## Modeling a Waste Disposal Process via a Discrete Mixture of Count Data Models

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## Overview

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## Efficient collection of recyclables in Geneva



## In more detail...

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- Vehicles are dispatched to carry out the daily schedules produced by the routing algorithm
- Efficient waste collection thus depends on the ability to:
- make good forecasts of the container levels at the time of collection
- and optimally route the vehicles to service the selected containers
- In this talk we will focus on the first part, i.e. short-term operational container level forecasting



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## Routing problem illustration

- The routing problem was presented at STRC 2014 (Markov et al., 2014)
- It is a rich VRP with intermediate facilities, which integrates:
- a heterogeneous fixed fleet with fixed and vairable costs
- a flexible assignment of start and end depot
- The constraints and features are inspired by practical applications to collectors in Switzerland and France



## Solution and results

- The problem was modeled as a MILP
- It was solved using a local search algorithm
- Applied to a set of executed tours for collecting white glass and PET in Geneva, it reduced travel distance by $15 \%$ on average

Figure 2: Executed vs. optimized tours in Geneva


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## Literature

- The literature on waste generation forecasting is abundant and varied (for a survey see Beigl et al., 2008)
- Much of it is focused on city and regional level: Tainan, Taiwan (Chen and Chang, 2000); San Antonio, US (Dyson and Chang, 2005); Beijing, China (Li et al., 2011), etc...


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- And a fairly small amount on the container (micro) level, e.g.:
- Inventory levels in pharmacies (Nolz et al., 2011, 2014)
- Recyclable materials from old cars (Krikke et al., 2008)
- Charity donation banks (McLeod et al., 2013)
- Waste container levels (Johansson, 2006; Faccio et al., 2011; Mes, 2012; Mes et al., 2014)


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- Charity donation banks (McLeod et al., 2013)
- Waste container levels (Johansson, 2006; Faccio et al., 2011; Mes, 2012; Mes et al., 2014)
- Contribution:
- Operational container level forecasting
- We develop a forecasting model estimated and validated on real data, whereas most of the container level literature is focused on critical levels. Moreover, much of it uses simulated data.


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## Data preparation

- Container levels are:
- detected by internal ultrasound sensors
- periodically transmitted to a central database
- post-processed for noise removal
- extrapolated at the end of each date
- Let $L_{i, t}$ denote the level of container $i$ at the end of date $t$
- Let $C_{i}$ denote the usable capacity of container $i$
- Then the observed quantity deposited in container $i$ at date $t$ is:

$$
\begin{equation*}
Q_{i, t}=C_{i}\left(L_{i, t}-L_{i, t-1}\right) \tag{1}
\end{equation*}
$$

- In case there was an emptying event at date $t$, we have:

$$
\begin{equation*}
Q_{i, t}=C_{i} L_{i, t} \tag{2}
\end{equation*}
$$

## Formulation

- Let $n_{i, t, k}$ denote the number of deposits in container $i$ at date $t$ of size $q_{k}$. We define the data generating process as follows:

$$
\begin{equation*}
Q_{i, t}^{\star}=\sum_{k=1}^{K} n_{i, t, k} q_{k} \tag{3}
\end{equation*}
$$

- Let $n_{i, t, k} \xrightarrow{\text { iid }} \mathcal{P}\left(\lambda_{i, t, k}\right)$ with probability $\pi_{i, t, k}$. Then we obtain:

$$
\begin{equation*}
\mathbb{E}\left(Q_{i, t}^{\star}\right)=\sum_{k=1}^{K} q_{k} \lambda_{i, t, k} \pi_{i, t, k} \tag{4}
\end{equation*}
$$

- We minimize the sum of squared differences between observed and expected over all containers and dates:

$$
\begin{equation*}
\min _{\lambda, \pi} \sum_{i=1}^{N} \sum_{t=1}^{T}\left(Q_{i, t}-\sum_{k=1}^{K} q_{k} \lambda_{i, t, k} \pi_{i, t, k}\right)^{2} \tag{5}
\end{equation*}
$$

assuming strict exogeneity

## Formulation

- Given vectors of covariates $\mathbf{x}_{i, t}$ and $\mathbf{z}_{i, t}$ and vectors of parameters $\boldsymbol{\beta}_{k}$ and $\gamma_{k}$, we define Poisson rates and logit-type probabilities:

$$
\begin{array}{r}
\lambda_{i, t, k}(\boldsymbol{\theta})=\exp \left(\mathbf{x}_{i, t}^{\top} \boldsymbol{\beta}_{k}\right) \\
\pi_{i, t, k}(\boldsymbol{\theta})=\frac{\exp \left(\mathbf{z}_{i, t}^{\top} \boldsymbol{\gamma}_{k}\right)}{\sum_{j=1}^{K} \exp \left(\mathbf{z}_{i, t}^{\top} \gamma_{j}\right)} \tag{7}
\end{array}
$$

- Then, in compact form, the minimization problem writes as:

$$
\begin{equation*}
\min _{\boldsymbol{\theta} \in \boldsymbol{\Theta}} \sum_{i=1}^{N} \sum_{t=1}^{T}\left(Q_{i, t}-\sum_{k=1}^{K} \frac{\exp \left(\mathbf{x}_{i, t}^{\top} \boldsymbol{\beta}_{k}+\mathbf{z}_{i, t}^{\top} \gamma_{k}+\ln \left(q_{k}\right)\right)}{\sum_{j=1}^{K} \exp \left(\mathbf{z}_{i, t}^{\top} \gamma_{j}\right)}\right)^{2} \tag{8}
\end{equation*}
$$

- $\boldsymbol{\Theta}:=\left(\boldsymbol{\beta}_{k}, \gamma_{k}: \forall k\right)$, and $\gamma_{k^{\star}}=\mathbf{0}$ for one arbitrarily chosen $k^{\star}$
- We will refer to this minimization problem as the mixture model


## Formulation

- In case of only one deposit quantity, it degenerates to a pseudo-count data process:

$$
\begin{equation*}
\min _{\boldsymbol{\theta} \in \Theta} \sum_{i=1}^{N} \sum_{t=1}^{T}\left(Q_{i, t}-\exp \left(\mathbf{x}_{i, t}^{\top} \boldsymbol{\beta}+\ln (q)\right)\right)^{2} \tag{9}
\end{equation*}
$$

- We will refer to this minimization problem as the simple model


## Forecasting

- Using new sets of covariates $\dot{\mathbf{x}}_{i, t}$ and $\dot{\mathbf{z}}_{i, t}$, and the estimates $\hat{\boldsymbol{\beta}}_{k}$ and $\hat{\gamma}_{k}$, we can generate a forecast as follows:

$$
\begin{equation*}
\dot{Q}_{i, t}=\sum_{k=1}^{K} \frac{\exp \left(\dot{\mathbf{x}}_{i, t}^{\top} \hat{\boldsymbol{\beta}}_{k}+\dot{\mathbf{z}}_{i, t}^{\top} \hat{\gamma}_{k}+\ln \left(q_{k}\right)\right)}{\sum_{j=1}^{K} \exp \left(\dot{\mathbf{z}}_{i, t}^{\top} \hat{\gamma}_{j}\right)} \tag{10}
\end{equation*}
$$

- Given the operational nature of the problem, the covariates should be quick and easy to obtain
- Examples include days of the week, months, weather data, holidays, etc...


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## Data

- 36 containers for PET in the canton of Geneva with capacity of 3040 or 3100 liters
- Balanced panel covering March to June, 2014 (122 days), which brings the total number of observations to 4392
- The final sample excludes unreliable level data (removed after visual inspection)
- Missing data is linearly interpolated for the values of $Q_{i, t}$


## Residual plots

Figure 3: Residual plot of the mixture model


Figure 4: Residual plot of the simple model


## Seasonality pattern

- Waste generation exhibits strong weekly seasonality
- Peaks are observed during the weekends
- There also appear to be longer-term effects for months

Figure 5: Mean daily volume deposited in the containers


- Mean daily volume


## Covariates

- Based on the above observations, we use the following covariates
- They are all used both for $\mathbf{x}_{i, t}$ (rates) and $\mathbf{z}_{i, t}$ (probabilities)

Table 1: Table of covariates

| Variable | Type |
| :--- | :--- |
| Container fixed effect | dummy |
| Day of the week | dummy |
| Month | dummy |
| Minimum temperature in Celsius | continuous |
| Precipitation in mm | continuous |
| Pressure in hPa | continuous |
| Wind speed in kmph | continuous |

## Evaluating the fits

- Coefficient of determination

$$
\begin{equation*}
R^{2}=1-\frac{S S_{\mathrm{res}}}{S S_{\mathrm{tot}}} \tag{11}
\end{equation*}
$$

with higher values for a better model

- Akaike information criterion (AIC):

$$
\begin{equation*}
\mathrm{AIC}=\left(\frac{S S_{\mathrm{res}}}{N}\right) \exp (2 K / N) \tag{12}
\end{equation*}
$$

with lower values for a better model. The exponential penalizes model complexity

- $S S_{\text {res }}$ is the residual sum of squares
- $S S_{\text {tot }}$ is the total sum of squares
- $K$ is the number of estimated parameters
- $N$ is the number of observations


## Estimation on full sample

- Mixture model: $R^{2}$ of 0.341 (AIC 52900)
- Simple model: $R^{2}$ of 0.300 (AIC 53700)

Table 2: Estimated coefficients of mixture model

|  | $\hat{\boldsymbol{\beta}}_{1}(5 \mathrm{~L})^{* * *}$ | $\hat{\boldsymbol{\beta}}_{2}(15 \mathrm{~L})^{* * *}$ | $\hat{\boldsymbol{\gamma}}_{2}{ }^{* * *}$ |
| :--- | ---: | ---: | ---: |
| Minimum temperature in Celsius | 1461.356 | 0.022 | -0.037 |
| Precipitation in mm | -0.821 | -0.009 | 0.018 |
| Pressure in hPa | -13.724 | -0.001 | 0.010 |
| Wind speed in kmph | 7.580 | -0.004 | 0.020 |
| Monday | 402.235 | 2.166 | -9.693 |
| Tuesday | 1908.233 | 2.293 | -9.977 |
| Wednesday | -844.662 | 1.432 | 0.202 |
| Thursday | 1937.385 | 1.198 | 1.453 |
| Friday | 1876.162 | 1.239 | 4.419 |
| Saturday | -6981.339 | 1.358 | 4.723 |
| Sunday | 1831.715 | 1.905 | 2.832 |
| March | -27.136 | 2.955 | -1.453 |
| April | 1071.406 | 2.746 | -1.532 |
| May | 1689.979 | 2.988 | -1.603 |
| June | -2604.520 | 2.901 | -1.452 |

## Validation

- We performed 50 experiments
- Both the mixture and the simple model are estimated on a random sample of $90 \%$ of the panel
- They are validated on the remaining $10 \%$
- It was made sure that all containers and all months appeared in the random samples

Table 3: Mean $R^{2}$ for estimation and validation sets

|  | Mixture model mean $R^{2}$ | Simple model mean $R^{2}$ |
| :--- | ---: | ---: |
| Estimation | 0.364 (AIC 51400) | 0.302 (AIC 53600) |
| Validation | 0.286 | 0.274 |

## Validation

Figure 6: Histograms for estimation and validation samples



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## Conclusion

- Mixture model representing the data generating process of a realistic underlying behavior
- Preliminary testing shows its better in- and out-of-sample performance
- Future research will focus on:
- reformulating the objective function as a likelihood function
- testing a higher number if discrete deposit sizes
- and a continuous distribution of the deposit size
- integrating the forecasting approach and the vehicle routing algorithm into an inventory routing platform


## Thank you for your attention! Questions?

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