

THREE-DIMENSIONAL IMAGE RECONSTRUCTION IN J-PET USING FILTERED BACK-PROJECTION METHOD*

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We present a method and preliminary results of the image reconstruction in the Jagiellonian PET tomograph. Using GATE (Geant4 Application for Tomographic Emission), interactions of the 511 keV photons with a cylindrical detector were generated. Pairs of such photons, flying back-to-back, originate from e^+e^- annihilations inside a 1 mm spherical source. Spatial and temporal coordinates of hits were smeared using experimental resolutions of the detector. We incorporated the algorithm of the 3D Filtered Back Projection, implemented in the STIR and TomoPy software packages, which differ in approximation methods. Consistent results for the Point Spread Functions of $\sim 5 \div 7$ mm and $\sim 9 \div 20$ mm were obtained, using STIR, for transverse and longitudinal directions, respectively, with no time-of-flight information included.

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1. Introduction

Recent studies of plastic scintillators [1–9] proved their usefulness in the Positron Emission Tomography (PET) for the detection of gamma-quanta that originate from the electron–positron e^+e^- annihilation in matter. Such materials exhibit better timing properties than inorganic crystals, traditionally used in PET [10–13], while low scintillation efficiency remains the main disadvantage. A novel Jagiellonian PET (J-PET) scanner, composed of plastic scintillator strips, utilizes the Compton scattering for the detection of gamma quanta [1, 2, 4, 7]. This technology is expected to provide a superior figure of merit (see Ref. [7]) for the whole-body imaging, with a good axial (longitudinal) and transaxial (transverse) resolution. Preliminary experiments, made for the 30-cm single scintillator strip, reveal temporal resolution of about 80 ps (sigma of time of hit determination), corresponding to spatial resolution of ~ 2.2 cm (full width at half maximum — FWHM) along axial direction [2]. Further tests are in progress now, for the already built full scale prototype of J-PET detector.

In this paper, we analyse the spatial resolution for the J-PET scanner, based on three-dimensional (3D) image reconstruction of a simulated 1 mm spherical back-to-back gamma source, generated by the Geant4 Application for Tomographic Emission (GATE) simulation toolkit [14, 15]. Additional filtering and preprocessing were performed afterwards (described in Refs. [6, 16]). Times and positions of interactions (hits) were smeared with Gaussian distributions, reflecting the experimental resolutions of the J-PET scanner.

The parameters of the simulations are suitable for the estimation of characteristics, defined by the National Electrical Manufacturers Association (NEMA) [17]. The norm NEMA-NU-2 requires 3D Filtered Back Projection (FBP) algorithm to be used for the image reconstruction. We, therefore, incorporated this method only, foreseeing the estimation of NEMA characteristics for J-PET. As no software for 3D FBP that correctly reflects J-PET geometry has been developed yet, we adapted methods from STIR [18] and TomoPy [19] packages. Both frameworks, however, impose constraints on the algorithm, which may impact the estimation of spatial resolution.

2. Simulation setup

Simulations in GATE framework [14, 15] were performed at the Świerk Computing Centre, National Centre for Nuclear Research. The J-PET scanner was defined for an ideal geometry (Fig. 1, left) with radius $R = 437.3$ mm and length $L = 500$ mm, comprising single layer of tightly composed plastic EJ-230 scintillator strips with rectangular cross section and dimensions $7 \text{ mm} \times 19 \text{ mm} \times 500 \text{ mm}$, 384 strips in total [6, 16].

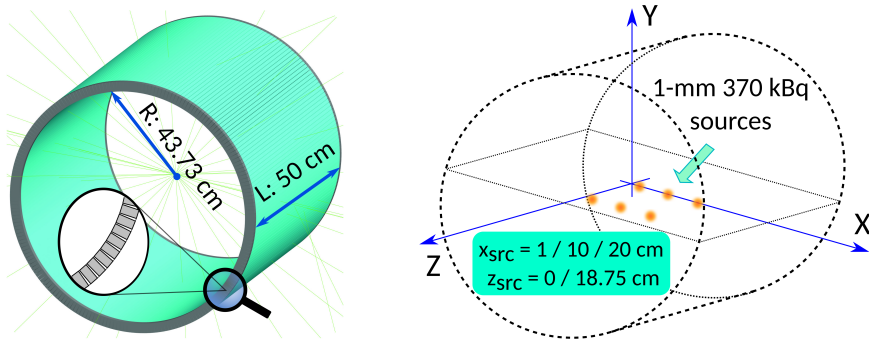


Fig. 1. Left: simulated geometry of J-PET scanner with zoom depicting the composition of strips. Right: geometrical locations of the source, one per simulation.

A point-like source was defined as a simulated phantom. Its shape, size (a sphere 1 mm in diameter) and activity (370 kBq or 10 μ Ci) were selected according to the NEMA requirements for the estimation of spatial resolution [17]. NEMA also defines locations of the source inside the scanner, specifically for detectors (like J-PET) that operate with large axial field of view (AFOV). Thus, we set 6 different, defined by the norm, locations ($x_{\text{src}}, y_{\text{src}}, z_{\text{src}}$) for the simulation (see Fig. 1, right). Along the axial coordinate z , the source was placed at the centre of the AFOV ($z_{\text{src}} = 0$ mm), or at the distance of three-eighths of the AFOV length from the centre of the scanner ($z_{\text{src}} = 187.5$ mm). For the transverse direction, x coordinate was defined at $x_{\text{src}} = 10$ mm, 100 mm and 200 mm with y always at $y_{\text{src}} = 0$ mm.

Only subsample of simulated events (pairs of hits) was selected for the reconstruction, fulfilling selection criteria required for true coincidences, which include scattering filters and energy thresholds applied (see detailed description in Refs. [6, 16]). At least 150 000 events were used for the reconstruction, for each source position. The data include coordinates and times of hits inside the strips for each photon pair, *i.e.* ($x_1, y_1, z_1, t_1, x_2, y_2, z_2, t_2$).

The tests, described in this article, encompasses three cases (for the smearing applied): assuming the spatial resolution in axial direction to be $\sigma_z = 2$ mm, 5 mm or 10 mm, whilst for the time of hit being fixed at $\sigma_t = 80$ ps (corresponding to $\sigma_z = 10$ mm [7]). The latter was chosen intentionally to test the worst possible case of time of flight (TOF) taken into account.

Thus 3D sinogram could be composed, collecting lines of response (LOR) with TOF information optionally used for each event [20].

3. Reconstruction procedure

The reconstruction of the 3D image of the source, selected for the simulations, is essential for the estimation of spatial resolution of PET detectors, which is characterized by the so-called Point Spread Function (PSF). It is defined as the width of the reconstructed profile of a point source, measured similarly to FWHM along three principal axes [20].

3.1. FBP algorithm

For a general 2D case, FBP algorithm, based on the inverse Radon transformation [21], can be defined as mapping filtered sinogram $p^F(s, \phi)$ by an operator X^* , which returns an image $f(x, y)$

$$f(x, y) = (X^* p^F)(x, y) = \int_0^\pi d\phi p^F(s = x \cos \phi + y \sin \phi, \phi), \quad (1)$$

where $p^F(s, \phi)$ is obtained by applying an apodized ramp filter $h(s)$ on the initial sinogram $p(s, \phi)$ [20]

$$p^F(s, \phi) = \int_{-R_F}^{R_F} ds' p(s', \phi) h(s - s'). \quad (2)$$

Here, R_F denotes the radius of the field of view (FOV).

In reality, scanner geometry requires sinogram variables (displacement s and angle ϕ) to be mapped onto discrete pairs (s_i, ϕ_i) . Furthermore, it transforms (1) into a sum, containing functions $p_i^F(s = x \cos \phi + y \sin \phi, \phi_i)$. Here, $p_i^F(s, \phi_i)$ can be derived for any arbitrary Cartesian pair (x, y) that defines unmapped s , using linear interpolation between $p^F(s_k, \phi_i)$ and $p^F(s_{k+1}, \phi_i)$, calculated for two “known” neighbours s_k and s_{k+1} ($s_k < s < s_{k+1}$) [20]. Practical implementations of FBP occasionally incorporate such interpolation for the increase of the resolution of the reconstructed image $f(x, y)$.

Equations for 3D FBP could be derived by turning values into vectors in (1)–(2) and simplifying the formulas, eventually using 4-dimensional sinogram functions $p(s, \phi, \zeta, \theta)$, where ζ and θ denote axial coordinate and tilt angle (obliqueness) of LOR plane, respectively [20].

3.2. Software frameworks

For the reconstruction of the point source using 3D FBP, required by [17], STIR [18] and TomoPy [19] software packages were chosen.

Since TomoPy does not provide a full 3D version of the FBP algorithm, additional data transformation must be applied. All LORs are projected onto XY -planes, orthogonal to Z -axis (as in Fig. 2, left top), which would also reduce the size of 3D sinogram. Reconstructed image is a stack of XY -slices, each obtained using 2D FBP ASTRA algorithm [22]. The number of such slices is not limited, but the simplified procedure would constrain the estimation of the longitudinal spatial resolution PSF_z . However, it could evidently be improved by adjusting axial coordinate of projected planes to e^+e^- annihilation point along LOR, estimated from times of hits t_1 and t_2 , which reflect TOF data (see Fig. 2). It is important to note that such “TOF correction” does not change FBP algorithm, with no additional kernel used, unlike known TOF reconstruction methods (see, for example, [23]).

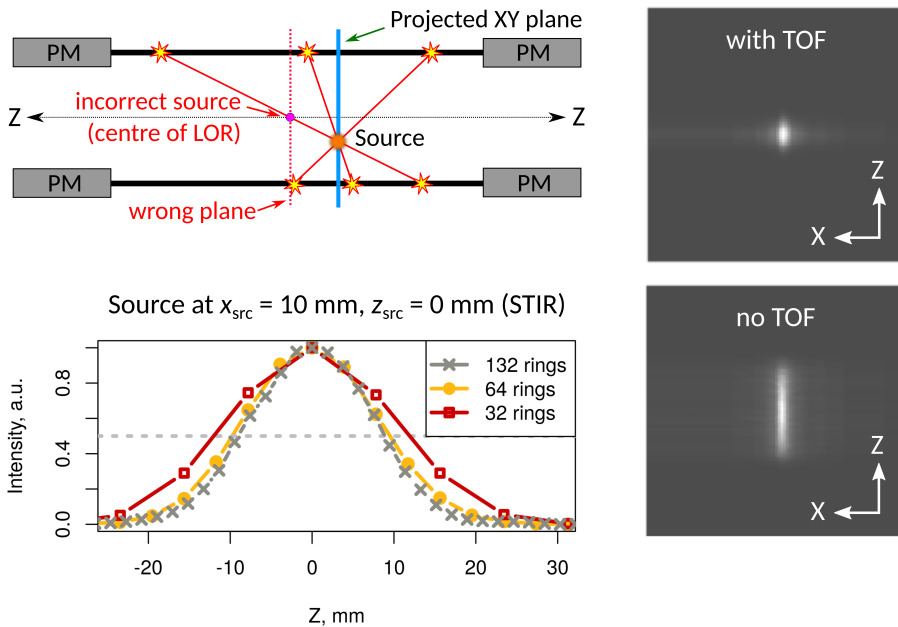


Fig. 2. (Colour on-line) Left top: LOR projection scheme. Transverse planes with and without TOF corrections are denoted by vertical solid (blue) and dashed (red) lines, respectively. Right: reconstructed image in TomoPy (using 2D FBP ASTRA algorithm) for both cases with Z -axis aligned vertically. Left bottom: axial intensity profile of the reconstructed image for various strip discretisation by rings.

STIR accepts few input formats with Interfile type of data storage [24] used for reconstruction. Because of that, for conversion of list mode output from GATE to Interfile, we employed a dedicated package, developed for SAFIR project [25, 26]. Unlike TomoPy, STIR conserves the LOR geometry

in sinogram completely, including its obliqueness towards Z -axis. Moreover, for the compensation of partial truncation of the image near the edges of AFOV, the Kinahan and Rogers method [27] for 3D FBP is implemented.

STIR and SAFIR define cylindrical scanner as a stack of axially aligned narrow rings, made of smaller size detectors. Therefore, z -component of each hit position is mapped to discrete values and eventually stored as a 1-byte index, which sets the limit of maximum number of rings to 256 [26]. This might distort the image during reconstruction, deteriorating the PSF_z estimation for J-PET. We observed little change, though, in intensity profile along Z -direction, for the number of rings above 64 (Fig. 2, left bottom).

TomoPy determines transverse resolution of the reconstructed image (number of pixels) from FOV discretisation, *i.e.* from the number of J-PET strips in our case. For better analysis, we additionally incorporated PET package [28], developed for 2D image reconstruction in R environment [29]. Unlike TomoPy, both STIR and PET packages have an option to increase image resolution for X - and Y -axes, using interpolation technique, mentioned in Sect. 3.1, which allows more accurate PSF estimation.

4. Results and discussion

The spatial resolution $\text{PSF}_{x,y,z}$ of J-PET was determined by FWHM estimation in transverse (X, Y) and longitudinal (Z) directions from the reconstructed images of a point source. Two cuts, made along maximum intensity of Z - and Y -axis (XY and XZ planes, respectively), were created for TomoPy and STIR (only XY for R PET package). Pixel size of each cut determines the error of $\text{PSF}_{x,y,z}$. For X and Y directions, these errors are the same with the maximum value of $\Delta x_{\text{TomoPy}} = 3.6$ mm. Applying interpolation, we diminished transaxial pixel size to $\Delta x_{\text{STIR}} = 1.8$ mm (by setting the zoom parameter in STIR to 2) and $\Delta x_{\text{R PET}} < 0.9$ mm.

The longitudinal errors for TomoPy (200 cuts along Z) and STIR (64 rings) were $\Delta z_{\text{TomoPy}} = 2.5$ mm and $\Delta z_{\text{STIR}} = 3.9$ mm, respectively. Such parameters are sufficient for the PSF estimation for different σ_z (see left bottom of Fig. 3). The resulting voxel size ($\Delta x \times \Delta y \times \Delta z$) for STIR and TomoPy was $1.8 \text{ mm} \times 1.8 \text{ mm} \times 3.9 \text{ mm}$ and $3.6 \text{ mm} \times 3.6 \text{ mm} \times 2.5 \text{ mm}$, respectively.

For the transverse direction, the values of $\text{PSF}_{x,y}$ that correspond to various frameworks, tend to differ significantly if the source is distant from the centre of the scanner (Fig. 3, left top). In comparison, $\text{PSF}_{x,y}$ are inside the span of Δx for the position closest to the centre ($x_{\text{src}} = 10$ mm, $y_{\text{src}} = 0$ mm, $z_{\text{src}} = 0$ mm), resulting in effective spatial resolution of $\sim 5 \div 7$ mm. We did not observe any influence of σ_z , reflecting the axial smearing of hit position, on the transverse resolution: in all cases, $\text{PSF}_{x,y}$ were increasing similarly if moving phantom far from the centre.

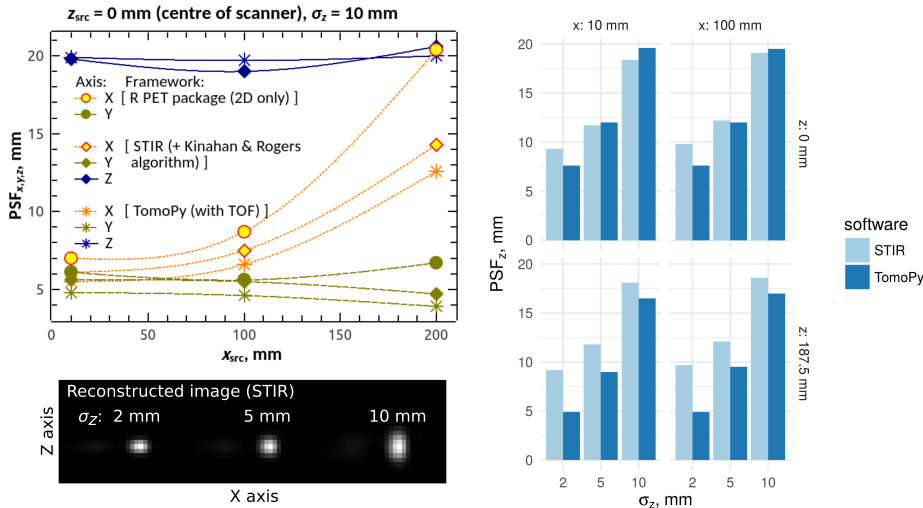


Fig. 3. Left top: preliminary results for PSF_{x,y,z}(x_{src}) dependencies, estimated in different software frameworks, for z_{src} = 0 mm and σ_z = 10 mm. Left bottom: XZ-projections of reconstructed images in STIR, for different smearing parameter σ_z. Right: preliminary estimations of longitudinal PSF_z for various positions of the source and smearing parameters σ_z (notation “src” omitted for x and z).

Estimated longitudinal resolution PSF_z differs for various softwares used. TOF correction, implemented in TomoPy, reduces PSF_z systematically for the case of z_{src} = 187.5 mm, compared to z_{src} = 0 mm (darker bars in Fig. 3, right). The explanation of this is the activity of the source and irradiation time: if the source is closer to the edge, much smaller obliqueness is allowed for LORs (see Fig. 2), so that both photons would interact with the scanner. Therefore, longer exposure is required for z_{src} = 187.5 mm to achieve ~ 150 000 events that match selection criteria. Together with TOF correction it would definitely improve resolution. Conversely, Kinahan and Rogers algorithm, implemented in STIR, artificially adds oblique LORs by expanding scanner along Z, which eventually diminishes the role of the exposure [27].

To sum up, implementation of TOF technique proved to be promising for J-PET scanners. Minimal PSF, estimated in TomoPy for the smallest smearing σ_z = 2 mm is below 5 mm in both longitudinal and transverse directions, which is comparable to modern, commercially available TOF-PET/CT systems [30, 31]. However, these results are yet to be confirmed by a more accurate approach, since full 3D FBP algorithm has not been employed. For the correct estimation, all NEMA requirements are to be fulfilled.

On the contrary, STIR 3D FBP algorithms return consistent and reproducible results. Hence, preliminary PSF values, obtained in this framework, should be considered reliable, with projected longitudinal resolution for J-PET scanner of $\sim 9 \div 10$ mm and $\sim 18 \div 19$ mm for the smallest and the largest σ_z , respectively, with no TOF correction applied. Summarized results are listed in Table I. As one can see, there is little influence of axial position of the source on the longitudinal resolution, as well as axial smearing on the transverse resolution. This might be considered as a benefit of STIR application in J-PET for 3D image reconstruction.

TABLE I

Estimated (preliminary) PSF values for 3D FBP reconstruction of 1 mm point source in STIR framework, located at $(x_{\text{src}}, y_{\text{src}}, z_{\text{src}})$ in J-PET scanner. Transaxial position is defined by x_{src} (y_{src} is equal to zero), “centre” and “edge” denote axial coordinate ($z_{\text{src}} = 0$ mm and $z_{\text{src}} = 187.5$ mm, respectively). Voxel size $\Delta x \times \Delta y \times \Delta z = 1.8$ mm \times 1.8 mm \times 3.9 mm.

Along axis:		PSF [mm]					
		X		Y		Z	
σ_z [mm]	x_{src} [mm]	centre	edge	centre	edge	centre	edge
2.0	10	5.8	5.8	5.8	5.4	9.3	9.2
	100	7.7	7.6	5.4	5.4	9.8	9.7
	200	13.8	13.8	4.5	4.5	9.7	9.7
5.0	10	5.8	5.8	5.8	5.4	11.7	11.8
	100	7.1	7.1	5.4	5.4	12.2	12.1
	200	13.4	13.4	4.5	4.5	13.6	12.6
10.0	10	5.8	5.8	5.8	5.4	18.4	18.1
	100	7.6	7.6	5.4	5.4	19.6	16.5
	200	13.4	13.8	4.5	4.5	19.4	20.4

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