# Robust and Recoverable Maintenance Routing Schedules

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#### Abstract

We present a methodology to compute more efficient airline schedules that are less sensitive to delay and can be recovered at lower cost in case of severe disruptions.

We modify an original schedule by flight re-timing with the intent of improving some structural properties of the schedule. We then apply the new schedules on different disruption scenarios and then recover the disrupted schedule with the same recovery algorithm. We show that solutions with improved structural properties better absorb delays and are more efficiently recoverable than the original schedule.

We provide computational evidence using the public data provided by the ROADEF Challenge 2009<sup>1</sup>.

**Keywods:** Airline scheduling, Robust optimization, Disruption recovery

#### 1 Introduction

In the modern society, the demand for transportation, of goods and people, is constantly increasing in terms of volume and distance. In particular, as the fastest transportation mode for mid and long distances, airline transportation develops at an impressive rate. Due to the competition between the airlines, many of them use operations research techniques to schedule their operations. This allows to keep prices low and thus attract customers while making profit. Airlines have to deal with irregular events, called disruptions, making the schedule unfeasible. The process of repairing a disrupted schedule is known as the recovery problem. It aims at retrieving the initial schedule as quickly as possible while minimizing the recovery costs incurred by recovery decisions (typically delaying or canceling flights).

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<sup>1</sup>http://challenge.roadef.org/2009/index.en.htm

A major drawback of optimized schedules is that they are sensitive to perturbations. Small disruptions propagate through the whole schedule, and may have a huge impact.

The focus of this study is to implicitly consider the occurrence of future disruptions at the planing phase in order to ameliorate two properties of the schedule, namely:

- 1. the *robustness*: the ability of the schedule to remain feasible in the presence of small disruptions;
- 2. the *recoverability*: the average performance of the recovery algorithm when the schedule is disrupted.

At the planing phase, we solve the Maintenance Routing Problem (MRP), which aims at finding a feasible route for each aircraft and a departure time for each flight minimizing the loss of revenue as a metric which depends on the deviation from a desired schedule.

On the day of operation, the problem of recovering the planed schedule from a disrupted state is the Aircraft Recovery Problem (ARP) given the original schedule and the current disrupted *state*. The recovery costs for the ARP are mainly delay and cancellation costs.

The originality of the proposed algorithms is the absence of any explicit predictive model of possible disruptions for the scheduling problem. Uncertainty Features capture implicitly the uncertainty the problem is due to. An additional *budget constraint* ensures that the obtained solution is not too far from the original deterministic optimum, and the computational complexity is similar to the original deterministic problem.

We solve the MRP by applying the Uncertainty Feature Optimization (UFO) framework of Eggenberg et al. (2009) on a real case study and we present computational results for different MRPs using public instances of the ROADEF Challenge 2009. Recovery statistics are obtained with the recovery algorithm presented in Eggenberg et al. (forthcoming).

### 2 Literature Review

For a detailed description on the airline scheduling process, see Rosenberger et al. (2003a); for general surveys on airline scheduling and recovery problems, we refer to Clausen et al. (forthcoming), Kohl et al. (2007), Weide (2009) and Eggenberg et al. (forthcoming).

Airline Scheduling Barnhart et al. (1998a) introduce the *string based fleeting and routing model*, where a string is a sequence of connected flights between two maintenances. The problem is solved using a Column Generation scheme. This model is the reference for solving the MRP; it is used, for example, by Ageeva (2000), Rosenberger et al. (2004) and Lan et al. (2006).

Rosenberger et al. (2004) solve a robust fleet assignment problem where maximizing short cycles and hub isolation aims at improving the short cycle cancellation recovery strategy. The authors conclude that using sub-optimal solutions of the deterministic problem allow for improving a schedule's robustness.

Bian et al. (2005) study the robust airline fleet schedules for KLM, which is among the largest European airlines, showing that robustness is correlated with the number of aircrafts on ground. The presented results on eleven schedules of KLM in the year 2002 show a significant correlation between the plane on ground metric and the arrival and departure punctuality predictions.

Lan et al. (2006) propose two flight retiming models for solving the MRP. The former aims at reducing the delay propagation and the latter at reducing the missed passenger connections. In the reported results, the robust schedules allow for a reduction of about 40% of disrupted passengers and the total passenger delay is reduced by 20%.

Shebalov and Klabjan (2006) modify original crew schedules in order to maximize the *move-up crews*, i.e. pairings that can be swapped in operations. The main conclusion is that the trade-off between crew cost and the robustness factor is crucial: too large an investment in terms of additional crew costs to impose robustness leads to increased operational costs.

Yen and Birge (2006) describe a stochastic integer programming algorithm to solve the crew scheduling problem. Interestingly, the obtained solutions exhibit a simple but constant property: the crew tend to stay on the same plane as much as possible. The solutions show an increased average connection time between two successive flights.

**Airline Recovery** The literature on recovery algorithms developed mainly in the last 15 years, motivated by the growth of air traffic.

Argüello et al. (1997) and Bard et al. (2001) use a time-band model to solve the ARP. An extension of this mode is presented by Thengvall et al. (2000). They penalize the deviation from the original schedule and they allow human planners to specify preferences related to the recovery operations.

Eggenberg et al. (forthcoming) introduce the *constraint specific net-work* model for solving the general unit recovery problem, where a unit is either an aircraft, a crew member (or team) or a passenger; each unit is associated with a network encoding all feasible routes for the unit.

The literature shows that deterministic models do not lead to operationally efficient solutions. But non-deterministic models have a larger computational complexity. Remarkably, many authors conclude that more robust or recoverable solutions exhibit some improved structural properties of the solutions related to the number of aircraft on ground, the number of potential swaps (both for crew and aircraft) in the recovery phase or an increased idle time.

This motivates the use of the UFO framework of Eggenberg et al. (2009), which considers uncertainty implicitly through such features. This allows to keep the computational complexity similar to the deterministic problem.

### 3 Models and Algorithms

The global structure of both MRP and ARP algorithms is a Column Generation scheme based on the constraint-specific networks presented in Eggenberg et al. (forthcoming). As the two problems are similar, we use the same notation for both of them. Note that despite the structural similarities of the models, the MRP and ARP have different objectives, which is modeled by an appropriate cost structure. Additionally, the unit-specific constraints are modeled by a set of resources, as described in Eggenberg et al. (forthcoming).

We denote F the set of flights to be covered and P the set of available planes. S denotes the set of final states. Each of them corresponds to the expected location at the end of the scheduling/recovery period, and is characterized by an aircraft type, a location, a latest arrival time and maximal allowed resource consumption. T is the length of considered the period, which corresponds to the scheduling period for the MRP and the recovery period for the ARP. A route r is defined by the covered flights in the route, the final state and the plane. Let  $\Omega$  be the set of all feasible routes r,  $x_r$  the binary variable being 1 if route r is chosen in the solution and 0 otherwise, and  $c_r$  the cost of route r. Variables  $y_f$  capture flight cancellation and are 1 if flight f is canceled, incurring cost  $c_f$ , and 0 otherwise; note that for the MRP, flight cancellation is not allowed and  $c_f = \infty$ .

We define the time-space intervals  $\ell=(\mathfrak{a},\mathfrak{t})$  to account for airport capacities.  $\mathfrak{t}$  is the index of a discretized time period (starting from

index 0) of length  $\Delta$  (typically  $\Delta = 60$  minutes),  $a \in A$  is the airport. We denote L the set of all such intervals, of cardinality  $|A| \times \left[\frac{T}{A}\right]$ . For each interval  $\ell \in L$ , the maximum number of departures is denoted by  $q_{\ell}^{\text{Dep}}$  and the maximum number of arrivals by  $q_{\ell}^{\text{Arr}}$ .

We also introduce the following set of binary coefficients:  $\mathfrak{b}_{\mathfrak{r}}^{\mathfrak{f}},$  1 if route r covers flight  $f \in F$ , 0 otherwise;  $b_r^s$ , 1 if route r reaches the final state  $s \in S$ , 0 otherwise;  $b_r^p$ ,1 if route r is assigned to plane  $p \in P$ , 0 otherwise;  $b_r^{\text{Dep},\ell}$ , 1 if there is a flight in route r departing within time-space interval  $\ell \in L$ , 0 otherwise;  $b_r^{Arr,\ell}$ , 1 if there is a flight in route r arriving within time-space interval  $\ell \in L$ , 0 otherwise.

With this notation, the Master Problem (MP) of both the MRP and the ARP is the following integer linear program:

$$\min z_{MP} = \sum_{r \in \Omega} c_r x_r + \sum_{f \in F} c_f y_f \tag{1}$$

$$\sum_{r \in O} b_r^f x_r + y_f = 1 \qquad \forall f \in F \qquad (2)$$

$$\sum_{r \in \Omega} b_r^f x_r + y_f = 1 \qquad \forall f \in F \qquad (2)$$

$$\sum_{r \in \Omega} b_r^s x_r = 1 \qquad \forall s \in S \qquad (3)$$

$$\sum_{r \in \Omega} b_r^p x_r \le 1 \qquad \forall p \in P \qquad (4)$$

$$\sum_{r \in \Omega} b_r^{\text{Dep},\ell} x_r \le q_\ell^{\text{Dep}} \qquad \forall \ell \in L$$
 (5)

$$\sum_{r \in \Omega} b_r^{Arr, \ell} x_r \le q_\ell^{Arr} \qquad \forall \ell \in L$$
 (6)

$$x_r \in \{0, 1\} \qquad \forall r \in \Omega \tag{7}$$

$$y_f \in \{0, 1\} \qquad \forall f \in F \qquad (8)$$

Objective (1) minimizes total costs. Constraints (2) ensure that each flight is covered by exactly one route  $r \in \Omega$ . Constraints (3) ensure that each final state is reached by a plane and constraints (4) ensure each aircraft is assigned to at most one route. Finally, constraints (5) and (6) ensure the departure and arrival capacities of the airports are satisfied, and constraints (7) ensure integrality of the variables.

The Column Generation process combines solving the linear relaxation of (MP) and branching to find an integer solution. The pricing problem aims at finding new feasible columns improving the current (partial) solution of the linear relaxation. It is solved as a Resource-Constrained Elementary Shortest Path Problem (RCESPP) on the constraint-specific networks. We use the dynamic programming algorithm described by Righini and Salani (2006), which is a bidirectional label setting algorithm. The algorithm creates labels, corresponding to partial paths, at each node of the constraint-specific network; dominated labels, that are proved to lead to sub-optimal paths, are discarded.

The main difference between the MRP and the ARP algorithms is the specification of the constraint specific networks and its cost structure. For the MRP, all flights are potentially feasible for an aircraft, unless the aircraft is technically not able to cover them. However, using a different aircraft than desired for a given flight may incur a loss of revenue. Such costs, in addition to retiming costs, are captured independently for each aircraft in its associated constraint-specific network and determine the costs of a route. In the ARP, the cost of a route is the sum of delay costs; the feasible flights and feasible final states are usually restricted those originally assigned to aircrafts of the same fleet type.

### 3.1 Uncertainty Feature Optimization

The problem (1)-(8) is a deterministic model. As discussed in Eggenberg et al. (2009), using deterministic models for problems due to imperfect information leads to unstable solutions, i.e. sensitive to data variations. The MRP is clearly prone to noisy data; the nature of the noise is, however, difficult to capture due to the many factors influencing an airline's schedule: meteorological changes, economical factors such as the price of fuel, human factors such as crew illness, crew strikes, political manifestations, etc. Deriving an explicit model of the uncertainty through the characterization of an uncertainty set, is thus a difficult problem itself. As the MRP is already an NP-hard problem in its deterministic form, it is extremely hard to solve general MRP problems accounting for an uncertainty set. Finally, as shown in Eggenberg et al. (2009), solutions computed with a model involving an explicit uncertainty set are sensitive to errors in the uncertainty characterization.

An Uncertainty Feature (UF) is a structural property of a solution that is known to perform well for a general type of noise: for example, an increased idle time is known to allow for more delay absorption; increasing idle time thus improves the robustness of a solution against delays of any form; additionally, no specification of the delays is required.

When selecting UFs, we both have to consider their potential in

terms of robustness and recoverability and in terms of the implications on the algorithm. In order to preserve the column generation structure, the UFs must be formulated linearly.

#### 3.2 UFO reformulation of the MRP

The initial objective of the MRP is to find a feasible solution for the plane routing as close as possible to the input schedule; the cost  $c_r$  of route  $r \in \Omega$  is the total number of minutes the flights of route r deviate from their desired departure times, which has to be minimized.

In the framework described by Eggenberg et al. (2009), the initial objective  $\sum_{r\in\Omega}c_rx_r$  is relaxed as the following budget constraint:

$$\sum_{r\in\Omega}c_rx_r\leq (1+\rho)z_{\mathrm{MRP}}^*,$$

where  $\rho$  is the *budget ratio*. However, the optimal solution for the MRP is  $z_{\mathrm{MRP}}^* = 0$ , i.e. all flights are scheduled as desired and the relative budget constraint does not allow for any change in the schedule.

We therefore use an absolute budget, with a constant C. We get the following formulation:

$$\max z_{\mathsf{UFO}} = \mu(\mathbf{x}) \tag{9}$$

$$\sum_{r \in \Omega} c_r x_r \le C \tag{10}$$

$$(2) - (8)$$
 (11)

The budget C is an upper bound on the total deviation (in time units) between original and new schedule.

Note that the additional budget constraint (10) changes the definition of the reduced cost of a column: the cost  $c_r$  is multiplied by the dual multiplier of the budget constraint in the reduced cost formulation. The structure of the pricing problem highly depends on the chosen UF  $\mu(\mathbf{x})$ , which we present, along with the implications for the pricing problem, in the next section.

# 4 Uncertainty Features for the Maintenance Routing Problem

The UFs are designed based on what practitioners do in reality: increasing idle time, which allows for delay absorption, increasing the number of plane crossings, which allows for more plane swaps in the ARP and increasing the connecting passenger's connection time. We postulate that solutions with higher values for these properties are featuring more robustness and recoverability.

#### 4.1 The IT and MIT models

The idle time of a single route is

$$\mu_{\text{IT}}(\mathbf{x}) = \sum_{r \in \Omega} \delta_r x_r,$$

where  $\delta_r$  is the total idle time on route r

Using  $\mu_{IT}$  leads to a linear UFO formulation, and the structure of the pricing problem is not changed: it remains an RCESPP where the total idle time corresponds to the cost  $\delta_r$  of the column.

 $\mu_{IT}$  accounts for the total idle time. An alternative is to maximize the *minimal* idle time in order to get smaller but more uniformly distributed buffer time windows, i.e. use

$$\zeta = -\min_{r \in \Omega} \delta_r^{\text{min}} x_r,$$

where  $\delta_r^{min}$  is the minimal idle time in route r. This UF is however no longer linear but can be reformulated as

$$\begin{aligned} \max & -\zeta \\ \text{s.t. } & \zeta \geq \delta_r^{\text{min}} x_r \\ & (10) - (11) \end{aligned} \quad \forall r \in \Omega$$

However there is an exponential number of variables and constraints (at least  $\mid \Omega \mid$ ), which is not affordable for Column Generation.

Therefore we maximize the sum of the minimal idle times of each route with the following UF:

$$\mu_{\text{MIT}}(\mathbf{x}) = \sum_{r \in \Omega} \delta_r^{\text{min}} x_r.$$

The resulting UFO formulation is the same than for  $\mu_{IT}$ , except

we use  $\delta_r^{\min}$  instead of  $\delta_r$ . For the pricing the structure remains an RCESPP. The algorithm must however consider adapted label domination criteria. Unlike the total idle time, which is a cumulative metric during the label extension phase, the minimal idle time is decreasing in a non-homogeneous way. In order to compare labels and discard suboptimal ones, the partial reduced cost must contain a partial value of the minimal idle time that is comparable for different labels. This is the case when the minimal idle time is computed up to the end of the end of the last activity.

#### 4.2 The CROSS model

The CROSS model captures the number of plane crossings, allowing for more swapping possibilities to facilitate recovery. It is not associated to a single route and thus unmanageable in the current CG scheme.

To address this issue, we introduce the concept of *meeting points*: we create a constraint for each airport for a discretized number of time intervals. We denote such a meeting point by the pair  $\mathfrak{m}=(\mathfrak{a},\mathfrak{t}),$  corresponding to the meeting point at airport  $\mathfrak{a}$  and time interval  $\mathfrak{t};$  the number  $\Delta$  of time intervals is a fixed parameter, and M is the set of all meeting points, i.e.  $M=\{(\mathfrak{a},\mathfrak{t})\mid \mathfrak{a}\in A,\mathfrak{t}=0,\cdots,\Delta\}$ . The number |M| of meeting point constraints is pseudo-polynomial (number of airports times number of time intervals).

We denote by  $\mathfrak{b}_r^{\mathfrak{m}}$  the binary coefficient being 1 if route r visits meeting point  $\mathfrak{m} \in M$  and 0 otherwise. We then include the following set of constraints:

$$\sum_{r \in \Omega} b_r^{\mathfrak{m}} x_r - y_{\mathfrak{m}} \ge 0 \qquad \forall \mathfrak{m} \in M.$$
 (12)

The UF corresponding to the plane crossing maximization is

$$\mu_{CROSS}(\mathbf{x}) = \sum_{m \in M} (y_m - 1),$$

and we have to maximize  $\mu_{CROSS}(\mathbf{x})$  subject to the constraints (10)-(11) and with the additional crossing count constraints (12).

The reduced cost of a column now contains the term

$$-\sum_{m\in M}b_r^m\lambda_m,$$

where  $\lambda_m$ ,  $m \in M$  are the dual multipliers of constraints (12).

#### 4.3 The PCON model

IT, MIT and CROSS are all aircraft-based metrics. Another possibility is to use passenger-centric UFs based, for instance, on idle connection time for passenger itineraries with multiple flights.

Let I be the set of all existing passenger connections in the schedule; each of them is defined by a pair of flights  $(f_i, f_j) \in I$ . We define the idle connection time  $\delta_{ij}$  of  $(f_i, f_j) \in I$  as the time between the landing time of flight  $f_1$  and the departure of  $f_2$  minus the minimum passenger connection time (typically 30 minutes), denoted MPC. We assume a constant value for MPC, as assumed by most airlines and in literature (e.g. Lan et al., 2006).

PCON is the UF maximizing the passenger idle time:

$$\mu_{PCON} = \sum_{(f_i, f_j) \in I} \delta_{ij}.$$

Given a route r,  $t_r^{\mathrm{dep}}(f_j)$  is the landing time of flight  $f_j$ , which is 0 if  $f_j$  is not covered by route r and the exact departure time of  $f_j$  if route r covers it. Similarly,  $t_r^{\mathrm{land}}(f_i)$  is the landing time of flight  $f_i$  if it is covered by route r, 0 otherwise. As the covering of all flights is imposed by constraints (2), we always have one route r in the solution with non-zero values of  $t_r^{\mathrm{land}}(f_i)$  or  $t_r^{\mathrm{dep}}(f_j)$ .

In addition to constraints (10)-(11), we have to impose non-negativity of each connection time as follows:

$$\delta_{ij} - \left(\sum_{r \in \Omega} t_r^{\text{dep}}(f_j) - \sum_{r' \in \Omega} t_{r'}^{\text{land}}(f_i) - \text{MPC}\right) \le 0 \quad \forall (f_i, f_j) \in I \quad (13)$$
$$\delta_{ij} \ge 0 \quad \forall (f_i, f_j) \in I \quad (14)$$

When maximizing  $\mu_{PCON}$ , the model with constraints (10)-(11) and (13)-(14) ensures that the total passenger connection time is maximized, while satisfying the minimum passenger connection time for all connections I.

From the algorithmic point of view, the structure of the pricing problem is unchanged up to the consideration of additional prices to be collected in the RCESPP algorithm; when taking discretized times for  $t_r^{\rm land}(f_i)$  and  $t_r^{\rm dep}(f_j)$ , the collection is similar to the price collection of take-off and landing slots.

#### 4.4 Implementation

The four MRP algorithms, IT, MIT, CROSS and PCON corresponding to the presented UFs, and the recovery algorithm solving the ARP are implemented using the same Column Generation heuristic: column generation is performed only at the root node. The branching scheme is meant to derive an integer solution from the columns obtained at the root node. Furthermore, to speed up computation, we derive three heuristic pricing levels depending on the number of columns found:

- the number of labels to be extended at each node is limited and domination criteria are heuristic, i.e. labels might be erroneously discarded;
- 2. same than level 1, but we increase the number of labels extended at each node;
- 3. the number of labels to extend is unlimited.

When one heuristic level fails to find any column, we proceed to the next level. Eggenberg et al. (forthcoming) show that this leads to a fast heuristic that generates good quality solutions in terms of optimality deviation.

Moreover, when the flight retiming window is smaller than twice its duration for each flight, this procedure leads to the optimal solution of the pricing.

The algorithms are written in C++ using the COIN-OR BCP framework<sup>2</sup>, each algorithm containing around 12,000 lines of code in addition to the COIN-OR BCP framework.

### 4.5 Simulation Methodology

To validate the above models, we generate different schedules from the same original one with each model using different budget values for C. We then apply a same disruption to each schedule and then run the same recovery algorithm to recover the disrupted schedule.

As some models do not consider passenger connections, it may occur that some of them are no longer feasible after re-timing flights. In such cases, we assume that no ticket using such a connection can be sold, i.e. the passengers are lost and the tickets have to be refunded. The consequence is a loss of revenue, which is the cost of making the schedule more robust/recoverable.

In order to compare the efficiency of different schedules for a same disruption scenario, We adopt a similar approach than Lan et al.

<sup>&</sup>lt;sup>2</sup>http://www.coin-or.org

(2006): given the original schedule and a disruption characterization, we identify, for each flight, the so called *independent delay* and the *propagated delay*. The independent part of the delay is single-flight dependent and is, therefore, part of the disruption characterization. The propagated delay is a consequence of the schedule, which is a consequence of the disruption and must be recomputed.

# 5 Computational Results

For the computational results, we use public data provided for the ROADEF Challenge 2009<sup>3</sup>. We use the A instance set, i.e. the set of instances used for the Challenge qualification phase.

Each instance is composed of an original schedule and disruption scenario. The original schedule is composed of the existing legs, the routes of each aircraft (including maintenances, that cannot be rescheduled) and the passenger's itineraries. Additionally, there are airport arrival and departure capacities, which are given as upper bounds for each one-hour interval of a typical day. Disruption scenarios are characterized by an operational period prior to the start of the recovery period, for which observed flight delays and flight cancellations are reported. Additionally, mandatory rest periods for aircraft and modified airport capacities at given time slots are also provided.

The recovery algorithm computes new routes for the aircraft and the passengers in order to minimize recovery costs; only flights departing after the start of the recovery period can be rescheduled, all other flights are fixed; the same holds for passenger itineraries. External cost-checker and checker for feasibility are provided, allowing to externally evaluate the solutions according to the real cost-metric.

The qualifying instances A01-A10 are based on the same schedule with 35 airports and 85 planes.

Instances A01-A04 and A06-A09 are single-day schedules with 608 flights and between 36010 and 46619 passenger itineraries, whereas A05 and A10 are a two days schedule with 1216 flights and between 71910 and 95392 passenger itineraries; we refer to them as the 1-day and 2-days instances, respectively.

As discussed in section 4.5, a preprocessing phase is required to apply a disruption scenario to a modified schedule. First of all, for each solution, we remove from the formulation the passengers missing a connection, i.e. with less than 30 minutes connection time, due to

 $<sup>^3</sup>$ http://challenge.roadef.org/2009/index.en.htm

Model	0r	IT_1000	IT_2500	IT_5000	IT_10000	MIT_1000	MIT_2500	MIT_5000	MIT_10000
Used Budget [min]	0	1000	2500	5000	8530	1000	2500	5000	9830
# Modified Flts	0	20	52	97	182	56	105	191	304
IT [min]	12000	13000	14500	17000	18975	12610	13520	14710	16720
MIT [min]	790	940	1025	1150	1230	1645	2210	2835	3330
CROSS	3430	3454	3455	3496	3488	3440	3450	3438	3416
PCON [min]	130470	132575	135760	141090	148190	130460	132260	134555	141013
# Lost Pax	0	0	56.5	95.5	295	77	135	249.5	443.5
Pax Lost [%]	0.00	0.00	0.14	0.24	0.71	0.19	0.34	0.62	1.10
Revenue Loss [%]	0.00	0.00	0.29	0.65	2.42	0.47	0.99	1.71	3.51
CPU Time [s]	< 1	313	321	279	348	336	331	321	393

Model	MIT_20000	CROSS_1000	CROSS_2500	CROSS_5000	CROSS_10000	PCON_1000	PCON_2500	PCON_5000
Used Budget [min]	10025	1000	2500	5000	5980	1000	1250	2500
# Modified Flts	308	109	178	248	255	31.5	26.5	52.5
IT [min]	16750	11880	11415	11450	10965	12815	12960	13670
MIT [min]	3355	690	620	505	460	782.5	807.5	795
CROSS	3410	3494	3517	3530	3519	3447.5	3444	3459.5
PCON [min]	141218	129143	127318	127743	127468	134533	135888	140573
# Lost Pax	438.5	73.5	262.5	366	405.5	0	0	0
Pax Lost [%]	1.09	0.20	0.67	0.90	1.02	0.00	0.00	0.00
Revenue Loss [%]	3.56	0.71	2.35	3.37	3.65	0.00	0.00	0.00
CPU Time [s]	408	406	412	583	285	757	1058	1073

Table 1: Average a priori statistics on instances A01-A04 and A06-A09.

flight retiming. These *lost* passengers correspond to the loss of revenue sacrificed to increase the schedule's robustness and recoverability; the number of lost passengers and the corresponding loss of revenue are shown for each instance.

#### 5.1 A priori results

For the presentation of the results, we separate the 1-day instances from the 2-days ones.

The original schedules (as provided in the data set) are labeled  $\tt Or$ ; the schedules obtained by the UFO models are labeled  $\tt IT$ ,  $\tt MIT$ , CROSS and PCON. The UF solutions are followed by a number specifying  $\tt C$  in (10), corresponding to total allowed deviation of departure times in minutes. Thus, for example, instance  $\tt AO1\_CROSS\_1000$  corresponds to the solution of instance  $\tt AO1$  solved with UF CROSS and a budget  $\tt C=1000$  minutes.

For each instance, we generate one schedule for five different budgets, namely C = 1,000, 2,500, 5,000, 10,000 and 20,000 minutes respectively; the maximal deviation of a single flight is set to 60 minutes. The complete results are reported in Appendix A.

Table 1 summarizes the average a priori statistics on the 1-day instances and Table 2 for the 2-day instances. Displayed informations are used budget (in minutes), the value of the different UFs for each solution, the statistics of lost passengers (absolute, relative and corresponding relative loss of revenue with respect to the original schedule) and CPU times.

Model	Or	IT_10000	MIT_10000	CROSS_10000	PCON_1000
Used Budget [min]	0	10000	10000	8515	1000
# Modified Flts	0	252	407	424	31
IT [min]	77865	85068	80160	76925	78220
MIT [min]	490	408	1965	140	475
CROSS	6100	6176	6085	6184	6105
PCON [min]	258143	276113	268178	257348	263173
# Lost Pax	0	298	414	671	0
Pax Lost [%]	0.00	0.36	0.50	0.82	0.00
Revenue Loss [%]	0.00	1.30	1.79	2.90	0.00
CPU Time [s]	< 1	10828	5412	6291	41292

Table 2: Average a priori statistics for different models for instances A05 and A10.

First note that Table 1 does not report results for PCON\_10000 and for models IT\_20000 and CROSS\_20000. For model PCON, the algorithm is not able to find a solution different from 0r; for the other models, there is no difference between a budget C=10,000 and C=20,000. This is due to the fact that we have a disaggregate bound on retiming for each flight which is independent of C. When C is large enough, the total retiming is limited by the disaggregate bounds before reaching the aggregate bound C, which is the case for models IT\_20000 and CROSS\_20000.

Table 2 shows that the computational effort for the 2-day instances is increased up to a factor between 13 and 55 with respect to the 1-day instances. The number of aircraft, however, is unchanged, namely 85, and the number of flights is multiplied only by a factor 2. This shows the combinatorial complexity of the problem. Moreover, the UF values are much higher than for the 1-day, explaining why the relative increase of the UFs is lower.

A remarkable point is the number of lost passengers and associated loss of revenue. Indeed, all models except PCON do not consider connections at all. However, for the 1-day instances, the maximal loss of passengers is 1.31% for a single instance and 1.10% in the average. The loss of revenues are slightly higher than the number of lost passengers. The reason is that the misconnected passengers are those with tight connections, which often corresponds to the profile of business passengers, who also pay higher fares. The loss of revenue due to retiming is thus always lower than 4.3% (3.65% in average) of the original revenue, but note that this is an upper bound: indeed, we do not consider the possibility of attracting additional customers with the connections created in the new schedule.

We also see from Table 1 that the models are able to significantly increase the values of their corresponding UF. We also see that increasing the budget leads to solutions with higher values for the UFs. The increase is not necessarily homogeneous: the value of CROSS is higher for model CROSS\_5000 than CROSS\_10000, which is due to the fact we are using heuristics.

Interestingly, IT, MIT and PCON are correlated, as solutions with higher values of one of these UFs also have higher value for the others. This is however not always the case, which shows the UFs are not equivalent. Surprisingly, solutions computed with CROSS tend to decrease the value of IT, MIT and PCON but the reverse is not observed.

### 5.2 Recovery statistics

For instances A05 and A10, there is no operational phase before the start of the recovery period. Therefore, different initial schedules do not affect the disruption scenario. Moreover, for both A05 and A10, the disruption is a severe global capacity reduction: the initial number of departures and arrivals are 3012 and 2892 respectively; in the disrupted scenario, there is a total reduction of 1110 departures and 1051 arrivals, i.e. a total airport capacity reduction of more than 30%. The consequence is a massive flight cancellation, which highly dominates delays and hides differences of the original schedules. The comparison of recovery statistics for these instances is therefore irrelevant and not reported here.

The detailed results after applying the recovery algorithm for the 1-day instances are listed in Appendix B. We report, for each 1-day scenario, the recovery costs as computed by the cost checker provided for the ROADEF Challenge 2009, the total number of canceled flights (including the forced cancellations from the operational period), the number of canceled passengers, which does not include the lost passengers from the scheduling phase (these are removed from the formulation).

The recovery algorithm is exploiting the non-trivial recovery cost structure as expected. The relation between recovery costs and a posteriori statistics such as number of canceled flights, total delay or number of canceled passengers is not uniform. Indeed, these values are not strictly decreasing for decreasing recovery costs.

The reduction of recovery costs is not uniform for a same model with increasing values of budget C. This is not surprising, as the budget allows for better *a priori* solutions, but does not guarantee the solution

to be appropriate a posteriori for any given scenario. However, some models generate solutions with an impressive recovery cost reduction: model MIT\_20000 reduces the recovery costs by 68.5% in average over the 8 instances. In absolute numbers, the highest savings are obtained with model MIT\_20000 for instance A09, saving up to 1.32 Million€, which corresponds to a saving of 70.6% compared to the recovery costs for the original schedule. The highest relative saving is 93.0%, again achieved by MIT\_20000 for instance A08. CROSS\_1000 is the model that has the most often higher recovery costs than 0r, namely in 4 out of 8 instances. PCON\_2500 is actually the only model higher total recovery costs summed over all scenarios than 0r.

CROSS\_1000 and Or both have the highest recovery costs for 2 out of 8 instances. In the remaining 4 instances, it is always a different model that has highest recovery costs. The highest increase in recovery costs occurs at instance A07 with model MIT\_5000, with an increase of 239,777€, i.e. 37.9% more than Or.

Although we observe significant differences among the different solutions, there is no homogeneous relation between any UF and the recovery statistics: in general, solutions with higher slack have indeed lower recovery costs, but, for example, MIT\_2500 has lower recovery costs than MIT\_5000.

As the different disruption scenarios are not equally probable, average results are not representative. We therefore analyze the *performance profile* (Dolan and Moré, 2002) of the different models. They represent, for each model s and each instance p, the probability

$$P(r_{s,p} \le \tau : 1 \le s \le n_s)$$

of the model's solution to be withing a factor  $\tau$  of the best found solution in the same instance.  $r_{s,p}$  is the value of the solution obtained with model s on instance p divided by the best found solution for instance p and  $n_s$  is the number of instances solved with model s (in our case,  $n_s = 8$  for each model).

When  $\tau=0$ , the value of  $P(r_{s,p}\leq \tau:1\leq s\leq n_s)$  is the probability of model s to lead to the best solution. Eventually, when  $\tau$  grows lager, all models s will have a probability  $P(r_{s,p}\leq \tau:1\leq s\leq n_s)=1$ , as all models are able to solve the solution and therefore have a finite value.

Figure 1 shows the performance profile with respect to the recovery costs for Or, IT\_10000, MIT\_20000, CROSS\_5000 and PCON\_5000, which correspond to the best solutions for each model. Figure 2 shows more in details the evolution of the performance profiles shown in Figure 1

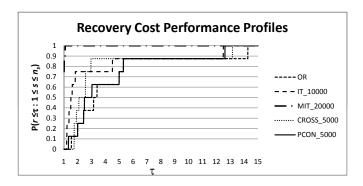


Figure 1: Performance profile for Or, IT\_10000, MIT\_20000, CROSS\_5000 and PCON\_5000.

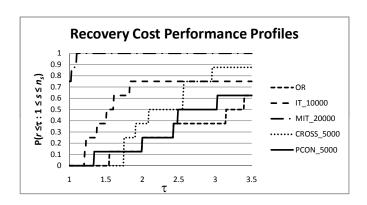


Figure 2: Details for the evolution of the performance curves in Figure 1 for  $\tau \leq 3.5$ .

The best model is clearly MIT\_20000, as its probability to be the best model is 0.75. Moreover, it has probability 1 to have recovery costs at most 1.1 times the lowest found solution. Interestingly, for all other models displayed in Figures 1 and 2, there is at least one instance for which the recovery costs are more than 12 times higher than the recovery costs of MIT\_20000. We observe also that the second-best model is IT\_10000, as is has probability 0.75 to have recovery costs within 1.6 times the lowest found recovery costs. The original solution is the one with lowest probability of being within 3.4 times the best found solution, and also has the highest ratio  $r_{s,p} = 14.27$  for instance A08.

For the models not displayed in Figures 1 and 1, only MIT\_10000 is competing with MIT\_20000, having probability 0.875 to be within a factor  $\tau=1.2$  of the best solution; it is also the only solution with ratio  $\tau<10$  for instance A08. All other models are below the performance profile of IT\_10000 for  $\tau\leq 2$ . The highest ratio is  $\tau=14.60$ , obtained with CROSS\_1000 for instance A08.

Next, we have to answer the question whether the proposed UFs are significantly correlated or not with the different recovery statistics. Table 3 shows the correlation between the UFs and the different recovery metrics, and Table 4 shows the significance test for the correlations. The statistical test is a bilateral significance test with confidence level  $\alpha=0.01$  and 166 degrees of liberty (there are 168 observed solutions in total: 8 scenarios, each being evaluated on 21 different solutions). The correlation is significant if the t-value of the test satisfies | t min > 2.606.

UF	IT	MIT	CROSS	PCON
Recovery Costs	-0.371	-0.480	0.052	-0.269
Total Delay	-0.614	-0.393	0.154	-0.562
Pax Delay	-0.550	-0.404	-0.005	-0.269
Canceled Flights	-0.004	-0.194	0.152	-0.026
Rerouted Pax	-0.267	-0.412	0.016	-0.166
Canceled Pax	-0.631	-0.403	0.037	-0.634

Table 3: Values of the correlation between UF values and recovery statistics.

t-values	IT	MIT	CROSS	PCON
Recovery Costs	-5.147	-7.046	0.666	-3.596
Total Delay	-10.014	-5.510	2.009	-8.753
Pax Delay	-8.475	-5.683	-0.067	-3.596
Canceled Flights	-0.055	-2.541	1.988	-0.337
Rerouted Pax	-3.569	-5.822	0.210	-2.170
Canceled Pax	-10.481	-5.669	0.483	-10.558

Table 4: Significance test for the correlation with confidence level  $\alpha=0.01$ ; the correlation is significant if  $\mid t \mid \geq 2.606$ .

Table 3 shows that IT, MIT and PCON have a large negative correlation with all the recovery statistics but the number of canceled flights; CROSS has only low correlation with the metrics. The significance test in Table 4 show that CROSS is not significantly correlated with any of the recovery statistics. Moreover, non of the UFs is significantly correlated with the number of canceled flights.

Interestingly, PCON is not significantly correlated with the number of rerouted passengers. This is somewhat surprising, as the model maximizes the slack for passenger connections and should, therefore, have a higher number of passengers making the connection. A possible explanation is that in (13)-(14), we consider the set I of *all* possible connections. In the data, however, some connections have large connection time (around 6-8 hours) whereas some are tight (30 minutes to 1-2 hours). In the model, however, connection time is considered for both large and tight connections in the same way. An alternative is to restrict I to the set of tight connections, allowing for focusing on the risky connections only. This also simplifies the PCON model, as the number of constraints in (13)-(14) depends on | I |.

#### 5.3 Synthesis

We solve instances with more than 1200 flights and 85 aircrafts within reasonable computation times. The obtained solutions show that there is a negative correlation between recoverability and IT, MIT and PCON. The correlation is not significant for CROSS, which contradicts the practitioners intuition.

There are two explanations for this. First of all, the results show a reduction of idle time to gain plane crossings, thus also a diminution in the schedule's recoverability. On the other hand, although the recovery algorithm allows for plane swaps, it is the case only for planes of the same fleet. Moreover, CROSS does not differentiate fleets, and assumes homogeneous fleet. To distinguish fleets, we need the meeting point constraints for each fleet type, increasing by another factor the size of the model. This explains why CROSS is not effective in our results. This does, however, not imply that this UF should be discarded, but only that the combination of the CROSS model and *our* recovery algorithm does not lead to significant increase of recoverability.

The trade-off between loss of revenue at the scheduling phase and savings at the recovery phase is impressive: with MIT\_20000, a loss of less than 143,000€ of booking revenue (3.57%) enables to save ove 3.82 Mio€ in terms of recovery costs on the 8 1-day instances.

### 6 Conclusion

In this paper, we present an application of the UFO framework (Eggenberg et al., 2009) to the airline scheduling problem. We present a quantitative simulation to evaluate a solution's performance on real instances,

using an external evaluation tool.

The obtained results show that although our models do not consider any explicit uncertainty characterization, the solutions are able to significantly improve the original solution's recoverability. We prove that an increased idle time improves recoverability of a schedule. In the best case, the total recovery costs over 8 1-day instances can be reduced by more than 3.82 Mio€ which corresponds to a saving of 68.5% with respect to the recovery costs of the original schedule. Additionally, the loss in terms of revenue are small when the models do not consider missed connections: the loss in terms of passenger revenue is always lower than 4.3% of the initial revenue, i.e. less than 22,100€; however, these losses do not consider the possibily of additional bookings on the new connections created in the schedule.

This study opens different research directions. From the computational part, the developed algorithms have still potential for improvements: replace the heuristic by the exact version of the algorithm, improve convergence speed with smart branching decisions, etc. The recovery algorithm would also benefit from an efficient generator of repositioning flights.

In terms of application, other UFs and the combination with different recovery algorithms should be tested in order to better understand the relations between UFs and recoverability; the relation between UFs and different recovery algorithms; the correlation between the different UFs; the efficiency of UFs for different airlines. Finally, the simulations should be extended considering crews and crew recovery, as this is a crucial part in airline operations; this would allow to test crew-based UFs.

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## A Complete proactive statistics

Tables 5-12 report the a priori statistics for the 1-day instances (A01-A04 and A06-A09), and Tables 13 and 14 for the 2-day instances A05 and A10.

# B Complete recovery statistics

Tables 15-22 report the recovery statistics for the 1-day instances (A01-A04 and A06-A09).

IT_20000	8530	182	18975	1230	3488	149065	243	29.0	2.36	327
IT_10000	8530	182	18975	1230	3488	149065	243	29.0	2.36	367
IT_5000	5000	97	17000	1150	3496	141825	85	0.24	0.59	271
$_{ m IT\_2500}$	2500	52	14500	1025	3455	136555	46	0.13	0.27	311
IT_1000	1000	20	13000	940	3454	133450	0	00.00	00.00	331
Cross_20000	5980	255	10965	460	3519	128630	467	1.30	4.29	267
Cross_10000	5980	255	10965	460	3519	128630	467	1.30	4.29	267
Cross_5000	2000	248	11450	505	3530	129345	372	1.03	3.69	605
Cross_2500	2500	178	11415	620	3517	128115	341	0.95	3.1	394
Cross_1000	1000	109	11880	069	3494	130040	128	0.36	1.37	384
0r	0	0	12000	790	3430	130470	0	0.00	0.00	0.2
Model	Used Budget [min]	# Modified Flts	IT [min]	MIT [min]	CROSS	PCON [min]	# Lost Psg	Psg Lost [%]	Revenue Loss [%]	CPU Time [s]

000						_			-	
PCON_2000	0	0	12000	790	3430	130470	0	0.00	0.00	1000
PCON_10000	0	0	12000	790	3430	130470	0	0.00	0.00	1000
PCON_5000	0	0	12000	790	3430	130470	0	0.00	0.00	1009
PCON_2500	0	0	12000	790	3430	130470	0	0.00	0.00	1041
PCON_1000	1000	40	12715	092	3453	134685	0	0.00	0.00	140
MIT_20000	10025	308	16750	3355	3410	142375	473	1.31	4.11	007
MIT_10000	9830	304	16720	3330	3416	141990	460	1.28	3.86	606
MIT_5000	2000	191	14710	2835	3438	135640	260	0.72	1.90	006
MIT_2500	2500	105	13520	2210	3450	133235	139	0.39	0.99	216
MIT_1000	1000	56	12610	1645	3440	131245	99	0.18	0.48	066
Model	Used Budget [min]	# Modified Flts	IT [min]	MIT [min]	CROSS	PCON [min]	# Lost Psg	Psg Lost [%]	Revenue Loss [%]	[2] cm:m IIQD

Table 5: A priori statistics for instance A01.

IT_20000	8530	182	18975	1230	3488	149065	243	0.67	2.36	327
IT_10000	8530	182	18975	1230	3488	149065	243	29.0	2.36	367
IT_5000	5000	97	17000	1150	3496	141825	85	0.24	0.59	271
IT_2500	2500	52	14500	1025	3455	136555	46	0.13	0.27	311
IT_1000	1000	20	13000	940	3454	133450	0	00.00	00.00	296
Cross_20000	5980	255	10965	460	3519	128630	467	1.30	4.29	266
Cross_10000	5980	255	10965	460	3519	128630	467	1.30	4.29	294
Cross_5000	2000	248	11450	505	3530	129345	372	1.03	3.69	543
Cross_2500	2500	178	11415	620	3517	128115	341	0.95	3.1	396
Cross_1000	1000	109	11880	069	3494	130040	128	0.36	1.37	384
0r	0	0	12000	790	3430	130470	0	0	0.00	0.2
Model	Used Budget [min]	# Modified Flts	IT [min]	MIT [min]	CROSS	PCON [min]	# Lost Psg	Psg Lost [%]	Revenue Loss [%]	CPU Time [s]

CON_20000	0	0	0003	- 06	430	30470	0	00.	00.	
PCON			1	_	<u>ო</u>	13		_	_	
PCDN_10000	0	0	12000	790	3430	130470	0	0.00	0.00	
PCON_5000	0	0	12000	790	3430	130470	0	0.00	0.00	
PCON_2500	0	0	12000	790	3430	130470	0	0.00	0.00	
PCUN_1000	1000	40	12715	092	3453	134685	0	0.00	0.00	
MIT_20000	10025	308	16750	3355	3410	142375	473	1.31	4.11	1
MIT_10000	9830	304	16720	3330	3416	141990	460	1.28	3.86	
MIT_5000	2000	191	14710	2835	3438	135640	260	0.72	1.90	
MIT_2500	2500	105	13520	2210	3450	133235	139	0.39	0.99	
MIT_1000	1000	56	12610	1645	3440	131245	99	0.18	0.48	
Model	Used Budget [min]	# Modified Flts	IT [min]	MIT [min]	CROSS	PCON [min]	# Lost Psg	Psg Lost [%]	Revenue Loss [%]	

Table 6: A priori statistics for instance A02.

11-20000	8530	182	18975	1230	3488	149065	243	29.0	2.36	326
0000T-1T	8530	182	18975	1230	3488	149065	243	29.0	2.36	365
0006-11	2000	26	17000	1150	3496	141825	85	0.24	0.59	271
0002-11	2500	52	14500	1025	3455	136555	46	0.13	0.27	310
T1-1000	1000	20	13000	940	3454	133450	0	0.00	0.00	331
CLOSS-ZOOO	5980	255	10965	460	3519	128630	467	1.30	4.29	268
CLOSS-TOOO	5980	255	10965	460	3519	128630	467	1.30	4.29	267
CLOSS-2000	5000	248	11450	505	3530	129345	372	1.03	3.69	604
CLOSS_ZSOU	2500	178	11415	620	3517	128115	341	0.95	3.1	394
CLOSS-TOOO	1000	109	11880	069	3494	130040	128	0.36	1.37	384
i i	0	0	12000	790	3430	130470	0	0	0.00	0.2
INIONE	Used Budget [min]	# Modified Flts	IT [min]	MIT [min]	CROSS	PCON [min]	# Lost Psg	Psg Lost [%]	[%]	CPU Time [s]

$\overline{}$				_	_			_	_
0	0	12000	790	3430	130470	0	0.00	0.00	1423
0	0	12000	790	3430	130470	0	0.00	0.00	1083
0	0	12000	790	3430	130470	0	0.00	0.00	1087
0	0	12000	790	3430	130470	0	0.00	0.00	1241
1000	40	12715	092	3453	134685	0	0.00	0.00	754
10025	308	16750	3355	3410	142375	473	1.31	4.11	430
9830	304	16720	3330	3416	141990	460	1.28	3.86	383
2000	191	14710	2835	3438	135640	260	0.72	1.90	310
2500	105	13520	2210	3450	133235	139	0.39	0.99	345
1000	56	12610	1645	3440	131245	99	0.18	0.48	331
Used Budget [min]	# Modified Flts	IT [min]	MIT [min]	CROSS	PCON [min]	# Lost Psg	Psg Lost [%]	Revenue Loss [%]	CPU Time [s]
	5000 9830 10025 1000 0 0 0	5000         9830         10025         1000         0         0         0           191         304         308         40         0         0         0	n]         1000         2500         5000         9830         10025         1000         0         0         0         0           s         56         105         191         304         308         40         0         0         0           12610         13520         14710         16720         16750         12715         12000         12000         12000	n]         1000         2500         5000         9830         10025         1000         0         0         0           s         56         105         191         304         308         40         0         0         0           12610         13520         14710         16720         16750         12715         12000         12000         12000           1645         2210         2835         3330         3355         760         790         790         790	n]         1000         2500         5000         9830         10025         1000         0         0         0         0           s         56         105         191         304         308         40         0         0         0         0           12610         13520         14710         16720         16750         12715         12000         12000         12000           1645         2210         2835         3330         3355         760         790         790           3440         3450         3450         3430         3430         3430	n]         1000         2500         5000         9830         10025         1000         0         0         0         0           s         56         105         191         304         308         40         0         0         0         0           12610         13520         14710         16720         16750         12715         12000         12000         12000           1645         2210         2835         3330         3355         760         790         790         790           3440         3450         3438         3416         3410         13685         130470         130470         130470	1000         2500         5000         9830         10025         1000         0         0         0           56         105         191         304         308         40         0         0         0           12610         13520         14710         16720         16750         12715         12000         12000         12000           1645         2210         2835         3330         3355         760         790         790         790           3440         3450         3438         3416         3410         3453         3430         3430         3430           131245         133235         135640         141990         142375         134685         130470         130470         130470           66         139         260         460         473         0         0         0         0	1000         2500         5000         9830         10025         1000         0         0         0           56         105         191         304         308         40         0         0         0           12610         13520         14710         16720         16750         12715         12000         12000         12000           1645         2210         2835         3330         3355         760         790         790         790           3440         3450         3416         3410         3453         3430         3430         3430           131245         133235         135640         141990         142375         134685         130470         130470         130470           66         139         0.72         1.28         1.31         0.00         0.00         0.00         0.00	n]         10000         2500         5000         9830         10025         1000           s         56         105         191         304         308         40           12610         13520         14710         16720         16750         12715         1           1645         2210         2835         3330         3355         760         3433         3410         3453         3           131245         133235         135640         141990         142375         134685         13         6         139         0

Table 7: A priori statistics for instance A03.

	_									
11-20000	8530	182	18975	1230	3488	149065	243	0.67	2.36	368
11-10000	8530	182	18975	1230	3488	149065	243	29.0	2.36	329
0006-11	2000	26	17000	1150	3496	141825	85	0.24	0.59	271
0067-11	2500	52	14500	1025	3455	136555	46	0.13	0.27	348
11-1000	1000	20	13000	940	3454	133450	0	0.00	0.00	296
CLOSS_ZOOO	5980	255	10965	460	3519	128630	467	1.30	4.29	270
CLOSS-IOOOO	5980	255	10965	460	3519	128630	467	1.30	4.29	299
CLOSS-2000	5000	248	11450	505	3530	129345	372	1.03	3.69	547
CLOSS_ZSOU	2500	178	11415	620	3517	128115	341	0.95	3.1	394
CLOSS-IOOO	1000	109	11880	069	3494	130040	128	0.36	1.37	429
J.	0	0	12000	790	3430	130470	0	0	0.00	0.2
INIOGEI	Used Budget [min]	# Modified Flts	IT [min]	MIT [min]	CROSS	PCON [min]	# Lost Psg	Psg Lost [%]	Revenue Loss [%]	CPU Time [s]

Model	MIT_1000	MIT_2500	MIT_5000	MIT_10000	MIT_20000	PCON_1000	PCON_2500	PCON_5000	PCON_10000	PCON_20000
Used Budget [min]	1000	2500	2000	9830	10025	1000	0	0	0	0
# Modified Flts	56	105	191	304	308	40	0	0	0	0
IT [min]	12610	13520	14710	16720	16750	12715	12000	12000	12000	12000
MIT [min]	1645	2210	2835	3330	3355	200	790	190	190	790
CROSS	3440	3450	3438	3416	3410	3453	3430	3430	3430	3430
PCON [min]	131245	133235	135640	141990	142375	134685	130470	130470	130470	130470
# Lost Psg	99	139	260	460	473	0	0	0	0	0
Psg Lost [%]	0.18	0.39	0.72	1.28	1.31	0.00	0.00	0.00	0.00	0.00
Revenue Loss [%]	0.48	0.99	1.90	3.86	4.11	0.00	0.00	0.00	0.00	0.00
CPU Time [s]	329	309	350	383	383	890	1461	928	1082	1223

Table 8: A priori statistics for instance A04.

$IT_{-}20000$	8530	182	18975	1230	3488	147315	347	0.74	2.47	400
IT_10000	8530	182	18975	1230	3488	147315	347	0.74	2.47	377
IT_5000	5000	97	17000	1150	3496	140355	106	0.23	0.70	332
$_{ m IT\_2500}$	2500	52	14500	1025	3455	134965	29	0.14	0.30	359
IT_1000	1000	20	13000	940	3454	131700	0	00.00	00.00	360
Cross_20000	5980	255	10965	460	3519	126305	344	0.74	3.01	305
Cross_10000	5980	255	10965	460	3519	126305	344	0.74	3.01	305
Cross_5000	2000	248	11450	505	3530	126140	360	0.77	3.04	656
Cross_2500	2500	178	11415	620	3517	126520	184	0.39	1.60	454
Cross_1000	1000	109	11880	069	3494	128245	19	0.04	0.04	464
Or.	0	0	12000	790	3430	130470	0	0	0	0.2
Model	Used Budget [min]	# Modified Flts	IT [min]	MIT [min]	CROSS	PCON [min]	# Lost Psg	Psg Lost [%]	Revenue Loss [%]	CPU Time [s]

00										
PCON_2000	0	0	12000	790	3430	128670	0	0.00	0.00	1061
PCON_10000	1000	229	17310	805	3565	160980	0	0.00	0.00	1,000
PCON_5000	5000	105	15340	800	3489	150675	0	0.00	0.00	1990
PCON_2500	2500	53	13920	825	3458	141305	0	0.00	0.00	000
PCON_1000	1000	23	12915	805	3442	134380	0	0.00	0.00	0 H
MIT_20000	10025	308	16750	3355	3410	140060	404	0.87	3.00	270
MIT_10000	9830	304	16720	3330	3416	140035	427	0.92	3.15	166
MIT_5000	2000	191	14710	2835	3438	133470	239	0.51	1.52	926
MIT_2500	2500	105	13520	2210	3450	131285	131	0.28	86.0	278
MIT_1000	1000	56	12610	1645	3440	129675	88	0.19	0.46	000
Model	Used Budget [min]	# Modified Flts	IT [min]	MIT [min]	CROSS	PCON [min]	# Lost Psg	Psg Lost [%]	Revenue Loss [%]	CDII Timo [a]

Table 9: A priori statistics for instance A06.

Model	0r	Cross_1000	Cross_2500	Cross_5000	Cross_10000	Cross_20000	$\mathrm{IT\_1000}$	$_{ m IT\_2500}$	IT_5000	IT_10000	IT_20000
Used Budget [min]	0	1000	2500	5000	5980	5980	1000	2500	5000	8530	8530
# Modified Flts	0	109	178	248	255	255	20	52	97	182	182
IT [min]	12000	11880	11415	11450	10965	10965	13000	14500	17000	18975	18975
MIT [min]	790	069	620	505	460	460	940	1025	1150	1230	1230
CROSS	3430	3494	3517	3530	3519	3519	3454	3455	3496	3488	3488
PCON [min]	130470	128245	126520	126140	126305	126305	131700	134965	140355	147315	147315
# Lost Psg	0	19	184	360	344	344	0	29	106	347	347
Psg Lost [%]	0	0.04	0.39	0.77	0.74	0.74	00.00	0.14	0.23	0.74	0.74
Revenue Loss [%]	0	0.04	1.60	3.04	3.01	3.01	00.00	0.30	0.70	2.47	2.47
CPU Time [s]	0.2	434	475	622	313	267	296	311	272	328	327

Model	MIT_1000	MIT_2500	MIT_5000	MIT_10000	MIT_20000	PCON_1000	PCON_2500	PCON_5000	PCGN_10000	PCON_20000
Used Budget [min]	1000	2500	2000	9830	10025	1000	2500	2000	1000	0
# Modified Flts	56	105	191	304	308	23	53	105	229	0
IT [min]	12610	13520	14710	16720	16750	12915	13920	15340	17310	12000
MIT [min]	1645	2210	2835	3330	3355	805	825	800	805	790
CROSS	3440	3450	3438	3416	3410	3442	3458	3489	3565	3430
PCON [min]	129675	131285	133470	140035	140060	134380	141305	150675	160980	128670
# Lost Psg	88	131	239	427	404	0	0	0	0	0
Psg Lost [%]	0.19	0.28	0.51	0.92	0.87	0.00	0.00	0.00	0.00	0.00
Revenue Loss [%]	0.46	0.98	1.52	3.15	3.00	0.00	0.00	0.00	0.00	0.00
CPU Time [s]	330	308	309	383	382	683	729	1177	2923	808

Table 10: A priori statistics for instance A07.

11-20000	8530	182	18975	1230	3488	147315	347	0.74	2.47	327
11-10000	8530	182	18975	1230	3488	147315	347	0.74	2.47	328
0006-11	2000	26	17000	1150	3496	140355	106	0.23	0.70	271
0002-11	2500	52	14500	1025	3455	134965	29	0.14	0.30	311
T1-1000	1000	20	13000	940	3454	131700	0	0.00	0.00	295
Cross_Z0000	5980	255	10965	460	3519	126305	344	0.74	3.01	266
Cross_IOOOO	5980	255	10965	460	3519	126305	344	0.74	3.01	268
CLOSS-2000	5000	248	11450	505	3530	126140	360	0.77	3.04	545
CLOSS_ZSOU	2500	178	11415	620	3517	126520	184	0.39	1.60	395
CLOSS-IOOO	1000	109	11880	069	3494	128245	19	0.04	0.04	386
J.	0	0	12000	790	3430	130470	0	0	0	0.2
INIOGEI	Used Budget [min]	# Modified Flts	IT [min]	MIT [min]	CROSS	PCON [min]	# Lost Psg	Psg Lost [%]	Revenue Loss [%]	CPU Time [s]

Model	MIT_1000	MIT_2500	MIT_5000	MIT_10000	MIT_20000	PCON_1000	PCON_2500	PCON_5000	PCON_10000	PCON_20000
Used Budget [min]	1000	2500	2000	9830	10025	1000	2500	2000	1000	0
# Modified Flts	56	105	191	304	308	23	53	105	229	0
IT [min]	12610	13520	14710	16720	16750	12915	13920	15340	17310	12000
MIT [min]	1645	2210	2835	3330	3355	805	825	800	802	190
CROSS	3440	3450	3438	3416	3410	3442	3458	3489	3565	3430
PCON [min]	129675	131285	133470	140035	140060	134380	141305	150675	160980	128670
# Lost Psg	88	131	239	427	404	0	0	0	0	0
Psg Lost [%]	0.19	0.28	0.51	0.92	0.87	0.00	0.00	0.00	0.00	0.00
Revenue Loss [%]	0.46	0.98	1.52	3.15	3.00	0.00	0.00	0.00	0.00	0.00
CPU Time [s]	329	309	309	383	383	683	728	1020	2401	608

Table 11: A priori statistics for instance A08.

IT_20000	8530	182	18975	1230	3488	147315	347	0.74	2.47	237
IT_10000	8530	182	18975	1230	3488	147315	347	0.74	2.47	326
$IT_5000$	2000	26	17000	1150	3496	140355	106	0.23	0.70	271
$_{ m IT\_2500}$	2500	52	14500	1025	3455	134965	29	0.14	0.30	310
1T_1000	1000	20	13000	940	3454	131700	0	00.00	00.00	295
Cross_20000	5980	255	10965	460	3519	126305	344	0.74	3.01	267
Cross_10000	5980	255	10965	460	3519	126305	344	0.74	3.01	267
Cross_5000	2000	248	11450	505	3530	126140	360	0.77	3.04	542
Cross_2500	2500	178	11415	620	3517	126520	184	0.39	1.60	394
Cross_1000	1000	109	11880	069	3494	128245	19	0.04	0.04	382
0r	0	0	12000	790	3430	130470	0	0	0	0.2
Model	Used Budget [min]	# Modified Flts	IT [min]	MIT [min]	CROSS	PCON [min]	# Lost Psg	Psg Lost [%]	Revenue Loss [%]	CPU Time [s]

0										
PCDN_2000	0	0	12000	790	3430	128670	0	0.00	0.00	1078
PCON_10000	1000	229	17310	805	3565	160980	0	0.00	0.00	2480
PCUN_5000	2000	105	15340	800	3489	150675	0	0.00	0.00	1020
PCON_2500	2500	53	13920	825	3458	141305	0	0.00	0.00	73.5
PCON_1000	1000	23	12915	805	3442	134380	0	0.00	0.00	889
MIT_20000	10025	308	16750	3355	3410	140060	404	0.87	3.00	38.9
MIT_10000	9830	304	16720	3330	3416	140035	427	0.92	3.15	383
MIT_5000	2000	191	14710	2835	3438	133470	239	0.51	1.52	310
MIT_2500	2500	105	13520	2210	3450	131285	131	0.28	86.0	310
MIT_1000	1000	56	12610	1645	3440	129675	88	0.19	0.46	329
Model	Used Budget [min]	# Modified Flts	IT [min]	MIT [min]	CROSS	PCON [min]	# Lost Psg	Psg Lost [%]	Revenue Loss [%]	CPII Time [s]

Table 12: A priori statistics for instance A09.

0000 IT_20000		•	85 85000	-					•	
0 IT_10			85085							
IT_500	2000	66	82865	550	6157	276910	107	0.15	0.45	21369
IT_2500	2500	49	80365	550	6143	270795	23	0.03	0.08	10369
IT_1000	1000	23	78865	535	6103	267150	37	0.05	0.14	17064
Cross_20000	9105	442	76920	165	6205	262365	643	0.89	2.79	6209
Cross_10000	8515	424	76925	140	6184	263895	661	0.92	2.95	6914
Cross_5000	2000	360	77450	215	6195	263965	271	0.38	1.22	6040
Cross_2500	2500	234	77710	365	6185	263965	187	0.26	96.0	9753
Cross_1000	1000	127	77870	430	6169	264350	46	90.0	0.17	6202
Or.	0	0	29822	490	6100	264480	0	0	0	
Model	Used Budget [min]	# Modified Flts	IT [min]	MIT [min]	CROSS	PCON [min]	# Lost Psg	Psg Lost [%]	Revenue Loss [%]	CPU Time [s]

000	MIT_2500	MIT_5000	MIT_10000	MIT_20000	PCON_1000	PCON_2500	PCON_5000	PCON_10000	PCON_20000
	2500	2000	10000	16260	1000	230	230	230	230
	146	251	407	578	32	∞	∞	∞	œ
1-	8590	79055	80160	81385	78210	77870	77870	77870	77870
	1270	1355	1965	2345	460	485	485	485	485
9	140	9209	6085	6050	6103	6105	6105	6105	6105
2	35655	270640	275100	283775	269230	264870	264870	264870	264870
	22	244	377	370	0	0	0	0	0
_	).11	0.34	0.52	0.51	0	0	0	0	0
_	0.28	1.14	1.67	1.63	0	0	0	0	0
9	5257	4843	5034	6397	54089	35175	61236	37901	10740

Table 13: A priori statistics for instance A05.

Model	0r	Cross_1000	Cross_2500	Cross_5000	Cross_10000	Cross_20000	IT_1000	IT_2500	IT_5000	IT_10000	IT_20000
Used Budget [min]	0	1000	2500	5000	8515	9105	1000	2500	2000	10000	10105
# Modified Flts	0	127	234	360	424	442	23	49	66	248	254
IT [min]	77865	77870	77710	77450	76925	76920	78865	80365	82865	85050	82000
MIT [min]	490	430	365	215	140	165	535	550	550	410	350
CROSS	6100	6169	6185	6195	6184	6205	6103	6143	6157	6174	6154
PCON [min]	251805	251700	250920	250305	250800	248945	254255	257580	263570	269870	269910
# Lost Psg	0	92	152	401	089	547	62	32	65	291	236
Psg Lost [%]	0	80.0	0.16	0.42	0.71	0.57	90.0	0.03	0.07	0.31	0.25
Revenue Loss [%]	0	0.21	0.70	1.60	2.85	2.10	0.2	0.13	0.33	1.18	0.92
CPU Time [s]		8776	11273	6551	2992	5495	16971	10416	20659	11575	10485

Model	MIT_1000	MIT_2500	MIT_5000	MIT_10000	MIT_20000	PCUN_1000	PCON_2500	PCON_5000	PCGN_10000	PCON_20000
Used Budget [min]	1000	2500	2000	10000	16260	1000	2500	710	755	755
# Modified Flts	61	146	251	407	578	30	28	25	29	29
IT [min]	78235	78590	79055	80160	81385	78230	78925	78005	78040	78040
MIT [min]	950	1270	1355	1965	2345	490	200	475	475	475
CROSS	6108	6140	9209	6085	6050	6107	6118	6117	6106	6106
PCON [min]	252495	253290	256390	261255	269555	257115	265245	252835	253380	253380
# Lost Psg	44	86	242	450	656	0	0	0	0	0
Psg Lost [%]	0.05	0.1	0.25	0.47	69.0	0	0	0	0	0
Revenue Loss [%]	0.14	0.31	Н	1.9	2.53	0	0	0	0	0
CPU Time [s]	7326	4910	4805	5789	6157	28494	10004	41222	12851	24752

Table 14: A priori statistics for instance A10.

71305.7	0	1026	31.1	33	33	3105	98
71305.7	0	1026	31.1	33	33	3105	98
81686.25	0	1028	26.4	39	39	3762	130
82003.8	0	1188	27	44	38	4477	180
89106.85	0	1242	27.6	45	42	5250	181
46225.55	0	1602	29.1	55	10	0330	201
46225.55	0	1602	29.1	55	10	0689	201
40569.4	0	1498	30.6	49	7	4636	199
42569.75	0	1366	28.5	48	10	4341	192
79101.2	0	1384	26.6	52	34	5151	228
83820.2	0	1390	27.3	51	37	5861	239
Recovery Costs [€]	# Canceled Flts	Total Delay [min]	Avg Delay [min]	# Delayed Flts	# Canceled Psg	Total Pax delay [min]	# Rerouted Psg
	83820.2 79101.2 42569.75 40569.4 46225.55 46225.55 89106.85 82003.8 81686.25 71305.7	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$

Model	MIT_1000	MIT_2500	MIT_5000	MIT_10000	MIT_20000	PCDN_1000	PCON_2500	PCON_5000	PCON_10000	PCUN_20000
Recovery Costs [€]	81353.3	22162.6	19382.95	16224.6	15822.35	87750.75	83820.2	83820.2	83820.2	83820.2
# Canceled Flts	0	0	0	0	0	0	0	0	0	0
Total Delay [min]	1336	1303	1230	710	200	1282	1390	1390	1390	1390
Avg Delay [min]	27.3	27.7	26.7	28.4	29.2	25.6	27.3	27.3	27.3	27.3
# Delayed Flts	49	47	46	25	24	20	51	51	51	51
# Canceled Psg	36	0	0	0	0	42	37	37	37	37
Total Pax delay [min]	4731	4541	3726	3410	3100	3810	5861	5861	5861	5861
# Rerouted Psg	235	212	120	83	72	218	239	239	239	239

Table 15: Recovery statistics for instance A01.

UT         Cross_1000         Cross_1000         Cross_1000         Cross_1000         Cross_1000         Cross_11000         LT-500         LT-500         LT-500           359898.35         300908.5         28647         310565.3         207042.95         316583.85         317546.45         264725.65           2         2         2         2         2         2         2         2           900         945         1060         743         1118         1118         900         878         753           40.9         39.4         37.9         23         29         29         29         21         16           21         161         151         172         126         176         175         142           211         605         597         749         552         544         566         528	T.I20000	224186.35	4	317	31.7	10	153	2668	543
OF         Cross_1000         Cross_2500         Cross_1000         Cross_2500         Cross_2500         Cross_2500         Cross_2500         Cross_2500         II_2500         II_2500           359898.35         300908.5         28647         310565.3         207042.95         316583.85         317546.4f           2         2         2         2         2         2         2         2           900         945         1060         743         1118         1118         900         878           40.9         39.4         27.9         23         29         29         22         21           21         161         151         172         126         176         175           211         161         151         1724         10828         9840         11667           572         605         597         749         552         552         544         566									
OF         Cross_1000         Cross_2500         Cross_1000         Cross_2500         Cross_2500         Cross_2500         Cross_2500         Cross_2500         II_2500         II_2500           359898.35         300908.5         28647         310565.3         207042.95         316583.85         317546.4f           2         2         2         2         2         2         2         2           900         945         1060         743         1118         1118         900         878           40.9         39.4         27.9         23         29         29         22         21           21         161         151         172         126         176         175           211         161         151         1724         10828         9840         11667           572         605         597         749         552         552         544         566	T.I5000	264725.65	2	753	47.1	16	142	11300	528
Ur         Cross-1000         Cross-2500         Cross-1000         Cross-2000         Cross-2000           359898.35         300908.5         286647         310565.3         207042.95         27042.95         27042.95         27042.95         37042.95 <t< td=""><td>T.I2500</td><td>317546.45</td><td>2</td><td>878</td><td>41.8</td><td>21</td><td>175</td><td>11667</td><td>266</td></t<>	T.I2500	317546.45	2	878	41.8	21	175	11667	266
Ur         Cross_1000         Cross_2500         Cross_1000         Cross_1000           359898.35         300908.5         286647         310565.3         207042.95           2         2         4         2           40.9         945         1060         743         1118           40.9         39.4         37.9         32.3         28.6           22         24         28         23         29           211         161         151         172         126           11990         11735         9583         11264         10828           572         605         597         749         552	T.I. 1000	316583.85	2	006	40.9	22	176	9840	544
Ur         Cross_1000         Cross_2500         Cross_1000         Cross_1000           359898.35         300908.5         286647         310565.3         207042.95           2         2         4         2           40.9         945         1060         743         1118           40.9         39.4         37.9         32.3         28.6           22         24         28         23         29           211         161         151         172         126           11990         11735         9583         11264         10828           572         605         597         749         552	Cross_20000	207042.95	2	1118	28.6	29	126	10828	552
	Cross_10000	207042.95	2	1118	28.6	29	126	10828	552
	Cross_5000	310565.3	4	743	32.3	23	172	11264	749
	Cross_2500	286647	2	1060	37.9	28	151	9583	262
	Cross_1000	300908.5	2	945	39.4	24	161	11735	605
Model  Recovery Costs [€]  # Canceled Fits Total Delay [min]  Avg Delay [min]  # Delayed Fits  # Canceled Psg  Total Pax delay [min]  # Rerouted Psg	n O	359898.35	2	006	40.9	22	211	11990	572
	Model	Recovery Costs [€]	# Canceled Flts	Total Delay [min]	Avg Delay [min]	# Delayed Flts	# Canceled Psg	Total Pax delay [min]	# Rerouted Psg

Model	MIT_1000	MIT_2500	MIT_5000	MIT_10000	MIT_20000	PCON_1000	PCON_2500	PCON_5000	PCON_10000	PCDN_20000
Recovery Costs [€]	318993.4	294180.2	186216.95	151054.25	148676	223478.05	359898.35	359898.35	359898.35	359898.35
# Canceled Flts	2	2	2	2	2	2	2	2	2	2
Total Delay [min]	006	850	839	629	579	710	006	006	006	006
Avg Delay [min]	40.9	44.7	44.2	41.2	38.6	32.3	40.9	40.9	40.9	40.9
# Delayed Flts	22	19	19	16	15	22	22	22	22	22
# Canceled Psg	176	156	106	68	68	140	211	211	211	211
otal Pax delay [min]	11490	10505	9345	8159	7549	11121	11990	11990	11990	11990
# Rerouted Psg	262	571	208	492	473	541	572	572	572	572

Table 16: Recovery statistics for instance A02.

$IT_{-}20000$	487815.75	∞	546	27.3	20	376	10756	812
IT_10000	487815.75		546	27.3	20	376	10756	812
IT_5000	551878.05	∞	682	31	22	417	11031	825
IT_2500	651824.05	∞	908	32.2	25	469	10679	878
IT_1000	633834.2	∞	840	27.1	31	470	10347	811
Cross_20000	598755.75	∞	1089	33	33	461	9515	822
Cross_10000	598755.75	∞	1089	33	33	461	9515	822
Cross_5000	673347.85	∞	915	30.5	30	488	12167	831
Cross_2500	688652.05	∞	981	31.6	31	494	12469	838
Cross_1000   Cross_2500	714408.4	∞	982	29.8	33	495	12717	913
$^{ m 0r}$	704030.7	∞	939	29.3	32	499	10543	006
Model	Recovery Costs [€]	# Canceled Flts	Total Delay [min]	Avg Delay [min]	# Delayed Flts	# Canceled Psg	Total Pax delay [min]	# Rerouted Psg

Model	MIT_1000	MIT_2500	MIT_5000	MIT_10000	MIT_20000	PCUN_1000	PC0N_2500	PCON_5000	PCUN_10000	PCON_20000
Recovery Costs [€]	702840.15	661410.55	481024.4	353766.35	353736.95	۳	704030.7	704030.7	704030.7	704030.7
# Canceled Flts	∞	∞	∞	∞	∞		∞	∞	∞	∞
Total Delay [min]	922	810	714	357	350	816	939	939	939	939
Avg Delay [min]	28.8	27	29.8		21.9	26.3	29.3	29.3	29.3	29.3
# Delayed Flts	32	30	24		16	31	32	32	32	32
# Canceled Psg	499	464	352		272	473	499	499	499	499
Total Pax delay [min]	10350	14054	11403		10479	10496	10543	10543	10543	10543
# Rerouted Psg	855	988	606		858	006	006	006	006	006

Table 17: Recovery statistics for instance A03.

114417.1	12	7092	62.8	113	29	14425	1531
114417.1	12	7092	62.8	113	29	14425	1531
209884.05	15	7104	61.2	116	160	19960	1807
314208.05	16	7409	57.4	129	230	24728	1986
137228.45	20	5611	52.4	107	107	26339	2310
137228.45	20	5611	52.4	107	107	26339	2310
162547.65	16	6127	49.4	124	81	16545	1875
191147.5	16	7197	49.3	146	119	20636	1937
252423.8	18	6869	51.8	135	168	24331	2224
465695.65	20	6223	51.4	121	359	31107	2379
Recovery Costs [€]	# Canceled Flts	Total Delay [min]	Avg Delay [min]	# Delayed Flts	# Canceled Psg	Total Pax delay [min]	# Rerouted Psg
	$\left \begin{array}{cccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	465695.65         252423.8         191147.5         162547.65         137228.45         137228.45         378402.2         314208.05         209884.05         114417.1           20         18         16         16         20         20         16         16         15         12           6223         6989         7197         6127         5611         5611         7218         7409         7104         7092           51.4         51.8         49.3         49.4         52.4         52.4         53.9         57.4         61.2         62.8           121         135         146         124         107         107         134         129         116         113	252423.8         191147.5         162547.65         137228.45         137228.45         378402.2         314208.05         209884.05         114417.1           18         16         16         20         20         16         15         12           6989         7197         6127         5611         7218         7409         7104         7092           51.8         49.3         49.4         52.4         52.4         53.9         57.4         61.2         62.8           135         146         124         107         107         281         230         160         67           168         119         81         107         107         281         230         160         67	465695.65 20 6223 51.4 121 359 3 31107

MIT_1000 MIT_2500			MIT_5000	MIT_10000	MIT_20000	PCON_1000	PCON_2500	PCON_5000	д	PCON_20000
208562.75 142528.65 243143.45 1	243143.45		-	10454.15	93369.15	193056.15	465695.65	465695.65	465695.65	465695.65
		16		10	∞	16	20	20		20
6827		6323		6388	0289	7180	6223	6223		6223
		52.7		50.3	54.5	53.2	51.4	51.4		51.4
134		120		127	126	135	121	121		121
88		240		89	41	141	359	359		359
18237		24719		12280	11430	23752	31107	31107		31107
1918		1880		1329	1171	2132	2379	2379		2379

Table 18: Recovery statistics for instance A04.

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9.86938	0	1026	31.1	33	10	3441	128
35698.6	0	1026	31.1	33	10	3441	128
67259.75	0	1028	26.4	39	24	5733	175
56621.4	0	1188	27	44	15	4305	194
98170.2	0	1242	27.6	45	44	4759	208
81454.15	0	1602	29.1	55	35	4795	238
81454.15	0	1602	29.1	55	35	4795	238
75371.9	0	1498	30.6	49	31	7807	270
60224	0	1366	28.5	48	14	5930	267
120595.75	0	1384	26.6	52	28	5450	250
92998.75	0	1390	27.3	51	39	5065	248
Recovery Costs [€]	# Canceled Flts	Total Delay [min]	Avg Delay [min]	# Delayed Flts	# Canceled Psg	Total Pax delay [min]	# Rerouted Psg
	92998.75   120595.75   60224   75371.9   81454.15   81454.15   98170.2   56621.4   67259.75   35698.6	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$ \begin{bmatrix} 92998.75 & 120595.75 & 60224 & 75371.9 & 81454.15 & 81454.15 & 98170.2 & 56621.4 & 67259.75 & 35698.6 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1390 & 1384 & 1366 & 1498 & 1602 & 1602 & 1242 & 1188 & 1028 & 1026 \\ \end{bmatrix} $	$ \begin{vmatrix} 92998.75 & 120595.75 & 60224 & 75371.9 & 81454.15 & 81454.15 & 98170.2 & 56621.4 & 67259.75 & 35698.6 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1390 & 1384 & 1366 & 1498 & 1602 & 1602 & 1242 & 1188 & 1028 & 1026 \\ 27.3 & 26.6 & 28.5 & 30.6 & 29.1 & 29.1 & 27.6 & 27 & 26.4 & 31.1 \\ \end{vmatrix} $	92998.75         120595.75         60224         75371.9         81454.15         81454.15         98170.2         56621.4         67259.75         35698.6           0         0         0         0         0         0         0         0         0         0           1390         1384         1366         1498         1602         1602         1242         1188         1028         1026           27.3         26.6         28.5         30.6         29.1         29.1         27.6         27.         26.4         31.1           51         52         48         49         55         55         45         44         39         33	9 2998.75         120595.75         60224         75371.9         81454.15         81454.15         98170.2         56621.4         67259.75         35698.6           1 30         0 <t< td=""><td><math display="block"> \begin{vmatrix} 92998.75 &amp; 120595.75 &amp; 60224 &amp; 75371.9 &amp; 81454.15 &amp; 81454.15 &amp; 98170.2 &amp; 56621.4 &amp; 67259.75 &amp; 35698.6 \\ 0 &amp; 0 \\ 1390 &amp; 1384 &amp; 1366 &amp; 1498 &amp; 1602 &amp; 1602 &amp; 1242 &amp; 1188 &amp; 1028 &amp; 1026 \\ 27.3 &amp; 26.6 &amp; 28.5 &amp; 30.6 &amp; 29.1 &amp; 29.1 &amp; 27.6 &amp; 27 &amp; 26.4 &amp; 31.1 \\ 51 &amp; 52 &amp; 48 &amp; 49 &amp; 55 &amp; 55 &amp; 45 &amp; 44 &amp; 39 &amp; 33.1 \\ 39 &amp; 588 &amp; 14 &amp; 31 &amp; 35 &amp; 356 &amp; 4759 &amp; 4759 &amp; 4759 &amp; 4759 &amp; 4759 &amp; 5733 &amp; 3441 \\ \end{vmatrix} </math></td></t<>	$ \begin{vmatrix} 92998.75 & 120595.75 & 60224 & 75371.9 & 81454.15 & 81454.15 & 98170.2 & 56621.4 & 67259.75 & 35698.6 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1390 & 1384 & 1366 & 1498 & 1602 & 1602 & 1242 & 1188 & 1028 & 1026 \\ 27.3 & 26.6 & 28.5 & 30.6 & 29.1 & 29.1 & 27.6 & 27 & 26.4 & 31.1 \\ 51 & 52 & 48 & 49 & 55 & 55 & 45 & 44 & 39 & 33.1 \\ 39 & 588 & 14 & 31 & 35 & 356 & 4759 & 4759 & 4759 & 4759 & 4759 & 5733 & 3441 \\ \end{vmatrix} $

Recovery Costs $[\epsilon]$ 85847.7 81601.25 96777.55 29547.35 29532.35 84718.05 74152.25 $\#$ Canceled Flts 0 0 0 0 0 0 0 0 Total Delay $[\min]$ 1336 1303 1370 720 700 1287 1102 $A_{Vor}$ Delay $[\min]$ 97.3 97.7 30.4 97.7 99.9 98 96.0
0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
1336 1303 1370 720 700 1287 1102 273 277 304 277 292 28 26.9
97 304 977 308 98 980
0.10
1:00
1:07
1:00
5:11
Cress triting
0.11

Table 19: Recovery statistics for instance A06.

11-20000	654615.45	4	317	31.7	10	489	10305	374
11-10000	654615.45	4	317	31.7	10	489	10305	374
11_5000	510132.05	2	753	47.1	16	369	8965	284
11-2500	624182.6	2	878	41.8	21	437	10156	378
11-1000	616084.1	2	006	40.9	22	430	12598	427
Cross_20000	514637.6	2	1118	38.6	29	353	12549	438
Cross_10000	514637.6	2	1118	38.6	29	353	12549	438
Cross_5000	713479.05	4	743	32.3	23	501	13498	563
Cross_2500	567780.35	2	1060	37.9	28	393	14948	444
Ur Cross_1000	648540.15	2	945	39.4	24	451	12921	443
n C	632674.5	2	006	40.9	22	441	13608	445
Model	Recovery Costs [€]	# Canceled Flts	Total Delay [min]	Avg Delay [min]	# Delayed Flts	# Canceled Psg	Total Pax delay [min]	# Rerouted Psg

Model	MIT_1000	MIT_2500	MIT_5000	MIT_10000	MIT_20000	PCUN_1000	PCON_2500	PCON_5000	PCON_10000	PCON_20000
Recovery Costs [€]	608928.85	624172.2	872451.2	408797.65	418226.15	604811.9	602647.5	544054.75	535246	632674.5
# Canceled Flts	2	2	2		2	2	2	2	2	2
Total Delay [min]	006	850	839	629	579	879	209	543	447	006
Avg Delay [min]	40.9	44.7	44.2	41.2	38.6	40	31.9	30.2	37.3	40.9
# Delayed Flts	22	19	19	16	15	22	19	18	12	22
# Canceled Psg	424	436	398	296	305	422	426	388	383	441
Total Pax delay [min]	12756	9837	0666	11494	11284	13152	12302	11309	8123	13608
# Rerouted Psg	431	385	405	332	323	444	402	334	309	445

Table 20: Recovery statistics for instance A07.

IT_20000	1203636.35	∞	546	27.3	20	894	15158	664
	1203636.35						15158	
IT_5000	1243736.25	∞	682	31	22	885	14830	752
IT_2500	1260995.35	∞					17135	
$\mathrm{IT}1000$	1363939	∞					18766	
Cross_20000	1232016.15	~	1089	33	33	864	17524	898
	1232016.15	∞	1089	33	33	864	17524	898
Cross_5000	1266517.5	∞	915	30.5	30	913	18228	998
Cross_2500	1349184.1	∞	981	31.6	31	955	16938	805
Cross_1000	1374174.1 1406386.5 1349184.1	∞	982	29.8	33	226	19278	817
0r	1374174.1	∞	939	29.3	32	962	19828	835
Model	Recovery Costs [€]	# Canceled Flts	Total Delay [min]	Avg Delay [min]	# Delayed Flts	# Canceled Psg	Total Pax delay [min]	# Rerouted Psg

Model	MIT_1000 MIT_2500	MIT_2500	MIT_5000	MIT_10000	MIT_20000	PCON_1000		PCON_5000	PCON_10000	PCON_20000
Recovery Costs [€]	1268172.4	1269514.1	1130037.45	941794.75	96305.6	1303642.85	1315030.15	1215338.05	1167150.95	1374174.1
# Canceled Flts	∞	∞	∞	∞	œ	œ		∞	∞	∞
Total Delay [min]	922	810	714	357	350	841	816	789	740	939
Avg Delay [min]	28.8	27	29.8	22.3	21.9	31.1	31.4	34.3	33.6	29.3
# Delayed Flts	32	30	24	16	16	27	26	23	22	32
# Canceled Psg	880	884	826	892	787	971	982	938	923	962
Total Pax delay [min]	18031	18405	17896	14989	14999	16608	17071	16923	14853	19828
# Rerouted Psg	853	849	814	725	902	719	691	652	646	835

Table 21: Recovery statistics for instance A08.

11-20000	1005869.1	12	7317	62.9	111	622	22390	1188
11-10000	1005869.1	12	7317	62.9	111	779	22390	1188
11_5000	1102431.5	12	7544	59.9	126	838	24650	1187
11_2500	1632488.5	16	6802	57.6	123	1287	26910	1341
11-1000	1847358.7	18	6193	51.6	120	1472	30787	1212
Cross_20000	1795185.35	18	6401	54.7	117	1294	23256	1456
Cross_10000	1795185.35	18	6401	54.7	117	1294	23256	1456
Cross_5000	1625465.7	18	5572	45.2	118	1154	24379	1386
Cross_2500	2144286.9	20	6042	47.6	127	1579	30147	1340
Cross_1000   Cross_2500	1554966	14	8099	55.1	147	1163	26819	1280
r O	1869636.1	18	8299	53.3	125	1487	30119	1255
Model	Recovery Costs [€]	# Canceled Flts	Total Delay [min]	Avg Delay [min]	# Delayed Flts	# Canceled Psg	Total Pax delay [min]	# Rerouted Psg

Model	MIT_1000 MIT_	MIT_2500	MIT_5000	MIT_10000	MIT_20000	PCDN_1000	PCON_2500		PCON_10000	PCON_20000
Recovery Costs [€]	1317424.45 1198856.8	1198856.8	1282413.95	560891.3	603669.3	1671449.9	2002377.65	1665945.2	550323.9	1869636.1
# Canceled Flts	14	12	14	∞	∞	18	20		9	18
Total Delay [min]	7594	7772	9819	6853	6755	7278	6216	6586	6915	6658
Avg Delay [min]	53.9	56.3	54.1	50.4	52.8	55.1	55.5		57.6	53.3
# Delayed Flts	141	138	126	136	128	132	112		120	125
# Canceled Psg	1016	925	1014	431	452	1366	1603		402	1487
Total Pax delay [min]	26550	23817	25143	17780	16005	31365	31153	.,	17355	30119
# Rerouted Psg	1342	1238	1152	939	1027	1406	1302		559	1255

Table 22: Recovery statistics for instance A09.