

LIGHT-PRESSURE EFFECTS ON ION SPECTRA  
IN TWO-ION LASER PLASMAS

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In plasmas produced by high-power lasers, the electron temperature  $T_e$  may be so high that the ion temperature trail well behind (slow relaxation), and  $T_e$  be spatially uniform (large heat conductivity). Then a simple, often used, model, having initially  $n=N_0$  ( $x < 0$ ),  $n=0$  ( $x > 0$ ), involves ion continuity, and ion and electron momentum equations

$$\frac{Dn}{Dt} + n \frac{\partial v}{\partial x} = 0, \quad \frac{D}{Dt} = \frac{\partial}{\partial t} + v \frac{\partial}{\partial x}, \quad (1)$$

$$m \frac{Dv}{Dt} = neZE, \quad 0 = -\frac{\partial P}{\partial x} - n_e e E \quad (2)$$

where  $n, v, m, Z$  refer to ions,  $E$  is the charge separation field, and we take  $n_e = Zn$ . If electrons are Maxwellian ( $P_e = n_e k T_e$ ), and  $T_e = \text{const}$ , we obtain

$$\frac{d \ln n}{dn} = -\frac{1}{M} \left( 1 + \frac{dM}{dn} \right), \quad (M^2 - 1) \left( 1 + \frac{dM}{dn} \right) = 0, \quad (3)$$

where  $M = v/c_s$ ,  $M = v/c_s$  and  $c_s^2 = kT_e/m$ . Solutions to (3) are  $dM/dn = -1$  ( $v = \text{const}$ ,  $n = \text{const}$ ) and  $M = 1$ . The solution then is

$$M = 1 \quad (v = c_s + x/t), \quad n = n_0 \exp(-v/c_s), \quad \text{for } n > -1$$

(isothermal rarefaction wave) [1]. The number of ions in the interval  $v, v + \Delta v$  is  $\Delta N = n \Delta x = n \Delta v$ , and the ion velocity spectrum is then

$$\frac{dN}{dv} = C \frac{n}{dv/dn} = \frac{n}{1 + dM/dn} \quad (C = \text{const}); \quad (4)$$

here,

$$\frac{dN}{dv} = \exp(-v/c_s),$$

a well known result [1].

In some experiments, where two species with different  $Z/m$  ratio ( $H^+$ ,  $C^{6+}$  in Ref. 1) are involved,  $dN/dv$  for that one with larger  $Z/m$  presents a large peak superposed to the exponential decay law. It may be shown that using a two-temperature electron population (which explains the shape of the current registered by a remote collector in certain cases [2]), does not lead to a peak in  $dN/dv$ , as required. On the other hand, it is clear from (4) that if a spatial region exists where  $v = \text{const} = v_0$ ,  $dN/dv$  will present a peak around  $v_0$ . In this respect it should be noted that Gurevich et al. [3] claimed that when two species 1, 2 exist, where  $Z_1/m_1 > Z_2/m_2$  say,  $n_2$  vanishes at some point and a plateau ( $n_1 = \text{const}$ ) appears, where  $v_1 = \text{const}$ . Let us consider the two-species case; the continuity equations read

$$\frac{d \ln n_j}{dn} = -\frac{1}{M_j} \left( 1 + \frac{dM_j}{dn} \right), \quad (j=1,2) \quad (5)$$

while the momentum equations (using  $n_e = \sum n_j Z_j$ ) additionally yield

$$\frac{M_j}{c_s^2} \left( 1 + \frac{dM_j}{dn} \right) = \frac{M_1}{c_s^2} \left( 1 + \frac{dM_1}{dn} \right), \quad (6)$$

$$\sum \frac{Z_j n_j}{M_j} \left( 1 + \frac{dM_j}{dn} \right) \left( \frac{M_j^2}{c_s^2} - 1 \right) = 0 \quad (7)$$

where  $c_s^2 = c_j^2/c_s^2$ ,  $c_j^2 = Z_j k T_e / m_j$ . Unless  $d \ln n_j / dn = 1 + dM_j / dn = 0$ , from (6) and (7) there results [3]

$$\sum n_j Z_j \left( \frac{M_j^2}{c_s^2} - 1 \right) = 0. \quad (8)$$

From (5), (6) and (8) we finally get

$$\frac{dM_2}{dn} \frac{M_2 (c_1^2 M_2 - c_2^2 M_1) (M_1^2 - 3c_1^2) + c_2^2 M_1 (M_1 - M_2) (M_1^2 - c_1^2)}{M_1 (c_2^2 M_1 - c_1^2 M_2) (M_2^2 - 3c_2^2) + c_1^2 M_2 (M_1 - M_2) (M_2^2 - c_2^2)} = \frac{M_2^2 - c_2^2}{M_1^2 - c_1^2} \quad (9)$$

The figure shows the singular points E (degenerated node), S (saddle) and N (node) of Eq. (9) in the nonshaded regions where the solution must remain [see Eq. (8)]; making the disturbance front to occur at  $n = -1$ , we have there  $M_j = 1$ , and from (8),  $c_s^2 = k T_e (\sum Z_j n_{j0} Z_j / m_j) (\sum Z_j n_{j0})^{-1}$ . The solution to (9) starts at point I, crosses E, turns around [near S for  $Z_2 n_{20} \gg Z_1 n_{10}$ ], and finally reaches N, where

$$M_1 = (v/c_1 - x/c_1 t) c_1 / c_s = c_1 \approx c_1 / c_s,$$

and, from (8),  $n_2 = 0$  (at some point  $n_N$ ). Since 1 is the only species from

there on, no plateau appears [see the discussion following (3)] (in opposition to [3]), the solution being of the type

$$v_1 = c_1 + x/t, \quad n_1 = n_1(n_N) \exp[(v_1(n_N) - v_1)/c_1], \quad \text{for } n > n_N.$$

Gurevich et al. [4] claimed that a nearly-flat range observed in experimental ion spectra provide support for the  $n$ -profile plateau predicted in [3]; as pointed out above however, a plateau leads, contrarily, to a peak in  $dN/dv$ .

It appears that light-pressure is the cause of the peak in Ref. 1. When the light-to-thermal pressure ratio is not small ( $\sim 3$  in Ref. 1), a plateau develops in the overdense region of a one-species plasma with  $T_e = \text{const}$ , in order to satisfy some appropriate conditions in the thin layer around critical density [5]; if  $T_e$  grows slowly with time, a near-plateau develops leading to a peak in  $dN/dv$ . However, the area under that peak is too small:

$$\int_{v > v_0} \frac{dN}{dv} dv = \int C n dn = -C \int d(nM) = -C n M \Big|_{v_0}, \quad (10)$$

where the continuity equation and Eq. (4) have been used; for  $T_e = \text{const}$ , (10) gives  $C n(v_0)$ , which equals an area of width  $\Delta v = c_s$  and height  $dN/dv|_{v_0}$

$$\frac{dN}{dv} \Big|_{v_0} \times \Delta v = C n \frac{dv}{dn} \Big|_{v_0} \times c_s = C n(v_0)$$

much less than that observed. Moreover the above discussion makes no distinction between plasmas with ions of equal ( $D^+$ ,  $C^{6+}$  in Ref. 1) and different ( $H^+$ ,  $C^{6+}$ ) values of  $Z/m$ , whereas results for  $D^+$  in Ref 1 show no peak comparable to that for  $H^+$ . [The reasoning around Eq. (10) also shows that finite Debye effects [1] cannot explain the large peak in  $dN/dv$  for  $H^+$ ].

Nonetheless, consider light-pressure for one species, when  $T_e$  decreases with time; then an isothermal shock appears, to adjust the plasma to conditions in the critical layer [5], carrying the flow from values ahead  $n_a, v_a$  (supersonic) to  $n_b > n_a, v_b$  (subsonic)  $< v_a$ . Clearly, a large peak in  $dN/dv$  will appear around  $v_b$ . Now, for two species with different  $Z/m$  ratio, and  $T_e = \text{const}$  (or even slowly increasing), the dominant, lowest  $Z/m$ , species will be supersonic in a broad flow region ( $M_1 > c_1$  in between points E and N of the figure), and light-pressure will produce a shock

leading again to a peak in  $dN/dv$  for that species. An estimate of the peak area for  $H^+$  in Ref. 1 is in reasonable agreement with the observed data.

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