

A Multi-layer Network Framework of Scientometrics and  
Its Application to Name Disambiguation, Diversity  
Measure and Ranking

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$$\frac{e^{\pm\beta H}}{Z}$$

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# A three-layer network

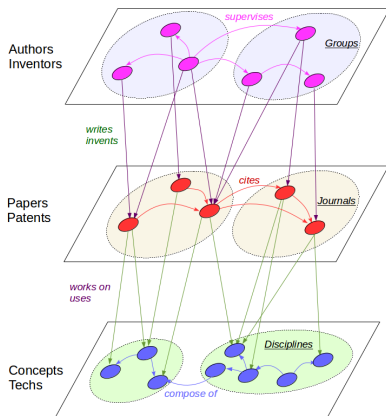


Figure: One network captures various (all?) relational data

## A three-layer network, continued

- Within layers: authors (supervising), papers (citing), concepts (logic)
- Among layers, authors write papers, papers work on concepts
- Many kinds of co-occurrence relations may be represented
- Important to take contents into consideration to certain degree, concept
- New questions, new methods can be applied to old questions
- We branch out for now and we will come back to this main trunk

# Direct and indirect connections

- On a network of papers with citing relation, not all citations should be considered equal, thus the PageRank method, EigenFactor and SCImago
- Similar ideas in Leontief's Input-Output Analysis (LIOA) in Economics and our general input-output analysis (GIOA)
  - links should be different, not only via the more important nodes (PageRank), but maybe also a weight on the links itself (GIOA)
  - Eigenvectors (PageRank, GIOA) or inverse (LIOA) of matrices take both direct and indirect relation into consideration

# Overly simplified intro to LIOA

- Definition,  $x_j^i$  means the amount of input from the sector  $i$  to the sector  $j$
- Definition, total output from the sector  $i$

$$X^i = \sum_{j=1}^{N-1} x_j^i + y^i = \sum_{j=1}^{N-1} b_j^i X^j + y^i, \forall i \neq N. \quad (1)$$

$$b_j^i = x_j^i / X^j. \quad (2)$$

- Thus that in order to supply enough  $Y$ ,  $X$  has to be

$$X = \left(1 - B^{(N-1)}\right)^{-1} Y = Y + B^{(N-1)} Y + B^{(N-1)} B^{(N-1)} Y + \dots \quad (3)$$

takes both direct and indirect connections into consideration

# Overly simplified intro to GIOA

- For closed systems, instead of  $B^{(-N)}$  we have to consider direct  $B$
- Naively, we might try the right largest eigenvector of  $B$ , however

$$BX = X. \quad (4)$$

- Naively, we might try the left largest eigenvector of  $B$ , however it is simply the PageRank vector (ask me question, 😊)
- Since  $X$  is the largest right eigenvector of  $B$ , what are the intuitive meaning of the largest right eigenvector of  $B^{-i}$ ?
- Let us denote them as  $\lambda_{max}^{-i}$  and  $|\lambda_{max}^{-i}\rangle$  (we skip the meaning of this vector for now), and we define

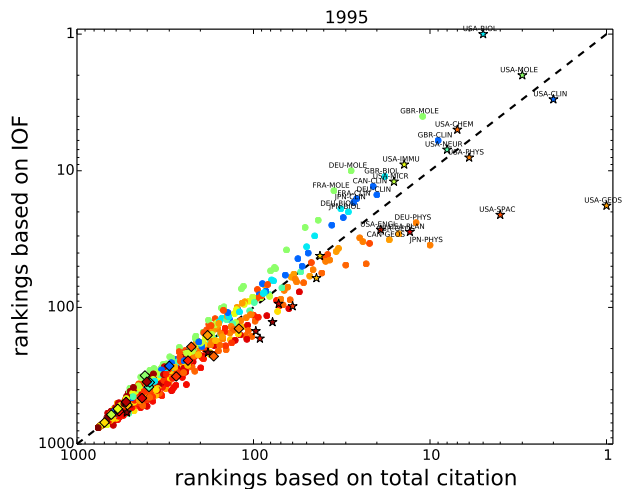
$$S_{IO}^j = 1 - \lambda_{max}^{(-j)}, \quad (5)$$

## Results on contries and fields

- Data on citation and classification from WoS, but not JCR
- Define a matrix  $B$  with  $40(\text{counties}) \times 22(\text{subjects})$  entries
- Calculate  $S_{IO}^j$  for each combination of country and subject
- We also have results on contries and on subjects (not shown here)



## Results on contries and fields, continued









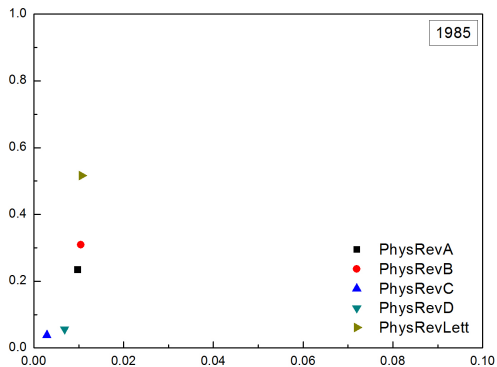
## Results on contries and fields, continued



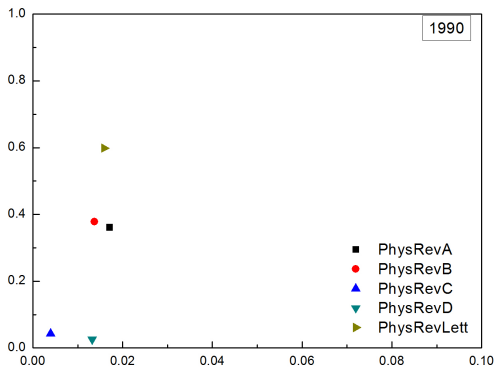
# Ideas

- Ranking authors, papers, concepts and more
- Measure of diversity and novelty (paper, author, reference)
- Merging author names (author-fields, similarity)
- Key ingredients: propagation over the network

# Some very preliminary results

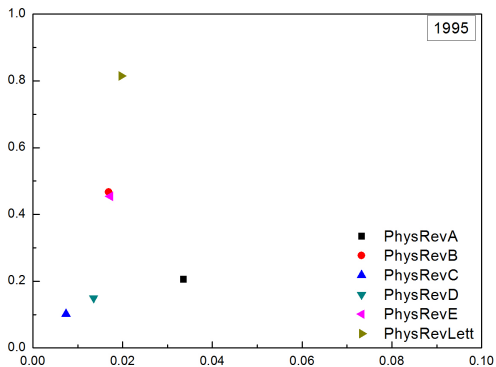


# Some very preliminary results

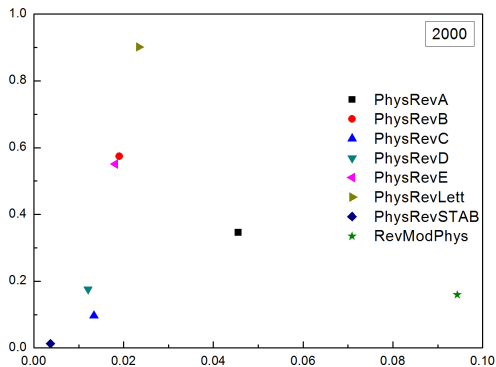




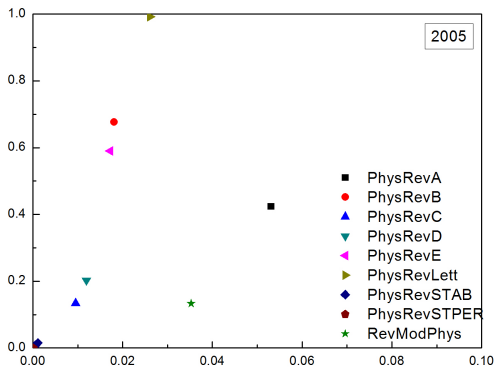
# Some very preliminary results



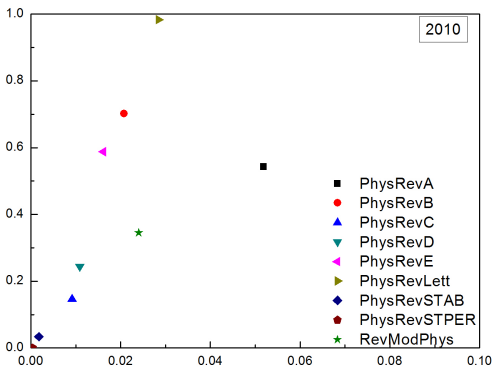
# Some very preliminary results



## Some very preliminary results



## Some very preliminary results



## to make it short

- The three-layer framework has a lot of potential
- Both direct and indirect effects should be considered
- Especially over the multi-layer network
- Lots of phenomena can be investigated in this way

# Acknowledgement and time for questions

- Thanks to Zhesi Shen, Menghui Li, Jianzhang Bao, Tian Wei, Jiansuo Pei, Liying Yang, Chensheng Wu, Zengru Di, Ronald Rousseau, Xiaoyong Yan, Peng Bao, Qian Zhuang
- Thanks to APS and National Science Library CAS for providing data
- Thanks to you all for listening to this all

# PageRank and Input-output eigenvectors

- There is one-one correspondence between eigenvectors of  $B$  and  $MB$

$$r^i = \sum MB_j^i r^j \Rightarrow r^i = \sum \frac{x_j^i}{X^i} r^j$$

$$\Rightarrow X^i r^i = \sum \frac{x_j^i}{X^j} X^j r^j \Rightarrow X^i r^i = \sum B_j^i X^j r^j$$

Thus,

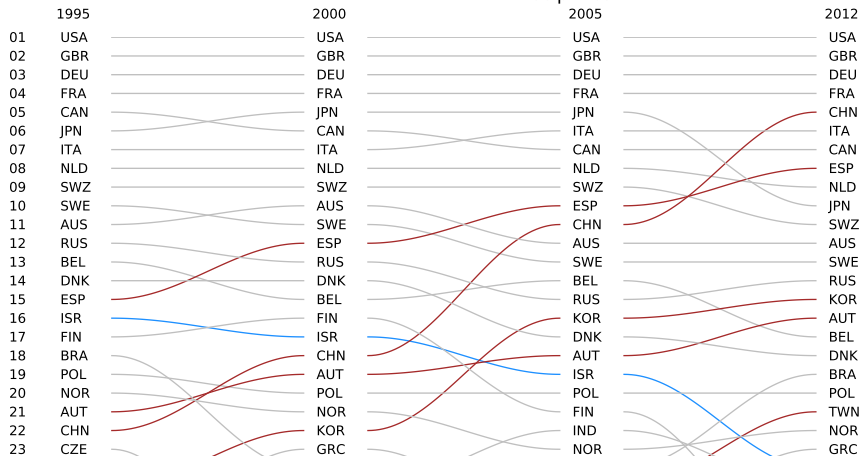
$$|1\rangle_B = X \cdot |1\rangle_{MB}. \quad (6)$$

Similarly for left vector, we have  $\langle 1|_{MB} = X \cdot \langle 1|_B$ .

- In this sense, we unified and extended PageRank and Input-output analysis
- Hypothetically removing one node is a key technique in our work

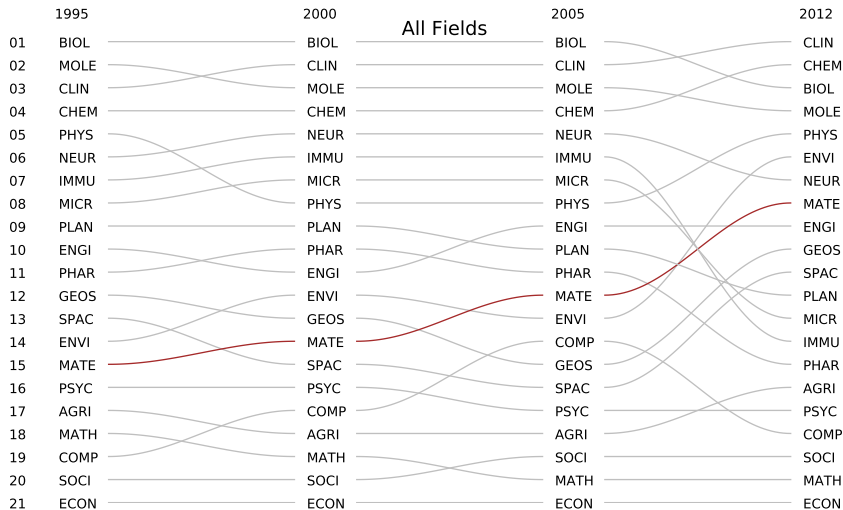
## Additional results on countries and subjects

## All Disciplines





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