

1 **An investigation of the wake recovery of two model hori-** 2 **zontal-axis tidal stream turbines measured in a laboratory** 3 **flume with particle image velocimetry**

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13 **ABSTRACT:** The uptake of tidal stream-turbine (TST) technology lags other renewable energy sources
14 despite the advantages of predictability, stability and increased power output in comparison to wind tur-
15 bines of the same dimensions. There remains a need to address environmental concerns about the poten-
16 tial impacts of TSTs including the suspension and deposition of bed sediments if TSTs are to be more
17 widely accepted and deployed. Sediment mobilisation and persistent flow vortices will also adversely af-
18 fect the performance of other TST devices in an array downstream of the wake. The focus of this work is
19 to improve our understanding of the wake recovery structure of a TST to build on the limited field and
20 laboratory data currently available in order better predict the impact of TSTs on flow and sediment
21 transport. Detailed measurements of the wake flow structures generated by scaled TST devices are pre-
22 sented. These results are the first to be derived from the application of high spatial resolution stereoscopic
23 Particle Image Velocimetry (PIV). Two scale model horizontal-axis TSTs were manufactured and de-
24 ployed in a laboratory flume (11m long, 1.6m wide and 0.6m deep) at different flow speeds and heights
25 above the bed. The results demonstrate greater wake recovery lengths for the rotor design with wider
26 blade tips, despite the higher wake turbulence generated by the blades. Wake recovery is more rapid at the

27 higher flow speed when greater turbulence from the tips is observed, but wake recovery lengths increase
28 when both rotors are positioned closer to the bed.

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30 *Keywords: Renewable, Power, Tidal, Turbine, Flow, Wake*

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32 1 INTRODUCTION

33 Horizontal-axis TSTs can harness energy from a current stream without the requirement to either channel-
34 ize or impound the flow stream (Khan et al., 2009). TSTs generate more power than equivalent-sized
35 wind turbines due to the higher density of water compared with air but consequently, there are greater
36 structural stresses placed on the turbine rotor and supporting structures (Bahaj et al., 2007). Another ad-
37 vantage that makes tidal stream devices desirable as a renewable energy source is the repeatability and
38 predictability of the power generation of bi-directional TSTs that are able to harness both ebb and flood
39 currents (Charlier, 2003). Tidal power generation has the potential to become a major source of renewable
40 energy, particularly in the UK (Burrows et al., 2009). However, take-up of the technology remains slow,
41 due partly to concerns about adverse environmental impacts on the sea-bed ecosystem (e.g. Cada et al.,
42 2007, Couch and Bryden, 2007).

43 TST wakes are characterised by a reduction in flow velocity downstream of the rotor and accelerated
44 flow around the rotor (McCombes et al., 2011). For an array of TSTs, the wake effects of the upstream
45 turbines affect the inflow conditions for downstream turbines causing a potential decrease in kinetic en-
46 ergy available to the rotor and an increase in unsteady flow velocity fluctuations. Turbulence generated at
47 the rotor blade tips increases the bed shear stress downstream of the TST (Jordan et al., 2015) with poten-
48 tial adverse impacts on sediment transport and scour in the vicinity of the downstream TST supports. A
49 good understanding of the wake development is therefore necessary to determine the optimal distance be-
50 tween TST devices in an array. Wake widths expand with distance downstream of the turbine but may
51 become constrained by the water surface, altering the wake structure when compared with unconstrained
52 flows (Myers et al., 2008). The lateral spacing of TST devices is also an important consideration as the
53 wake recovery length has been shown to decrease as a result of the increased mixing caused by higher
54 turbulence generated between the two adjacent TST wake structures (Stallard et al., 2013). Physical mod-
55 elling of TSTs has previously focused on wake characterisation and the influence of turbulence on gener-
56 ating performance (e.g. Maganga et al., 2010) and, more recently, on scour development (Hill et al.,
57 2014). Measurement of flow in laboratory flumes has tended to focus on the central vertical plane of a
58 single rotor design using Acoustic Doppler Velocimeters (ADV) to obtain point measurements of flow
59 across planes intersecting the TST wake (e.g., Chamorro et al. (2013), Maganga et al., (2010)). More re-
60 cently, Simmons et al. (2015) demonstrated the importance of the rotor design on the generation of vorti-
61 ces at the blade tips and the influence of those vortices in the development of turbulent flow structures

62 several rotor diameters downstream of the TST using Particle Image Velocimetry (PIV). Similarly, Jordan
63 et al. (2015) reported on the wake asymmetry that arose from the deployment of one design of rotor posi-
64 tioned close to a roughened bed using PIV.

65 This study utilises a PIV system to measure flow velocity vectors in high resolution within 2D vertical
66 interrogation areas at different positions across the channel. This enables an improved characterisation of
67 the turbulent wake structure downstream of the TST rotor and the recovery of the structure through inter-
68 action with the surrounding flow. Results are presented from an examination of factors thought to affect
69 wake recovery downstream of the rotor including comparisons between two different rotor designs, two
70 different rotor heights above the bed within the turbulent boundary layer and two different inlet flow
71 speeds. A discussion of the effect of these factors on the wake structure is presented that focusses on dif-
72 ferences in mixing related to the structure and magnitude of turbulent kinetic energy in the downstream
73 wake.

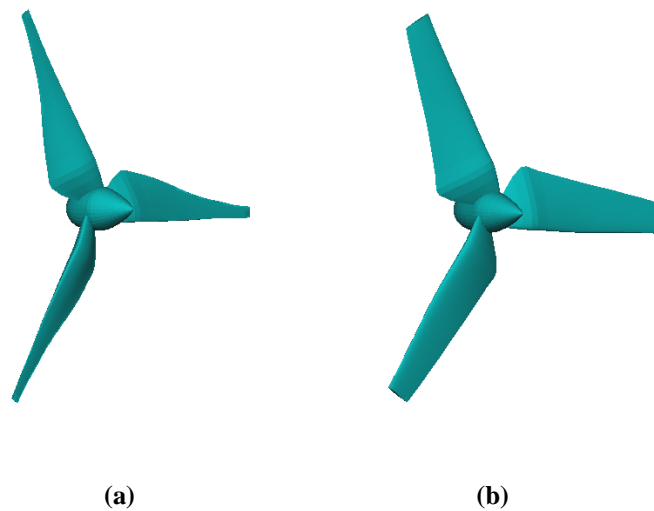
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75 2 EXPERIMENTAL SETUP

76 Experiments to quantify the impact on flow structure of two contrasting model rotors were conducted at
77 the Total Environment Simulator (TES) at the University of Hull. The TES is a re-circulating flume and a
78 working channel of 1.6 m width was constructed using partition walls to give a working section of 11 m
79 length with a water depth of 0.6 m. The channel width minimised the side-wall effect and enabled the PIV
80 camera housing to be mounted on a traverse in a separate section of still water outside the experimental
81 channel. The bed of the channel was constructed from varnished, plywood boards and the flow depth en-
82 sured that the 0.2 m diameter rotors were sufficiently separated from flow surface effects (Stallard et al.,
83 2013). Two flow regimes were used in the experiments with depth-averaged streamwise flow speeds of
84 0.26 ms^{-1} and 0.50 ms^{-1} . These are referred to herein as low flow and high flow respectively. The high
85 flow regime flow rate was chosen as it was the highest flow rate at which the rotational speed of the mo-
86 tor, used to control the speed of the rotor, could be kept constant.

87 Two different rotor models were designed at the University of Strathclyde for the experiments and are
88 shown in Fig. 1. Both horizontal-axis three-bladed rotors have a diameter of 200 mm. Rotor A has a twist
89 of 17.6° and 5° fixed blade pitch, NACA 63-415 aerofoil and a tip thickness to blade radius ratio of 0.05.
90 The blade design for Rotor B is based on that described by Vybulkova et al. (2015). It has a blade twist of
91 18.58° from root to tip (including blade pitch angle that was fixed), aerofoil NACA 0012 aerofoil and a
92 tip thickness to blade ratio of 0.141. The rotor designs are available as stereolithography (STL) files in the
93 supplemental material. Both rotors have comparable power coefficients but different aerofoil and blade-
94 tip shapes to provide a comparison between the impact of narrow-bladed and wide-bladed rotors on flow
95 structure. In practice, TSTs are likely to be designed with wider blade tips than similar horizontal-axis
96 wind-turbine rotors in order to provide structural strength to withstand the greater forces placed on them

97 (Fraenkel, 2010). The model rotors used in the flume were manufactured from these designs using stereo-
98 lithography and were mounted on an 8 mm diameter shaft attached to a motor through a watertight seal
99 and flexible coupling. The rotor speed was controlled by the 25W DC motor that enabled the tip-speed
100 ratio of the rotor to be set and controlled remotely. The motor was chosen to provide sufficient stability
101 and power to control the rotor at a tip-speed ratio of 5.5, chosen to represent the maximum of the power
102 curve, for the low flow regime (137 RPM) and high flow regime (263 RPM) but with a small diameter to
103 minimise the impact of the motor housing on the flow. The motor housing and support were designed as a
104 solid piece with a 32mm diameter housing attached to a 68 mm x 6 mm solid fin that enabled the rotor to
105 be supported from above and positioned at different heights above the channel bed. The rotor was sup-
106 ported from above to enable quantification of the rotor's impact on flow without the impediment of a bed-
107 mounted support. The rotor was positioned ~6.5 m from the inlet to allow the flow to become fully devel-
108 oped before encountering the rotor. Fig. 2(a) shows Rotor B attached to the housing from a position up-
109 stream in the channel looking towards the channel outlet. The power and control cables exit the housing
110 through a seal at the downstream end of the housing.



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Fig. 1. CAD images of the two rotor designs: (a) Rotor A and (b) Rotor B

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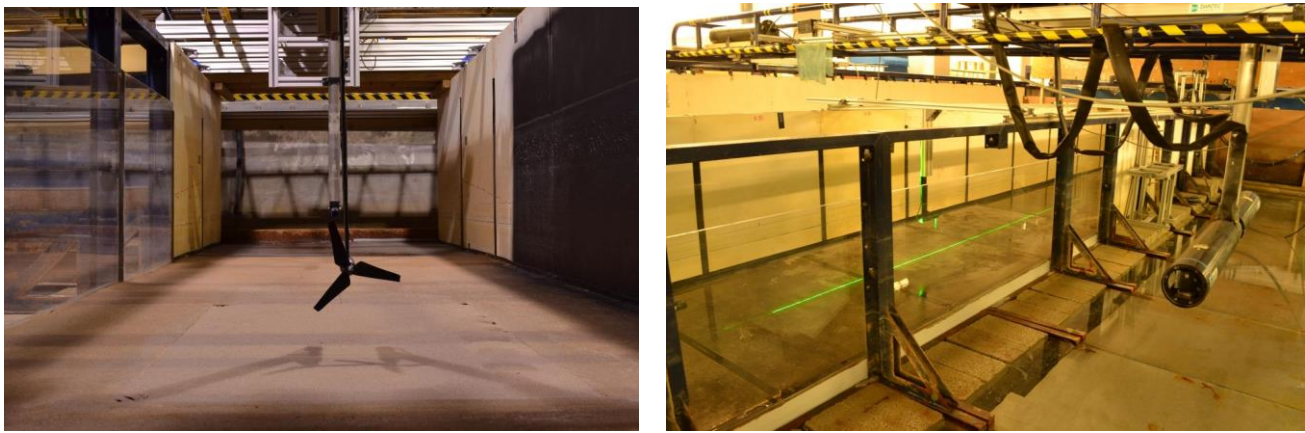
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Images of the laser-illuminated, seeded flow downstream of the rotor were captured with two submersed cameras that formed a stereoscopic, dual-pulse laser PIV system. The system thus enabled the derivation of 3-component velocity vectors across a 2D interrogation area aligned with the streamwise axis. The laser was positioned downstream of the rotor on a frame mounted above the channel. The laser beam was directed through an optic, positioned approximately 0.2 m above the channel bed at around 2 m downstream of the rotor, which created a vertical, light-sheet orientated parallel to the channel centreline. The intersection of the light-sheet with the channel bed and the cylindrical camera housing is seen in Fig. 2(b) before the tank was filled with water. The laser-mounting and the camera housing traverse allowed the light-sheet to be re-positioned at different locations across the channel whilst maintaining the geometrical arrangement between the light-sheet and the two cameras, which captured images through the clear, Perspex walls from positions downstream and upstream of the interrogation area. The traverse also allowed

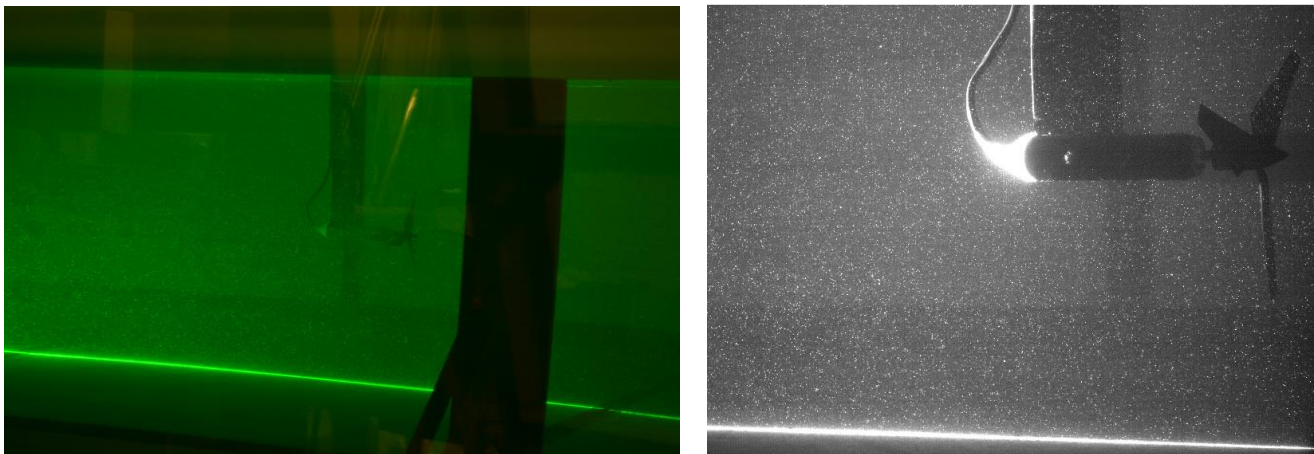
125 the camera housing to be moved to different positions in the streamwise and vertical axes. Image pairs of
126 2320 pixels by 1726 pixels were captured with an interval of 3000 μ s on two digital cameras at a repeti-
127 tion frequency of 30 Hz covering a field of view of approximately 440 mm x 310 mm. A 3D calibration
128 was obtained for the system using a multi-level target positioned on the centreline of the channel. During
129 experiments, the flow was carefully seeded with a concentration of particles that enabled high resolution
130 PIV processing without attenuating the light-sheet due to particle scattering. The seeding material used
131 throughout the experiments was a copolymer coating powder with a quoted size range of 95% less than
132 180 μ m. Fig. 3(a) shows the seeding material illuminated by the light-sheet during acquisition. Fig. 3(b)
133 shows a typical PIV camera image of the seeded flow with Rotor B in operation. The motor housing and
134 channel bed are illuminated on the centreline by the light-sheet and the control and communications cable
135 can be seen exiting the rear of the motor housing.



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137 (a)

(b)

138 Fig. 2. (a) Looking downstream towards Rotor B positioned at the centre of the channel and (b) the PIV camera housing
139 mounted below the traverse (right-hand side of image) looking through the Perspex channel side-wall prior to filling with wa-
140 ter



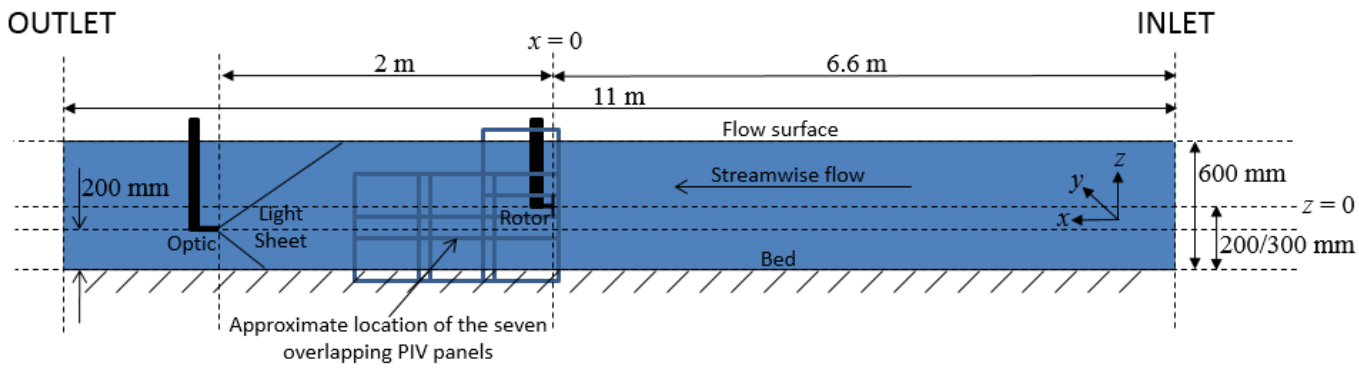
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142 (a)

(b)

143 Fig. 3. (a) Particles illuminated by the laser light-sheet at position $y = 0$ and (b) single PIV camera image

144 The schematic diagram in Fig. 4 shows a cross-section of the channel and the coordinate system used
145 herein, with x representing the streamwise direction towards the outlet, y representing the across-stream

146 direction from true left-hand side to true right-hand side and z the vertical direction upwards. Positions are
 147 described relative to the origin at the rotor cone tip. The positions of the interrogation areas in relation to
 148 the rotor and light-sheet optic are shown down-stream of the rotor. Images were acquired with the camera
 149 housing positioned at three streamwise positions downstream of the rotor cone tip, centred at $x = 196$ mm,
 150 $x = 341$ mm and $x = 586$ mm and at three vertical positions centred at $z = -49$ mm, $z = 116$ mm and $z =$
 151 281 mm relative to a rotor cone tip positioned at 200 mm above the bed. The six lower positions shown in
 152 Fig. 4 represent the full interrogation domain for the rotor experiments, covering an area of approximately
 153 three quarters of the flow depth above the bed and a length of 930 mm in the x -axis. The three positions in
 154 the vertical from the bed to the flow surface at the upstream location of $z = -49$ mm coincident with the
 155 rotor mounting were used to determine the baseline measurements of the flow in the plain channel with-
 156 out the rotor and support.
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 159 Fig. 4 Flume cross section showing the positions of the seven PIV interrogation areas in relation to the rotor and light-sheet
 160 optic

161 Sets of 3600 image pairs were acquired at each location over a period of 120 s which was sufficient to
 162 capture the mean flow statistics. Image sets were collected at intervals of 30 minutes to allow for data ac-
 163 quired to RAM to be transferred to storage disks. The acquired PIV images were processed using Dantec
 164 Dynamic's capture and processing software, Dynamic Studio. The results presented herein were obtained
 165 using the 'Adaptive PIV' algorithm (Theunissen et al., 2007), which iteratively adjusts the size and shape
 166 of the image interrogation window on the basis of local seeding density and velocity gradient. Baseline
 167 profiles for the plain channel without the rotor and support, were obtained with a grid spacing of 16 x 16
 168 pixels, a minimum interrogation area of 32 x 32 pixels and a maximum interrogation area of 64 x 64 pix-
 169 els.

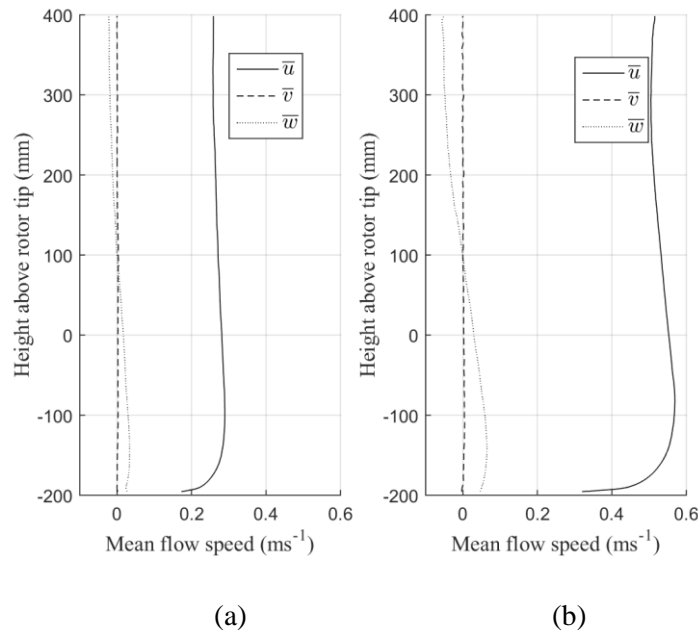
170 3 RESULTS

171 Fig. 5 shows the mean values of the streamwise, u , across-stream, v , and vertical, w , components of the
 172 velocity vectors obtained by averaging the velocity vector components between the x -axis limits of 125
 173 mm and 384 mm downstream of where the rotor cone tip would be positioned at ~ 200 mm above the bed

174 ($x = 0, y = 0, z = 0$). Fig. 5(a) and (b) show the respective mean profiles for the low flow and high flow
 175 regimes. Similar patterns in the mean components of velocity, \bar{u} , \bar{v} , and \bar{w} , are observed for both flow
 176 regimes: \bar{u} increases as expected from the boundary at the channel bed to $z = \sim 100$ mm, however there is
 177 a marginal decrease in mean flow speed higher in the water column with a local minimum below the flow
 178 surface at around 400 mm above the origin. This effect is likely to be caused by secondary currents that
 179 characterize flow in channels with low width to depth ratios (e.g. Nezu and Nakagawa., 1993). The mean
 180 of the vertical component, \bar{v} , is close to zero throughout the water column but a small across-stream cir-
 181 culation is shown in the values of \bar{w} with a root mean square value through the full flow depth of 0.019 m
 182 s^{-1} at the low flow regime and 0.042 m s^{-1} at the high flow regime. Values of shear velocity, u_* , are de-
 183 rived as $u_* = 0.016$ m s^{-1} for the low flow regime and $u_* = 0.031$ m s^{-1} for the high flow regime using a
 184 regression of the lower 50 mm of the streamwise velocity and log of the normalised height above the bed,
 185 where

$$u_* = \frac{\kappa \cdot u}{\ln(Z/Z_0)} \quad (1)$$

186 and κ is the von Karman constant, with a value of 0.40, Z is the height above the bed, and Z_0 is the full
 187 flow depth from bed to surface.



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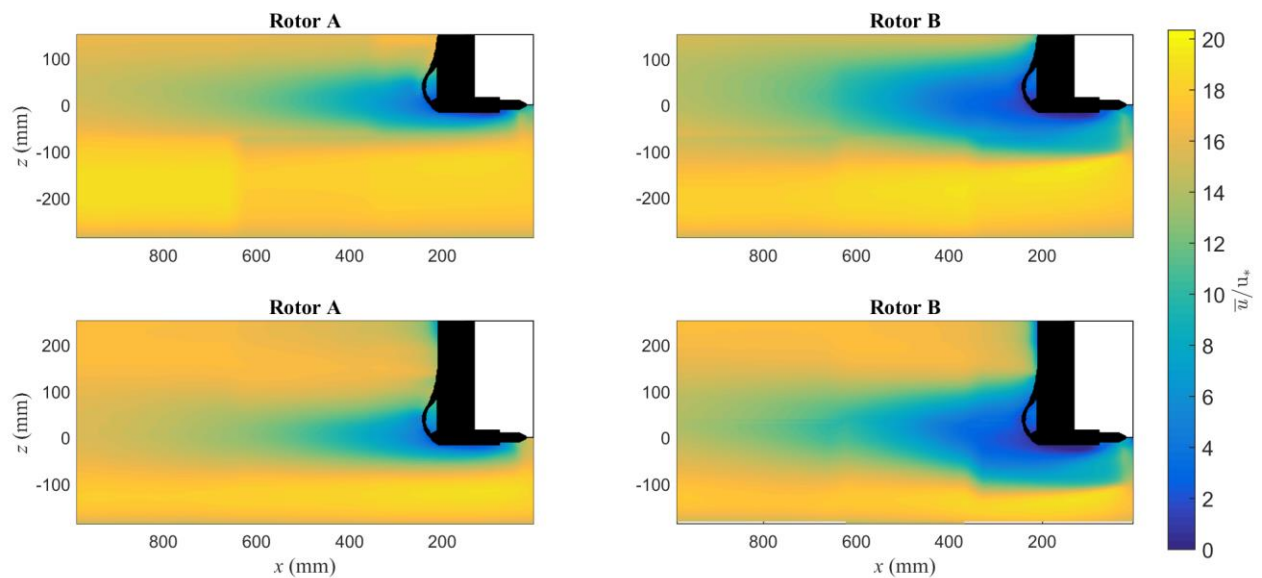
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190 Fig. 5. Mean velocity components, \bar{u} , \bar{v} and \bar{w} , for the plain channel low flow regime, (a), and high flow regime, (b)

191 Figs. 6-11 show flow maps derived by combining the statistics of six PIV interrogation areas for both
 192 Rotor A and Rotor B with the rotor centres positioned at 200 mm and 300 mm above the bed. The veloc-
 193 ity statistics were derived from the results obtained by processing using adaptive PIV with a grid spacing
 194 of 32×32 pixels, a minimum interrogation area of 16×16 pixels and a maximum interrogation area of 32
 195 $\times 32$ pixels. The overlapping areas of the interrogation areas around the border were removed and slight
 196 differences between adjoining areas can be seen which probably result from the low frequency flow struc-
 197 tures present in the channel. The approximate location of the rotor tip, shaft, motor housing, support and

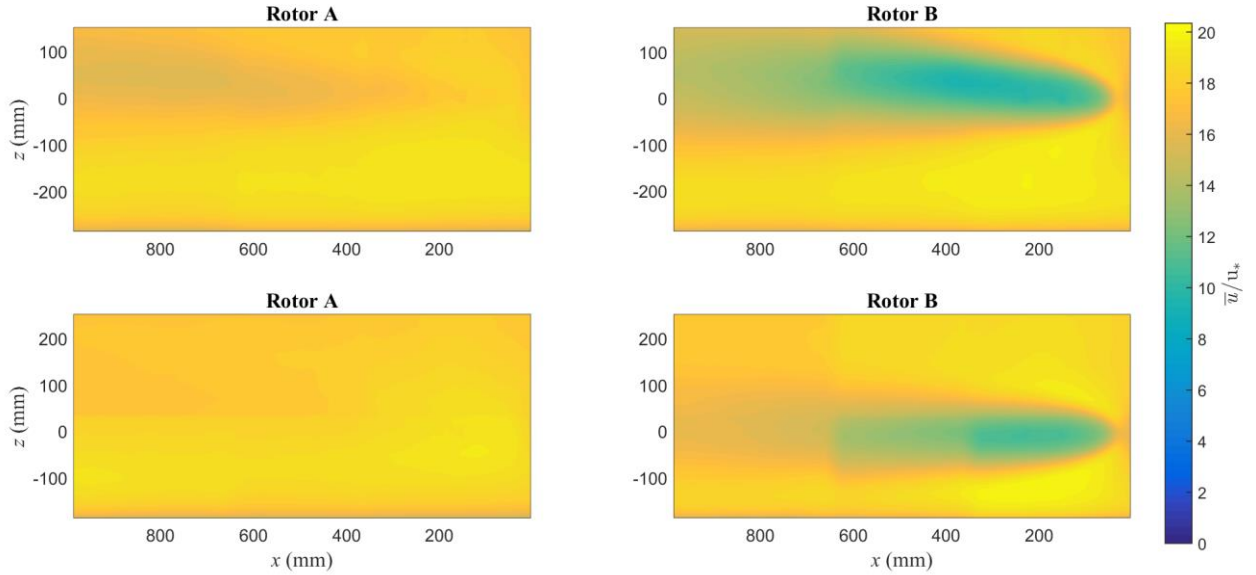
198 control cable are blanked out in black for results obtained on the centreline. However, there are regions
199 near the blanked area that may contain artefacts related to the solid objects in the image. The top right
200 corner of the images are blanked out in white as this region, upstream of the housing and support, was not
201 illuminated by the light-sheet.

202 Fig. 6 shows the normalised mean of the streamwise component of velocity, \bar{u}/u_* , for the high flow
203 regime on the centreline. A wake region of decelerated mean flow can clearly be discerned downstream
204 of the rotors. The vertical width of the decelerated wake structure is greater for Rotor B compared with
205 Rotor A. Fig. 7 shows the equivalent plots for the data acquired at $y = -100$ mm. There is little change to
206 the mean values of \bar{u}/u_* for Rotor A compared with the plain channel flow without the rotor shown in
207 Fig. 5. However, there is a marked deceleration for Rotor B. The greater vertical extent of the wake decel-
208 eration on the centreline and the deceleration at $y = -100$ mm for rotor B can be explained by the in-
209 creased blockage to the flow related to Rotor B's wider rotor blade tips.



210

211 Fig. 6. Flow maps of normalised mean streamwise flow speed for Rotor A (left) and Rotor B (right) positioned at 300 mm
212 (top) and 200 mm (bottom) above the bed for the channel centre ($y = 0$) at the high flow regime



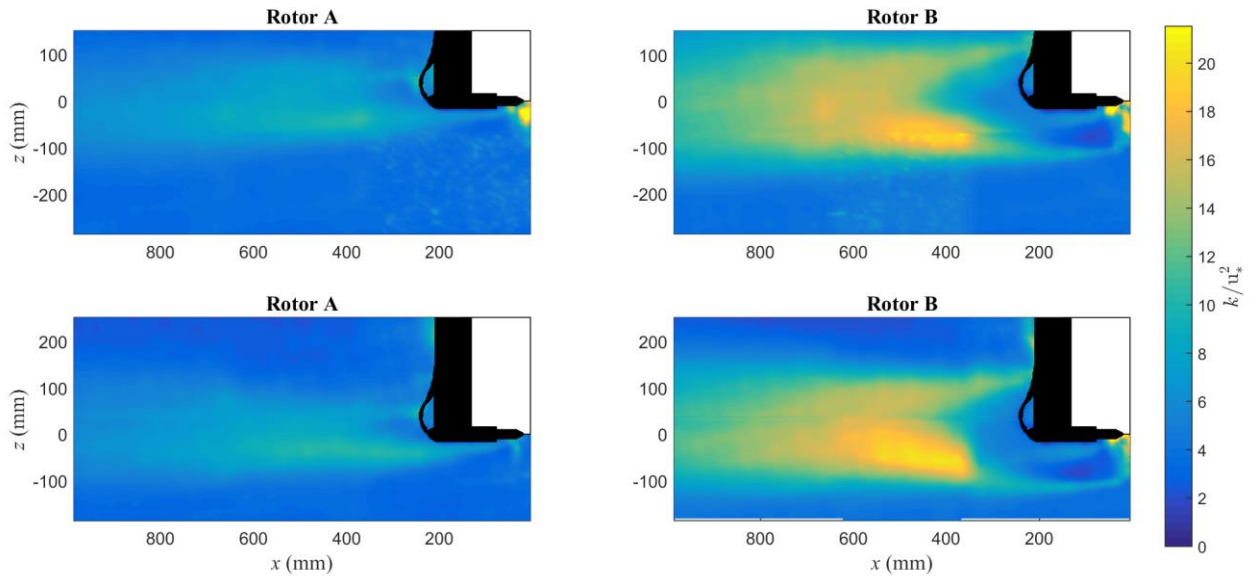
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214 Fig. 7. Flow maps of normalised mean streamwise flow speed for Rotor A (left) and Rotor B (right) positioned at 300 mm
 215 (top) and 200 mm (bottom) above the bed at 100 mm off the channel centre on the true left-hand side ($y = -100$ mm) at the high
 216 flow regime

217 The plots in Fig. 8 show the normalised turbulent kinetic energy, k/u_*^2 , for Rotor A and Rotor B and
 218 for rotor tip positions of 300 mm and 200 mm above the bed where k is defined as:

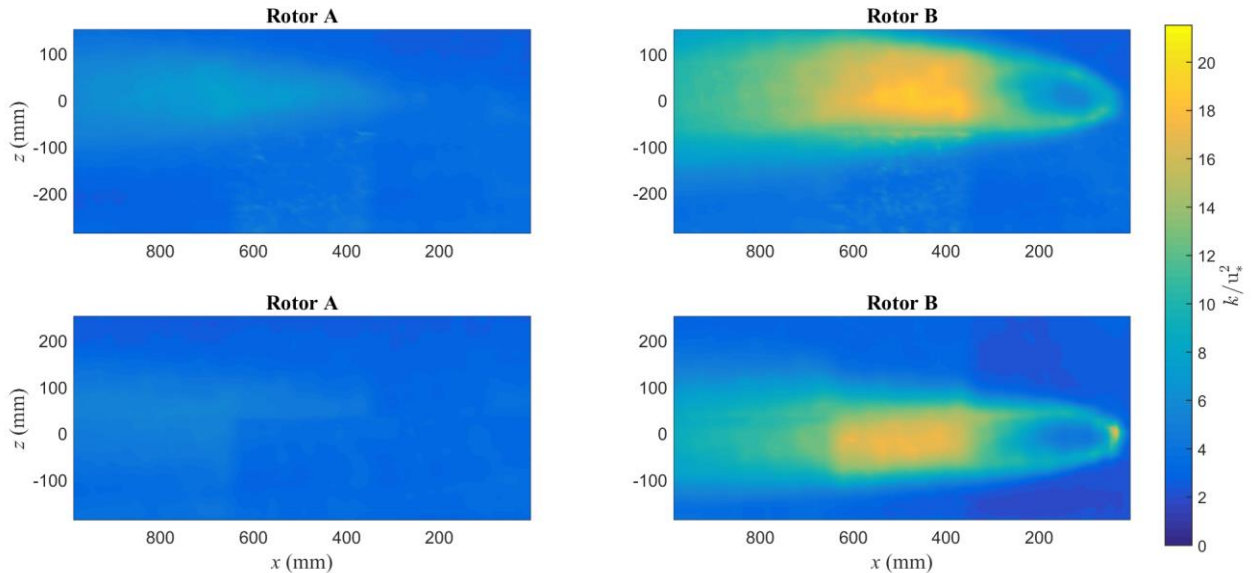
$$k = \frac{1}{2} (\overline{u'^2} + \overline{v'^2} + \overline{w'^2}) \quad (2)$$

219 and where u' , v' and w' , denote the fluctuating component of u , v , and w about their respective mean
 220 values. Two regions of higher magnitude turbulent kinetic energy, originating from the upper and lower
 221 surface of the motor housing, can be seen propagating downstream from an origin close to the centre of
 222 Rotor A and merging between $x = 300$ and $x = 400$ mm. Similar regions of higher intensity k/u_*^2 origi-
 223 nating from the surfaces of the motor housing, can be seen for Rotor B. However, a much larger magni-
 224 tude wake structure develops from two narrow regions of higher k/u_*^2 values that propagate from the
 225 location of the rotor blade tips of Rotor B at $x = 0$ mm, $y = 0$ mm, $z = \pm 100$ mm and which then merge to
 226 form a single region of high intensity between 400 mm and 600 mm downstream of the rotor. At $y = -100$
 227 mm, for Rotor A (Fig. 9), there is a marginal increase in k/u_*^2 downstream from around $x = 400$ mm cen-
 228 tred on the $z = 0$ mm axis but there is a much more marked increase in the magnitude of k/u_*^2 in the
 229 wake of Rotor B. Two narrow regions originating from a position coincident with the centre of the rotor
 230 in the $y = -100$ mm plane extend downstream and merge around $x = 200$ mm to $x = 300$ mm. The upper
 231 and lower boundaries of the high intensity region grow in vertical extent with distance downstream with
 232 the highest magnitudes around the vertical centre of the wake between approximately $x = 300$ mm to $x =$
 233 700 mm. The results show the greater vorticity generated by the wider tips of Rotor B.



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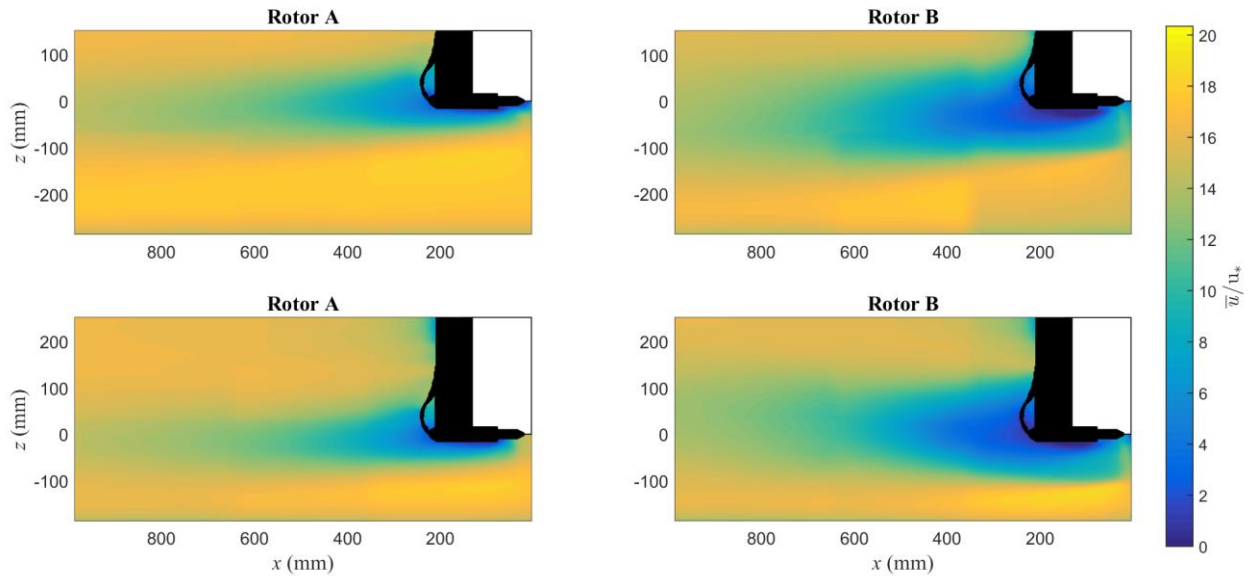
235 Fig. 8. Flow maps of normalised turbulent kinetic energy for Rotor A (left) and Rotor B (right) positioned at 300 mm (top) and
 236 200 mm (bottom) above the bed for the channel centre ($y = 0$) at the high flow regime



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238 Fig. 9. Flow maps of normalised turbulent kinetic energy for Rotor A (left) and Rotor B (right) positioned at 300 mm (top) and
 239 200 mm (bottom) above the bed at 100 mm off the channel centre on the true left-hand side ($y = -100$ mm) at the high flow re-
 240 gime

241 Fig. 10 shows the flow maps of the normalised mean streamwise velocity, \bar{u}/u_* , and Fig. 11 shows
 242 the flow maps of the normalised turbulent kinetic energy, k/u_*^2 , at the low flow regime. The wake struc-
 243 tures in Fig. 10 can be seen to extend further downstream compared with the equivalent plots for the high
 244 flow regime shown in Fig. 6. Lower magnitude values of k/u_*^2 can be seen in the wake at around $x = 300$
 245 mm to $x = 700$ mm at the lower flow regime in Fig. 11 compared with the same four scenarios presented
 246 in Fig. 8 at the high flow regime.

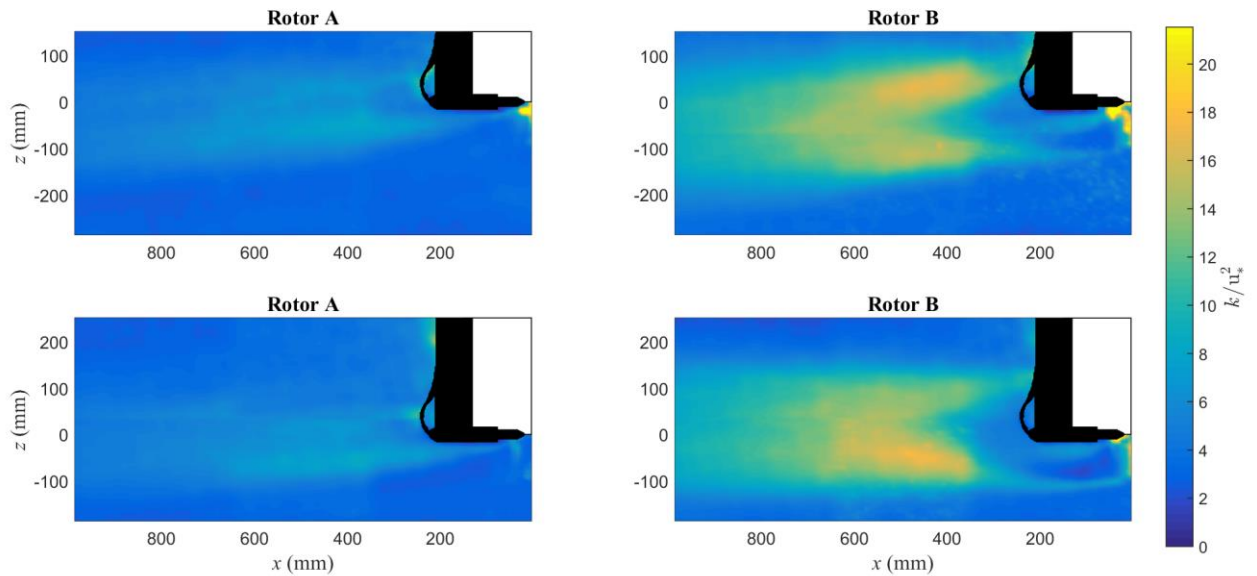


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Fig. 10. Flow maps of normalised mean streamwise flow speed for Rotor A (left) and Rotor B (right) positioned at 300 mm (top) and 200 mm (bottom) above the bed for the channel centre ($y = 0$) at the low flow regime



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Fig. 11. Flow maps of normalised turbulent kinetic energy for Rotor A (left) and Rotor B (right) positioned at 300 mm (top) and 200 mm (bottom) above the bed for the channel centre ($y = 0$) at the low flow regime

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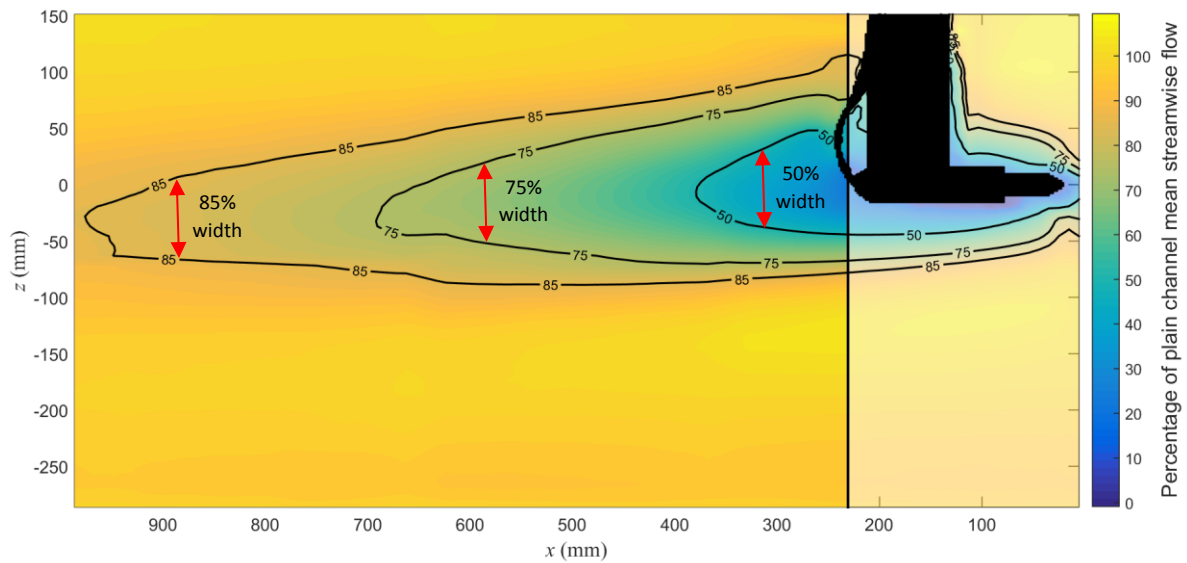
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To assess the development of the wake recovery with distance downstream from the rotor, the mean streamwise component of flow is expressed as a percentage of the mean streamwise profile through the water column that was measured for the plain channel without the rotor and support present for both flow regimes, as shown in Fig. 5. Fig. 12 demonstrates an example of the wake structure expressed in these terms for one of the scenarios, with Rotor A positioned 300 mm above the bed at the low flow regime. The vertical width of the wake is evaluated downstream of $x = 230$ mm, denoted by the vertical line, as velocity vectors in the region closer to the rotor are reasoned to be influenced by the image of the rotor support. The contour lines denote where the mean streamwise flow velocity is 85%, 75% and 50% of the plain channel values at the same height above the bed. The vertical width of the wake is defined as the vertical distance between the same contour line, as shown in the plot. The vertical width is thus evaluated

263 for the eight different experimental scenarios involving Rotor A and Rotor B at both flow regimes and
 264 with the rotor cone tip positioned at 200 mm and 300 mm above the bed. Fig. 13 shows the development
 265 of the vertical width for the eight scenarios for widths defined as (a) 85%, (b) 75% and (c) 50% of the
 266 mean streamwise flow velocity.



267
 268 Fig. 12 Mean streamwise flow as a percentage of the mean vertical profile of the plain channel flow for Rotor A positioned 300
 269 mm above the bed at the low flow regime. The vertical wake widths are defined by the contours at 50%, 75% and 85%
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271 For three of the scenarios, all involving Rotor A, the wake velocity recovers to exceed 85% of the
 272 mean plain channel flow velocity within the measurement area, as shown in Fig. 13(a). At the other ex-
 273 trem, the vertical width is still between ~ 75 and ~ 200 mm at the farthest measurement location down-
 274 stream at $x = 986$ mm for all four scenarios involving Rotor B, which all have slower wake recovery
 275 throughout the extent of the downstream measurement range compared with the same flow regimes and
 276 positions above the bed for Rotor A. The wake remains larger in vertical extent at the end of the measure-
 277 ment area ($x = 986$ mm) in all cases where the rotor positioned at 200 mm above the bed compared with
 278 the rotor at 300 mm above the bed, suggesting that wake recovery is slower when the rotor mounted
 279 closer to the bed surface. The wake width is also reduced at the farthest extent downstream or has fully
 280 recovered more rapidly for all scenarios at the high flow regime compared with the low flow regime. Fig.
 281 13(b) shows that the wake velocity has fully recovered to 75% of the mean plain channel flow velocity
 282 within the measurement area. The wake velocity exceeds 75% of the mean plain channel flow velocity for
 283 all four Rotor A scenarios between $x = \sim 630$ mm and $x = \sim 730$ mm. This contrasts sharply with Rotor B,
 284 for which the mean streamwise flow velocity recovers to exceed 75% of the mean plain channel flow ve-
 285 locity between $x = \sim 800$ mm and $x = \sim 900$ mm. For all scenarios, recovery to greater than 75% occurs at a
 286 greater distance downstream with the rotor positioned at 200 mm above the bed compared with 300 mm
 287 above the bed. Except for Rotor B at 300 mm above the bed, the distance downstream to full recovery
 288 above 75% of the mean flow velocity occurs at a greater distance downstream for the low flow regime

289 than for all other scenarios. For recovery to greater than 50% of the mean plain channel streamwise flow
290 velocity, shown in Fig. 13(c), the difference in recovery distance downstream of the rotor cone tip is no-
291 ticeably different for Rotor A at $x = \sim 400$ mm and Rotor B at $x = \sim 440$ mm to $x = \sim 450$ mm. Differences
292 in full recovery distance to greater than 50% are difficult to discern for comparisons between flow re-
293 gimes and rotor position.

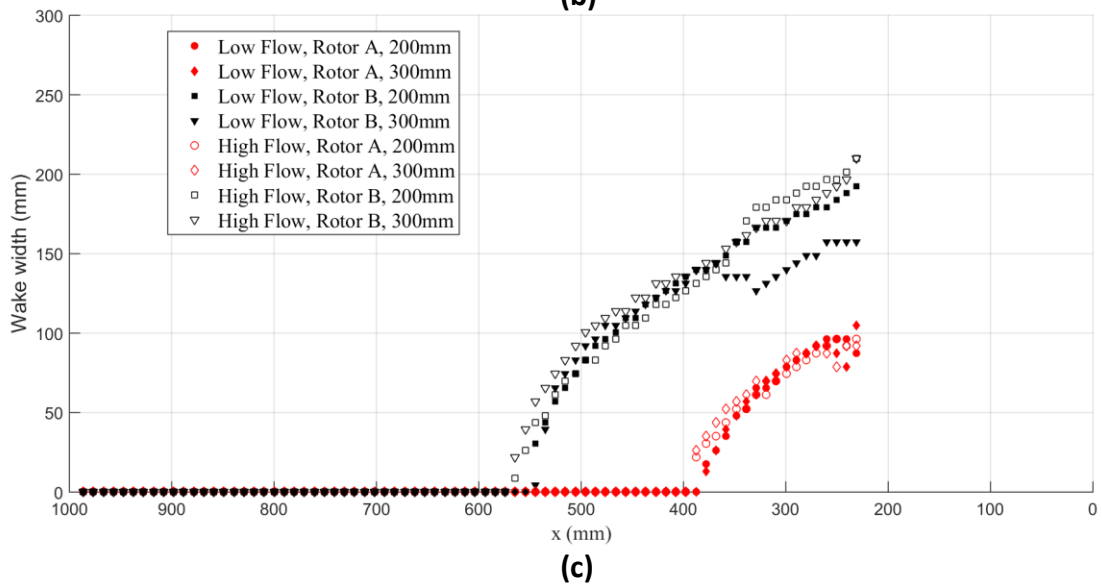
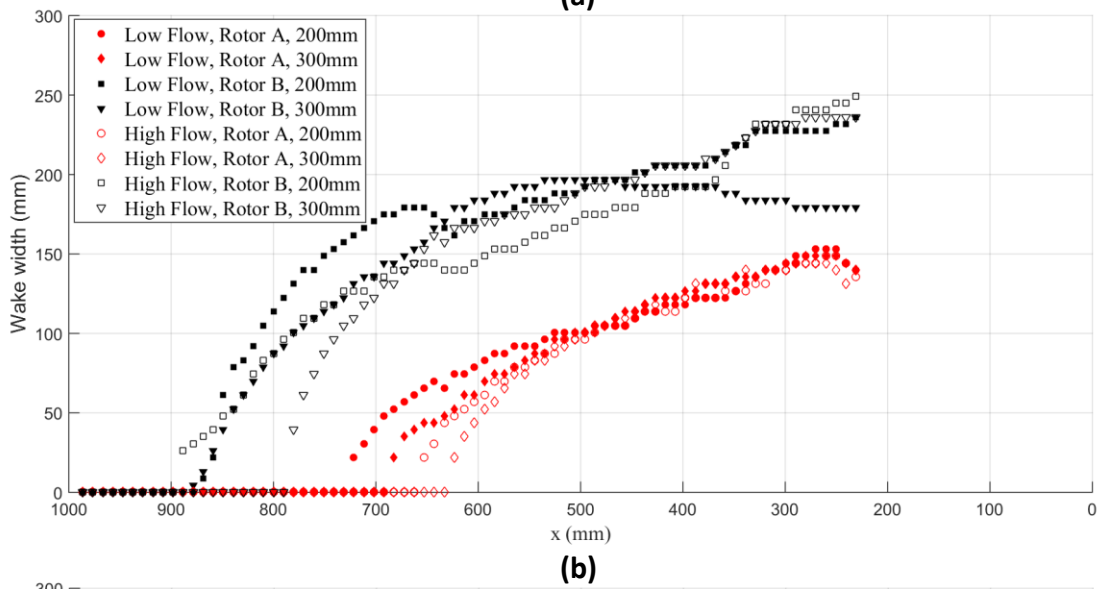
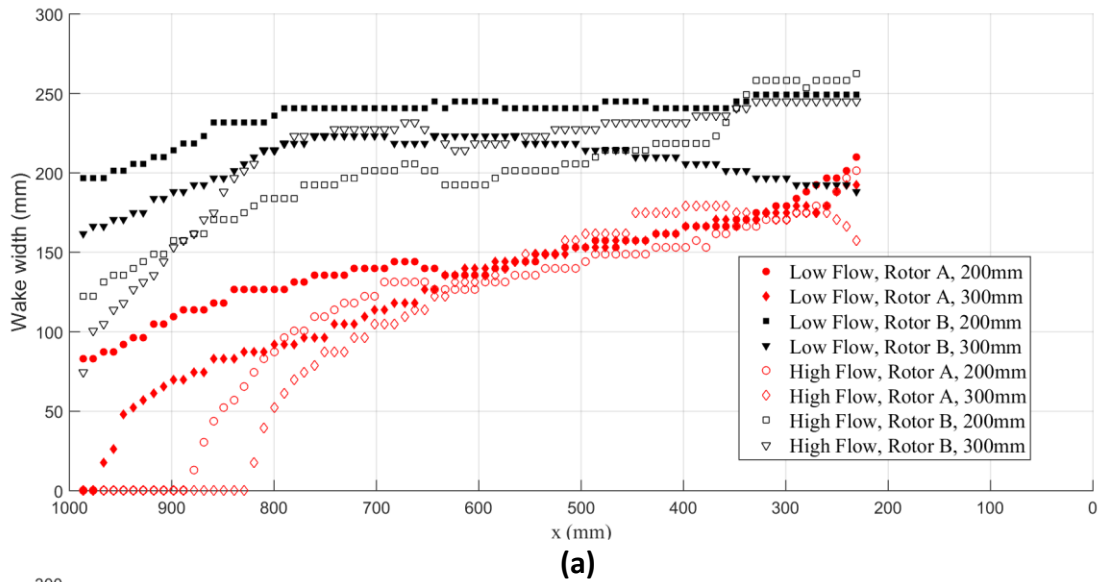
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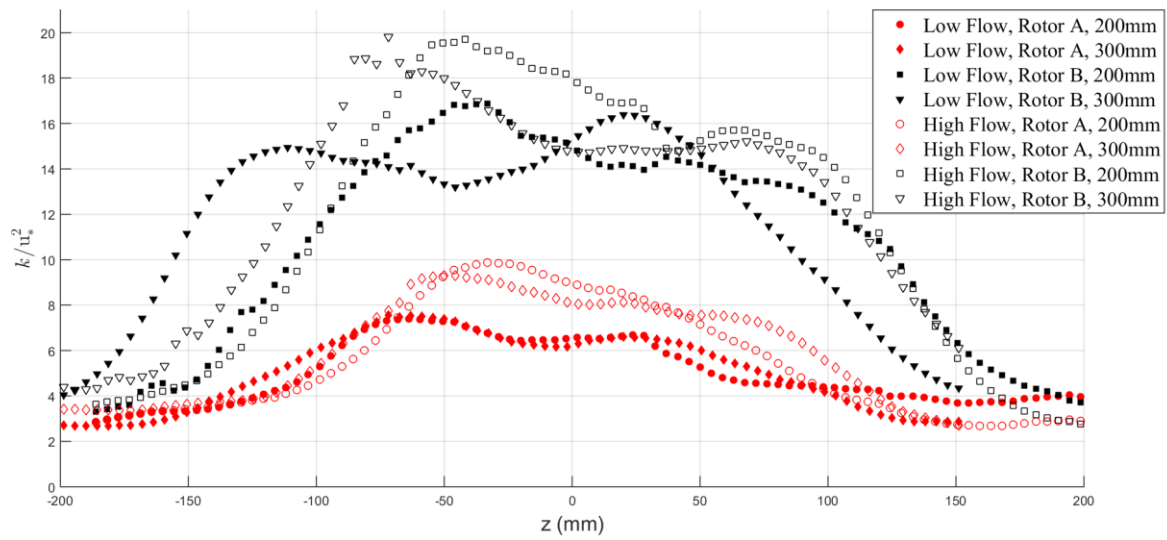
300 Fig. 13. Wake width downstream of the rotor calculated using a threshold of (a) 85%, (b) 75% and (c) 50% of plain channel
 301 mean streamwise flow

302

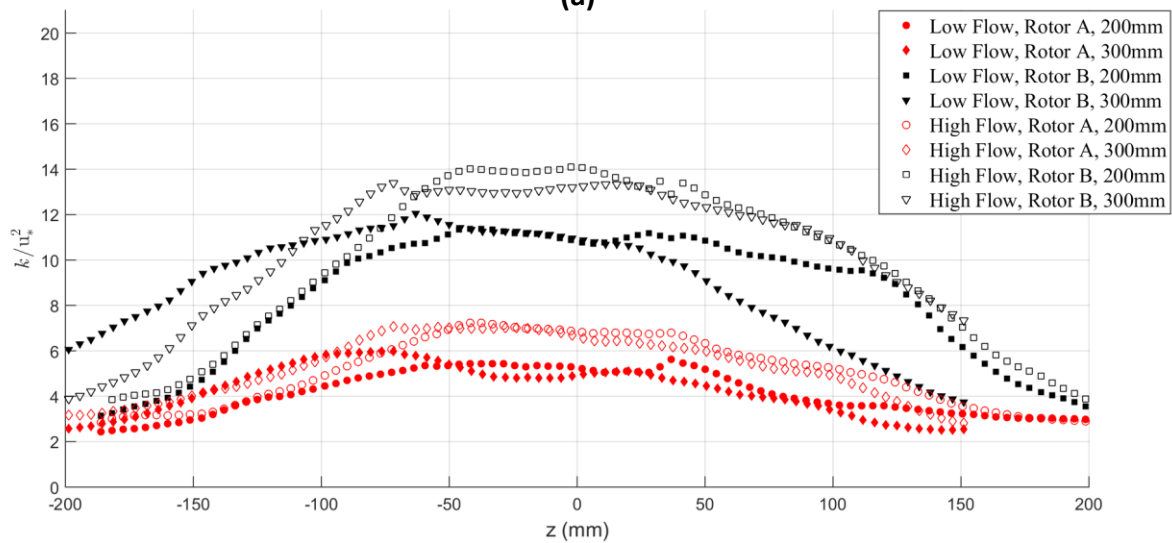
304 The slower wake recovery of the high flow regime scenarios compared with the low flow regime scenar-
305 ios shown in Fig. 13 appear to be related to reduced mixing efficiency related to the lower magnitude val-
306 ues of k/u_*^2 within the wake flow-structure which can be seen in the differences of the flow maps in Fig.
307 11 compared with Fig. 8. However, the much higher values of k/u_*^2 observed with rotor B compared with
308 Rotor A for all four scenarios in Fig. 8 and Fig. 11 do result in greater wake recovery lengths in Fig. 13
309 rather than shorter recovery lengths. This is probably due to the greater mixing required break-down the
310 initially wider wake structure that develops immediately downstream from Rotor B (Fig. 6 and Fig. 10)
311 resulting from Rotor B's greater relative flow blockage due to the wider rotor tips. Myers and Bahaj
312 (2010) report greater recovery lengths for a porous actuator disk when positioned closer to the bed but
313 without an increase in turbulent kinetic energy in the wake or between the bed and the lower boundary of
314 the wake. Similarly, Jordan et al. (2015) report results that compares the wake of Rotor B, as described
315 herein, over a roughened, flat bed with the rotor cone tip position 200 mm and 120 mm above the bed.
316 There is a marked decrease in turbulent kinetic energy in the lower half of the wake with the rotor posi-
317 tioned at 120 mm above the bed compared with 200 mm above the bed, but an increase in the wake re-
318 covery length. The increase in wake recovery lengths at 200 mm compared with 300 mm shown in Fig.
319 13 agrees, therefore, with previous observations of increased recovery lengths as the rotor is positioned
320 closer to the bed. There are noticeable changes to the distribution of normalised turbulent kinetic energy
321 in the vertical between the two rotor positions. Profiles of k/u_*^2 as a function of z are shown in Fig. 14 for
322 two locations downstream of the rotor. When the rotor is positioned at 300 mm above the bed, the profiles
323 are noticeably asymmetric for the larger wake of Rotor B at both $x = 500$ mm and $x = 800$ mm down-
324 stream of the rotor. There is greater turbulent energy for both low and high flow regimes between the bed
325 and $z = -50$ mm to -100 mm when Rotor B is positioned at 300 mm compared with the same near-bed re-
326 gion when the rotor is positioned at 200 mm above the bed. The reduction in near-bed turbulent kinetic
327 energy agrees with the larger asymmetry observed by Jordan et al. (2015) with the same rotor positioned
328 at 120 mm above the bed and suggests that less efficient mixing in the near-bed region is extending the
329 wake recovery length.

330 Factors that affect wake recovery lengths are important considerations in the layout design of TST ar-
331 rays. A longer wake recovery distance will necessitate greater streamwise distances between TST devices
332 in a rectilinear grid array to minimise the impacts of velocity deficits and unsteady fluctuations on TST
333 efficiency, and also the transport and scour of bed sediment around turbine support structures. Con-
334 versely, staggered grid arrays (see Turnock et al., 2011) may benefit from the accelerated flows surround-
335 ing the wake that will persist with greater wake recovery lengths.

336



(a)



(b)

337

338 Fig. 14 Profiles of normalised turbulent kinetic energy as a function of vertical distance relative to the rotor cone tip at (a) $x =$
 339 500 mm and (b) $x = 800$ mm downstream of the rotor

340 5 CONCLUSIONS

341 Detailed flow maps have been presented of the normalised mean streamwise flow and turbulent kinetic
 342 energy of the wakes downstream of two designs of TST rotor. The effects on wake recovery of factors
 343 including rotor design, rotor height above the bed and flow speed have been examined. The broad-tipped
 344 Rotor B generates significant vortex shedding from the blade tips that converge to form a region of high
 345 energy turbulence in the centre of the wake. In comparison, Rotor A produces a narrower wake with a re-
 346 gion of comparatively lower magnitude turbulence originating from the motor housing without significant
 347 vortex shedding from the blade tips. Wake recovery lengths for Rotor B are greater than for Rotor A de-
 348 spite the increased turbulence in the wake. This is reasoned to be caused by the increased flow decelera-
 349 tion related to the larger blockage to flow of the rotor's wider blade tips. Recovery lengths are shorter for
 350 the high flow regime where there is a region of larger magnitude turbulence in the wake compared with

351 the low flow regime. The higher magnitude turbulence is assumed to cause more efficient mixing of the
352 wake and surrounding fluid. Recovery lengths are also observed to increase when both rotors are posi-
353 tioned lower in the flow and these results agree with the results of other physical model results for rotors
354 and actuator disks within the boundary layer.

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