

Quantitative Determination of Luminescent Coupling in Multijunction Solar Cells from Spectral Photovoltage Measurements

D. Fuertes Marrón,^{*} E. Barrigón,[†] M. Ochoa, and I. Artacho

*Instituto de Energía Solar, Universidad Politécnica de Madrid, ETSI Telecomunicación,
Ciudad Universitaria s/n, 28040 Madrid, Spain*

(Received 8 April 2016; revised manuscript received 15 April 2016)

We present a simple method to quantify the magnitude of luminescent coupling (LC) between stacked subcells in multijunction photovoltaic devices. The effect of luminescence produced at high-band-gap subcells on underlying low-gap units within the same device can be directly accessed as a measurable open-circuit voltage difference by comparing two photovoltage spectra. Additionally, our study unambiguously identifies LC as the modulation mechanism across multijunction solar cells generating a response from buried subcells in photoreflectance measurements.

DOI:

I. INTRODUCTION

Multijunction solar cells (MJSCs) based on III-V semiconductors are currently the most efficient devices for photovoltaic energy conversion [1]. Despite its technological complexity, monolithic integration is the standard procedure in the design of these devices, by which subcells based on semiconductors of different energy band gaps are electrically connected in series with tunnel junctions, by piling up a multilayer structure. The resulting two-terminal devices are convenient for subsequent electrical connection and module processing but complicate the characterization and quality assessment of specific parts or individual junctions within the device. Nonetheless, current-voltage (J - V) characteristics, quantum efficiency (QE), and electro- or photoluminescence are routinely used in MJSC characterization, providing useful information of the optoelectronic properties of the subcells [2,3]. Monolithic integration imposes, in addition, characteristic constraints on the operation of devices, particularly concerning current matching between subcells under a given spectrum, in order to optimize its performance. Such constraints, affecting a large number of layers in the structure, translate into a tight set of growth and material parameters. Ideally, the grower would count with a bunch of characterization techniques that would permit independent assessment of each part of the device; however, such parameters are very often interrelated, affecting other parts in the device and complicating any separated diagnostics attempted.

One subtle difficulty in the optimization and characterization of subcells for current matching is luminescent coupling (LC): Band-to-band radiative recombination events at top cells generate light that can be reabsorbed

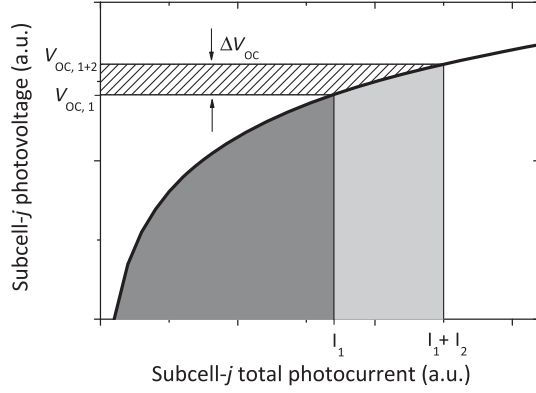
at underlying lower-gap subcells and effectively contribute to the photocurrent. This additional photocurrent must be thus accounted for when designing high-efficiency devices, as to ensure operation as close as possible to current matching. As LC depends on the actual operation point of top cells, no single solution in the form of a closed set of parameters is expected as to ensure optimal performance under arbitrary illumination conditions. Still, the availability of a simple and reliable diagnostics tool capable of quantifying the magnitude of LC and the associated increase of photocurrent resulting from it is of high value. The implications of LC in the characterization, operation, and optimization of MJSCs are currently a matter of active research [4–8]. In what follows, we propose a simple method of quantifying LC as a measurable photovoltage generated at low-gap subcells. This approach has two distinct advantages: It (i) can easily be implemented in current setups for standard MJSC characterization and (ii) provides direct access to the magnitude of quasi-Fermi level splitting of subcells operating under LC effects, from which the optoelectronic response can be predicted.

II. THEORETICAL BACKGROUND

The proposed method is based on the measurement of the photovoltage generated in the device under two different pump-and-probe illumination sources. From Shockley's diode equation, the open-circuit voltage can be expressed as a function of the photogenerated currents. For multijunction devices, the overall open-circuit voltage expression, considering a single-diode model for each subcell, will include the summation of as many diode terms as junctions forming the device. Each diode term consists of a log factor, containing the currents, multiplied by a prefactor, the product of the corresponding diode ideality factor n and the thermal voltage kT/q . For example, the photovoltage of a two-junction solar cell can be expressed as

^{*}dfuertes@ies-def.upm.es

[†]Present address: Division of Solid State Physics-Nano Lund, Lund University, SE-22100 Lund, Sweden.



F1:1 FIG. 1. Logarithmic dependency of photovoltage upon photo-
 F1:2 generated current in the j subcell under two illumination sources
 F1:3 generating currents I_1 and I_2 , respectively. The increase in overall
 F1:4 photovoltage results from current summation inside the log term.

$$V_{OC} = \frac{n^{TC} kT}{q} \ln \left(\frac{\sum_{\alpha} I_{\alpha}^{TC}(\lambda)}{I_0^{TC}} + 1 \right) + \frac{n^{BC} kT}{q} \ln \left(\frac{\sum_{\beta} I_{\beta}^{BC}(\lambda)}{I_0^{BC}} + 1 \right), \quad (1)$$

80 where the first and second term on the right correspond to the
 81 top (TC) and bottom cell (BC), respectively, and α and β
 82 indicate different current contributions at each diode junction
 83 stemming from different light sources. In what follows,
 84 we consider the case $I_{\alpha,\beta} \gg I_0$ and neglect the $+1$ terms in
 85 the logarithms.

86 The effect of more than a single illumination source
 87 inducing photogeneration on the photovoltage of a given
 88 subcell is illustrated in Fig. 1. The curve represents the
 89 logarithmic dependence of the output voltage on the
 90 photocurrent I_1 . Adding a second light source contributing
 91 I_2 increases V_{OC} to a magnitude proportional to the
 92 logarithm of the sum of the currents $I_1 + I_2$. The magnitude
 93 ΔV_{OC} thus corresponds to the additional contribution
 94 generated by I_2 . It will be shown that under certain
 95 illumination conditions such an increase in the recorded
 96 open-circuit voltage can be unambiguously ascribed to the
 97 effect of luminescent coupling between subcells in multi-
 98 junction devices, thereby providing a simple way to
 99 estimate its magnitude.

100 III. EXPERIMENT

101 Simultaneous photovoltage and photoreflectance (PR)
 102 measurements are performed on a (Ga, In)P/GaAs tandem
 103 solar cell grown by MOVPE. The application of spectral
 104 photovoltage measurements to single-junction solar cells
 105 and its relationship to the spectral response of the short-
 106 circuit current is discussed by Mackel and Cuevas [9],
 107 although our scope and method are different in this work.
 108 Additionally, PR is used in this work as a complementary
 109 technique, supporting our main conclusions drawn from

photovoltage measurements, as explained later on. PR 110
 belongs to the family of modulation spectroscopies [10], 111
 which consist of the measurement of small changes in the 112
 optical properties of the samples under study driven by 113
 applied perturbations, like electric fields, strain, or temper- 114
 ature gradients. In PR, such perturbations are induced by 115
 means of carrier photogeneration by a pump beam of 116
 sufficient photon energy. The photogenerated excess carriers 117
 diffuse and screen electric fields already present at 118
 space-charge regions within the semiconductor, inducing 119
 small changes in the dielectric constant of the material that 120
 are in turn recorded by means of a probe light beam as 121
 slight changes in the reflectance of the specimen. 122

The sample structure under study is shown schematically 123
 in Table I, and further details on the growth method can be 124
 found in Ref. [11]. The sample is provided with a Ni pad on 125
 the front side to permit electrical contact, and In is used to fix 126
 the sample back surface onto a Cu-disk holder. The 127
 estimated efficiency of the device is 25% under one-sun 128
 illumination, based on QE results and accounting for the 129
 lack of a front metal grid and antireflection coating (in order 130
 to facilitate PR measurements), as well as a larger effective 131
 area (approximately 0.25 cm²) as compared to 1-mm² 132
 standard devices. Metal tips on the front and rear contacts 133
 are used connected to a voltmeter to record the spectral 134
 photovoltage during the measurements. Sharma and Hosea 135
 [12] report on photovoltage results obtained using contact 136
 and contactless measurements, and we use a similar setup in 137
 this work. The photovoltage V_{OC} reading is fed to an analog- 138
 to-digital converter and incorporated to the data-acquisition 139
 control during PR scans. Measurements are carried out 140
 illuminating the front side of the sample simultaneously with 141
 two light sources: the 325-nm line of a 15-mW HeCd laser 142

TABLE I. Layer structure of the (Ga, In)P/GaAs tandem solar cell including nominal layer thickness and fundamental band gap (ind., indirect).

		Thickness	
		(nm)	E_g (eV)
Top cell	(Al,In)P:Si (window)	25	2.36 (ind.)
	(Ga,In)P:Si (emitter)	140	1.84
	(Ga,In)P:Zn (base)	730	1.84
	(Al,Ga,In)P:Zn (BSF)	70	2.13
Tunnel junction	(Al,Ga)As:C	64	2.05
	(Al,Ga)As:C	28	2.00
	GaAs:Te	15	1.39
	(Al,Ga)As:Si	30	2.05
Bottom cell	(Al,Ga)As:Si (window)	32	2.05
	GaAs:Si (emitter)	80	1.42
	GaAs:Zn (base)	3600	1.42
	(Al,Ga)As:C (BSF)	165	1.95
Buffer	GaAs	1000	1.42
Substrate	GaAs (1 0 0)		1.42

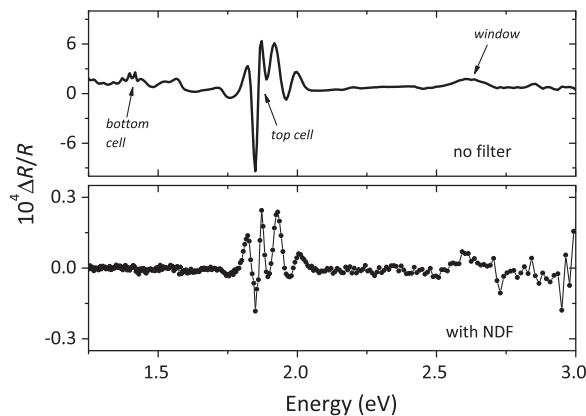
143 mechanically chopped at 777 Hz (hereafter, pump) and a
 144 monochromatized beam from a 150-W quartz-halogen-tung-
 145 sten (QTH) lamp (hereafter, probe). Direct reflectance of the
 146 probe beam containing average (dc) and modulated (ac)
 147 components is detected with a Si photodiode connected to a
 148 preamp and a lock-in amplifier. The PR signal is defined as the
 149 spectral ac/dc ratio. In all measurements, 2-nm step sweeps
 150 **6** are used for the probe beam. A description of the setup and
 151 further references on the technique can be found in Ref. [13].

152 **IV. RESULTS**

153 **A. Photoreflectance**

154 The calculated absorption profile of the 325-nm pump
 155 light under normal incidence across the first layers of the
 156 cell structure reveals that about 20% of the incoming light
 157 intensity is transmitted across the (Al,In)P window layer.
 158 Further absorption at the (Ga,In)P emitter of the TC reduces
 159 the light intensity reaching the top-cell *p-n* junction to
 160 about 0.001%. The following 730-nm-thick (Ga,In)P-base
 161 region virtually ensures that no pump light is transmitted to
 162 deeper layers in the structure.

163 **7** Despite full absorption of pump light occurring at the top
 164 cell, the PR spectrum shown in the top panel in Fig. 2
 165 reveals that 325-nm light pump is actually able to modulate
 166 the whole device structure, with neat signatures attributed
 167 to the top window, TC, and BC going from high to low
 168 energies. Notice that PR is sensitive to direct transitions
 169 only, and consequently the signature attributed to the
 170 (Al,In)P window at 2.62 eV corresponds to its direct
 171 gap. The lower panel in Fig. 2 shows a second PR spectrum
 172 obtained under identical conditions but including a variable
 173 neutral-density filter (NDF) attenuating the laser pump
 174 beam. The pump intensity is in this case lowered down to a
 175 level at which the bottom-cell signatures lie below the noise
 176 level (mind the reduction in the amplitude of signatures
 177 in the top-cell range by about one order of magnitude).
 178 These two PR spectra are later associated with the existence
 179 and absence of a measurable LC in the device.

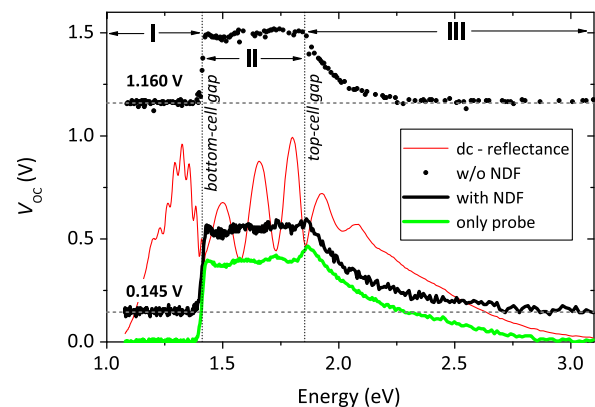


F2:1 FIG. 2. PR spectra of the (Ga,In)P/GaAs tandem solar cell
 F2:2 using a 325-nm laser line without NDF (upper) and with NDF
 F2:3 (lower).

B. Spectral photovoltage

180 Figure 3 shows the spectral photovoltage V_{OC} recorded
 181 simultaneously during PR measurements shown in Fig. 2,
 182 together with the corresponding dc reflectance (as
 183 recorded, in volts). Three V_{OC} spectra are shown: (i) using
 184 an (unfiltered) pump and probe (dots), with PR revealing a
 185 bottom-cell signature; (ii) using a (filtered) pump and
 186 probe, such that the PR response from bottom cell lies
 187 below noise level (black line); and (iii) a third spectrum
 188 using the probe beam only (thus PR silent), with the pump
 189 laser turned off (light line).
 190

191 The band gaps of TC and BC (vertical dotted lines)
 192 divide the energy spectrum into three regions labeled
 193 I, II, and III in Fig. 3. Region I corresponds to the
 194 transparency region of the device ($E < 1.42$ eV); region
 195 II corresponds to the absorption range of the BC only
 196 (1.42 eV $< E < 1.84$ eV); and region III also includes the
 197 absorption of light at the TC ($E > 1.84$ eV). From Fig. 3, it
 198 can be observed that V_{OC} from the probe beam alone at
 199 energies below the BC band gap at 1.42 eV (region I) is
 200 zero, in agreement with no photogeneration occurring
 201 within the device. The same applies at the high-energy
 202 end of the spectrum in region III due to the decaying
 203 spectral content of the QTH lamp. The contribution to V_{OC}
 204 generated by the probe beam is clearly resolved for energies
 205 within region II. The absorption range of the BC is
 206 characterized by a fairly constant photovoltage with a
 207 superimposed Fabry-Perot oscillation (the anticorrelation
 208 V_{OC} maximum and dc-reflectance minimum confirms the
 209 interferometric origin of the rippling). The inflection point
 210 from which the photovoltage enters in region III and decays
 211 monotonically with increasing energy corresponds to the
 212 absorption threshold of the TC at 1.84 eV, in agreement
 213 with the corresponding PR signature in Fig. 2. Above this
 214 energy, the photovoltage generated by the probe beam



F3:1 FIG. 3. Photovoltage recorded during PR spectra: under full
 F3:2 pump intensity (no NDF, dots); under filtered pump intensity
 F3:3 (with NDF, black line); and with the laser off (only probe, green
 F3:4 line). dc reflectance is also shown (thin red line). Regions I, II,
 F3:5 and III correspond to the transparency region, absorption range of
 F3:6 BC alone, and joint absorption at TC and BC, respectively.

includes contributions from both top and bottom subcells, the latter resulting from incomplete absorption at TC.

V_{OC} spectra obtained under the pump and probe with and without NDF appear shifted by 0.145 and 1.160 V, respectively, in comparison to the case of the probe beam alone in the transparency and high-energy regions. Such values correspond to the photovoltage generated by a 325-nm laser line in the device for the two different laser-beam intensities, which according to previous calculations is fully absorbed in the TC in every case. The contribution to V_{OC} from the pump beam has two components: (i) direct photogeneration at TC, where the beam is fully absorbed, and (ii) eventual coupled photogeneration at BC stemming from TC luminescence (LC). We shall rewrite Eq. (1) for V_{OC} in region III as

$$V_{OC}^{III,p\&p} = \frac{n^{TC}kT}{q} \ln \left(\frac{x \times I_{pump} + I_{probe}^{TC}(\lambda)}{I_0^{TC}} \right) + \frac{n^{BC}kT}{q} \ln \left(\frac{I_{probe}^{BC}(\lambda) + I^{LC}}{I_0^{BC}} \right). \quad (2)$$

As explained before, the expression includes one log term per cell with the corresponding prefactor and different current contributions at each subcell from the various active light sources. The wavelength dependency of the probe-based photogenerated current is specifically maintained in the expression reflecting the varying spectral content of the QTH lamp, in contrast to the wavelength-independent contribution from the pump. The effect of pump-beam photogeneration at the TC is included in the first, TC-related log term (expressed as $x \times I_{pump}$, where x accounts for different pump intensities). The eventual activation of LC is also included via I^{LC} in the BC log term. Notice the presence of probe-beam photogenerated currents in both log terms accounting for wavelength-dependent partial transparency of the TC within its absorption range.

A similar expression can also be given for V_{OC} in transparency region I. For the case of the probe beam alone, the result is trivial with $I_{probe} = 0$. For pump-and-probe spectra,

$$V_{OC}^{I,p\&p} = \frac{n^{TC}kT}{q} \ln \left(\frac{x \times I_{pump} + 0}{I_0^{TC}} \right) + \frac{n^{BC}kT}{q} \ln \left(\frac{0 + I^{LC}}{I_0^{BC}} \right), \quad (3)$$

the major difference with respect to the previous expression for region III being the absence of probe-beam photogenerated currents for $E < 1.42$ eV. The latter expression confirms the origin of V_{OC} in transparency region I stemming from pump-beam photogeneration and allows the distinction of its two contributions: direct photogeneration at TC and related coupled luminescence generating at the BC. It is, in principle, possible to adjust the intensity of the pump beam (reducing the factor x in the previous

expression) as to effectively make LC negligible. Should this be the case, V_{OC} in transparency region I recorded in pump-and-probe spectra would be originated solely at the TC by direct photogeneration of the pump beam [the last term of Eq. (3) drops off]. Indeed, this is the case of the pump-and-probe measurement performed with NDF.

To demonstrate this, Fig. 4 shows the same plot as Fig. 3 with both pump-and-probe spectra shifted down by the respective V_{OC} readings in the transparency range (labeled as V_{OC}^I). All three spectra appear now zeroed in the transparency region. Almost perfect overlapping between spectra corresponding to the cases of pump and probe with NDF and just the probe beam can be observed up to the energy corresponding to the TC band gap at 1.84 eV. With V_{OC}^I zeroed, the device response in this energy range is solely controlled by the BC. According to the observations made for Eq. (3), the magnitude of V_{OC}^I in the spectrum with NDF in Fig. 3 corresponds solely to the photovoltage generated at the TC by the pump beam, with no additional contribution due to LC at the BC. The overlapping spectra also rule out eventual LC activation by the probe beam alone across the absorption range of the top cell. It is also recalled that no PR signature from the bottom cell could be detected in this measurement, in agreement with the absence of any measurable LC.

However, an offset of some 67 mV in V_{OC} is found within the absorption range of the BC for the case of pump-and-probe measurement at full laser intensity (no filter in Fig. 4). Should V_{OC}^I correspond to the contribution from the TC alone under the action of the pump beam, the photovoltage spectrum under full laser intensity should overlap the photovoltage developed under the probe beam alone, as in the case with NDF. It is then concluded that the offset detected in the photovoltage spectrum of the pump and probe without NDF (after zeroing V_{OC}^I) relative to the probe beam alone corresponds indeed to a contribution to the photovoltage originated at the bottom cell upon the action of the laser beam and, consequently, is not spectrally sensitive. In other words, the last term in Eq. (3) does

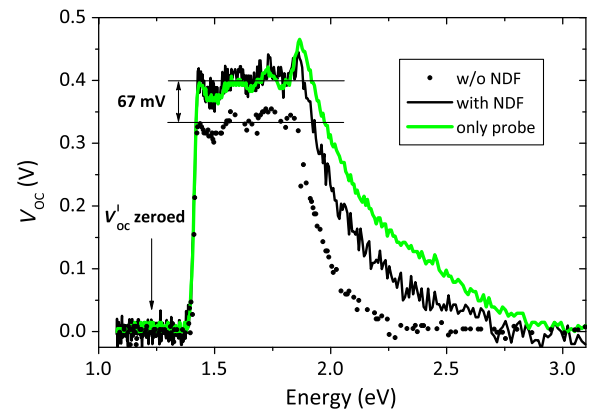


FIG. 4. The same photovoltages from Fig. 3, zeroed to the value in the transparency region, V_{OC}^I .

298 not vanish if LC is active. Such an offset, well above the
 299 noise level of V_{OC} spectra, is thus a direct measurement of
 300 the BC contribution to V_{OC} stemming from LC.

301 We can estimate the relative luminescence intensity
 302 responsible for BC response under LC in region II. The
 303 analytic expression of the zeroing procedure as applied to
 304 the spectrum under pump-and-probe illumination without
 305 NDF can be written as

$$V_{OC}^{II,p\&p} - V_{OC}^{I,p\&p} = \frac{n^{BC}kT}{q} \ln \left(\frac{I_{probe}^{BC}(\lambda)}{I^{LC}} + 1 \right). \quad (4)$$

306 Notice that $V_{OC}^{II,p\&p}$ is similar to Eq. (2) with $I_{probe}^{TC}(\lambda) = 0$,
 307 that $V_{OC}^{I,p\&p}$ is given by Eq. (3), and that the resulting +1
 308 term is not necessarily negligible now. The recorded
 309 photovoltage offset of approximately 67 mV corresponds,
 310 as indicated in Fig. 4, to the difference between $V_{OC}^{II,probe}$ and
 311 Eq. (4), namely,
 312

$$V_{OC}^{II,probe} - (V_{OC}^{II,p\&p} - V_{OC}^{I,p\&p}) = \frac{n^{BC}kT}{q} \ln \left(\frac{I_{probe}^{BC}(\lambda)}{I_0^{BC}} \right) - \frac{n^{BC}kT}{q} \ln \left(\frac{I_{probe}^{BC}(\lambda)}{I^{LC}} + 1 \right). \quad (5)$$

313 The first term on the right (probe spectrum in region II) is
 314 nearly constant except for the interference rippling and
 315 equal to 0.4 V. Inverting the expression, we estimate a
 316 relative value of $I_{probe}^{BC}(\lambda) \approx 4.3 \times 10^4 \times I^{LC}$, assuming
 317 26-mV thermal voltage and $n = 1.2$ for the BC [14].
 318 Referring back to Sec. II, Eq. (5) corresponds to the
 319 magnitude ΔV_{OC} of Fig. 1, from which the relative
 320 magnitudes of $I_{probe}^{BC}(\lambda)$ and I^{LC} are deduced (to be
 321 identified with I_1 and I_2 in the figure).
 322

323 Differences are observed in V_{OC} spectra in region III,
 324 above the top-cell band gap. The nonoverlapping nature of
 325 zeroed spectra in region III can be expected from the
 326 varying ratios of pump-and-probe photogeneration at the
 327 top cell (adding logarithmically to V_{OC}), plus the increasing
 328 contribution of the bottom cell excited by the probe beam,
 329 from the expressions before. Considering the pair of spectra
 330 probe alone and filtered pump and probe (setting $x = 1$ for
 331 convenience), its difference in region III of the zeroed plot
 332 in Fig. 4 corresponds to

$$V_{OC}^{III,NDF} - V_{OC}^{III,probe} - V_{OC}^{I,NDF} = \frac{n^{TC}kT}{q} \ln \left(1 + \frac{I_{pump}^{TC}}{I_{probe}^{TC}(\lambda)} \right) - 0.145 \quad (6)$$

333 with $V_{OC}^{I,NDF} = 0.145$ V. The wavelength dependency of
 334 $I_{probe}(\lambda)$ and thus of the ratio $I_{pump}/I_{probe}(\lambda)$ in the log term
 335 explains the different curvatures observed in V_{OC} spectra in
 336 region III.

C. Effect of luminescent coupling on photoreflectance

337
 338
 339 Finally, we turn now back to the PR spectrum in Fig. 2
 340 (upper panel) under full pump-beam intensity. With direct
 341 evidence of LC operating during the PR measurement, LC
 342 is proposed as the modulation mechanism responsible for
 343 the bottom-cell PR signature. The LC-mediated modulation
 344 mechanism operates right at the same frequency as the
 345 chopper modulating the pump beam. The probe beam, in
 346 turn, measures changes in reflectance induced by the
 347 absorption of light that has been generated at other parts
 348 within the structure. We propose that this sort of cascade
 349 process, by which light emitted by high-gap materials
 350 excites deeper layers of lower band gaps, effectively
 351 transmits modulation into the structure far beyond the
 352 penetration depth of the pump beam. Furthermore, it is
 353 concluded that the absolute distance upon which effective
 354 modulation can be transmitted in PR measurements of
 355 multilayer semiconductor structures is not necessarily
 356 limited by the diffusion length of photogenerated minority
 357 carriers [15,16]. As an example, optically transmitted
 358 modulation by LC satisfactorily describes the propagation
 359 of the perturbation across layers expected to block diffusive
 360 transport of minority carriers, like the case of tunnel
 361 junctions between subcells in open-circuit conditions
 362 [17]. The results of Fig. 2 support this conclusion: PR
 363 spectra in which LC was selectively activated do show the
 364 signature of a buried junction, whereas the same signature
 365 becomes PR silent in the absence of LC.

V. CONCLUSION

366
 367 We provide evidence of the impact of LC in spectral
 368 photovoltage measurements performed on MJSCs, deriving
 369 thereof a simple method to quantify the magnitude of LC as
 370 a measurable photovoltage difference. The quantification of
 371 LC by means of spectral photovoltage does not require the
 372 realization of simultaneous PR measurements; it can rather
 373 be performed separately or in combination with alternative
 374 characterization measurements like, e.g., QE. Nevertheless,
 375 we show that the activation of PR signatures from deep
 376 layers as a function of the pump-beam intensity can act as a
 377 fair indicator of LC action.

ACKNOWLEDGMENTS

378
 379 Financial support from Comunidad de Madrid (MADRID
 380 PV, S2013/MAE-2780) is gratefully acknowledged.

-
- 381
 382 [1] M. A. Green, K. Emery, Y. Hishikawa, W. Warta, and E. D.
 383 Dunlop, Solar cell efficiency tables v. 47, *Prog. Photo-*
 384 *voltatics* **24**, 3 (2016).
 385 [2] M. A. Steiner, J. F. Geisz, T. E. Moriarty, R. M. France,
 386 W. E. McMahon, J. M. Olson, S. R. Kurtz, and D. J.
 387 Friedman, Measuring I-V curves and subcell photocurrents
 388

- 389 in the presence of luminescent coupling, *IEEE J. Photo-*
390 *voltatics* **3**, 879 (2013).
- 391 [3] T. Kirchartz, U. Rau, M. Hermle, A. W. Bett, A. Helbig, and
392 J. H. Werner, Internal voltages in GaInP/GaInAs/Ge multi-
393 junction solar cells determined by electroluminescence
394 measurements, *Appl. Phys. Lett.* **92**, 123502 (2008).
- 395 [4] D. Friedman, J. Geisz, and M. Steiner, Analysis of multi-
396 junction solar cell current-voltage characteristics in the
397 presence of luminescent coupling, *IEEE J. Photovoltaics*
398 **3**, 1429 (2013).
- 399 [5] C. Baur, M. Hermle, F. Dimroth, and A. W. Bett, Effects of
400 optical coupling in III-V multilayer systems, *Appl. Phys.*
401 *Lett.* **90**, 192109 (2007).
- 402 [6] S. H. Lim, J. J. Li, E. H. Steenbergen, and Y. H. Zhang,
403 Luminescence coupling effects on multijunction solar cell
404 external quantum efficiency measurement, *Prog. Photo-*
405 *voltatics* **21**, 344 (2013).
- 406 [7] M. Z. Shvarts, M. A. Mintairov, V. M. Emelyanov, V. V.
407 Evstropov, and V. M. Lantratov, Method for direct mea-
408 surements of luminescent coupling efficiency in concen-
409 trator MJ-SCs, *AIP Conf. Proc.* **1556**, 147 (2013).
- 410 [8] M. A. Steiner and J. F. Geisz, Non-linear luminescent
411 coupling in series-connected multijunction solar cells, *Appl.*
412 *Phys. Lett.* **100**, 251106 (2012).
- 413 [9] H. Mackel and A. Cuevas, The spectral response of the
414 open-circuit voltage: a new characterization tool for solar
415 cells, *Sol. Energy Mater. Sol. Cells* **81**, 225 (2004).
- 416 [10] M. Cardona, *Modulation Spectroscopy* (Academic,
417 New York, 1969).
- [11] I. García, I. Rey-Stolle, B. Galiana, and C. Algora, A 32.6%
418 efficient lattice-matched dual-junction solar cell working at
419 1000 suns, *Appl. Phys. Lett.* **94**, 053509 (2009). 420
- [12] T. Sharma and T. Hosea, A method of obtaining simulta-
421 neous complementary spectroscopic information on self-
422 assembled quantum dots, *Jpn. J. Appl. Phys.* **48**, 082301
423 (2009). 424
- [13] D. Fuertes Marrón, E. Cánovas, I. Artacho, C. R. Stanley,
425 M. Steer, T. Kaizu, Y. Shoji, N. Ahsan, Y. Okada, E.
426 Barrigón, I. Rey-Stolle, C. Algora, A. Martí, and A. Luque,
427 Application of photoreflectance to advanced multilayer
428 structures for photovoltaics, *Mater. Sci. Eng. B* **178**, 599
429 (2013). 430
- [14] P. Espinet, I. Rey-Stolle, and C. Algora, Advanced charac-
431 terization of multijunction solar cells with electrolumines-
432 cence, in *2009 Spanish Conference on Electron Devices*,
433 (IEEE Conference Publications, 2009), p. 390. 434
- [15] M. Motyka, R. Kudrawiec, and J. Misiewicz, On the
435 deepness of contactless electroreflectance probing in semi-
436 conductor structures, *Phys. Status Solidi (a)* **204**, 354
437 (2007). 438
- [16] Y. Mochizuki, T. Ishii, and M. Mizuta, Role of minority-
439 carrier diffusion in photoreflectance measurements
440 of epitaxial GaAs wafers, *Jpn. J. Appl. Phys.* **34**, 6106
441 (1995). 442
- [17] E. Cánovas, D. F. Marrón, A. Martí, A. Luque, A. W. Bett, F.
443 Dimroth, and S. P. Philipps, Photoreflectance analysis of a
444 GaInP/GaInAs/Ge multijunction solar cell, *Appl. Phys.*
445 *Lett.* **97**, 203504 (2010). 446
447