

## Accepted Manuscript

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Author: Frédéric M. Hamelin Frank M. Hilker T. Anthony Sun Michael J. Jeger M. Reza Hajimorad Linda J.S. Allen Holly R. Prendeville



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## Highlights

- \* We use adaptive dynamics theory to study the evolution of plant-virus symbioses
- \* Ecological bistability in a discrete-time model with frequency-dependent transmission
- \* Darwinian extinction can occur under optimizing selection
- \* Evolutionary branching of parasitic and mutualistic viral symbioses
- \* Mutualism can outcompete parasitism in the long-run

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The evolution of parasitic and mutualistic plant-virus  
symbioses through transmission-virulence trade-offs

Frédéric M. Hamelin<sup>\*†</sup>, Frank M. Hilker<sup>‡</sup>, T. Anthony Sun<sup>‡</sup>, Michael J. Jeger<sup>§</sup>,  
M. Reza Hajimorad<sup>¶</sup>, Linda J.S. Allen<sup>||</sup>, Holly R. Prendeville<sup>\*\*</sup>

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Running title: The evolution of mutualistic viral symbioses

**Keywords:** horizontal; vertical; seed; vector; adaptive dynamics; bi-stability

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<sup>\*</sup>IGEPP, Agrocampus Ouest, INRA, Université de Rennes 1, Université Bretagne-Loire, 35000 Rennes, France

<sup>†</sup>Corresponding author (fhamelin@agrocampus-ouest.fr)

<sup>‡</sup>Institute of Environmental Systems Research, School of Mathematics/Computer Science, Osnabrück University, 49076 Osnabrück, Germany

<sup>§</sup>Division of Ecology and Evolution, Centre for Environmental Policy, Imperial College London, SL5 7PY, UK

<sup>¶</sup>Department of Entomology and Plant Pathology, University of Tennessee, Knoxville, TN 37996-4560, USA

<sup>||</sup>Department of Mathematics and Statistics, Texas Tech University, Lubbock, TX 79409-1042, USA

<sup>\*\*</sup>USDA Forest Service, Pacific Northwest Research Station, Corvallis, OR 97331, USA

## 8 **Abstract**

Virus-plant interactions range from parasitism to mutualism. Viruses have been shown to increase fecundity of infected plants in comparison with uninfected plants under certain environmental conditions. Increased fecundity of infected plants may benefit both the plant and the virus as seed transmission is one of the main virus transmission pathways, in addition to vector transmission. Trade-offs between vertical (seed) and horizontal (vector) transmission pathways may involve virulence, defined here as decreased fecundity in infected plants. To better understand plant-virus symbiosis evolution, we explore the ecological and evolutionary interplay of virus transmission modes when infection can lead to an increase in plant fecundity. We consider two possible trade-offs: vertical seed transmission vs infected plant fecundity, and horizontal vector transmission vs infected plant fecundity (virulence). Through mathematical models and numerical simulations, we show 1) that a trade-off between virulence and vertical transmission can lead to virus extinction during the course of evolution, 2) that evolutionary branching can occur with subsequent coexistence of mutualistic and parasitic virus strains, and 3) that mutualism can out-compete parasitism in the long-run. In passing, we show that ecological bi-stability is possible in a very simple discrete-time epidemic model. Possible extensions of this study include the evolution of conditional (environment-dependent) mutualism in plant viruses.

# 1 Introduction

26 Plant viruses exhibit the full symbiont spectrum and thus can have a range of effects on plants  
(Roossinck, 2011; Bao and Roossinck, 2013; Fraile and García-Arenal, 2016). Plant viruses  
28 can confer herbivore resistance (Gibbs, 1980), pathogen resistance (Shapiro et al., 2012), and  
drought tolerance (Xu et al., 2008; Davis et al., 2015). Differential effects of viruses on plants  
30 occur due to variation in environment and genetics of plants and viruses (Johansen et al., 1994,  
1996; Domier et al., 2007, 2011; van Mølken and Stuefer, 2011; Davis et al., 2015; Hily et al.,  
32 2016). Some viruses have neutral or positive effects on plants by not affecting or increasing  
components of fitness, respectively (van Mølken and Stuefer, 2011; Davis et al., 2015; Hily et al.,  
34 2016). These recent works contradict decades of extensive research on plant viruses elucidating  
the negative effects of viruses in agronomic systems. Results from these previous works have led  
36 to the convention of virologists referring to viruses as pathogens. In light of recent findings, it is  
clear that plant viruses do not always lead to disease and therefore by definition are not always  
38 pathogens (Pagán et al., 2014; Fraile and García-Arenal, 2016).

Virus-plant interactions are obligate, symbiotic interactions that exist along a spectrum from  
40 parasitism to commensalism to mutualism. Parasitic associations occur when one species exists  
at a cost to the other, which follows the convention of virus-plant interactions. Commensalism  
42 occurs when one species profits from the interaction, but has no effect on the other species.  
The plant benefits the virus by promoting virus transmission. In the common bean (*Phaseolus*  
44 *vulgaris*) seed number and weight were not affected by *Phaseolus vulgaris* endornavirus 1 and 2  
(R. A. Valverde pers. comm.). In a mutualistic relationship net effects are positive with enhanced  
46 survival and/or reproduction for both the plant and virus, thus as with all mutualisms the benefits  
outweigh the costs of the relationship. *Cucumber mosaic virus* (CMV) benefits *Arabidopsis*  
48 *thaliana* by increasing seed production in comparison to plants without virus though this effect

depends upon environmental conditions (Hily et al., 2016). CMV alters volatiles in *Solanum*  
50 *lycopersicum* making it more attractive to pollinators (Groen et al., 2016), which may enhance  
virus transmission by seed.

52 Plant viruses have evolved various modes of transmission resulting in genetic variation within  
and among virus species to interact with the genetic variation within and among plant species  
54 (Johansen et al., 1994, 1996; Domier et al., 2007, 2011). Some viruses are integrated into the  
plant genome and thus are persistent (Harper et al., 2002). Certain virus species can circulate  
56 within an insect vector or propagate within an insect vector resulting in persistent virus trans-  
mission to plants, while other vector-transmitted viruses are transferred in a semi-persistent to  
58 non-persistent manner (intermediate to short timeframe). Most viruses depend upon more than  
one mode of natural transmission by pollen, seed, and vector (reviewed in Hamelin et al. 2016)  
60 though having a suite of transmission modes can lead to trade-offs among modes of transmission.

Trade-offs between seed and vector transmission may occur when vector transmission is  
62 positively correlated with virulence, defined here as reduced fecundity in infected plants, as  
opposed to increased mortality in infected plants (Doumayrou et al., 2013). Serial passage of the  
64 *Barley stripe mosaic virus* in *Hordeum vulgare* through vectors resulted in an increase in vector  
transmission rate and virulence (reduced seed production), whereas serial passage through seed  
66 led to an increase in seed transmission and a decrease in virulence (increased seed production)  
(Stewart et al., 2005). Likewise, serial passage of *Cucumber mosaic virus* (CMV) by seed of  
68 *Arabidopsis thaliana* led to an increase in seed transmission rate, decline in CMV virulence  
(increased total seed weight) and reduction in virus accumulation (Pagán et al., 2014). A trade-  
70 off between virulence and vector transmission in a parasitic virus can lead to the emergence  
and coexistence of virulent vector-borne strains and less virulent, non-vector borne strains of  
72 virus (Hamelin et al., 2016). Furthermore, trade-offs between modes of transmission can result  
in the coexistence of different modes of virus transmission within a plant population that is

74 evolutionarily stable (Hamelin et al., 2016).

To better understand plant-virus symbiosis evolution, we explore the ecological and evolu-  
 76 tionary interplay of virus transmission modes between seeds and vectors when infection can  
 lead to an increase in plant fecundity, which was not addressed by (Hamelin et al., 2016). We  
 78 consider two possible trade-offs: vertical seed transmission vs infected plant fecundity, and hor-  
 izontal vector transmission vs infected plant fecundity (virulence). We use mathematical models  
 80 and numerical simulations to address three questions: 1) Can a trade-off between virulence and  
 vertical transmission lead to virus extinction in evolutionary time? 2) As a virus evolves, can evo-  
 82 lutionary branching occur with subsequent coexistence of mutualistic and parasitic virus strains?  
 3) Can mutualism outcompete parastism in the long-run?

## 84 **2 Ecological model**

### **2.1 Discrete-time model**

The model includes two methods for viral transmission to a host plant: (1) infected vectors and  
 (2) infected seeds. A discrete-time model is formulated since each of the transmission events  
 occur at different time periods during the year. Therefore, the year is divided into two periods,  
 corresponding to vector and seed transmission, denoted as  $V$  and  $S$ , respectively:

$$t \xrightarrow[V]{} t' \xrightarrow[S]{} t + 1.$$

86 During the time interval  $[t, t']$ , the newly developed plants are colonized by vectors. Virus trans-  
 mission from the vector to the host plant occurs during this first time interval. During the second  
 88 time interval  $[t', t + 1]$ , seeds drop to the ground and those that survive, either uninfected or in-  
 fected seeds, germinate and produce new uninfected or infected plants, respectively. We assume

90 there is no seed bank. At the beginning of the next year,  $t + 1$ , seeds have germinated and pro-  
duced new plants. The annual cycle repeats.

92 To keep the model simple, there are no explicit vector dynamics. The acquisition of the virus  
by non-viruliferous vectors, and inoculation of the host plant by viruliferous vectors are modeled  
94 implicitly. Only the dynamics of the host plant are modeled. Two variables account for the  
plant dynamics during each of these two stages. The two variables are  $H$  and  $I$ , the density of  
96 uninfected and infected plants, respectively. The total density of uninfected and infected plants  
is denoted as  $T = H + I$ . The plant dynamics are observed each year at time  $t$ ,  $t = 0, 1, 2, \dots$  after  
98 seed transmission and before vector transmission.

During the vector stage  $V$ , the Poisson distribution is used to model virus transmission be-  
100 tween the vector and the host plant. Let  $\Lambda_V$  denote the parameter in the Poisson distribution: it  
is the average number of viruliferous vector visits per plant per year that result in subsequent in-  
102 oculation of an uninfected plant. Horizontal transmission parameter  $\beta$  relates this number to the  
infection prevalence at the beginning of the vector stage. Virus transmission through vectors is  
104 assumed to depend on the frequency of infected plants,  $I/T$ , rather than on their density  $I$  (Ross,  
1911; Hamelin et al., 2016). Then

$$\Lambda_V = \beta \frac{I(t)}{T(t)}$$

106 Hence, the probability of no successful virus transmission from vectors to a given host plant is  
 $\exp(-\Lambda_V)$  and the probability of successful transmission is  $1 - \exp(-\Lambda_V)$ . Therefore, at time  $t'$ ,  
108 the model takes the form:

$$\begin{aligned} H(t') &= H(t)e^{-\Lambda_V} = H(t) \exp\left(-\beta \frac{I(t)}{T(t)}\right), \\ I(t') &= I(t) + H(t)[1 - e^{-\Lambda_V}] = I(t) + H(t) \left[1 - \exp\left(-\beta \frac{I(t)}{T(t)}\right)\right]. \end{aligned} \quad (1)$$



Notice that at low infected plant density ( $I(t) \ll H(t) \approx T(t)$ ),

$$I(t') \approx I(t) + H(t)\beta \frac{I(t)}{T(t)} \approx I(t)(1 + \beta), \quad (2)$$

110 i.e.,  $\beta$  is like a multiplication factor of infected plants associated with vector transmission.

For the second transmission stage  $S$ , we assume competition and overcrowding between  
 112 neighboring plants reduces the number of seeds per plant (Watkinson and Harper, 1978; Pacala  
 and Silander Jr, 1985). Density-dependent effects apply equally to uninfected and infected plants.  
 114 Let  $b_H$  and  $b_I$  denote the effective number of seeds produced per uninfected or infected plant,  
 respectively, at low plant density. We assume that the virus infects both the maternal plant and  
 116 the seeds. Thus, only infected plants produce infected seeds. At low plant density, more than one  
 effective seed is produced per uninfected plant,

$$b_H > 1. \quad (3)$$

118 The seeds that survive germinate into either uninfected or infected plants. If vertical transmission  
 is full, all seeds produced by an infected plant are infected but if not, only a proportion  $p$  produced  
 120 is infected and the remaining proportion  $q = 1 - p$  is not infected.

We apply a well-known form for plant density-dependence due to de Wit (1960) (also known  
 122 as Beverton-Holt density-dependence in animal populations). The model in the second stage is

$$\begin{aligned} H(t+1) &= \frac{b_H H(t') + q b_I I(t')}{1 + \lambda T(t')}, \\ I(t+1) &= \frac{p b_I I(t')}{1 + \lambda T(t')}, \end{aligned} \quad (4)$$

where  $T(t) = H(t) + I(t)$  and  $\lambda$  describes density-dependent competition between plants.

124 The full vector-seed transmission model consists of the preceding models for the two stages

Table 1: Model parameters and variables.

Notation	Definition	Unit
$t$	time in years, $t = 0, 1, 2, \dots$	time
$T(t)$	total plant density at time $t$	per area
$H(t)$	uninfected plant density at time $t$	per area
$I(t)$	infected plant density at time $t$	per area
$b_H$	effective number of seeds per uninfected plant	none
$b_I$	effective number of seeds per infected plant	none
$p = 1 - q$	infected seed transmission probability	none
$\beta$	vector transmission parameter	none
$\lambda$	plant competition parameter	area

$V$  and  $S$ , equations (1)–(4). Combining these two pairs of difference equations, the model can be  
 126 expressed as a first-order difference equation for uninfected and infected plants, i.e.,

$$\begin{aligned}
 H(t+1) &= \frac{b_H H(t) P(t) + q b_I (I(t) + H(t) (1 - P(t)))}{1 + \lambda T(t)}, \\
 I(t+1) &= \frac{p b_I (I(t) + H(t) (1 - P(t)))}{1 + \lambda T(t)},
 \end{aligned}
 \tag{5}$$

where

$$P(t) = \exp\left(-\beta \frac{I(t)}{T(t)}\right)$$

128 is the probability an uninfected plant escapes infection during year  $t$ . Table 1 lists all model  
 variables and parameters with their definition.

## 130 2.2 Basic reproductive number

At virus-free equilibrium (VFE), the density of infected plants is zero and the density of unin-  
 132 fected plants is

$$\bar{H} = \frac{b_H - 1}{\lambda}.$$

The basic reproductive number for model (5) is computed from linearization of the difference  
 134 equation for the infected host  $I$  about the VFE:

$$\mathcal{R}_0 = \frac{pb_I}{b_H}(1 + \beta). \quad (6)$$

If the reproductive number is greater than one, then our annual plant model shows that these two  
 136 transmission mechanisms may be able to maintain the virus within the host population. If viral  
 transmission is purely vertical, limited only to seed transmission ( $\beta = 0$ ), then  $\mathcal{R}_0 > 1$  if and  
 138 only if  $pb_I > b_H$ , which requires  $b_I > b_H$ . That is, this simple model shows that purely vertical  
 transmission of a virus through the seed cannot maintain the virus in the host population unless  
 140 infected plants have greater fecundity than uninfected plants (Fine, 1975; Hamelin et al., 2016).  
 Note that the ratio  $b_I/b_H$  represents the extent to which host fecundity is reduced/increased by  
 142 virus infection. If reduced, then the ratio is a measure of the virulence of the virus (virus-induced  
 loss of fitness).

In the mathematical analysis (Appendix A), we focused on the case  $p = 1$  (full vertical trans-  
 mission), while simulations were additionally performed for  $p < 1$  (partial vertical transmission;  
 Figure 1). For the case  $p = 1$ , a second basic reproductive number for invasion of uninfected  
 plants into an entirely infected plant population is derived. The equilibrium where the entire plant  
 population is infected is referred to as the susceptible-free equilibrium (SFE). A new threshold  
 value for the SFE is defined as

$$\overline{\mathcal{R}}_0 = \frac{b_H}{b_I} \exp(-\beta).$$

144 If  $\overline{\mathcal{R}}_0 < 1$ , then the SFE is stable and if  $\overline{\mathcal{R}}_0 > 1$  then the SFE is unstable (Appendix A.2). It  
 appears that  $p < 1$  is required for stable coexistence of both uninfected and infected plants to  
 146 occur (Appendix A). Figure 1-B shows that for  $b_I > 1$  and  $p < 1$ , the dynamics indeed converge

to an endemic equilibrium where uninfected and infected plants coexist.

## 148 2.3 Parameterization

The uninfected plant fecundity parameter  $b_H$  can be estimated from plant population dynamics. For instance,  $b_H$  ranges between 1.6 and 3.3 for the sand dune annual *Vulpia fasciculata* (Watkinson and Harper, 1978; Watkinson, 1980). By contrast,  $b_H$  is approximately 85 in Kherson oat (Montgomery, 1912; de Wit, 1960). Thus,  $b_H$  may range from 1 to 100, depending on the plant species considered. In this paper, infected plants may have greater fitness than uninfected plants, so  $b_I$  may range from 0 to 100 as well. Throughout the paper, we scale the plant densities by assuming a spatial unit such that  $\lambda = 1$ , without loss of generality.

In our model,  $\beta$  is a multiplication factor (Eq. 2) comparable to the basic reproductive number but restricted to the vector transmission period  $V$  (Eq. 6). Basic reproductive numbers are gaining increasing attention in the plant virus literature (Froissart et al., 2010; Péréfarres et al., 2014), yet few studies provide estimated values for this quantity. Reasonable values of  $\beta$  may range from 0 to 10 (Holt et al., 1997; Madden et al., 2000; Jeger et al., 2004), even though larger values might also be relevant (Escriu et al., 2003; Madden et al., 2007).

## 162 3 Evolutionary analysis

We follow an adaptive dynamics approach (Metz et al. 1992; Dieckmann and Law 1996; Geritz et al. 1998; Dieckmann 2004). To address the evolution of mutualistic viral symbioses, the single-strain model (5) is first extended to  $n$  virus strains which differ in their abilities to be seed-transmitted ( $b_I, p$ ) or vector-transmitted ( $\beta$ ). We then consider a plant population infected with  $n = 2$  virus strains,  $I_i$ ,  $i = 1, 2$ , which differ in their phenotypes. To simplify the notations, we drop the subscript  $I$  in  $b_I$  to replace it by the strain index  $i$ . Let  $x_1 = (\beta_1, b_1, p_1)$  be the resident

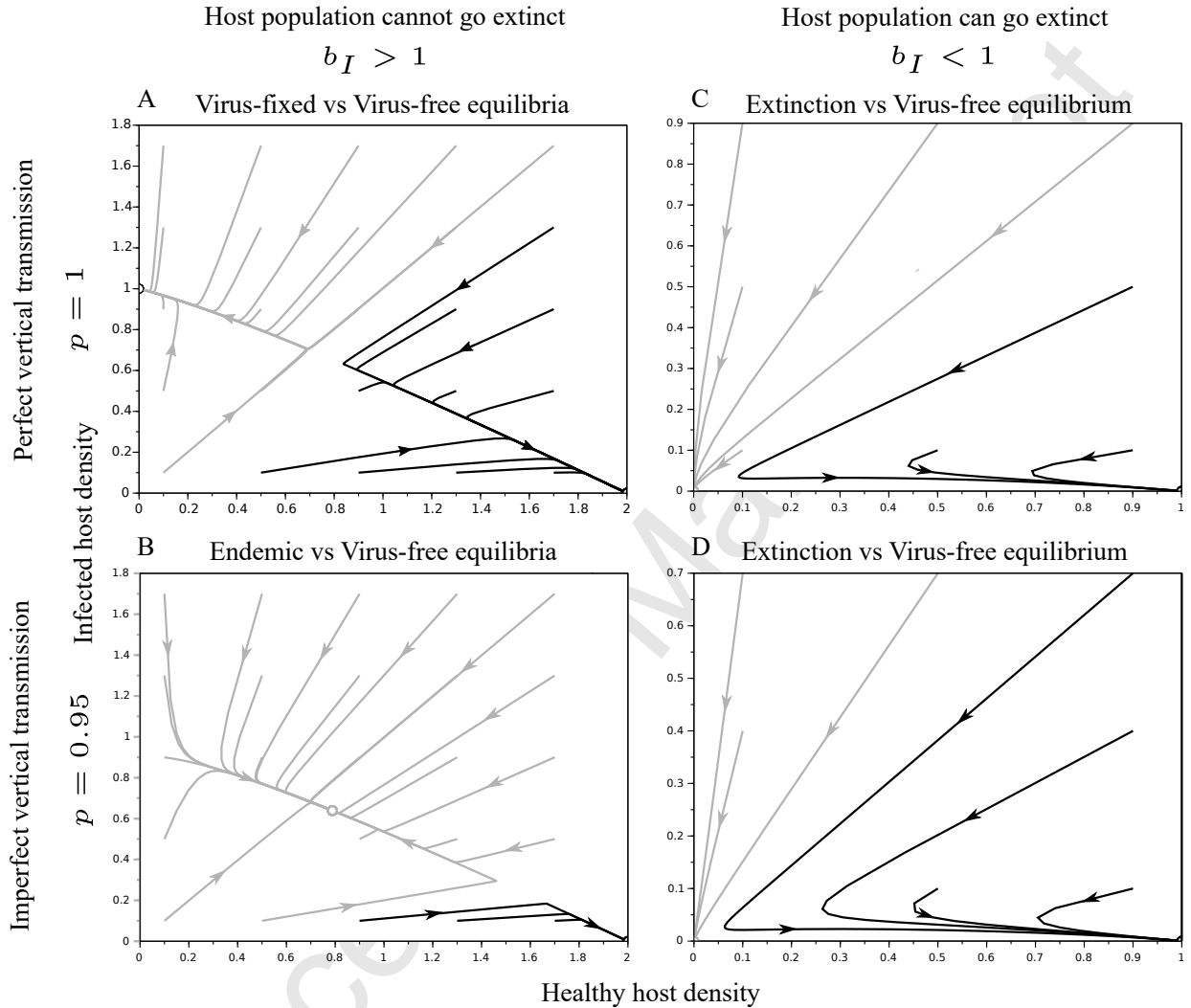


Figure 1: Virus and plant host population dynamics in the phase plane  $(H, I)$ . Each panel shows a set of possible orbits. Ecological bi-stability occurs for these parameter values ( $\mathcal{R}_0 < 1$  and, for  $p = 1$ ,  $\overline{\mathcal{R}_0} < 1$ ). Depending on initial conditions, the dynamics converge to the virus-free equilibrium (black curves) or to an alternative equilibrium (grey curves): (A) virus fixation in the plant population, (B) coexistence of uninfected and infected plants, (C-D) complete extinction of the plant host population. Parameter values: (A-B)  $b_H = 3$ ,  $b_I = 2$ ,  $\lambda = 1$ , (A)  $\beta = 0.45$ ,  $p = 1$ , (B)  $\beta = 0.57$ ,  $p = 0.95$ , (C-D)  $b_H = 2$ ,  $b_I = 0.5$ ,  $\lambda = 1$  (C)  $\beta = 2$ ,  $p = 1$ , (D)  $\beta = 2$ ,  $p = 0.95$ .

phenotype and let  $x_2 = (\beta_2, b_2, p_2)$  be the mutant phenotype. We assume the mutant initially  
 170 represents a relatively small subpopulation as compared to the resident. That is,  $I_2 \ll I_1$ .

### 3.1 Multi-strain dynamics

172 A natural extension of the single-strain model (5) to  $n$  virus strains,  $I_i$ ,  $i = 1, \dots, n$ , with traits  
 ( $\beta_i, b_i, p_i$ ) is

$$\begin{aligned} H(t+1) &= \frac{b_H H(t) P(t) + \sum_{k=1}^n (1-p_k) b_k \left( I_k(t) + H(t) (1-P(t)) \frac{\beta_k I_k(t)}{\sum_{j=1}^n \beta_j I_j(t)} \right)}{1 + \lambda T(t)}, \\ I_i(t+1) &= \frac{p_i b_i \left( I_i(t) + H(t) (1-P(t)) \frac{\beta_i I_i(t)}{\sum_{j=1}^n \beta_j I_j(t)} \right)}{1 + \lambda T(t)}, \end{aligned} \quad (7)$$

174 where  $T(t) = H(t) + \sum_{j=1}^n I_j(t)$ . The probability uninfected plants escape vector infection be-  
 comes

$$P(t) = \exp \left( - \sum_{j=1}^n \beta_j \frac{I_j(t)}{T(t)} \right), \quad (8)$$

176 whereas the expression  $(1 - P(t))$  is the probability of vector infection from some strain (Hamelin  
 et al., 2011).

### 3.2 Evolutionary invasion analysis

Following Metz et al. (1992), we are interested in testing whether the mutant can invade. In  
 180 particular, if

$$\lim_{t \rightarrow \infty} \frac{1}{t} \log \left( \frac{I_2(t)}{I_2(0)} \right) < 0, \quad (9)$$

the mutant cannot invade the resident. For simplicity, we assume that the resident population with  
 182 phenotype  $x_1$  is at ecological equilibrium, i.e.,  $I_1(0) \approx i(x_1) = i_1 > 0$  and  $H(0) = h(x_1) = h_1 > 0$ .

Thus, the resident population is at an equilibrium corresponding to coexistence of uninfected and

184 infected plants. We therefore define an evolutionary invasion condition as

$$\log \left( \frac{I_2(1)}{I_2(0)} \right) > 0. \quad (10)$$

From the assumptions  $I_2 \ll I_1$  and the resident population at ecological equilibrium, it follows  
 186 from model (7) with  $n = 2$  strains that the evolutionary invasion condition (10) can be expressed  
 as

$$\frac{I_2(1)}{I_2(0)} \approx \frac{p_2 b_2 \left( 1 + h_1 (1 - P_1) \frac{\beta_2}{\beta_1 i_1} \right)}{1 + \lambda (h_1 + i_1)} > 0, \quad (11)$$

188 with

$$P_1 = \exp \left( -\beta_1 \frac{i_1}{h_1 + i_1} \right),$$

where  $P_1$  is the probability that uninfected plants escape vector infection at the ecological equi-  
 190 librium corresponding to the resident phenotype  $x_1$ . Using the fact that the resident population  $I_1$   
 is at ecological equilibrium,

$$\frac{I_1(1)}{I_1(0)} \approx \frac{p_1 b_1 \left( 1 + h_1 (1 - P_1) \frac{\beta_1}{\beta_1 i_1} \right)}{1 + \lambda (h_1 + i_1)} = 1,$$

192 simplifies the evolutionary invasion condition to

$$\frac{p_2 b_2 \left( 1 + h_1 (1 - P_1) \frac{\beta_2}{\beta_1 i_1} \right)}{p_1 b_1 \left( 1 + h_1 (1 - P_1) \frac{\beta_1}{\beta_1 i_1} \right)} > 1. \quad (12)$$

Let  $F_1$  be the number of vector-borne infections per year relative to the force of infection of the  
 194 resident population, i.e.,

$$F_1 = \frac{h_1 (1 - P_1)}{\beta_1 i_1}. \quad (13)$$

The evolutionary invasion condition (12) can equivalently be expressed as

$$\underbrace{(p_2 b_2 - p_1 b_1)}_{\text{seed-only transmission}} + \underbrace{(\beta_2 p_2 b_2 - \beta_1 p_1 b_1) F_1}_{\text{vector-seed transmission}} > 0. \quad (14)$$

196 The expression on the left side of (14) is an invasion fitness proxy function,  $s(x_1, x_2)$ , sign-  
equivalent to the invasion fitness function in (10). The dynamics of  $s(x_1, x_2)$  as a function of the  
198 mutant phenotype  $x_2$  determine the evolutionary trajectories.

In this paper, virulence is defined as the negative impact of the virus on host fitness, i.e.,  
200  $b_H/b_I$ . The remainder of the analysis is restricted to the case of bipartite transmission-virulence  
trade-offs with negative correlations between  $b_I$  and  $p$  (vertical transmission), and  $b_I$  and  $\beta$   
202 (horizontal transmission).

### 3.3 Trade-off between vertical transmission and virulence

204 To consider a trade-off between seed transmission and virulence, we assume vector transmission  
is constant,  $\beta_i = \beta$ ,  $i = 1, 2$ , then the invasion condition (14) reads

$$(p_2 b_2 - p_1 b_1)(1 + \beta F_1) > 0.$$

206 Since  $F_1 \geq 0$ , the preceding inequality is equivalent to

$$p_2 b_2 - p_1 b_1 > 0.$$

Next, assume there is a trade-off between virulence and seed transmission, i.e.,  $p_i = g(b_i)$ ,  $i =$   
208  $1, 2$ , with  $g'(b_i) < 0$ . Then the invasion fitness proxy function depends only on  $b_1$  and  $b_2$ . That



is,

$$s(b_1, b_2) = g(b_2)b_2 - g(b_1)b_1. \quad (15)$$

210 The dynamics of  $s(b_1, b_2)$  as a function of  $b_2$  determine the evolutionary trajectory. In this case,  $b$  evolves so as to maximize the product  $g(b)b$  (Gyllenberg et al., 2011). This result was  
 212 confirmed by numerical simulations (Figure 2 A-B; Appendix B). However, it may be that the value of  $b$  that maximizes  $g(b)b$  is such that  $b \leq 1$  (Figure 2 C-D). In this case, evolution  
 214 drives the virus population to extinction (see also Figure 1). Such a phenomenon has recently been found to occur in a similar but continuous-time model with frequency-dependent horizontal  
 216 transmission (Boldin and Kisdi, 2016). Darwinian extinction under optimizing selection can also occur through a catastrophic bifurcation (Parvinen and Dieckmann, 2013).

### 218 3.4 Trade-off between horizontal transmission and virulence

The trade-off between vector transmission and virulence yields a different evolutionary outcome  
 220 than the trade-off between seed transmission and virulence. Assume seed transmission is constant,  $p_i = p > 0$ ,  $i = 1, 2$ . The invasion condition (14) is equivalent to

$$(b_2 - b_1) + (\beta_2 b_2 - \beta_1 b_1) F_1 > 0.$$

222 Let  $\beta_i = f(b_i)$ ,  $i = 1, 2$ , with  $f'(b_i) < 0$ . Then an invasion fitness proxy function is

$$s(b_1, b_2) = (b_2 - b_1) + (f(b_2)b_2 - b_1 f(b_1)) F_1(b_1). \quad (16)$$

In this case, there may exist an evolutionary singular point,  $b^*$ , if the selection gradient is zero,

$$G(b^*) = \frac{\partial s}{\partial b_2}(b^*, b^*) = 1 + (f(b^*) + b^* f'(b^*)) F_1(b^*) = 0. \quad (17)$$

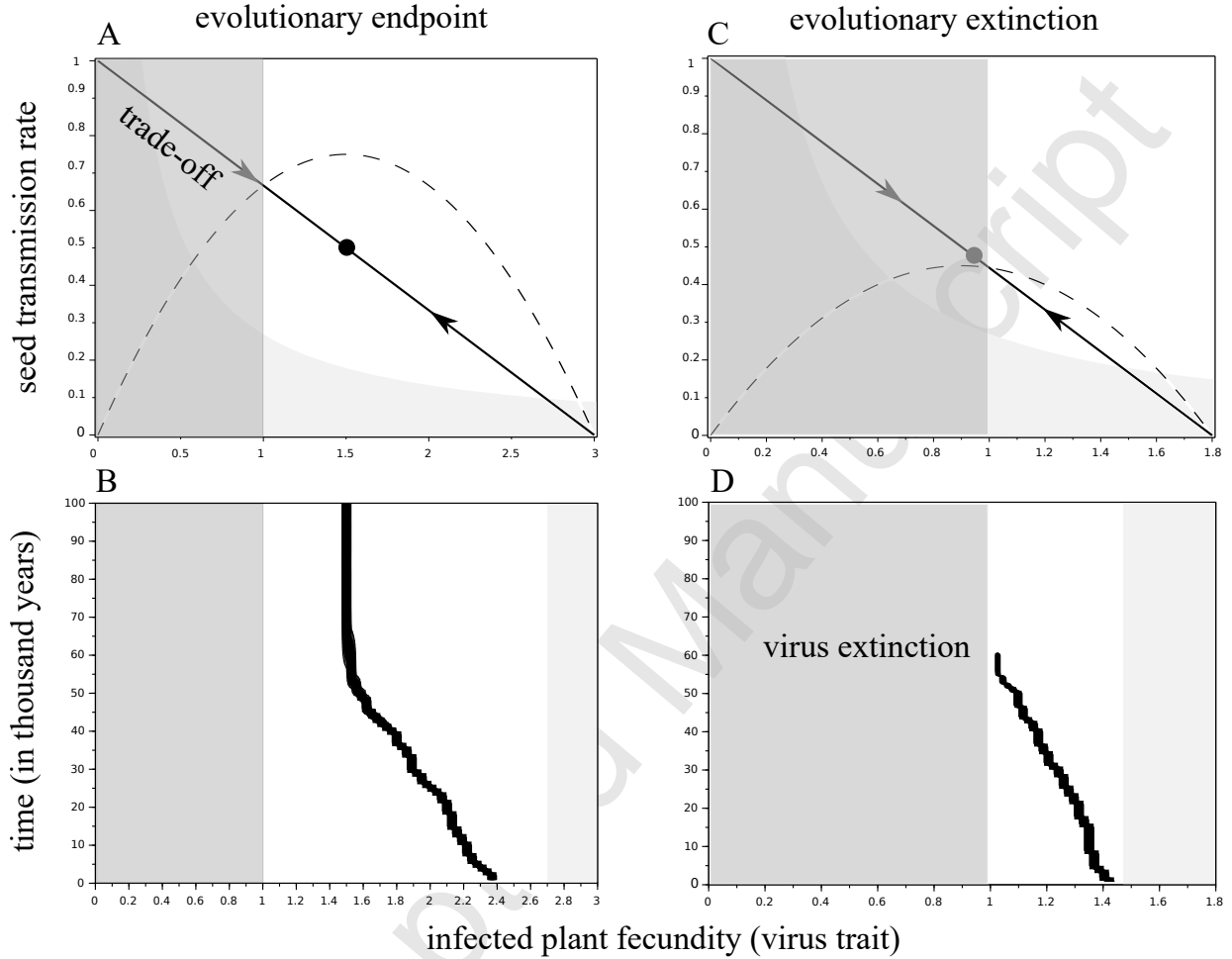


Figure 2: Evolutionary dynamics along a trade-off between infected plant fecundity ( $b_I$ ) and seed transmission rate ( $p$ ). The straight lines correspond to linear trade-off functions, i.e.,  $p = g(b_I) = 1 - b_I/B$ , with (A-B)  $B = 3$ , (C-D)  $B = 1.8$ . The dashed curves correspond to the associated functions  $g(b_I)b_I$ . The dots denote trait values maximizing  $g(b_I)b_I$ . The arrows denote the direction of evolution. The light gray regions correspond to  $\mathcal{R}_0 \leq 1$  (virus unable to invade). The darker gray regions correspond to  $b_I \leq 1$ , which leads to virus extinction (Fig. 1). The thick curves correspond to numerical simulations of the evolutionary dynamics (Appendix B): (B) starting from  $b_I \approx 2.4$ , evolution selects for decreasing  $b_I$  values until reaching an evolutionary endpoint ( $b_I = 1.5$ ) corresponding to the maximum of  $g(b_I)b_I$ , (D) starting from  $b_I \approx 1.4$ , evolution selects for decreasing  $b_I$  values until reaching  $b_I = 1$  where the virus population goes extinct. Other parameter values:  $b_H = 3$ ,  $\lambda = 1$ ,  $\beta = 10$ .

224 Whether  $b^*$  is evolutionarily stable is determined by the sign of the second derivative of  $s$  with respect to  $b_2$ , evaluated at  $b_1 = b_2 = b^*$ . The stability condition is

$$\frac{\partial^2 s}{\partial b_2^2}(b^*, b^*) = (2f'(b^*) + b^* f''(b^*)) F_1(b^*) < 0. \quad (18)$$

226 Since  $F_1(b^*) > 0$  and  $f'(b^*) < 0$ ,  $b^*$ , if it exists, is evolutionarily stable for concave or linear trade-off functions ( $f''(b^*) \leq 0$ ). For convex trade-off functions ( $f''(b^*) > 0$ ),  $b^*$  may be unsta-  
228 ble.

The singular point  $b^*$  is evolutionarily attractive if the derivative of the selection gradient  $G$   
230 in (17) at  $b^*$  is negative, i.e.,

$$G'(b^*) = (f(b^*) + b f'(b^*)) F_1'(b^*) + (2f'(b^*) + b f''(b^*)) F_1(b^*) < 0. \quad (19)$$

Unfortunately, we have no explicit expression of  $F_1$ , which makes conditions (18) and (19) in-  
232 tractable to analysis. Therefore, the trade-off between virulence and vector transmission is ex-  
plored through numerical simulations.

234 To perform the numerical computations, we considered the trade-off form:

$$\beta = f(b) = \beta_{\max} \exp(-k(b - b_{\min})).$$

This exponential form is convex and its curvature increases with  $k$  ( $f''(b) = k^2 f(b) > 0$ ). Also,  
236 this exponential form allows us to check the stability of a singular point as in this special case,  
the stability condition (18) becomes:

$$\frac{\partial^2 s}{\partial b_2^2}(b^*, b^*) = (2 - kb^*) f'(b^*) F_1(b^*) < 0.$$

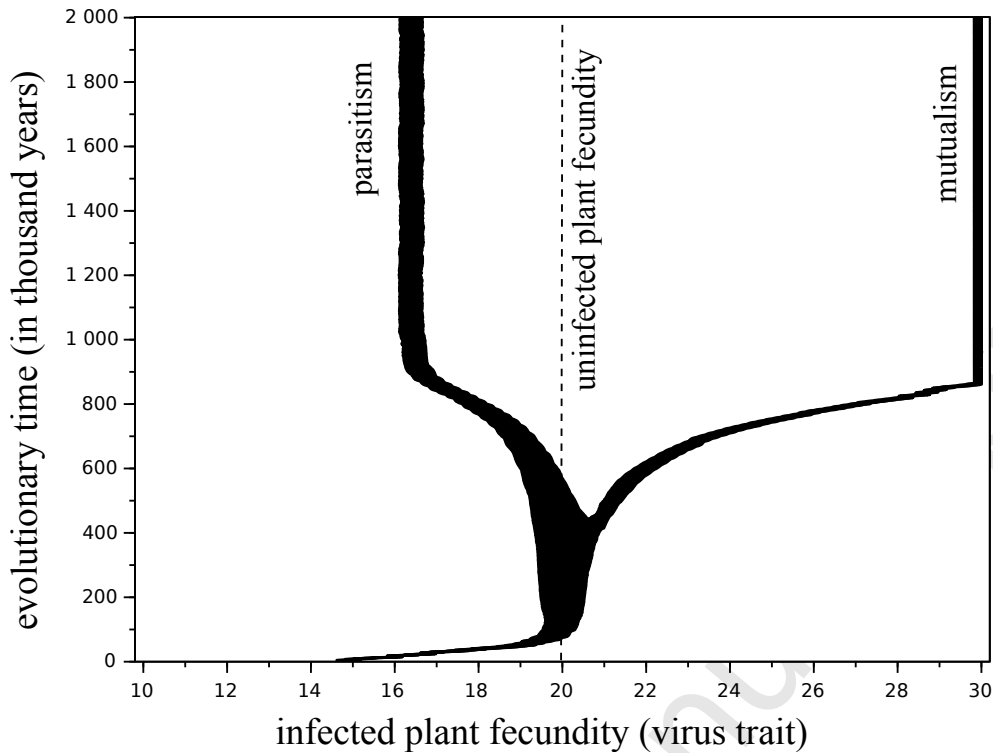


Figure 3: Evolutionary branching of parasitic and mutualistic viral symbioses and their long-run coexistence. We assumed a trade-off between transmission and virulence of the form:  $\beta = f(b) = \beta_{\max} \exp(-k(b - b_{\min}))$ . Parameter values:  $b_H = 20$ ,  $\lambda = 1$ ,  $b_{\min} = 10$ ,  $b_{\max} = 30$ ,  $p = 0.5$ ,  $\beta_{\max} = 10$ ,  $k = 0.1$ .

238 Since  $f'(b^*) < 0$ , the evolutionary stability of a singular point  $b^*$  requires

$$2 - kb^* > 0.$$

For the parameter set corresponding to Figures 3 and 4, including  $b_H = 20$  and  $k = 0.1$ , the critical value (indeterminate stability) is  $b_c = 2/k = 20$ . In our simulations,  $b^*$  seems to be slightly  
 240 above  $b_c$ , thus branching occurs after a relatively long period of apparent stability. Extensive  
 242 numerical simulations indicate that evolutionary branching is the rule rather than the exception  
 in this model. However the fact that  $b^*$  approximately coincides with both  $b_c$  and  $b_H$  is a coincidence used for illustrative purposes only. For instance, for  $b_H = 15$  and the other parameters  
 244 unchanged,  $b^* \approx 21$  is clearly greater than  $b_c = 20$  and  $b_H = 15$  (not shown).

246 Figures 3 and 4 show that it is possible for a mutualistic symbiosis to evolve ( $b_I/b_H > 1$ )

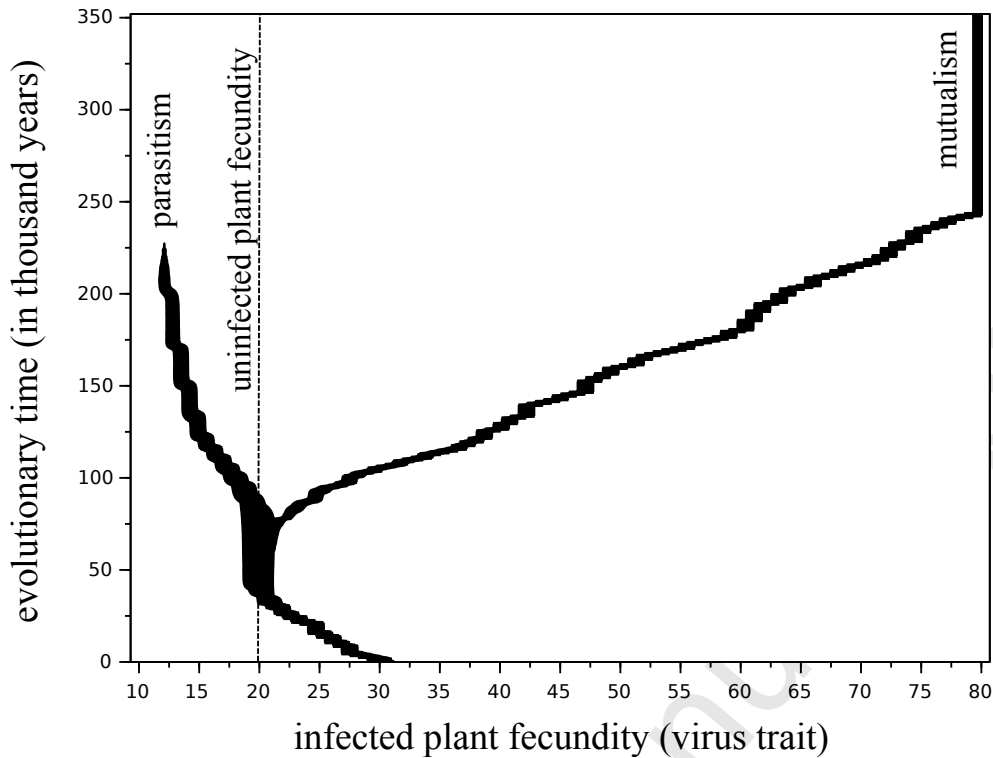


Figure 4: Evolutionary branching of parasitic and mutualistic viral symbioses and the eventual exclusion of parasitism by mutualism. We assumed a trade-off between transmission and virulence of the form:  $\beta = f(b) = \beta_{\max} \exp(-k(b - b_{\min}))$ . Parameter values:  $b_H = 20$ ,  $\lambda = 1$ ,  $b_{\min} = 10$ ,  $b_{\max} = 80$ ,  $p = 0.5$ ,  $\beta_{\max} = 10$ ,  $k = 0.1$ .

(or not) from a parasitic symbiosis ( $b_I/b_H < 1$ ) (Fig. 3), or conversely for a parasitic symbiosis  
 248 to evolve (or not) from an initial mutualistic symbiosis (Fig. 4). Starting from a monomorphic  
 virus population, evolutionary dynamics may converge towards commensalism and split into two  
 250 branches: parasitism and mutualism ( $b_I/b_H < 1$  and  $b_I/b_H > 1$ , respectively). The evolutionary  
 outcome depends on the biologically feasible maximum plant host fecundity value: if it is large  
 252 then mutualism may exclude parasitism in the long-run (Fig. 4), otherwise both parasitic and  
 mutualistic variants may coexist in the long-run (Fig. 3).

## 254 4 Discussion

### 4.1 Findings

#### 256 4.1.1 Ecological model

The discrete-time ecological model of an annual plant virus we developed included two modes of transmission: vector and seed. Key parameters include vector transmissibility  $\beta$ , uninfected and infected plant fecundities  $b_H$  and  $b_I$ , resp., and seed transmissibility  $p \leq 1$ . We can summarize our findings in terms of these parameters and the basic reproductive number  $\mathcal{R}_0$  that defines a threshold for successful invasion of infected plants. The main conclusions concern the type of virus–plant interaction, coexistence of infected and uninfected plants, and ecological bistability.

First, if there is only seed transmission, i.e.,  $\beta = 0$ , then  $\mathcal{R}_0 = pb_I/b_H$  indicating that purely vertical transmission through seed cannot maintain the virus in the host population unless the plant–virus symbiosis is mutualistic ( $b_I > b_H$ ). If, however, vector transmission is included with seed transmission ( $\beta > 0$ ) then a parasitic virus ( $b_I < b_H$ ) may be maintained in the host population.

Second, we checked conditions for the coexistence of uninfected and infected plants in specific models. In the case of full vertical transmission ( $p = 1$ ), there is a susceptible-free equilibrium corresponding to virus fixation. It is stable if the threshold  $\overline{\mathcal{R}_0}$  for successful invasion of uninfected plants is below one. However, numerical simulations indicate that a stable coexistence state between uninfected and infected plants does not exist for full vertical transmission. Instead, simulations suggest that stable coexistence requires partial seed transmission ( $p < 1$ ).

Third, we have found bistability in this model. That is, the dynamic behavior and the long-term solutions in particular depend on the initial conditions. There are three different types of bistability.

- (i) There is bistability between the virus-free and susceptible-free equilibria, i.e., either infected or uninfected plants go extinct but not both. This occurs if  $p = 1$ ,  $b_I > 1$ ,  $\mathcal{R}_0 < 1$  and  $\overline{\mathcal{R}_0} < 1$ . It is remarkable because the virus can infect the entire plant population even though  $\mathcal{R}_0 < 1$ . However, virus fixation in this case requires that healthy host plants have not reached their carrying capacity and the initial density of infected plants is sufficiently large, see the example in Figure 1A.
- (ii) There is bistability between an endemic coexistence equilibrium and the virus-free equilibrium, i.e., either both uninfected and infected plants coexist or infected plants go extinct. This has been observed for  $p < 1$ ,  $b_I > 1$ , and  $\mathcal{R}_0 < 1$ . The virus persists in the population in coexistence with uninfected plants, provided the latter are away from the uninfected carrying capacity state and the density of infected plants is sufficiently large, see the example in Figure 1B. That is, the infection can establish itself in the host population even though  $\mathcal{R}_0 < 1$ .
- (iii) There is bistability between the virus-free equilibrium and extinction, i.e., either the virus infects all plants or drives the entire plant population to extinction. This has been observed for both full and partial vertical transmission,  $\mathcal{R}_0 < 1$ ,  $\overline{\mathcal{R}_0} < 1$  and  $b_I < 1$ . The latter condition means that infected plants cannot persist on their own. If the virus is introduced in sufficiently large density of plants that have not reached their uninfected carrying capacity state, the virus drives the entire plant population extinct, see the examples in Figure 1C,D. Disease-induced host extinction is well-known to occur in time-continuous models with frequency-dependent horizontal transmission for the case  $\mathcal{R}_0 > 1$  (e.g. Getz and Pickering, 1983; Busenberg and van den Driessche, 1990), as virus transmission is ongoing even when the population density is close to zero. In discrete-time models, host extinction caused by disease-related mortality seems to have been less investigated (but see Franke and Yakubu,

2008, who also consider  $\mathcal{R}_0 > 1$ ). Here, we have shown that disease-induced host extinction  
302 can occur even if  $\mathcal{R}_0 < 1$ .

The occurrence of ecological bistability in an epidemiological model as simple as the one  
304 considered here is remarkable for three reasons. First, infection can persist in the population  
even if  $\mathcal{R}_0 < 1$ . This can be particularly important if control measures to combat virus infec-  
306 tions are aimed at reducing the basic reproduction number below one, because this will not be  
sufficient and a higher level of control will be necessary. The reason for this apparent ‘failure’ of  
308 the basic reproduction number is its derivation from the assumption that the system is at virus-  
free equilibrium. However, this of course not always the case, and one may even argue that this  
310 assumption rarely holds true considering the plethora of perturbations in variable and stochastic  
environments. That is, if the densities of infected and uninfected plants are far from this equilib-  
312 rium, the basic reproduction number does not apply anymore and may grossly underestimate the  
possibility of virus invasion. In particular, we have shown that if the density of infected plants is  
314 high or the density of uninfected plants low, the virus is likely to invade the population or even  
drive it extinct even if  $\mathcal{R}_0 < 1$ . Similar observations have been made in epidemiological models  
316 with backward bifurcations (e.g. Dushoff et al., 1998). In fact, numerical simulations (not shown  
here) suggest that our model exhibits a backward bifurcation as well.

318 Second, short-term dynamics can become particularly important if the system is bistable.  
Figure 5A shows the long-term total plant density as a function of vector transmissibility  $\beta$ . For  
320 an intermediate parameter range ( $0.29 < \beta < 0.33$ ) there is bistability between the susceptible-  
free and virus-free equilibrium. However, if we consider the plant densities after short-term  
322 (Fig. 5B), they show a range of values between the two equilibrium values. This is because the  
system dynamics becomes very slow for some initial plant densities such that they take very  
324 long to approach the equilibrium (there is an unstable coexistence state which slows down the



dynamics in its vicinity; cf. Appendix A.1). Transients are therefore important if the system is  
 326 bistable, as they ‘diversify’ the values taken by the plant densities. Moreover, due to this effect,  
 the bistability region has effectively ‘expanded’ to neighboring parameter regions.

328 Third, there is no bistability in similar (and even more general) continuous-time models possible  
 (Zhou and Hethcote, 1994). The simplest model with frequency-dependent transmission  
 330 that we know of and leads to bistability is of SEI type, i.e., has an extra compartment of latent  
 infections (Gao et al., 1995). In this model, bistability is possible for complete disease-induced  
 332 sterilization of the host population (Gao et al., 1995, Sect. 5), i.e., in terms of our model parameters  
 $b_I = 0$ . Considering that a latent infection compartment introduces a form of time delay in  
 334 the disease and host reproduction dynamics, it may not be too surprising that our discrete-time  
 SI model and the continuous-time SEI model show similar behavior.

#### 336 4.1.2 Evolutionary analysis

The ecological model was used to explore the evolution of the plant-virus symbiosis (parasitic or  
 338 mutualistic). The main conclusions from the evolutionary analysis are summarized below:

- (i) Vertical (seed) transmission ( $p$ ) versus virulence (defined as  $b_H/b_I$ ): evolution maximizes  
 340 the product  $pb_I$ , i.e., maximizes transmission relative to virulence. Interestingly, such a  
 trade-off can lead to virus extinction in evolutionary time.
- 342 (ii) Horizontal (vector) transmission ( $\beta$ ) versus virulence: evolutionary branching and the subsequent  
 coexistence of parasitic and mutualistic symbioses is possible, as well as the extinction  
 344 of the parasitic branch.

In the evolutionary simulations of vector transmission versus virulence, we assumed a simple  
 346 exponential trade-off function. Its convex shape allows for richer evolutionary dynamics than  
 linear or concave trade-off forms. Consideration of other trade-off shapes (e.g. linear) indicated

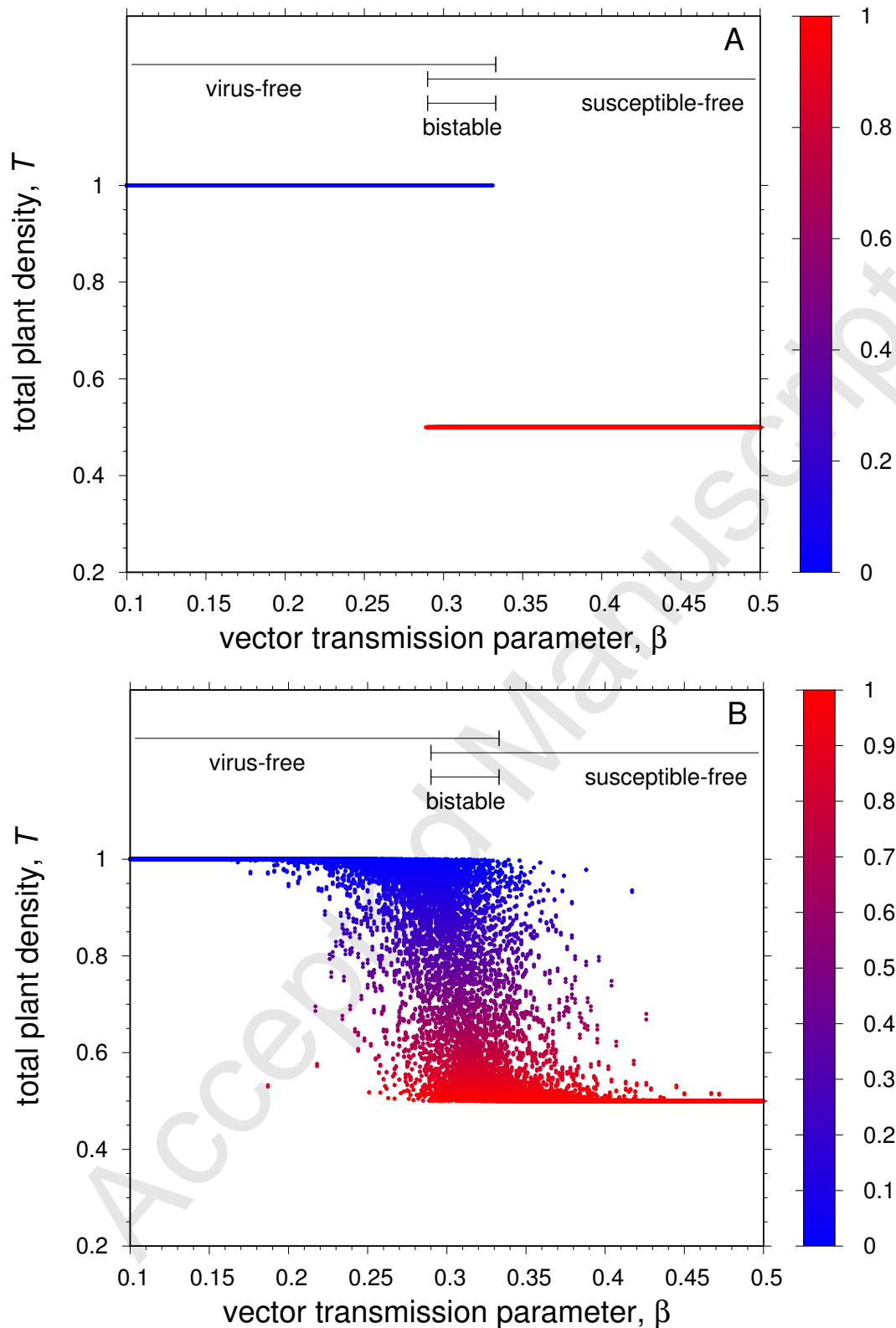


Figure 5: Total plant population density as a function of vector transmission parameter  $\beta$ . (A) Long-term dynamics, approximated after 10,000 years, (B) short-term dynamics after 100 years. The threshold criteria  $\mathcal{R}_0 = 1$  and  $\mathcal{R}_0 = 1$  correspond to  $\beta \approx 0.33$  and  $\beta \approx 0.29$ , respectively. In between these parameter values, the system tends to either the virus-free equilibrium with  $T = (b_H - 1)/\lambda = 1$  or the susceptible-free equilibrium with  $T = (b_I - 1)/\lambda = 0.5$ , depending on initial conditions. The color coding indicates the infection prevalence. For each value of  $\beta$ , 100 initial conditions were drawn from a pseudo-uniform random distribution. Parameter values:  $b_H = 2$ ,  $b_I = 1.5$ ,  $\lambda = 1$ ,  $p = 1$ .

348 that other outcomes are theoretically possible, such as directional selection and convergence to a  
 stable monomorphic evolutionary endpoint (as expected from the mathematical analysis). How-  
 350 ever, we never observed parasitism excluding mutualism after evolutionary branching occurred.  
 This might be because seed production is a necessary condition for virus year-to-year persistence  
 352 in our annual plant model.

## 4.2 Limits and prospects

354 In this study, we focused on unconditional mutualism, i.e., when infected plant fecundity is  
 always greater than uninfected plant fecundity. However, conditional mutualism occurs when in-  
 356 fected plants have lower fecundity than uninfected plants under favorable conditions, and higher  
 fecundity than uninfected plants under unfavorable conditions such as water stress (Hily et al.,  
 358 2016). Our model may be extended to address the evolution of conditional mutualism. A pos-  
 sibility would be to consider that  $b_H$  is a random variable that can take two values  $b_H^{\min}$  and  
 360  $b_H^{\max}$ , corresponding to unfavorable and favorable conditions, respectively, with mean  $\bar{b}_H$ . One  
 may then let  $b_I = \bar{b}_H + c(b_H - \bar{b}_H) - v$ , where  $v$  (for virulence) is the possible loss of fecundity  
 362 due to infection, and  $c \in [0, 1]$  is a coefficient buffering the variations of fecundity in infected  
 plants, subject to selection (if  $c = 0$ , the variance is zero). For instance,  $c = 0$  implies infected  
 364 plants have constant fecundity regardless of environmental variability. Whether and how such  
 conditional mutualism would evolve is left for future research.

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## 376 **References**

Bao, X. and M. J. Roossinck, 2013. A life history view of mutualistic viral symbioses: quantity  
378 or quality for cooperation? *Curr. Opin. Microbiol.* 16:514–518.

Boldin, B. and É. Kisdi, 2016. Evolutionary suicide through a non-catastrophic bifurcation:  
380 adaptive dynamics of pathogens with frequency-dependent transmission. *J. Math. Biol.*  
72:1101–1124.

382 Busenberg, S. and P. van den Driessche, 1990. Analysis of a disease transmission model in a  
population with varying size. *J. Math. Biol.* 28:257–270.

384 Davis, T. S., N. A. Bosque-Pérez, N. E. Foote, T. Magney, and S. D. Eigenbrode, 2015. Envi-  
ronmentally dependent host–pathogen and vector–pathogen interactions in the barley yellow  
386 dwarf virus pathosystem. *J. Appl. Ecol.* 52:1392–1401.

Dieckmann, U. and R. Law, 1996. The dynamical theory of coevolution: a derivation from  
388 stochastic ecological processes. *J. Math. Biol.* 34:579–612.

Diekmann, O., 2004. A beginner’s guide to adaptive dynamics. *Banach Center Publ.* 63:47–86.

390 Domier, L. L., H. A. Hobbs, N. K. McCoppin, C. R. Bowen, T. A. Steinlage, S. Chang, Y. Wang,

- and G. L. Hartman, 2011. Multiple loci condition seed transmission of soybean mosaic virus  
392 (SMV) and SMV-induced seed coat mottling in soybean. *Phytopathology* 101:750–756.
- Domier, L. L., T. A. Steinlage, H. A. Hobbs, Y. Wang, G. Herrera-Rodriguez, J. S. Haudenshield,  
394 N. K. McCoppin, and G. L. Hartman, 2007. Similarities in seed and aphid transmission among  
soybean mosaic virus isolates. *Plant Dis.* 91:546–550.
- 396 Doumayrou, J., A. Avellan, R. Froissart, and Y. Michalakis, 2013. An experimental test of the  
transmission-virulence trade-off hypothesis in a plant virus. *Evolution* 67:477–486.
- 398 Dushoff, J., W. Huang, and C. Castillo-Chavez, 1998. Backwards bifurcations and catastrophe  
in simple models of fatal diseases. *J. Math. Biol.* 36:227–248.
- 400 Escriu, F., A. Fraile, and F. García-Arenal, 2003. The evolution of virulence in a plant virus.  
*Evolution* 57:755–765.
- 402 Fine, P., 1975. Vectors and vertical transmission: an epidemiological perspective. *Ann. N. Y.*  
*Acad. Sci.* 266:173–194.
- 404 Fraile, A. and F. García-Arenal, 2016. Environment and evolution modulate plant virus patho-  
genesis. *Curr. Opin. Virol.* 17:50–56.
- 406 Franke, J. E. and A.-A. Yakubu, 2008. Disease-induced mortality in density-dependent discrete-  
time S-I-S epidemic models. *J. Math. Biol.* 57:755–790.
- 408 Froissart, R., J. Doumayrou, F. Vuillaume, S. Alizon, and Y. Michalakis, 2010. The virulence-  
transmission trade-off in vector-borne plant viruses: a review of (non-) existing studies. *Phil.*  
410 *Trans. R. Soc. B* 365:1907–1918.
- Gao, L. Q., J. Mena-Lorca, and H. W. Hethcote, 1995. Four SEI endemic models with periodicity  
412 and separatrices. *Math. Biosci.* 128:157–184.

- Geritz, S. A., E. Kisdi, G. Meszéna, and J. A. Metz, 1998. Evolutionarily singular strategies and  
414 the adaptive growth and branching of the evolutionary tree. *Evol. Ecol.* 12:35–57.
- Getz, W. M. and J. Pickering, 1983. Epidemic models - thresholds and population regulation.  
416 *Am. Nat.* 121:892–898.
- Gibbs, A., 1980. A plant virus that partially protects its wild legume host against herbivores.  
418 *Intervirology* 13:42–47.
- Groen, S. C., S. Jiang, A. M. Murphy, N. J. Cunniffe, J. H. Westwood, M. P. Davey, T. J. Bruce,  
420 J. C. Caulfield, O. J. Furzer, A. Reed, et al., 2016. Virus infection of plants alters pollinator  
preference: A payback for susceptible hosts? *PLoS Pathog.* 12:e1005790.
- 422 Gyllenberg, M., J. H. Metz, and R. Service, 2011. When do optimisation arguments make evolutionary  
sense? *The Mathematics of Darwin's Legacy* Pp. 233–268.
- 424 Hamelin, F. M., L. J. Allen, H. R. Prendeville, M. R. Hajimorad, and M. J. Jeger, 2016. The  
evolution of plant virus transmission pathways. *J. Theor. Biol.* 396:75–89.
- 426 Hamelin, F. M., M. Castel, S. Poggi, D. Andrivon, and L. Mailleret, 2011. Seasonality and the  
evolutionary divergence of plant parasites. *Ecology* 92:2159–2166.
- 428 Harper, G., R. Hull, B. Lockhart, and N. Olszewski, 2002. Viral sequences integrated into plant  
genomes. *Annu. Rev. Phytopathol.* 40:119–136.
- 430 Hily, J.-M., N. Poulicard, M.-Á. Mora, I. Pagán, and F. García-Arenal, 2016. Environment  
and host genotype determine the outcome of a plant–virus interaction: from antagonism to  
432 mutualism. *New Phytol.* 209:812–822.
- Holt, J., M. Jeger, J. Thresh, and G. Otim-Nape, 1997. An epidemiological model incorporating

- 434 vector population dynamics applied to african cassava mosaic virus disease. *J. Appl. Ecol.* Pp.  
793–806.
- 436 Jeger, M., J. Holt, F. Van Den Bosch, and L. Madden, 2004. Epidemiology of insect-transmitted  
plant viruses: modelling disease dynamics and control interventions. *Physiol. Entomol.*  
438 29:291–304.
- Johansen, E., M. C. Edwards, and R. O. Hampton, 1994. Seed transmission of viruses: current  
440 perspectives. *Annu. Rev. Phytopathol.* 32:363–386.
- Johansen, I., W. Dougherty, K. Keller, D. Wang, and R. Hampton, 1996. Multiple viral determi-  
442 nants affect seed transmission of pea seedborne mosaic virus in *Pisum sativum*. *J. Gen. Virol.*  
77:3149–3154.
- 444 Kisdi, E. and S. A. Geritz, 2003. On the coexistence of perennial plants by the competition-  
colonization trade-off. *Am. Nat.* 161:350–354.
- 446 Madden, L., M. Jeger, and F. Van den Bosch, 2000. A theoretical assessment of the effects  
of vector-virus transmission mechanism on plant virus disease epidemics. *Phytopathology*  
448 90:576–594.
- Madden, L. V., G. Hughes, and F. van den Bosch, 2007. The study of plant disease epidemics.  
450 American Phytopathological Society (APS Press).
- Metz, J. A. J., R. Nisbet, and S. Geritz, 1992. How should we define fitness for general ecological  
452 scenarios? *Trends Ecol. Evol.* 7:198–202.
- van Mølken, T. and J. F. Stuefer, 2011. The potential of plant viruses to promote genotypic  
454 diversity via genotype  $\times$  environment interactions. *Ann. Bot.* 107:1391–1397.
- Montgomery, E. G., 1912. Competition in cereals. *J. Hered.* Pp. 118–127.

- 456 Pacala, S. W. and J. Silander Jr, 1985. Neighborhood models of plant population dynamics. i.  
single-species models of annuals. *Am. Nat.* 125:385–411.
- 458 Pagán, I., N. Montes, M. G. Milgroom, and F. García-Arenal, 2014. Vertical transmission selects  
for reduced virulence in a plant virus and for increased resistance in the host. *PLoS Pathog.*  
460 10:e1004293.
- Parvinen, K. and U. Dieckmann, 2013. Self-extinction through optimizing selection. *J. Theor.*  
462 *Biol.* 333:1–9.
- Péréfarres, F., G. Thébaud, P. Lefeuvre, F. Chiroleu, L. Rimbaud, M. Hoareau, B. Reynaud,  
464 and J.-M. Lett, 2014. Frequency-dependent assistance as a way out of competitive exclusion  
between two strains of an emerging virus. *Proc. R. Soc. B* 281:20133374.
- 466 Roossinck, M. J., 2011. The good viruses: viral mutualistic symbioses. *Nature Rev. Microbiol.*  
9:99–108.
- 468 Ross, R., 1911. *The Prevention of Malaria*. Murray, London, UK.
- Shapiro, L., C. M. Moraes, A. G. Stephenson, and M. C. Mescher, 2012. Pathogen effects on veg-  
470 etative and floral odours mediate vector attraction and host exposure in a complex pathosystem.  
*Ecol. Lett.* 15:1430–1438.
- 472 Stewart, A. D., J. M. Logsdon, and S. E. Kelley, 2005. An empirical study of the evolution of  
virulence under both horizontal and vertical transmission. *Evolution* 59:730–739.
- 474 Watkinson, A., 1980. Density-dependence in single-species populations of plants. *J. Theor. Biol.*  
83:345–357.
- 476 Watkinson, A. and J. Harper, 1978. The demography of a sand dune annual: *Vulpia fasciculata*:  
I. the natural regulation of populations. *J. Ecol.* Pp. 15–33.



478 de Wit, C. T., 1960. On competition. Versl. Landbouwk. Onderz. 66.

Xu, P., F. Chen, J. P. Mannas, T. Feldman, L. W. Sumner, and M. J. Roossinck, 2008. Virus  
480 infection improves drought tolerance. *New Phytol.* 180:911–921.

Zhou, J. and H. W. Hethcote, 1994. Population size dependent incidence in models for diseases  
482 without immunity. *J. Math. Biol.* 32:809–834.

## A Additional analyses

### 484 A.1 Full vertical transmission

Focusing on the case  $p = 1$  (full vertical transmission), model (5) reads:

$$\begin{aligned} H(t+1) &= \frac{b_H H(t) P(t)}{1 + \lambda T(t)}, \\ I(t+1) &= \frac{b_I (I(t) + H(t) (1 - P(t)))}{1 + \lambda T(t)}. \end{aligned} \quad (20)$$

486 If  $b_I > 1$ , there exists a “susceptible-free” equilibrium (SFE) which is found by setting  $H = 0$   
and solving for  $I$ . The SFE value for  $I$  is

$$\bar{I} = \frac{b_I - 1}{\lambda}.$$

488 Linearizing the difference equation for the uninfected host  $H$  about the SFE, we obtain the basic  
reproductive number of an uninfected host introduced into a fully infected population:

$$\overline{\mathcal{R}}_0 = \frac{b_H}{b_I} \exp(-\beta).$$

490 The notation  $\overline{\mathcal{R}}_0$  stands for the dual of  $\mathcal{R}_0$  (Hamelin et al., 2016). If  $\overline{\mathcal{R}}_0 > 1$  then the SFE is

unstable. If both  $\mathcal{R}_0 > 1$  and  $\overline{\mathcal{R}}_0 > 1$ , then infected and uninfected plants can invade each other  
 492 when rare, so coexistence of uninfected and infected plants is protected (Kisdi and Geritz, 2003).

It appears that there is no stable coexistence equilibrium with both uninfected and infected  
 494 plants. The ecologically relevant results are summarized for  $b_I > 1$  and  $b_I < 1$ .

In the case  $b_I > 1$ , there exist both a VFE and a SFE. The two reproductive numbers equal

$$\mathcal{R}_0 = \frac{b_I}{b_H}(1 + \beta) \quad \text{and} \quad \overline{\mathcal{R}}_0 = \frac{b_H}{b_I} \exp(-\beta),$$

496 respectively. It follows that

$$\mathcal{R}_0 \overline{\mathcal{R}}_0 < 1.$$

Therefore,  $\mathcal{R}_0 > 1$  and  $\overline{\mathcal{R}}_0 > 1$  is impossible; coexistence of uninfected and infected plants is  
 498 not protected. Moreover, in Section A.1.1 it is shown that there exists an endemic equilibrium  
 (EE) such that  $H, I > 0$  if and only if  $\mathcal{R}_0 < 1$  and  $\overline{\mathcal{R}}_0 < 1$  but it does not appear to be stable. In  
 500 addition, it is shown that if  $\overline{\mathcal{R}}_0 < 1$ , then the SFE is locally stable. Both reproductive numbers  
 less than 1 leads to ecological bi-stability. The three ecologically relevant cases are summarized  
 502 below (see also Figure 6).

- 1: If  $\mathcal{R}_0 < 1$  and  $\overline{\mathcal{R}}_0 > 1$ , then the VFE is globally stable.
- 504 2: If  $\mathcal{R}_0 < 1$  and  $\overline{\mathcal{R}}_0 < 1$ , then there is bi-stability of the VFE and the SFE (either infected or  
 uninfected plants go extinct but not both).
- 506 3: If  $\mathcal{R}_0 > 1$  and  $\overline{\mathcal{R}}_0 < 1$ , then the SFE is globally stable.

For the case  $b_I < 1$ , there is no SFE, only the VFE. The numerical results indicate that there  
 508 are only two ecologically relevant cases.

- 4: If  $\overline{\mathcal{R}}_0 < 1$ , then there is bi-stability of the VFE and the extinction “equilibrium” (either

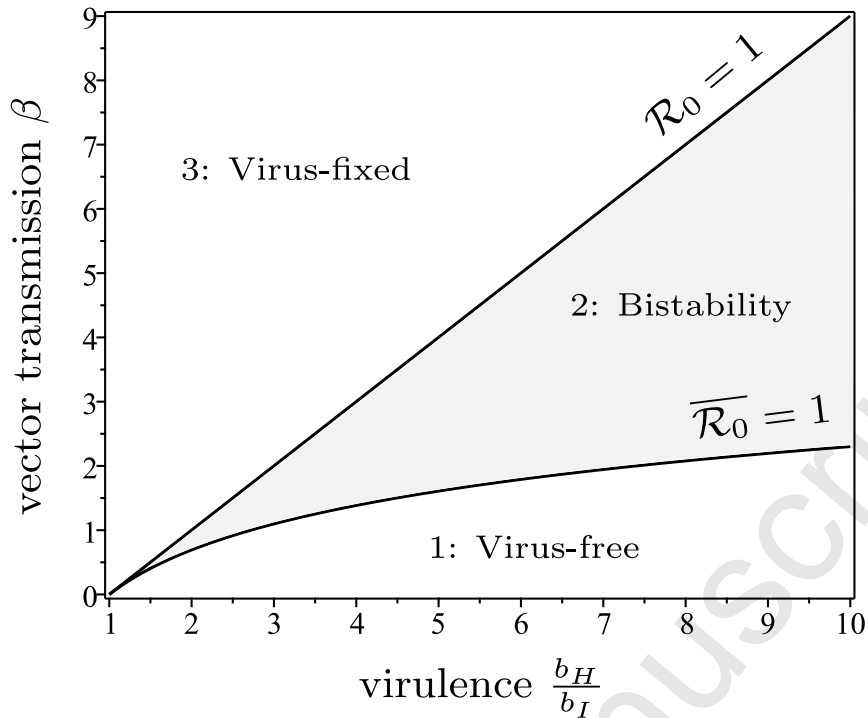


Figure 6: The three ecologically relevant cases for  $p = 1$  and  $b_I > 1$ , with  $\mathcal{R}_0 = (b_I/b_H)(1 + \beta)$  and  $\overline{\mathcal{R}}_0 = (b_H/b_I)\exp(-\beta)$  (see text). The range of  $\beta$  values for which ecological bistability occurs increases with  $b_H/b_I$  (virulence).

510 infected plants go extinct or there is complete population extinction).

5: If  $\overline{\mathcal{R}}_0 > 1$ , then the VFE is globally stable.

512 Simulations performed for  $q = 1 - p \ll 1$  (slightly partial vertical transmission) showed similar results to the case  $p = 1$  with the exception that the SFE becomes an endemic equilibrium  
 514 (for which we have no explicit expression). Therefore, coexistence of uninfected and infected plants is possible in this model.

516 **A.1.1 Existence conditions of an endemic equilibrium**

Model (5) has the following form:

$$H(t+1) = \frac{b_H H(t) \exp\left(-\frac{\beta I(t)}{T(t)}\right) + qb_I \left[ I(t) + H(t) \left[ 1 - \exp\left(-\frac{\beta I(t)}{T(t)}\right) \right] \right]}{1 + \lambda T(t)}$$

$$I(t+1) = \frac{pb_I \left[ I(t) + H(t) \left[ 1 - \exp\left(-\frac{\beta I(t)}{T(t)}\right) \right] \right]}{1 + \lambda T(t)}.$$

518 We focus on the case  $p = 1 - q = 1$  (full vertical transmission). Let

$$H^* = \frac{H}{\bar{H}}, I^* = \frac{I}{\bar{H}}.$$

The dimensionless model (asterisk notation has been dropped) simplifies to

$$H(t+1) = \frac{b_H H(t) \exp\left(-\frac{\beta I(t)}{H(t) + I(t)}\right)}{1 + (b_H - 1)(H(t) + I(t))} \quad (21)$$

$$I(t+1) = \frac{b_I \left[ I(t) + H(t) \left[ 1 - \exp\left(-\frac{\beta I(t)}{H(t) + I(t)}\right) \right] \right]}{1 + (b_H - 1)(H(t) + I(t))}. \quad (22)$$

520 There exist at most three equilibria:

$$(1, 0), \left(0, \frac{b_I - 1}{b_H - 1}\right), \text{ and } (h, i).$$

Consider the proportions  $\hat{i} = i/(h+i)$  and  $\hat{h} = h/(h+i)$ . Then  $\hat{i} + \hat{h} = 1$ . If  $b_I \geq 1$ , then the total plant population is bounded below by a positive constant (Appendix A.2). If the population does not go extinct, then existence of a unique  $\hat{i}$ ,  $0 < \hat{i} < 1$  implies existence of a unique  $(h, i)$ . We derive conditions for existence of a unique  $\hat{i}$ ,  $0 < \hat{i} < 1$ . Using the notation  $h$ ,  $i$  and  $\hat{i}$  in Eq. (21), it follows that  $1 + (b_H - 1)(h+i) = b_H e^{-\beta \hat{i}}$ . Substituting this latter expression into Eq. (22), we

obtain an implicit expression for  $\hat{i}$ :

$$\hat{i} = \frac{b_I(1 - (1 - \hat{i})e^{-\beta\hat{i}})}{b_H e^{-\beta\hat{i}}}$$

which can be expressed as

$$\hat{i} \left( \frac{b_H}{b_I} - 1 \right) + 1 = e^{\beta\hat{i}}. \quad (23)$$

The two curves  $f_1(\hat{i}) = \hat{i} \left( \frac{b_H}{b_I} - 1 \right) + 1$  and  $f_2(\hat{i}) = e^{\beta\hat{i}}$  intersect at  $\hat{i} = 0$  so that a unique positive solution exists  $\hat{i}$ ,  $0 < \hat{i} < 1$ , if and only if the following conditions hold:

$$\frac{b_H}{e^\beta} < b_I < \frac{b_H}{1 + \beta}$$

522 ( $f_1'(0) > f_2'(0)$  and  $f_1(1) < f_2(1)$ ). The left side of the inequality is equivalent to  $\overline{\mathcal{R}_0} < 1$  and the right side is equivalent to  $\mathcal{R}_0 < 1$ .

## 524 A.2 Plant population is bounded

For model (1)–(4), it is shown that the total plant population is bounded and if the average number  
526 of seeds per infected plant is greater than one,  $b_I > 1$ , then the plant population always persists.

The total plant population,  $T(t) = H(t) + I(t)$  is bounded below by zero;  $H(t)$  and  $I(t)$  are  
528 nonnegative. In addition, we show that the total population is bounded above and for the case  
 $b_I > 1$ , the total population is bounded below by a positive constant. The total plant population  
530 satisfies the inequality

$$T(t+1) \leq \frac{b_H T(t)}{1 + \lambda T(t)} = f_H(T(t)),$$

since  $b_H > b_I$ . Comparing the solution  $T(t)$  with the solution of the difference equation,  $x(t +$   
532  $1) = f_H(x(t))$ , where  $x(0) = T(0) > 0$ , it follows that  $T(1) \leq f_H(T(0)) = f_H(x(0)) = x(1)$ .

Since  $f_H(x)$  is monotone increasing for  $x \in [0, \infty)$ ,  $f_H(T(1)) \leq f_H(x(1))$ , leads to  $T(2) \leq x(2)$

534 and in general, from induction it follows that  $T(t) \leq x(t)$  for  $t \in \{0, 1, 2, 3, \dots\}$ . The fact that  $x(t)$  approaches  $\bar{H} = (b_H - 1)/\lambda$  monotonically implies  $T(t) \leq \max\{T(0), \bar{H}\}$ .

536 A similar argument applies in the case  $b_I > 1$  to show that the total plant population is bounded below by a positive constant, e.g., uniform persistence. The inequality  $b_H > b_I$  leads to  
538 the reverse inequality for the total plant population:

$$T(t+1) \geq \frac{b_I T(t)}{1 + \lambda T(t)} = f_I(T(t)).$$

Comparing the solution of  $T(t)$  with the solution of  $y(t+1) = f_I(y(t))$ ,  $T(0) = y(0)$ , leads to  
540  $T(t) \geq y(t)$  for  $t \in \{0, 1, 2, \dots\}$ . Since  $b_I > 1$ , the solution  $y(t)$  converges monotonically to  $\bar{I} = (b_I - 1)/\lambda > 0$  which implies  $T(t) \geq \min\{T(0), \bar{I}\}$ .

### 542 A.3 Absence of vector transmission

Focusing on the case  $\beta = 0$  (no vector transmission), model (5) reads:

$$\begin{aligned} H(t+1) &= \frac{b_H H(t) + (1-p)b_I I(t)}{1 + \lambda T(t)}, \\ I(t+1) &= \frac{pb_I I(t)}{1 + \lambda T(t)}, \end{aligned} \quad (24)$$

544 where  $T(t) = H(t) + I(t)$ . There exist at most three equilibria:

$$(0, 0), \quad \left( \frac{b_H - 1}{\lambda}, 0 \right), \quad \left( h = \frac{b_I(1-p)(1-pb_I)}{\lambda(b_H - b_I)}, i = \frac{(pb_I - b_H)(1-pb_I)}{\lambda(b_H - b_I)} \right).$$

If  $b_H > b_I$ , then  $h > 0$  implies  $pb_I < 1$ , and  $i > 0$  thus implies  $pb_I > b_H$  which is impossible since  
546  $b_H > 1$ . If  $b_I > b_H$  then  $h > 0$  implies  $pb_I > 1$  and  $i > 0$  thus implies  $pb_I > b_H > 1$ . Therefore, the endemic equilibrium  $(h, i)$  existence requires  $pb_I > b_H$ .

## 548 **B Evolutionary simulations**

Evolutionary computations in Figures 2, 3 and 4 were realized from the multi-strain model (7) using the following algorithm. The evolving phenotype  $b$  ranges from  $b_{\min}$  to  $b_{\max}$ , the biologically feasible minimum and maximum plant host fecundity values. The interval  $[b_{\min}, b_{\max}]$  is divided into a finite number of subintervals (here 100), each with length  $\Delta b$ . The evolutionary dynamics are governed by the following iteration scheme. The scheme is initiated with a given value of  $b$  equal to one of the endpoints of the subintervals. Next, the ecological equilibrium is computed from the multi-strain model (here after a fixed time horizon of 1,000 years), then a small mutation  $\pm\Delta b$  occurs in  $b$  with equal likelihood of being smaller or larger than  $b$ . Time is advanced by one unit in evolutionary time (1,000 years) and  $b$  is changed to either  $b + \Delta b$  or  $b - \Delta b$ . The evolutionary process continues with this new  $b$  value.