

## A STUDY OF THE GROUND STATE OF ACCEPTORS IN SILICON FROM THERMAL TRANSPORT EXPERIMENTS

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**ABSTRACT** - Thermal conductivity measurements of silicon crystals doped with B or In have shown the presence of several phonon scattering processes. The resonant effect observed below 1 K is ascribed to the existence of a distribution of splittings  $N(\delta)$  of the  $\Gamma_8$  ground state of the acceptor, which could be related to the presence of oxygen and carbon impurities. In two cases, the maximum of  $N(\delta)$  occurs for  $\delta_{\max}$  near 6 GHz, in agreement with previous ultrasonic studies ( $\delta_{\max} > 4$  GHz).

**Samples and Experiments** - The thermal conductivity of four Si single crystals doped with B or In has been measured from 50 mK to 200 K. Three crystals have been studied by ultrasonic absorption in Stuttgart and some of these results have been already published [1]. The characteristics of the samples are given in table 1.

TABLE 1

Sample	S 80 g	S 87 d	S 52	S 33 *
Dimensions (mm×mm×mm)	2.6 × 3.0 × 35	3.0 × 3.0 × 34	2.3 × 3.0 × 14	0.85 × 3.03 × 11
Acceptor	B	B	In	In
$\rho$ ( $\Omega$ cm)	10.8	2.5	0.1	2
$N_A$ ( $\text{cm}^{-3}$ )	$1.2 \cdot 10^{15}$	$5.4 \cdot 10^{15}$	$5 \cdot 10^{17}$	$5 \cdot 10^{15}$
$n_D$ ( $\text{cm}^{-3}$ )	$5.7 \cdot 10^{17}$	$\leq 2 \cdot 10^{15}$	$8 \cdot 10^{17}$	$7 \cdot 10^{17}$
$n_C$ ( $\text{cm}^{-3}$ )	$4.1 \cdot 10^{16}$	$\leq 5 \cdot 10^{15}$	?	?
Growth method	Cz	Fl. zone	Cz	-
$\delta_{\max}$ (GHz) (from ultrasonics)	$\geq 4$	1.3	$> 4$	-

\* This sample has been measured previously above 1.2 K [2]

**Results and qualitative discussion** - The experimental results are displayed in fig.1 in a log-log plot and show that three temperature ranges can be considered.

(i)  $T < 2$  K Resonant phonon scattering is present in the three samples measured in this temperature range. We ascribe this scattering to a direct process between the two energy levels arising from the  $\Gamma_8$  acceptor ground state, the splitting being variable from site to site due to random strains and electric fields. The distri-

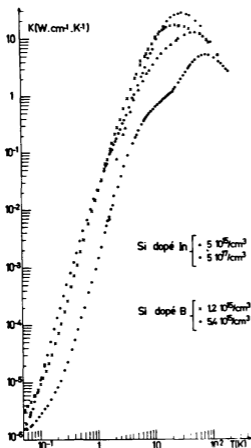


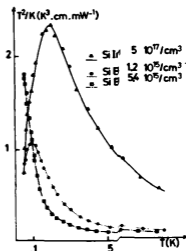
Figure 1.

butions  $N(\delta)$  have been studied at frequencies less than 4 GHz by ultrasonic attenuation and related to the presence of carbon or oxygen impurities in the crystals [1]. The phonon relaxation rate due to this process is given approximatively by :

$$\tau^{-1}(\omega) = \pi \bar{D}^2 \omega N(\delta=\omega) / M \rho v^2 \quad (1)$$

where  $\bar{D}$  is a mean value of the coupling constant, and the qualitative shape of  $N(\delta)$  is given by the function  $T^2/K$  [3]. In fig. 2,  $T^2/K$  is plotted as a function of  $T$  for the three samples studied. A maximum is observed near 0.19 K in the case of Si : In ( $5.10^{17}/\text{cm}^3$ ) and 0.09 K in the case of Si : B ( $1.2 \cdot 10^{15}/\text{cm}^3$ ), which would correspond very crudely to frequencies  $\delta_{\text{max}}$  of 15 and 7 GHz respectively. In the case of Si : B ( $5.10^{15}/\text{cm}^3$ ) the maximum is not reached at the lowest temperatures, so that  $\delta_{\text{max}}$  must be less than 4 GHz. These results are in very good qualitative agreement with those obtained by ultrasonic measurements and given in table 1.

(ii) 2 < T < 30 K A very clear dip appears near 20 K in the case of the In-doped samples, which has been already observed and attributed to an excited Jahn-Teller level of the acceptor near  $40 \text{ cm}^{-1}$  [2]. A small effect could be present near 3 K in the more highly doped Si : B sample so that the ratio of the transition energies for

Figure 2. Solid lines are not calculated

the two systems would be about 5, a value noticeably larger than previously supposed [4].

(iii)  $T > 30$  K The dip near 40 K present in the lightly doped Si : B crystal and not in the highly doped one is attributed to the presence of isolated oxygen interstitials ; the two crystals contain different amount of oxygen (see table 1) and in fact, the two curves cross near 20 K. This resonant scattering observed near 40 K is also probably present in the In-doped samples and could be related to a transition near  $80 \text{ cm}^{-1}$ , in reasonable agreement with the energy level scheme of oxygen deduced from FIR absorption measurements [5].

Quantitative analysis - A preliminary analysis of the results in the temperature range  $T < 1$  K for the two samples containing oxygen and carbon has been carried out within the Debye approximation. Only boundary scattering ( $\tau_B^{-1} = \text{constant}$ ) and scattering by the acceptors as described by equation (1) have been considered. We have used an expression of  $N(\delta)$  which gives a satisfactory description of the distribution obtained by a Monte-Carlo calculation for point defects such as carbon [1]. The general features of the experimental  $T^2/K$  curves (fig.2) can be described by such an analysis and, with the parameters given in table 2, the position and intensity of the maximum are well reproduced, but not the detailed shape of the curves. The values of  $\delta_{\text{max}}$  obtained from these fits are similar in the two crystals, in contrast with the crude estimations from the position of the pics given above.

TABLE 2

Sample	$\delta_{\text{max}}$ (GHz)	$N_A \bar{D}^2 (\text{erg}^2 \text{ cm}^{-3})$	$N_A (\text{cm}^{-3})$	$\bar{D}$ (eV)
Si : B (S 80 g)	$6.2 \pm 0.4$	$6.5 \cdot 10^{-9}$	$1.2 \cdot 10^{15}$	1.5
Si : In (S 52)	$5.6 \pm 0.4$	$5.1 \cdot 10^{-7}$	$5.10^{17}$	0.63

This analysis also gives values of  $N_A \bar{D}^2$  and, supposing that all the acceptors contribute to the scattering, we obtain the values of  $\bar{D}$  given in table 2, which are not unreasonable. Full details will be published elsewhere.

#### References

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