. 11 and 12.

166 2.4. Extreme Values of the Wiener Bounds

As discussed above, the Wiener bounds are used to gain insights into the anisotropic structure of pharmaceutical tablets. The S_a and S parameter depend on how close the upper and lower bounds of the Wiener limits are to each other and how they are related

to the porosity. The maximum separation of the Wiener bounds for two-phase compacts is studied on the basis of the function

$$F(f) = \varepsilon_U(f) - \varepsilon_L(f). \quad (13)$$

Combining Eqs. 3, 4 and 13 gives

$$F(f) = f(1 - \varepsilon_s) + \varepsilon_s - \frac{\varepsilon_s}{f(\varepsilon_s - 1) + 1}. \quad (14)$$

The maximum separation condition for the Wiener bounds can be determined by forming the derivative with respect to the porosity:

$$F'(f) = (1 - \varepsilon_s) + \frac{(\varepsilon_s - 1)\varepsilon_s}{[f(\varepsilon_s - 1) + 1]^2}. \quad (15)$$

The porosity maximising the separation of the Wiener bounds, f_{\max} , can be calculated by setting $F'(f_{\max}) = 0$, which yields

$$\begin{aligned} \frac{(\varepsilon_s - 1)\varepsilon_s}{[f_{\max}(\varepsilon_s - 1) + 1]^2} &= (\varepsilon_s - 1) \\ f_{\max} &= \frac{\sqrt{\varepsilon_s} - 1}{\varepsilon_s - 1}. \end{aligned} \quad (16)$$

We can now replace the permittivity by the refractive index ($n_s = \sqrt{\varepsilon_s}$) in Eq. 16 and f_{\max} can then be expressed as

$$f_{\max} = \frac{n_s - 1}{n_s^2 - 1} = \frac{1}{n_s + 1}. \quad (17)$$

Eq. 17 gives the porosity which maximises the separations of the Wiener bounds for a two-phase system and also for a multi-phase system as described by Eqs. 11 and 12. This can be confirmed by forming the second derivative $F''(f)$:

$$\begin{aligned} F''(f) &= -\frac{2[f((\varepsilon_s - 1) + 1)(\varepsilon_s - 1)^2\varepsilon_s]}{[f(\varepsilon_s - 1) + 1]^4} \\ F''(f_{\max}) &= -\frac{2(\varepsilon_s - 1)^2\varepsilon_s}{[f_{\max}(\varepsilon_s - 1) + 1]^3} < 0 \end{aligned} \quad (18)$$

¹⁶⁷ This inequality is always true as $\varepsilon_s > 1$, which confirms that Eq. 17 yields a maximum.

168 **3. Materials and Methods**

169 *3.1. Materials*

170 In the following we present data from several different formulations ranging from a
 171 simple one with only one excipient to a complex formulation consisting of several excip-
 172 ients and an API. The terahertz transmission data of these formulations were already
 173 reported previously as indicated below, but we use these datasets to demonstrate how the
 174 concept of S_a can be applied to better understand the microstructure of pharmaceutical
 175 tablets in general and the anisotropic pore structure in particular.

The porosity was calculated by relating the bulk density, ϱ_b , to the known true density, ϱ_t , of the used materials:

$$f = 1 - \frac{\varrho_b}{\varrho_t}. \quad (19)$$

176 The bulk density of flat-faced tablets (first two sets of samples, M01 and M02) was
 177 determined by $\varrho_b = W/(\pi (\frac{D}{2})^2 H)$ with W , D and H as the weight, diameter and
 178 thickness of the tablet. The third set of samples (M03) were tablets compacted by dual
 179 radius punches and the bulk density was thus calculated by $\varrho_b = W/(0.25H_{\text{fill}}\pi D^2 + V_{\text{cup}})$,
 180 where H_{fill} and V_{cup} are the fill depth and the tablet cup volume, respectively.

181 The first set of samples (henceforth referred to as M01) consisted of pure func-
 182 tionalised calcium carbonate (FCC, Omyapharm[®], Omya International AG, Oftringen,

Table 1: Summary of the M01 samples, namely pure FCC tablets with target porosities from 45% to 67%. More details about these tablets were reported previously in Markl et al. (2017b). Each batch consisted of 15 tablets and the properties listed are averaged values for each batch. The porosity was calculated using Eq. 19 with a true density of 2.96 g cm⁻³.

Batch ID	Thickness	Weight	Porosity
	H	W	f
	(mm)	(mg)	(-)
B01	1.67	217	0.45
B02	1.64	190	0.50
B03	1.63	168	0.55
B04	1.62	147	0.61
B05	1.61	122	0.67

183 Switzerland) particles. Details about this set of samples are provided in Markl et al.
184 (2017b) and a summary is given in Table 1. The FCC powder was compacted to flat-
185 faced tablets with a target diameter of 10 mm using a compaction simulator (PuuMan
186 Ltd, Kuopio, Finland). The highly-porous nature of FCC allowed the compaction of
187 tablets with porosities ranging from 45% – 67%.

188 The second set of samples consisted of microcrystalline cellulose (MCC, Avicel PH101,
189 FMC BioPolymer, Philadelphia, USA) and indomethacin (Hangzhou Dayangchem Co.
190 Ltd, Hangzhou, China), as reported in Bawuah et al. (2016b) and Ridgway et al. (2017).
191 These samples were varied in terms of API/MCC concentrations, tablet thickness and
192 porosity (Table 2). Several different subsets were produced by a compaction simulator
193 (PuuMan Ltd, Kuopio, Finland), where each flat-faced tablet had a diameter of 13 mm.

194 Another set of samples consists of 18 batches from a production-scale design of ex-
195 periments (DoE) (Table 3). The tablet formulation was kept constant throughout all
196 batches. Each tablet consisted of a micronised poorly water soluble drug substance
197 which was combined with lactose monohydrate, MCC, hypromellose and croscarmellose
198 sodium by a high shear wet granulator. A fluid-bed dryer was employed to dry the gran-
199 ules prior to blending them with extra-granular croscarmellose sodium and magnesium
200 stearate. This blend was then compacted by a Fette 2090 tablet press (Fette Compact-
201 ing GmbH, Schwarzenberg, Germany, fitted with 43 stations) to curved-face tablets using
202 dual radius punches with a diameter of 10.5 mm. A split-plot DoE was used to study
203 the effect of three process variables (water amount, wet massing time and water addition
204 rate) of the granulation and one compaction factor (tablet breaking force) on the disin-
205 tegration and dissolution performance of the tablets. More details about these samples
206 are provided in Markl et al. (2017a) and van den Ban and Goodwin (2017).

207 *3.2. Terahertz Time-Domain Spectroscopy*

208 The effective refractive index of each sample was determined from terahertz transmis-
209 sion measurements. A Terapulse 4000 spectrometer (TeraView Ltd, Cambridge, UK) was
210 used for the samples M01 and M03. The measurements were performed in a transmission
211 chamber, which was purged with dry nitrogen gas. 60 waveforms were co-averaged and
212 the total measurement time was about 1.5 min for M01 and M03. n_{eff} was determined
213 for every tablet by analysing the frequency-dependent refractive index and selecting the

214 refractive index at 1 THz. More details about the measurement procedure are provided

Table 2: Properties of the M02 samples. The concentration of indomethacin, ϕ , was varied from 0% to 15% and the fraction of MCC was adjusted accordingly. Each subset (labelled with S01-S08) consisted of 5 tablets. The porosity, f , was calculated using Eq. 19 with a true density of 1.56 g cm^{-3} and 1.37 g cm^{-3} for MCC and indomethacin, respectively.

Batch ID	API ϕ (wt%)	Thickness H (mm)	Weight W (mg)	Porosity f (-)
B01-S01	10.00	3.03	342	0.46
B01-S02	10.00	3.03	357	0.43
B01-S03	10.00	3.02	371	0.41
B01-S04	10.00	3.01	385	0.38
B01-S05	10.00	3.01	400	0.36
B02-S01	10.00	2.74	361	0.36
B02-S02	10.00	3.33	439	0.36
B02-S03	10.00	3.63	476	0.36
B02-S04	10.00	3.93	515	0.36
B03-S01	0.00	3.03	411	0.36
B03-S02	3.75	3.02	403	0.36
B03-S03	7.50	3.03	403	0.36
B03-S04	8.75	3.00	402	0.36
B03-S05	10.00	3.02	401	0.36
B03-S06	11.25	3.04	401	0.36
B03-S07	12.50	3.03	400	0.36
B03-S08	15.00	3.04	400	0.36
B04-S01	9.00	2.74	406	0.28
B04-S02	9.50	2.96	405	0.34
B04-S03	10.00	3.28	406	0.40
B04-S04	10.50	3.65	403	0.47
B04-S05	11.00	3.95	404	0.51

Table 3: Summary of properties of M03 samples. This set consisted of 18 different batches from a production-scale DoE. The porosity was calculated from the ratio between the bulk density and the true density ($\rho_t = 1.51 \text{ g cm}^{-3}$) of the formulation following Eq. 19. The granule density was computed by $\rho_g = W/(0.25H_{\text{fill}}\pi D^2 + V_{\text{cup}})$, where H_{fill} is the fill depth, $D = 10.5 \text{ mm}$ is the tablet diameter and V_{cup} is the tablet cup volume. More details about these batches are provided in Markl et al. (2017a) and van den Ban and Goodwin (2017).

Batch ID	Thickness H (mm)	Weight W (mg)	Porosity f (-)	Granule density ρ_{granule} (g cm^{-3})
B01	5.27	399.6	0.17	0.60
B02	5.10	401.0	0.13	0.60
B03	5.31	400.2	0.18	0.59
B04	5.21	399.5	0.15	0.63
B05	5.06	398.8	0.11	0.59
B06	5.15	399.0	0.14	0.64
B07	4.97	399.3	0.08	0.63
B08	4.94	400.8	0.09	0.63
B09	5.13	399.4	0.13	0.64
B10	4.85	399.7	0.07	0.69
B11	4.86	399.1	0.06	0.59
B12	4.84	400.3	0.06	0.60
B13	4.87	402.3	0.07	0.69
B14	4.82	399.3	0.05	0.64
B15	4.86	401.5	0.07	0.69
B16	4.88	400.9	0.07	0.64
B17	4.67	399.4	0.01	0.64
B18	4.73	401.6	0.02	0.64

215 in Markl et al. (2017b) and Markl et al. (2017a) for M01 and M03, respectively. The
216 samples M02 were measured using a custom-built terahertz spectrometer as described in
217 Parrott et al. (2009) and Li et al. (2010). n_{eff} is retrieved from the terahertz pulse delay

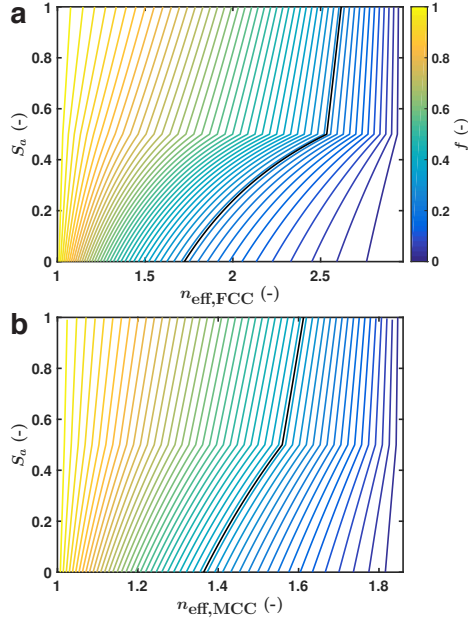


Figure 3: Simulation of the S_a parameter for (a) FCC (M01) and (b) MCC (M02). The intrinsic refractive indices are given in Table 4. The solid black line indicates the S_a parameter at the porosity that maximises the Wiener bounds (Eq. 17).

218 difference between the sample and the reference pulse. Bawuah et al. (2016b) reported
 219 more details about the measurement procedure of these samples.

220 .

221 4. Results

222 4.1. Simulations of the Extreme Cases and the S_a Parameter

223 The S_a parameter was calculated for a range of n_{eff} covering porosities of the porous
 224 medium from 0–1 and using the intrinsic refractive indices of FCC and MCC (Figure 3).
 225 The discontinuity at $S_a = 0.5$ is by definition the transition point between the two cases,
 226 i.e. serial and parallel arrangement of the constituents. The values of S_a must always
 227 be a real number between zero and one. Thus, for the two extremes of S_a , $S_a = 1$
 228 represents a porous medium with all its components purely arranged in parallel, whereas
 229 $S_a = 0$ depicts a porous medium with components displaying ideal serial arrangement.

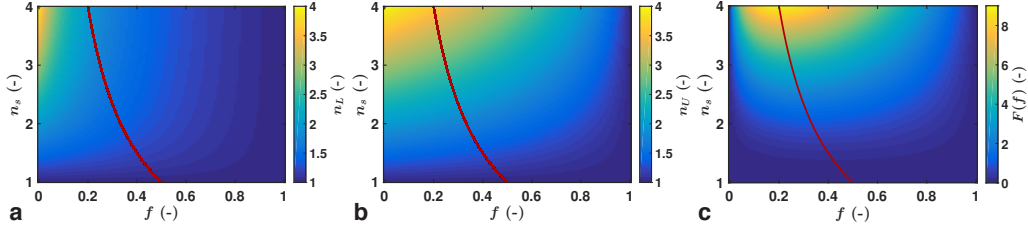


Figure 4: Intrinsic refractive index, n_s , as a function of porosity, f . (a) Lower Wiener bound (n_L , Eq. 3). (b) Upper Wiener bound (n_U , Eq. 4). (c) Separation function (F , Eq. 13). The red solid line indicates the maximum separation of the Wiener bounds as given by Eq. 17.

230 $S_a > 0.5$ is linear due to the linear nature of Eqs. 4 and 7, whereas S_a exhibits a non-
 231 linear relationship with n_{eff} for $S_a < 0.5$ as evident in Eqs. 3 and 6. The non-linear
 232 relationship between S_a and n_{eff} is particularly pronounced for medium range porosities
 233 and this strongly depends on the upper and lower Wiener bounds.

234 It is therefore important to understand the dependence of the porosity, f , and the in-
 235 trinsic refractive index, n_s , on these limits (Figure 4). The bounds are clearly very close
 236 to each other for very small porosities (n_{eff} approaches n_s) and for very high porosities
 237 (n_{eff} approaches $n_0 = 1$). The porosity maximising the separation of the Wiener
 238 bounds, f_{max} , is of particular importance as it provides the highest resolution for the S_a
 239 parameter. The fact that f_{max} is < 0.5 for all n_s renders the proposed method highly
 240 sensitive for the study of pharmaceutical tablets as these powder compacts have typically
 241 porosities < 0.5 .

242 The assumption of low terahertz absorption by the tablet samples for the derivation
 243 of Eq. 8 holds for the M01 and M02 samples. The definition of S_a , however, is broader
 244 and also allows for high absorption. The only adjustment required is the introduction
 245 of an effective refractive index that has a real (dispersion of terahertz waves) and imagi-
 246 nary (absorption of terahertz waves) part instead of the effective refractive index being
 247 confined to a real number (Peiponen and Gornov, 2006). The definition is, therefore,
 248 not limited to low absorption only. This fact is particularly important for the analysis of
 249 the M03 samples, where significant absorption of terahertz radiation by the formulation
 250 takes place.

Table 4: Summary of the models used to determine the intrinsic refractive indices, n_s . More details about these models are provided in Markl et al. (2017b). The listed n_s for M03 is the lumped intrinsic refractive index for the solid material. L is the depolarisation factor used to describe the pore shape in the AB-EMA model. The references provide further details about the materials.

Set		n_s	Model	Ref
M01	FCC	2.97	AB-EMA $L = 0.21$	Markl et al. (2017b)
M02	MCC	1.86	ZPA	Bawuah et al. (2016b)
	API	1.73	ZPA	Ridgway et al. (2017)
M03	Complex formulation	1.74	AB-EMA $L = 0.35$	Markl et al. (2017a)

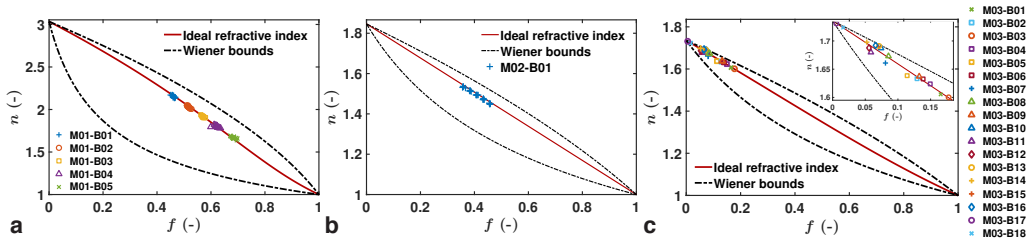


Figure 5: Refractive index, n , as a function of porosity, f , for (a) M01 (FCC tablets), (b) M02 (MCC and API tablets), and (c) M03 (complex formulation). The solid red line indicates the ideal refractive index for each material, which was calculated using the AB-EMA for (a,c) and ZPA for (b). (b) Shows only the n_{eff} from B01 as these tablets have the same intrinsic refractive index of 1.85 (10% API) and varied only in porosity.

251 4.2. S_a Parameter of the Different Materials

252 The effective permittivity, ϵ_{eff} , and thus the effective refractive index, n_{eff} , always lie
253 within the upper and lower limit of the Wiener bounds (Figure 5). The ideal refractive
254 index was calculated from the model used to relate n_{eff} and f as well as to determine n_s .
255 Here, we employ two different models for this purpose: the anisotropic Bruggeman EMA
256 (AB-EMA) and the ZPA. The used models as well as the intrinsic refractive index values
257 are summarised in Table 4 for the three different sets. Besides the use of these models
258 to determine the intrinsic refractive indices and to predict the porosity from terahertz
259 measurements, they were utilised to calculate the ideal refractive index required for the

260 calculation of the S_a parameter.

261 The AB-EMA was applied for M01 and M03 as it outperformed other EMA models
262 as well as ZPA due to the fact that it accounts for a non-spherical shape of the inclusions
263 and solid material by a depolarisation factor (Markl et al., 2017b). This depolarisation
264 factor was estimated to be $L = 0.21$ for M01, which can be related to a needle-like
265 shape of the pores with an aspect ratio of 1.7 (ratio between the dimensions in x - and
266 z -direction). This means that the pores have a preferred orientation perpendicular to
267 the compaction direction, and thus parallel to the \mathbf{E} vector. The AB-EMA exhibits a
268 non-linear dependence of the refractive index and the porosity (Figure 5a and c), which
269 is not the case for the ZPA (Figure 5b). The depolarisation factor of M03 was $L = 0.35$,
270 which is very close to that of spherical shaped pores ($L = 1/3$) and the performance of
271 the AB-EMA model was only slightly better than when using ZPA.

The M02 set consisted of several batches with varying porosity, thickness and API concentration. Since these samples are three-phase systems, the MCC and API particles were considered as one solid material. The lumped intrinsic refractive index, $n_{s,\text{lumped}}$, is not a constant for these samples as they vary in their composition (batches B03 and B04). The dependence of $n_{s,\text{lumped}}$ on the API concentration, ϕ , is accounted for by

$$n_{s,\text{lumped}}(\phi) = (n_{s,\text{API}} - n_{s,\text{MCC}})\phi + n_{s,\text{MCC}}. \quad (20)$$

272 $n_{s,\text{API}}$ and $n_{s,\text{MCC}}$ are given in Table 4 and they were determined by the ZPA for a
273 three-phase system following the approach presented in Bawuah et al. (2016b).

274 Figure 5b only depicts the data of M02-B01, which has a constant composition (90%
275 MCC and 10% API) and only varies in terms of its porosity. The ideal refractive in-
276 dex changes with the composition leading to varying intersection points with the y -axis
277 ranging from 1.73 (100% API) to 1.86 (100% MCC).

278 On the contrary, the M03 samples differed only in their microstructure and there were
279 no changes in their composition. The lumped intrinsic refractive index ($n_{s,\text{lumped}} = 1.74$)
280 was thus constant across all 18 batches.

281 The S_a parameter of the M01 samples reveals that the structure changes with in-
282 creasing porosity (Figure 6). A parallel arrangement of the FCC material and the pores
283 becomes emphasised for a larger pore space, which is fully in line with the results in

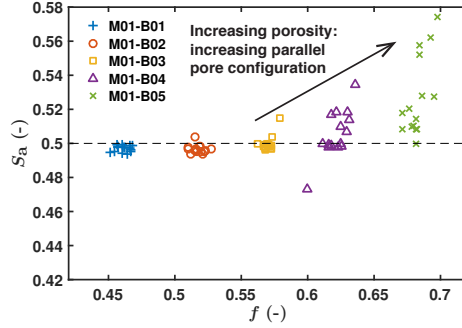


Figure 6: S_a as a function of the porosity, f , for set M01 (FCC tablets). n_s and the used model are provided in Table 4.

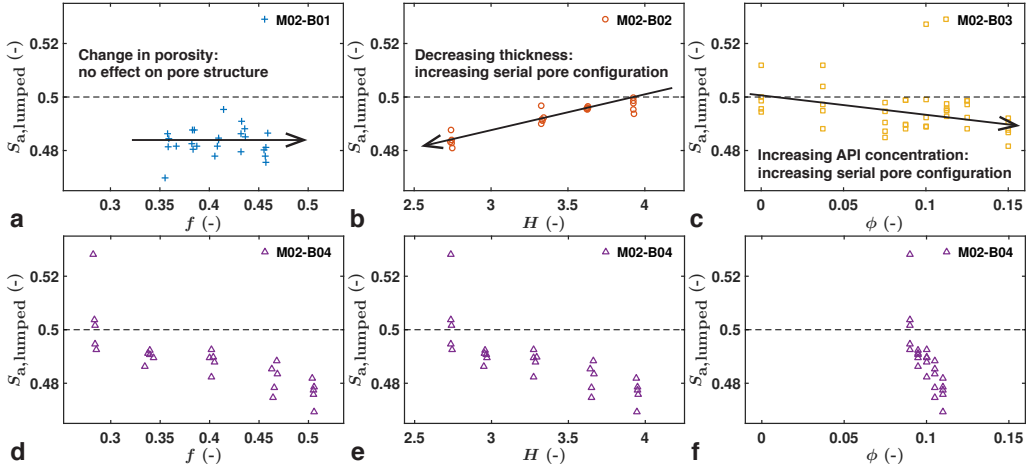


Figure 7: S_a as a function of (a,d) the porosity, f , (b,e) the tablet thickness, H , and (c,f) the API concentration, ϕ , for set M02 (MCC/API tablets). Only one variable at a time was varied for results of the batches in the top row (a,b,c). The bottom row (d,e,f) shows the results from batch M02-B04, where all three variables were changed simultaneously. Eq. 20 was applied to calculate the intrinsic refractive index, $n_{s,lumped}(\phi)$, as a function of ϕ .

284 Markl et al. (2017b). Although the FCC particles have a very large intraparticle porosity
 285 the anisotropic pore structure is primarily attributed to the interparticle voids that
 286 are formed during the compaction of the powder, as the FCC particles are known to be
 287 mechanically stable under compaction.

288 The results of a three-phase system (M02 samples) are depicted in Figure 7. Only

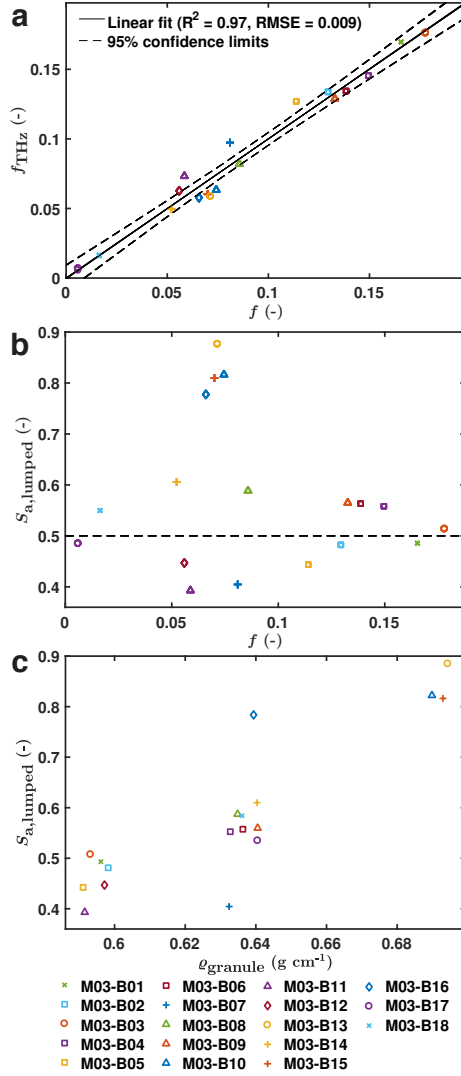


Figure 8: Results from terahertz measurements and analysis of the M03 set (complex formulation). (a) Porosity predicted from the terahertz measurements, f_{THz} , as a function of the porosity determined by Eq. 19, (b) and (c) depict the S_a parameter depending on the porosity and the granule density, respectively. AB-EMA was used to determine the intrinsic refractive index of the lumped solid material ($n_{s,\text{lumped}} = 1.74$). AB-EMA, adopting $n_{s,\text{lumped}}$ was also applied to calculate f_{THz} and S_a .

289 one parameter was varied at a time for the batches M02-B01 (porosity, Figure 7a),
 290 M02-B02 (tablet thickness, Figure 7b) and M02-B03 (API concentration, Figure 7c),

291 whereas all three variables were modified for batch M02-B04 (Figure 7d-f). Surprisingly,
292 the porosity does not considerably affect the arrangement of the solid material/pores
293 construct (Figure 7a), although the overall configuration is a serial connection of the
294 two phases. On the contrary, tablet thickness causes a change of the structure as a
295 thinner tablet yields a more pronounced serial arrangement of solid material and pores
296 (Figure 7b). The thicker the tablet the more randomly arranged the pores are. An
297 increase of API particles in the powder compact has an opposite effect on the structure:
298 the higher the API concentration, the more pronounced is a serial arrangement of solid
299 material and air inclusions (Figure 7c). This is mostly attributed to the significantly
300 different particle size of indomethacin ($\approx 13\mu\text{m}$) compared to that of MCC ($\approx 50\mu\text{m}$).
301 The increase in the API concentration thus causes a bimodal particle size distribution. It
302 is well-known that in the majority of cases a smaller size of particles yields a higher tablet
303 strength as the smaller particles provide a larger total surface area for bonding than the
304 larger particles (Sun and Grant, 2001). However, a multimodal particle size distribution
305 also affects the pore structure as smaller particles fit within the pores between larger
306 particles, which eventually affects the arrangement of the solid phase and the pores.

307 Moreover, the most significant changes in the pore structure were observed when
308 altering porosity, tablet thickness and API concentration simultaneously (Figure 7d-f).
309 This yields a serial arrangement of solid material and pores for the highest values of each
310 factor. This particularly highlights the interrelationship between these factors and the
311 microstructure of the powder compact. The orientation and shape of the pores cannot
312 be controlled by one single variable and it is the result of the initial particle properties
313 as well as the process settings.

314 The M03 batches were produced for a production-scale DoE with its main objective
315 to study the impact of three granulation states and one compaction factor on the dis-
316 integration as well as the dissolution performance of the tablets. Markl et al. (2017a)
317 recently demonstrated how the terahertz measurements of the M03 batches can be used
318 to determine the disintegration time and the API dissolved after a certain time period.
319 This study also revealed that there is a good correlation between the terahertz effective
320 refractive index, n_{eff} , and the solid fraction, i.e. porosity calculated from the true density
321 values of each constituent and the bulk density (Eq. 19). The anisotropic Bruggeman

322 model was used in this study to compute the porosity from the terahertz measurements,
323 f_{THz} (Figure 8a). Even though the range of porosities between samples is very small
324 (< 0.18) and the formulation is highly complex (four excipients and one API), the cor-
325 relation between f_{THz} and f is excellent ($R^2 = 0.97$). The very small porosities of these
326 samples render the S_a parameter very sensitive to minor deviations of the n_{eff} from
327 the ideal refractive index. This is also reflected by Figure 5c, where the span between
328 the upper and lower limits of the Wiener bounds is narrow compared to that around
329 $f_{\text{max}} = 0.37$ (porosity maximising the Wiener bounds as denoted in Eq. 17). The S_a
330 parameter ranges from 0.39 – 0.88 and there are four outliers around $S_a = 0.8$ (Fig-
331 ure 8b). These outliers correspond to the batches with the most dense granules except
332 for M03-B16 which is a batch with a slightly smaller granule density. We show here,
333 for the first time, how the granule density impacts the pore structure that affects the
334 disintegration process. The structure of the tablets thus clearly depend on the density
335 of the granules (Figure 8c). The effect of the granule density on the compaction process
336 is three-fold: i) initial granules rearrangement, ii) deformation potential, and iii) degree
337 of fragmentation of the granules.

338 The data suggest that the degree of fragmentation of the granules increases with
339 decreasing granule density and low dense granules are, therefore, acting as a more friable
340 material. Fragmentation of the granules results in smaller particles, which leads to a
341 larger total surface area for the formation of stronger bonds. In addition, the small
342 particles fill the larger pore spaces between larger particles/granules, which has a similar
343 effect on the pore structure as the increase of the API concentration for the M02 samples
344 (Figure 7c). The very low granule density yields a serial arrangement of the solid phase
345 and pores, whereas more dense granules cause a highly parallel arrangement of the two
346 phases. The highly dense granules have a preference to deform rather than fragment and
347 thus keep their integrity to some extent during compaction. Consequently, the tablet
348 can be described as a large aggregate of the original granules.

349 The total pore space is therefore constructed by the structure between and within
350 granules. The breakdown or collapse of the granules thus may also result in a less open
351 pore structure in the tablet and it will impact the tablet permeability (Wikberg and
352 Alderborn, 1990) and eventually the disintegration as well as dissolution performance.

353 However, the disintegration time and also the API dissolved after a certain period of
354 time is a function of the intragranular and intergranular pore structure as well as of the
355 surface area of agglomerated particles that are formed when the compact breaks apart
356 during disintegration (Markl et al., 2017a; van den Ban and Goodwin, 2017).

357 5. Conclusions

358 This study presents a new parameter to quantify anisotropy of porous media on the
359 basis of terahertz transmission measurements. The developed concept is not only limited
360 to the analysis of terahertz measurements, it can also be applied to data from other
361 techniques, such as ultrasound and dielectric spectroscopy. The validity and importance
362 of the proposed S_a parameter was demonstrated for three different data sets ranging
363 from a simple formulation to a complex tablet composition that is highly relevant for the
364 industry. The results of the simple formulation (set M01) confirmed the observations from
365 a previous study, which revealed that the pores are preferably orientated perpendicular
366 to the compaction direction and that this phenomenon becomes more pronounced with
367 increasing porosity.

368 The results of the second set of samples (set M02) revealed that a change in the
369 particle size distribution of the initial powder impacted the structure of the finished tablet
370 as the smaller particles filled the pores between larger particles. This could be observed
371 by increasing the API concentration (smaller particles), which caused an increase of the
372 serial arrangement of the solid phase and the pores.

373 The analysis of the pore structure of the complex formulation (set M03) indicated that
374 a high granule density causes a significant change in the pore structure, i.e. the pores and
375 solid material structure exhibits a parallel arrangement for granules with high density.
376 This strong correlation between the pore structure and the granule density supports the
377 conclusion from the formulation M02 that material properties considerably impact the
378 pore architecture. This study clearly demonstrates that the particle size and granule
379 density are of particular importance for the configuration of the pores in the finished
380 product. However, we want to stress here that the pore structure cannot be controlled
381 by one single variable. It is the result of a complex interrelationship between raw material
382 attributes (e.g. particle size and shape) and process settings (e.g. compression pressure

383 and speed) as well as process configuration (e.g. punch geometry and die size). The
384 geometry and die size particularly influence the microstructure at the edges of the tablet,
385 which would result in a change of the S_a parameter at the edge compared to that in the
386 tablet centre (as performed in this study). In future, transmitted terahertz waveforms
387 could be acquired via a raster-scan to form an image of the entire tablet, which facilitates
388 the investigation of structural variations within a tablet.

389 We have shown how terahertz transmission measurements of pharmaceutical powder
390 compacts coupled with the S_a parameter provide an approach to gain new insights into
391 the pore structure. This will eventually lead to a better understanding of the relationship
392 between the structure and the disintegration as well as the dissolution performance of
393 pharmaceutical tablets.

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