
A path choice approach to activity modeling with a pedestrian case study

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Presentation outline

- **Motivation:** Why pedestrian activities?
- **Detection:** Where are pedestrians?
- **Modeling** pedestrian behavior:
 - Activity-episode sequences and activity patterns
 - Activity network
 - Activity paths
 - Choice set generation
 - Activity path choice model for WiFi traces
- **Conclusion**
- **Future work**

MOTIVATION



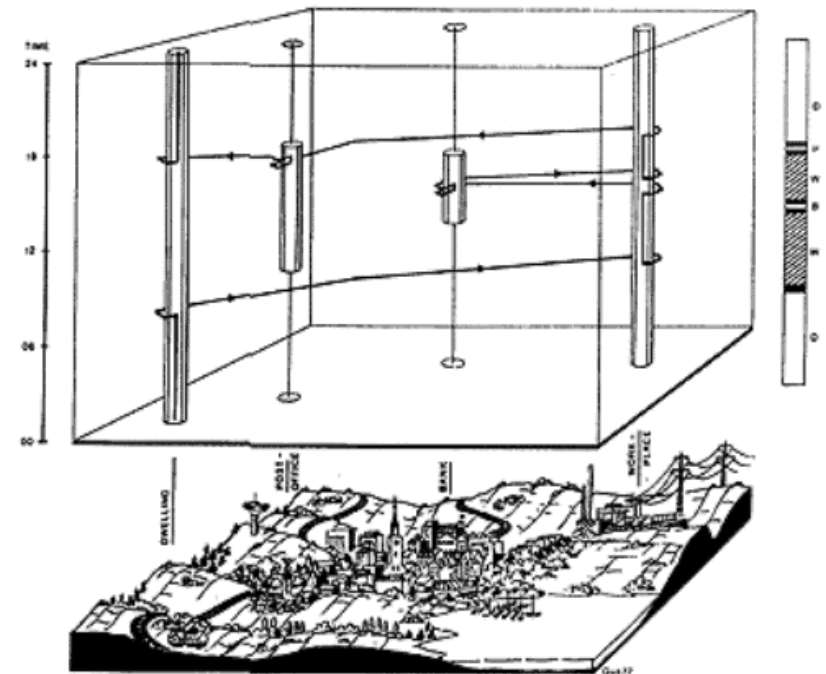
Activity modeling for pedestrian infrastructure

Goal

- Adapt traditional activity modeling framework for pedestrian activities

Challenges

- Detect pedestrians
- Model activity patterns
- Forecast scenarios



Carlstein, T. (1978)

3 examples

- **Multimodal transport hubs:**
Lausanne railway station
- **Mass gathering:**
Paléo music festival
- **Campus:**
EPFL new “Quartier Nord”

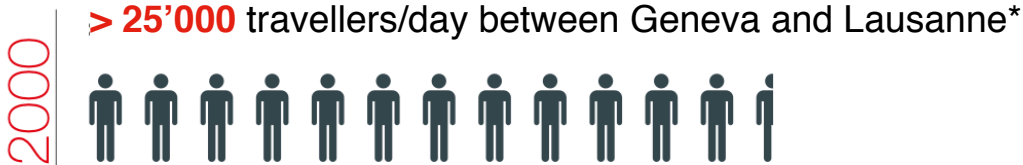
Walking is the key for efficient multimodal transport systems



Crowd in a railway station in Mumbai, India
Photo: National Geographic

Lake Geneva region: Léman 2030

By 2030, **100'000** passengers per day between Geneva and Lausanne



 = 2000 travelers/day

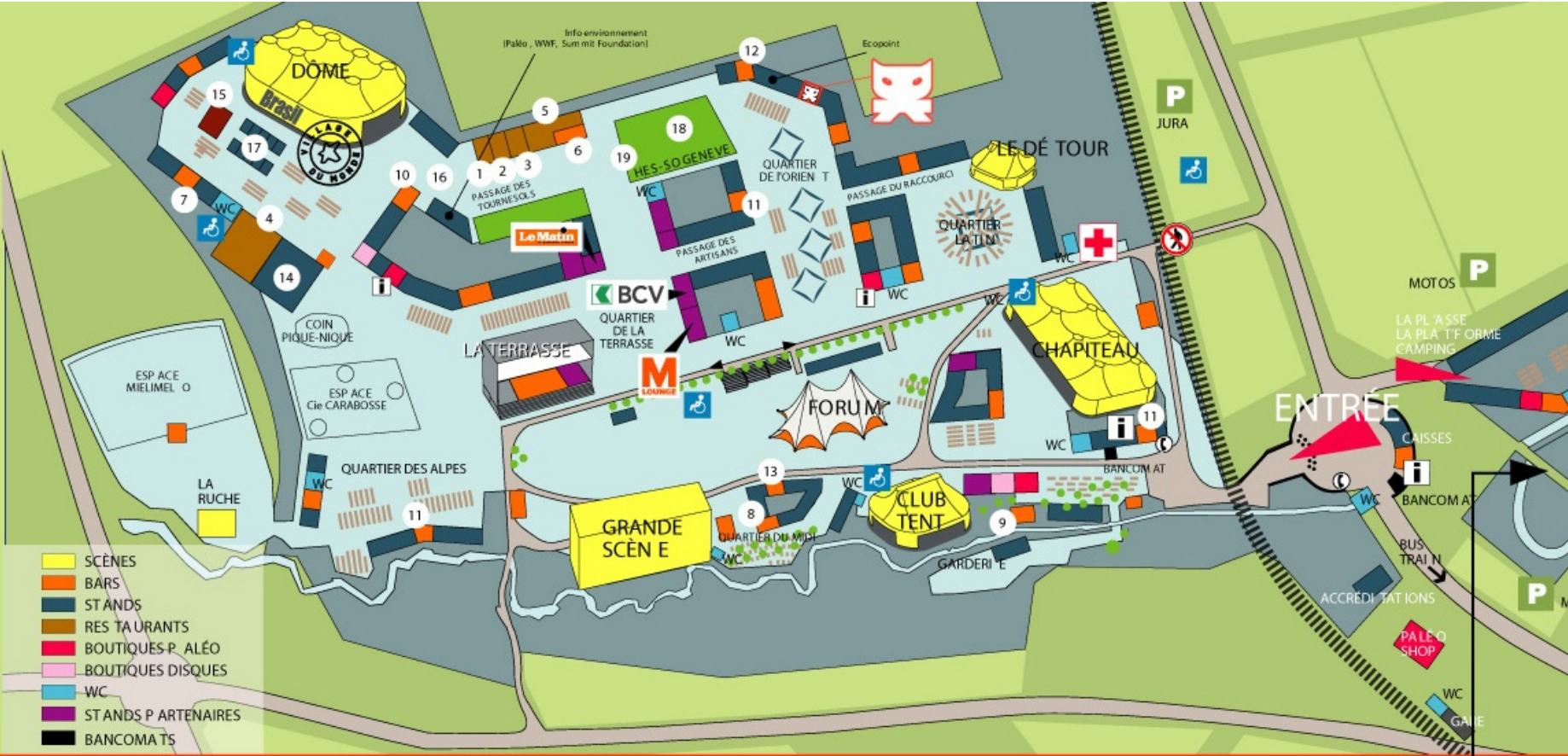
* Forecast by Swiss Railways for the maximum scenario



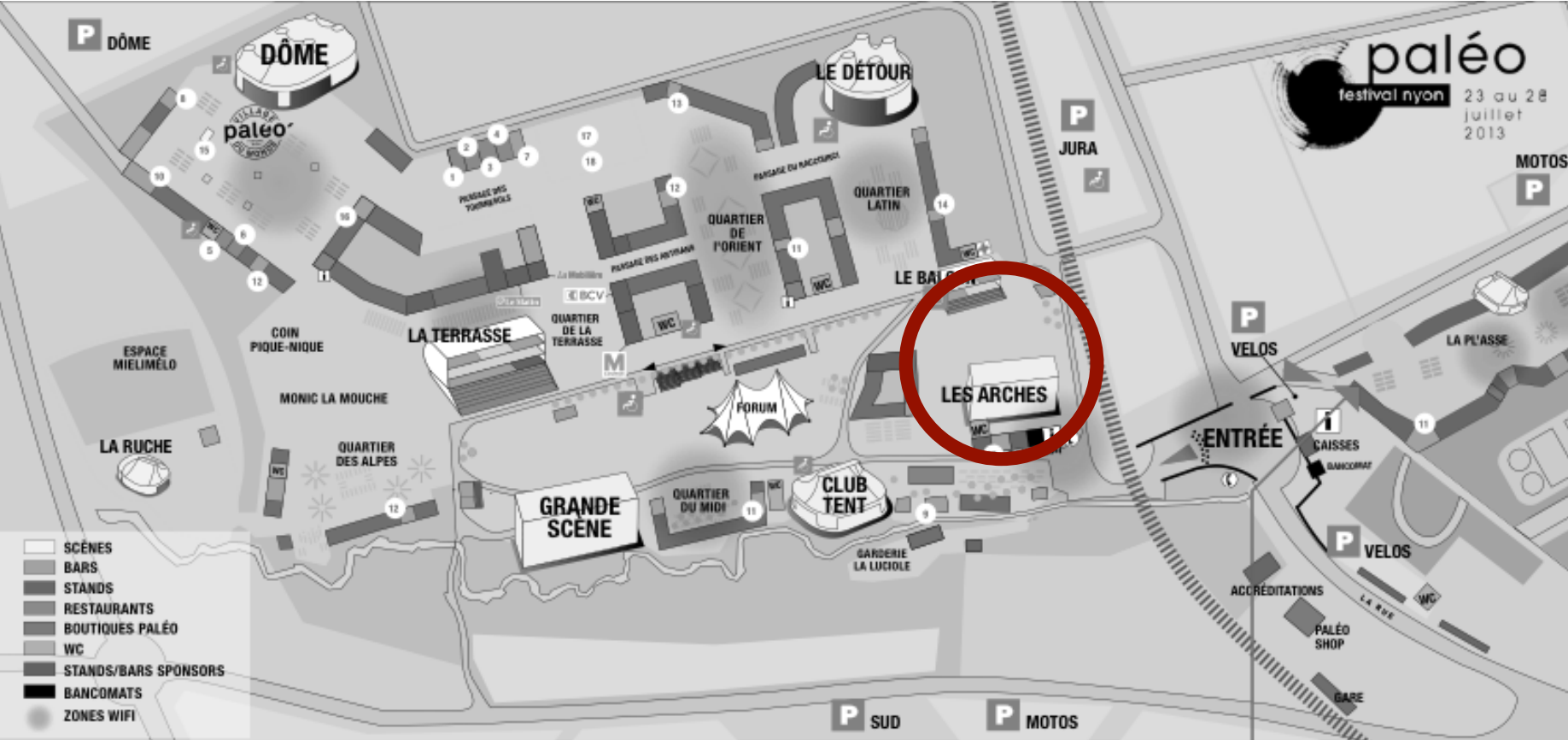
Mass gathering



Paléo 2012



Paléo 2013



Campus



EPFL

Quartier Nord



Campus



DETECTION



Data input

- Localization data with full coverage of the facility
- Semantically-enriched routing graph for pedestrians
- Potential attractivity measure

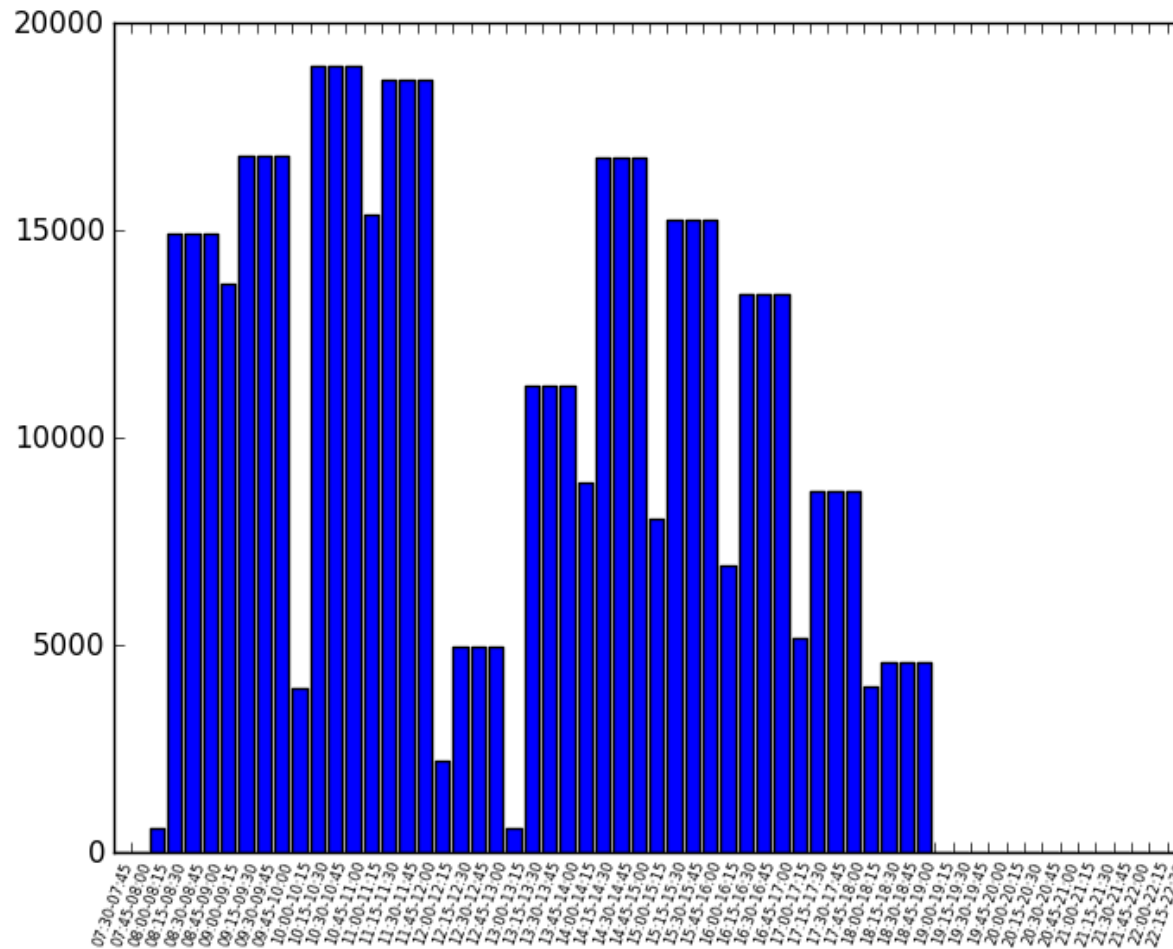
Data requirement: Potential attractivity

- **Potential attractivity measure (PAM)** depends on
 - **Destination attractivity** $att(x, t)$
 - Classroom, platform, scene, ...
 - **Time-constraints** $\delta_{x,i}(t)$
 - Class schedules, train schedules, opening hours, ...

$$PAM_{x,i}(t^-, t^+) = \int_{t=t^-}^{t^+} \delta_{x,i}(t) \cdot att(x, t)$$

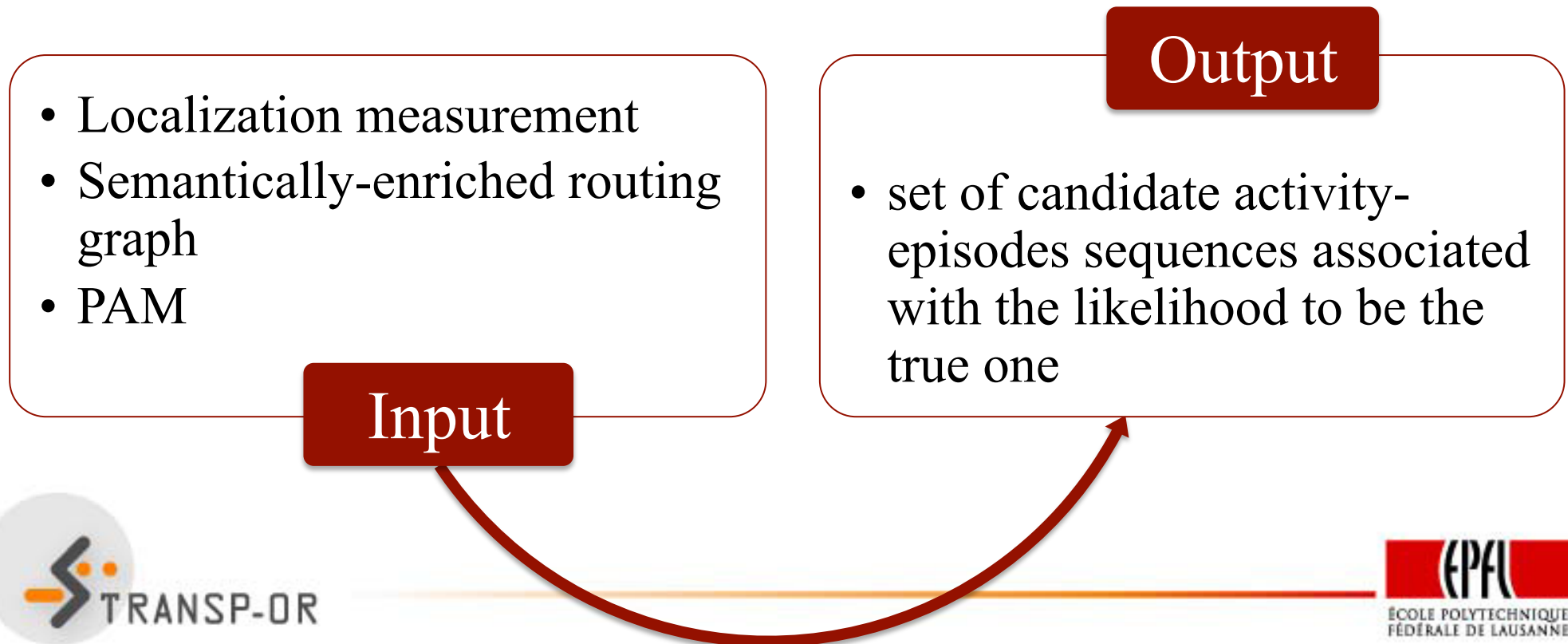
- **Examples:**
 - 1500 passengers on platform 4 arriving at 16h04
 - 32 students in a classroom from 8h15 to 10h
 - 400 seats in a restaurant open from 11h to 14h30

Data requirement: Potential attractiveness



Methodology

- **Goal:** extract the possible activity-episodes performed by pedestrians from digital traces from communication networks



Probabilistic measurement model

Measurement likelihood

Prior

$$P(a_{1:m} | \hat{s}_{1:n}) \propto P(\hat{s}_{1:n} | a_{1:m}) \cdot P(a_{1:m})$$

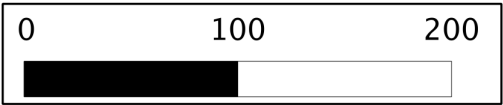
Activity probability

Legend

WiFi Data

◆

Pedestrian network



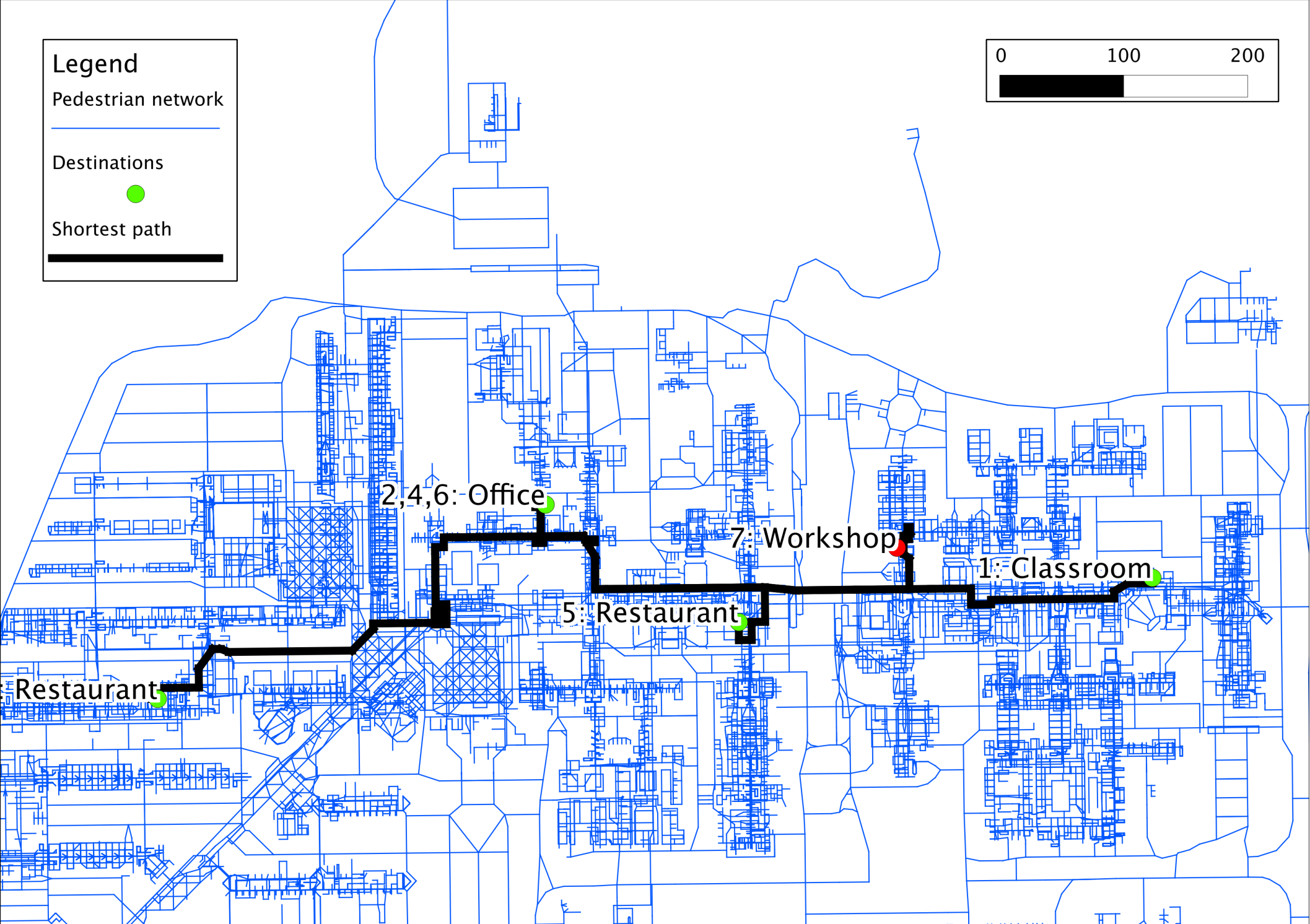
Legend

Pedestrian network

Destinations

Shortest path

0 100 200



2,4,6: Office

7: Workshop

1: Classroom

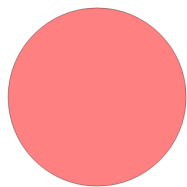
5: Restaurant

Restaurant

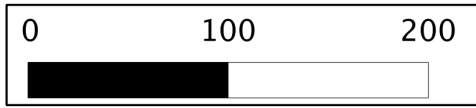
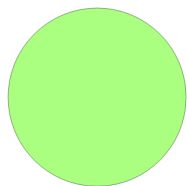
Legend

Pedestrian network

Wrong activity type



Correct activity type



More on detection

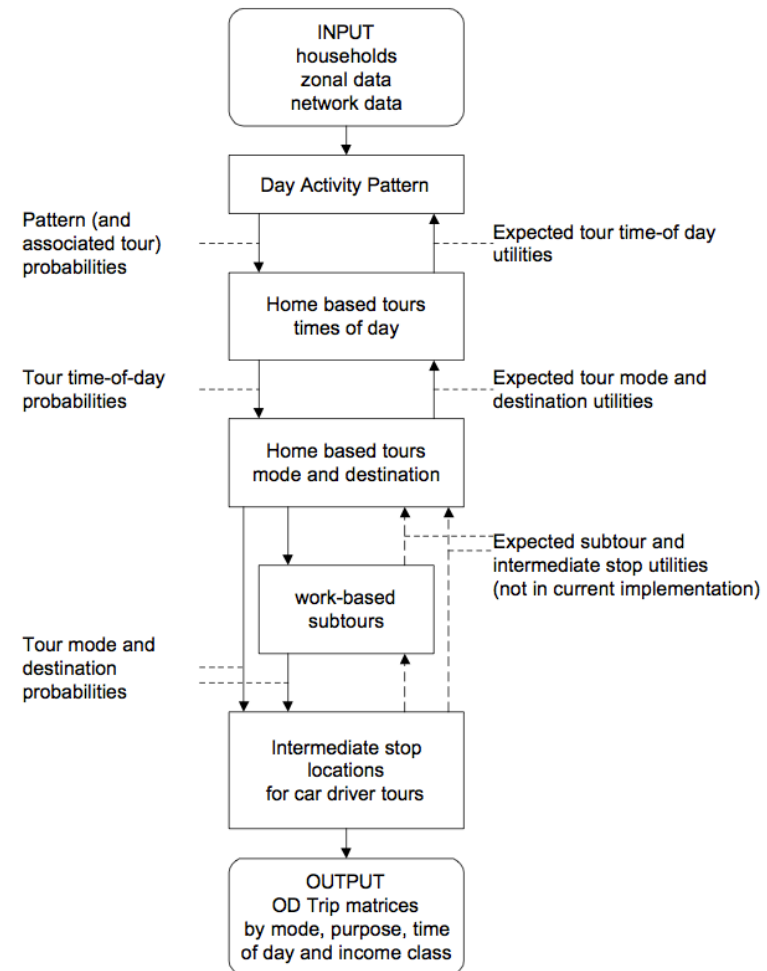
- Technical report:
[A. Danalet, B. Farooq and M. Bierlaire. A Bayesian Approach to Detect Pedestrian Destination-Sequences from WiFi Signatures, 2013.](#)

A PATH CHOICE APPROACH TO ACTIVITY MODELING



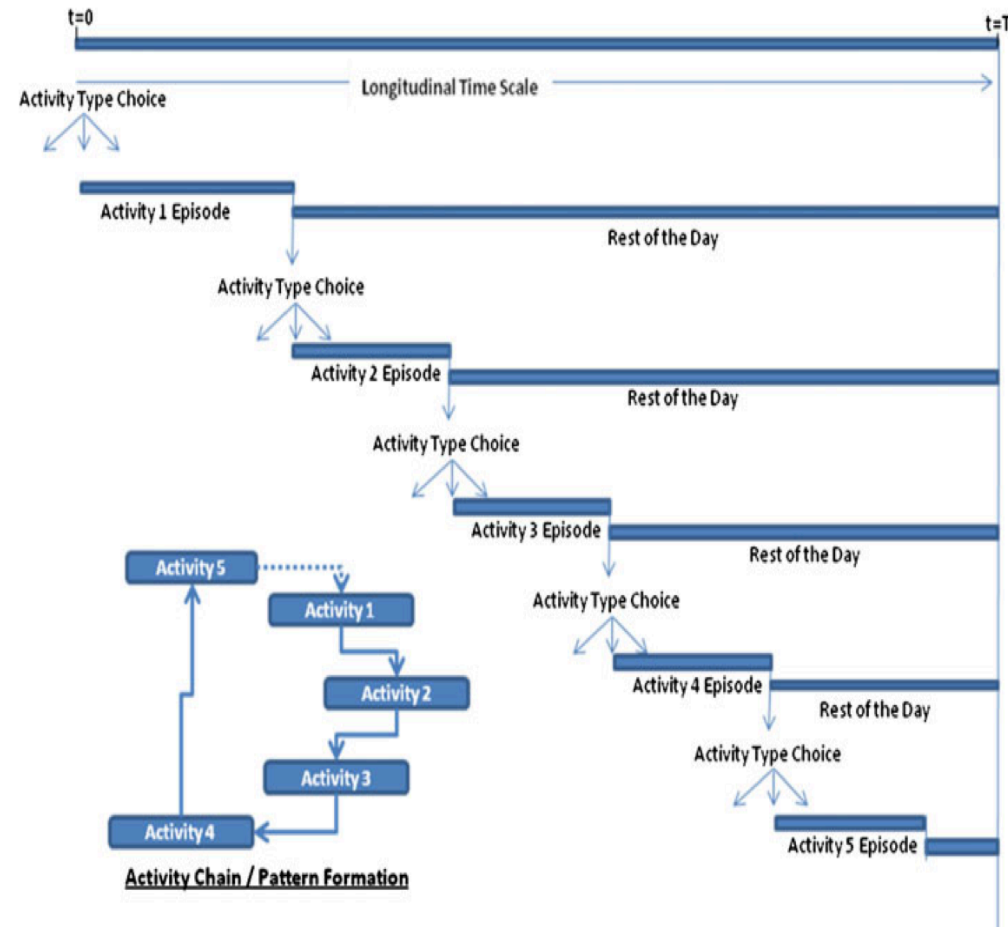
Activity travel pattern

- System of choice models (Bowman, 1998)
 - Activity pattern choice model
 - Tour choice model
 - primary destination
 - mode choice
 - time of day
 - number of stops in the tour
 - Trip choice model
 - idem, for secondary destinations



Dynamic discrete continuous models

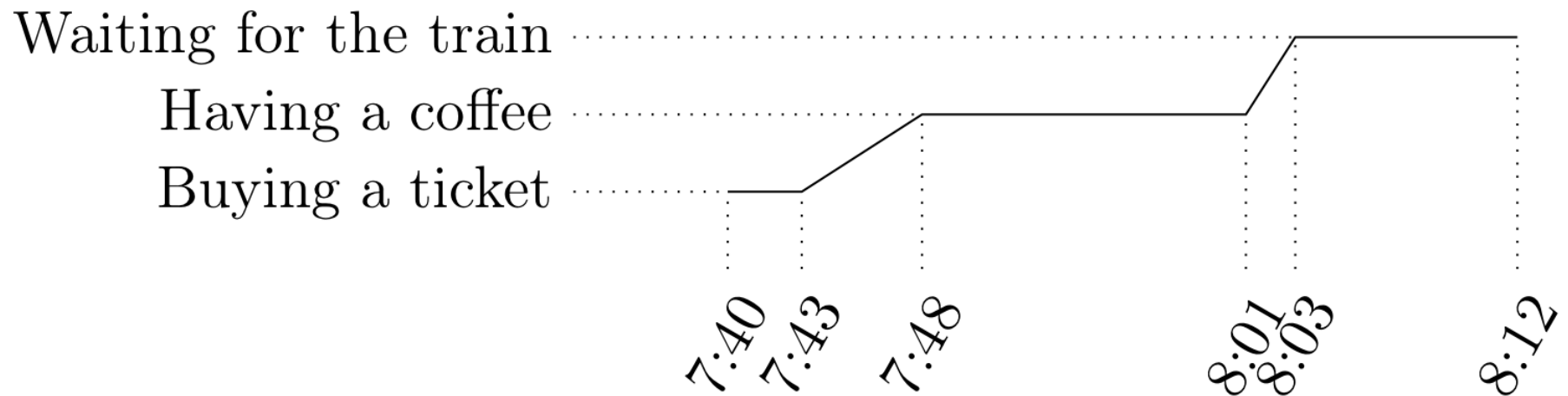
- Continuous time
- Composite activity integrating all activities in the rest of the day
- Maximization of utility between the current specific activity and the composite future activity
- Activity pattern built sequentially



Habib, K. M. N. (2011)

Activity-episode sequences and activity patterns

Activity types



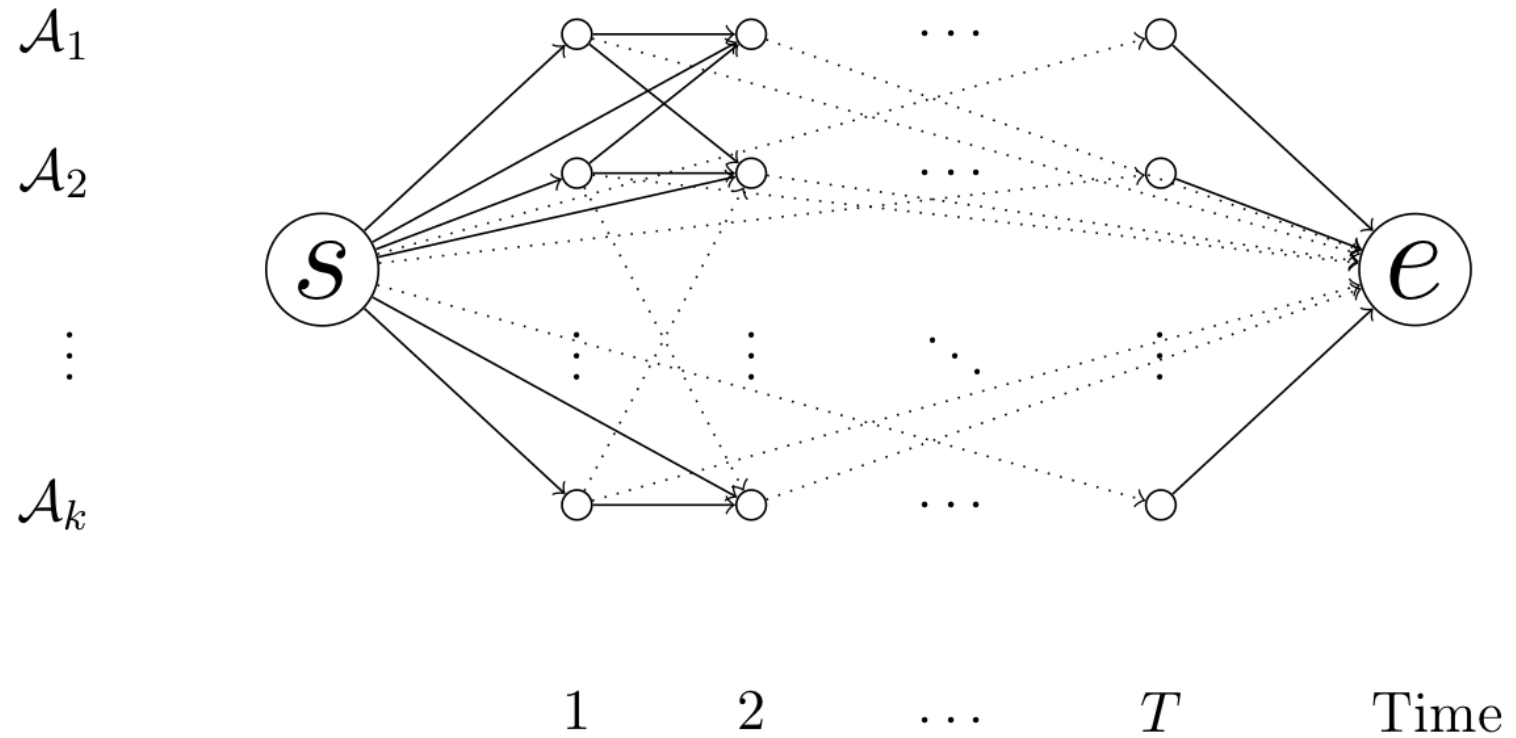
Activity-episode sequences and activity patterns

- Activity episode $a_n = (x, t^-, t^+)$
 - Start and end times are continuous random variables
 - Activity-episode sequences $(a_1, \dots, a_{M_n}) = a_{1:M_n}$
- Activity types $\mathcal{A}_1, \mathcal{A}_2, \dots, \mathcal{A}_K$
- Activity $A_n = (A(a_n), t^-, t^+)$
 - Activity pattern $(A_1, \dots, A_{M_n}) = A_{1:M_n}$
 - Set of all activity patterns corresponding to an observation \mathcal{L}_i
- All activity patterns are associated to a measurement likelihood
- Activity patterns are the behavior we observe

Activity network

Activity types

Activity network



Activity network

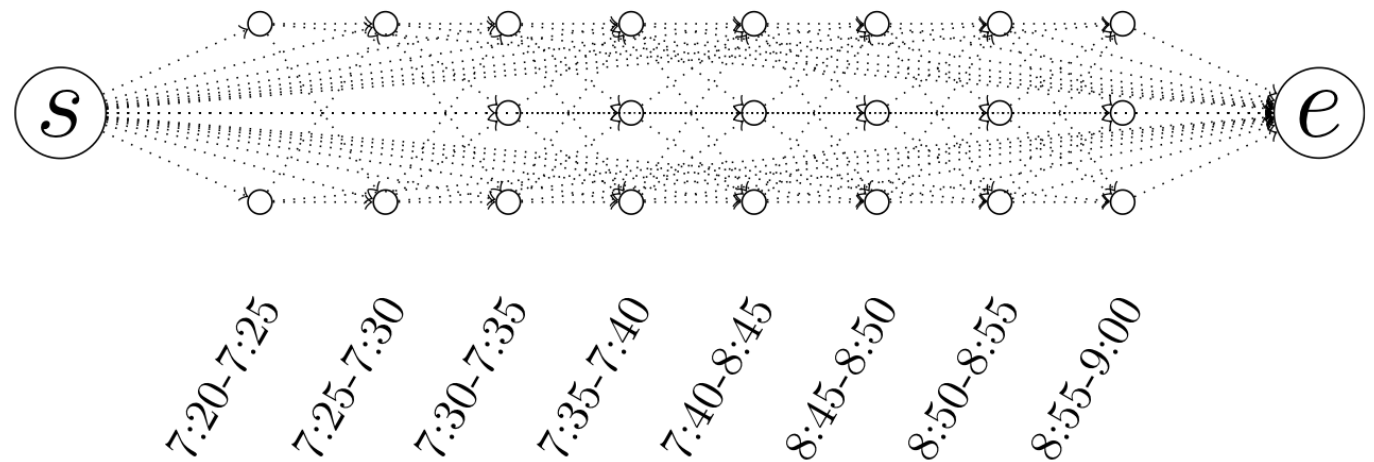
Activity types

Activity network

Waiting for the train

Having a coffee

Buying a ticket



Activity network

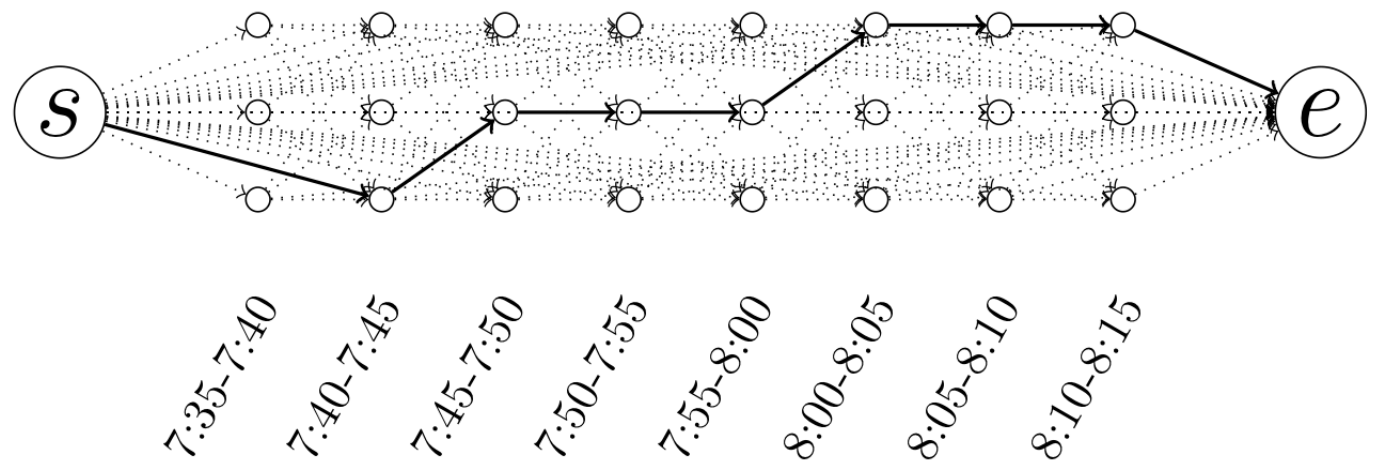
- Contains all possible activity patterns
 - Universal choice set
- Discretization of time $\tau \in 1, 2, \dots, T$
- Nodes $\mathcal{A}_{k,\tau}$
 - represent the performance by an individual of an activity type k for a unit of time τ
 - Beginning and end of the observed activity pattern: s, e
 - Max number of nodes: $KT + 2$
- Edges
 - Max number of edges: $2KT + K^2T$

Activity paths

Waiting for the train

Having a coffee

Buying a ticket



Activity paths $\mathcal{A}_{1:T}$

- Representation of $A_{1:M_n}$ in an activity network
- All activity paths are associated to a measurement likelihood
- Activity of the time unit in the activity network = longest activity in the activity pattern for this time interval

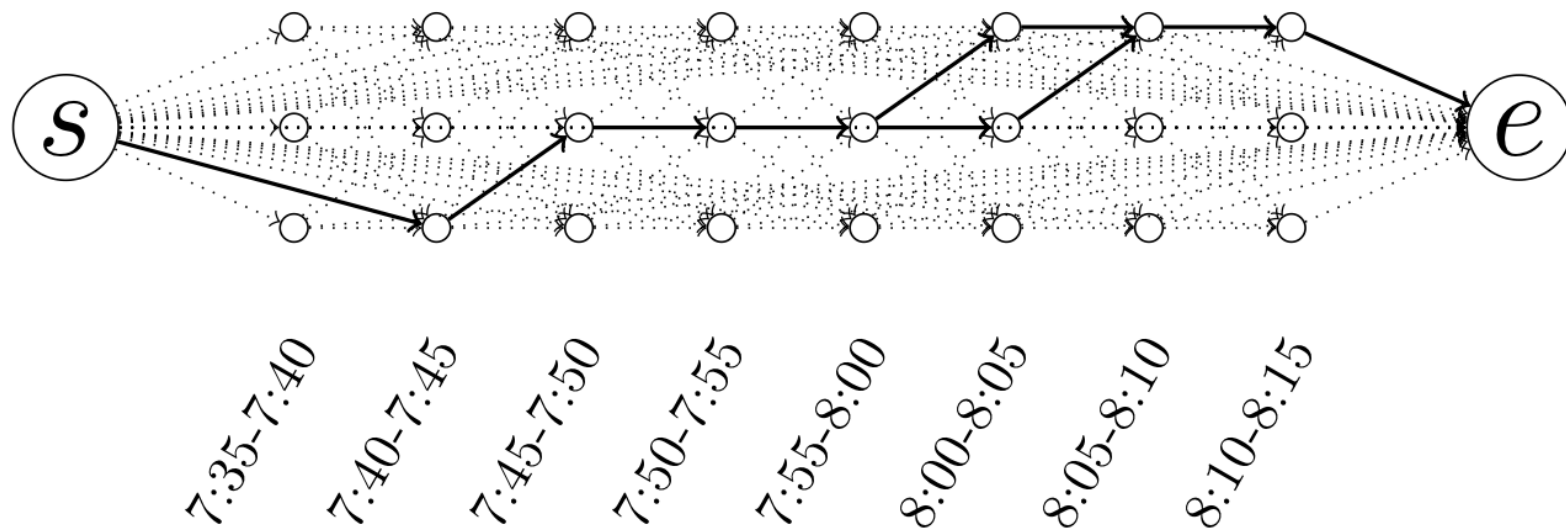
Activity paths

- Time is a random variable. If support is larger than a time unit, one activity pattern can be represented by several activity paths

Waiting for the train

Having a coffee

Buying a ticket



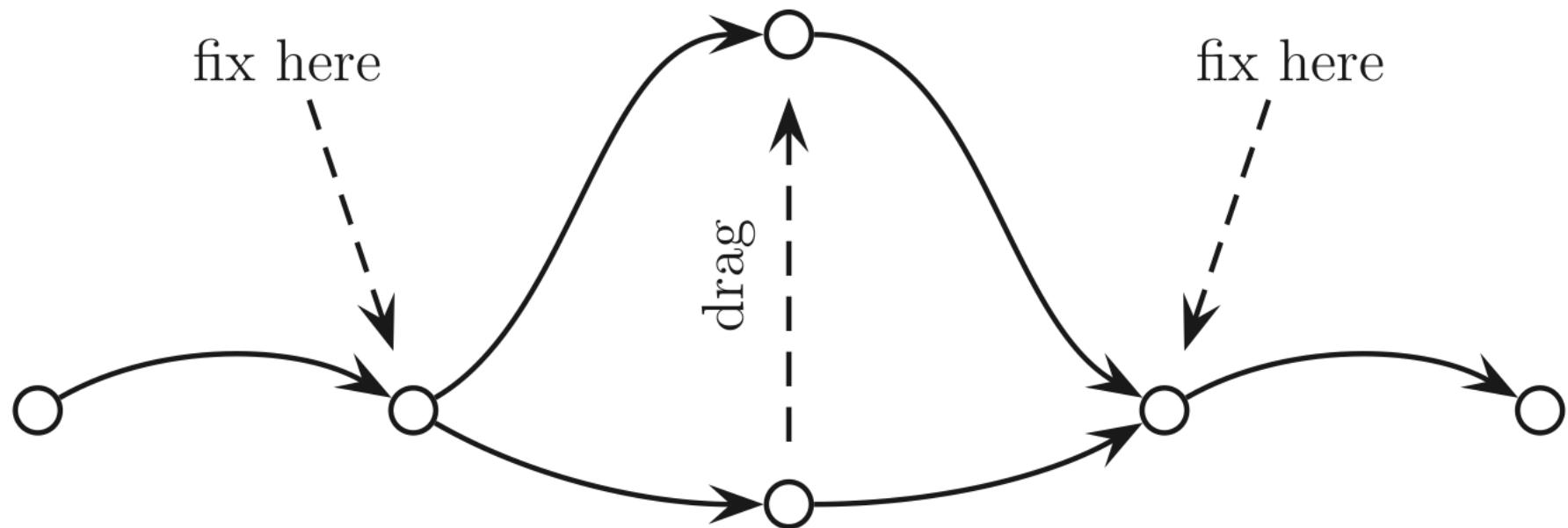
Choice set generation

- In route choice context, universal choice set is big
- Decision maker doesn't consider all of them
- Consideration choice set not available or too small
- Consideration choice set modeling
 - Latent class choice model
 - Repeated shortest path search
 - Branch-and-bound
- Sampling of alternatives from the universal choice set
 - Frejinger, Bierlaire and Ben-Akiva (2009)
 - Fosgerau, Frejinger and Karlstrom (2013)

Choice set generation: Metropolis-Hastings algorithm

- Flötteröd and Bierlaire (2013)
- Paths are sampled according to an arbitrary distribution, avoiding complete enumeration
- Sampling probabilities do not need to be defined by link, but can be defined directly for the whole path
- Chen (2013) in Ch.5: weight function is composed of the length and frequency of observation
- Frejinger and Bierlaire (2010): « sample should include attractive alternatives »

Choice set generation: Metropolis-Hastings algorithm



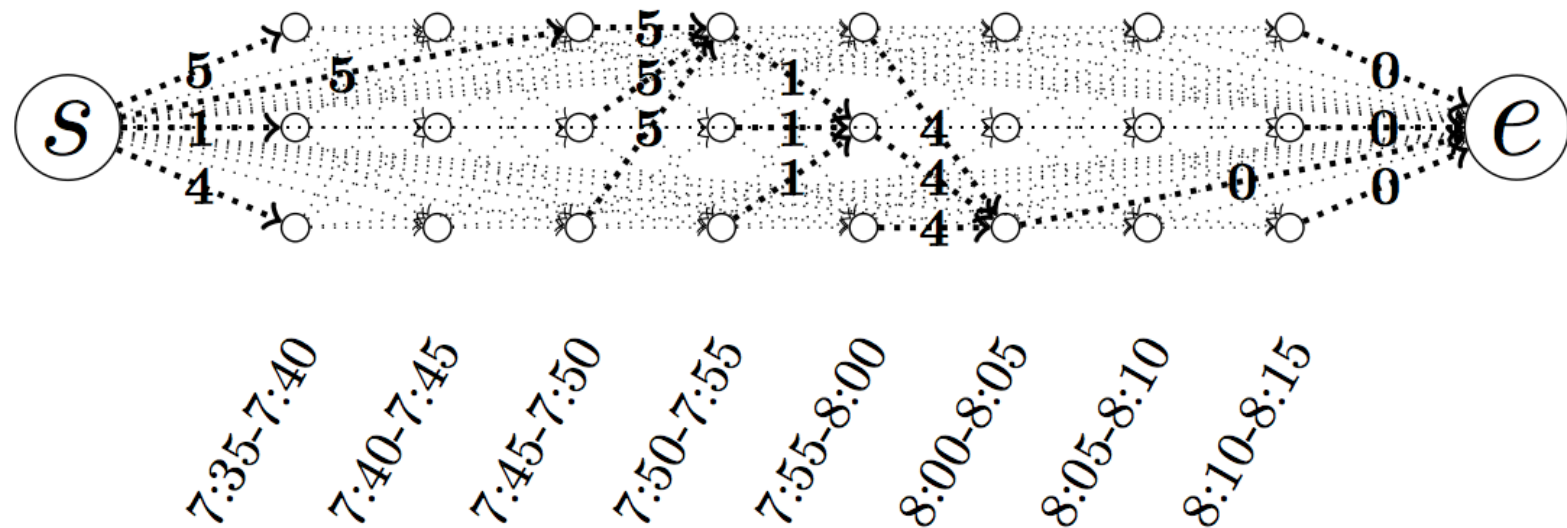
Choice set generation in the activity network

- We propose to use potential attractivity measure

Waiting for the train

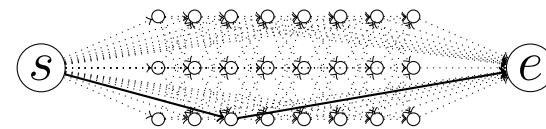
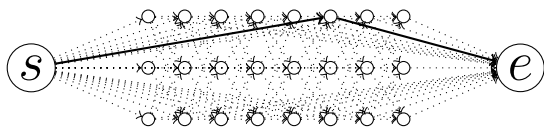
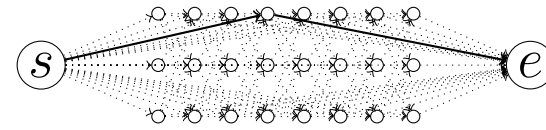
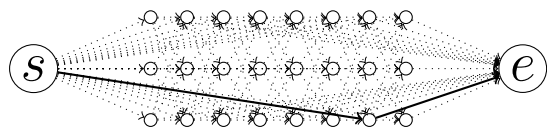
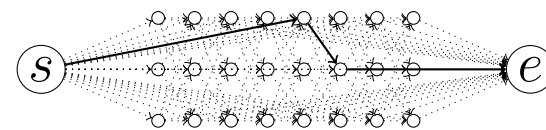
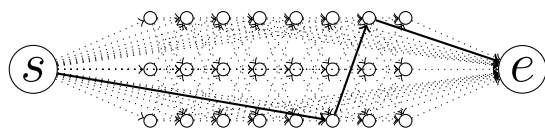
Having a coffee

Buying a ticket



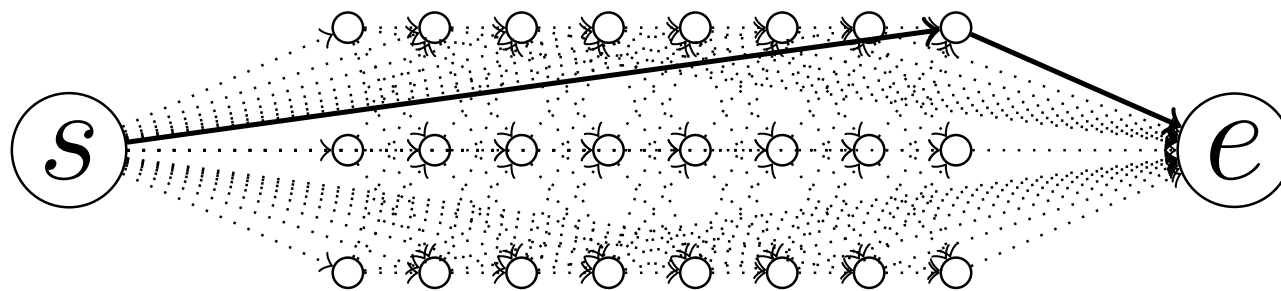
Choice set generation in the activity network

- Based only on potential attractivity measure:
too short (based on shortest path)



Choice set generation in the activity network

- Force it to end on the platform: same problem
- Most likely output is



Choice set generation in the activity network

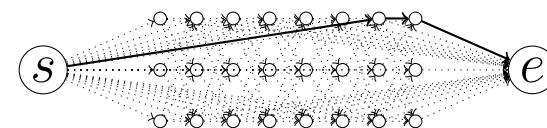
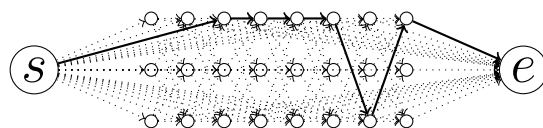
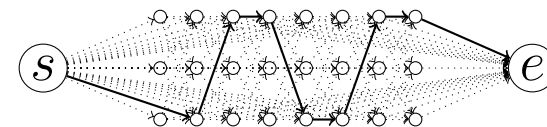
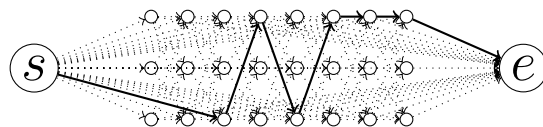
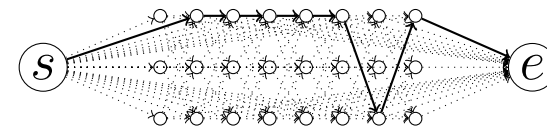
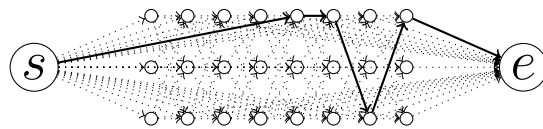
- Attractivity is link additive
- With the Metropolis-Hastings algorithm, possibility to define non-link-additive cost
- Penalty for path length different from the observed ones

$$\delta_{\Gamma}(\Gamma) = \prod_{k=1}^K \left(\frac{1}{N} \sum_{\mathcal{A}_{1:T} \in N} \mathcal{I}(|\mathcal{A}_{1:T,k}| = |\Gamma_k|) \right)$$

Choice set generation in the activity network

- With target weight defined as

$$\delta(\Gamma) = -\mu_v \cdot \sum_{v \in \Gamma} \delta_v(v) - \delta_{\Gamma}(\Gamma)$$



Activity path choice model for WiFi traces

- Inspired by Bierlaire and Frejinger (2008) and Chen (2013): each individual n generates J network-free signals $\hat{s}_{1:J}$

$$P(\hat{s}_{1:J}) = \sum_{\mathcal{A}_{1:T} \in \mathcal{U}} P(\hat{s}_{1:J} | \mathcal{A}_{1:T}) \cdot P(\mathcal{A}_{1:T} | \mathcal{U}; \beta)$$

Measurement likelihood

Choice model

Activity path choice model for WiFi traces: route choice model

- To be operationalized, the model must correct
 - for the sampling of alternatives
 - for the correlation structure of a route choice

Activity path choice model for WiFi traces: sampling of alternatives

- Frejinger et al. (2009): a sampling correction term must be added

$$\ln q(\mathcal{C}_n | \Gamma) = \ln \frac{k_{\Gamma_n}}{q(\Gamma)}$$

Nb of occurrences

Sampling probability

- Sampling probability requires full enumeration

$$q(\Gamma) = \frac{b(\Gamma)}{\sum_{\Gamma' \in \mathcal{U}} b(\Gamma')}$$

but cancels out in logit

Activity path choice model for WiFi traces: sampling of alternatives

$$\begin{aligned}
 P(\Gamma | \mathcal{C}_n) &= \frac{e^{\mu V_{\Gamma n} + \ln \frac{k_{\Gamma n}}{q(\Gamma)}}}{\sum_{\Gamma' \in \mathcal{C}_n} e^{\mu V_{\Gamma' n} + \ln \frac{k_{\Gamma' n}}{q(\Gamma')}}} \\
 &= \frac{\sum_{\Gamma' \in \mathcal{U}} b(\Gamma') \cdot e^{\mu V_{\Gamma' n}} \cdot \frac{k_{\Gamma' n}}{b(\Gamma')}}{\sum_{\Gamma' \in \mathcal{U}} b(\Gamma') \cdot \sum_{\Gamma' \in \mathcal{C}_n} e^{\mu V_{\Gamma' n}} \cdot \frac{k_{\Gamma' n}}{b(\Gamma')}}} \\
 &= \frac{e^{\mu V_{\Gamma n}} \cdot \frac{k_{\Gamma n}}{b(\Gamma)}}{\sum_{\Gamma' \in \mathcal{C}_n} e^{\mu V_{\Gamma' n}} \cdot \frac{k_{\Gamma' n}}{b(\Gamma')}}}
 \end{aligned}$$

Activity path choice model for WiFi traces: path size

- Ben-Akiva and Bierlaire (1999): path size logit
- Path size attribute PS_p corrects the utility for the correlation related to overlapping segments

$$PS_{\Gamma} = \sum_{a \in \Gamma} \frac{1}{M_a} \frac{L_a}{L_{\Gamma}}$$

L_a ← Arcs and
 L_{Γ} ← path length

- When using universal choice set, full enumeration

$$M_a = \sum_{\Gamma' \in \mathcal{U}} \delta_{a\Gamma'}$$

$\delta_{a\Gamma'}$ ← link-path
 incidence variable

- Frejinger et al. (2009): use a large set of paths

Activity path choice model for WiFi traces: activity path size

- Due to the structure of the activity network, the activity path size is:

$$APS_{\Gamma} = \frac{1}{K^{\tau-1}}$$

- The deterministic part of the utility function

$$V_{\Gamma n} = \beta x + \ln \frac{k_{\Gamma n}}{b(\Gamma)} + \beta_{PS} \ln APS_{\Gamma}$$

CONCLUSION



Conclusion

- Discretization of time: loosing information but
 - Easier to specify
 - Integration of measurement error in the model
- Modeling framework
 - allows to define choice attributes related to the whole activity pattern (e.g., number of episodes, number of times in the shopping mall or restaurant, etc.)
 - does not need an *a priori* definition of primary activity
 - does not need the definition of *home*

FUTURE WORK



Future work

- Implementation of the model on campus data
- Currently: activity = location category (e.g. “studying = classroom”)
 - If the share of activities per location category does not change over time: prediction still all right
 - If they change? Stated preference survey about activities per location category?
- Once activity/location category chosen: destination choice conditional on it

$$P(a_{1:M_n}) = P(\mathcal{A}_{1:T}) \cdot P(x|\mathcal{A}_{1:T})$$

THANK YOU



References

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