

# DESIGN OF ACTIVE MULTIPLE-DEGREES-OF-FREEDOM ELECTROACOUSTIC RESONATORS FOR USE AS BROADBAND SOUND ABSORBERS

H. Lissek<sup>1</sup>, E. Rivet<sup>1</sup>, S. Karkar<sup>2</sup> and R. Boulandet<sup>1</sup>

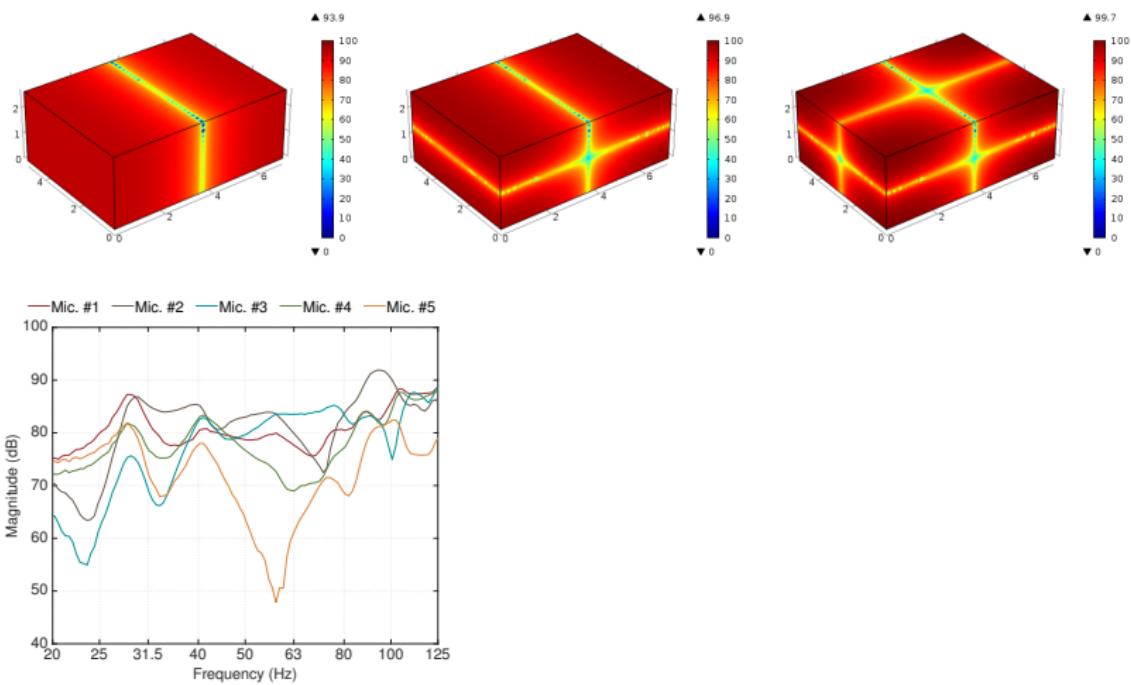
<sup>1</sup>LTS2, École Polytechnique Fédérale de Lausanne, Switzerland

<sup>2</sup> LTDS, Ecole Centrale Lyon, France

April 25, 2016

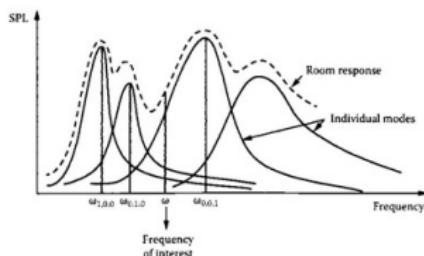
## Introduction

## Rooms at Low Frequencies



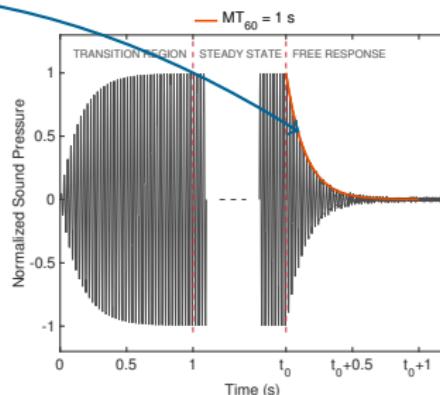
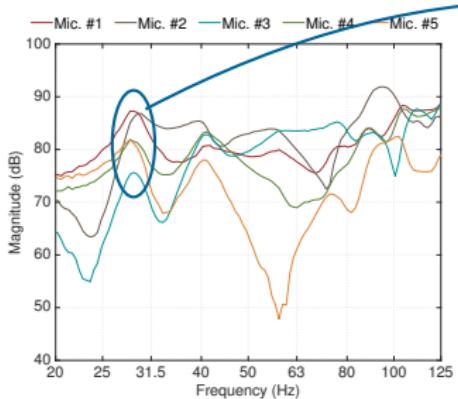
## Introduction

## Rooms at Low Frequencies



Modal decay time of mode  $n$

$$MT_{60,n} = \frac{3 \ln(10) Q_n}{\pi f_n}$$

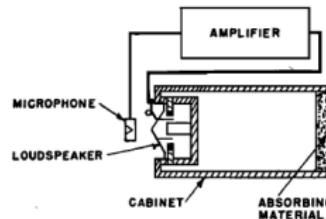


→ How to improve the listening experience in any room at low frequencies?

## Introduction

## Correction Strategies

- Active absorption



Olson and May, *J. Acoust. Am.*, 1953.

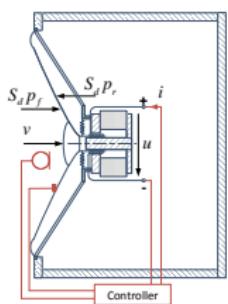
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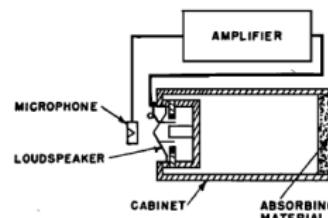
- Active absorption

→ Electroacoustic absorbers

Direct



Nicholson, *PhD thesis*, 1994



Olson and May, *J. Acoust. Am.*, 1953.

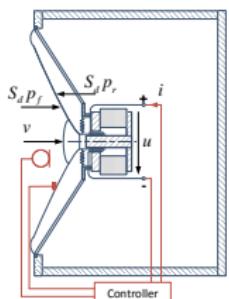
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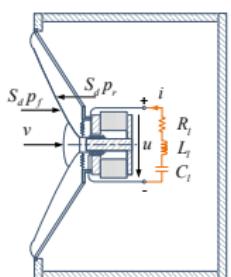
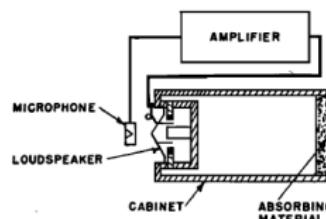
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→ Electroacoustic absorbers

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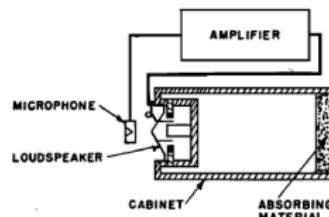
Shunt-based

Nicholson, *PhD thesis*, 1994Boulandet, *PhD thesis*, 2012Olson and May, *J. Acoust. Am.*, 1953.

## Introduction

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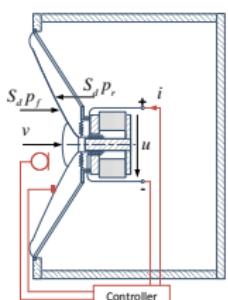
- Active absorption



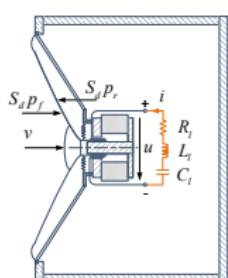
Olson and May, *J. Acoust. Am.*, 1953.

→ Electroacoustic absorbers

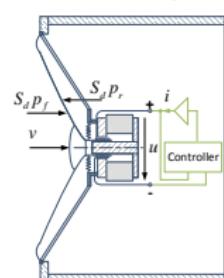
Direct



Shunt-based



Self-sensing



Nicholson, *PhD thesis*, 1994

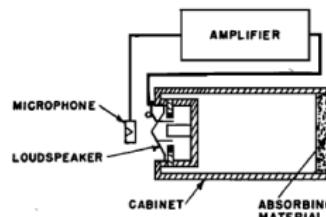
Boulandet, *PhD thesis*, 2012

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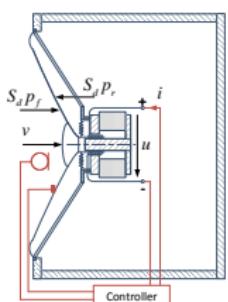
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Olson and May, *J. Acoust. Am.*, 1953.

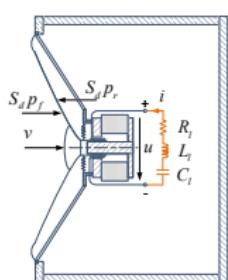
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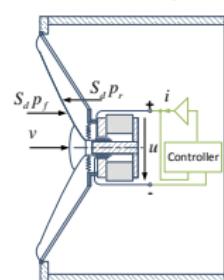
Nicholson, *PhD thesis*, 1994

Shunt-based



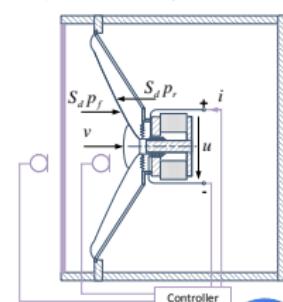
Boulandet, *PhD thesis*, 2012

Self-sensing



Boulandet, *PhD thesis*, 2012

Hybrid passive/active



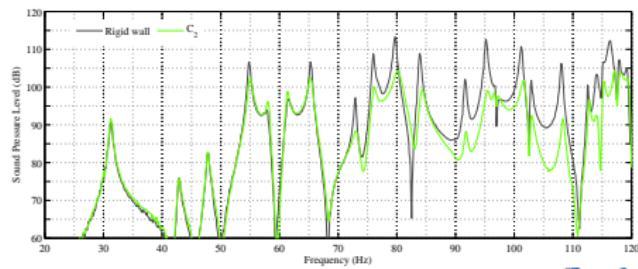
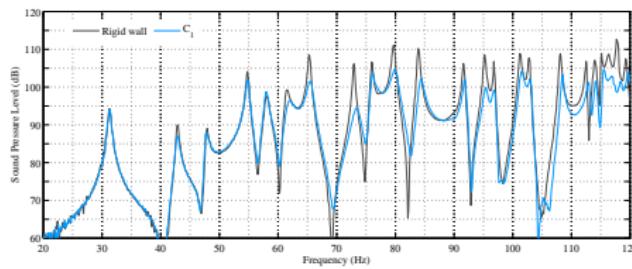
Galland et al., *Applied Acoustics*, 2005  
**MEDYNA 2017**

## Introduction

## Motivation



- Preliminary experiment with sensorless (“self-sensing”) electroacoustic absorbers in a lightly damped room  
R. Boulandet, Tunable electroacoustic resonators through active impedance control of loudspeakers, *PhD thesis No. 5331*, Ecole polytechnique fédérale de Lausanne (EPFL), 2012.



# Motivation



- Preliminary experiment with sensorless (“self-sensing”) electroacoustic absorbers in a lightly damped room  
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- Good results in highly reverberant conditions (only 0.2 m<sup>2</sup> of active area for 94.3 m<sup>2</sup> of hardwall surfaces)
- However, hardly measurable **and audible** in conventional listening rooms  
→ **need to present different acoustic resistances to each modal resonance**
- **Idea:** design passive or active methods to assign multiple target acoustic resistances as a function of frequency  
→ Multiple-Degree Of Freedom (**MDOF**) Electroacoustic Absorbers

## 1 Introduction

## 2 Electroacoustic absorbers

- (Passive) Electroacoustic absorbers principle
- Passive MDOF Electroacoustic Absorbers

## 3 Active Electroacoustic absorbers

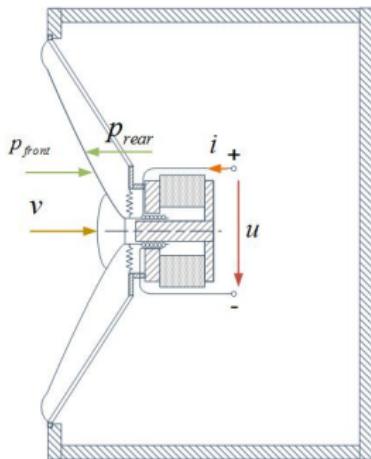
- Specific feedforward principle
- Synthesizing active MDOF Electroacoustic Absorbers

## 4 Performance Evaluation

- Assessment in an impedance tube
- Evaluation in a room

## (Passive) Electroacoustic absorbers principle

## General description



Mobile equipment:  $M_{ms}$ ,  $R_{ms}$ ,  $C_{ms}$

Moving coil:  $R_e$ ,  $L_e$

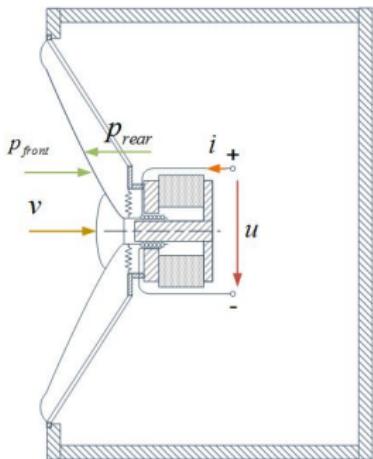
Electrodynami c transduction:  $B\ell$

Enclosure:  $V_b$

Diaphragm area:  $S_d$

## (Passive) Electroacoustic absorbers principle

## General description

Mobile equipment:  $M_{ms}$ ,  $R_{ms}$ ,  $C_{ms}$ Moving coil:  $R_e$ ,  $L_e$ Electrodynamic transduction:  $B\ell$ Enclosure:  $V_b$ Diaphragm area:  $S_d$ Newton's law on the mobile equipment  
(Laplace domain:  $s = j\omega$ )

$$Z_{ms}(s)V(s) = S_d P_{front}(s) - B\ell I(s)$$

$$\text{where } Z_{ms}(s) = sM_{ms} + R_{ms} + \frac{1}{sC_{mc}}$$

$$\text{and } C_{mc} = \frac{C_{ms} V_b}{V_b + \rho c^2 S_d^2 C_{ms}}$$

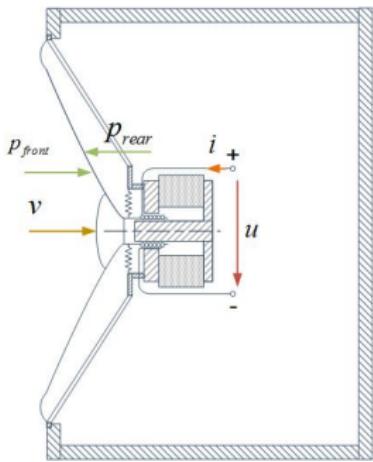
Mesh law on the electric circuit  
(Laplace domain:  $s = j\omega$ )

$$U(s) = Z_e(s)I(s) - B\ell V(s)$$

$$\text{where } Z_e(s) = sL_e + R_e$$

## (Passive) Electroacoustic absorbers principle

## General description



Newton's law on the mobile equipment  
(Laplace domain:  $s = j\omega$ )

$$Z_{ms}(s)V(s) = S_d P_{front}(s) - B\ell I(s)$$

Mesh law on the electric circuit  
(Laplace domain:  $s = j\omega$ )

$$I(s) = \frac{1}{Z_e(s)} (U(s) + B\ell V(s))$$

Mobile equipment:  $M_{ms}$ ,  $R_{ms}$ ,  $C_{ms}$

Moving coil:  $R_e$ ,  $L_e$

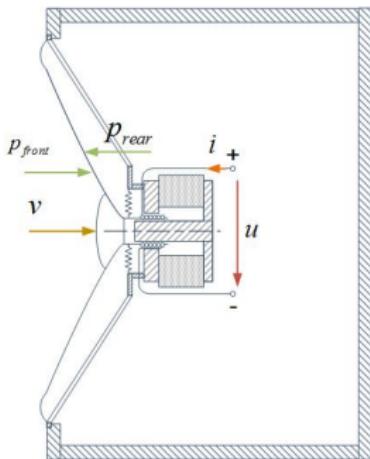
Electrodynamic transduction:  $B\ell$

Enclosure:  $V_b$

Diaphragm area:  $S_d$

## (Passive) Electroacoustic absorbers principle

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Mobile equipment:  $M_{ms}$ ,  $R_{ms}$ ,  $C_{ms}$ Moving coil:  $R_e$ ,  $L_e$ Electrodynami c transduction:  $B\ell$ Enclosure:  $V_b$ Diaphragm area:  $S_d$ 

## Newton's law on the mobile equipment

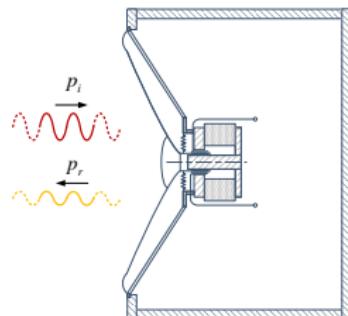
$$S_d P_{front}(s) = \left[ Z_{ms}(s) + \frac{(B\ell)^2}{Z_e(s)} \right] V(s) + \frac{B\ell}{Z_e} U(s)$$

## Diaphragm acoustic impedance

$$Z_s(s) = \frac{P_{front}(s)}{V(s)} = \left[ Z_{ms}(s) + \frac{(B\ell)^2}{Z_e(s)} \right] + \frac{B\ell}{Z_e} \frac{U(s)}{V(s)}$$

## (Passive) Electroacoustic absorbers principle

## Absorption performance

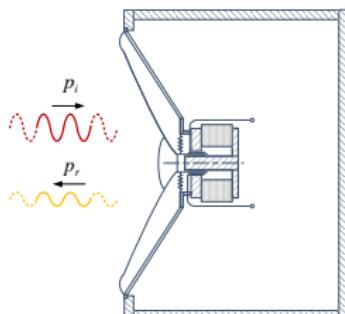


- Incident pressure  $p_i$
- Reflected pressure
$$p_r = \Gamma(s)p_i = \frac{Z_s(s) - Z_c}{Z_s(s) + Z_c} p_i$$
(under normal incidence)
- Total pressure  $p_{front} = p_i + p_r$

# Absorption performance

## Sound absorption coefficient

$$\alpha(f) = \frac{I_a}{I_i} = 1 - \left| \frac{Z_s(f) - Z_c}{Z_s(f) + Z_c} \right|^2$$

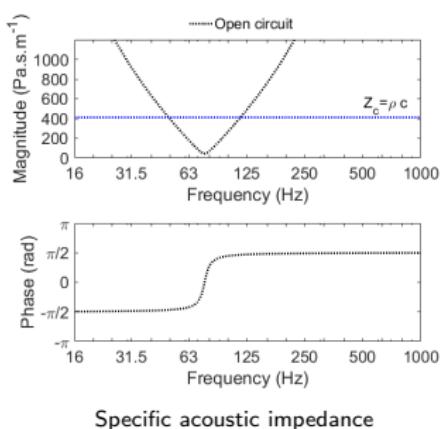
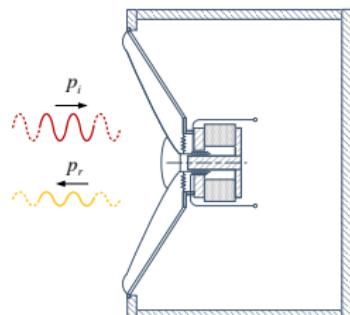


## Bandwidth of efficient sound absorption *BW*

Frequency range over which  $\frac{1}{2}\mathcal{I}_{tot} \leq \mathcal{I}_{ideal\ case}$   
 $\rightarrow \alpha_{th} \simeq 0.83$

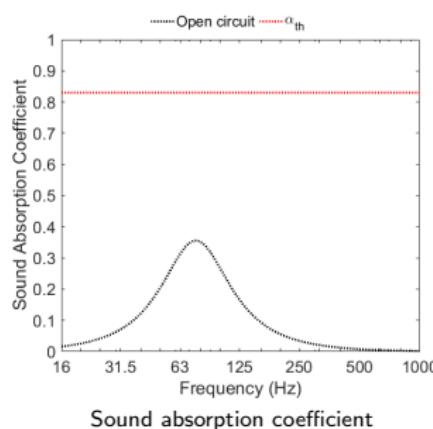
## (Passive) Electroacoustic absorbers principle

## Absorption performance



Example: open-circuit loudspeaker ( $I = 0$ )

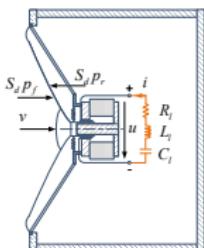
$$Z_s(s) = \frac{Z_{ms}(s)}{S_d} = \frac{1}{S_d} \left[ sM_{ms} + R_{ms} + \frac{1}{sC_{mc}} \right]$$



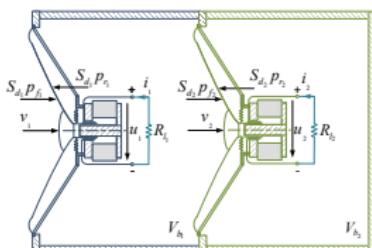
## Passive MDOF Electroacoustic Absorbers

## Designing Multiple Degree-of-Freedom Resonators

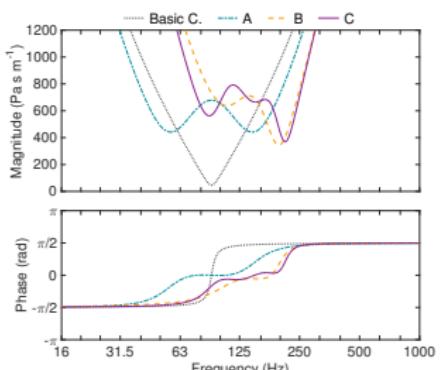
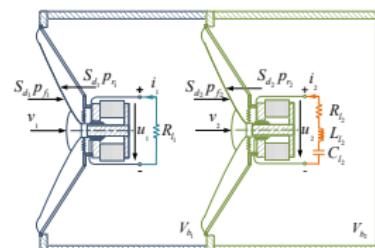
## Electrical resonator



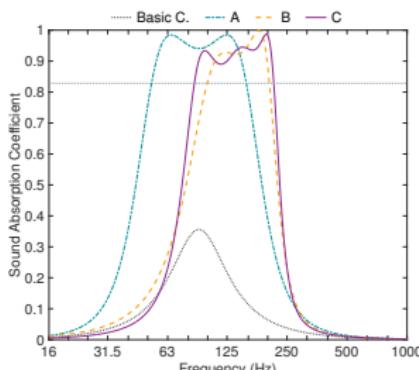
## Mechanical resonator



## Electromechanical resonator



Specific acoustic impedance



Sound absorption coefficient

## Passive MDOF Electroacoustic Absorbers

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### 3 Active Electroacoustic absorbers

- Specific feedforward principle
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Specific feedforward principle

# Hybrid Sensor-/Shunt-Based Control

## Constitutive laws

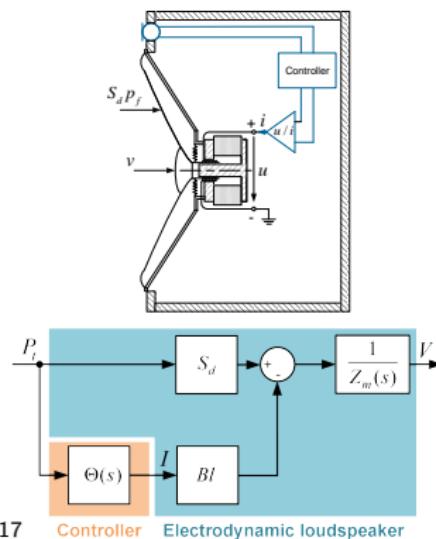
$$Z_{ms}(s)V(s) = S_d P_{front}(s) - B\ell I(s)$$

$$I(s) = \Theta(s)P_{front}(s)$$

## Acoustic impedance

$$Z_s(s) = \frac{Z_{ms}(s)}{S_d - B\ell\Theta(s)}$$

Rivet et al., *IEEE Transactions on Control Systems Technology*, 2017



## Specific feedforward principle

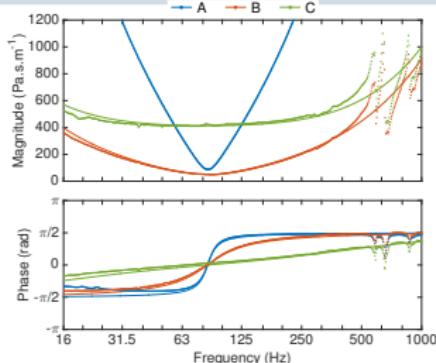
## Active 1DOF Electroacoustic Absorber

## Transfer function

$$\Theta(s) = \frac{I(s)}{P_{\text{front}}(s)} = \frac{S_d}{B\ell} \left( 1 - \frac{Z_{ms}(s)}{S_d Z_{st}(s)} \right)$$

## Target impedance

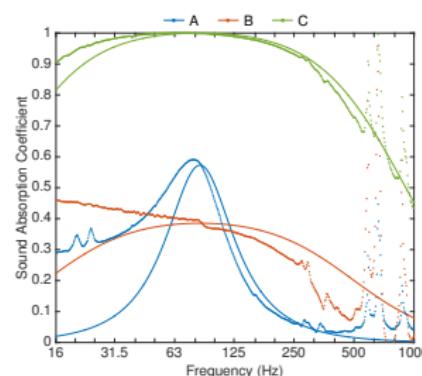
$$Z_{st}(s) = s \frac{M_{ms}}{S_d \nu_1} + R_{st} + \frac{1}{s S_d \nu_2 C_{mc}}$$



Sound absorption coefficient

Rivet et al., IEEE Transactions on Control Systems Technology, 2017

| Case | $\nu_1 = \nu_2$ | $R_{st}$     |
|------|-----------------|--------------|
| A    | 1               | $R_{ms}/S_d$ |
| B    | 6               | $\rho c/8$   |
| C    | 6               | $\rho c$     |



Specific acoustic impedance

# Active MDOF Electroacoustic Absorber

## Transfer function

$$\Theta(s) = \frac{I(s)}{P_{front}(s)} = \frac{S_d}{B\ell} \left( 1 - \frac{Z_{ms}(s)}{S_d Z_{st,nDOF}(s)} \right)$$

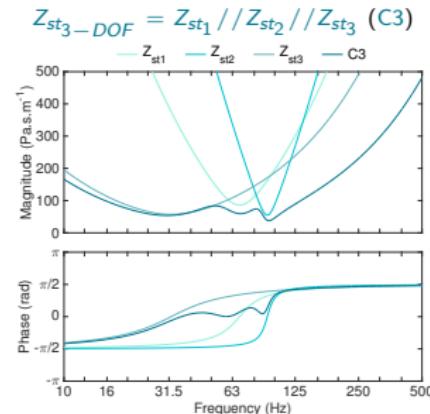
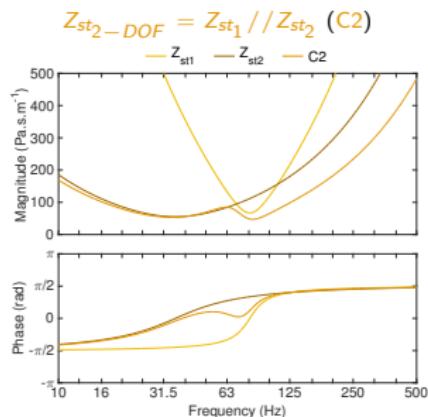
## MDOF target impedance

$$Z_{st,nDOF}(s) = \frac{1}{\sum_{k=1}^n \frac{1}{s \frac{M_{ms}}{S_d \nu_{2k-1}} + R_{st,k}} + \frac{1}{s S_d \nu_{2k} C_{mc}}}$$

- $R_{st,k}$ : target acoustic resistances
- $\nu_i$ : real coefficients, allowing adjusting the resonance frequency of each 1DOF impedance in the summation.

## Synthesizing active MDOF Electroacoustic Absorbers

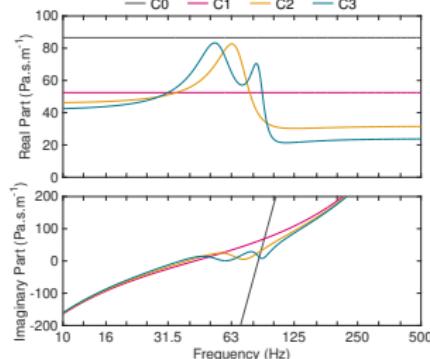
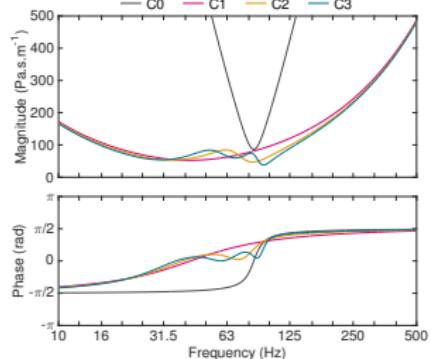
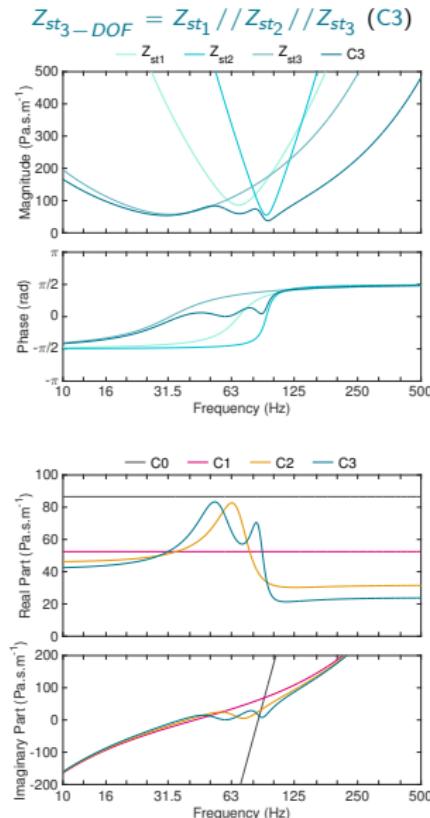
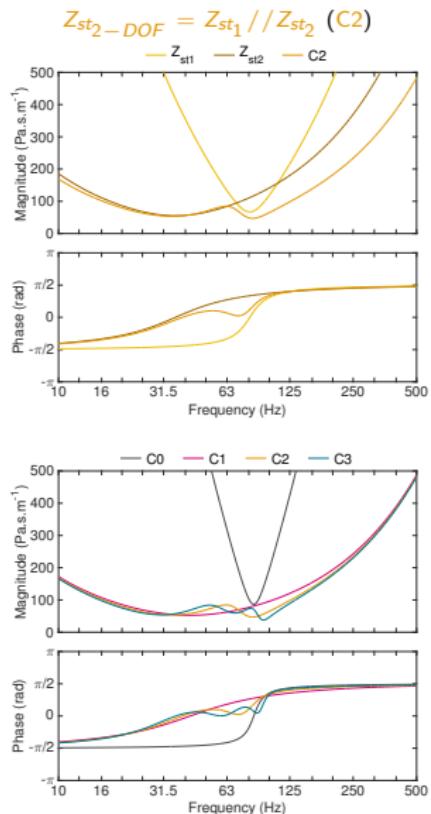
## Simulations



|    | $Z_{st_1}$     |  |                | $Z_{st_2}$     |  |                | $Z_{st_3}$     |  |                |
|----|----------------|--|----------------|----------------|--|----------------|----------------|--|----------------|
|    | $\nu_1$<br>(-) | $R_{st_1}$<br>( $\text{Pa}\cdot\text{s}\cdot\text{m}^{-1}$ ) | $\nu_2$<br>(-) | $\nu_3$<br>(-) | $R_{st_2}$<br>( $\text{Pa}\cdot\text{s}\cdot\text{m}^{-1}$ ) | $\nu_4$<br>(-) | $\nu_5$<br>(-) | $R_{st_3}$<br>( $\text{Pa}\cdot\text{s}\cdot\text{m}^{-1}$ ) | $\nu_6$<br>(-) |
| C0 | 1.00           | $R_{ms}/S_d$   | 1.00           | -              | -  | -              | -              | -  | -              |
| C1 | 6.25           | 52.20  | 25.00          | -              | -  | -              | -              | -  | -              |
| C2 | 2.16           | 67.01  | 2.36           | 4.09           | 55.24  | 22.64          | -              | -  | -              |
| C3 | 1.86           | 85.99  | 2.86           | 1.32           | 54.81  | 1.11           | 3.07           | 57.32  | 21.03          |

## Synthesizing active MDOF Electroacoustic Absorbers

## Simulations



## Synthesizing active MDOF Electroacoustic Absorbers

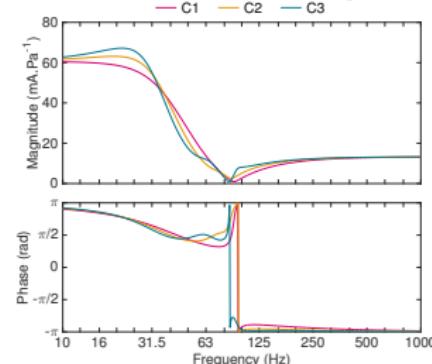
## Simulations

## Transfer function

$$\Theta(s) = \frac{I(s)}{P_{front}(s)} = \frac{S_d}{B\ell} \left( 1 - \frac{Z_{ms}(s)}{S_d Z_{st,nDOF}(s)} \right)$$

## MDOF target impedance

$$Z_{st,nDOF}(s) = \frac{1}{\sum_{k=1}^n \frac{1}{s S_d \nu_{2k-1}} + R_{st_k} + \frac{1}{s S_d \nu_{2k} C_{mc}}}$$

Controller  $\Theta$  Bode Diagram

- $R_{st_k}$ : target acoustic resistances
- $\nu_i$ : real coefficients, allowing adjusting the resonance frequency of each 1DOF impedance in the summation.

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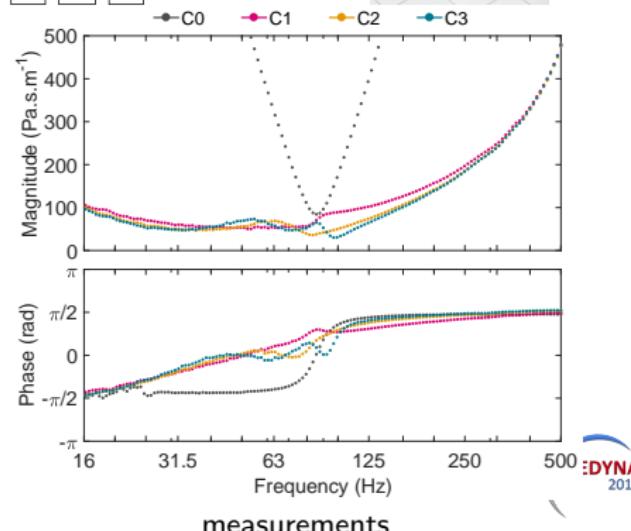
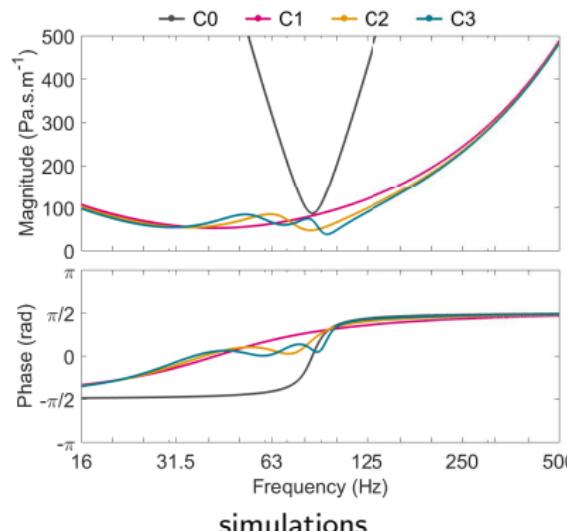
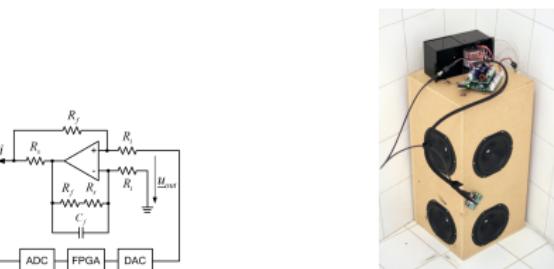
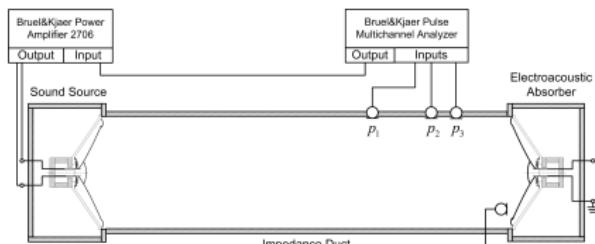
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- Assessment in an impedance tube
- Evaluation in a room

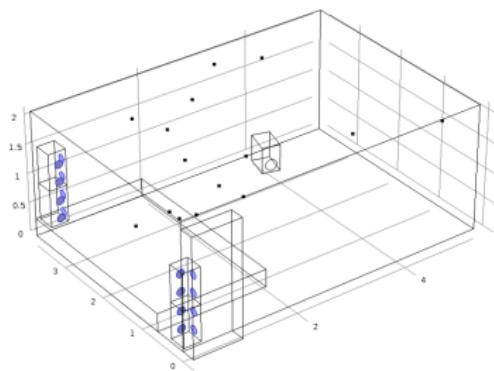
## Assessment in an impedance tube

## Experimental Setup: Impedance tube (ISO 10534-2 standard)

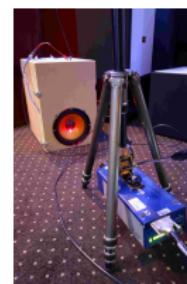


Evaluation in a room

## Experimental Setup: Small Room

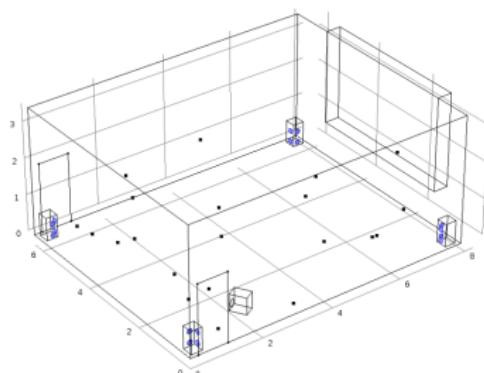


floor area =  $20.04 \text{ m}^2$ , volume =  $42.69 \text{ m}^3$

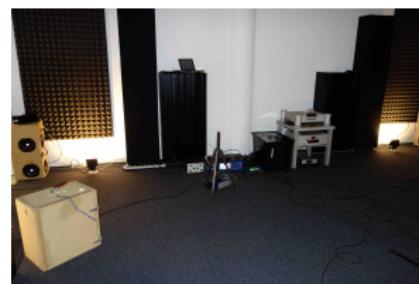


Evaluation in a room

## Experimental Setup: Medium Room



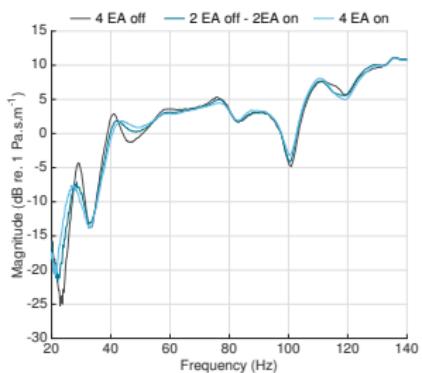
floor area =  $50.05 \text{ m}^2$ , volume =  $174.18 \text{ m}^3$



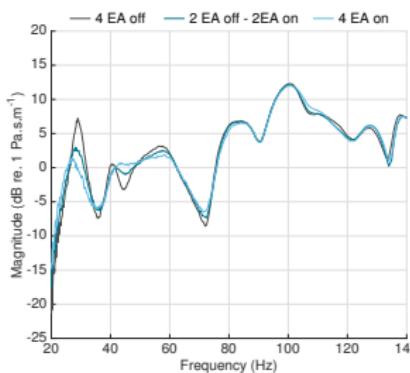
Evaluation in a room

## Modal Equalisation: Small Room

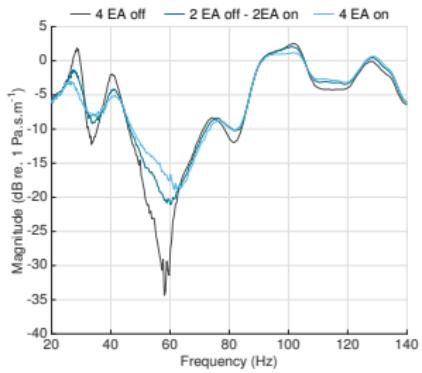
Mic #1



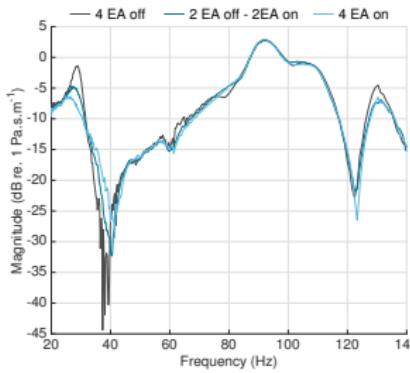
Mic #2



Mic #3



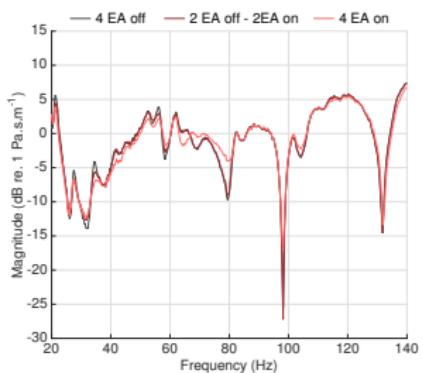
Mic #4



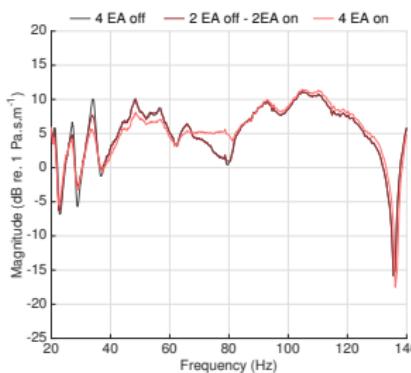
Evaluation in a room

## Modal Equalisation: Medium Room

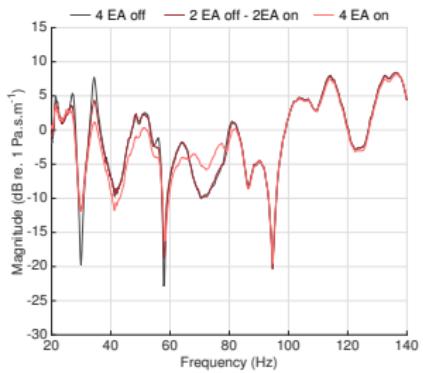
Mic #1



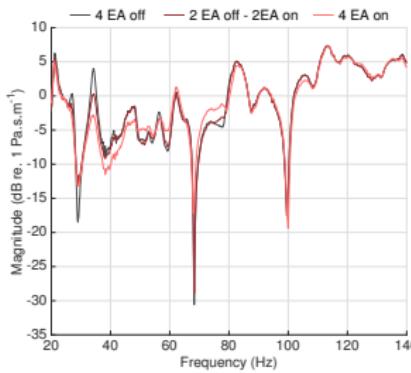
Mic #2



Mic #3



Mic #4

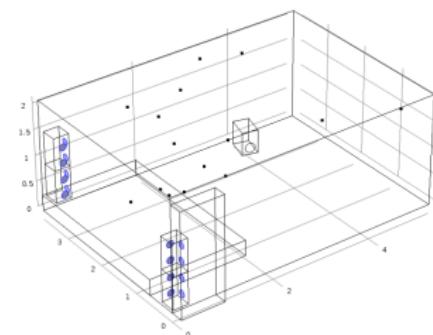
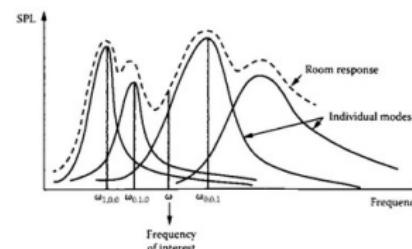
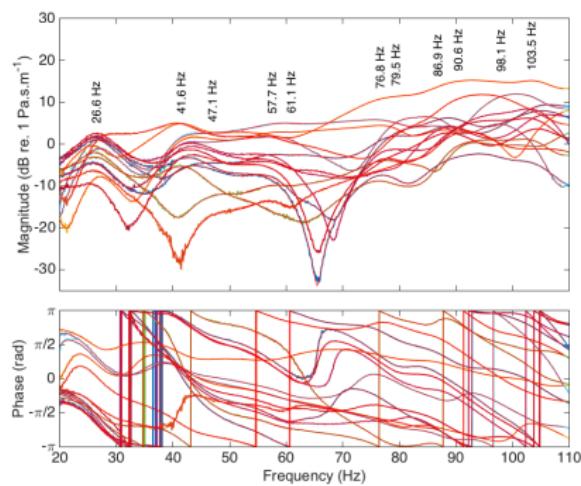


Evaluation in a room

# Decrease of Modal Decay Times

## Modal decay time of mode $n$

$$MT_{60,n} = \frac{3 \ln(10) Q_n}{\pi f_n}$$

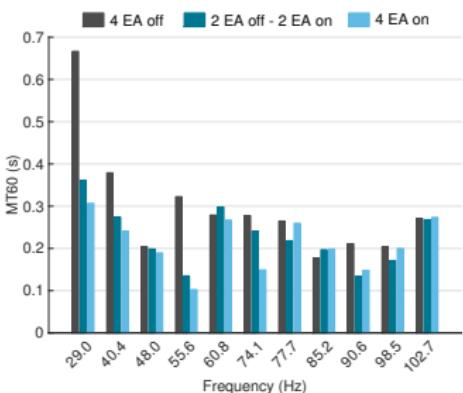


M. H. Richardson, D. L. Formenti, "Global curve fitting of frequency response measurements using the rational fraction polynomial method." *Proceedings of the Third International Modal Analysis Conference*, 1985.

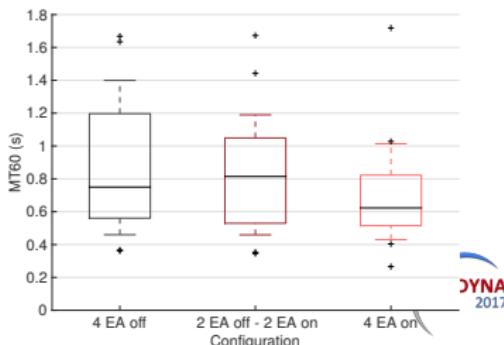
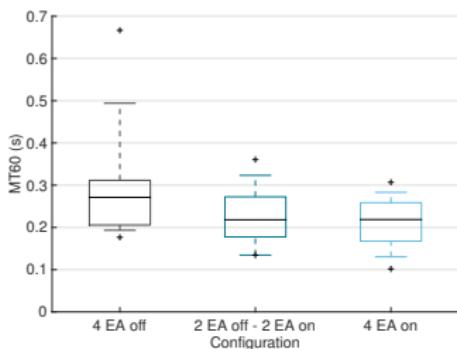
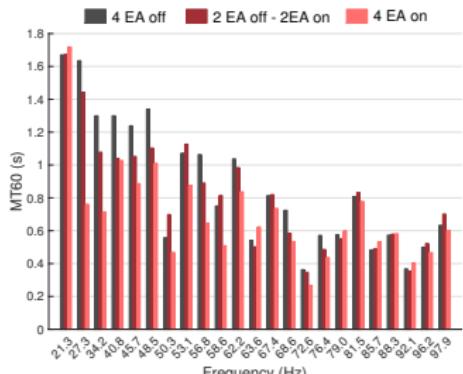
## Evaluation in a room

## Decrease of Modal Decay Times

Small room



Medium room

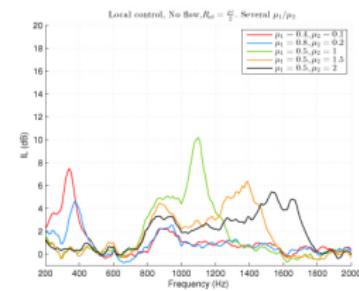
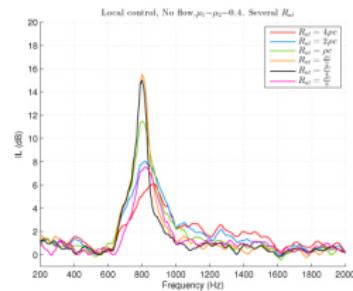


## Summary of results

- Design guidelines for setting electroacoustic absorbers
  - Impedance control through multiple degree-of-freedom resonators
  - Hybrid sensor-/shunt-based impedance control
- Performance optimisation
  - Definition of new performance metrics:  $MT_{60}$
  - Specify varying acoustic resistances as a function of frequency (not presented here)
- Performance evaluation for modal equalisation
  - Development of demonstration prototypes
  - Objective evaluation in real rooms
  - Subjective evaluation of music playback in rooms (not presented here)

# Other applications

- Ongoing work on active liners for aircraft engine noise reduction
- Assessed array of  $3 \times 10$  small loudspeakers ( $5 \text{ cm} \times 5 \text{ cm} \times 8 \text{ cm}$ )
- Achievement of 15 dB IL at the natural resonance frequency of the loudspeakers
- Possibility to adapt the frequency depending on the aircraft engine regime



# Perspectives

- Absorber design
  - Ratio surface/mass
  - Active panels controlled by electrodynamic inertial actuators
  - Development of electroacoustic absorption-diffusion systems
- Performance optimisation
  - Target impedance (reactive terms in simulations)
  - Calibration of electroacoustic absorbers directly in the room
- Performance evaluation
  - Spatial sound field reconstruction (compressive sensing)

## Thank you for your Attention

- This research was supported by the Swiss Commission for Technology and Innovation (CTI) under the project INTERACTS, grant agreement no. 14220.1 PFNM-NM, in collaboration with:
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  - Relec S.A. (Yverdon, Switzerland)
  - Goldmund International (Plan-les-Ouates, Switzerland)
- Etienne Rivet PhD Thesis No. 7166 is accessible online  
<https://infoscience.epfl.ch/record/222866>