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# Pedestrian flow characteristics based on individual trajectories

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# Content

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- Interest & Motivation
- Methodology
- Preliminary results
- Conclusions and future work

# Interest & motivation

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- Mathematical modeling of pedestrian dynamics
- Understanding and predicting the evolution of pedestrians
  - Efficient design of new facilities
  - Large events gathering a high number of people
  - Travel guidance
  - **Congestion**

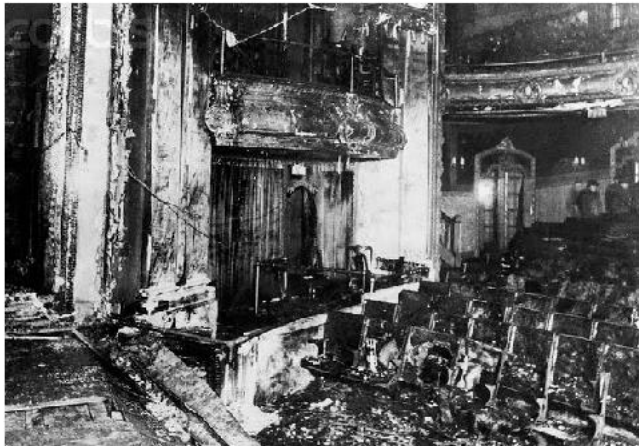
# Evacuation

**More Than 950 Iraqis Die in Stampede on Baghdad Bridge**



*The New York Times*

Iroquois Theatre fire, 605 people died



WIKIPEDIA  
The Free Encyclopedia

1989: Football fans crushed at Hillsborough



BBC News

# Congestion

## *Lausanne railway station*



# Related work

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- Modeling approaches inspired by physics, artificial intelligence, biology, traffic flow theory
- Microscopic vs. macroscopic
  - Social force model (Helbing and Molnár, 1995)
  - Continuum models (Hughes, 2002)
- Aggregated vs. disaggregated
  - Social force model; Queuing model (Løvås, 1994)
  - Discrete choice models (Antonini et al., 2006)
- Discrete vs. continuous
  - Cellular automata (Blue and Adler, 2001)
  - Continuum models (Hughes, 2002)
  - ...

Missing – detailed representation of congestion based on recent data

# Strategy

## *Step by step*

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- Evaluation of data potential
- Good estimation of congestion indicators
  - Density, flow, speed

# Strategy

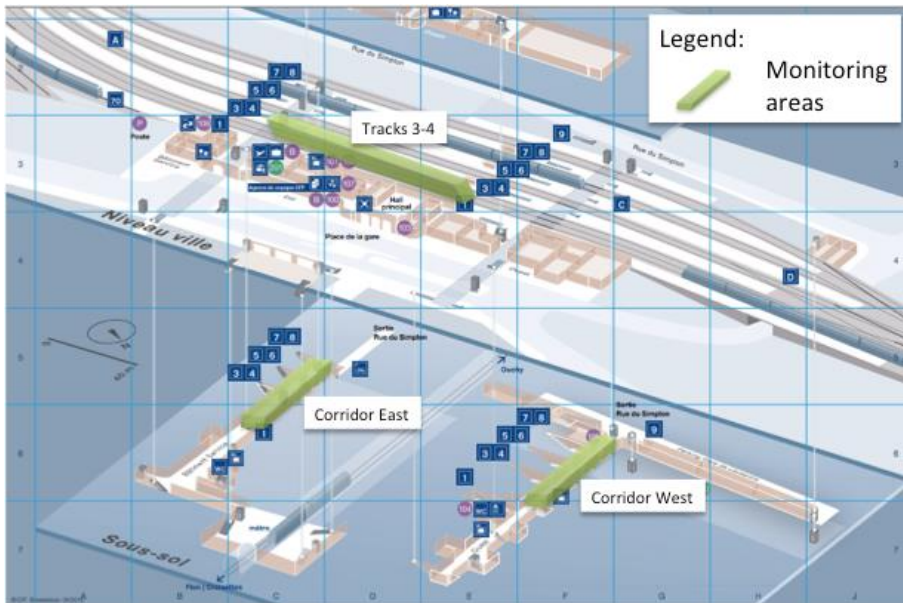
## *Step by step*

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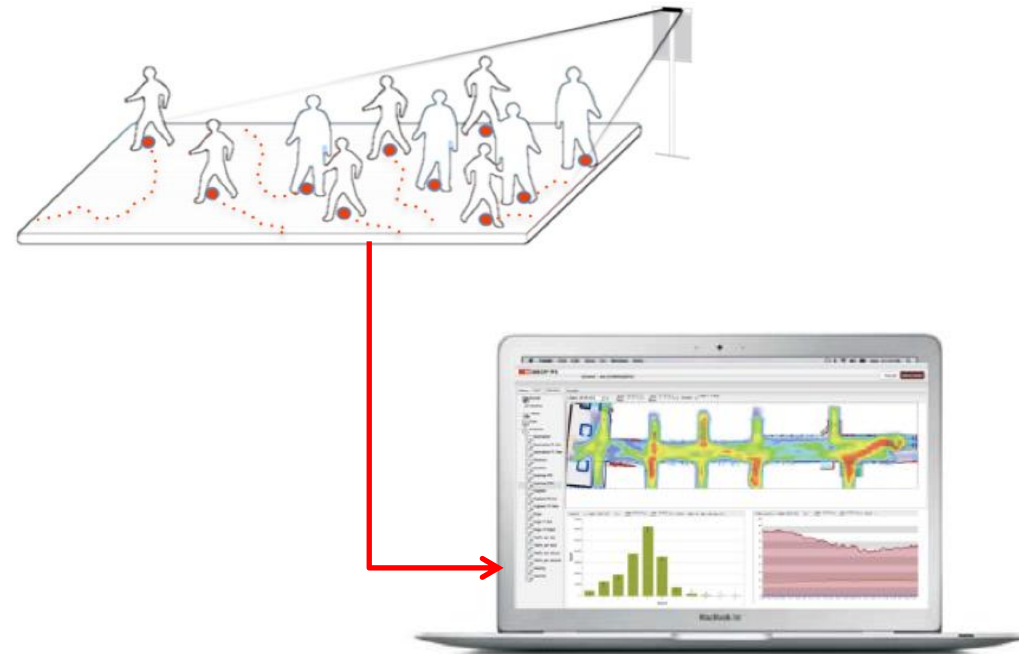
- **Evaluation of data potential**
- Good estimation of congestion indicators
  - Density, flow, speed



# Data collection



Source: (Alahi et al., 2013)



- 76 smart sensors capture flow at Lausanne train station
  - Corridors West (PIW) and East (PIE)
  - Tracks 3-4

- People are automatically:
  - Located in 3D
  - Tracked across time

# Data potential

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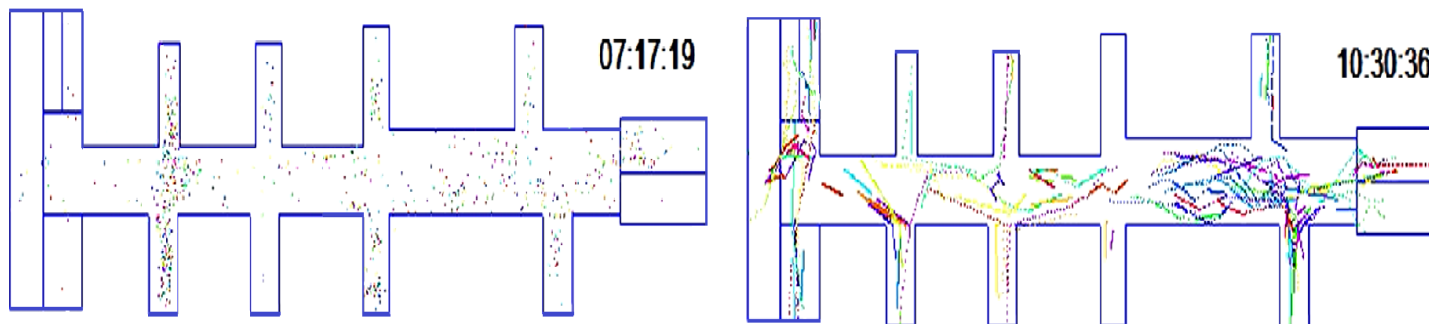
- Trajectory

*[time, x, y, pedestrian<sub>id</sub>]*

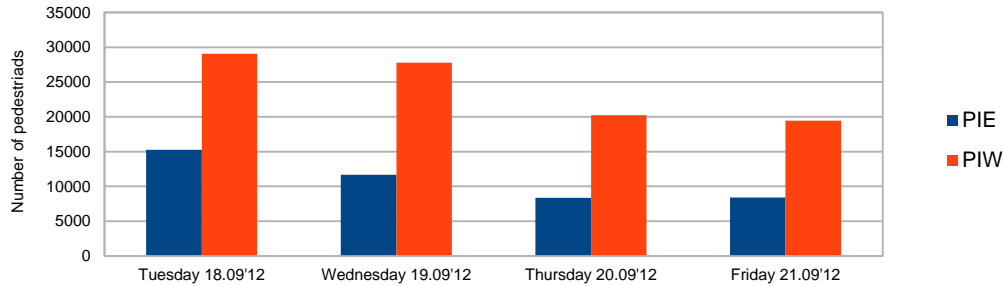
- Describe the essential parts of the pedestrian motion behavior
  - Interaction with moving and static objects (other pedestrians, obstacles)
  - Collective behavior and self-organization of pedestrian groups
  - Flow characteristics
- Model calibration and validation

# Exploratory data analysis

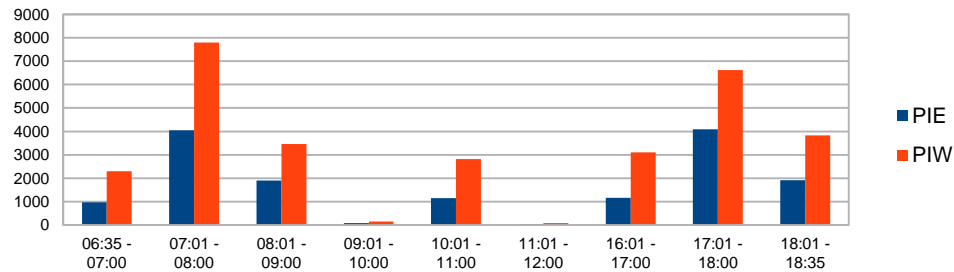
- Time-space patterns
- Qualitative analysis
  - Visualization tool
  - Macroscopic and microscopic aspects
- Quantitative analysis
  - Effects of congestion on pedestrian dynamics
  - Effects of different spatial aggregation levels on observables



# Critical time periods

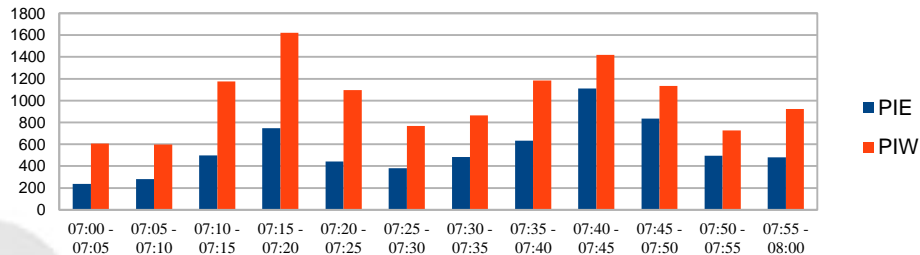


Decrease in traffic over the week days for PIE and PIW  
Higher rate of traffic observed for PIW



Two critical periods of time:

- 7am - 8am
- 5pm - 6pm

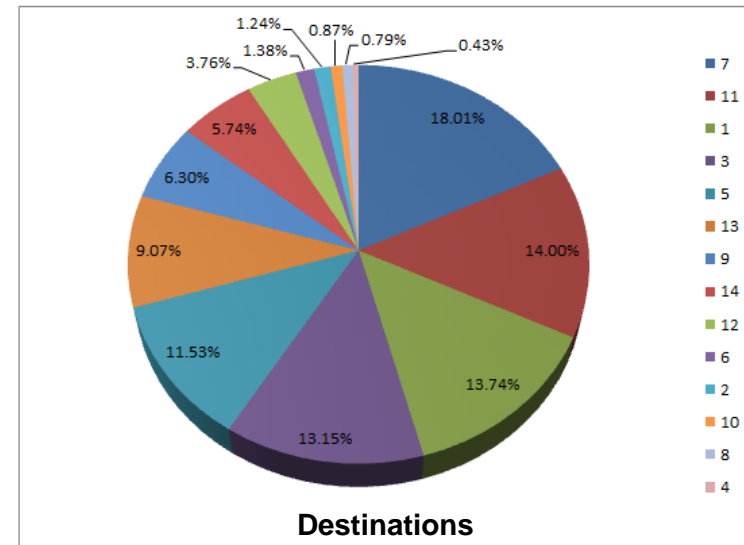
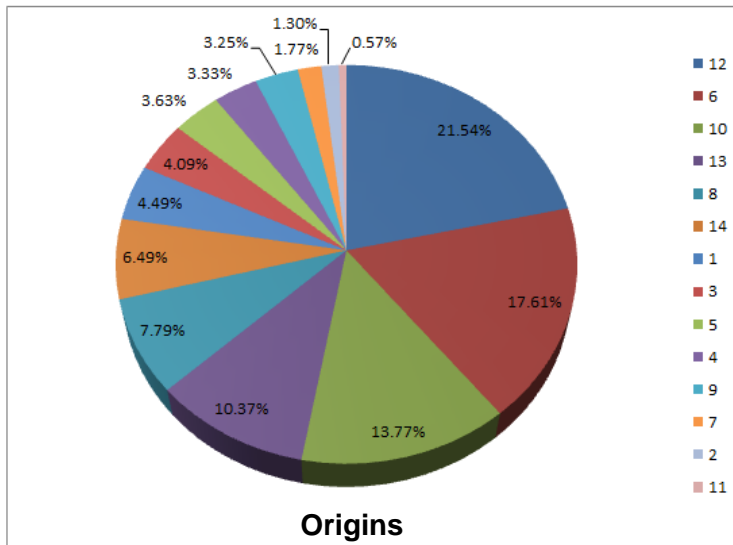
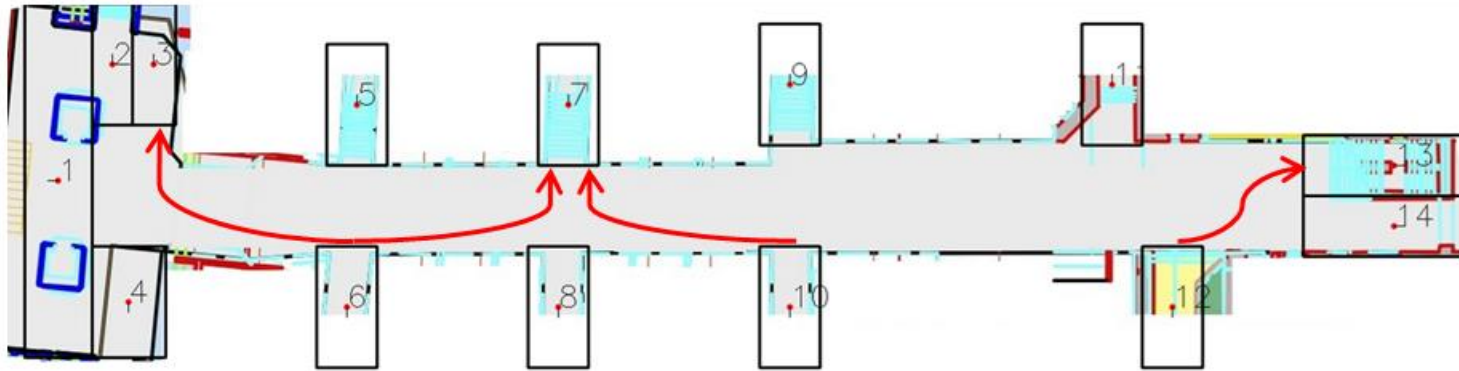


The most critical time:

- From 7:10 am to 7:25 am
- From 7:35 am to 7:50 am

# Frequently used paths and areas

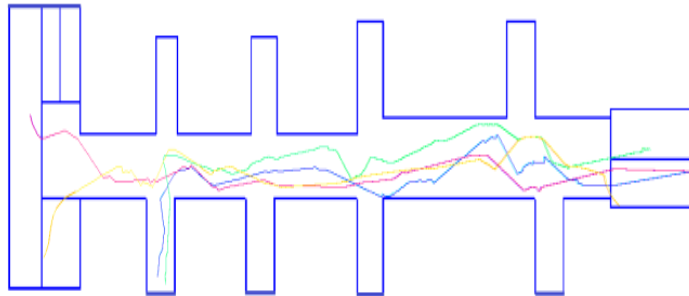
*PIW - peak day*



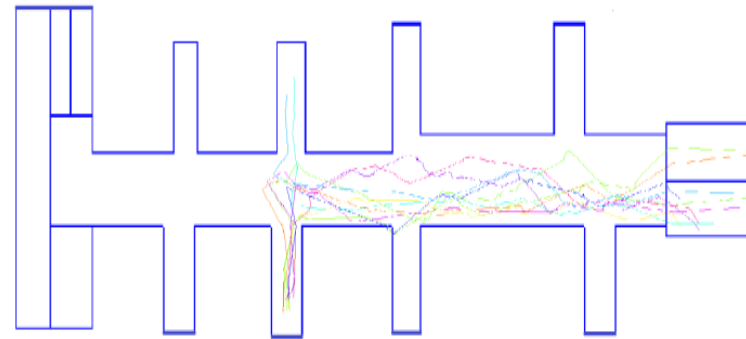
# Qualitative data analysis

## *Microscopic*

### PIW corridor

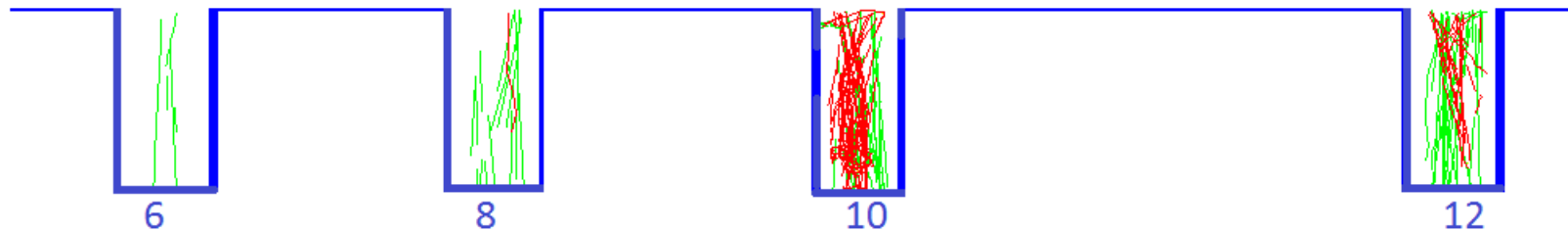


18.09.2012. 10:30-10:32



18.09.2012. 07:16-07:18

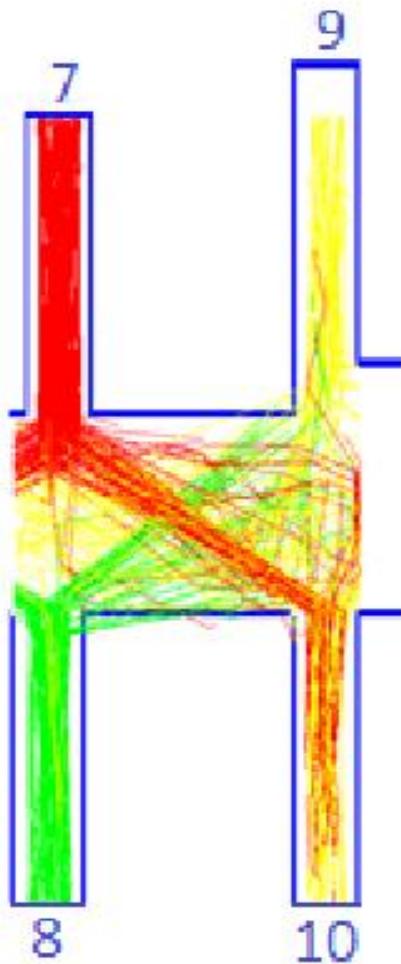
### PIW stairs/ramps



# Qualitative data analysis

## *Macroscopic*

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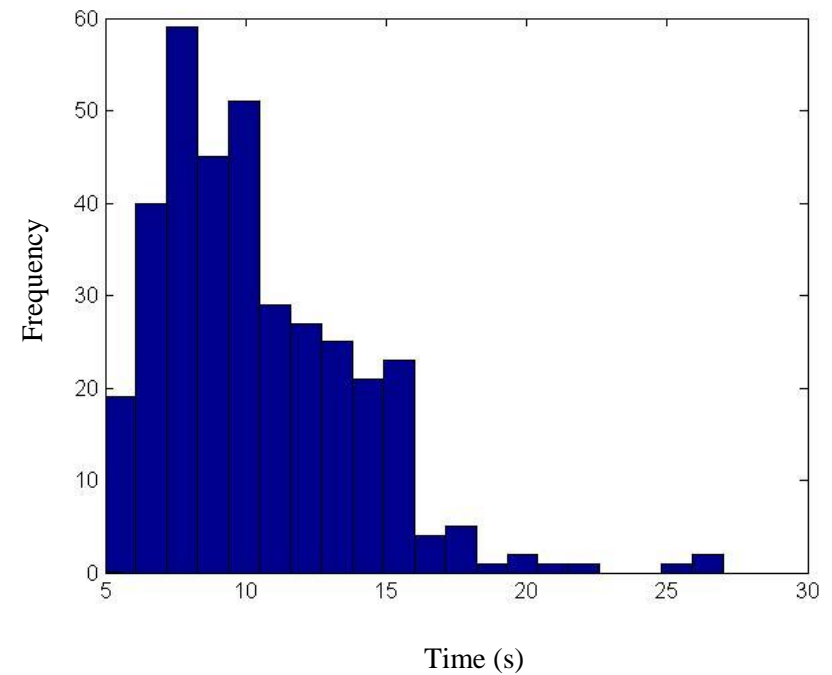
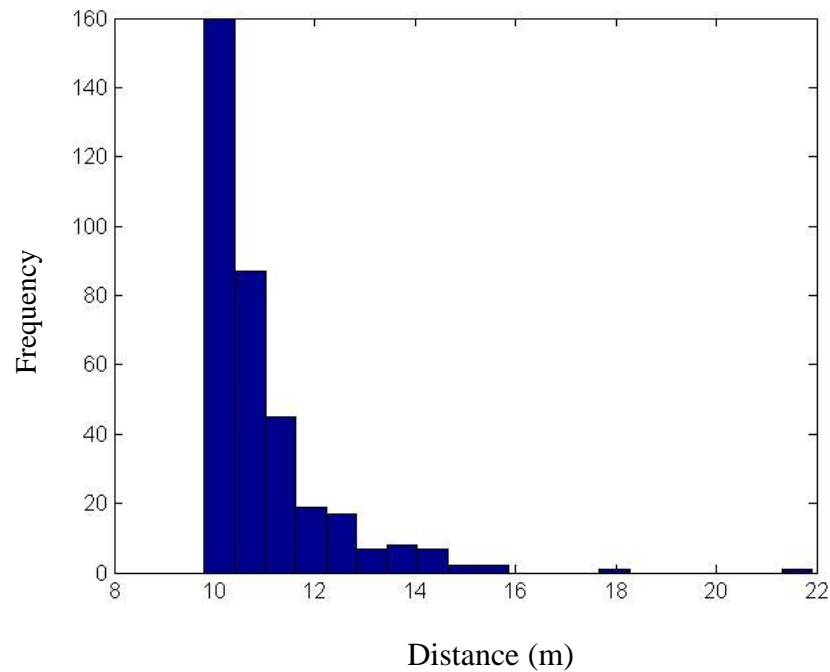


Lane formation

Hypothesis

- Lane allows for a more comfortable flow for people who walk in the same direction

# Distance & time observables



For more details (Nikolic et al., 2013)



# Strategy

## *Step by step*

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- Evaluation of data potential
- **Good estimation of congestion indicators**
  - **Density, flow, speed**

# Pedestrian flow characteristics

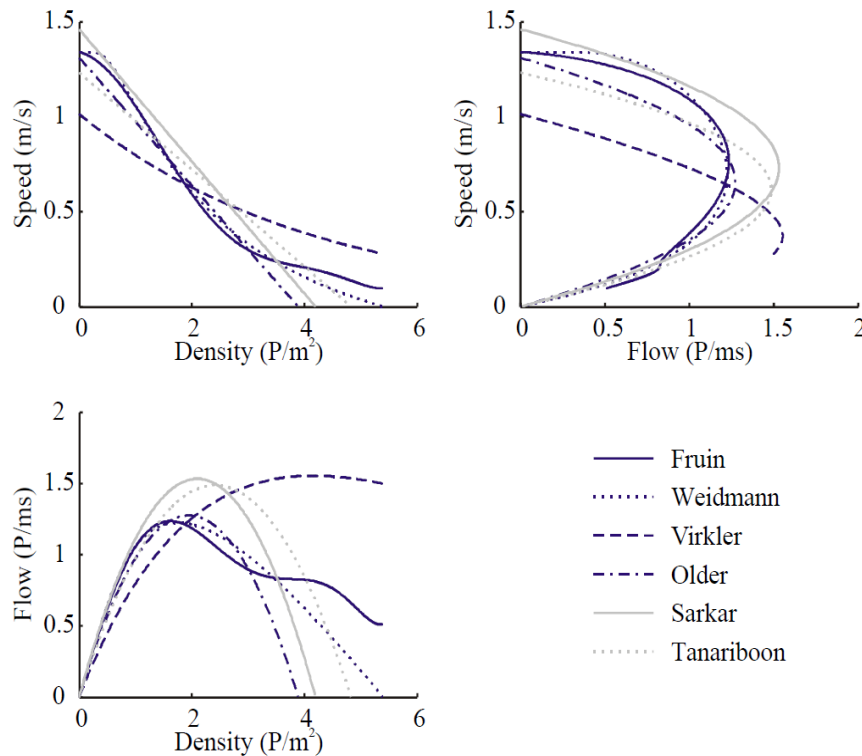
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- Density ( $k$ ) – number of pedestrians present at some instant per unit of space
- Flow ( $q$ ) – number of pedestrians passing a fixed point per unit of time
- Speed
  - Space mean speed ( $v_s$ ) - average speed of pedestrians at some instant per unit of space
  - Time mean speed ( $v_t$ ) - average speed of pedestrians passing through a given point per unit of time

Fundamental diagram:  $q = v_s \cdot k$

# Fundamental diagram

## *Literature*



Complex nature of pedestrian interactions

External factors

Social and psychological aspects

Different types of facilities

Different types of pedestrian flow

Measurement methods

Source: (Daamen et al., 2005)

# Fundamental diagram

## *Measurement methods*

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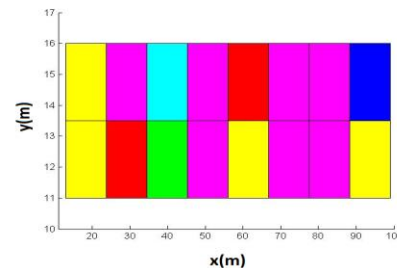
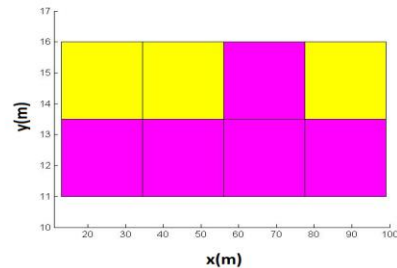
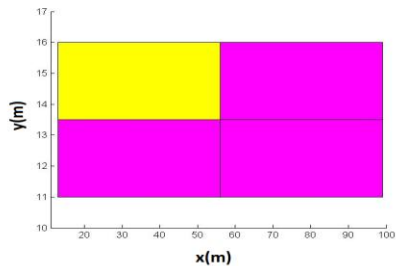
- Methods based on time aggregation
  - Mean value of flow
  - Time mean speed
- Methods based on space aggregation
  - Mean value of density
  - Space mean speed
- Time and space discretization

# Grid space representation

## Density

- The grid based method transforms the space into cell regions
  - Each cell is seen as entirely homogenous

Corridor density map (18.09.2012. 07:17:01)



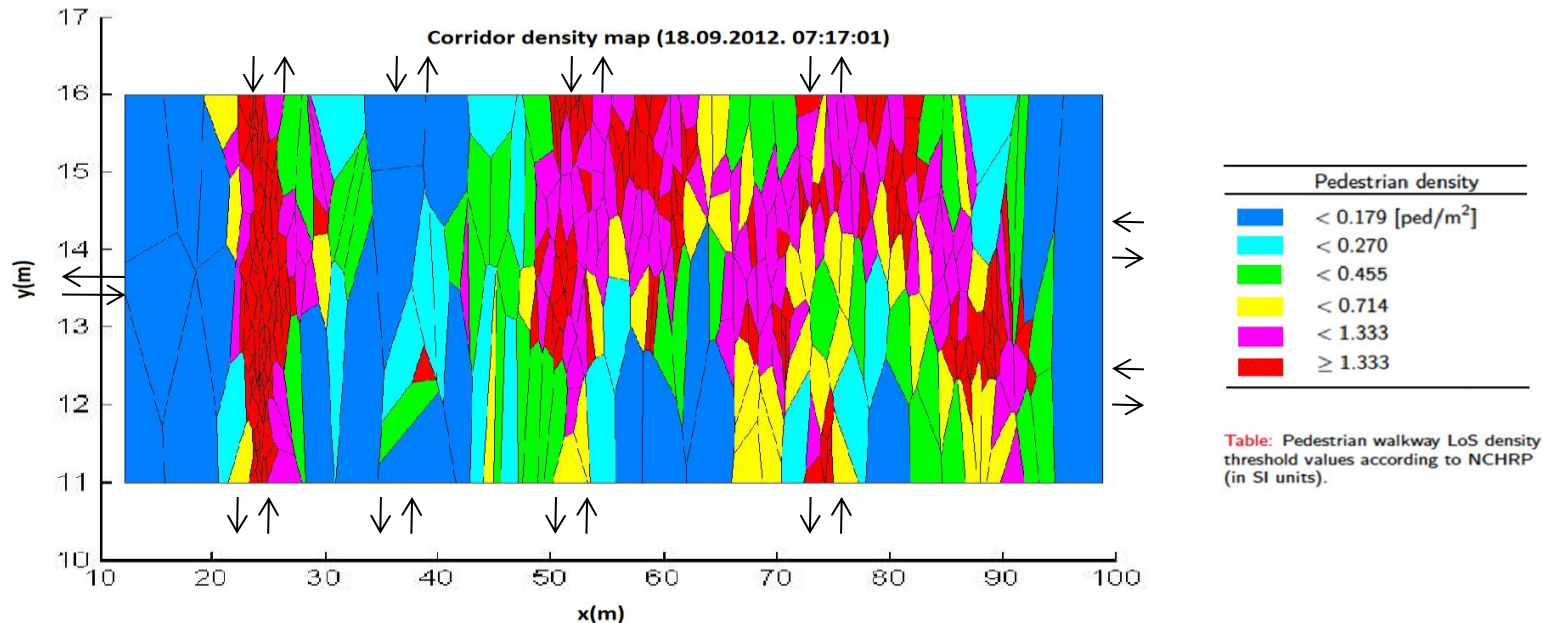
Pedestrian density	
Blue	< 0.179 [ped/m <sup>2</sup> ]
Cyan	< 0.270
Green	< 0.455
Yellow	< 0.714
Magenta	< 1.333
Red	≥ 1.333

Table: Pedestrian walkway LoS density threshold values according to NCHRP (in SI units).

- Cell sizes: 2.5m × 43m, 2.5m × 21.5m, 2.5m × 10.75m
- *Modifiable areal unit problem*

# Voronoi space representation

## Density



Voronoi space discretization

$$V_p(p_i) = \{p \mid \|p - p_i\| \leq \|p - p_j\|, j \in \{1, \dots, N_p\} \setminus \{i\}\}$$

$N_p$  - number of pedestrians

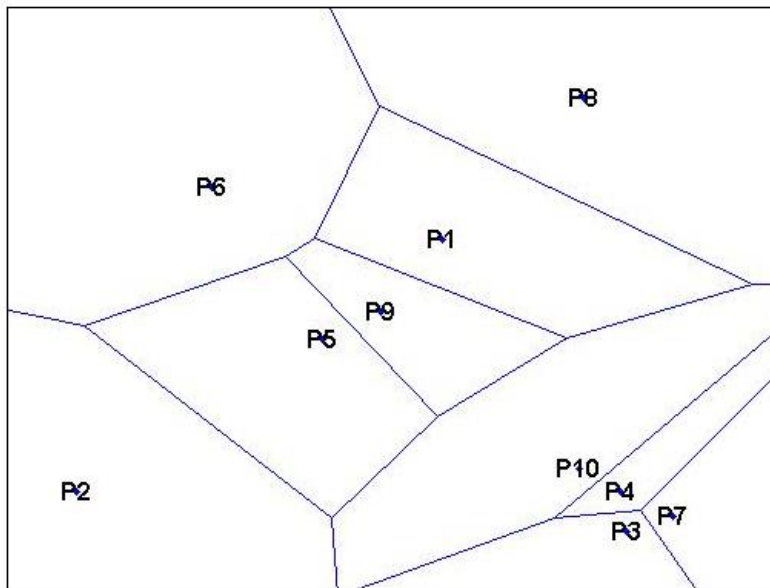
$p_i$  and  $p_j$  - pedestrians' position

- ✓ Flexible
- ✓ Better resolution in space

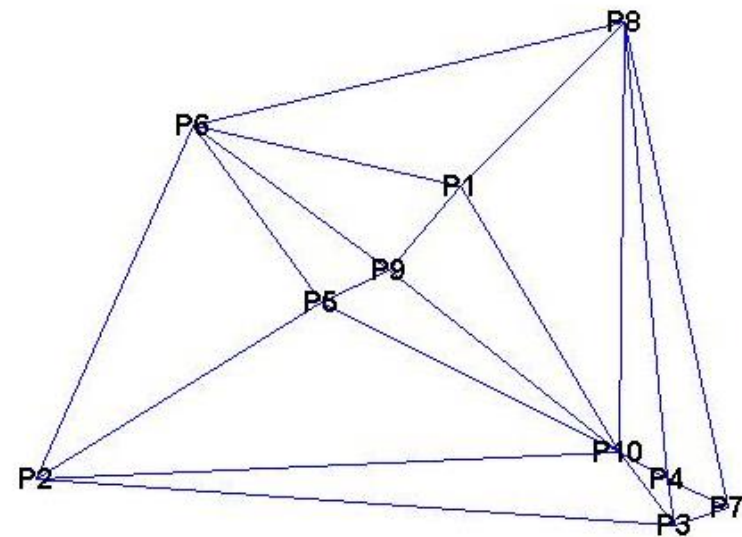
# Voronoi space representation

## *Issues*

- Small polygons allocated to pedestrians in very dense areas
  - Clustering based on Delaunay triangulation
  - Threshold distance: 0.1915m



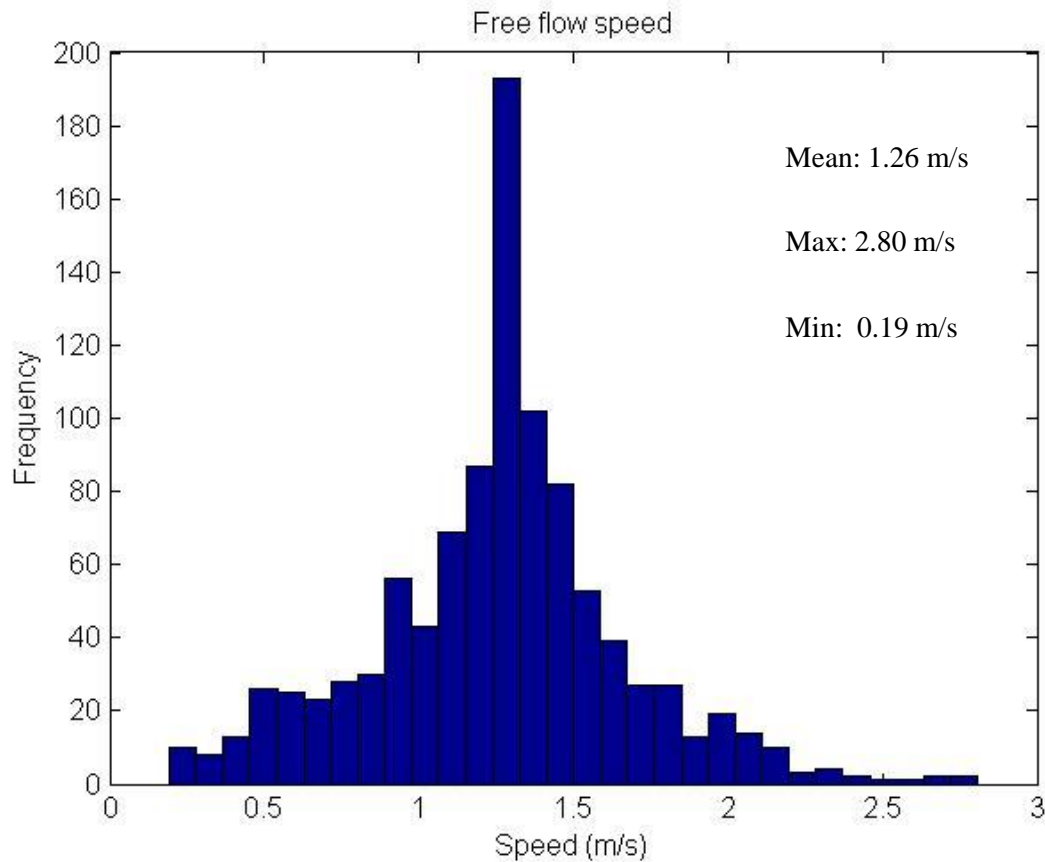
Voronoi diagram



Delaunay triangulation

# Free flow speed

## *Empirical observations*



- The speed pedestrians walk with when they are not constrained
- Voronoi based personal region - density less than 0.05 ped/m<sup>2</sup>

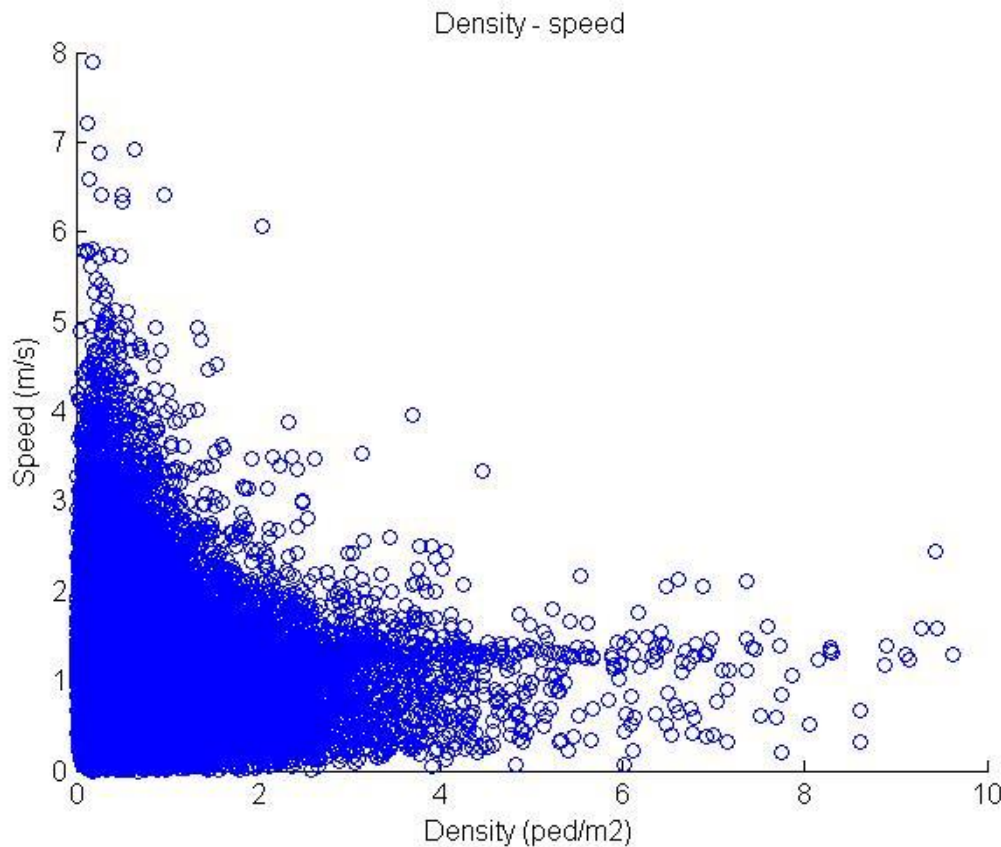
$$\vec{v}_i(t) = \frac{\vec{x}_i(t + \Delta t) - \vec{x}_i(t - \Delta t)}{2 \cdot \Delta t}$$

- Literature (Daamen et al., 2006)
  - Mean: 1.34 m/s
  - Max: 1.65 m/s
  - Min: 0.97 m/s



# Speed-density relationship

## *Empirical observations*



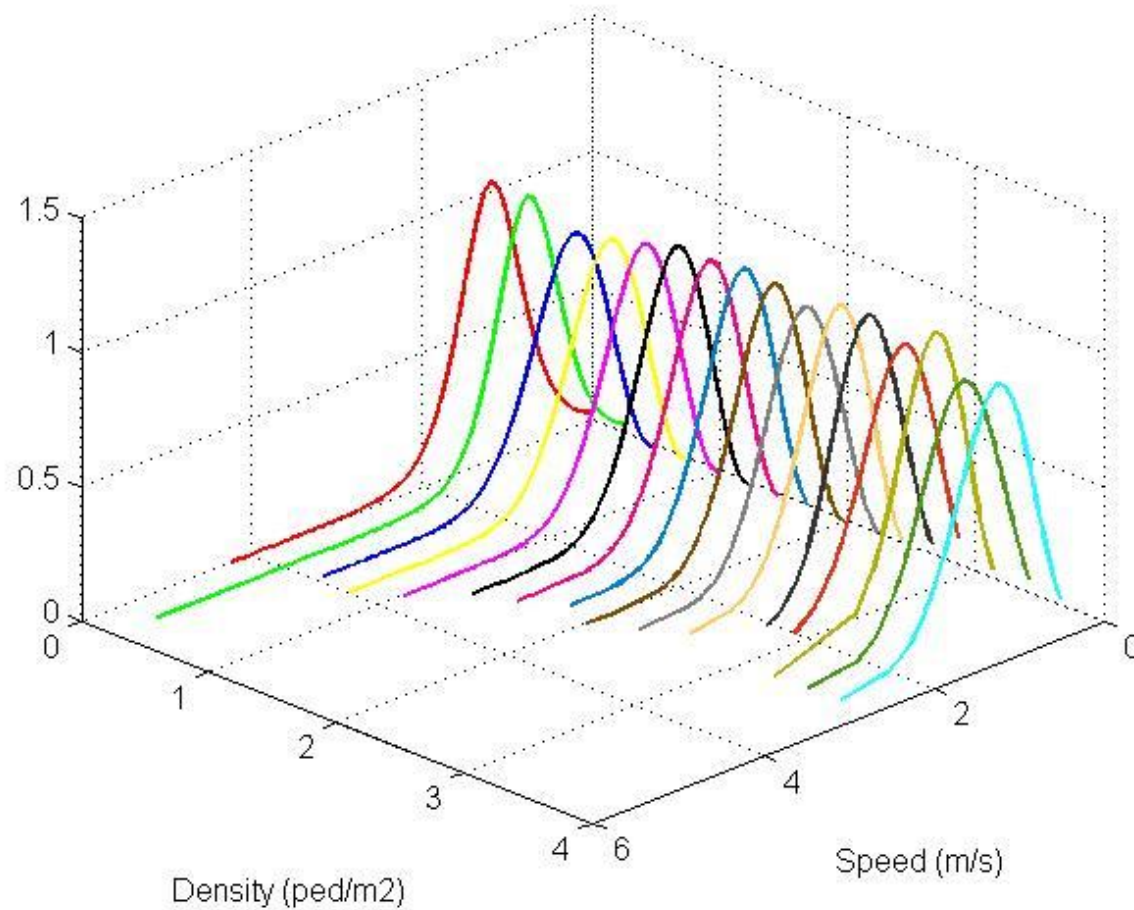
$$\text{Density: } \frac{1}{A_i}$$

$A_i$ -personal area assigned to pedestrian  $i$

$$\text{Speed: } \vec{v}_i(t) = \frac{\vec{x}_i(t+\Delta t) - \vec{x}_i(t-\Delta t)}{2 \cdot \Delta t}$$

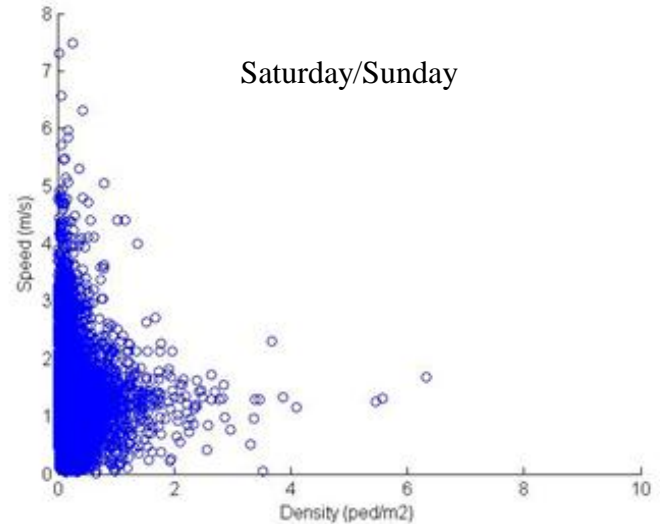
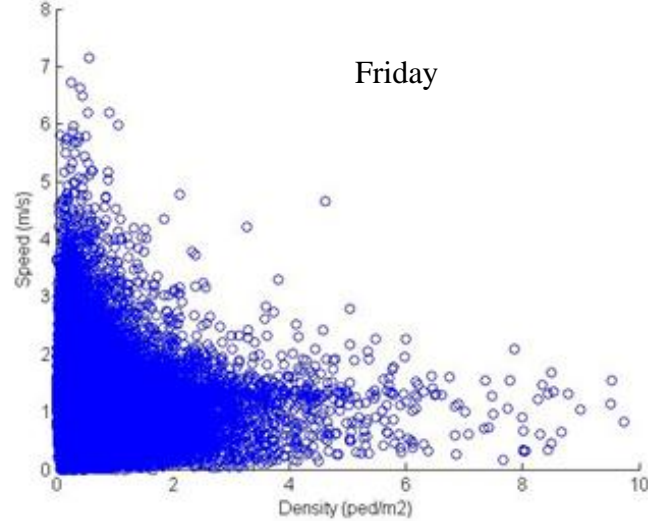
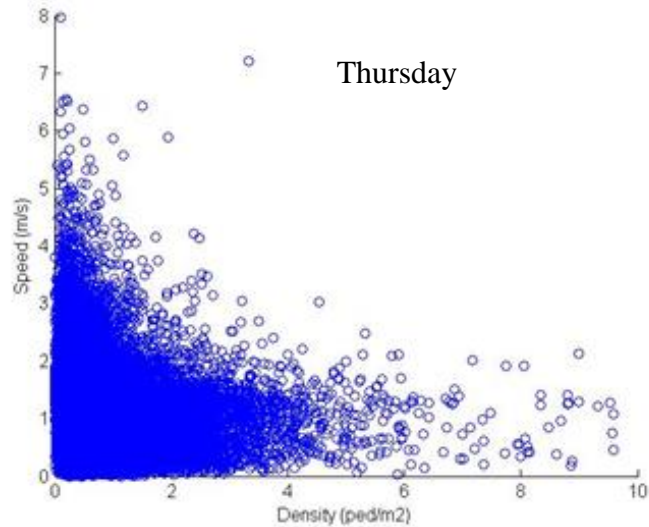
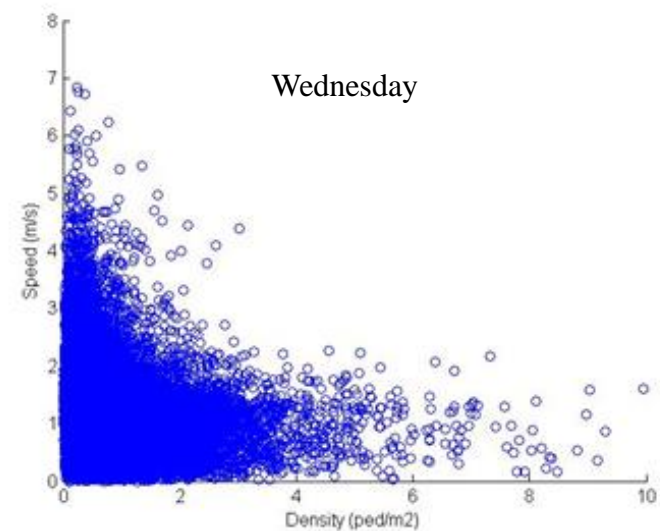
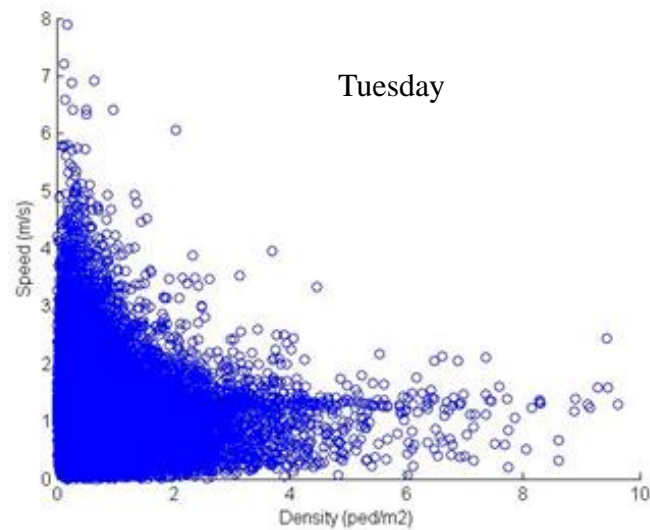
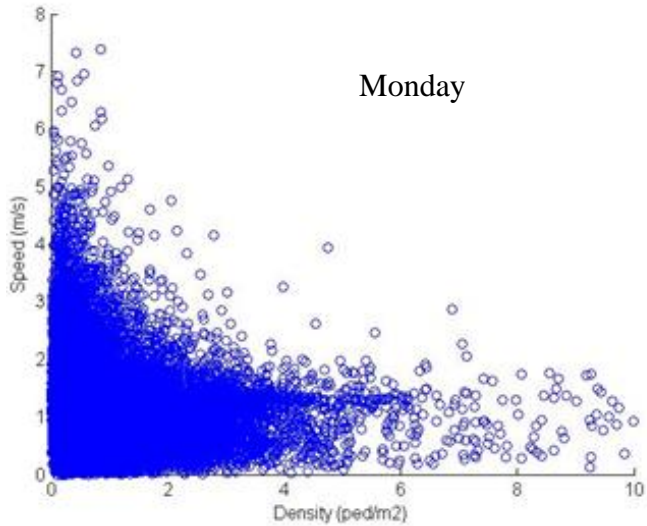
$\Delta t = 0.5s$

# Probabilistic speed-density model



# Weekly change of speed-density relationship

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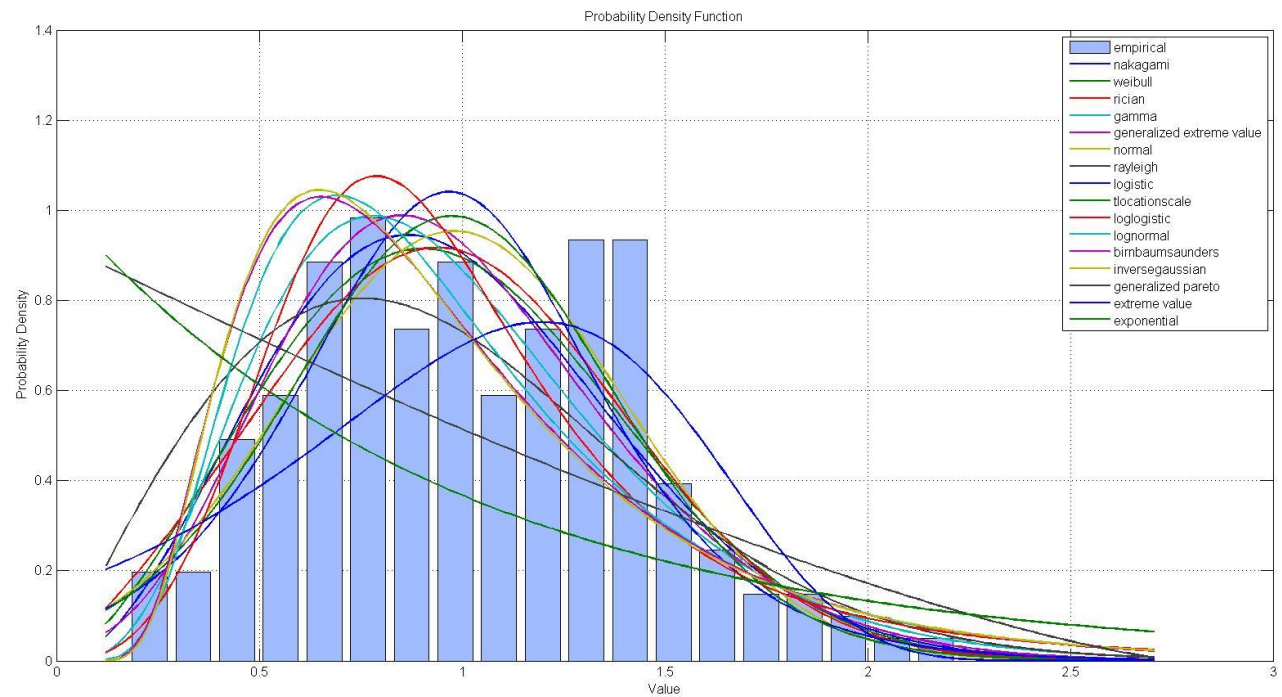


# Speed distribution

## *Maximum likelihood*

Density levels (ped/m<sup>2</sup>)

- 0 - 0.25
- 0.25 - 0.5
- 0.5 - 0.75
- 0.75 - 1
- 1 - 1.25
- 1.25 - 1.5
- 1.5 - 1.75
- 1.75 - 2
- 2 - 2.25
- 2.25 - 2.5
- 2.5 - 2.75
- 2.75 - 3
- 3 - 3.25
- 3.25 - 3.5
- 3.5 - 3.75
- ≥ 3.75



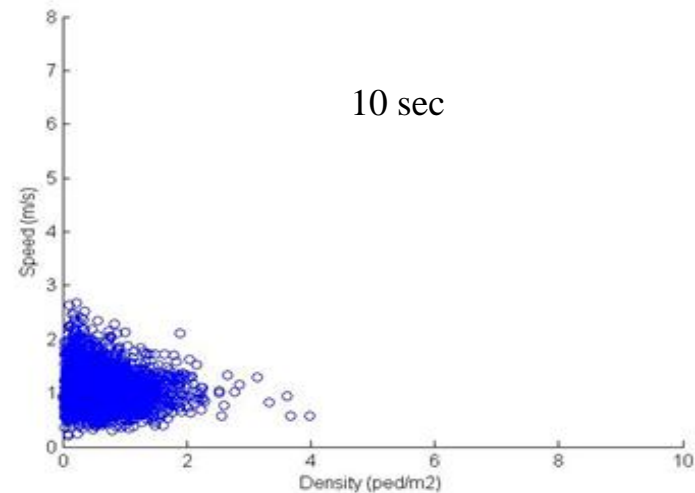
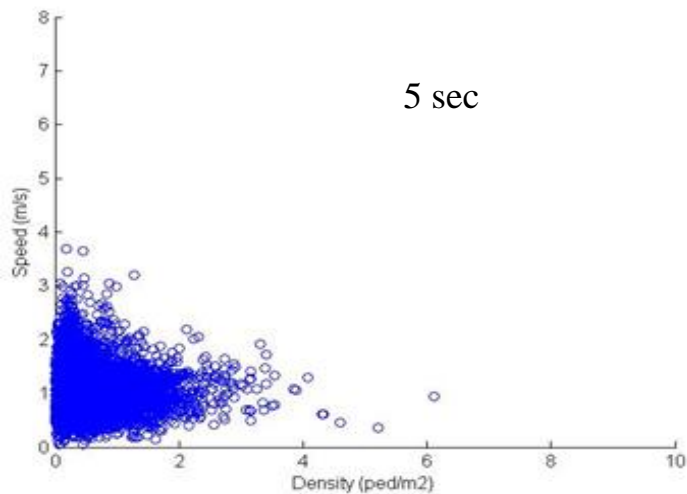
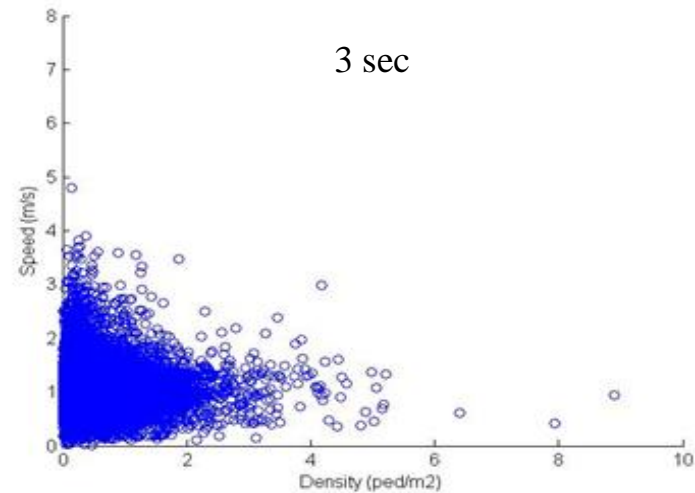
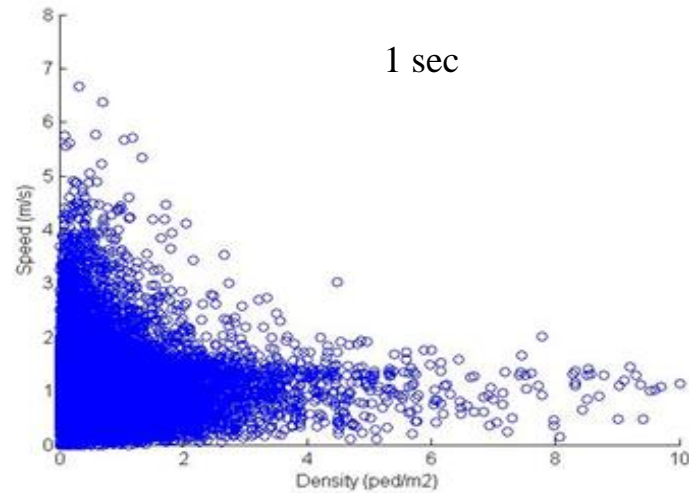
# Goodness of fit

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- Chi-squared test
  - $\chi^2 = \sum_i [(O_i - E_i)^2 / E_i]$
  - Null hypothesis: a statistical (theoretical) model fits a set of empirical observations
  - Result: rejected at 0.05 level of significance
- Fitting does not explain!
  - Addition of explanatory variables

# Speed-density relationship

## *Effects of time aggregation*



# Time discretization

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- Voronoi based
  - Fixed number of pedestrians within each time interval
- Motivation
  - Consistent with the philosophy of space decomposition
  - Observables have comparable statistical accuracy
  - Independent of the occurring flow

# Conclusion

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- High data potential
  - Behavioral and flow aspects
- Voronoi representation of space and time
  - Consistent philosophy for time and space decomposition
  - Good space resolution
  - Independent of the occurring flow
- Probabilistic fundamental diagram
- Lot of work need to be done!



# Future work

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- Voronoi based space representation
  - Dealing with obstacles
- Voronoi based time representation
  - Investigation of appropriate time discretization
- Probabilistic fundamental diagram

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**THANK YOU**

# References 1/2

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