



# Kinetic Modeling of Batch Slurry Reactions

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# Overall project goal – develop monitoring technique for batch processes involving slurries

- Extend kinetic modeling approach to a prototypical slurry reaction at DuPont: sulfonylurea coupling reaction for **monitoring** purposes
- Make optical measurements in light-scattering medium
- Modify kinetic models to include:
  - Dissolution of starting material A & flow-in of reagent B
  - Nucleation and crystallization of product, P
- Develop **empirical** models for dissolution, nucleation and crystallization
- Kinetic models with reagent flow-in impose strict mass balance



# Isothermal model with flow-in reagents

$$r_1 = k_1 C_{SA} C_{AA}$$

$$r_2 = k_2 C_I$$

$$r_3 = k_3 C_W C_{AA}$$

$$r_4 = k_4 C_{ASA} C_{AA}$$

$$\frac{dC_{AA}}{dt} = -r_1 - r_3 - r_4 + \frac{C_{AAin} - C_{AA}}{V} F_{AA}$$

$$\frac{dC_I}{dt} = r_1 - r_2 - \frac{C_I}{V} F_{AA}$$

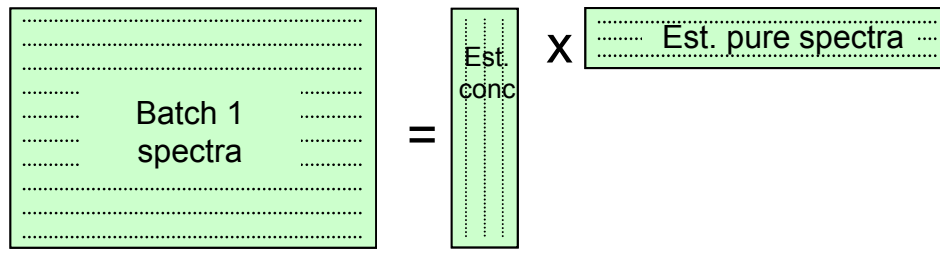
$$\frac{dC_{SA}}{dt} = -r_1 - \frac{C_{SA}}{V} F_{AA}$$

$$\frac{dC_W}{dt} = -r_3 - \frac{C_W}{V} F_{AA}$$

$$\frac{dC_{ASAA}}{dt} = r_4 - \frac{C_{ASAA}}{V} F_{AA}$$

$$\frac{dC_{HA}}{dt} = r_2 + 2r_3 + r_4 - \frac{C_{HA}}{V} F_{AA}$$

$$\frac{dV}{dt} = F_{AA}$$





# Slurries

- A dynamic system of crystalline material suspended in a liquid medium
- Common Examples
  - Production of pharmaceuticals
  - Production of fine chemicals
  - Biological absorption of pharmaceuticals
- Dynamic processes
  - Dissolution of starting materials
  - Nucleation and crystal growth of products
- Crystal products
  - Often desire specific properties
    - Size distribution, lattice form, etc.
  - Relative rates determine properties
  - Factors governing process rates
    - Temperature
    - Rate of stirring
    - Crystal surface area
    - Attrition
    - Agglomeration



# Challenges – Optical Methods in Slurries

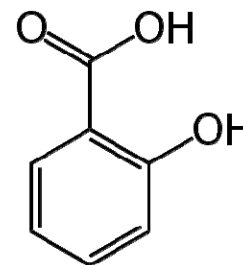
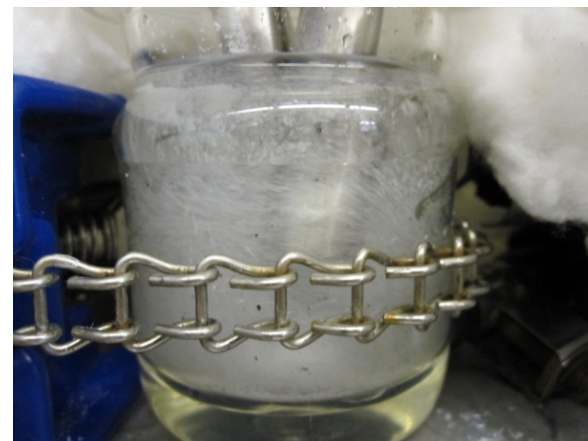
- Linear response is needed for kinetic modeling and self-modeling curve resolution
- Reflectance measurements include both light scattering and light absorption signals
  - Mathematical resolution of the two is needed to estimate solid fraction and dissolved fraction
  - Effective path length is dependent on
    - Number density of light scattering particles
    - Particle size distribution
    - Wavelength
- ATR measurements for light absorption (dissolved fraction)



# Project 1: modeling of dissolution of salicylic acid

$$r = k(c_{sat} - c)^n$$

- ❑ Develop a kinetic model for the dissolution of salicylic acid in a solvent mixture (52% ethanol, 48% water), based on a power law equation
  - ❑ simpler system, easily controlled
  - ❑ help **gain understanding** about kinetic of dissolution and crystallization in general
  - ❑ Precisely controlled conditions will facilitate model validation
- ❑ Optimize the rate constant ( $k$ ) and the exponent ( $n$ ) of the power law equation



**Salicylic acid**

M.W. 138.12 g mol<sup>-1</sup>

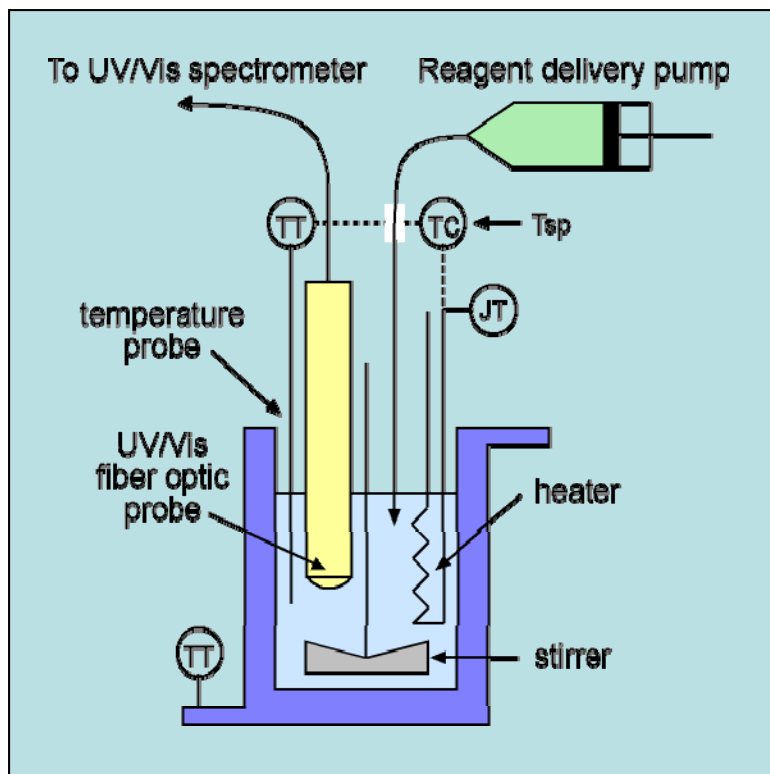
pKa 2.97

Monoclinic



# Laboratory scale batch reactors

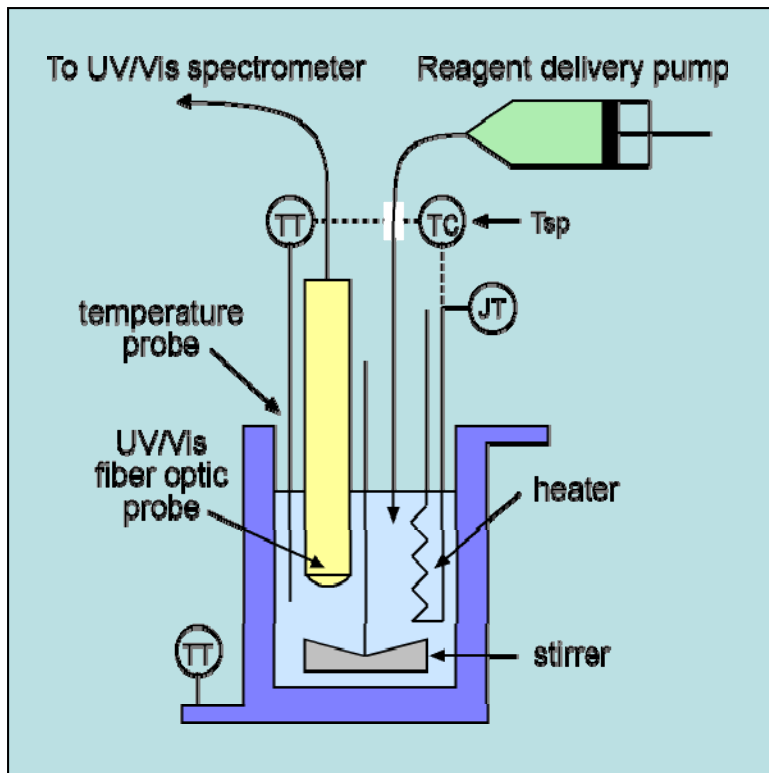
## Batch Titration Reactor





# Laboratory scale batch reactors

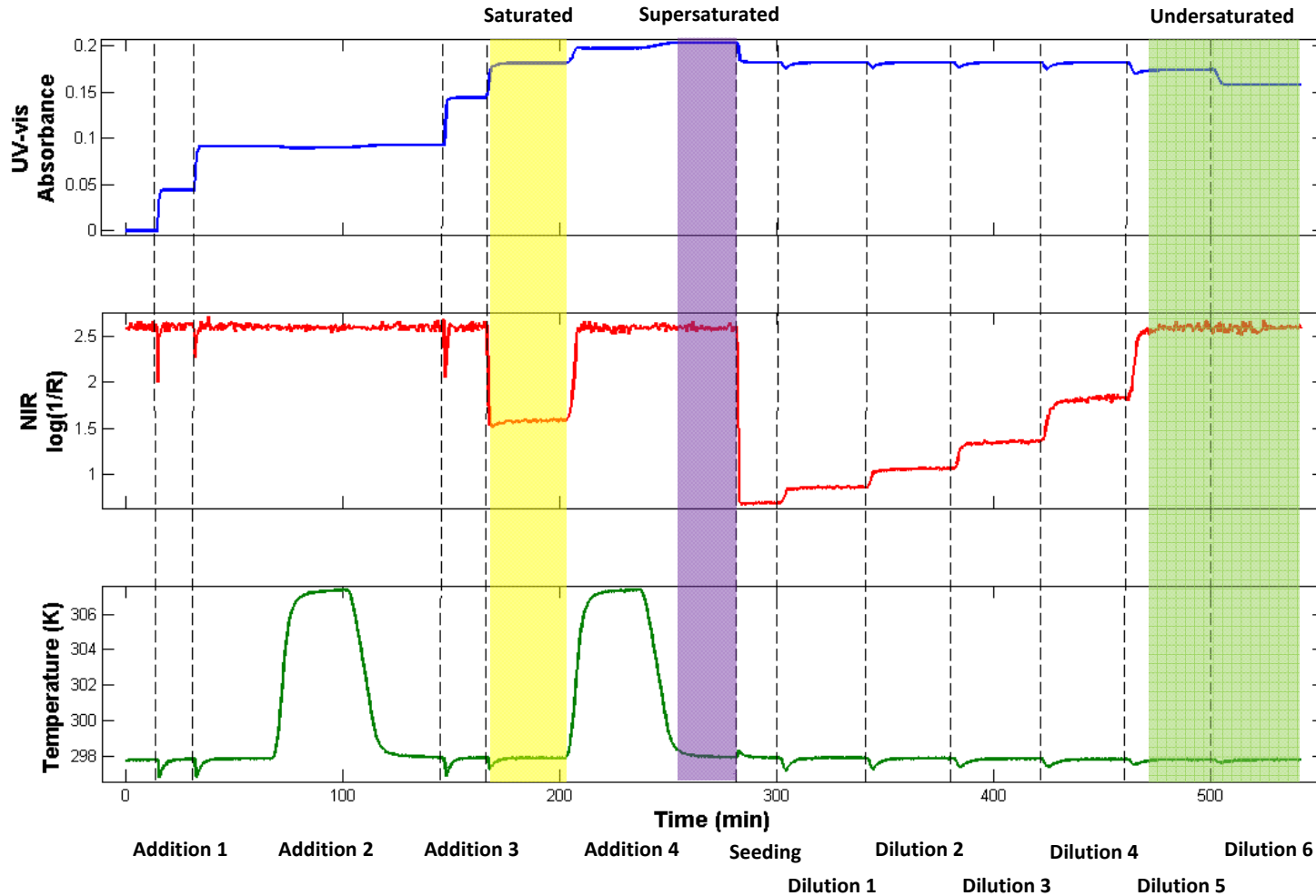
## Batch Titration Reactor







# Dissolution of salicylic acid





# Simplifying Assumptions

- Crystallization Rate

high theory model

$$r_c = \frac{\cancel{\Phi_s} \cancel{MW_s} k_c}{\cancel{3d_s} \cancel{\Phi_v}} \eta_r (c - c_{sat})^g$$

low theory model

$$r_c = k_c (c - c_{sat})^g$$

- Dissolution Rate

$$r_d = \frac{\cancel{2MW_s} k_d}{\cancel{d_s}} (c_{sat} - c)$$

$$r_d = m \cdot k_d (c_{sat} - c)^n$$

Assumptions:

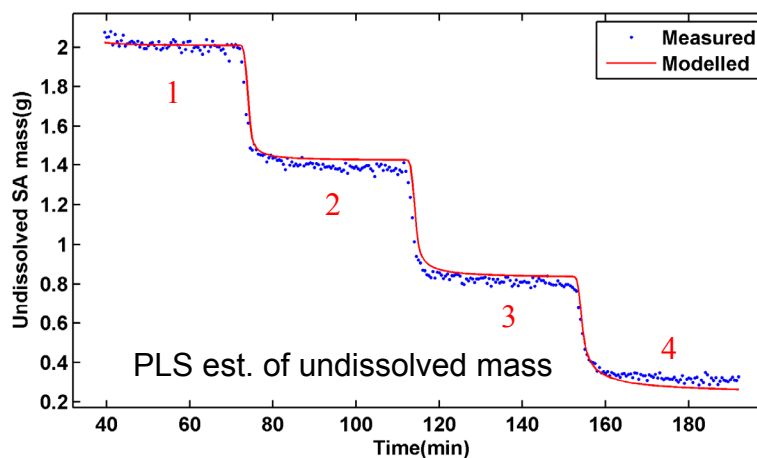
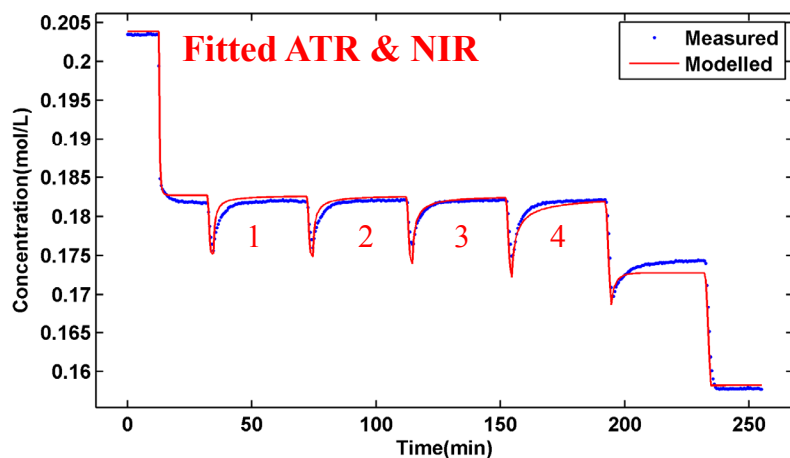
**Well-mixed** slurries, the **length** of crystals, solid density, effectiveness factor, molecular weight of the solid, **surface** factor and **volumetric** shape factor do not change significantly in these experiments.



# Model batch (08-29-10)

Hessian					
1.0000	-0.9383	-1.0000	0.6118	0.1929	0.1540
-0.9383	1.0000	0.9384	-0.5082	-0.2022	-0.1508
-1.0000	0.9384	1.0000	-0.6116	-0.1928	-0.1540
0.6118	-0.5082	-0.6116	1.0000	0.7244	0.0860
0.1929	-0.2022	-0.1928	0.7244	1.0000	-0.0514
0.1540	-0.1508	-0.1540	0.0860	-0.0514	1.0000

UV-vis range used:: 270 – 360 nm, NIR range used: 1100 nm



### Initial Conditions:

- Dissolution rate constant ( $k_d$ ) = 30.00 L<sup>n-1</sup>/(mol<sup>n-1</sup>min)
- Crystallization rate constant ( $k_c$ ) = 15.00 L<sup>n-1</sup>/(mol<sup>n-1</sup>min)
- Order parameter ( $n$ ) = 1.800
- Order parameter ( $g$ ) = 1.700
- Total SA mass added ( $m_t$ ) = 3.1882 g
- Concentration ( $c_0$ ) = 1.0176 (mol/L)
- Saturation limit ( $c_{sat}$ ) = 0.9075
- Initial volume ( $v_0$ ) = 22.7 mL
- Correction factor ( $cf$ ) = 15

### Optimized Parameters:

- Dissolution rate constant ( $k_d$ ) = 22.16 L<sup>n-1</sup>/(mol<sup>n-1</sup>min)
- Crystallization rate constant ( $k_c$ ) = 9.115 L<sup>n-1</sup>/(mol<sup>n-1</sup>min)
- Order parameter ( $n$ ) = 2.034
- Order parameter ( $g$ ) = 1.194
- Saturation limit ( $c_{sat}$ ) = 1.010 (mol/L)
- Correction factor ( $cf$ ) = 14.27
- Sum of Square (SSQ) = 0.5221



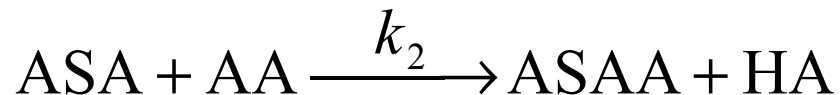
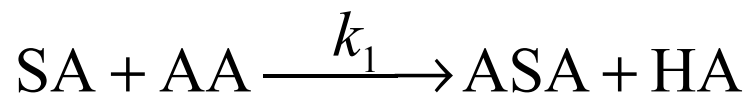
## Experiment 2

- Reaction of Salicylic Acid to form Acetylsalicylic Acid (Aspirin)
  - Simple, well understood reaction to test modeling ability
- Process includes:
  - Dissolution
  - 4 Primary Reactions
  - Crystallization

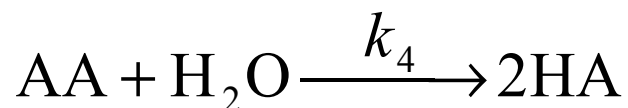
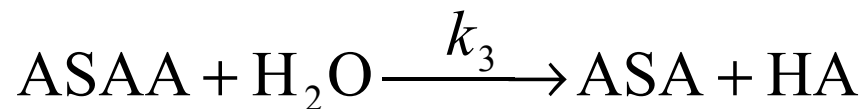


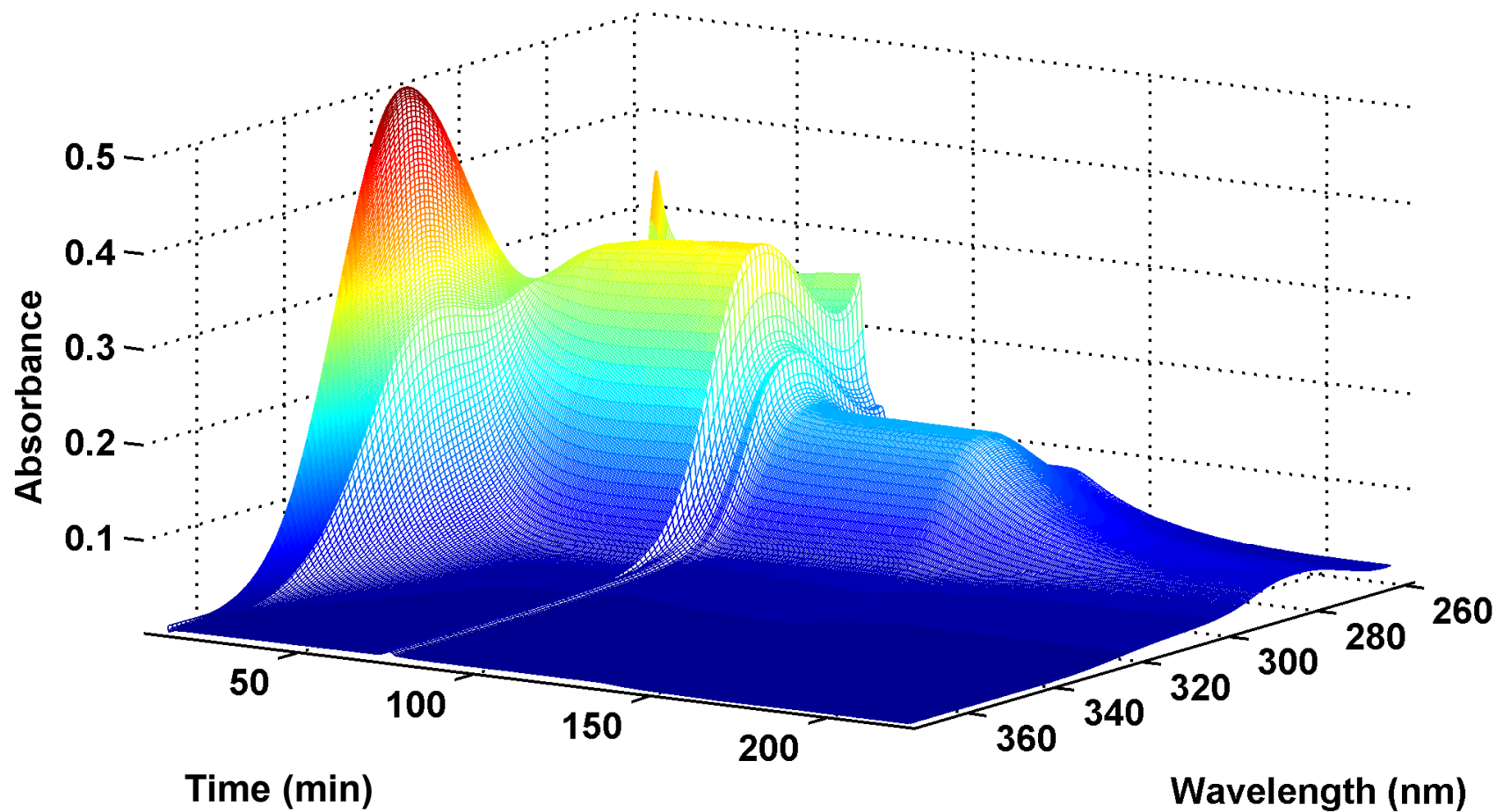
# Reaction Mechanisms

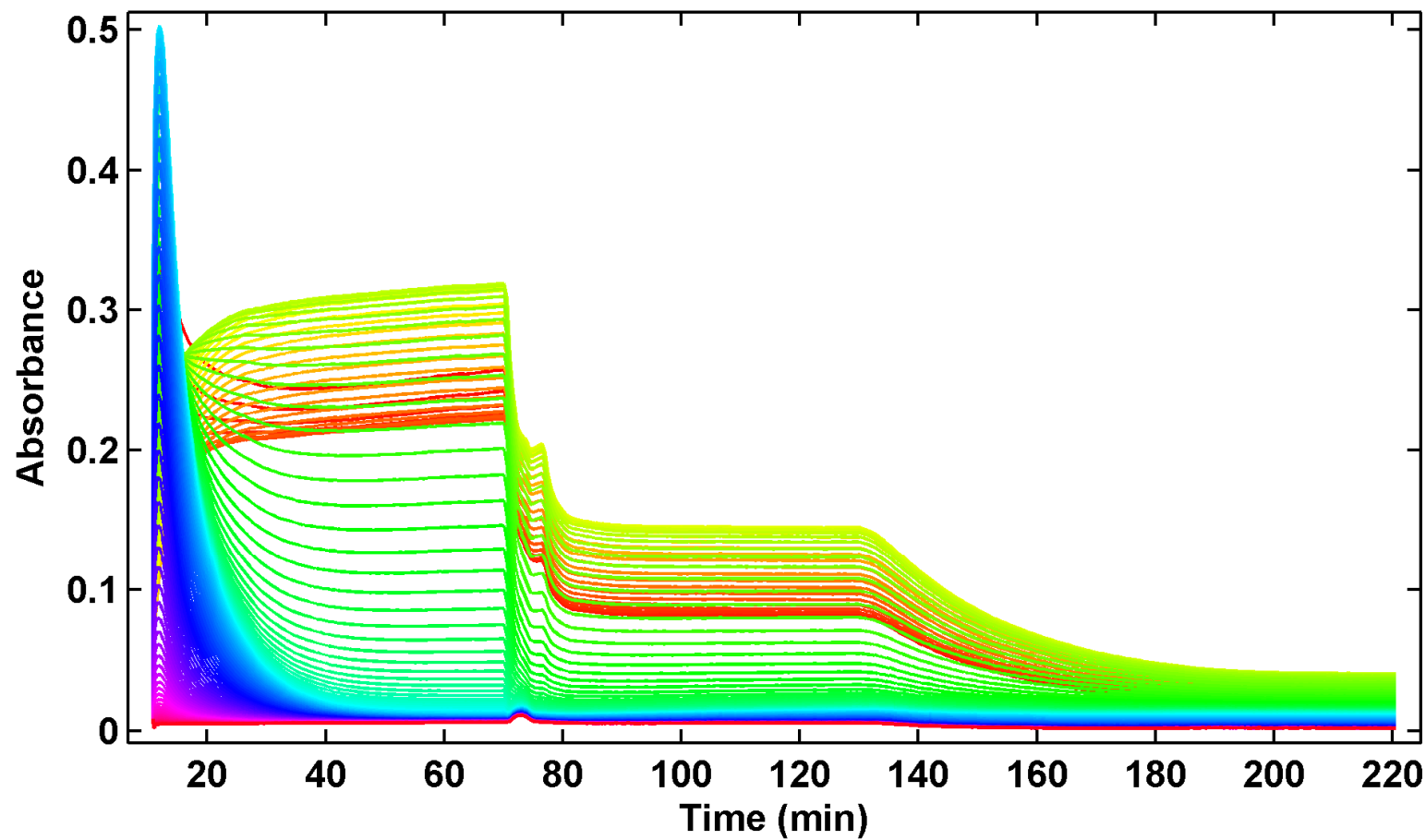
## Catalyzed Reaction



## Water Addition

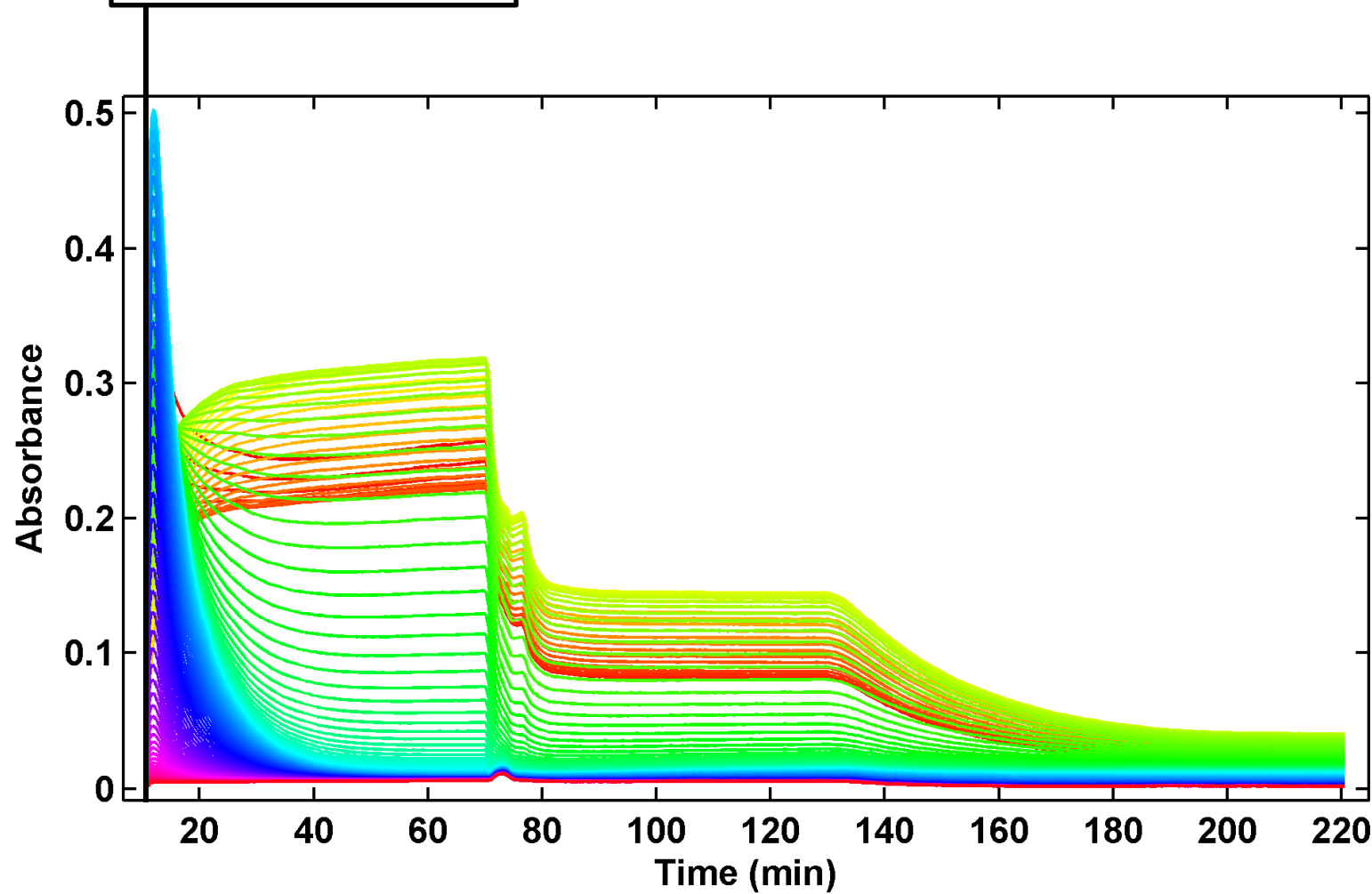








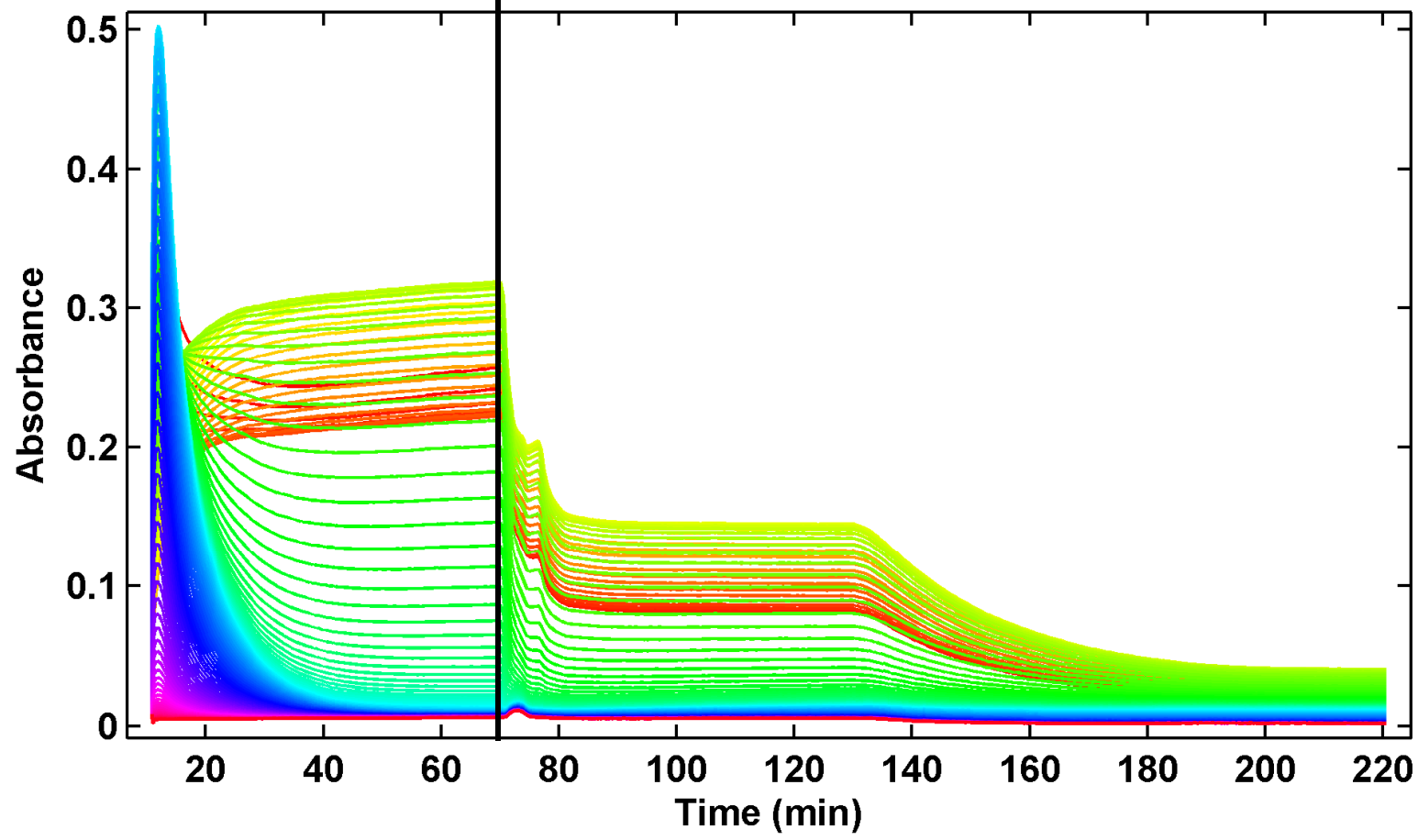
Addition of Solid SA





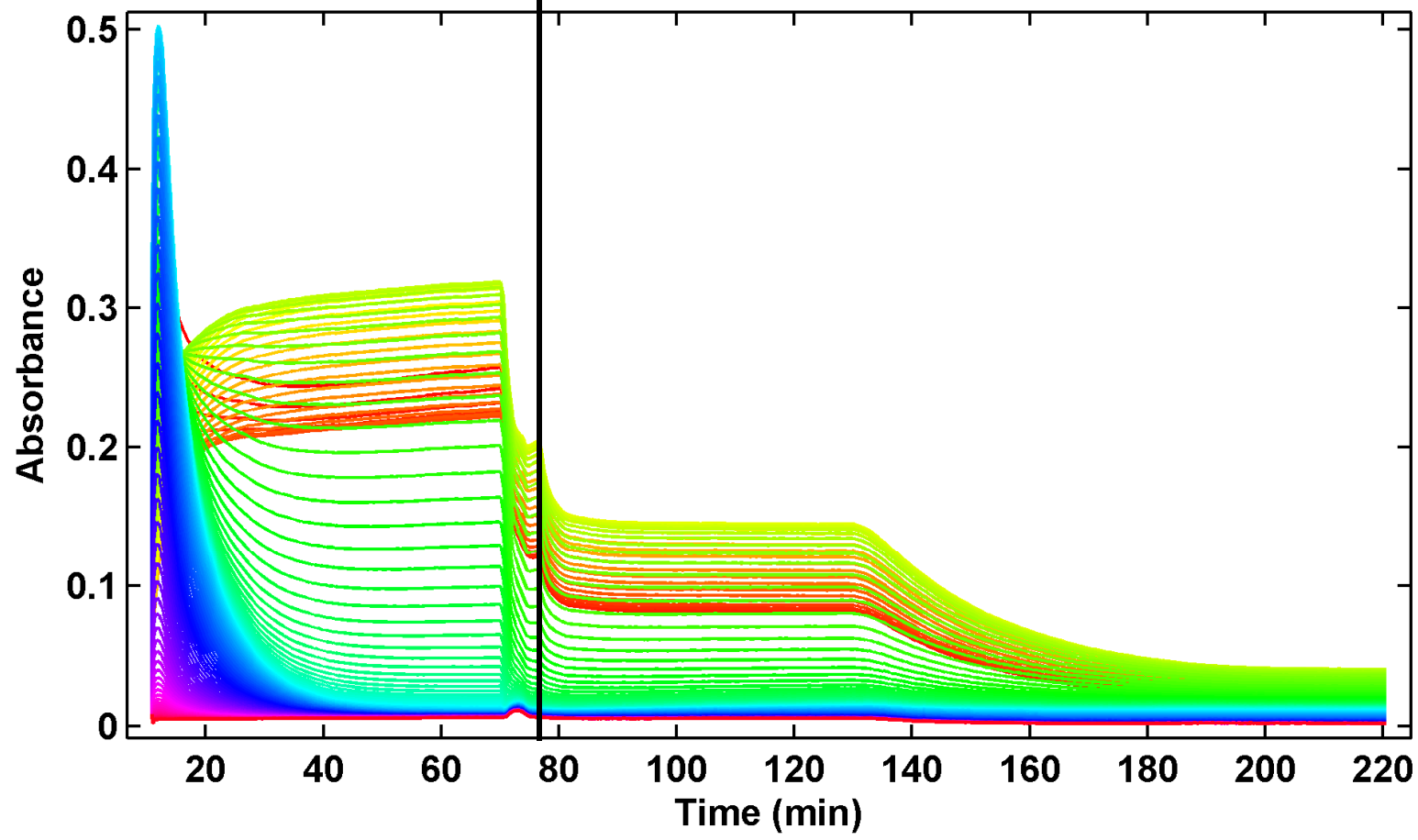


Addition of Water



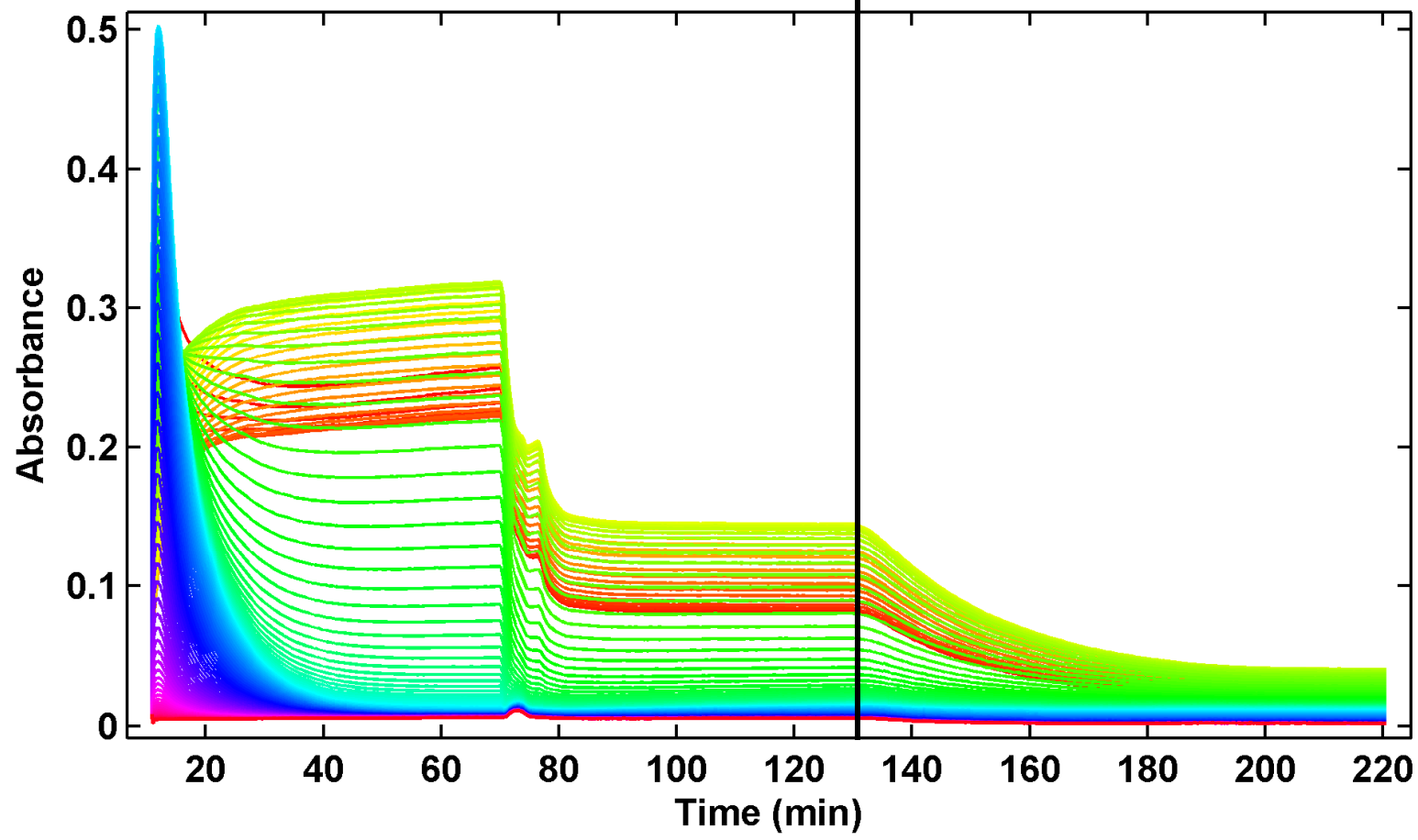


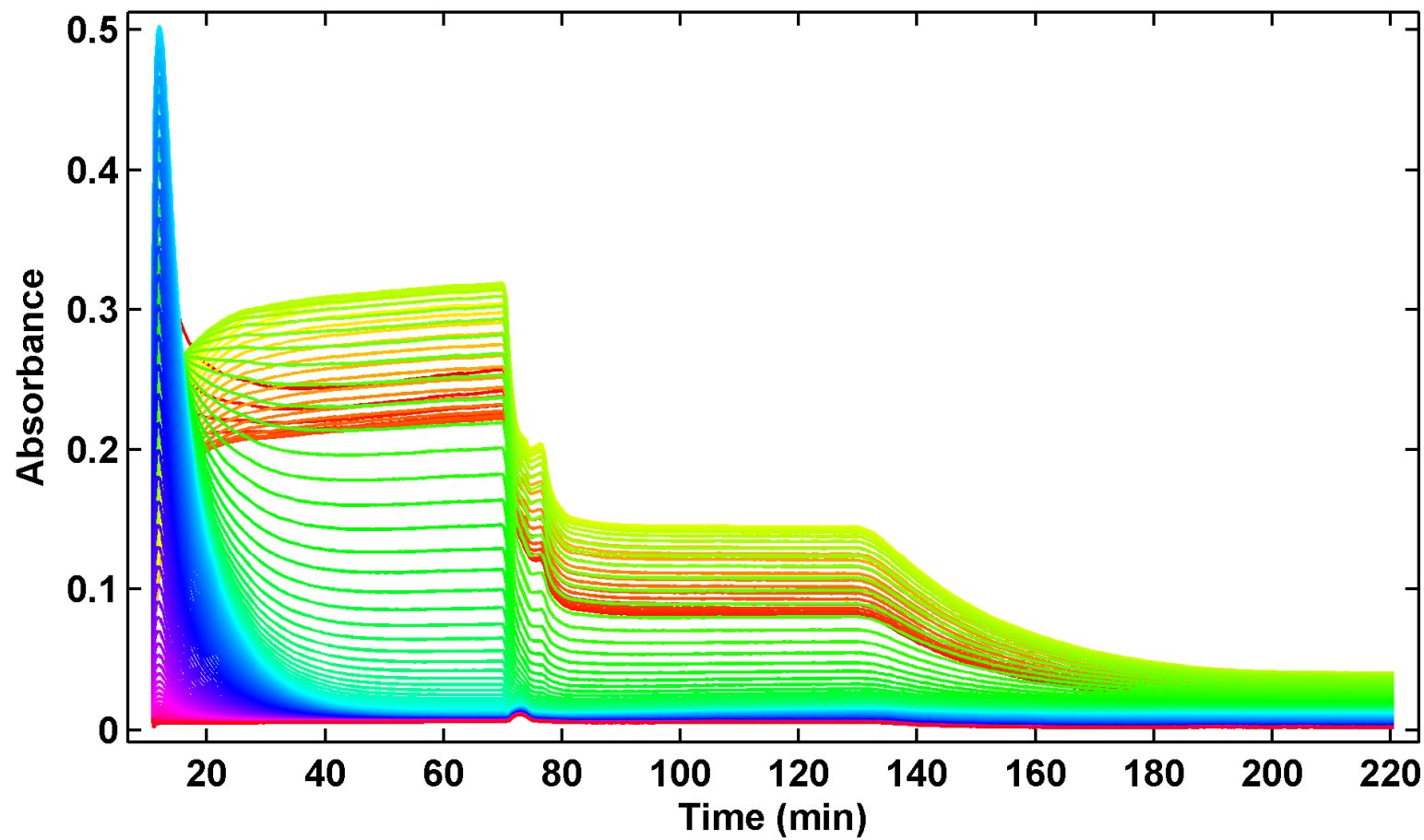
Onset of Crystallization





Begin Cooling Ramp



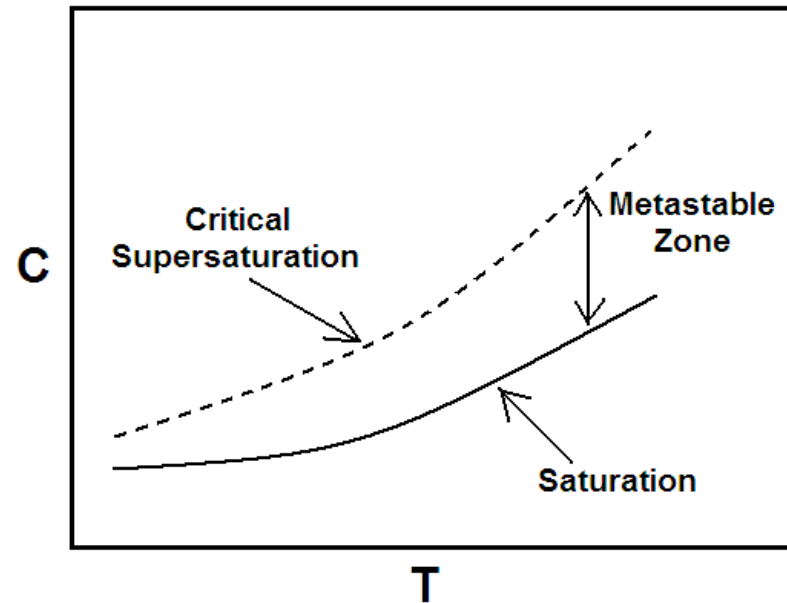




# Saturation and Supersaturation

- Considered relative to equilibrium solubility
- Super-saturation
  - “Driving force” of nucleation and crystal growth
  - Metastable
  - Generated by
    - Cooling
    - Anti-solvent addition
    - Solvent evaporation

## Metastability of Supersaturation





# Differential Equations

$$\frac{d[\text{SA}]_{\text{solid}}}{dt} = -r_d$$

$$\frac{d[\text{ASAA}]}{dt} = r_2 - \frac{dV}{dt} \frac{[\text{ASAA}]}{V}$$

$$\frac{d[\text{SA}]}{dt} = r_d - r_1 - \frac{dV}{dt} \frac{[\text{SA}]}{V}$$

$$\frac{d[\text{ASA}]}{dt} = r_1 - r_2 + r_3 - r_c - \frac{dV}{dt} \frac{[\text{ASA}]}{V}$$

$$\frac{d[\text{AA}]}{dt} = -r_1 - r_2 - r_4 - \frac{dV}{dt} \frac{[\text{AA}]}{V}$$

$$\frac{d[\text{H}_2\text{O}]}{dt} = -r_3 - r_4 + f \frac{[\text{H}_2\text{O}]_{\text{in}}}{V} - \frac{dV}{dt} \frac{[\text{H}_2\text{O}]}{V}$$

$$\frac{d[\text{HA}]}{dt} = r_1 + r_2 + r_3 + r_4 - \frac{dV}{dt} \frac{[\text{HA}]}{V}$$

$$\frac{d[\text{ASA}]_{\text{solid}}}{dt} = r_c$$



# Differential Equations

$$\frac{d[\text{SA}]_{\text{solid}}}{dt} = -r_d$$

$$\frac{d[\text{ASAA}]}{dt} = r_2 - \frac{dV}{dt} \frac{[\text{ASAA}]}{V}$$

$$\frac{d[\text{SA}]}{dt} = r_d - r_1 - \frac{dV}{dt} \frac{[\text{SA}]}{V}$$

$$\frac{d[\text{ASA}]}{dt} = r_1 - r_2 + r_3 - r_c - \frac{dV}{dt} \frac{[\text{ASA}]}{V}$$

$$\frac{d[\text{AA}]}{dt} = -r_1 - r_2 - r_4 - \frac{dV}{dt} \frac{[\text{AA}]}{V}$$

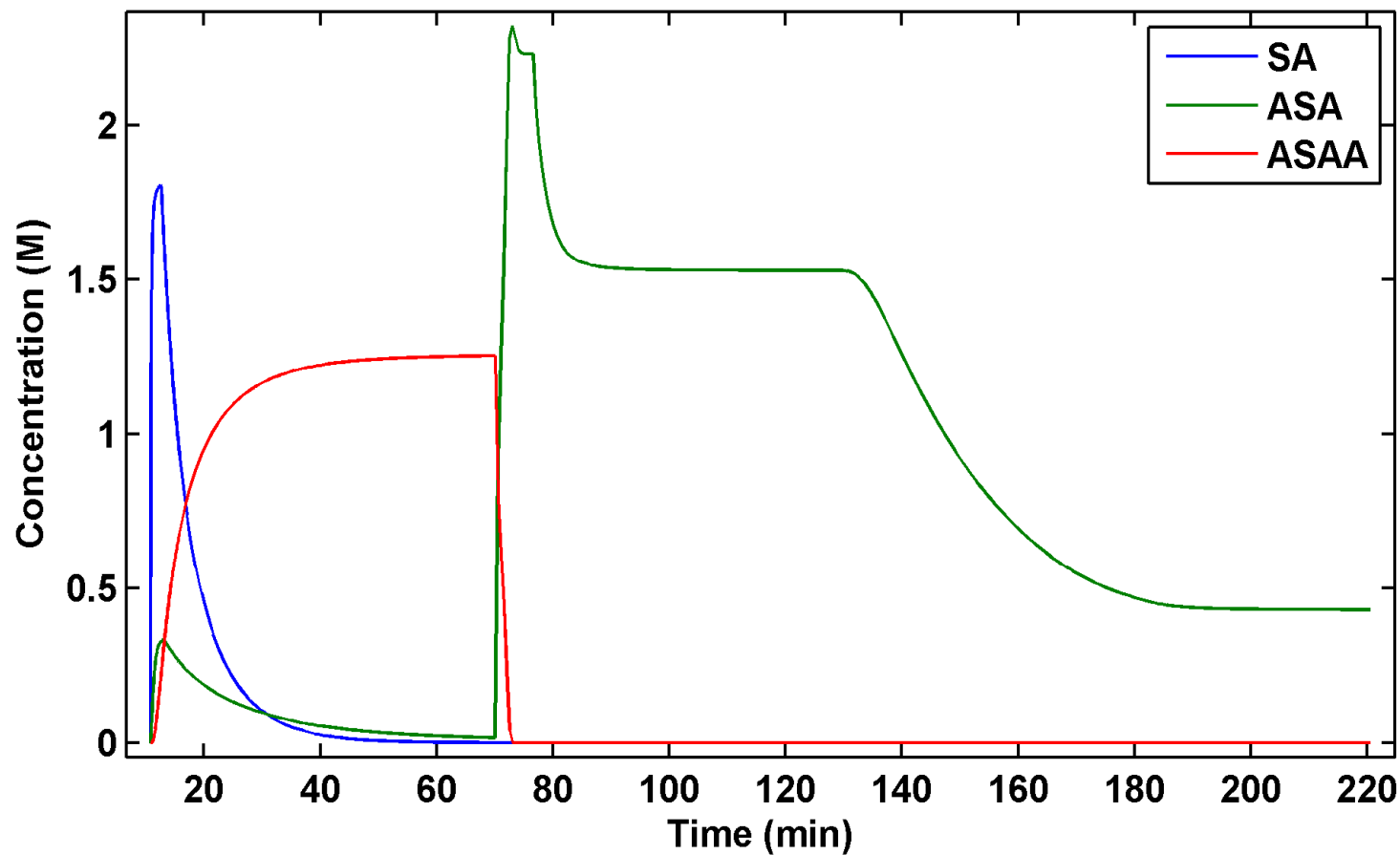
$$\frac{d[\text{H}_2\text{O}]}{dt} = -r_3 - r_4 + f \frac{[\text{H}_2\text{O}]_{\text{in}}}{V} - \frac{dV}{dt} \frac{[\text{H}_2\text{O}]}{V}$$

$$\frac{d[\text{HA}]}{dt} = r_1 + r_2 + r_3 + r_4 - \frac{dV}{dt} \frac{[\text{HA}]}{V}$$

$$\frac{d[\text{ASA}]_{\text{solid}}}{dt} = r_c$$



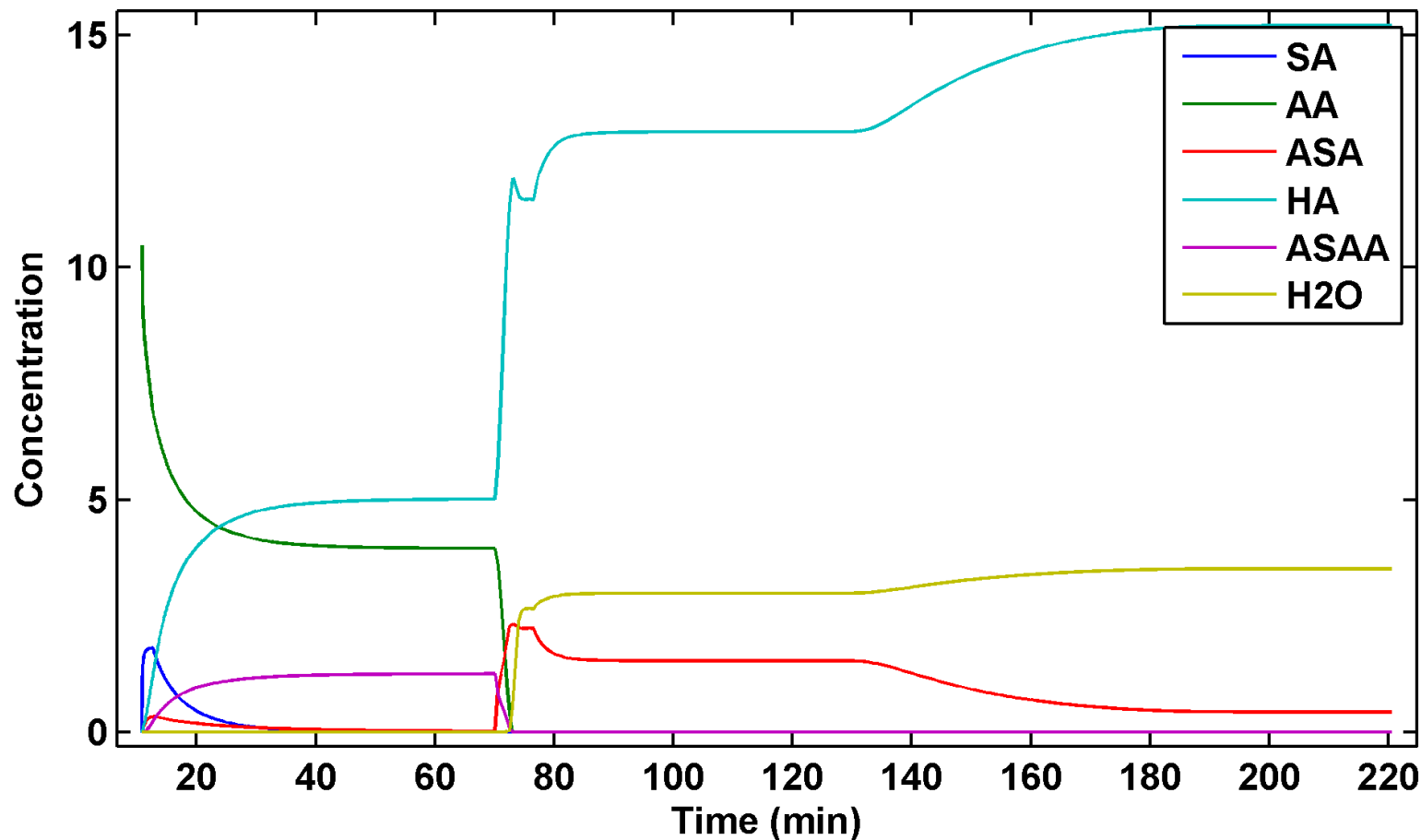
# Concentration Profile of Active Species





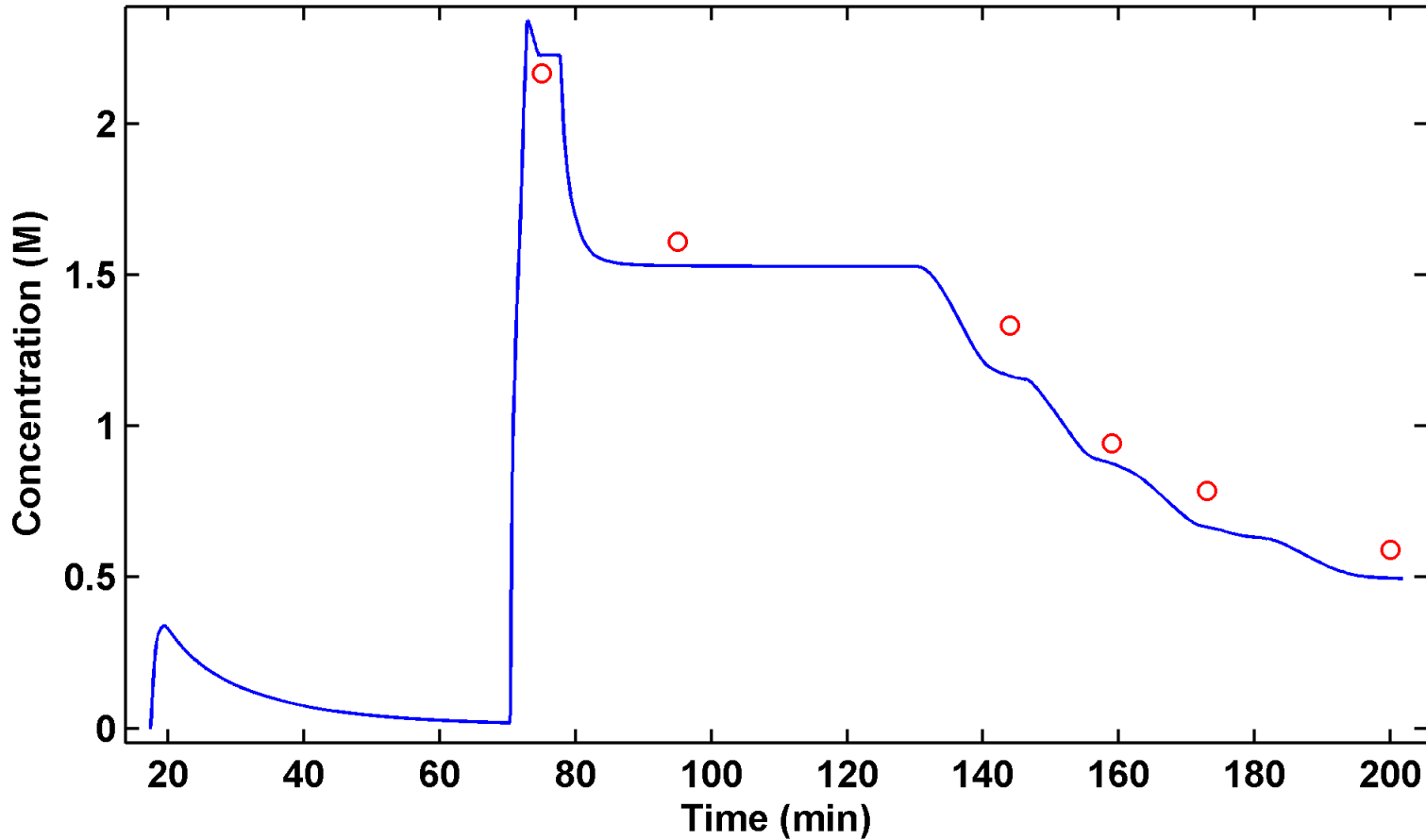


# Concentration Profiles of All Species





# Validation of ASA Concentration Profiles by HPLC – Preliminary results



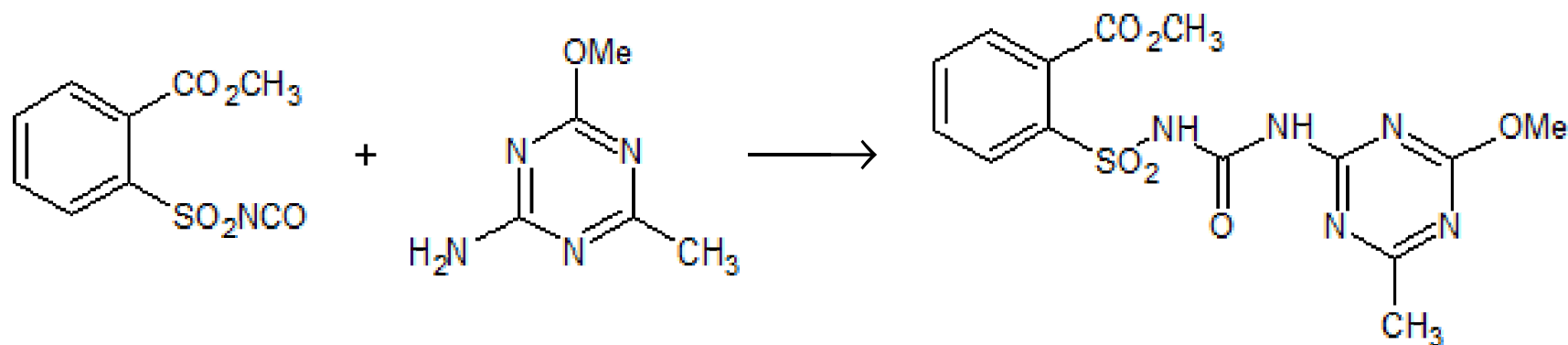


## Project 3: modeling of sulfonylurea coupling reaction

- ❑ Develop a combined kinetic model for the reaction, dissolution and crystallization for the slurry-based sulfonylurea coupling reaction.
- ❑ Use NIR diffuse reflectance spectroscopy<sup>3</sup> and kinetic model for monitoring purpose, and to perform endpoint and fault detections.
- ❑ Use High Performance Liquid Chromatography (HPLC) samples taken from the reaction mixture to validate kinetic models



# Sulfonyl Urea Coupling Reaction



CMBSI

benzoic acid 2-  
[(Isocyanato)sulfonyl]-  
methyl ester

A4098

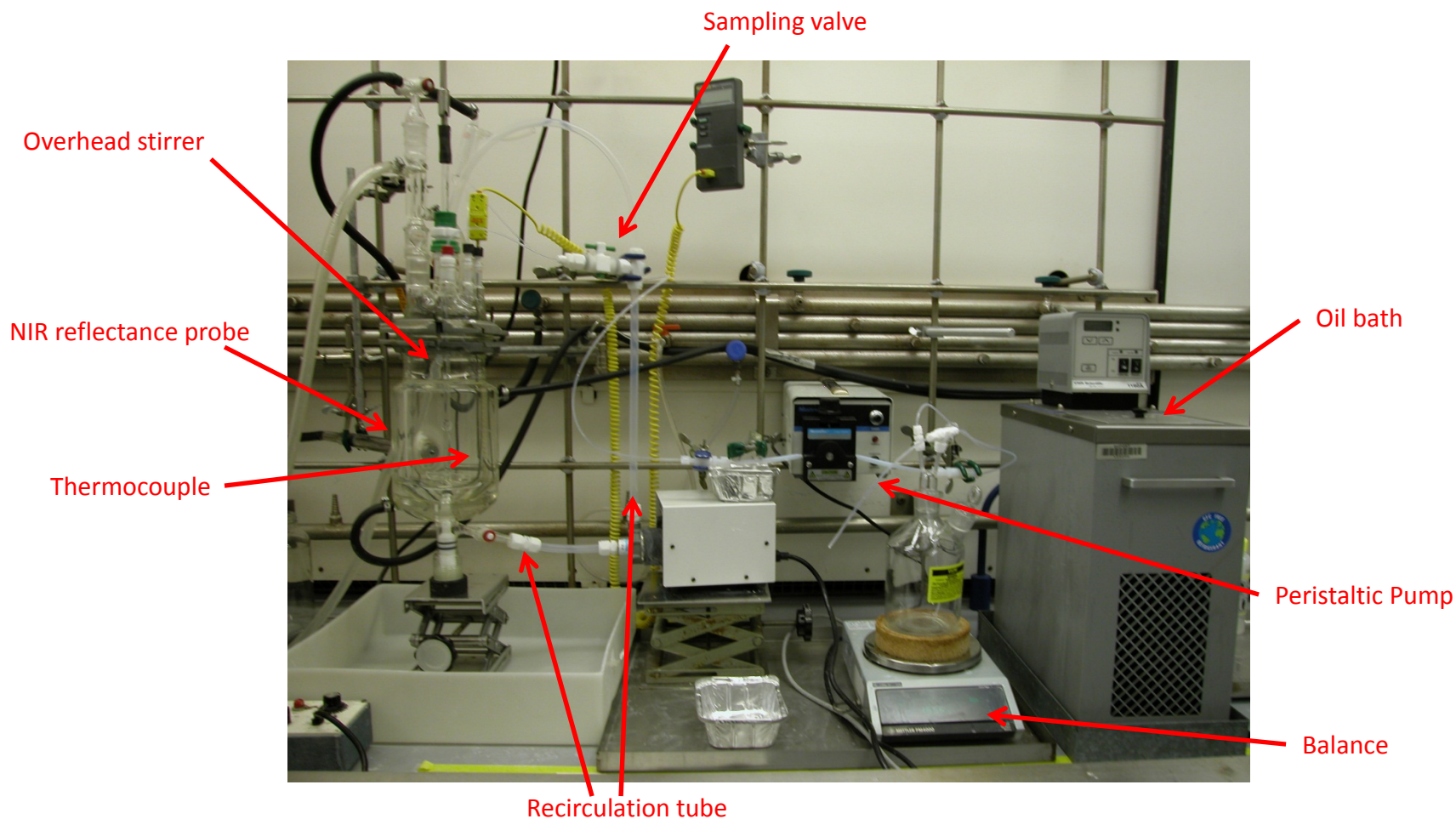
2-amino-4-methoxy-  
6-methyl-1,3,5-  
triazine

T6376

metsulfuron methyl

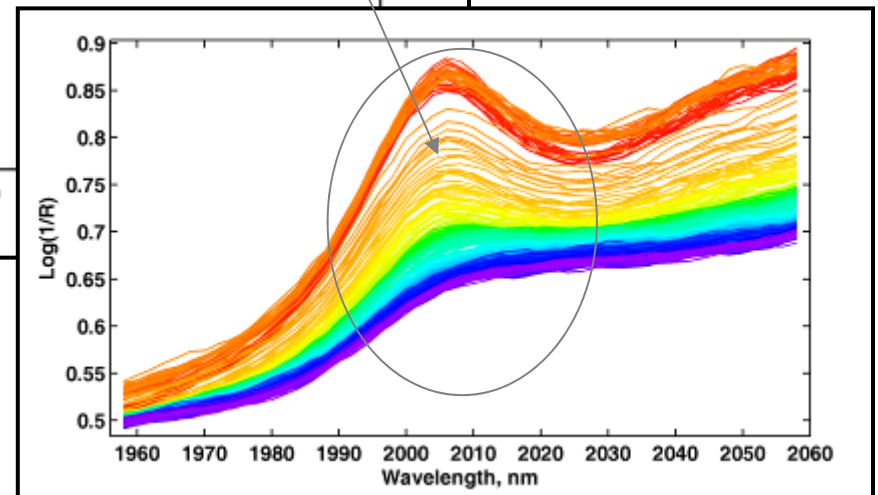
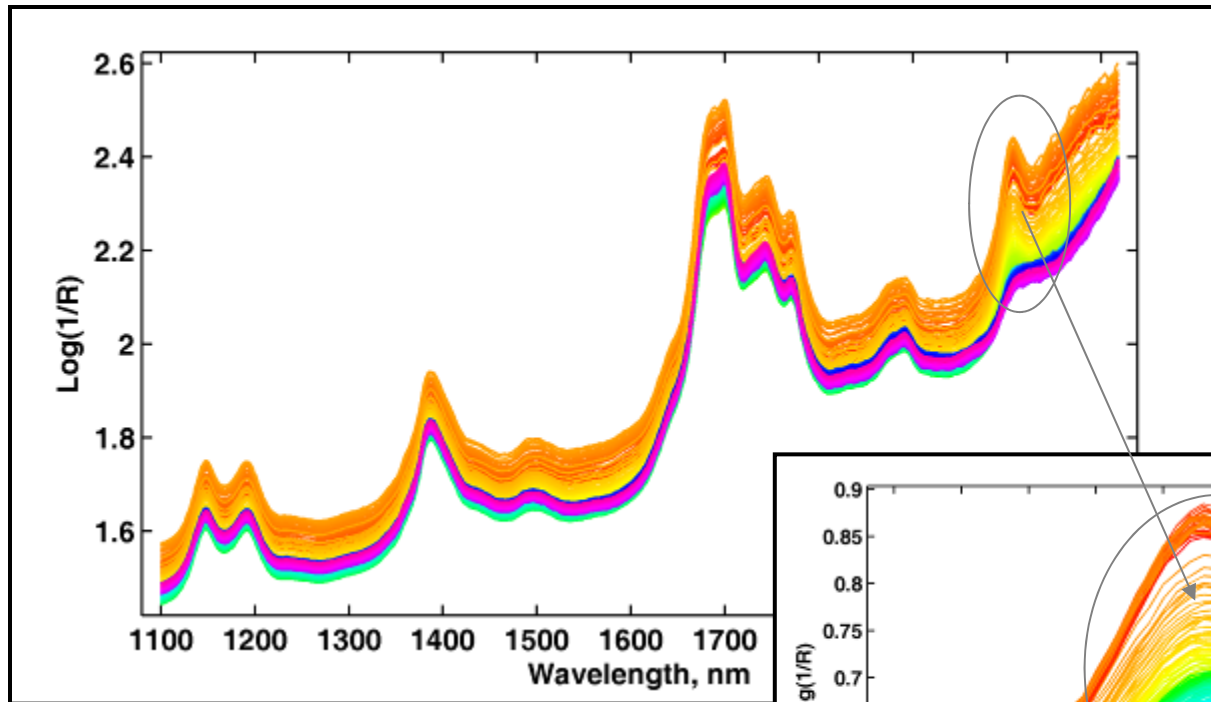


# Apparatus setup at DuPont





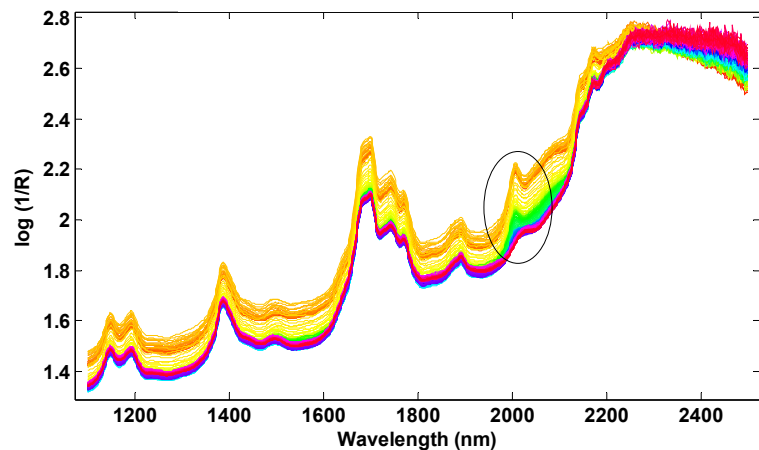
# Sample batch slurry system



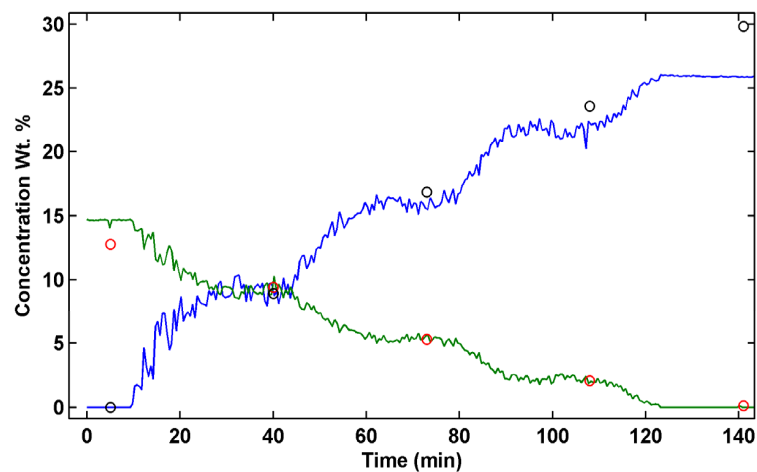
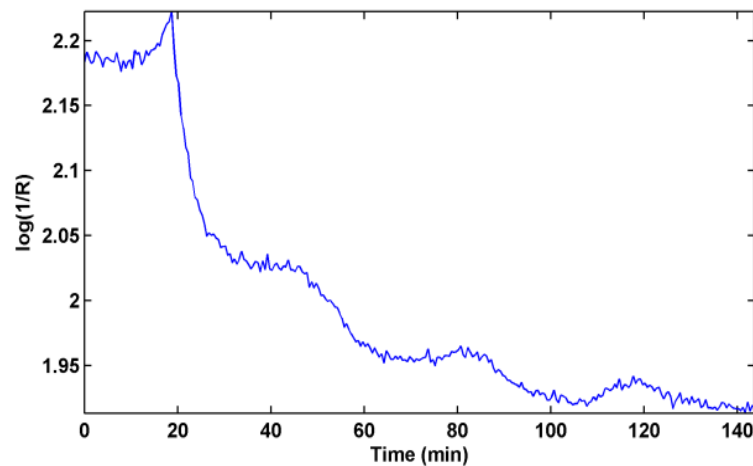
- Disappearance of NIR overtone band corresponds to consumption of starting material



# Sulfonylurea coupling reaction (NIR)



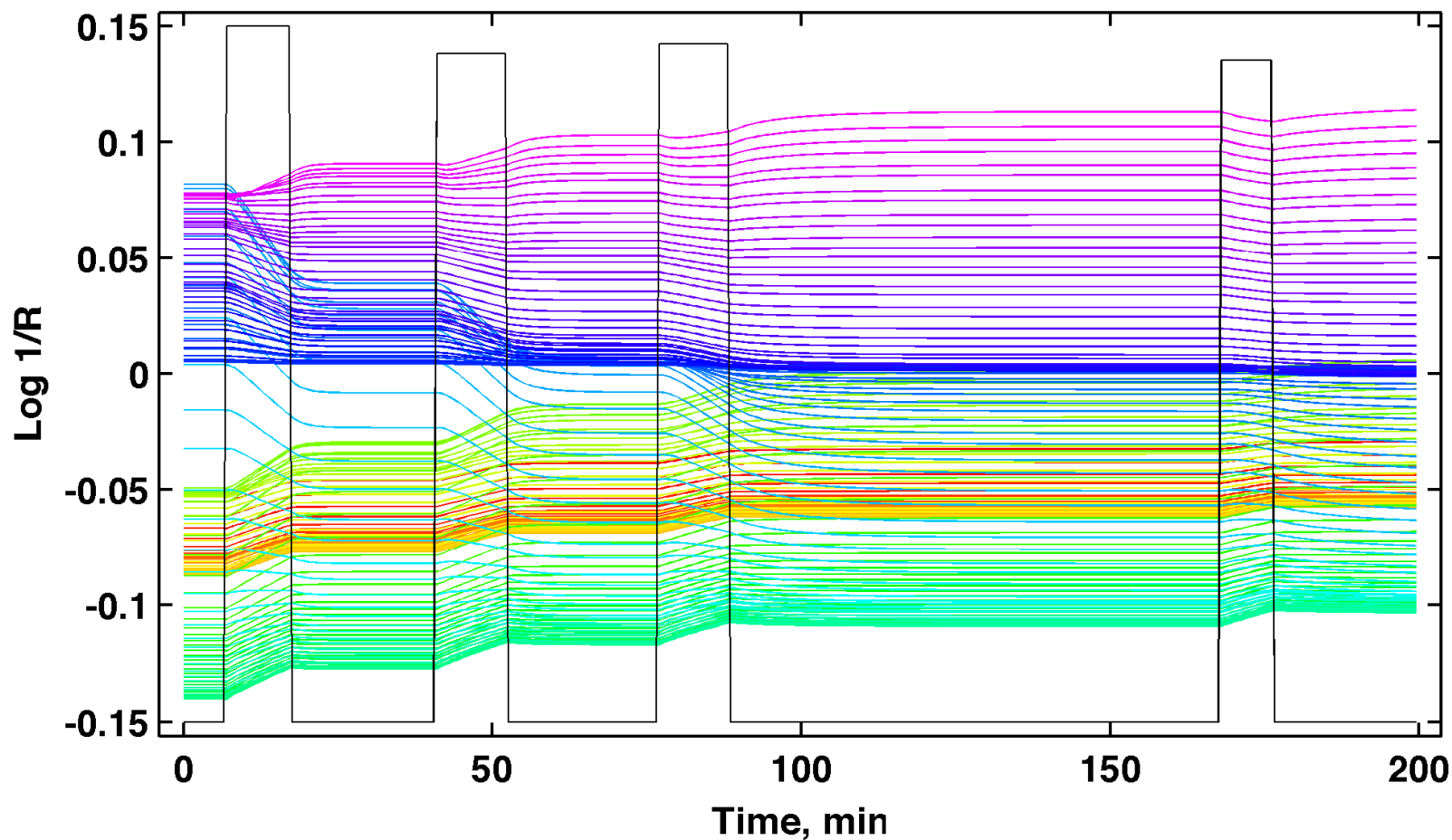
At 2010 nm





# Modeling the Coupling Reaction

blq-MSC simple kinetic model vs time, DuPont coupling reaction 7/28/2011

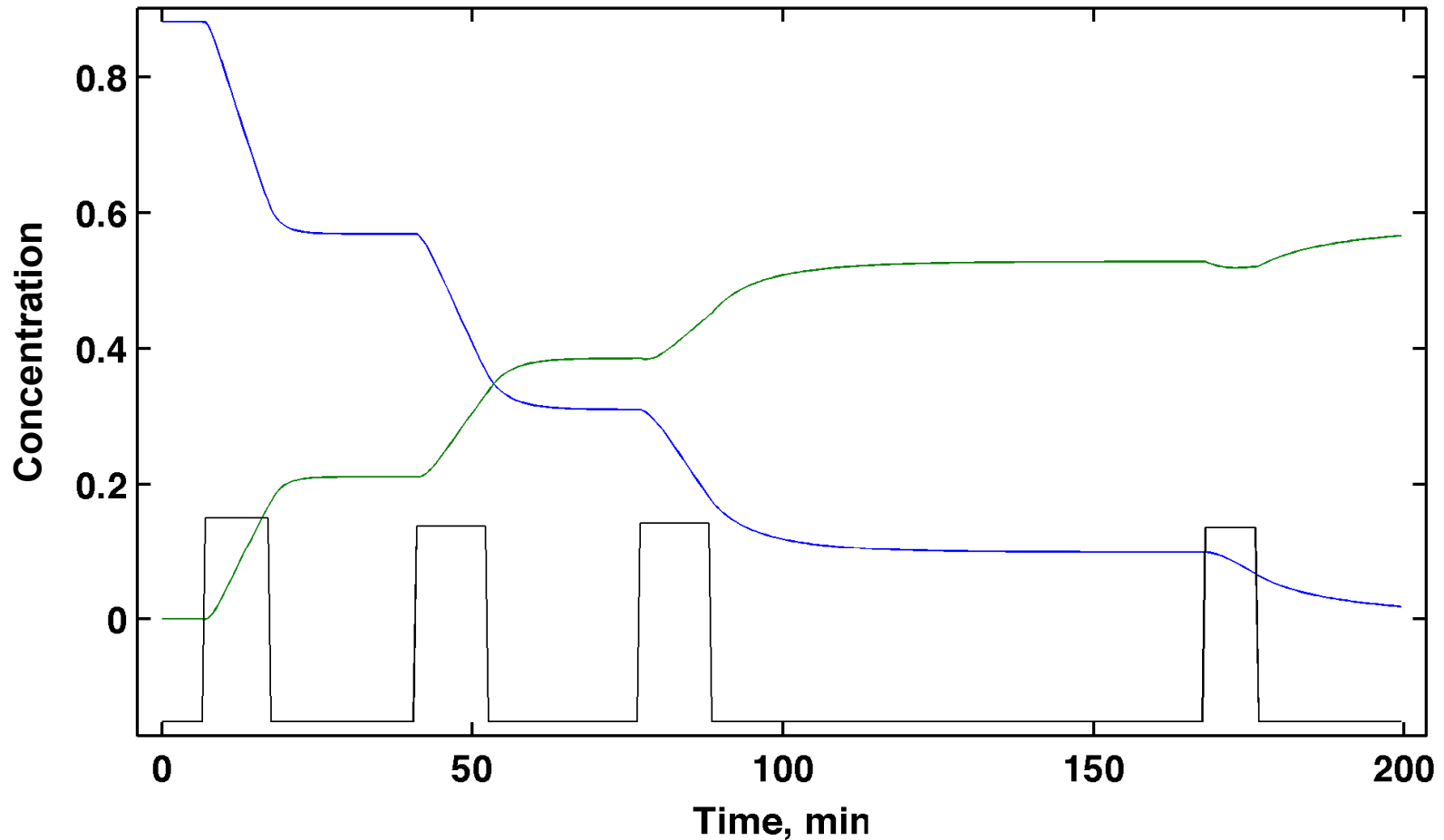






# Coupling Reaction - Kinetic Fitting Results

blq-MSC simple kinetic model vs time, DuPont coupling reaction 7/28/2011





# Acknowledgements

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