

Viscosity and Density Measurements on Compressed Liquid n-Tetradecane ^{a)}

Tânia V.M. Santos,¹ Marta F.V. Pereira,¹ Helena M.N.T. Avelino,^{1,2} Fernando J. P.
Caetano,^{1,3} João M. N. A. Fareleira¹

1) Centro de Química Estrutural, Instituto Superior Técnico, Universidade de Lisboa, Portugal

2) Instituto Superior de Engenharia de Lisboa, Portugal

3) Universidade Aberta, Lisboa, Portugal

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AIMS:

- **Long-term:** To develop a reference correlation for the viscosity of normal tetradecane ($n\text{-C}_{14}$) *at* high pressures and in a wide range of temperatures.
- **Short-term (present work):**
 1. To measure the **viscosity** of $n\text{-C}_{14}$ in wide temperature and pressure ranges _ special attention to (T,p) ranges where viscosity data are scarce (**or non-existent, v.g.: $T < 293$ K**).
 2. To **correlate the present viscosity** data with density.

MOTIVATION

1. General economic importance of alkanes;
2. Increasing importance of paraffins (and their mixtures) for energy storage systems as PHASE CHANGE MATERIALS;
3. Lack of rigorous viscosity data for n-tetradecane, at **low temperatures** and moderately high pressures (**$p < 10$ MPa**). Ranges that are relevant for the development of some sustainable processes.

SUMMARY OF THE PRESENT WORK

- New measurements of the **viscosity** of n-tetradecane (n- C_{14}) at moderately high pressures, using the vibrating wire technique.
- New measurements of the **density** of n-tetradecane using a model **HP Anton Paar U-tube** densimeter.
- Development of a **correlation of viscosity with density**, using a modified hard-spheres model.

Density

Experimental results obtained using an Anton Paar DMA HP model vibrating U-Tube instrument with model DMA 5000 as reading unit.

Measurements were performed along nine isotherms in the range $(283 \leq T \leq 373)$ K and pressures from $(0.1 \text{ to } 70)$ MPa

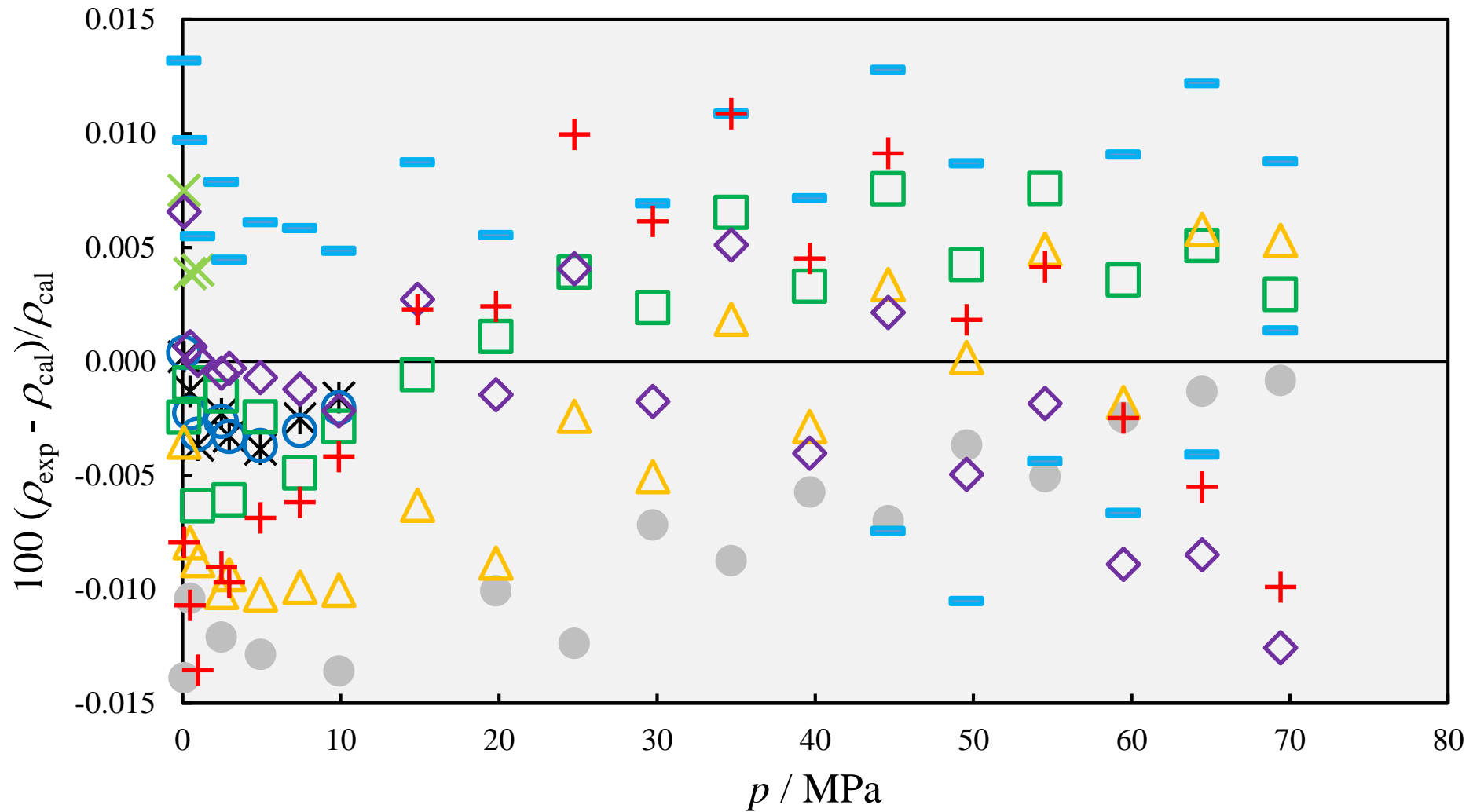
The experimental data were correlated by a modified Tait equation, proposed by

J.H. Dymond, R. Malhotra, The Tait equation: 100 years on, Int. J. Thermophys. 9 (1988) 941–951.

$$\rho = \rho_0 \left\{ 1 - C \ln \left[\frac{D + p}{D + p_0} \right] \right\}^{-1}$$

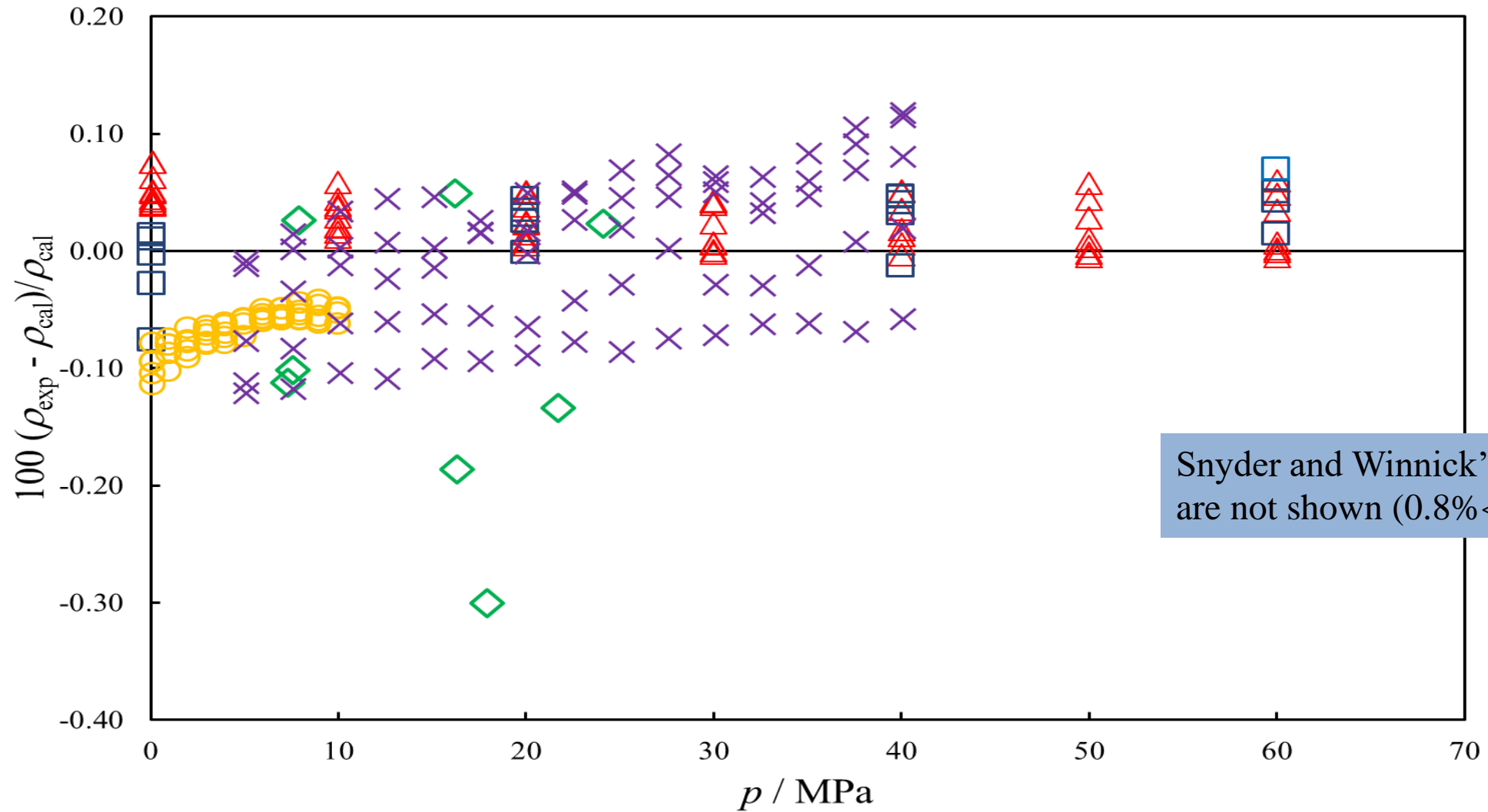
$$\text{with } \rho_0 = \sum_{i=0}^2 b_i T^i$$

Deviations of the density of n-tetradecane (this work) from the correlation



× 283 K; * 288 K; ○ 293 K; □ 298 K; ● 308 K; △ 318 K; — 338 K; ◇ 358 K; + 373 K

Deviations of literature density data (**after 1978**) from the correlation of our results



× Gouel; △ Valência et al.; ○ Kariznovi et al.; ◇ Gawronska et al.; □ Khasanshin et al.

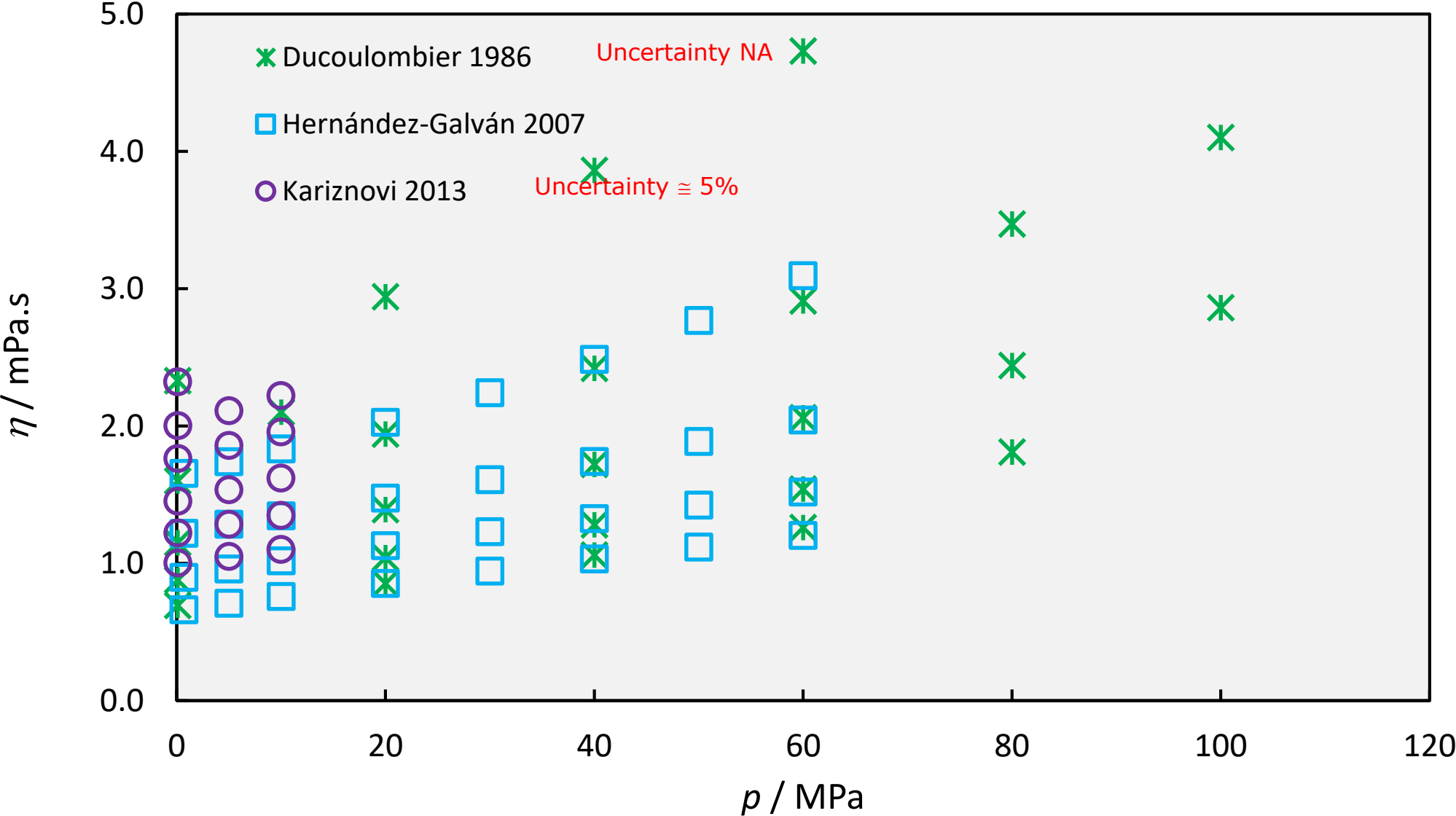
VISCOSITY

Literature viscosity data for liquid n-C₁₄

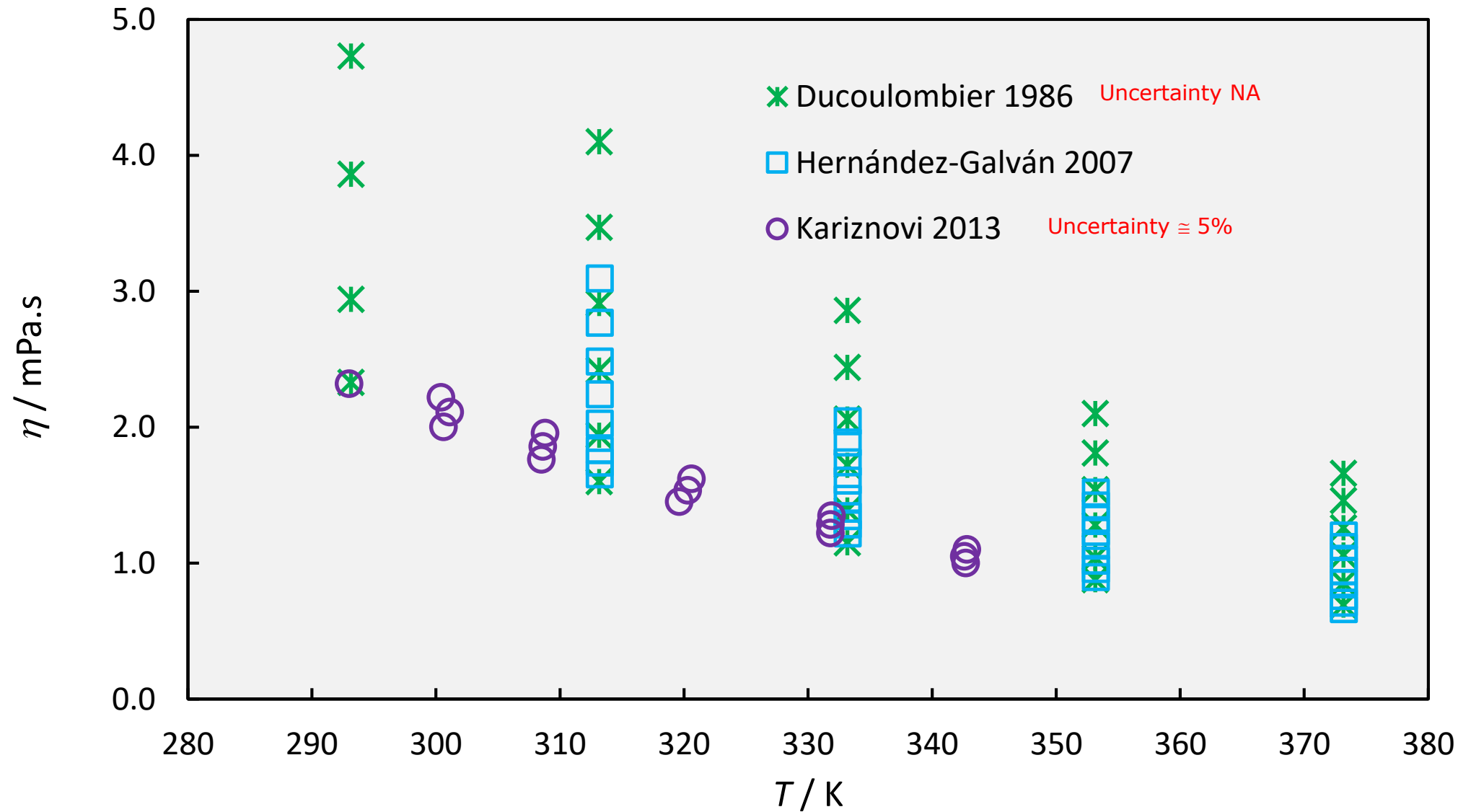
Year	First author	Temperature range/K	Pressure range/MPa	NP	Method	Purity /%	Nominal uncertainty
1986	Ducoulombier	293-373	0.1 - 100	24	falling body	NA	NA
1989	Knapstad	293-423	0.1	10	Oscillating viscometer	99	(0.33-0.56) %
2001	Franjo	298.15	0.1	1	capillary	99	$\pm 5 \times 10^{-4} \text{mm}\cdot\text{s}^{-1}$
2003	Nayak	298-308	0.1	3	capillary	99	$\pm 0.001 \text{ mPa}\cdot\text{s}$
2007	Hernández-Galván	313-393	0.69 - 60	40	rolling-ball ^{a)}	99	$\pm 2.0 \%$
2012	Mahajan	298.15	0.1	1	capillary	99	$\pm 0.003 \text{ mPa}\cdot\text{s}^{\text{c}}$
2013	Kariznovi	300-343	0.1-10	15	Cambridge Viscometer ^{b)}	99	5%

a) Kinematic Viscosity; b) Cambridge Viscometer Model SPC ; c) repeatability; NA – not available

Literature viscosity data (η vs. p) for compressed liquid n-C₁₄ (up to 100 MPa)

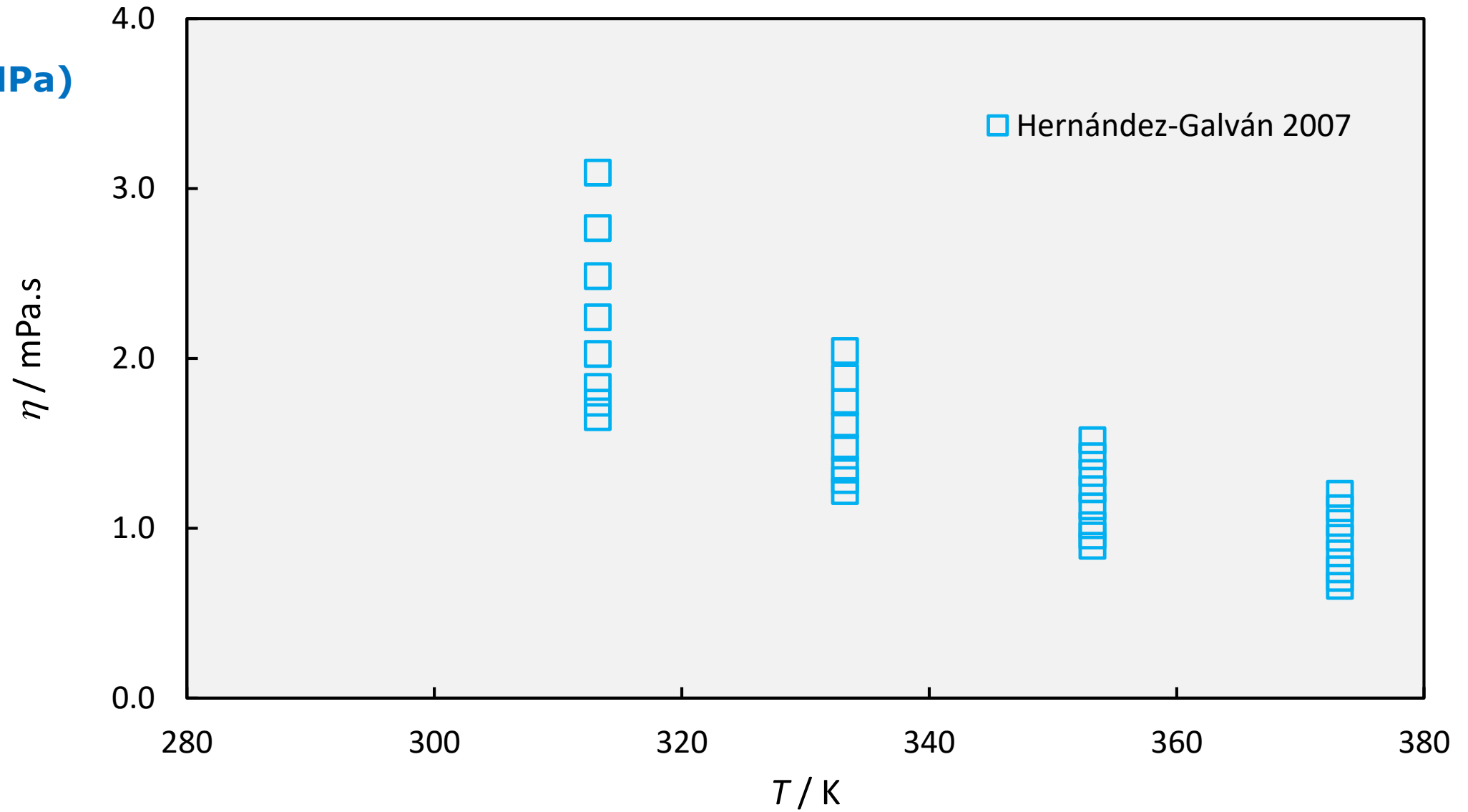


Literature viscosity (η vs. T) data for compressed liquid n-C₁₄



Literature viscosity data with specified uncertainty less than 5%

($p > 0.1$ MPa)

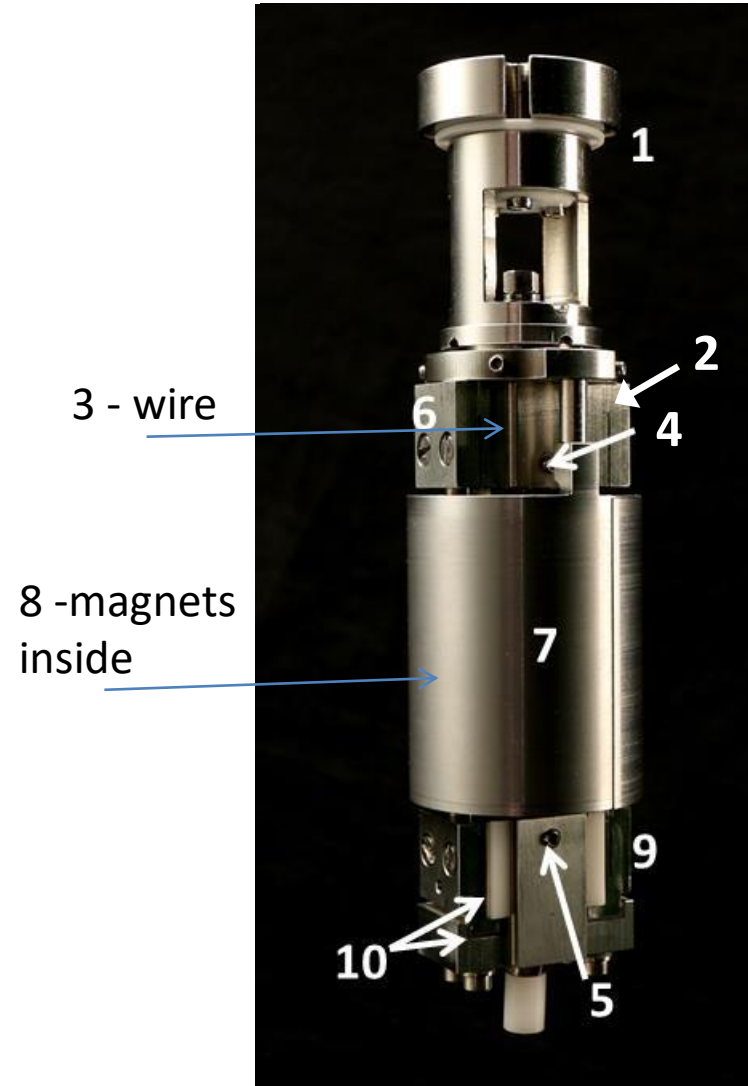


Viscosity:

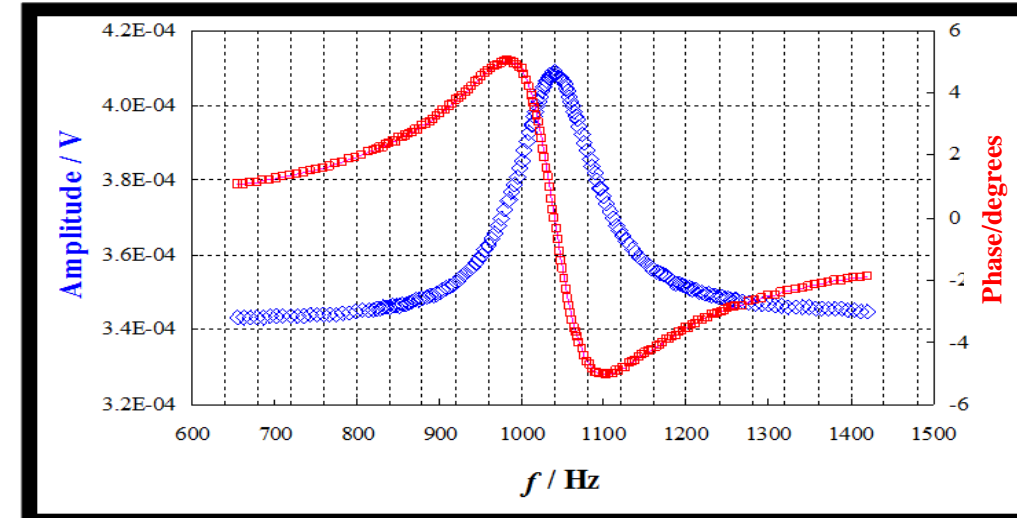
New **measurements of the viscosity of n-tetradecane** along eight isotherms in the range $(283 \leq T \leq 358)$ K and pressures up to 70 MPa, have been performed using the vibrating wire technique in the forced mode of operation.

Vibrating wire sensor

- 1 - top washers;
- 2 - upper claw chucks;
- 3 - vibrating wire;
- 4 - rod spacers;
- 5 - bottom claw chucks;
- 6 - upper rod clamping;
- 7 - magnetic circuit;
- 8 - magnets;
- 9 - lower rod clamping,
- 10 - bottom washers



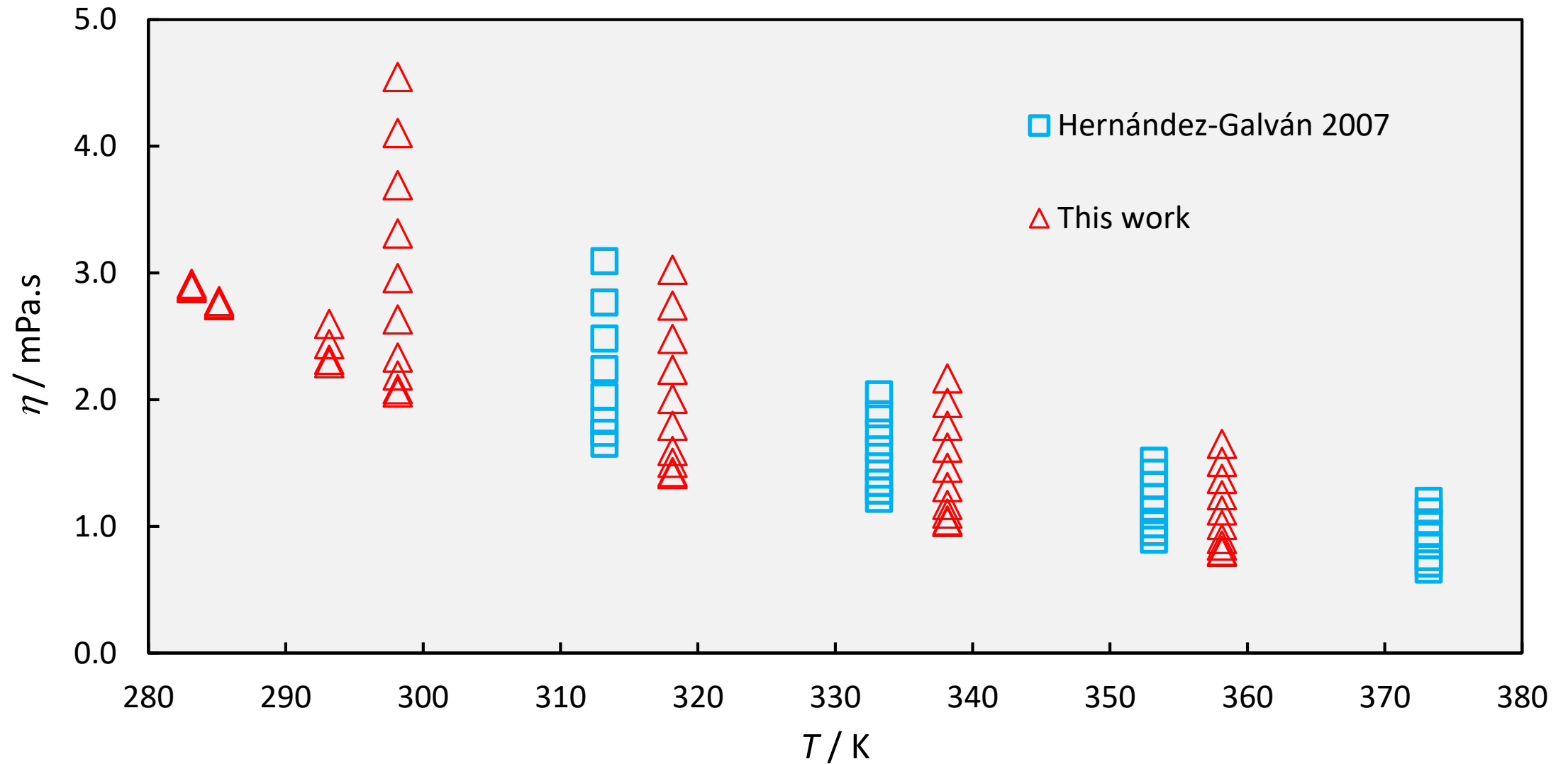
Raw data



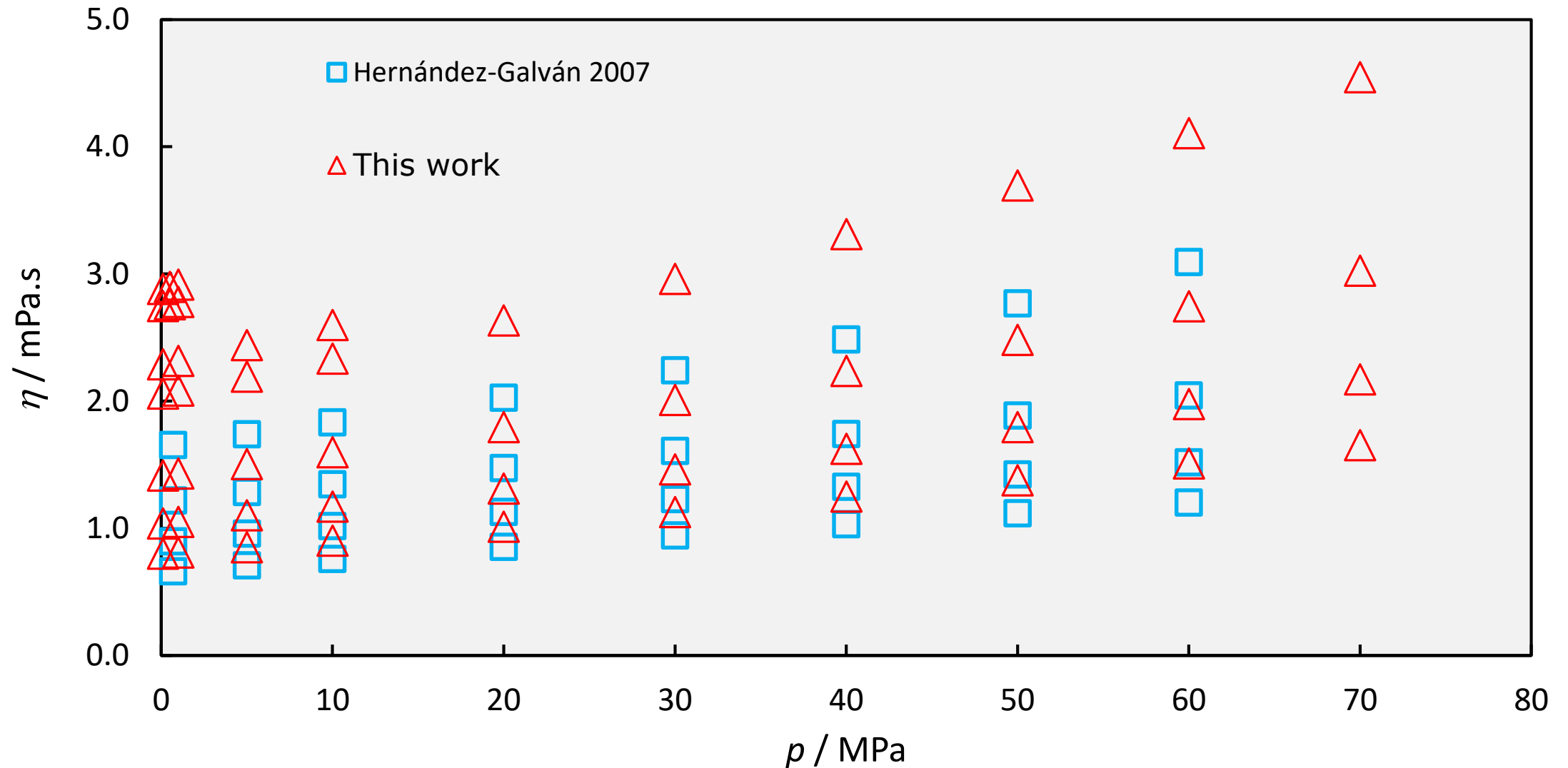
Hydrodynamic Model

Viscosity

Updated view: Viscosity (η vs. T) for n-C₁₄ ($p \geq 0.1$ MPa) with uncertainty less than 5%



Updated view: Viscosity (η vs. p) for n-C₁₄ ($p \geq 0.1$ MPa) with uncertainty less than 5%



Correlation scheme: A modified hard-spheres model of transport properties of fluids for **VISCOSITY**

Heuristic development¹ of the kinetic theory for dense hard-sphere fluids, applied to the van der Waals model of a liquid, proposed by Dymond.²

$$\eta^* = 6.035 \times 10^8 \left(\frac{1}{MRT} \right)^{1/2} (V_m)^{2/3} \eta$$

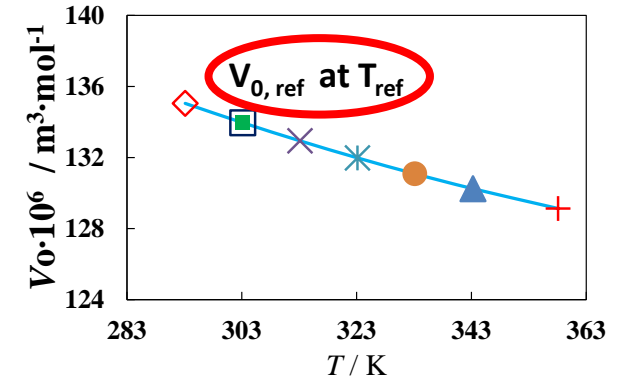
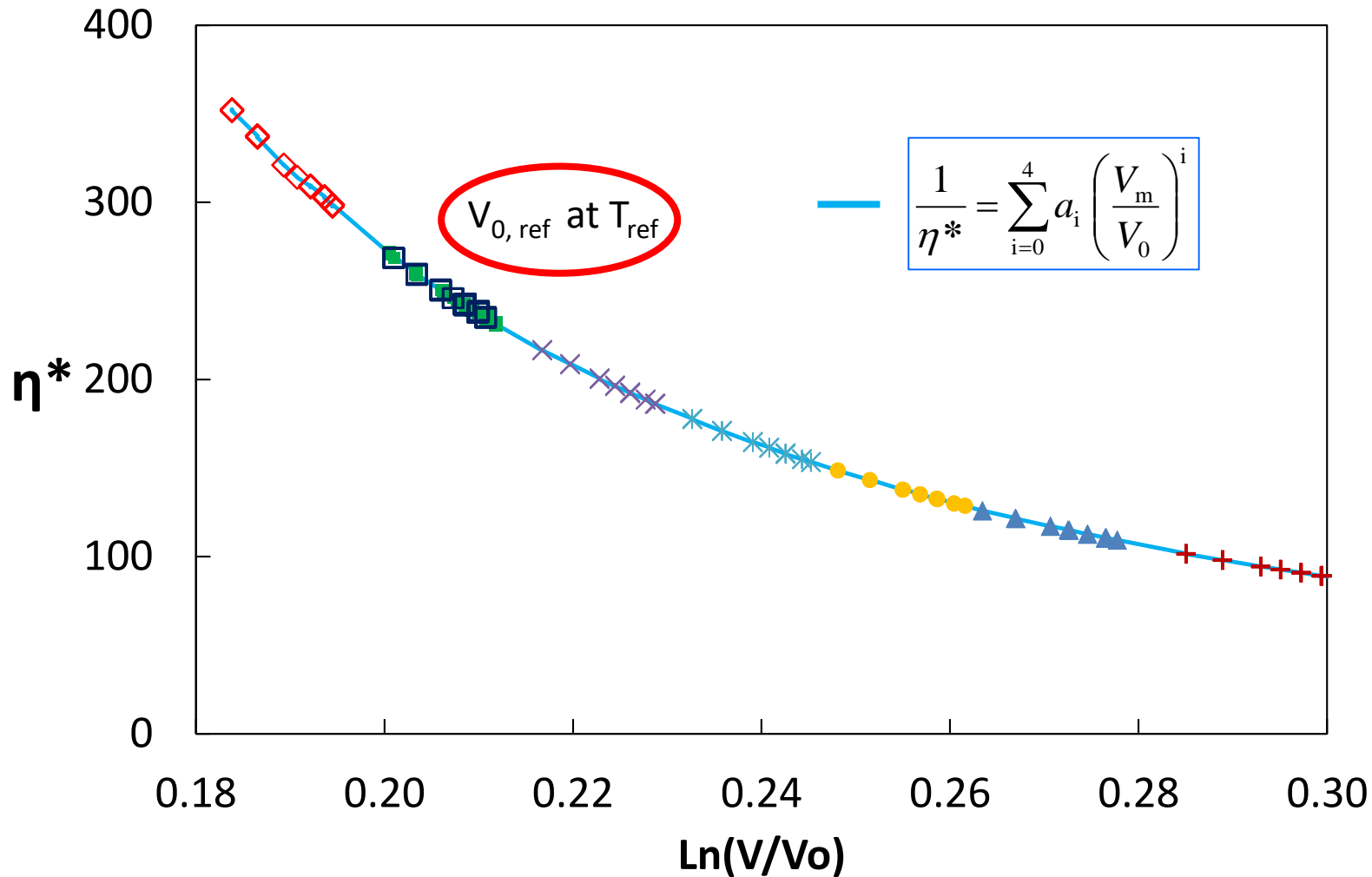
$$\eta^* = f \left(\frac{V_m}{V_0} \right) \quad V_0 = f(T)$$

1. S.F.Y. Li, R.D. Trengove, W.A. Wakeham, M. Zalaf, *Int. J. Thermophys.* 1986, **7**, 273-284
2. Dymond, J.H., *Chem.Soc. Rev.* 1985, **14**, 317-356

Viscosity Correlation

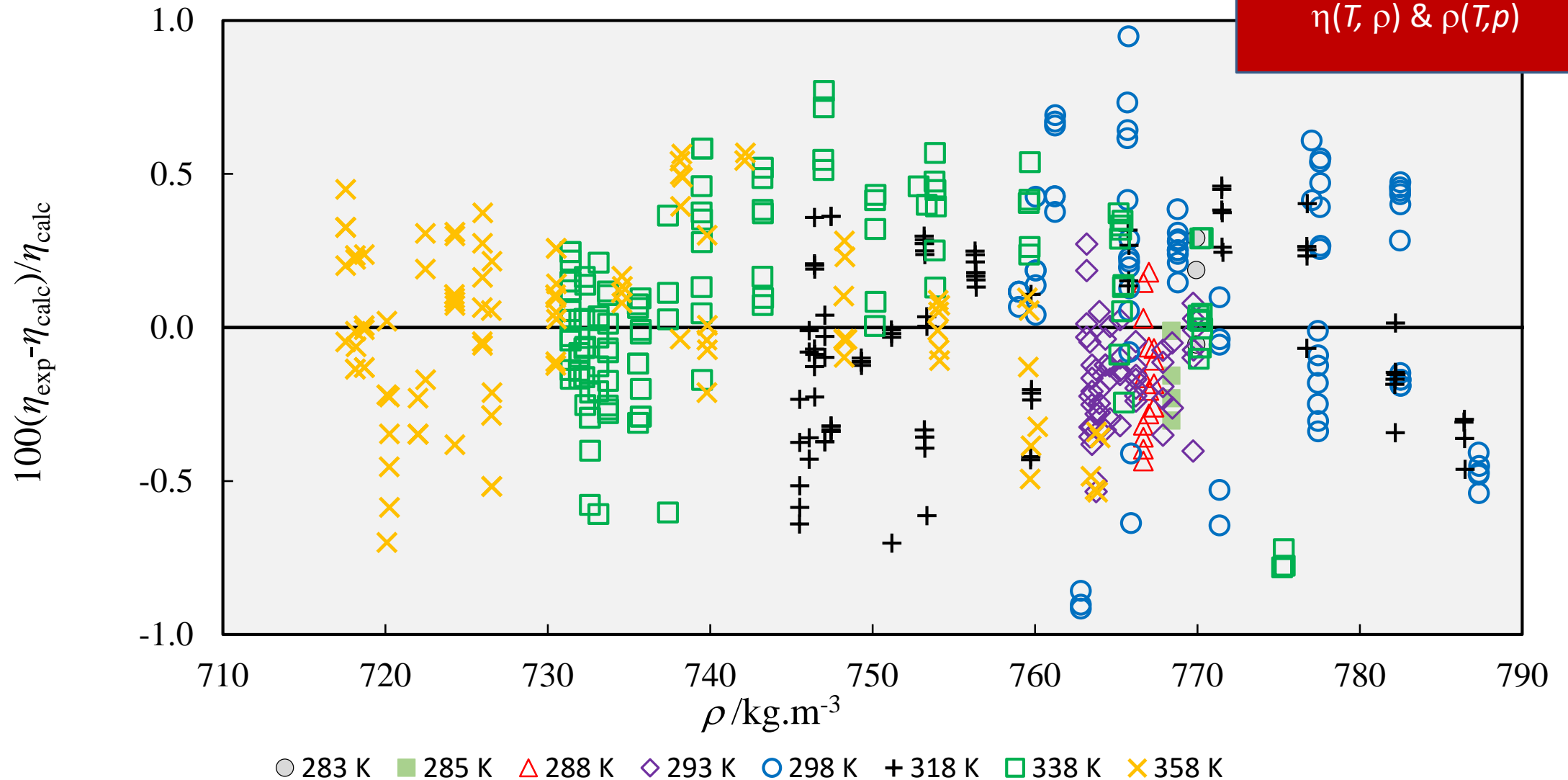
Smooth Hard-Spheres

$$V_0(T) \times 10^6 \text{ (m}^3\text{mol}^{-1}) = V_{0,ref} + l(T - T_{ref}) + m(T - T_{ref})^2$$

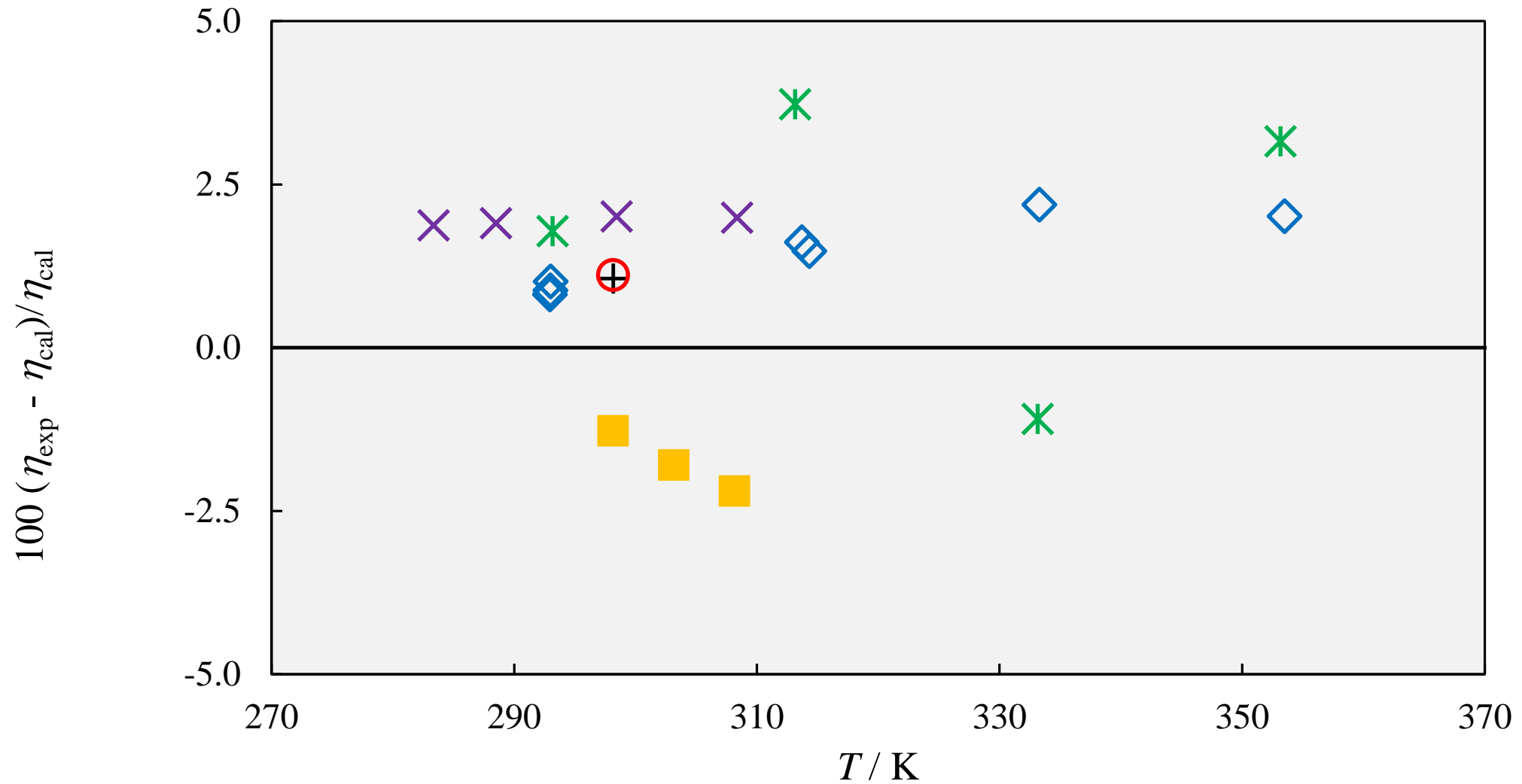


- ◇ T_1
- $T_{Ref}=T_0$
- × T_2
- * T_3
- T_4
- ▲ T_5
- + T_6

Deviations (η vs. ρ) for n-C₁₄ ($\rho \geq 0.1$ MPa) obtained in the present work with the vibrating-wire technique, from the present correlation scheme

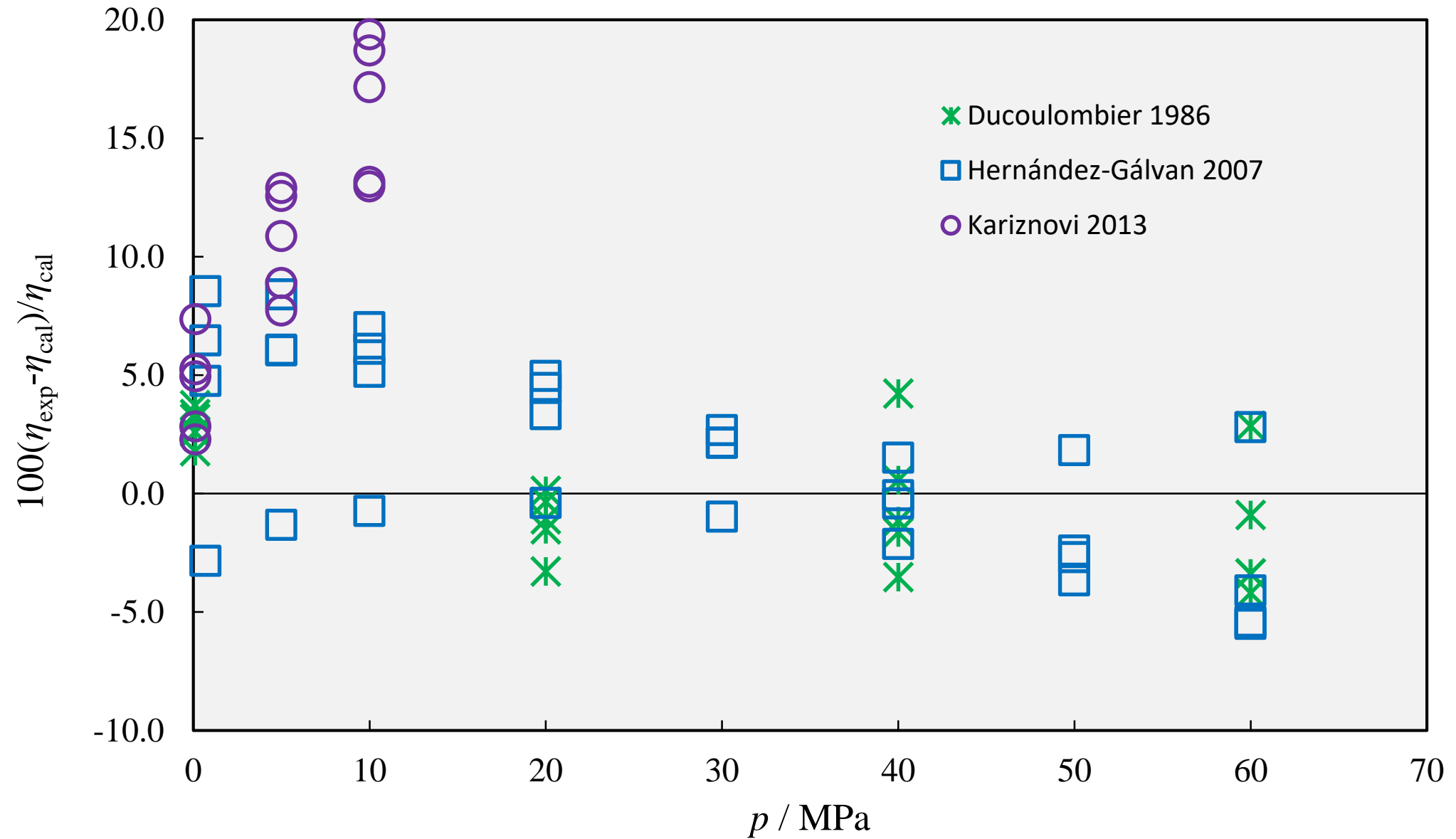


Deviations of n-C₁₄ viscosity **literature data** at 0.1 MPa , from our correlation



✱ Ducoolombier 1986; ◆ Knapstad 2002; ■ Nayak 2003; + Franjo 2001; ○ Mahanja 2012; ✕ This work (capillary)

Deviation of the viscosity **literature data** for n-C₁₄ from our correlation as a function of pressure



Conclusions:

- This work provides **new viscosity measurements** in ranges where literature data were scarce or totally absent (**No literature data below 293 K even at 0.1 MPa!**).
- New density measurements were also performed and used to develop a provisional **viscosity correlation**, which may be used to obtain $\eta = \eta(T, p)$ with low uncertainty in wide ranges of T and p .
- However, **large inconsistency** between literature results is observed, exceeding the nominal uncertainty of most of the available measurements, which hinders the possibility to develop **reference correlations** for the viscosity of n-tetradecane.
- A reference correlation for the **viscosity** of **n-C₁₄**, needs **new independent measurements**, using several experimental methods, covering the low temperature and intermediate pressure ranges (up to 10 MPa).

Acknowledgments:

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