

# Temperature considerations on Hall Effect sensors current-related sensitivity behaviour

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**Abstract** The present paper focuses on evaluating the temperature effects on Hall Effect sensors sensitivity behavior. To this purpose, an analysis of the factors affecting the sensors current-related sensitivity is performed, consisting of several pertinent considerations. An analytical investigation of the carrier concentration temperature dependence including the freeze-out effect influence was performed. This information was subsequently included in accurate prediction of the current-related sensitivity temperature behavior. For a specific CMOS integration process of the Hall sensors, a parabolic curve is obtained for the relative variation of the current-related sensitivity.

**Keywords** Hall Effect sensors · Temperature behavior · Freeze-out effect · Current-related sensitivity · Parabolic dependence

## 1 Introduction

The Hall Effect sensors are magnetic sensors which are used nowadays in a multitude of applications ranging from position detection, contactless switching, in DC brushless motors and as current-sensors in low-power applications [1]. Recent applications recommend these sensors for the detection of the superparamagnetic beads [2], for the measurements of the Brownian relaxation response of magnetic nanobeads in suspension [3], as well as for thermonuclear reactor magnetic diagnostics systems [4].

The performance of Hall Effect sensors resides in the highest sensitivity and the lowest offset. In recent papers, the authors analyzed the correlation between the Hall sensors geometry and their performance [5–8] and presented shapes [9, 10] that allowed offsets less than 30  $\mu\text{T}$  and drift less than 0.3  $\mu\text{T}/^\circ\text{C}$ . The achieved performance for specific sensors in terms of offset and its drift are a few times better than the state-of-the-art. Research was conducted by the authors to predict Hall Effect sensors behavior by three-dimensional physical simulations [11] and guide the designer in optimal Hall sensor shape selection process.

The current work is intended to analyze the temperature behavior of Hall Effect sensors current-related sensitivity, by taking into account the variation of the specific parameters. Section 2 is devoted to introducing general considerations about the Hall sensors and the design of a specific cell in particular which exhibited the best performance. Section 3 is reserved for a detailed analysis of the current-related temperature dependence while Sect. 4 aims to present an analytical discussion of carrier concentration temperature dependence including the freeze-out effect. Finally, Sect. 5 summarizes the results of simulations for temperature coefficients of the specific parameters and

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ultimately provides the shape of the absolute-sensitivity curve with the temperature.

## 2 Hall Effect sensors considerations

### 2.1 Hall voltage definition

When polarizing a semiconducting device with a current and subjecting the probe to a magnetic field, the carriers are deviated under the influence of Lorentz force and a voltage difference appears between the opposite contacts in the form of the Hall voltage. The Hall voltage is given by the following relation, for a current polarization with  $I_{bias}$ :

$$V_H = G \frac{r_H}{nqt} I_{bias} B \tag{1}$$

where  $G$  is the geometrical correction factor,  $r_H$  is the Silicon scattering factor,  $n$  is the carrier density,  $q$  is the elementary charge,  $t$  is the thickness of the implantation profile and  $B$  is the perpendicular component of the magnetic field induction, respectively [12].

From the equation above, we can see the need to use lightly doped semiconductors in order to achieve higher Hall voltages.

### 2.2 Hall Effect sensors implementation

In recent papers, the authors presented and analyzed nine integrated Hall sensors shapes in CMOS 0.35  $\mu\text{m}$  technology. Details about all the cells integration and performance tests can be found in [8–11]. In Fig. 1, precise design details

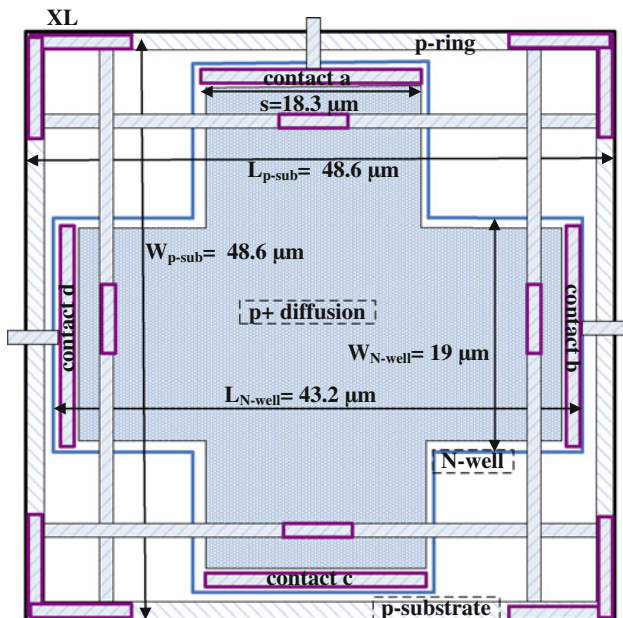


Fig. 1 The XL Hall cell detailed design parameters

of the XL cell which displayed the maximum performance in terms of offset and its drift [9] are depicted.  $W$  and  $L$  stand for the width and length of the Hall sensor respectively, while  $s$  denotes the contacts length. It is an n-doped semiconductor structure, with N-well implantation on a p-substrate. On top, to reduce the noise and to prevent the current to flow under the contacts, a p+ diffusion layer is also used.

### 2.3 Hall cells absolute and current-related sensitivity

The performance of the Hall cells is given by the analysis of their absolute sensitivity, the zero-magnetic field offset voltage and their corresponding temperature drifts [13, 14]. Therefore, in achieving Hall cells with good performance, a high sensitivity and a low offset drift are required.

An important figure of merit in Hall Effect sensors performance assessment is their sensitivity. The absolute sensitivity  $S_A$  is defined as the ratio of the detected Hall voltage  $V_H$  to the magnetic field induction,  $B$ . Moreover, one could also define the current-related sensitivity of the Hall sensor by the following relationship:

$$S_I = \frac{S_A}{I_{bias}} = \frac{V_H}{BI_{bias}} = G \frac{r_H}{nqt_{eff}} \tag{2}$$

When the doping density in the plate depends on the depth  $z$ , as in the case of ion-implanted layers, in Eqs. (1) and (2), the charge carrier density is a function of  $z$ , respectively  $n = n(z)$ .

The moment  $m_i$  for an arbitrary index  $i$  is computed as follows:

$$m_i = \frac{\int_0^\infty (z - R_p)^i n(z) dz}{\int_0^\infty n(z) dz} \tag{3}$$

The first order moment  $R_p$  is:

$$R_p = \frac{\int_0^\infty zn(z) dz}{\int_0^\infty n(z) dz} \tag{4}$$

The standard deviation  $\sigma$ , the skewness  $\gamma$  and the kurtosis  $\beta$  are defined as:

$$\sigma = \sqrt{m_2}, \quad \gamma = \frac{m_3}{\sigma^3}, \quad \beta = \frac{m_4}{\sigma^4} \tag{5}$$

The ion implantation profile, using the moment parameters is expressed by:

$$n(z) = n_0 \exp \left[ -\frac{(z - R_p)^2}{2\sigma^2} \right] \tag{6}$$

where  $n_0$  is the peak concentration, which is defined with respect to the implantation dose  $\Phi$  as:

$$n_0 = \frac{\Phi}{\sqrt{2\pi}\sigma} \tag{7}$$

A pure Gaussian distribution is obtained for  $\gamma = 0$  and  $\beta = 3$ . In the case of  $\gamma = 0$  and  $\beta = 2$ , the carrier concentration presents a strong flat region as in [15], respectively a quasi-constant concentration. Globally, these differences (for various values of  $\beta$ , also known as the effect of  $\beta$  on profile shape) do not practically influence the carrier concentration. For  $\gamma = 0$ , the distribution is symmetrical with respect to the axis  $z = R_p$ . In the simulation programs, a constant concentration can be however assumed tacitly, without producing major/significant modifications in the results obtained.

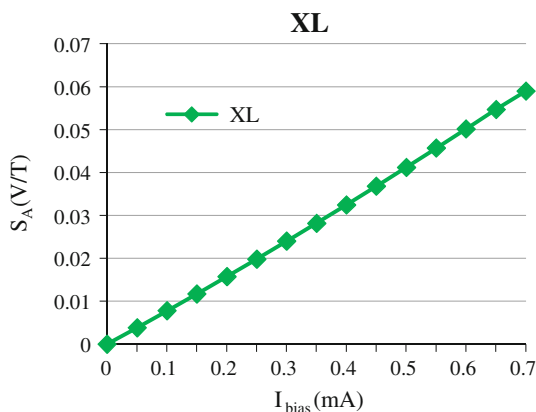
Nevertheless, a Gaussian implantation profile was considered by the authors in a recent paper dealing with three-dimensional simulation of the Hall cells [5], as well as the PhD thesis of Paun [7].

The sensitivity measurements were performed by subjecting the samples to a perpendicular magnetic field of  $B = 0.497$  T. The absolute sensitivity for the XL Hall cell of Run 1 as a function of the biasing current, between 0 and 0.7 mA, is presented in Fig. 2.

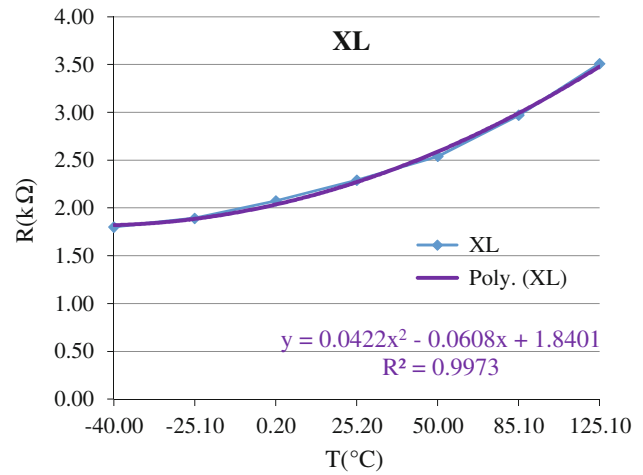
As presented in [3], the XL cell has  $S_I = 80.7$  V/AT, where  $G$  was computed for different structures by the authors [8]. This type of measurements was achieved with the automated setup and the data extracted is before the saturation occurs.

### 2.4 Input resistance temperature dependence

Measurements for the input resistance dependence with temperature of the XL integrated Hall cell is depicted in Fig. 3. The corresponding cell was placed in an oven and the temperature was cycled from  $-40$  to  $125$  °C. The curve is presented with a second order fit.



**Fig. 2** The absolute sensitivity (V/T) of the XL cell versus the  $I_{bias}$  (mA)



**Fig. 3** Input resistance  $R$  versus temperature for XL Hall cell

### 3 Temperature dependence of the Hall cells current-related sensitivity

From Eq. (2) above we can clearly see the factors that affect the absolute sensitivity temperature dependence:

$$S_I(T) = G \frac{r_H(T)}{n(T)qt_{eff}(T)} \tag{8}$$

The current-related sensitivity increases with the current, as the effective thickness of the active area if the Hall plate is reduced.

Let us consider that  $r_H = r_H(T)$ ,  $n = n(T)$  and  $t_{eff} = t_{eff}(T)$  are temperature dependent functions. We will have  $S_I = S_I(r_H(T), n(T), t_{eff}(T))$ , which means that it is an implicit function of  $T$ .

Therefore, we can write:

$$\frac{dS_I}{dT} = \frac{\partial S_I}{\partial r_H} \frac{\partial r_H}{\partial T} + \frac{\partial S_I}{\partial n} \frac{\partial n}{\partial T} + \frac{\partial S_I}{\partial t_{eff}} \frac{\partial t_{eff}}{\partial T} \tag{9}$$

where  $r_H$ ,  $n$  and  $t_{eff}$  are functions of a single variable “ $T$ ”, which makes the derivation operator  $\frac{\partial}{\partial T}$  to become actually  $\frac{d}{dT}$ .

From Eq. (5), we obtain:

$$\begin{aligned} \frac{\partial S_I}{\partial r_H} &= \frac{G}{nqt_{eff}}; \frac{\partial S_I}{\partial n} = -\frac{Gr_H}{n^2qt_{eff}} = -S_I \frac{1}{n}; \frac{\partial S_I}{\partial t_{eff}} = -\frac{Gr_H}{nqt_{eff}^2} \\ &= -S_I \frac{1}{t_{eff}} \end{aligned} \tag{10}$$

which replaced in Eq. (6) gives us:

$$\frac{dS_I}{dT} = S_I \left( \frac{1}{r_H} \frac{dr_H}{dT} \right) - S_I \left( \frac{1}{n} \frac{dn}{dT} \right) - S_I \left( \frac{1}{t_{eff}} \frac{dt_{eff}}{dT} \right) \tag{11}$$

We now make the specification that, by definition, the temperature coefficient of the physical quantity  $A$ , denoted by  $\alpha_A$  is:

$$\alpha_A = \frac{1}{A} \frac{dA}{dT} \quad (12)$$

where  $A$  is an element of the discrete set  $A \in \mathcal{A} \equiv \{S_I, r_H, n, t_{eff}, \dots\}$ .

As presented in [12], the temperature coefficient  $\alpha$  of a specific quantity  $Q$  is defined as follows:

$$\alpha = \frac{1}{Q_0} \frac{dQ}{dT} \quad (13)$$

where  $Q_0 = Q(T_0)$  is the value of the specific quantity at room temperature  $T_0 = 300K$ .

By consequence, the temperature coefficient  $\alpha_{S_I}$  of the current-related sensitivity is the following:

$$\alpha_{S_I} = \alpha_{r_H} - \alpha_n - \alpha_{t_{eff}} \quad (14)$$

In general, the effective thickness  $t_{eff}$  can be defined as follows:

$$t_{eff} = t_{NW} - t_{p+} - w_{NW,sub} - w_{NW,p+} \quad (15)$$

where  $t_{NW}$  is the depth of the N-well implantation region,  $t_{p+}$  is the thickness of the top p+ layer,  $w_{NW,sub}$  is the bottom depletion region between N-well and the p-type substrate,  $w_{NW,p+}$  is the upper depletion region between N-well and the top p+ layer [16].

As presented in a few papers published in the literature [16–18], the effective thickness  $t_{eff}$  is considered constant with the temperature, so its corresponding temperature coefficient is null,  $\alpha_{t_{eff}} = 0$ . This assumption is valid when  $V_{substrate}$  is constant and  $V_{output}$  is in common mode, resulting from the presence of the common voltage at the input. Indeed some specific biasing conditions were used for Hall cells, as presented in details by the authors in a recent paper [9] where the automated measurement setup is presented. The substrate is biased with a constant voltage (either 0 or 3.3 V), while the output voltage is collected with a lock-in amplifier.

However, the type of experimental data regarding the input resistance temperature dependence, in Fig. 3 could be useful when evaluating the temperature dependence of the effective thickness of the implantation profile, if needed. Nevertheless, this is not the objective of the present study and can be dealt with in a future paper.

A Taylor expansion of the function  $S_I = S_I(T)$ , around the value  $T_0$ , has the form:

$$S_I(T) = S_I(T_0) + \frac{1}{1!} \left. \frac{\partial S_I(T)}{\partial T} \right|_{T_0} (T - T_0) + \frac{1}{2!} \left. \frac{\partial^2 S_I(T)}{\partial T^2} \right|_{T_0} (T - T_0)^2 + \sum_{n=3}^{\infty} \frac{1}{n!} \left. \frac{\partial^n S_I(T)}{\partial T^n} \right|_{T_0} (T - T_0)^n \quad (16)$$

In the case in which:

$$\sum_{n=3}^{\infty} \frac{1}{n!} \left. \frac{\partial^n S_I(T)}{\partial T^n} \right|_{T_0} (T - T_0)^n = O\left[\left((T - T_0)^{n \geq 3}\right)\right] \rightarrow 0 \quad (17)$$

we have after a simple computation, the simplified version of Eq. (16):

$$S_I(T) = S_I(T_0) + \alpha_I(T - T_0) + \beta_I(T - T_0)^2 \quad (18)$$

where

$$\alpha_I = \frac{1}{S_I(T_0)} \left. \frac{\partial S_I(T)}{\partial T} \right|_{T_0} \quad (19)$$

is the “first (order) coefficient” of the current-related sensitivity and

$$\beta_I = \frac{1}{2S_I(T_0)} \left. \frac{\partial^2 S_I(T)}{\partial T^2} \right|_{T_0} \quad (20)$$

is the “second (order) coefficient” of the current-related sensitivity, in the sense of a natural generalization of coefficients.

In the linear crop case, Eq. (18) becomes the following:

$$S_I(T) = S_I(T_0) + \alpha_I(T - T_0) \quad (21)$$

The temperature dependence of the magnetic sensitivity of the Hall cells is influenced by the temperature influence on two competing factors namely the freeze-out effect of the electron density and the Hall scattering coefficient respectively, as it has been investigated in the previous sections.

#### 4 Analytical investigation of the carrier concentration temperature dependence

The carrier concentration temperature dependence was investigated in details, through an attentive analytical analysis including the consideration of the installation of freeze-out regime. The effect of carrier freeze-out on Hall sensors sensitivity was analyzed in a simplified way in [17]. The present study is more detailed than the latter one, giving the full set of precise analytical equations to be integrated in MATLAB for the complex carrier concentration temperature dependence. In addition to this, the computations are performed for a different CMOS integration technology.

In order to predict Hall Effect sensors sensitivity temperature behavior, one would need to calculate the temperature coefficient of the corresponding parameters that affect the sensitivity. By consequence, Eq. (14) needs to be taken into account.

The intrinsic carrier concentration,  $n_i$  is given by the following relationship, which depends on the effective density of states in the valence band and conduction band respectively:

$$n_i(T) = \text{Sqrt}(N_C(T)N_V(T))\exp\left(\frac{-E_g}{2kT}\right) \tag{22}$$

where  $N_C$  is the effective density of states in the conduction band,  $N_V$  is the effective density of states in the valence band,  $E_g$  is the bandgap of the semiconductor,  $k$  is the Boltzmann constant and  $T$  is the temperature in K. In our case of Silicon,  $E_g = 1.12$  eV.

$N_C$  and  $N_V$  are both of them temperature dependent and obey the following equations:

$$N_{C,V}(T) = 2\left(\frac{2\pi m_{n,p}kT}{h^2}\right)^{\frac{3}{2}} \tag{23}$$

where  $m_n$  is the mass of the donors ( $e^-$ ),  $m_p$  is the mass of the acceptors (holes) and  $h$  is the Planck constant. We know that  $m_n = 1.08m_e$  and  $m_p = 0.81m_e$  where  $m_e$  is the elementary mass.

We also introduce the notion of freeze-out carrier concentration,  $n_{fr}$ , which is computed after the following relationship including temperature dependence:

$$n_{fr}(T) = -\frac{\frac{N_C}{2}\exp\left(\frac{-E_d}{kT}\right) + N_A}{2} + \text{Sqrt}\left(\left(\frac{\frac{N_C}{2}\exp\left(\frac{-E_d}{kT}\right) + N_A}{2}\right)^2 + (N_D - N_A)\frac{N_C}{2}\exp\left(\frac{-E_g}{2kT}\right)\right) \tag{24}$$

where  $E_d$  is the donor energy of the donor impurity,  $N_D$  is the donor density and  $N_A$  is the acceptor density, for the impurities with which the semiconductor is doped. The ionization energy of donor impurities is  $E_d = 0.049$  eV for Arsenic and  $E_d = 0.045$  eV for Phosphorus respectively [19].

The equation above is valid for temperatures which satisfy the relation:

$$T \leq \frac{E_g}{k\ln N_C N_V - 2k\ln|N_D - N_A|} \tag{25}$$

We need to calculate the minimum between the net impurity density and the freeze-out carrier concentration which is above computed. Further on, the electron density  $n$ , which interests us, will be given by the maximum between the latter quantity and the intrinsic density as shown by the formula:

$$n = \text{Max}(n_i, \text{Min}(N_D - N_A, n_{fr})) \tag{26}$$

The detailed analysis of the carrier concentration temperature behavior gives us an insightful approach

which will be used in accurate sensitivity prediction. The goal is to see how this ultimately affects the sensitivity of the Hall cells.

## 5 Results and discussion

### 5.1 The current-related sensitivity temperature behaviour

The temperature dependence of the magnetic sensitivity of the Hall cells is influenced by the temperature influence on two competing factors namely the freeze-out effect of the electron density and the Hall scattering coefficient respectively.

The values of the parameters used to simulate the Hall cells within CMOS Process 1 are summed up in Table 1.

Besides our integration process (Process 1), another CMOS process (Process 2) was simulated for the same cell. The data for Process 2 was taken from [20] and it is presented in Table 2. This data was used for the simulations obtained in Fig. 12.

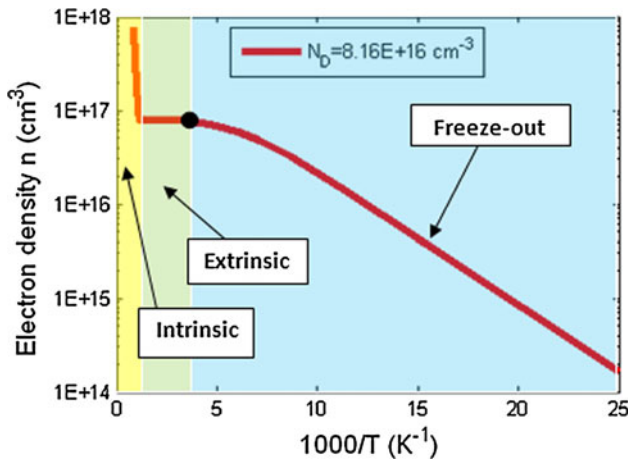
In Fig. 4, the carrier concentration (in this case n-type carriers) is represented against the reciprocal temperature, for  $N_D = 8.16E + 16 \text{ cm}^{-3}$ . From this graph we can see the three regions, namely intrinsic (yellow sector), extrinsic (or saturation) in the green sector and ionization (or freeze-

**Table 1** Process 1 parameters used in the Hall cells simulation

Parameter	Symbol	Numerical value
XL total length	$L_{sensor}$	$43.2 \times 10^{-6}$ m
XL total width	$W_{sensor}$	$19 \times 10^{-6}$ m
Thickness	$t$	$10^{-6}$ m
Donor concentration	$N_d$	$8.16 \times 10^{22} \text{ m}^{-3}$
Acceptor concentration	$N_a$	$10^{21} \text{ m}^{-3}$
Conductivity	$\sigma$	$933 \text{ Sm}^{-1}$
Mobility	$\mu$	$0.0715 \text{ m}^2 \text{ V}^{-1} \text{ s}^{-1}$
Magnetic field	$B$	0.5 T

**Table 2** Process 2 parameters used in the Hall cells simulation

Parameter	Symbol	Numerical value
XL total length	$L_{sensor}$	$43.2 \times 10^{-6}$ m
XL total width	$W_{sensor}$	$19 \times 10^{-6}$ m
Donor concentration	$N_d$	$3.3 \times 10^{22} \text{ m}^{-3}$
Acceptor concentration	$N_a$	$10^{21} \text{ m}^{-3}$
Conductivity	$\sigma$	$382.8 \text{ Sm}^{-1}$
Mobility	$\mu$	$0.1 \text{ m}^2 \text{ V}^{-1} \text{ s}^{-1}$
Magnetic field	$B$	0.5 T



**Fig. 4** Carrier density graphical representation as function of reciprocal temperature

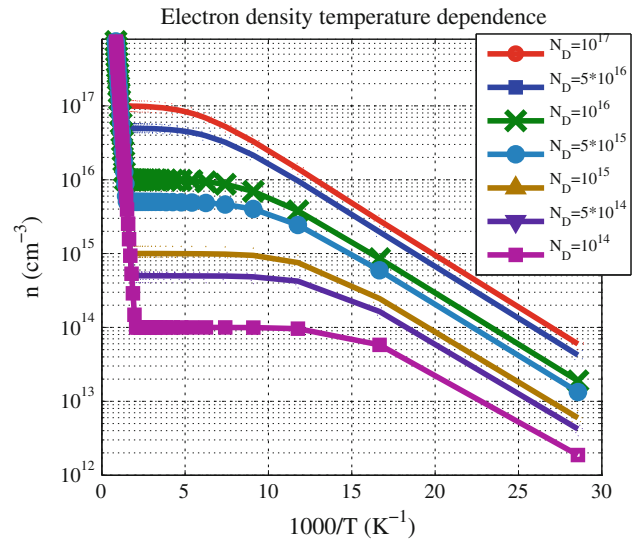
out) in the blue sector. The point displayed on the curve corresponds to  $n_{fr}$  which is obtained at the reciprocal of the freeze-out temperature,  $T_{fr}$ , more precisely  $1,000/T_{fr}$  abscissa point on the graph. In the case of our donor concentration,  $T_{fr} = 305$  K.

While the intrinsic region is identified in the zone where the carrier concentration increases with the temperature, the extrinsic region is where any increase in the temperature produces no increase in carrier concentration. To make it clear, the carrier density variation with temperature, due to reciprocal temperature, the graph in Fig. 4 should be “read” from right to left. In the very low temperatures range (equivalent to high  $1/T$ ), negligible intrinsic electron–hole-pairs exist and the donor electrons are bound to the donor atoms, giving birth to the ionization region [19].

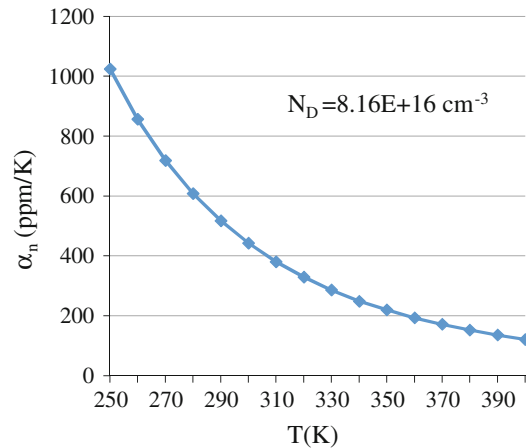
In the fabrication of Hall sensors, lower carrier concentrations yield higher sensitivity and in this case the freeze-out installs at lower temperatures. On the other hand, high carrier concentrations would have freeze-out temperatures approaching room temperature  $T_0 = 300$  K.

The semi-log graph in Fig. 5 presents the electron density temperature dependence, plotted against the reciprocal temperature (equivalent to  $1,000/T$ ), for seven different levels of donor concentrations. The temperature  $T$  is into the interval from 35 to 1,200 K and the donor concentrations  $N_D$  range from  $10^{14}$  to  $10^{17}$   $\text{cm}^{-3}$ . The graph is generated in MATLAB by using a code containing the full set of Eqs. (24–26).

For the specific CMOS process used in the integration of Hall cells, ( $N_D = 8.16E + 16 \text{ cm}^{-3}$ ) the temperature coefficient  $\alpha_n$  (ppm/K) of the electron density  $n$  has been calculated after extracting it from the curve in Fig. 4. The resulting  $\alpha_n$  versus temperature is displayed in Fig. 6.



**Fig. 5** Carrier concentration versus reciprocal temperature for different donor impurity concentrations



**Fig. 6** Temperature coefficient  $\alpha_n$  (ppm/K) of  $n$  versus temperature

In Fig. 6, we can observe that  $\alpha_n$  decreases from 1,000 ppm/K for 250 K to around 120 ppm/K for the maximum temperature considered of 400 K.

To obtain the temperature coefficient of the current-related sensitivity, we consider Eq. (8) with the addition that  $t_{eff}$  is constant and we use the value of  $r_H$  from [6]. Figure 7 depicts the obtained  $\alpha_S$ , plotted against the temperature. A zero temperature coefficient is obtained at  $T = 312$  K, so around  $\sim 40$  °C.

The relative variation  $\gamma$  of the current-related sensitivity,  $S_I$ , with respect to the room temperature  $T_0$ :

$$\gamma = \frac{S_I(T) - S_I(T_0)}{S_I(T_0)} \tag{27}$$

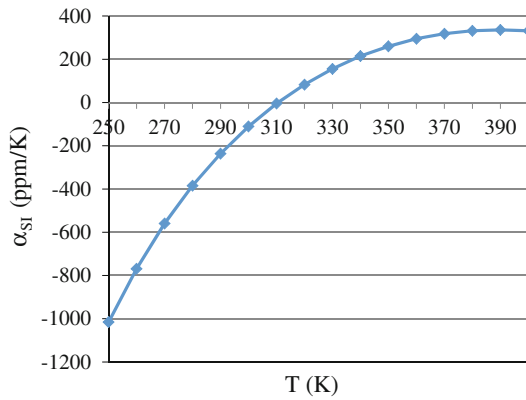


Fig. 7 Temperature coefficient  $\alpha_{S_I}$  (ppm/K) of  $S_I$  versus temperature

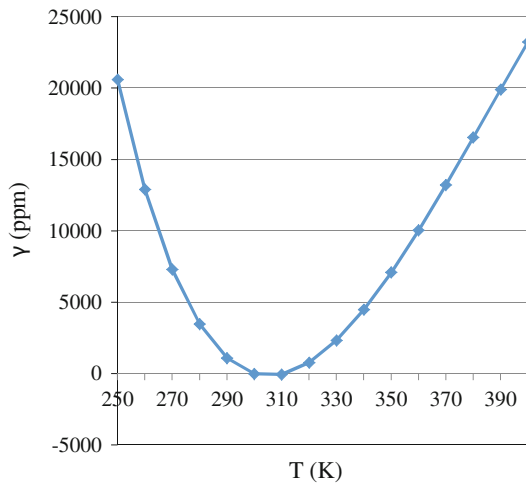


Fig. 8 The relative variation  $\gamma$  (ppm) of the current-related sensitivity versus temperature

is displayed in Fig. 8 versus temperature.

We observe a parabolic dependence of the current-related sensitivity relative variation with a minimum around 305 K. The drift of this relative variation is of maximum 24,000 ppm over the whole considered temperature interval.

This parabolic trend result obtained is in agreement with the experimental results presented in the literature, in [17]. Similar measurements results for the current-related sensitivity temperature are obtained in [21], for Hall samples integrated in the same CMOS process as the ones discussed in the present study, for a temperature range of  $-40$  to  $80$  °C. In another recent paper by the authors [22], by using a circuit model developed for Hall cells performance assessment, a second order curve is also obtained for the current-related sensitivity temperature dependence and compared with the theoretical results.

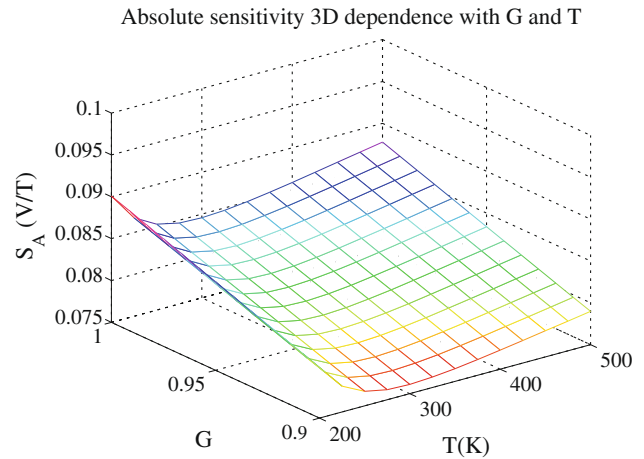


Fig. 9  $S_A = S_A(G, T)$

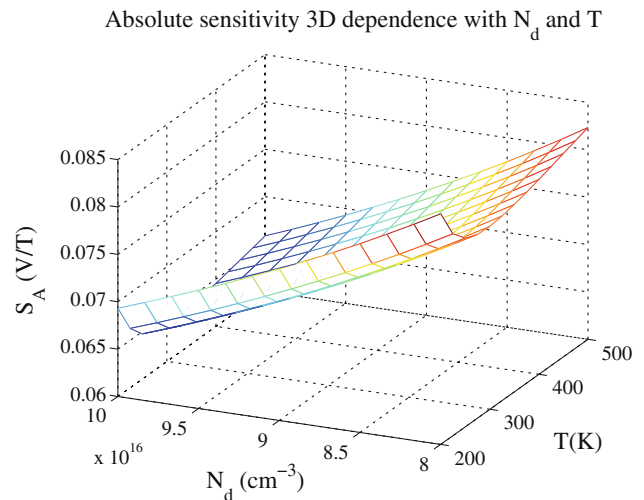


Fig. 10  $S_A = S_A(N_d, T)$

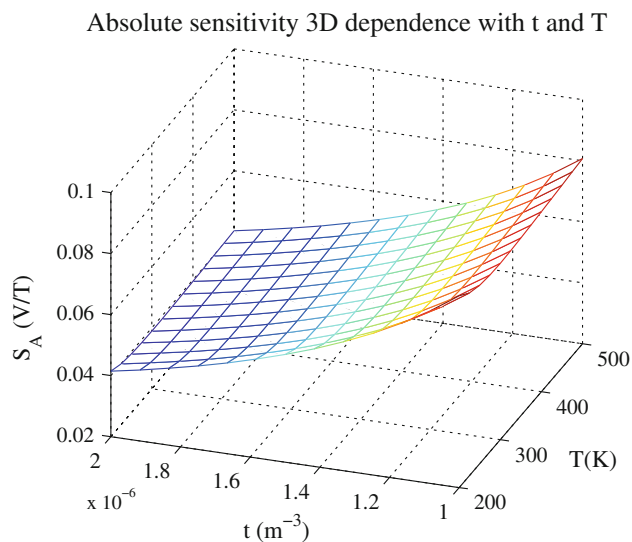
### 5.2 Three-dimensional representation of the results

Various three-dimensional representations of the simulations results were obtained in MATLAB. The focus is at this moment on the XL cell, but different integration processes are taken into account.

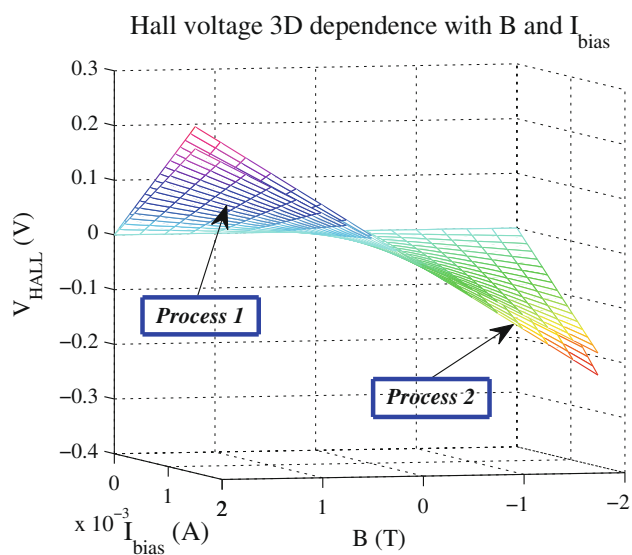
Figure 9 presents the three-dimensional representation of the absolute sensitivity as a function of both geometrical correction factor  $G$  and absolute temperature,  $S_A = S_A(G, T)$ .

Figure 10 depicts the three-dimensional representation of the absolute sensitivity as a function of both donor concentration  $N_d$  and absolute temperature,  $S_A = S_A(N_d, T)$ .

The representation of the absolute sensitivity as a function of both n-well implantation thickness  $t$  and absolute temperature,  $S_A = S_A(t, T)$  is incorporated in Fig. 11. The thickness  $t$  is considered from 1 to 2  $\mu\text{m}$ , while  $T$  is ramped from 200 to 500 K.



**Fig. 11**  $S_A = S_A(t, T)$



**Fig. 12**  $V_{\text{HALL}} = V_{\text{HALL}}(B, I_{\text{bias}})$

The Hall voltage as a function of magnetic field induction  $B$  and biasing current is represented in Fig. 12, for two integration processes. The biasing current is ramped from 0 to 1 mA and the magnetic field  $B$  from  $-2$  to 2 T.

## 6 Conclusions

The work in the present paper was devoted to presenting a detailed analysis of the Hall cells current-related sensitivity temperature dependence. A certain Hall cell which provides high performance is presented in details. To evaluate

its performance, experimental results for the sensitivity and input resistance temperature dependence were presented.

As one of the most important figure of merits in Hall cells performance is the current-related sensitivity and its temperature drift, an analytical procedure to assess this important parameter was proposed.

The current-related sensitivity temperature behavior of a particular Hall Effect sensor named XL is analyzed. To achieve this goal, all the parameters dependent with temperature were investigated. Analytical consideration of carrier concentration-temperature correlation reporting freeze-out effect was included. The drift of relative variation of the current-related sensitivity  $\gamma$  is of maximum 24,000 ppm over the entire considered temperature interval. The temperature dependence of  $\gamma$  is a parabolic-type curve with a minimum at 305 K. The results obtained are in accordance with the literature.

Three-dimensional representations of the absolute sensitivity dependence with the geometrical correction factor  $G$  and absolute temperature, as well as its variation with the n-well implantation thickness  $t$  and absolute temperature  $T$  are generated. The absolute sensitivity variation with respect to both donor concentration  $N_d$  and absolute temperature  $T$  is also depicted. The Hall voltage as a function of magnetic field induction and biasing current is represented for two different integration processes.

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