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## APPLICATION OF THE OPTION PRICING MODEL TO ESTIMATE EXPECTED STOCK RETURNS

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#### ABSTRACT

## APPLICATION OF THE OPTION PRICING MODEL TO ESTIMATE EXPECTED STOCK RETURNS

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This thesis refines and tests an option-based methodology for estimating the expected rate of return on firms' equity, being an approach proposed by Hsia (1991). Hsia's approach is based on an option-theoretic model of the firm, as proposed by Merton (1974) and others. Tests of the Hsia approach are thus joint tests of the Merton model and of the Hsia approach. The Merton model is successfully fitted in its basic form by solving for firm asset volatility and, consistent with prior studies, the implied volatility for firms' assets is found, on average, to be higher than that expected from examining historical equity volatility. The Hsia-based expected excess returns on equity are then estimated and tested in regressions against realised excess stock returns. The Hsia-based expected excess returns are found to be only weakly, positively associated with realised excess returns, and not of statistical significance. When the sample is split in half on the basis of various option-like characteristics (such as higher gearing), the Hsia approach is found to work better for the more option-like sub-sample. This research thus provides some tentative support for the Hsia approach, but does not provide a clear conclusion about its ability to explain the variation in realised excess stock It also provides some ideas and possible directions for further returns. research into applying the Hsia approach.

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Any errors in this thesis are solely the author's responsibility.

# TABLE OF CONTENTS

Ab	stract		••••••		i
Ac	know	ledgn	nent	s	ii
Ta	ble of	Cont	tents	J	iii
Lis	st of F	igure	s		vi
Lis	st of T	ables			vii
Gl	ossary				viii
1	Intro	ducti	ion		1
	1.1	Ba	ckgro	ound	1
	1.2	Re	searc	h Aim	3
	1.3	Ob	jecti	ves	3
	1.4	Re	, searc	h Undertaken	4
	1.5	Re	searc	h Findings	5
	1.6	Str	uctu	re of Thesis	6
2	Liter	ature	Rev	riew – Theoretical Framework	7
-	2.1	Th	e Or	otion-Theoretic View of the Firm	7
	2.2	Ex	tensi	ons of the Option-Theoretic Framework	12
	23	Cr	iticist	m of the Merton Model	14
	24	Us	ing t	he Option Pricing Model to Estimate the Cost of Equity	15
	2.1	41	Real	rranoing the Model	18
3	Liter	ature	Rev	riew – Empirical Tests	20
0	31	En	npirio	cal Tests of the Black-Scholes Ontion Pricing Model	20
	3	1.1	Blac	k and Scholes (1972)	20
	3	.1.2	Gal	ai (1977)	20
	3	.1.3	Mai	Beth and Merville (1979)	21
	3	.1.4	Bha	ttacharya (1980)	22
	3	.1.5	Rub	vinstein (1985)	22
	3	.1.6	May	yhew (1995)	23
	3	.1.7	Sum	mary on Empirical Tests of the Black-Scholes Option Pricing Model	23
	3.2	En	npirio	cal Tests of the Merton Model	24
	3	.2.1	Esti	imation of Credit Spreads	25
		3.2.	.1.1	Jones, Mason and Rosenfeld (1984)	25
		3.2	1.2	Ogden (1987) Socia and Warne (1980)	27
		3.2	1.2	Sarig and Warga (1989) Fons (1994)	30
		3.2	.1.5	Wei and Guo (1997)	31
		3.2	.1.6	Barth, Landsman and Rendleman (1998)	32
		3.2	.1.7	Helwege and Turner (1999)	33
		3.2	.1.8	Anderson and Sundaresan (2000)	34
	3	.2.2	Crea	dit Rating Prediction	35
	2	3.2	.2.1	Irussel (1997)	35
	2	.2.2	3 1	Il Raling Changes Deliandis and Caska (1999)	37
		1.4	1.1	L'UNANIVARIS GIRG (1999)	11

		3.2.4	Ex-dividend Stock Price Behaviour	38
		3.2	.4.1 French, Varson and Moon (1999)	38
		3.2.5	Market Valuation of Bankrupt Firms	39
		3.2	.5.1 Russel, Branch and Torbey (1999)	39
		3.2.6	Bankruptcy Prediction	40
		3.2	.6.1 Charitou and Trigeorgis (2000)	40
		3.2.7	Summary of Tests of the Merton Model	41
	3.3	Er	npirical Tests of the Hsia Approach	43
	3.4	As	set Pricing Benchmarks	43
4	Dat	ta and	Methodology	45
	4.1	Sp	ecifying the Model Parameters	45
		4.1.1	Overview	45
		4.1.2	Company Sample	47
		4.1.3	Market Value of Equity	47
		4.1.4	Market Value of Debt	48
		4.1.5	Firms' Cost of Debt	50
		4.1	.5.1 Credit Rating Based Approach	51
		4.1	.5.2 Calculation of Borrowing Margins	55
		4.1	.5.3 Risk-Free Rate of Return	55
		4.1	.5.4 Review of Borrowing Margins	55
		4.1	5.5 Supplementing the Lehman Brothers Non-investment Grade Bond Indexes	5/
		116	Calculation of Contorate Band Tarm	50
	12	7.7.0 D.	upping the Model	60
	1.2	C.	mining the Woder	61
	4.5		mputing Realised Excess Returns	01
	4.4	De	nchmark Data	62
		4.4.7	Beta Estimation	62
		4.4.2	Market V alue of Equity	63
		4.4.3	Book-to-market Katio	63
	4.5	4.4.4	Effect on Final Sample Selection	64
	4.5	Ci	oss-Sectional Regression Equations	64
		4.5.1	Hsia Approach	64
		4.5.2	Fama-French Three Factor Model	65
		4.5.3	CAPM	66
		4.5.4	Economic versus Statistical Significance	66
-		4.3.5	Ex Ante versus Ex Post Returns	6/
5	Ana	alysis :	and Results	68
	5.1	Fi	tting the Merton Model	68
		5.1.1	Role of the Merton model	68
		5.1.2	Descriptive Statistics – The Sample	68
		5.1.3	Descriptive Statistics – Fitting the Merton Model	70
		5.7	.3.1 Equity Valuation Errors	71
		5.1	.3.2 Relationship Detween Implied and Observed Equity V olatility 5.2 Fitted Asset Volatility	74
		514	Rick Neutral Probability of Default	74
		515	Summary on Fitting the Merton Model	75
	52	Δ.	onlying the Hsia Approach	77
	5.4	521	Descripting Statistics	77
		2.2.1	L'osorightero Statistics	11

iv

	5.2.2	Regression Analysis – Full Sample	79
	5.2.3	Regression Analysis – Split Sample	82
	5.2.4	Regression Analysis – By Calendar Month	89
6 (	Conclusi	92	
0	5.1 Si	ummary	92
	6.1.1	Research Undertaken	92
	6.1.2 Research Findings		93
6	5.2 Li	imitations	94
6	6.3 C	ontribution to the Body of Knowledge	94
6	5.4 Fu	uture Research	95
Bibl	iography	y	
Inde	ex		103
App	endix A.		108
N	Merrill Ly	nch High Yield Master II Index	108

# LIST OF FIGURES

Number	Page
Figure 1 Credit Spreads by Debt Maturity	11
Figure 2 Long-term Debt to Capital	49
Figure 3 Investment Grade Bond Index Spreads	57
Figure 4 Non-investment Grade Bond Index Spreads	58
Figure 5 Merton Model – Equity Valuation Errors	72
Figure 6 Merton Model - Implied/Historical Equity Volatility	73
Figure 7 Merton Model - Risk Neutral Default Probabilities	75
Figure 8 Hsia-based Expected v. Actual Excess Monthly Stock Returns,	
Pooled Data, Low Borrowing Margin	86
Figure 9 Hsia-based Expected v. Actual Excess Monthly Stock Returns,	
Pooled Data, High Borrowing Margin	87

# LIST OF TABLES

Number	Page
Table 1 Credit Rating Definitions	53
Table 2 Descriptive Statistics – Sample	69
Table 3 Descriptive Statistics - Fitted Merton Model	70
Table 4 Descriptive Statistics – Hsia Approach	77
Table 5 Correlation of Credit Rating and Asset Pricing Variables	78
Table 6 Regression Results - Hsia Approach, CAPM and Fama-French	1
Factors	80
Table 7 Criteria for Splitting Sample	82
Table 8 Regression Results - Hsia Approach with Split Sample	83
Table 9 Regression Results - Hsia Approach, Trimmed High Borrowing	5
Margin Sub-sample	88
Table 10 Regression Results - Hsia Approach, by Calendar Month	90

# GLOSSARY

$\boldsymbol{A}$	aggregate annual debt service charges of the firm
В	value of the firm's debt
CAPM	Capital Asset Pricing Model
CBOE	Chicago Board Options Exchange
CBOT	Chicago Board of Trade Options Exchange
d	Merton "quasi" debt-to-firm ratio
D	debt servicing as a percentage of the value of the firm's assets
FRB	US Federal Reserve Board
i	yield on the firm's debt
$k_B$	expected rate of return on the firm's debt
k <sub>s</sub>	expected rate of return on the firm's equity
$k_V$	expected rate of return on the firm's assets
m	borrowing margin
μ	instantaneous rate of return on the firm's assets
MLHYM	Merrill Lynch High Yield Master II corporate bond index
MM	Modigliani and Miller
N(.)	cumulative probability of the standard normal distribution
OPM	Option Pricing Model
r	risk-free rate of interest
$\sigma_s$	standard deviation of rates of return on the firm's equity
$\sigma_V$	standard deviation of rates of return on the firm's assets
S	value of the firm's equity
Т	time to maturity
v	value of the firm's assets
х	face value of the firm's debt, at maturity

### viii