# Molecular associative memory

An associative memory framework with exponential storage capacity for DNA computing



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### **1. Introduction**

Associative memory problem : Find the closest stored vector (in Hamming distance) to a given query vector.

#### Neural implementation

- Using neural networks, connection weights are adjusted in order to perform association.
- Recall procedure is iterative and relies on simple neural operations.
- Design criteria: maximizing the number of stored patterns C while having some noise tolerance.

#### Molecular implementation

- Synthesize C DNA strands as stored vectors.
- Recall procedure is usually done in one shot via chemical reactions and relies on highly parallelism of DNA computing.

## 2. The problem

Current molecular associative memories are either
low in storage capacity, if implemented using molecular realizations of neural networks [3].
Or
very complex to implement, if all the stored sequences have to be synthesized [7], [1].

### **3. The proposed solution**

We introduce an associative memory framework with exponential storage capacity based on transcriptional networks of DNA switches proposed by [3].

#### Advantages over current methods

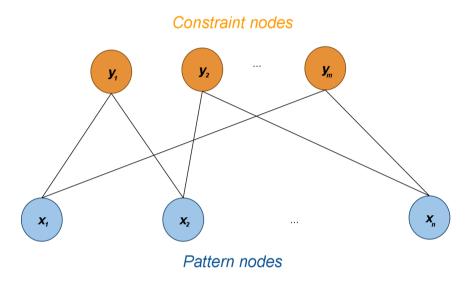
Exponential storage capacities with current neural network-based approaches can not be achieved.
For other methods, although having exponential storage capacities is possible, it is very complex as it

• Design criteria: finding proper DNA sequences to minimize probability of error during the recall phase.

requires synthesizing an extraordinarily large number of DNA strands.

#### 4. Model and method

We utilize a bipartite network of DNA switches with n pattern nodes and m constraint nodes.
The connectivity of the network is determined by the adjacency matrix H.



The state of each pattern node j, denoted by x<sub>j</sub>, can either be 1 (activation) or -1 (suppression).
The state of each constraint node i (denoted by y<sub>i</sub>) can be 1 (activation), -1 (suppression) or 0 (non-transcribed).

• Each constraint node  $y_i$  has a decision threshold  $b_i$ .

• Given the vector of decision thresholds b and pattern nodes states x, we fix H such that Hx = b.

Hence, instead of *memorizing* all possible random sequences of length n, we store only those that satisfy m constraints.

### 5. The association process

The proposed framework finds the closest stored pattern to the probe  $\hat{x}$  via forward and backward iterations.

Forward iteration

• Constraint nodes decide their state based on simple *neural* operations:

$$y_i = \begin{cases} 1, & h_i < b_i \\ 0, & h_i = b_i \\ -1, \text{ otherwise} \end{cases}$$

where  $h_i = \sum_{j=1}^n H_{ij} x_j$ , Backward iteration

• Each pattern node j computes the quantity

$$g_j = \frac{\sum_{i=1}^m H_{ij} y_i}{d_p}.$$

The sign of  $g_j$  is an indication of the sign of the noise that affects  $x_j$ , and  $|g_j|$  indicates the confidence level in the decision.

• The state of pattern DNA node j is updated using either of the following two strategies: 1. Winner-take-all strategy: only the node with the maximum  $|g_j|$  is updated.

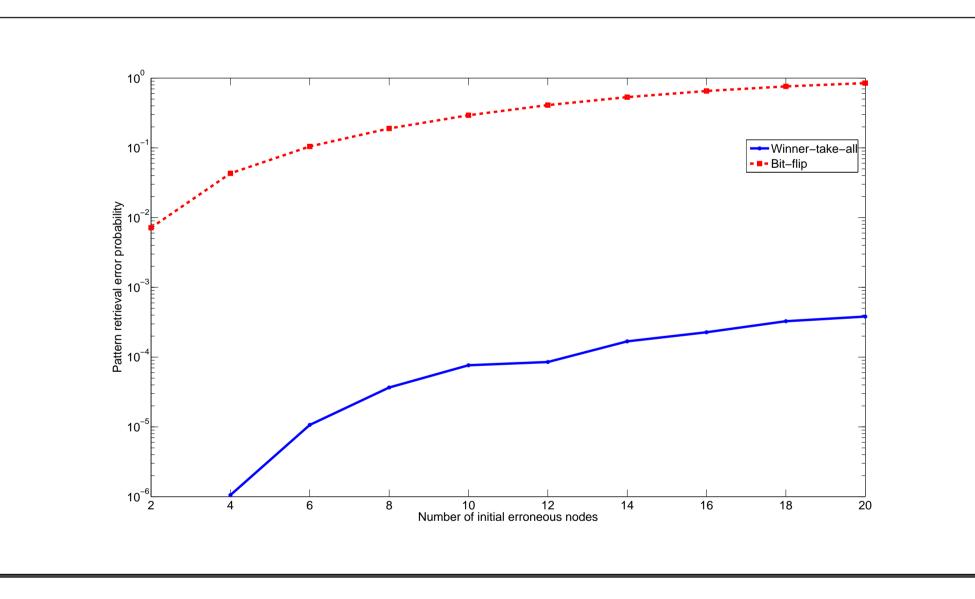
### 6. Results

Theoretical results

- The proposed framework is guaranteed to correct two erroneous nodes [4].
- For proper choice of row degrees in the constraint matrix, it also admits an exponential storage capacity in terms of *n*.

Numerical results

• The following graph illustrates the pattern retrieval error probability against the number of initial erroneous nodes.



#### 2. *Bit-flipping* strategy: all pattern nodes are updated based on the sign of $g_j$ .

<b>7. Some remarks</b> Full details about the approach can be found in [4].
<ul><li>The proposed method have other possible applications as well:</li><li>Designing artificial transcriptional networks to govern the activity of cells, for instance in combating certain diseases.</li></ul>
• Iterative error correction in DNA computing instead of pre-designed <i>error-avoiding</i> DNA sequences.

### 8. Previous works

#### Neural Associative Memory

• Extensive studies in past decades [2], [5].

• Storage capacity has been shown to be at best equal to n, the number of neurons, when required to memorize purely random patterns.

### References

- [1] J. Chen, R. Deaton, Y. Z. Wang, A DNA-based memory with in vitro learning and associative recall, Lect. Notes in Comp. Sci., Volume 2943, 2004, pp. 145-156.
- [2] J. J. Hopfield, Neural networks and physical systems with emergent collective computational abilities, Proc. Natl. Acad. Sci., Vol. 79, 1982, pp. 2554-2558.
- [3] J. Kim, J. J. Hopfield, E. Winfree, Neural network computation by in vitro transcriptional circuits, Adv. Neur. Inf. Proc. Sys. (NIPS), Vol. 17, 2004, pp. 681-688.
- Recently, some works have been done to improve the storage capacity by memorizing *structured patterns* (see [4] and references therein).

#### Molecular Associative Memory

- In contrast to neural associative memory, most approaches are already concerned with memorizing *structured patterns* to minimize recall probability of error.
- These approaches synthesize all the stored patterns and store them in a vessel [7], [1].
- Coding theory can help in designing DNA strands that admit low probability of error in the recall process [6].
- Some approaches that implement neural networks using DNA strands can be used as a means of implementing associative memory as well [3].

• However, the *storage capacity* of molecular associative memory is not well-studied yet.

- [4] K. R. Kumar, A. H. Salavati, A. Shokrollahi, *Exponential pattern retrieval capacity with non-binary* associative memory, submitted to Information Theory Workshop 2011.
- [5] R. McEliece, E. Posner, E. Rodemich, S. Venkatesh, *The capacity of the Hopfield associative memory*, IEEE Trans. Inf. Theory, Jul. 1987.
- [6] O. Milenkovic, N. Kashyap, "On the Design of Codes for DNA Computing" Lect. Notes in Comp. Sci., Vol. 3969, 2006, pp. 100-119.
- [7] J. H. Reif, T. H. LaBean, Computationally inspired biotechnologies: improved DNA synthesis and associative search using error-correcting codes and vector-quantization, Lect. Notes in Comp. Sci., Vol. 2054, 2001, pp. 145-172.

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