

# <sup>1</sup> **Direct MSTID mitigation in precise GPS** <sup>2</sup> **processing**

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3 In this paper, the authors summarize one simple and efficient approach de-  
4 veloped to mitigate the problem in precise GNSS positioning caused by the  
5 most frequent ionospheric wave signatures: the Medium Scale Travelling Iono-  
6 spheric Disturbances (MSTIDs). The direct GNSS Ionospheric Interferom-  
7 etry technique (hereinafter dGII), presented in this paper, is applied for cor-  
8 recting MSTID effects on precise Real Time Kinematic (RTK) and tropo-  
9 spheric determination. It consists on the evolution of the former climatic Dif-  
10 ferential Delay Mitigation Model for MSTIDs (DMTID), for real-time con-  
11 ditions, using ionospheric data from a single permanent receiver only. The  
12 performance is demonstrated with networks of GNSS receivers in Poland,  
13 treated as users under real-time conditions, during two representative days  
14 in winter and summer seasons (days 353 and 168 of year 2013). In range do-  
15 main, dGII typically reduces the ionospheric delay error up to 10-90%. The  
16 main dGII impact on precise positioning is that we can obtain reliable RTK  
17 position faster. In particular the ASR (ambiguity success rate) parameter  
18 increases, from 74% to 83%, with respect to the original uncorrected obser-  
19 vations. The average of time to first fix is shortened from 30s to 13s.. The  
20 improvement in troposphere domain was most difficult to demonstrate.

## 1. Introduction

21 The Medium Scale Travelling Ionospheric Disturbances (MSTIDs) are the iono-  
22 spheric signatures of waves, which are the ones most frequently affecting the precise  
23 Global Navigation Satellite Systems (GNSS) processing (see for instance Hernández-  
24 Pajares et al. 2006). The MSTIDs present up to few TECUs of amplitude in  
25 solar cycle maximum conditions (1 Total Electron Content Unit = 1 TECU =  
26  $10^{16}\text{m}^{-2} \simeq 16\text{cm}$  delay in L1 signal) with typical periods from several minutes to  
27 less than one hour, and velocities from 50 to 300 m/s, typically equatorward during  
28 daytime in fall and winter seasons, and westward during night in spring and summer  
29 seasons (see for instance Hernández-Pajares et al. 2012).

30 The MSTID modelling has become feasible thanks to the availability of dual-  
31 frequency GNSS, like the Global Positioning System (GPS), which has become  
32 likely the main ionospheric sounder in terms of both temporal and spatial resolution  
33 and precision (Shagimuratov et al. 2002, Hernández-Pajares et al. 2011, Krypiak-  
34 Gregorczyk et al. 2013). Indeed, GNSS is able to provide clear views of the same  
35 MSTID amplitude and propagation, either in receivers placed up to few tens of kilo-  
36 meters in local networks (see Figure 1), or from extense dense networks of hundreds  
37 of receivers, such as those in Japan or California (see Figure 2), corresponding to the  
38 same region and time interval as in the previous figure.

39 Although different techniques and applications are affected by MSTIDs (like pre-  
40 cise GNSS positioning and Very Large Base Interferometry, VLBI), it would be too  
41 difficult to determine in real time the exact cause behind each individual instances

of TIDs, and several potential sources are contemplated by different authors (see Table 1 in Hernández-Pajares et al. 2012 for additional details and references), such as, in decreasing order of feasibility or potential influence:

1. The Solar Terminator.
2. The Perkins instability (in order to explain the preferred westward propagation of local winter MSTIDs at night).
3. Particle precipitation at the auroral zone, which seems associated to the - sporadic- Large Scale TIDs (LSTIDs), with wavelengths around 1000 km and velocities within the range of 400- 1000 m/s.
4. Meteorological activity.

New or evolved physical and data-driven models have been proposed recently to reproduce MSTID features: the simultaneous occurrence of nighttime MSTIDs at the magnetic conjugate stations, in Yokoyama (2014); or in Deng et al. (2013), where the detrended Total Electron Content (TEC) from the German national network is interpolated to try to show up MSTID wave fronts, and then compared with the corresponding planar wave model in some given events. In another recent work (Penney and Jackson-Booth 2015) the authors detrend the Slant Total Electron Content (STEC) and correct the ionospheric pierce point movement, in a novel way.

Although the MSTID amplitude is not very important in relative terms, compared with the typical background electron content, MSTID's undulatory nature makes them likely the main non-linear error affecting precise GNSS processing, for instance in RTK or Wide Area Real Time Kinematic (WARTK) techniques (see Wielgosz

64 et. 2005, Hernandez-Pajares et al. 2006), or in Coster and Tsugawa (2015) and  
65 in Paziewski (2016). Regarding their mitigation a new approach has been recently  
66 proposed by Sieradzki & Paziewski 2016. By means of the observed TEC rate, the  
67 user is able to estimate a single initial double-differenced STEC per phase continuous  
68 arch.

69 Moreover, in the last few years, an increase of research in additional aspects of the  
70 Medium Scale Travelling Ionospheric Disturbances can be appreciated as well:

71 • Estimating its 3D structure by means of the Computerized Tomography applied  
72 to wide very dense GNSS ground networks like GEONET (Ssessanga et al. 2015,  
73 Chen et al. 2016).

74 • Signatures of natural and artificial events like major earthquakes and nuclear  
75 explosions (Jin et al. 2014, Zhang & Tang 2015),

76 • Recent works formed on the potential mechanisms to form the MSTIDS are  
77 Jonah et al. (2016) where the strong troposphere convection as seed mechanism of  
78 the Atmospheric Gravity Waves to trigger MSTTDS, is illustrated with collocated  
79 turbulence, temperature and electron content data.

80 • Observations of MSTIDS with different techniques beyond GPS: LOFAR  
81 (Mevius et al. 2016), OI 630.0nm all-sky image (Stefanello et al. 2015) and AM ra-  
82 dio transmissions (confirmed by simultaneous GPS total electron content, Digisonde,  
83 and Super Dual-Auroral Radar Network coherent backscatter radar measurements,  
84 Chilcote et al. 2015).

85 However the MSTID determination and application to precise GNSS positioning  
86 typically faces the lack of enough populated local GNSS networks over many regions,  
87 in order to apply the state of the art MSTID propagation techniques. Is in this  
88 context where the *direct GNSS Ionospheric Interferometry* (dGII) is introduced and  
89 applied as a simple way of mitigating the MSTID effect on GNSS positioning.

90 The layout of the manuscript is the following: After this introduction, the pros  
91 and cons of the main existing MSTID modelling techniques are described in section  
92 2. In section 3, dGII is introduced and illustrated by means of a case study. The  
93 two experiments in winter and summer time conditions will be described in section  
94 4, including the dGII assessments in terms of MSTID mitigation in range, precise  
95 positioning and tropospheric domains Finally, section 5. summarizes the conclusions.

## 2. Main existing MSTID modelling techniques

96 We can divide the main approaches to characterize the propagation of MSTIDs  
97 with GNSS within two families:

98 1. The GNSS Massive Ionospheric Detrending (GMID) method: the propagation  
99 of the MSTIDs (or any ionospheric perturbation with power in the spectral domain  
100 retained after the detrending, typically between 300s and 3000s) can be directly seen  
101 from the detrended VTEC, when, first, the separations between ground receivers is  
102 less than half wavelength (also referred to as semi-wavelength); and, second, when,  
103 moreover, such close permanent receivers are distributed over regions of hundreds  
104 of kilometers of extension (at least two wavelengths, see for instance Tsugawa et al.

105 2007b), in order to properly identify the wavefronts. One advantage of this approach  
106 is that it is not restricted to the most frequent case of ionospheric waves (a single train  
107 of planar waves) as it can be seen in Figure 3 and in Liu et al. 2011, for co-seismic  
108 circular ionospheric waves.

109 The great practical disadvantage is that such local and extended GNSS networks are  
110 available on just few sites, where they were mainly deployed for seismicity monitoring  
111 (such as GEONET network in Japan, or South California GNSS Integrated Network,  
112 SCIGN, in USA, see Figure 4). One of the first applications of the GMID approach,  
113 including data of such networks, can be found in Tsugawa et al. 2007a-b. One  
114 example for SCIGN has been previously introduced (see Figure 2, from Hernández-  
115 Pajares et al. 2012).

116 2. The GNSS Ionospheric Interferometric (GII) techniques derive the MSTID  
117 propagation velocity from the difference of MSTID phase and associated phase delay  
118 among reference receivers. It is computed from the detrended and bandwidth filtered  
119 (Fourier transform) VTEC, obtained from the ionospheric (geometry-free) combina-  
120 tion of dual-frequency GNSS data. The MSTID time delay is computed basically  
121 in two different ways, for each given GNSS satellite in view from a GNSS ground  
122 network, with a diameter less than the half of the typical MSTID wavelength (e.g.  $\lambda$   
123 50 km):

124 (i) By direct correlation of the detrended and bandwidth filtered VTEC, cor-  
125 responding to each given satellite observed from a given receiver, regarding to the  
126 reference receiver (Hernández-Pajares et al. 2006b, Husin et al. 2011).

127 (ii) By subtracting the complex phase for the reference receiver from the corre-  
128 sponding complex phase of the dominant mode (after the Fourier transform) for the  
129 given receiver (Hernández-Pajares et al. 2012).

130 One important advantage of this approach is that just few tens of GNSS receivers  
131 within local networks with a diameter of less than half of the wavelength, i.e. less  
132 than few tens of kilometers, are enough to give support to large regions of many  
133 hundreds of kilometers, due to the large extent of the MSTID planar wave behavior  
134 (Tsugawa et al. 2007b). Therefore:

135 • There are more GNSS facilities already suitable for GII in different regions of  
136 the world, compared with GMID (like available networks in Venice, New Zealand,  
137 California, Alaska or Hawaii, see Hernández-Pajares et al. 2012).

138 • The deployment of Local Networks is in any case much cheaper than the deploy-  
139 ment of extense dense networks, like GEONET or SCIGN.

140 However GII presents some significant drawbacks:

141 • Such local networks are not easily available worldwide, like in most part of Eu-  
142 rope, including Poland and other Central European countries, impeding or difficulting  
143 the nowcasting of MSTIDs (one main issue found in this research).

144 • It is based on the assumption of a single dominant planar wave, and this is not  
145 the case during some infrequent events commented above. Indeed, although two  
146 or more planar waves in different directions could be considered by extending the  
147 analysis to several dominant frequencies in parallel, the circular waves (Figure 3)  
148 cannot be properly characterized by GII.



149 We have taken into account the main goal of this work: to model and mitigate  
150 the the effect of the MSTID propagation in estimation for large regions of the  
151 world, such as East Europe, where no simultaneously extended and dense enough  
152 networks are available. In this context we have taken GII as baseline (see scenario at  
153 Figure 5). The main characteristics of the reference GII implementation (hereinafter  
154 called “comprehensive” GII, cGII) are summarized in the next section.

### 3. Comprehensive GNSS Ionospheric Interferometry (cGII)

155 The initially selected implementation of the MSTID detection and propagation  
156 estimation algorithm, cGII, is the evolved version presented in Hernández-Pajares  
157 et al. (2012) (regarding previous versions, see Hernández-Pajares et al. 2006b and  
158 Husin et al. 2011, where more details can be found). The method is based in the  
159 cross-correlation of the detrended Vertical Total Electron Content (VTEC) values  
160 observed for a given GPS satellite within a local network (see Hernández-Pajares  
161 et al. 2006b), but done directly in the frequency domain. Indeed, the MSTID time  
162 delay is obtained from the user-reference receiver subtraction of the complex phase of  
163 the dominant Fourier Transform terms, which allows to determine the propagation  
164 velocities, with a significant computation offloading (adequate for processing vast  
165 amounts of data), while being able to deal with several planar waves at different  
166 frequencies and with different velocities. cGII consists on the following steps:

167 1. Preprocessing, consisting on two phases:

168 (i) The TEC detrending, performed to make clear the MSTID signatures (for  
169 each given GNSS satellite), which can be done at least in two different ways:

170 a. Double difference in time of the ionospheric (geometry-free) combination  
171 of dual-frequency carrier phases,  $LI=L1-L2$ , and under the absence of cycle slips,  
172 with time separations of 300 s (see Hernández-Pajares et al. 2012).

173 b. Subtracting STEC from a smooth ionospheric model, exemplified in this  
174 work by the UPC GIM “UQRG” computed with tomographic and kriging techniques  
175 (see Hernández-Pajares et al 1999, Orús et al. 2004), at spatial and temporal scales  
176 of few hundreds of kilometers and 900 seconds (i.e. of the order of the MSTID  
177 wavelengths and periods).

178 (ii) The Fourier transform (in fact the Fast Fourier transform algorithm, FFT),  
179 which is applied to the detrended VTEC to show up the main modes, in particular  
180 the predominant frequency  $f$  (which can vary on time).

181 2. The MSTID propagation delay,  $\Delta t$ , from the reference to the given permanent  
182 receiver is given by the difference of complex phase of the dominant Fourier term in  
183 both the user and reference receivers  $(\Phi_f)_{\text{user}} - (\Phi_f)_{\text{ref}}$  (see again Hernández-Pajares  
184 et al. 2012).

185 3. Finally the MSTID velocity is estimated and provided to the users:

186 (i) From all the values  $\Delta t$  observed from all the permanent network receivers, the  
187 MSTID velocity is computed for each given satellite, taking consistently into account  
188 the ionospheric pierce point movement (see above mentioned reference).

189 (ii) With such MSTID velocity vector (estimated every epoch, i.e. each 30 sec-  
190 onds), the time delay is consistently computed and applied by the user to the GNSS  
191 network ionospheric corrections.

192 Nevertheless the application of the comprehensive GNSS Ionospheric Interferome-  
193 try approach -cGII- is limited by the small number of GNSS receivers in the available  
194 European Local Networks, within diameters up to  $\sim 50$  km. This network size (less or  
195 about half of typical MSTID wavelength) is suitable for applying unambiguously the  
196 GNSS Ionospheric Interferometry for characterizing MSTID. This problem affects in  
197 particular to Poland and other Central European countries, as it can be seen in the  
198 limited number density of available receivers (Figure 6).

#### 4. Direct GNSS Ionospheric Interferometry (dGII)

199 The direct GNSS Ionospheric Interferometry (dGII) approach is introduced to solve  
200 the limitation of the cGII technique related to the lack of close enough receivers over  
201 many countries in Europe. dGII is directly based on real-time conditions, generalizing  
202 the climatological DMTID model presented in Hernandez-Pajares et al. 2006, in a  
203 simple and optimized way. It can be summarized as follows:

204 1. The VTEC detrended,  $\delta V$ , showing up the MSTID signatures for each given  
205 GNSS satellite  $s$ , is computed directly based on single difference in time of consecu-  
206 tive measurements, for the same pair transmitter-receiver, of the geometry-free com-  
207 bination of dual-frequency GNSS carrier phase measurements  $LI=L1-L2$  (similarly  
208 to Deng et al. 2013), and with a time interval of  $dt=60$  sec (an optimal compromise

209 between MSTID signal level and time-space localization):  $\delta V = \delta LI / M$ , being  $M$   
210 the ionospheric mapping function, which relates the slant TEC with the vertical TEC  
211 (see for instance Hernández-Pajares et al. 2011). We consider in this problem the  
212 typical simplification of a spherical thin layer placed at 450 kilometers height (used  
213 for instance in the global VTEC ionospheric maps provided in IONEX format, see  
214 Schaer et al. 1998).

215 2. We assume that, for a given GPS satellite, the MSTID is affecting first to the  
216 reference receiver, and, a certain time  $\Delta t$  later, to the user. Then the MSTID time  
217 delay  $\Delta t$  can be estimated by cross-correlating  $\delta LI_{\text{ref}}$  with  $\delta LI_{\text{user}}$ , assuming initially  
218 a sliding window, depending on the distance distribution in the network (i.e. from  
219 600 sec, up to 1 hour, being then this period the di-facto minimal initial user cold-  
220 start time in dGII approach for real-time applications). Indeed, this can be always  
221 done by selecting as reference receiver one in the network located in Polarward / East  
222 direction during fall-winter / spring-summer seasons (see typical MSTID velocities  
223 occurrences in terms of season and local time in Hernandez-Pajares et al. 2012).  
224 And the distance between them can be still longer than the predominant MSTID  
225 wavelength when the unfiltered amplitude signatures, varying on time, allow the  
226 proper implicit distinction of the MSTID phase ambiguity.

227 3. Thanks to the static and precisely known position of permanent receivers dis-  
228 tributed in Wide Area GPS networks, it has been demonstrated that it is possible  
229 to compute very precise STEC values,  $S_{\text{ref}}$ , in real-time (see for instance Hernández-  
230 Pajares et al. 2000). In this point, we have considered a simple proxy of  $S_{\text{ref}}$ , from the

231 L1-L2 measurements calibrated with the VTEC GIM (see Hernández-Pajares et al.  
 232 2011), by using the likely most accurate GIM presently available: the tomographic-  
 233 kriging UPC GIM "UQRG" (see Hernández-Pajares et al. 2016). Then the precise  
 234 slant ionospheric delay,  $S_{ref}$ , provided by the permanent reference receiver for each  
 235 given GNSS transmitter in view, is taken as a proxy of the user value,  $S_{user}$ , in the  
 236 following simple RTK-like way:  $S_{user}(t) = V_{ref}(t-\Delta t) M_{user}(t)$  where  $V_{ref}(t-\Delta t)$  is  
 237 the corresponding VTEC measured at the reference receiver  $\Delta t$  seconds before and  
 238  $M_{user}(t)$  is the mapping function (see first point above) at the user location and  
 239 observations time. It has been shown that this approach is more accurate than other  
 240 simple proxies of  $S_{user}(t)$  such as  $S_{ref}(t-\Delta t)$  –see right-hand plot in Figure 11. In  
 241 other words, we are assuming that the main VTEC change due to the movement  
 242 of Ionospheric Pierce Point (IPP) and the MSTID propagation time between the  
 243 reference receiver and the user is basically due to the wave signature.

#### 4.1. Case study

244 To clarify the problem and the technique performance we have analyzed in depth  
 245 the result of applying dGII to the following case study: the GPS satellite PRN15,  
 246 observed during first day of year 2001, from two receivers belonging to SCIGN, p294  
 247 (reference) and p532 (user), see Figure 7.

248 It can be seen in Figure 8 the typical MSTID southward propagation signature on  
 249 STEC, during a winter day-time, which is compared with the spatially and tempo-  
 250 rally smoothed STEC provided by the GIM. It is fully in agreement with the expected  
 251 velocities for such local-time and season. The result of the preprocessing detrending

(point 1 of dGII algorithm, see above) can be seen in Figure 9. In particular it can be seen the periodic contribution of the GIM model discretization (see additional details in corresponding caption). This suggested us not using it for detrending, keeping just the derivative of the direct observation as a smoother detrender. In this way any *contamination* associated to the GIM gridding in the spectrum, and corresponding artifact in the results, is avoided. In upper-left plot of Figure 10, we show the directly observed detrended STEC for reference and user receivers, thus making visible again the propagation delay between them, so that the delay can be computed by cross-correlation (with a sliding window of about 15 minutes, see upper-left plot of Figure 10). We have mainly considered two different ways of applying dGII: (i) to use the instantaneous MSTID time delay maximizing the real-time correlation between the user and the reference receiver detrended STEC; and (ii) to use the common predominant MSTID time delay, available in near real-time or post-processing, which maximizes all correlations, available right after all the observations in each given continuous phase arch of each given satellite have been taken, from both user and reference receivers. By applying to the detrended VTEC (VTEC derivative) of the reference receiver, the instantaneous MSTID time delay on the one hand, and on the other hand the common predominant MSTID time delay (150 s in this case, see the upper-left and upper-right plots of Figure 10), we obtain the bottom-left and bottom-right plots of Figure 10.

The typical comparison of performance of the detrended VTEC (taking as proxy the VTEC derivative) measured from the user side, with the original (no time-shifted),

instantaneous and common shifted reference site time series, can be seen at the left-hand side of Figure 11. The corresponding comparison for STEC, translated directly from the reference receiver, or from translated VTEC by means of the on-time user ionospheric mapping function, can be seen at the right-hand side of Figure 11. The following features can be observed:

1. The STEC of the reference receiver synchronously applied (directly, without time shift) performs worse, as expected.
2. We observe the necessity of using consistently the user mapping function, in order to get the best results with this direct approach.
3. The reference STEC synchronized with the predominant common dGII MSTID time delay works slightly better (especially at 22-22.8h) than the instantaneous one (which is less smooth), except for very low elevation (likely related with the highly varying pierce point velocity, see Penney and Jackson-Booth 2015).
4. Error reduction of up to 50-85% of the initial error in MSTID peaks: from +1.5 TECU when the simple simultaneous RTK ionospheric correction is applied, reduced to 0.2-0.7 TECU, when the expected MSTID time delay is applied.

Finally the comparison of the real versus the estimated user STEC, which is computed with the reference site STEC under four different treatments as proxy of user STEC (reference site STEC original, common-time shifted, and common and instantaneous-time shifted with the user mapping function), can be seen in Figure 12, confirming the previous findings. In particular the suitability of the reference site VTEC, which is delayed by the constant MSTID time delay, estimated inde-

pendently for each phase-continuous arch receiver-transmitter, is shown and used in combination with the user mapping function (Figure 12, bottom-right hand side).

Finally, in the next section, we summarize an extensive application of dGII on different realistic scenarios over Poland, in particular its main impact on precise positioning and tropospheric determination is discussed.

## 5. dGII assessment over Poland in winter and summer conditions

The direct GII MSTID mitigation technique has been applied, emulating real-time conditions, to three different networks over Poland at NE and SW regions, and overall northern part of Poland (RTKfinal\_SW-large, RTKfinal\_NE-large and BERNESE\_final, respectively), during fall/winter and spring/summer experiments (days 353 and 168, 2013) in order to assess the RTK and tropospheric results.

### 5.1. Assessment on Range Errors

In figures 13 and 14 the network with the corresponding available receivers (left-hand columns), as well as the summary of the dGII performance in range domain for each user reference baseline (right-hand columns), is represented. A winter day (353, 2013) corresponds to Figure 13 and a summer day (168, 2013) to Figure 14.

These results confirm the best performance of dGII based on an estimated common MSTID time delay per satellite phase-continuous arch of data, plus the actual user mapping function (compared with the other three approaches shown in Figure 12), with daily reductions up to 10-90% of the initial range error when the synchronous ionospheric correction of the reference site is taken (which can be interpreted as a



315 proxy of the MSTID range error mitigation in a basic RTK-like approach), under  
316 a simple technique and without the need of estimating the MSTID velocity. The  
317 cases with worse performance only happen a few times during the winter day, with  
318 a maximum increase of error of 8%, and coinciding mostly with baselines almost not  
319 affected (i.e. mainly perpendicular) by the MSTID propagation.

## 5.2. Assessment on Precise GNSS Positioning Performance

320 The performance of the RTK positioning was evaluated with different strategies and  
321 corresponding files of observations (see Table 1 and Table 2) and based on processing  
322 several test baselines, in both winter and summer time.

323 There are some examples below of the application of dGII-derived corrections to  
324 kinematic processing over 57 and 81 km baselines. Table 3 presents the indicators of  
325 the RTK positioning performance on day of year (DOY) 168 of year 2013. It is clearly  
326 visible for both processed baselines that the application of the MSTID corrections  
327 (ModRNX(Prop.STEC)) causes the improvement in the ambiguity resolution (AR)  
328 domain. In particular, there can be seen the increase of the ambiguity succes rate  
329 (ASR) and the significant drop in the time to first fix. Indeed the daily performance  
330 can be seen in fourth column in Table 3, with comprises an still strongest time  
331 to first fix reduction under the MSTID modelling when the period with MSTID  
332 activity is considered only (from 22 epochs to 8 epochs, and from 16 to 9 epoch,  
333 for both BOR-KONI and GNIE-KONI baselines). Additional details can be seen in  
334 Figure 15. The ambiguity resolution success rate (ASR) is defined here as the ratio  
335 of epochs with correctly resolved ambiguities to total number of processed epochs.

336 TTFF is defined as the number of epochs required for obtaining correct ambiguity  
337 resolution in a processed session. By using MSTID corrections we can obtain reliable  
338 RTK position much faster. For BOR1-KONI baseline the ASR (ambiguity success  
339 rate) parameter increased from 63 to 78 % for ModRNX(Prop.STEC) observations  
340 in respect to the original uncorrected observations. For the second baseline the  
341 same parameter increased by 9 % to a value of 83 %. The value of time to first fix  
342 shortened from almost 30 s to 13 s, and from, 18 s to 16 s, for BOR1 and GNIE  
343 rover baselines respectively (Table 1). The repeatability of the kinematic coordinates  
344 on 168 DOY are on similar levels for both the strategies. The standard deviation of  
345 the mean coordinates varies in the range 11-13 mm, 6-9 mm and 25-36 mm, for N,  
346 E, U components respectively.

### 5.3. Assessment on Tropospheric Delay Estimates

347 The dGII impact in troposphere domain was verified with 24 daily solutions for ex-  
348 perimental network: 6 different sets of RINEX files were processed using two baseline  
349 definition strategies (SHORTEST, STAR) in each experimental campaign (summer  
350 and winter). These strategies, as well as OBS-MAX and DEFINED are used for base-  
351 line definition in Bernese GNSS Software v. 5.2 (Dach et al., 2015). The SHORTEST  
352 strategy leads to create the set of shortest baselines in given setup of processed sta-  
353 tions. The STAR strategy creates the set of baselines connecting one reference sta-  
354 tion with all remaining stations.. The results of the RMS of post-fit residuals of unit  
355 weight, station coordinate errors, number of ambiguity resolution (in four ambiguity  
356 resolution, AR, strategies), error of estimated Zenith Tropospheric Delay (ZTD) and

357 ZTD residuals with respect to Regional Reference Frame Sub-Commission for Eu-  
358 rope (EUREF) GNSS Positioning Network (EPN) final solution, were investigated in  
359 detail.

360 Negligible differences between solutions were found among the RMS of unit weight,  
361 station coordinate errors, and estimated ZTD errors. This is because we used 24-  
362 hour sessions for troposphere estimation where MSTID effects affecting a few per  
363 cent of observations in a session, vanish out due to large amount of the processed  
364 data compared to RTK.

365 The differences were significant for AR results (Figure 16). In SHORTEST baseline  
366 definition strategy, the significant improvement was noticed in Quasi Ionosphere-  
367 Free method (QIF) for all developed ionosphere models, while for the remaining  
368 AR strategies the results, comparing to RedRNX+CodeION, are very similar, ex-  
369 cept Prop.STEC model in winter campaign. In STAR strategy, that is consistent  
370 with the methodology of MSTID model determination, all three developed mod-  
371 els increased the percent of resolved ambiguities with respect to the solution with-  
372 out any ionosphere model ModRNX(Truth.STEC) solution was better than Re-  
373 dRNX+CodeION in every AR strategy, and ModRNX(Prop.STEC) was better than  
374 RedRNX+CodeION in QIF strategy (very long baselines). Similar results were ob-  
375 tained with Narrow Lane and Wide Lane strategies.

376 Significant differences were found in estimated ZTD values. The application of  
377 developed models resulted in ZTD biased with respect to EPN final solution and  
378 with respect to the solution with the Global Ionospheric VTEC Maps provided by

379 the Center for Orbit Determination in Europe (CODE) to the International GNSS  
380 Service, IGS (Figure 17). This bias is caused by the reduced number of observa-  
381 tions in RINEX files, as well as by inconsistency with the reference solution, that is  
382 based on the CODE ionosphere model. The obtained bias showed that the solutions  
383 with ionosphere model including MSTID are different than the EPN final solution  
384 (the differences were even larger during the periods of expected MSTID maximum  
385 activity), however there is no possibility to assess which one is better.

## 6. Conclusions

386 We present in this work an MSTID modeling that overcomes shortcomings of the  
387 existing methods. The modelling technique that we present is more suitable for  
388 sparse GNSS networks. The direct GNSS Ionospheric Interferometry (dGII) is ap-  
389 plied in real-time conditions, and depends only on reference ionospheric data from a  
390 single permanent receiver. The performance in range domain can reduce the error  
391 up to 10-90%, with only a worsening in some cases up to 8%. Subsequent applica-  
392 tion of MSTID corrections to relative kinematic positioning resulted in reduction of  
393 size and variability of between-pair-of-transmitter-and-receivers Double Differenced  
394 (DD) ionospheric residuals during MSTID occurrence. In particular, ambiguity suc-  
395 cess rate was improved, and the number of epochs required to obtain precise position  
396 decreased.

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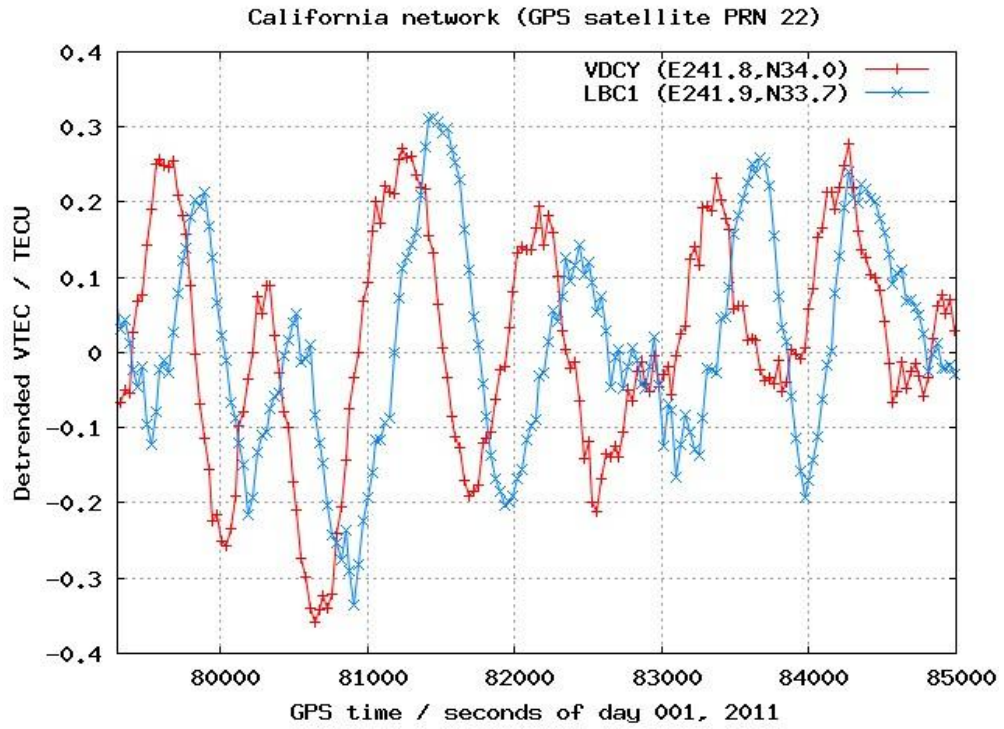
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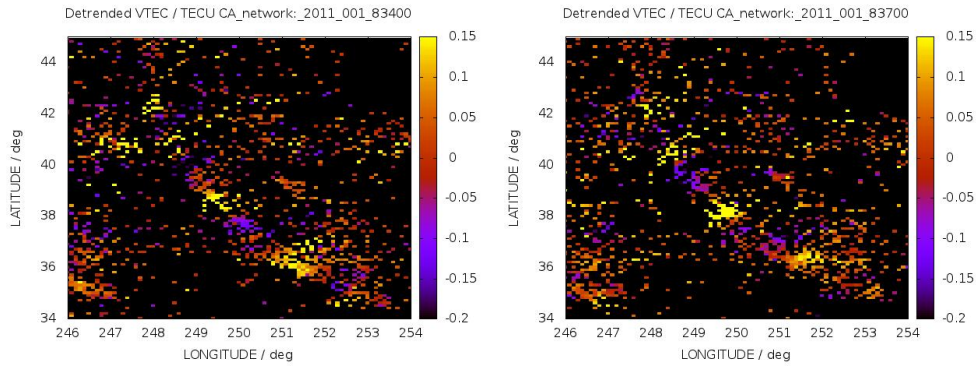
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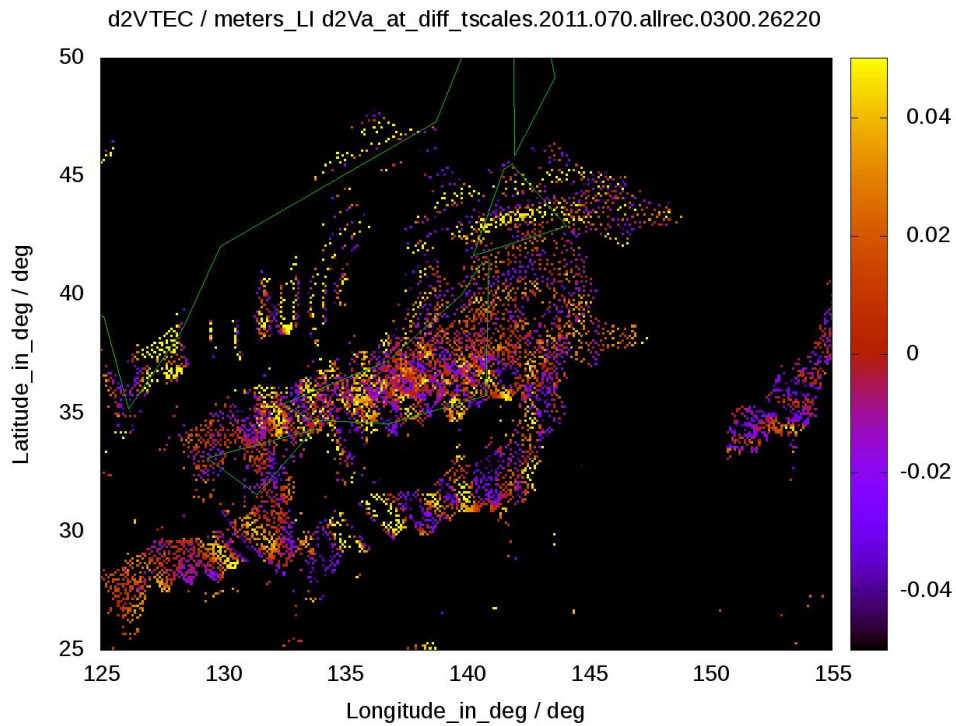
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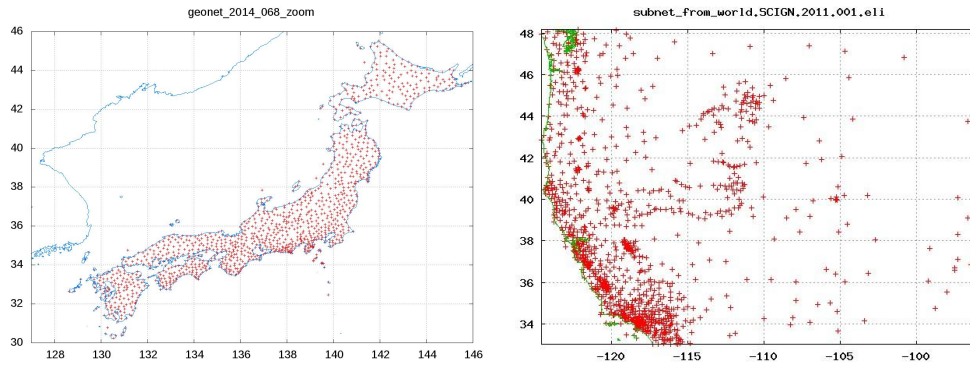
**Figure 1.** Example of MSTID signature in the detrended Vertical Electron Content (VTEC), directly obtained from the ionospheric combination of GPS carrier phases (see section 3) corresponding to an MSTID affecting GPS satellite PRN 22, advancing from receiver VDCY (E241.8,N34.0) toward LBC1 (E241.9,N33.7) in California network, January 1st, 2011 (reproduced from Hernández-Pajares et al. 2012).



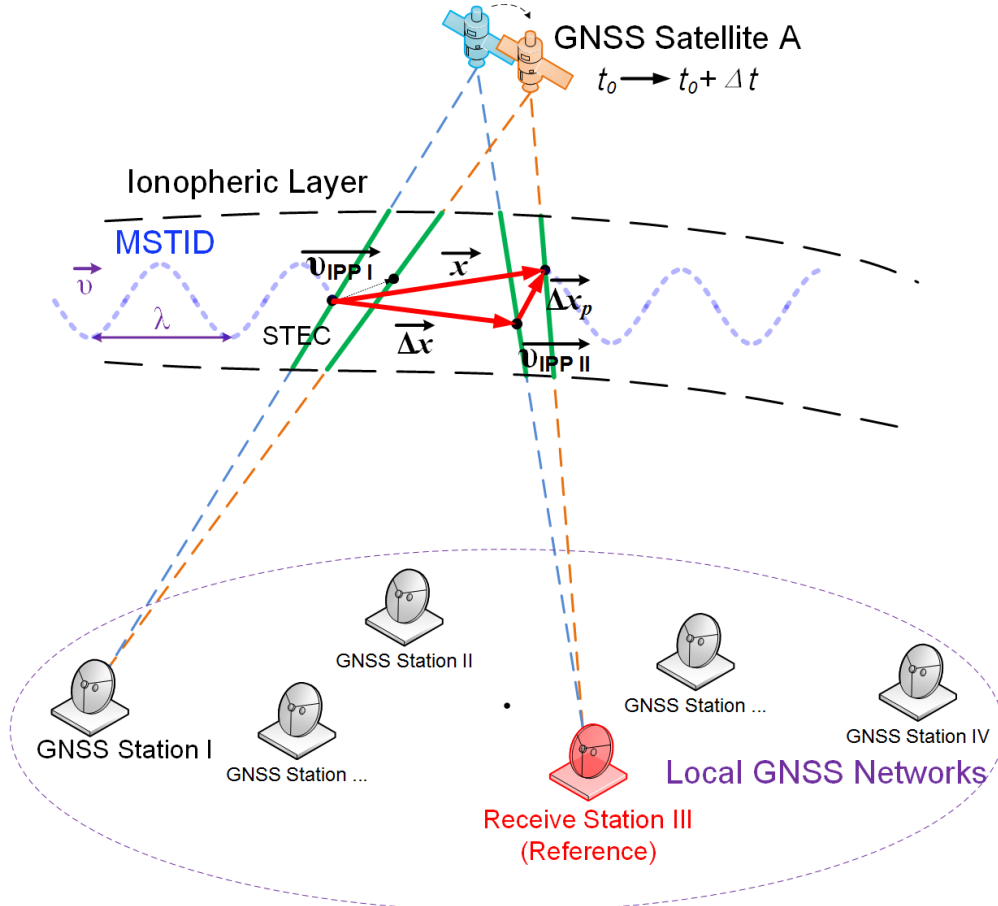
**Figure 2.** Daytime winter MSTID propagation fronts directly seen from detrended VTEC V (in TECUs; GMID method) over the whole dense network in California and West USA (first day of 2011, for GPS time epochs 83400 and 83700 s, reproduced from Hernández-Pajares et al. 2012).



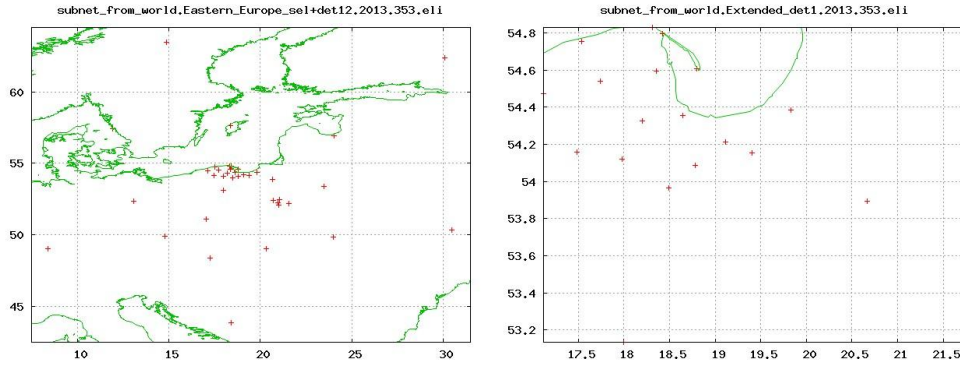
**Figure 3.** Detrended VTEC obtained from GEONET GPS data, coinciding with the Tohoku earthquake and tsunami (GPS second 26220 of day 70, 2011), where the circular ionospheric waves centered at the earthquake epicenter are evident (extracted from Hernández-Pajares 2013).



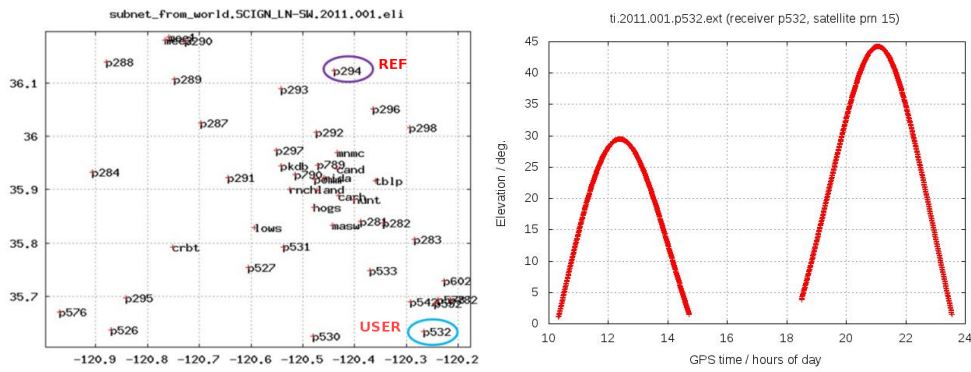
**Figure 4.** Main part of GEONET GNSS network (left-hand plot, corresponding to deployed receivers during day 68, 2014) and South California Integrated GNSS Network (SCIGN, for day 1, 2011, right-hand plot).



**Figure 5.** MSTID detection Model from GNSS Networks: The baseline vector between any static receiver and the reference one,  $\Delta x$ , the velocity of the Ionospheric Pierce Point, IPP, and the corresponding movement,  $\Delta x_p$ , during the time  $\Delta t$ , are represented.

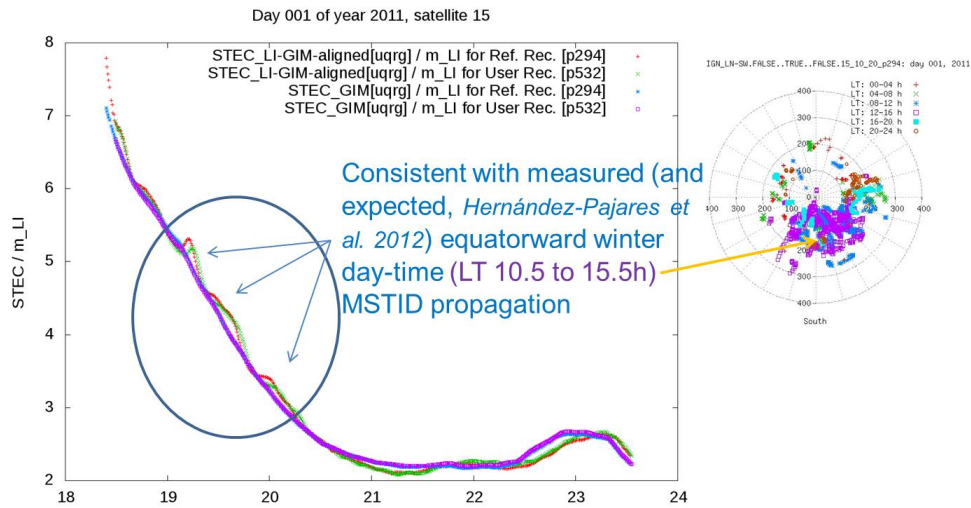


**Figure 6.** Distribution of GNSS receivers available in Eastern Europe for the study, during day 353, 2013 (left-hand plot, with zoom on the right-hand plot).

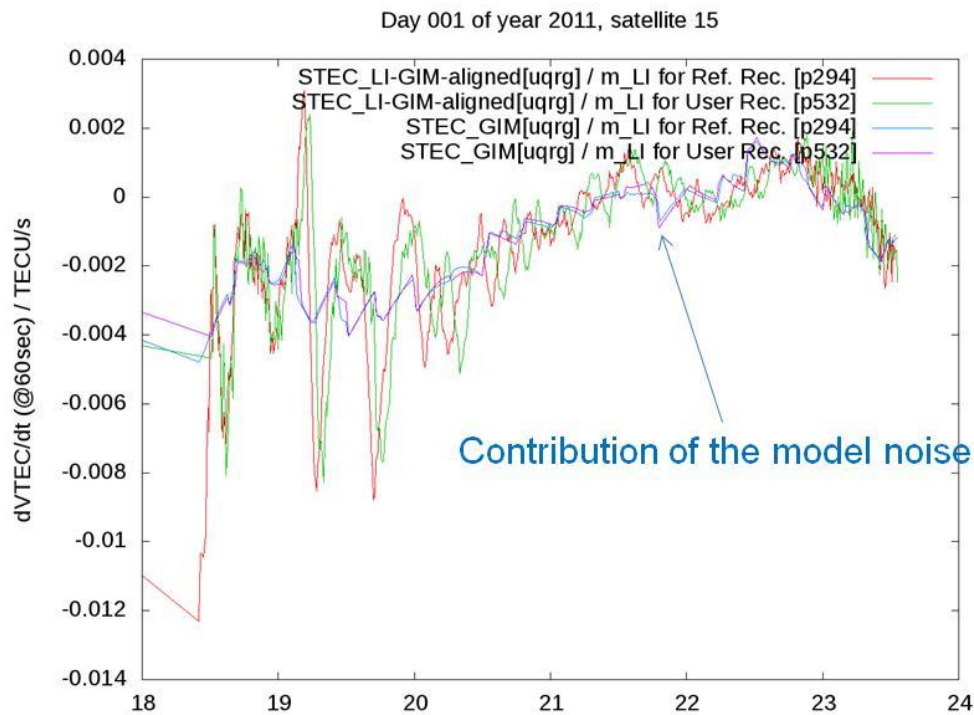


**Figure 7.** [Left] Location of two GNSS SCIGN receivers (p294 taken as reference -REF- and p532 treated as user -USER-), selected due to its southward-oriented baseline, for the GII test case studies. [Right] The elevation of satellite PRN15 is represented as function of the time from user receiver (PRN15, day 001, 2011).

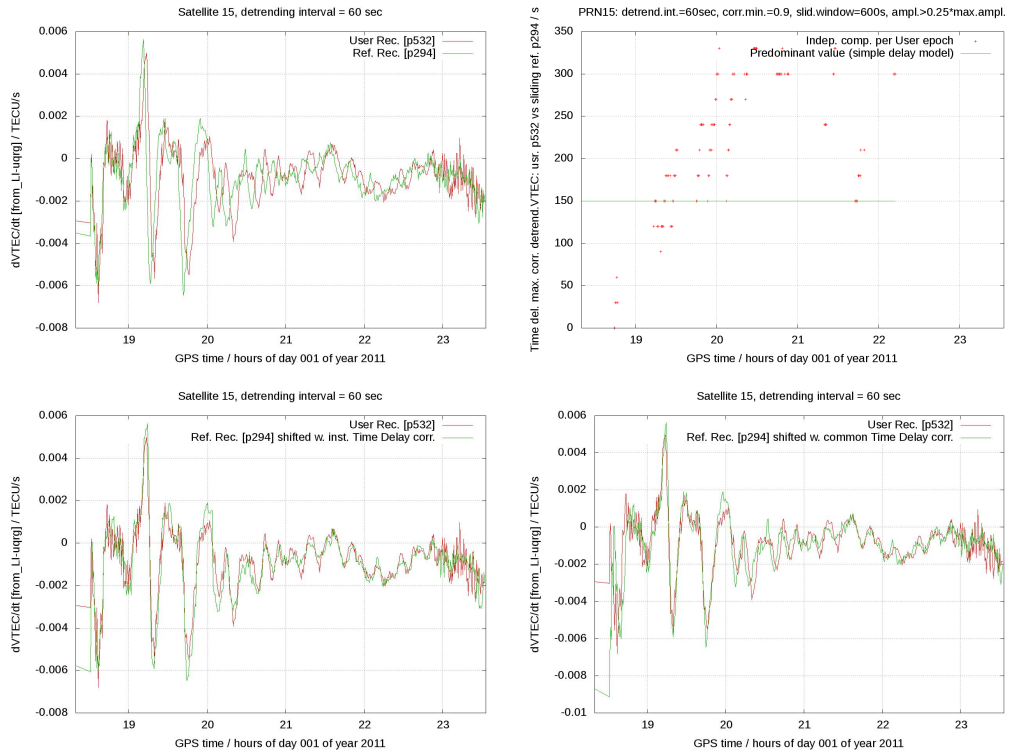




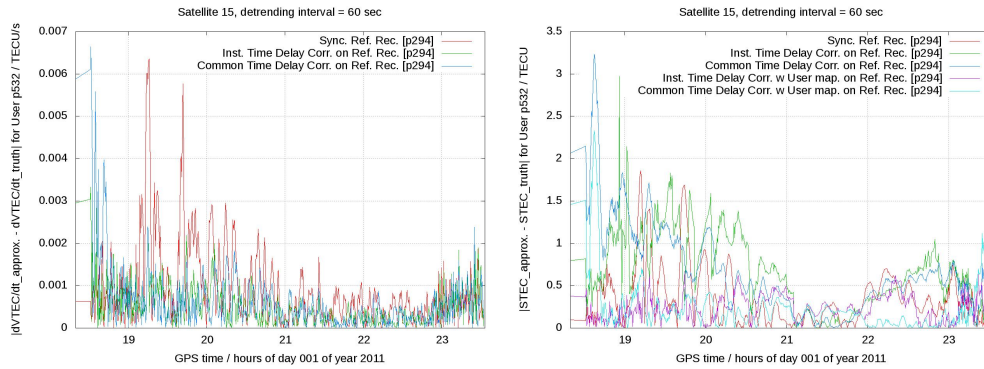
**Figure 8.** Correspondence of the MSTID signature in calibrated Slant Total Electron Content (STEC) in meters of LI=L1-L2 (left) with the estimated velocity with cGII (right) -SCIGN, day 001, 2011-.



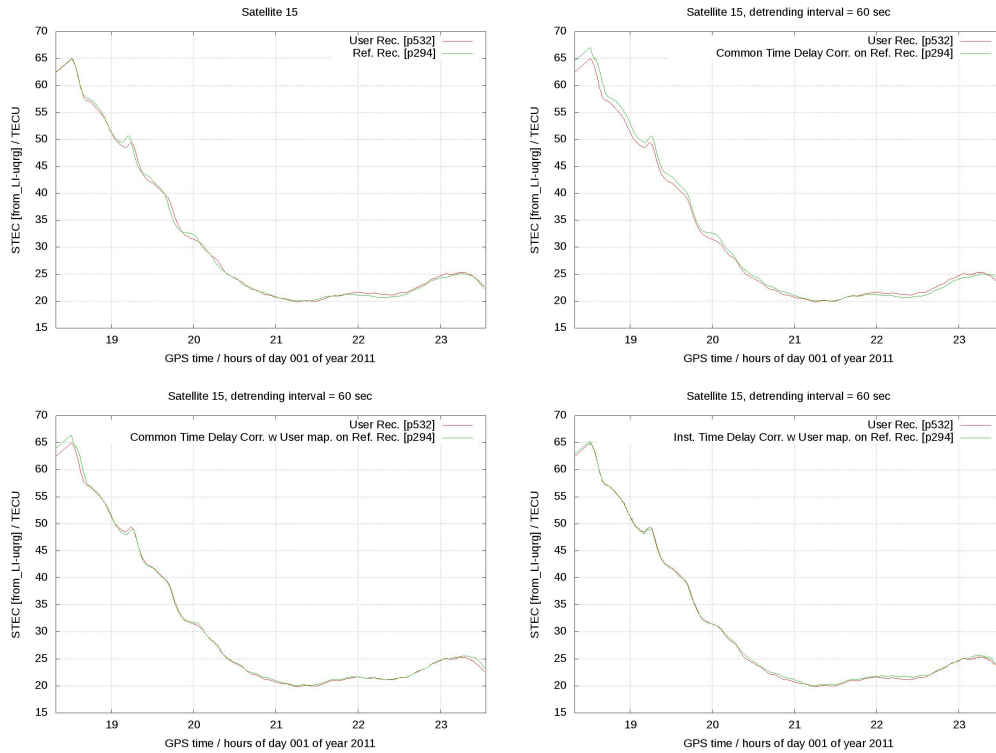
**Figure 9.** Derivative of the GIM detrended STECs and GIM STECs in dGII case study, projected vertically ( $dVTEC/dt$  computed for  $dt = 60$  seconds) where the GIM model noise, with a temporal and spatial resolution too low to capture the MSTID propagation, is evident in the peaks shown in magenta (receivers p294 and p532, satellite PRN15, day 1, 2011).



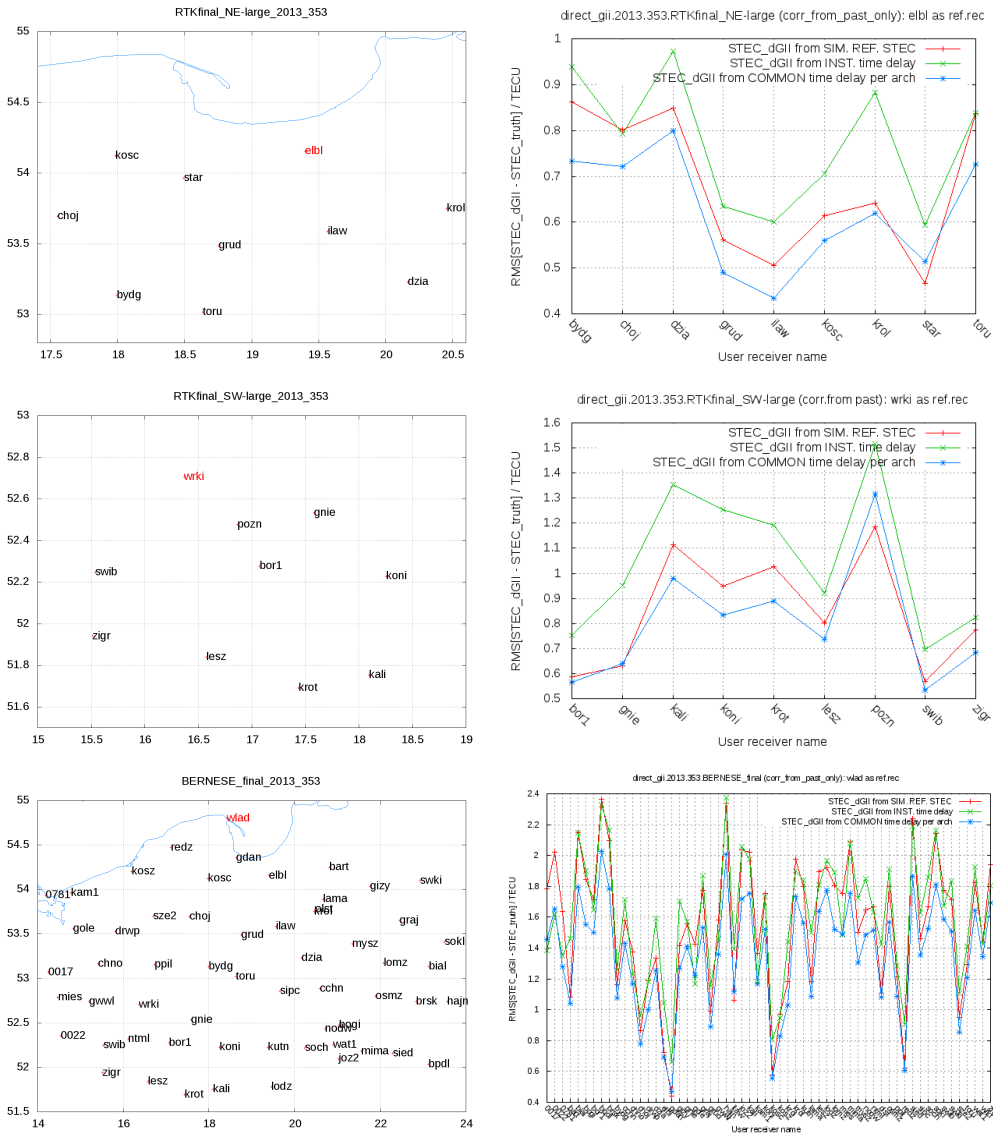
**Figure 10.** Top-left, bottom-left and bottom-right plots: Plain observed, instantaneously and common dVTEC-time shifted STEC derivative, respectively, following the estimated MSTID time delay obtained by direct cross correlation (top-right plot) –SCIGN, p294, p532 rec., PRN15, day 001, 2011-.



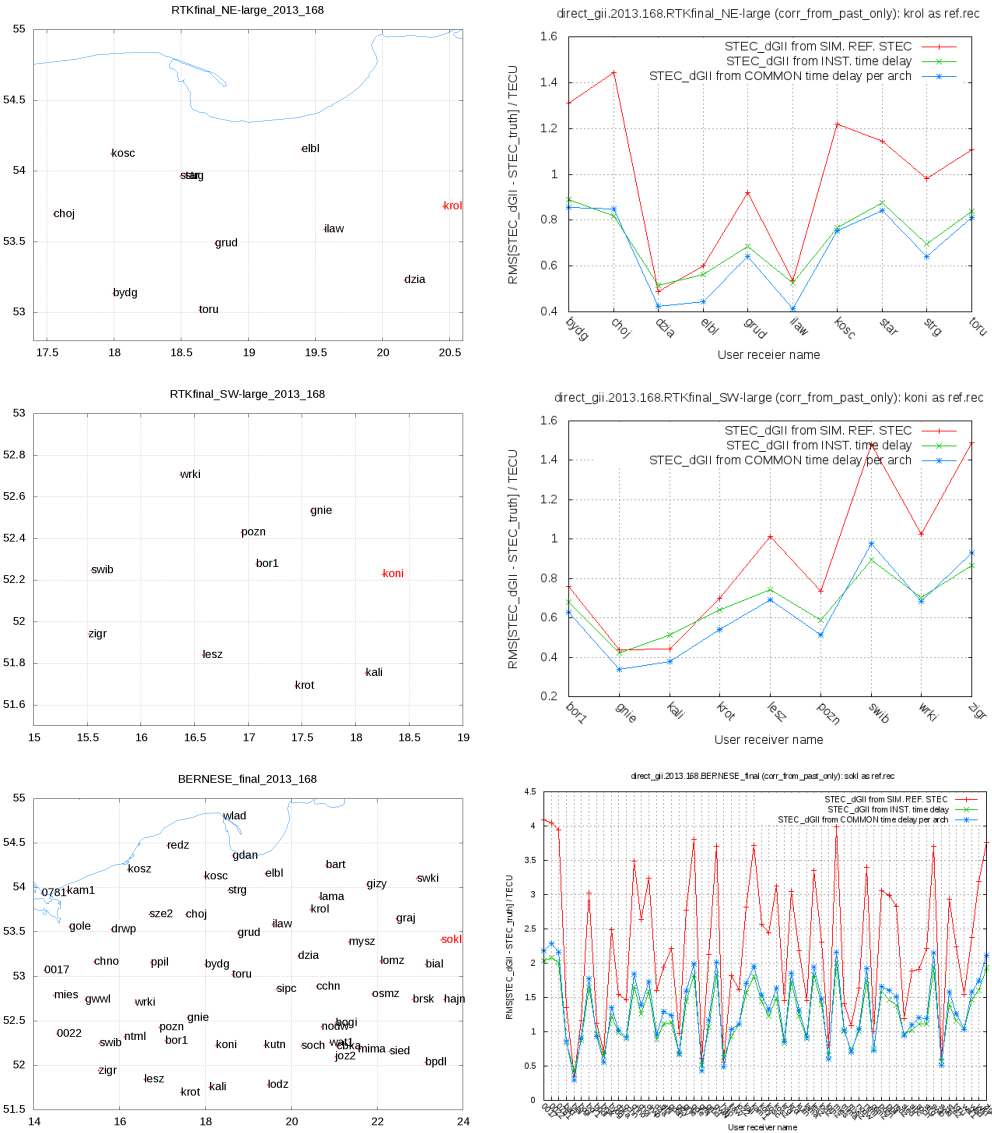
**Figure 11.** [Left] User VTEC derivative error vs. time, taking as modelled value the zero (red), instantaneous (green) and common (blue) dGII-time-shifted reference site STEC values. [Right] Similar comparison, but for the user STEC, and including as well the VTEC interpolation with the user mapping function for both instantaneous (magenta) and common (light blue) cases (receivers p294 [user] and p532 [ref.], PRN15, day 001, 2011).



**Figure 12.** Comparison of original user' STEC with the reference site' STEC: original (LI calibrated with UPC UQRG GIM, top-left), common-time shifted (by the common dGII MSTID time delay, top-right), common-time shifted VTEC + user mapping function (bottom-left) and instantaneous-time shifted VTEC + user mapping function (bottom-right) –receivers p294 [user] and p532 [ref.], PRN15, day 001, 2011-.



**Figure 13.** Map of dGII analyzed receivers in RTKfinal-NE-large, RTKfinal-SW-large and BERNESE-final networks (left column), and corresponding performance of dGII for different baselines, with northern reference sites elbl, wrki and wlad, respectively (right column, Poland, winter day of 353, 2013). The performances in the right-hand plots are shown, vs the user receiver name following an alphabetic order, under, i), zero time-shift (red), and time shifts determined by: ii) maximum correlation with the reference receiver ionospheric delay performed instantaneously (green), iii), the best value August 23, 2016, 8:06am only applied to it (blue). A F T



**Figure 14.** Map of dGII analyzed receivers in RTKfinal-NE-large, RTKfinal-SW-large and BERNESE-final networks (left column), and corresponding performance of dGII for different baselines, with eastern reference sites krol, koni and sokl, respectively (right column, Poland, summer day of 168, 2013). The performances in the right-hand plots are shown similarly to previous figure.

**Table 1.** Different ionospheric strategies compared on precise GNSS processing

| Acronym    | Brief description   |
|------------|---|
| noSTEC     | Observations uncorrected from any ionospheric model                       |
| Prop.STEC  | Observations corrected with MSTID dGII corrections only                   |
| CodeION    | Observations corrected with CODE VTEC GIMs                                |
| Truth.STEC | Reference STEC values (carrier phase obs. calibrated with UQRG VTEC GIMs) |

**Table 2.** Different type of observation RINEX files considered on precise GNSS

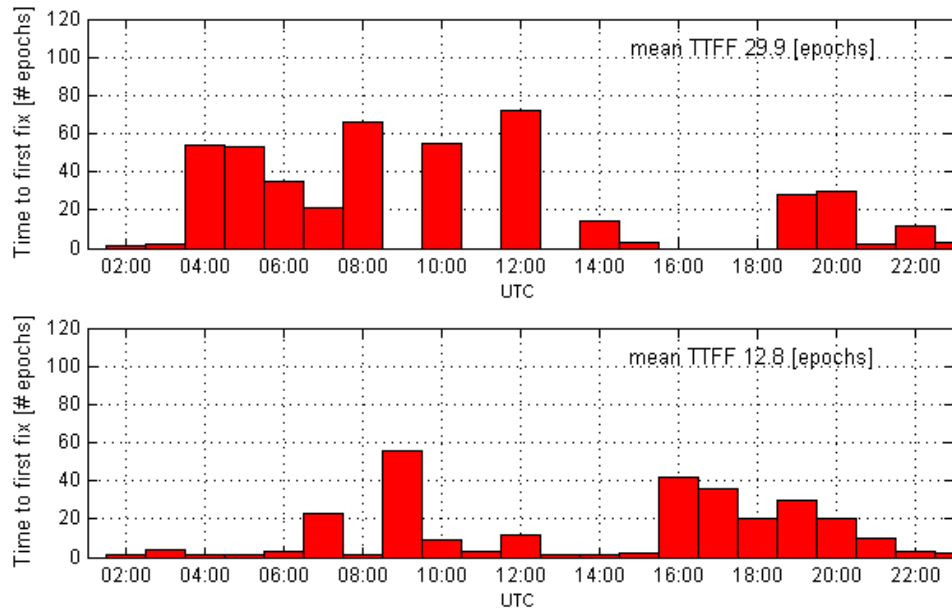
processing

| Acronym | Brief description  |
|---------|--|
| OrgRNX  | RINEX file containing original observations  |
| ModRNX  | Modified RINEX file containing observations corrected with available ionospheric information |
| RedRNX  | RINEX file with original observations when ionospheric corrections are available only        |

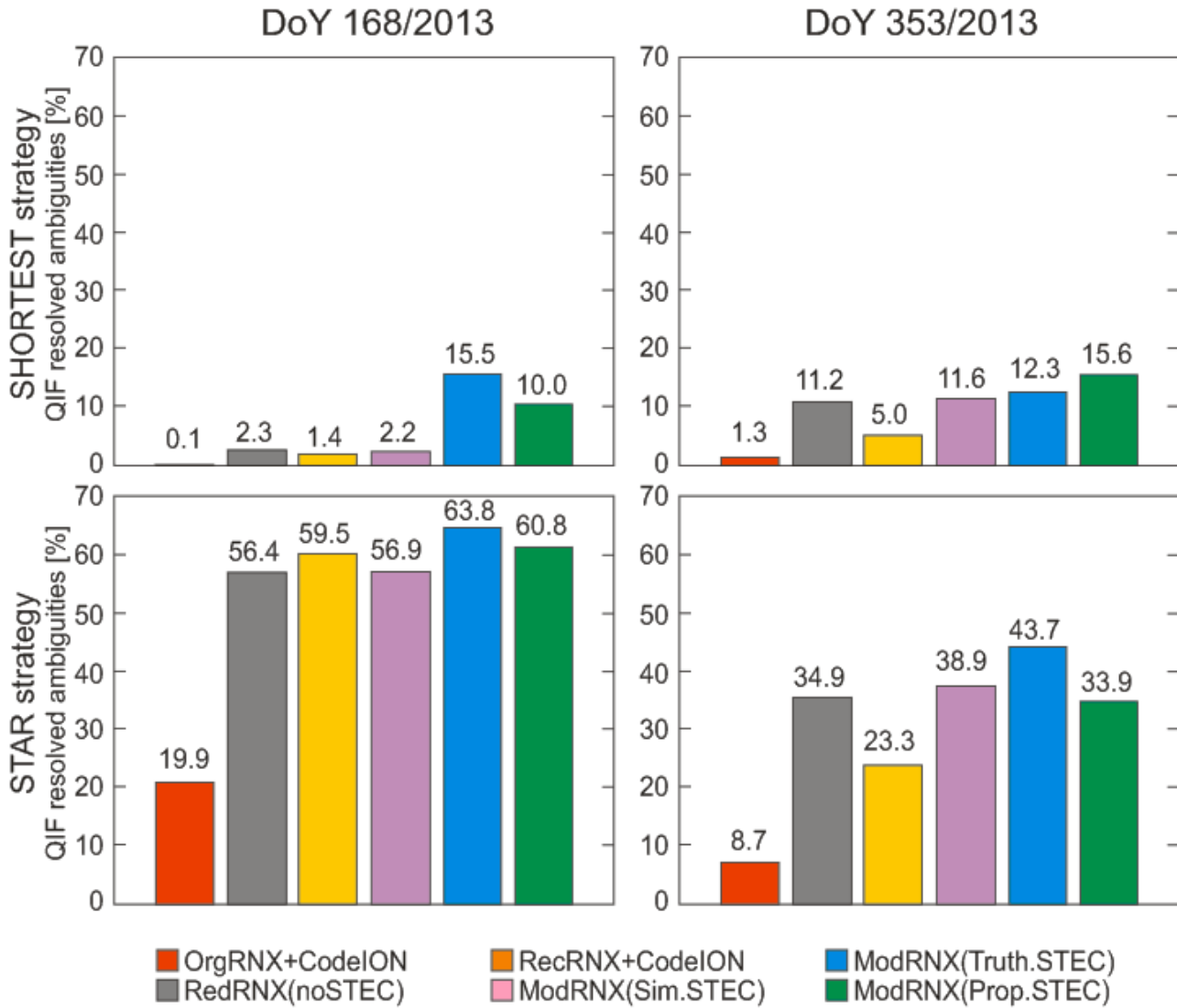


**Table 3.** RTK positioning performance statistics, including the standard deviation of the component (std), at central west Poland network on day 168 of year 2013.

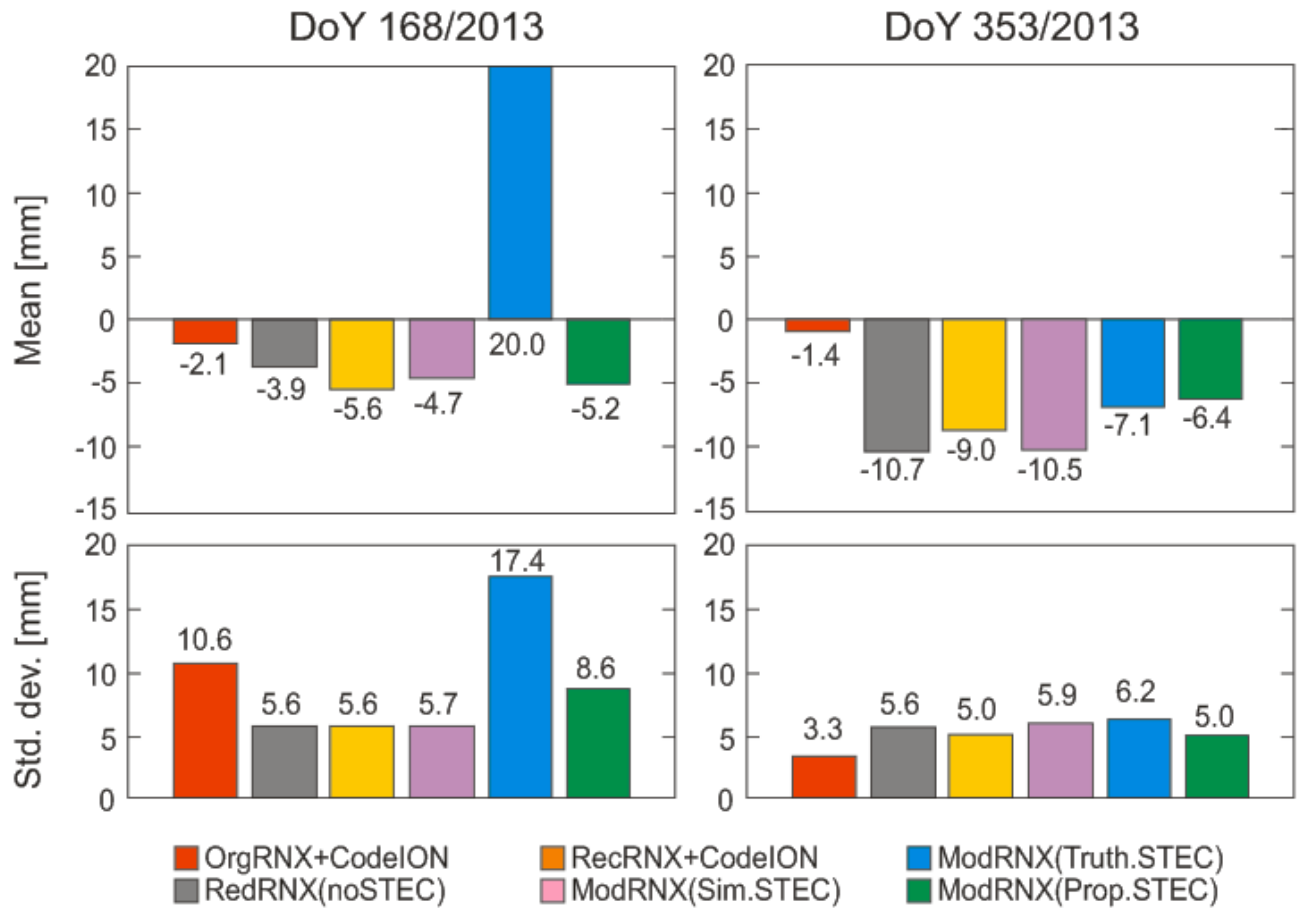
| Baseline  | Strategy          | ASR | TTF      | N std | E std | U std |
|-----------|-------------------|-----|----------|-------|-------|-------|
|           |                   | [%] | [epochs] | [m]   | [m]   | [m]   |
| BOR1-KONI | RedRNX(noSTEC)    | 63  | 29.9     | 0.011 | 0.006 | 0.029 |
|           | ModRNX(Prop.STEC) | 78  | 12.8     | 0.012 | 0.007 | 0.035 |
| GNIE-KONI | RedRNX(noSTEC)    | 74  | 18.3     | 0.013 | 0.008 | 0.025 |
|           | ModRNX(Prop.STEC) | 83  | 15.7     | 0.013 | 0.009 | 0.036 |



**Figure 15.** Time To First Fix (TTFF), baseline BOR1-KONI on 168 DOY (top panel- RedRNX(noSTEC), bottom panel- ModRNX(Prop.STEC))



**Figure 16.** Percent of QIF resolved ambiguities in SHORTEST (top) and STAR (bottom) baseline definition strategies, during summer (left) and winter (right) campaign, for 6 different network solutions.



**Figure 17.** Mean value (top) and standard deviation (bottom) of post-fit residuals between 6 different network solutions with SHORTEST baseline definition and EPN final solution