



27 **1. Introduction**

28 The activated sludge (AS) process is the most common system for biological treatment  
29 of municipal and industrial wastewater (Wei et al., 2003; Kamali and Khodaparast,  
30 2015). The main disadvantage of the AS process is the low settling of sludge, also  
31 known as “bulking” (Rankin et al., 2007), and the large amount of activated sludge  
32 produced. Wastewater pre-treatment with biofilm formation systems is an alternative  
33 that minimizes these weaknesses. Biofilm activated sludge (BAS) is composed of two  
34 aerobic stages: a moving bed biofilm reactor (MBBR) as pre-treatment, followed by an  
35 AS reactor. The MBBR is a continuously operating biofilm reactor using small carriers,  
36 to which microorganisms attach (Borkar et al., 2013). In aerobic processes, biofilm  
37 carriers are moved by blowers. Agitation generates collision between carriers, favouring  
38 detachment of biomass and resulting in better diffusion of the components in the layers  
39 of the biofilm.

40 The performance of biological wastewater treatment plants (WWTPs) is closely  
41 associated with the structure and functions of microbes. One of the unique  
42 characteristics of the BAS process is that microorganism populations in the two stages  
43 are different (Sointio et al., 2006). The biofilm stage generates a substantial amount of  
44 dispersed (non-floc-forming) bacteria, and the activated sludge stage, in turn, promotes  
45 the growth of microorganisms that contain a large amount of higher life forms (predator  
46 microorganisms) that live largely on dispersed bacteria.

47 Predation is not relevant for conventional AS process but becomes very significant in  
48 the second stage of the BAS process (Malmqvist et al., 2008). For conventional AS  
49 processes, the concentration of predator microorganisms is approximately 5%-10% of  
50 the total suspension solids (TSS) (Hauduc et al., 2013). Predator microorganisms are at

51 the top of the food chain in the ecological system of the AS stage, and their  
52 concentration depends on the sludge retention time (SRT) (Hao et al., 2010), food  
53 sources (Sointio et al., 2006) and wastewater composition. Due to predation on fast-  
54 growing MBBR bacteria in the AS system, excess sludge production will typically be  
55 30%-50% lower than that of a conventional AS process (Malmqvist et al., 2008).

56 Nutrient control in MBBR is also very relevant for the BAS process (van Haandel and  
57 van der Lubbe, 2015) because nutrients taken up by bacteria in the biofilm stage are  
58 released when the bacteria are consumed by predator microorganisms in the AS stage  
59 (Slade et al., 2004). Therefore, BAS processes can operate under nutrient limitation  
60 conditions (Rankin et al., 2007; Malmqvist et al., 2008). The BAS process is widely  
61 used in wastewater from the pulp and paper industry because this type of wastewater is  
62 typically characterized by low nutrient and high COD concentrations (Slade et al., 2004;  
63 Elsergany et al., 2015). The addition of nutrients has an important impact on the  
64 operational costs of this type of plant.

65 In a previous study, the authors presented a mathematical model of MBBR reactors  
66 (Revilla et al., 2016). This MBBR model confirmed the presence of predator  
67 microorganisms in the biofilm and in the bulk liquid under various inlet conditions and  
68 the dominance of heterotrophic microorganism in the outlet of MBBR reactors.

69 The success of current activated sludge models does not require the inclusion of  
70 predation, since this process is not relevant in a conventional activated sludge reactor  
71 (Henze et al., 2000). Moussa et al. (2005) and, later, Hao et al. (2011) present a model  
72 to describe a mixed culture in which nitrifiers, heterotrophs and predators (protozoa and  
73 metazoa) coexist. This predation process simplifies the complex reality of the predator-  
74 prey relationship, pooling all types of predators and assuming that the predation process

75 is a function of bacterial concentration. However, in the BAS process, the existence of  
76 heterotrophs and predators in the inlet of the AS reactor must also be considered in any  
77 model.

78 Many current papers use mathematical models to simulate a conventional AS process,  
79 but no literature report uses a mathematical model for a BAS process that integrates the  
80 MBBR and AS stages. Lindblom developed a mathematical model for the AS reactor of  
81 a BAS process without modelling the MBBR stage (Lindblom, 2003); in this model,  
82 heterotrophic microorganisms generated in the biofilm stage and entering the AS stage  
83 are slowly biodegradable compounds, and therefore, heterotrophic microorganisms are  
84 not the main food source in the AS. This is a major difference from the present study.

85 This paper proposes and validates a novel unified model for the two steps of the BAS  
86 process: an MBBR bacterial-predator stage and an AS predator stage where the food  
87 source is mainly bacteria from the MBBR and a low concentrations of readily  
88 biodegradable COD. The novelty of the model is that it considers a BAS process in  
89 which nitrifiers, heterotrophs and predators coexist, with a different microorganism  
90 distribution in the biological reactors of each stage. The removal of COD, nutrient  
91 requirements, sludge production and microbial distribution is analysed using the  
92 proposed model as applied to a full-scale wastewater treatment plant.

## 93 **2. Unified mathematical model for BAS process**

94 The mathematical model considers the fate of both soluble ( $S_i$ ) and particulate ( $X_i$ )  
95 compounds as described in the nomenclature section. The model is structured with 13  
96 model components or state variables (Ni et al., 2011) and is segregated as follows  
97 because three types of microorganisms are considered (Gernaey et al., 2010): i) seven  
98 soluble compounds, namely, dissolved oxygen ( $S_{O_2}$ ), readily biodegradable compounds

99 ( $S_F$ ), fermentation products ( $S_A$ ), phosphorous ( $S_{PO4}$ ), ammonium ( $S_{NH4}$ ), nitrate ( $S_{NO3}$ )  
 100 and organic nitrogen ( $S_{ND}$ ); ii) three microorganism groups, namely, heterotrophic  
 101 bacteria ( $X_H$ ), autotrophic bacteria ( $X_A$ ) and predators ( $X_{predators}$ ); and iii) two types of  
 102 slowly biodegradable compounds:  $X_S$  from inactivation of the microorganism groups  
 103 and  $X_{cellulose}$  since the model will be used for wastewater from the pulp and viscose  
 104 industry and iv) inert matter ( $X_I$ ) from inactivation of the microorganism groups.  
 105 Microorganisms grow under aerobic conditions in the BAS process for this study, but  
 106 anoxic and anaerobic conditions for the MBBR reactor biofilm have also been  
 107 considered (Table 1 and Table 2; Revilla et al., 2016).

108 The conversion of COD and total suspension solids (TSS) has been evaluated assuming  
 109 stoichiometric conversion parameters of 0.75 and 0.90 gTSS/g COD as in previous  
 110 studies (Revilla et al., 2016; Henze et al., 2000; Boltz et al., 2011; Tamis et al., 2011).  
 111 The TSS, filtered COD ( $COD_f$ ) and total nitrogen (TN) parameters are not introduced as  
 112 variables but are computed from state variables using equations 1, 2 and 3 (Revilla et  
 113 al., 2016):

$$114 \quad TSS = (0.75 X_I + 0.75 X_S + 0.90 X_H + 0.90 X_{Aut} + 0.90 X_{predators}) + X_{cellulose} \quad (1)$$

$$115 \quad COD_f = S_F + S_A + S_I \quad (2)$$

$$116 \quad TN = S_{NO3} + S_{NH4} + S_{ND} \quad (3)$$

### 117 *2.1. Biological conversion processes*

118 The structure of the biological process uses a matrix format that constitutes the model  
 119 backbone (Revilla et al., 2016). The stoichiometric coefficients are incorporated into  
 120 appropriate cells of the matrix and the rate of conversion for a given compound I ( $r_i$ ) is  
 121 obtained by multiplication of the related process stoichiometry ( $v_{ij}$ ) and kinetics ( $P_j$ )  
 122 (Ni et al., 2011) as shown in equation 4:

$$r_i = \sum_{j=1}^n P_j v_{i,j} \quad (4)$$

124 The predation mechanism can appear in the MBBR reactors when the soluble COD  
 125 loading rate (SCLR) is moderate (10-15 g COD/m<sup>2</sup><sub>carrier area</sub> day), a biofilm with  
 126 predators is promoted and consequently a bacterial-predator stage is considered.  
 127 However, when SCLR is high (>30 g COD/m<sup>2</sup><sub>carrier area</sub> day) a bacterial-stage is  
 128 considered since predator are absent (Ødegaard, 1999; van Haandel and van Lubbe,  
 129 2015). In the AS reactor of a BAS process, predators are the dominant microorganisms  
 130 acting as a predator-stage (Sointio et al., 2006).

131 The predation mechanism used in this work assumes a single type of predator  
 132 ( $X_{\text{predators}}$ ). This assumption can be justified by the lack of information on predation  
 133 rates by biomass type (Ni et al., 2009). As proposed by Moussa (Moussa et al., 2005),  
 134 the model considers that predators grow aerobically (consume  $S_{O_2}$ ) on the degradable  
 135 fraction of the two types of available bacteria, heterotrophic microorganisms ( $X_H$ ) and  
 136 autotrophic microorganisms ( $X_{\text{Aut}}$ ) and that the predation rate is a function of bacterial  
 137 concentration. When  $X_H$  and  $X_{\text{Aut}}$  are consumed by predators, large amounts of  
 138 nutrients ( $S_{PO_4}$  and  $S_{NH_4}$ ) (Lindblom, 2003) are regenerated and available to other  
 139 microorganisms (Revilla et al., 2016). Moreover, when predators graze on  $X_H$  and  $X_A$ ,  
 140 they convert the non-biodegradable fraction of  $X_H$  into inert biomass ( $X_I$ ) (Table 1).  
 141 Figure 1 shows a general scheme of the reactions for the predation mechanism, where  
 142 the transformation of compounds as consumed by predators is described.

143 A complete description of the stoichiometric matrix and process rate equations used to  
 144 model the MBBR and AS reactors of the BAS is described in Table 1 and 2.

## 145 2.2. MBBR model

146 The MBBR model is constituted by the biofilm model and bulk liquid model. The  
 147 biofilm model is based on the general one-dimensional mathematical mixed-culture  
 148 biofilm (MCB) model described in Wanner and Gujer (1986), which assumes that  
 149 changes in particulate and soluble compounds occur in the direction perpendicular to the  
 150 wall of the carrier.

151 The mass balance for particulate compounds by volume fraction ( $f_i(t, z)$ ) and for soluble  
 152 components ( $S_i^f$ ) in the biofilm are given by equations 5 and 6. The mass balance in the  
 153 bulk liquid is given by equations 7 and 8.

$$154 \quad \frac{df_i(t,z)}{dt} = [U_{o_i}(t, z) - \bar{U}_o(t, z)]f_i(t, z) - U(t, z) \frac{df_i(t,z)}{dz}; \quad i=S, H, Aut, I, \text{ predators} \quad (5)$$

$$155 \quad \frac{dS_i^f(t,z)}{dt} = D_i^f \frac{d^2 S_i^f(t,z)}{dz^2} + r_i(t, z); \quad i=F, A, NH_4, PO_4, NO_3, O_2, ND \quad (6)$$

$$156 \quad V_{MBBR} \frac{dS_i^b(t)}{dt} = Q^{in}(S_i^{in} - S_i^b) - J_i(t, z) AF + r_i(t) V_{MBBR}; \quad i=F, A, NH_4, PO_4, NO_3, ND \quad (7)$$

$$157 \quad V_{MBBR} \frac{dX_i^b(t)}{dt} = Q^{in}(X_i^{in} - X_i) + \lambda L(t)^2 AF \rho + r_i(t) V_{MBBR}; \quad i= S, H, Aut, I, \text{ predators} \quad (8)$$

158

159 A precise description of the equations appears in previous studies (Wanner and Gujer,  
 160 1986; Revilla et al., 2016).

### 161 2.3. AS process model

162 The aeration tank of the AS process is modelled as a continuous stirred-tank reactor  
 163 (CSTR) and the generic equations 9 and 10 describe the mass balance.

$$164 \quad V_{AS} \frac{dS_i(t)}{dt} = Q(S_i^{in} - S_i^b) + r_i(t) V_{AS}; \quad i=F, A, NH_4, PO_4, NO_3, O_2, ND. \quad (9)$$

$$165 \quad V_{AS} \frac{dX_i(t)}{dt} = Q(X_i^{in} - X_i^b) + r_i(t) V_{AS}; \quad i=S, H, Aut, I, \text{ cellulose, predators.} \quad (10)$$

166 The conversion rates  $r_i$  of the MBBR and AS models are obtained by summing the  
 167 product of the stoichiometric coefficients and the process rate expression, as obtained in  
 168 a previous study (Revilla et al., 2016).

169 *2.4. Secondary clarifier model*

170 The most widely used model for secondary clarifiers is the one-dimensional model  
171 proposed by Takács et al., 1991, known as double-exponential settling velocity, which  
172 can predict TSS concentrations in the effluent of BAS. This model assumes a non-  
173 reactive (no biological reactions) secondary clarifier, and therefore, the concentration of  
174 soluble compounds is the same in the effluent of the BAS process and the outlet stream  
175 of the AS reactor (Hreiz et al., 2015).

176 The general equation is as follows

$$177 \quad v_{s,j}(\text{TSS}) = \max \left\{ 0, \min \left\{ v'_0, v_0 \left( \exp^{r_h(\text{TSS}_j - f_{ns}\text{TSS}_{AS})} - \exp^{r_n(\text{TSS}_j - f_{ns}\text{TSS}_{AS})} \right) \right\} \right\} \quad (11)$$

178 *2.5. Calibration and validation of the unified model*

179 The proposed dynamic model was developed using Aspen Custom Modeler (ACM)  
180 software, which solves rigorous models using a specific language that customizes the  
181 models for the processes under study. The method of lines (MOL) was used to solve the  
182 system of equations, and BFD1 was the discretization method. The adjustment of  
183 parameters was done by NL2SOL algorithm for least-squares minimization of the  
184 deviation between experimental and theoretical values.

185 The BAS process for the treatment of wastewater from the cellulose and viscose  
186 industry is designed under nutrient-limitation conditions (Malmqvist et al., 2008). This  
187 enables the use of a simple strategy for calibration of models, where the biological  
188 degradation of organic matter under nutrient limitation dominates (Revilla et al., 2016).  
189 The nitrogen and phosphorus parameters  $i_{N,BM}$  and  $i_{P,BM}$  (nitrogen and phosphorous  
190 content of biomass), and  $i_{N,XI}$  and  $i_{P,XI}$  (nitrogen and phosphorous content of inert  
191 matter) were adjusted at steady state with average experimental values for each case.



192 Validation of the model was carried out using the calibrated input model parameters  
193 generated from a set of experimental values (Hao et al., 2011). The experimental data  
194 were measured every 7 days (Figure 3 and 4) during the operational time in each case  
195 study and standard deviations (SD) between the experimental and simulated  
196 concentrations were used to validate of the model.

### 197 **3. Materials and methods**

#### 198 *3.1. Set-up of the full-scale BAS plant*

199 The full-scale BAS plant design is shown in Figure 2. The plant consists of a fine grid  
200 of 6 mm to eliminate larger solids, followed by a 1,600-m<sup>3</sup> equalization tank used to i)  
201 adjust the inlet flow peaks, ii) dose the nitrogen as urea (40% w/w) and phosphorous as  
202 phosphoric acid (72%), and iii) adjust pH to 7-8 with NaOH to neutralize acid effluent.  
203 After the equalization tank, there are two MBBR reactors in-series (biofilm stage),  
204 referred to as MBBR<sub>1</sub> and MBBR<sub>2</sub>. The 5,331-m<sup>3</sup> MBBR reactors were filled with  
205 BiofilmChip P carriers from AnoxKaldnes™ to 10% of the total volume. The carriers  
206 have an effective specific surface area of 900 m<sup>2</sup>/m<sup>3</sup> and are 45 mm in diameter and 3  
207 mm in length. The carriers move freely due to agitation generated by a blower (airflow  
208 31,600 Nm<sup>3</sup>/h).

209 Later, a 47,000-m<sup>3</sup> AS reactor with two blowers (air flow 31,600 Nm<sup>3</sup>/h) was included  
210 in the process. It was necessary to recycle sludge from secondary clarifiers to the AS  
211 reactor in order to maintain a high biomass concentration. Finally, two parallel  
212 secondary clarifiers with a unit volume of 4,143 m<sup>3</sup> were used.

#### 213 *3.2. Stream characterization and operational conditions*

214 The sampling method was removal of 24-h mixed samples for the influent of BAS,  
215 outlet stream of AS and effluent of BAS. However for the outlet streams of MBBR<sub>1</sub> and  
216 MBBR<sub>2</sub>, grab samples were collected *in situ* during operation.

217 The full-scale BAS process ran continuously for six months with two types of influent:  
218 a wastewater mixture from a cellulose and viscose fibre plant (case study A) for 64 days  
219 and wastewater from a cellulose plant (case study B) for 121 days following the plant  
220 schedule. Each case study had different operational conditions including nutrient  
221 dosage, hydraulic retention time (HRT) and sludge retention time (SRT). The  
222 operational conditions for both case studies are illustrated in Table 3. It is observed that  
223 HRT and SRT are much lower in MBBR reactors than in the AS reactor.

### 224 3.3. Analytical methods

225 Characterization of the streams was based on the measurement of COD<sub>f</sub>, nitrogen forms  
226 (S<sub>NO3</sub>, S<sub>NH4</sub> and TN), S<sub>PO4</sub> and TSS. The soluble and particulate compounds were  
227 differentiated by filtration through 1.20-µm filters (Henze et al., 2000) prior to analyses.  
228 Analysis of the soluble compounds (nitrogen forms, S<sub>PO4</sub> and COD<sub>f</sub>) was performed  
229 using Dr. Lange cuvette tests (LCK138, LCK305, LCK339, LCK348, LCK514 and  
230 LCK014), and TSS was determined according to standard methods (APHA, 1998).

231 A Leitz Wetzlar ORTHOLUX 2 POL microscope was used to observe biomass in the  
232 MBBR and AS reactor.

## 233 4. Results and discussion

### 234 4.1. Experimental values and simulation results for the full-scale BAS plant

235 The experimental concentrations of soluble compounds (COD<sub>f</sub>, S<sub>PO4</sub>, TN, S<sub>NO3</sub> and  
236 S<sub>NH4</sub>) and particulate compounds (TSS) in the influent and outlet stream of AS and

237 effluent of the BAS process during the operational time (185 days) are shown in Figures  
238 3 and 4. Variability in the concentrations of the influent of BAS at full scale was related  
239 to upstream processes and driven by cellulose and viscose production. Reference values  
240 were used to maintain the confidentiality of the information (c, p, n and s as observed in  
241 Figure 3 and 4).

242 Figure 3 shows the experimental  $COD_f$  concentrations in the influent and effluent, and  
243 Table 3 details the average quantity of  $COD_f$  removed in each biological reactor  
244 comprising the BAS process. Figure 3 shows the adequate and stable evolution of  $COD_f$   
245 in the effluent of the BAS process over all operational time for both case studies, and  
246 Table 3 shows that the overall removal of  $COD_f$ : in case study A is 76%. Removal in  
247 case study B is higher (85%) because the inert fraction of  $COD_f$  in the influent ( $S_I$ ) is  
248 lower (15%) in case study B than in case study A (25%) (Revilla et al., 2016). It is also  
249 observed in Table 3 that  $COD_f$  is mainly eliminated in the  $MBBR_1$ , which, followed by  
250 the AS reactor and  $MBBR_2$ , is the reactor with the lowest amount removed. Similar  
251 results were obtained in previous studies (Rankin et al., 2007; Sointio et al., 2006) in a  
252 BAS process for pulp mill wastewater.

253 Figure 3 shows the experimental phosphorus ( $S_{PO4}$ ) and nitrogen ( $S_{NO3}$ ,  $S_{NH4}$  and TN)  
254 concentrations in the influent and effluent of the BAS process; it is observed that the  
255 concentrations of  $S_{PO4}$  in the effluent are approximately 75% of the influent  
256 concentration in both case studies. These concentrations are higher than expected for a  
257 conventional AS process (Malmqvist et al., 2008).

258 The TN in the influent of the BAS process is mainly composed of organic nitrogen  
259 ( $S_{ND}$ ) from urea (Figure 3) that is rapidly hydrolysed by heterotrophic microorganisms  
260 (Henze et al., 2000) in the  $MBBR$  reactors to ammonia nitrogen ( $S_{NH4}$ ). Excess  $S_{NH4}$  is

261 oxidized to nitrate nitrogen ( $S_{NO_3}$ ) by autotrophic microorganisms ( $X_{Aut}$ ) (Mozumder et  
262 al., 2014) in the AS reactor. Consequently, TN in the effluent is mainly composed of  
263  $S_{NO_3}$ .

264 The experimental concentrations of TSS in the influent, the outlet stream of the AS  
265 reactor and the effluent are shown in Figure 4. TSS in the influent is composed mainly  
266 of cellulose fibres ( $X_{cellulose}$ ) that will be hydrolysed in the AS reactor by heterotrophic  
267 microorganisms (Ruiken et al., 2013). As expected, the TSS in the outlet stream of AS  
268 reactor increased 10-fold due to the growth of microorganisms. Moreover, Figure 4 also  
269 shows the removal of TSS from the AS reactor in the secondary clarifiers: 98.5% in  
270 case study A and 98.7% in case study B.

271 The simulated concentrations of  $COD_f$ , TSS, TN,  $S_{PO_4}$ ,  $S_{NO_3}$  and  $S_{NH_4}$  in the outlet  
272 stream of the AS reactor and the effluent of BAS are show in Figures 3 and 4 as  
273 continuous and dotted lines. Good agreement is observed between experimental and  
274 simulated concentrations, as confirmed by the small standard deviations (SD) shown in  
275 Table 4. For the two case studies, the values of SD for all compounds are lower than  
276 14%; these low SD values validate the unified proposed model under operational  
277 conditions.

#### 278 *4.2. Microorganism distribution in BAS reactors*

279 A mathematical model is used to evaluate the microbial distribution profile (Moussa et  
280 al., 2005; Hao et al., 2011) in the bulk liquid of reactors involved in the BAS process.

281 Figure 5 shows the percentage of heterotrophic microorganisms, inert matter and  
282 suspended biodegradable compounds from inactivation, cellulose fibres, predators and  
283 autotrophic microorganisms in the bulk liquid of the MBBR<sub>1</sub>, MBBR<sub>2</sub> and AS ( $X_H$ ,  $X_I$ ,  
284  $X_S$ ,  $X_{cellulose}$ ,  $X_{predator}$  and  $X_{Aut}$ ) for both case studies at steady state. The mathematical

285 model details the microorganism populations in the two stages (biofilm and AS); the  
286 major particulate compounds in the MBBR<sub>1</sub> and MBBR<sub>2</sub> reactors are heterotrophic  
287 microorganisms, and in the AS reactor, they are inert matter and predator  
288 microorganisms (Figure 5). This is expected because MBBR reactors (short HRT)  
289 remove the most COD<sub>f</sub>, such that the growth of heterotrophic microorganisms is the  
290 main biological process. However, HRT in the AS reactor is approximately 10 times  
291 higher than that in MBBR reactors (Table 3), and predation and inactivation processes  
292 are the main biological processes at this AS stage. The difference in microorganism  
293 populations at each stage is one of the main characteristics of the BAS process (Wei et  
294 al., 2003). Other differences among the fractions of particulate compounds in each  
295 reactor of the BAS process and their causes were analysed:

296 i) The heterotrophic microorganisms ( $X_H$ ) in the MBBR reactors are 50% of TSS  
297 in case study A and 60-70% in case study B (Figure 5), removing 23.6 COD<sub>f</sub> ton/day  
298 in the two MBBR reactors in case study A and 24.1 COD<sub>f</sub> ton/day in case study B  
299 (Table 3). However, at the AS stage, fewer tons of COD<sub>f</sub> are removed for both case  
300 studies (11.8 and 4.2 ton/day for case study A and B, respectively), and the percentage  
301 of heterotrophic microorganisms is low (5-10%). The main food source at the AS  
302 stage is what is left over from MBBR reactors, mainly heterotrophic microorganisms  
303 instead of COD<sub>f</sub>.

304 ii) Predator microorganisms are absent in the MBBR<sub>1</sub> for both case studies since  
305 the soluble COD loading rate (SCLR) is high in the MBBR<sub>1</sub> (Ødegaard, 1999). In the  
306 MBBR<sub>2</sub>, predator microorganisms are also absent in case study A, but represent  
307 13.2% of the TSS for case study B (Figure 5) due to an SCLR value below 15 g  
308 COD/m<sup>2</sup> day (Revilla et al., 2016). In the AS reactor, the predator microorganisms and  
309 the inert material are the main particulate compounds in the TSS:  $X_{predators}$  is 32% in

310 case study A and 26% of total TSS in case study B, and inert matter ( $X_I$ ) is 57% in  
311 case study A and 69% in case study B. This high percentage of inert matter is  
312 explained because the predator microorganisms graze on active bacteria and convert  
313 the non-biodegradable fraction of  $X_H$  into inert biomass (Moussa et al., 2005). The  
314 presence of predator microorganisms such as ciliates (Wei et al., 2003) was observed  
315 microscopically in the AS reactor.

316 As the quantity of COD that reaches the AS reactor is small,  $X_H$  is under starvation  
317 conditions and  $COD_f$  is removed rapidly by  $X_H$ . In general, the longer the starvation  
318 period is, the greater is the extent of inactivation and, as a consequence, the higher is  
319 the inert fraction at AS (Ni et al., 2011). In addition, predation on  $X_H$  and  $X_{Aut}$   
320 generates high amounts of  $X_I$  (Moussa et al., 2005; Ni et al., 2009, 2011; Hao et al.,  
321 2011). As a consequence, the inert fraction ( $X_I$ ) is the main particulate compound in  
322 AS reactor.

323 iii) Slowly biodegradable compounds ( $X_{cellulose}$  and  $X_S$ ) must be hydrolysed to  $S_F$  by  
324  $X_H$  and then used by  $X_H$  as a food source. Biological hydrolysis of cellulose fibres  
325 ( $X_{cellulose}$ ) strongly depends on SRT (Ruiken et al., 2013). Therefore, in this work, it is  
326 assumed that hydrolysis of  $X_{cellulose}$  only occurs in the AS reactor (Table 3), where the  
327 SRT is high enough to break up cellulose fibres (average values of 19 and 30 days for  
328 case study A and B, respectively). Most  $X_{cellulose}$  in the AS reactor is hydrolysed, but  
329 for each case study, a small fraction (0.05%) remains.

330 In contrast to  $X_{cellulose}$ ,  $X_S$  can be hydrolysed by suspended bacteria in the MBBR  
331 reactors depending on SCLR (Helness and Ødegaard, 2005). In case study B,  $X_S$   
332 decreases slightly at MBBR<sub>2</sub> because SCLR is lower than 20 g COD/m<sup>2</sup>day, and  
333 hydrolysis is not neglected; however, in case study A,  $X_S$  increases at MBBR<sub>2</sub> due to

334 an SCLR higher than 20 g COD/m<sup>2</sup>day (Revilla et al., 2016). As a consequence, the  
335 fraction of  $X_S$  and  $X_{\text{cellulose}}$  is higher in the MBBR than in the AS reactor (Figure 5).

336 iv) The presence of  $X_{\text{Aut}}$  is fixed by the inlet  $\text{COD}_f/\text{S}_{\text{NH}_4}$  ratio of the biological  
337 reactor (Mozumder et al., 2014). Figure 5 shows that the MBBR reactors do not  
338 contain autotrophic microorganisms in case studies A and B. However, in the AS  
339 reactor, a small fraction of  $X_{\text{Aut}}$  is observed—0.5% in case study A and 0.2% in case  
340 study B—because of the low  $\text{COD}_f/\text{S}_{\text{NH}_4}$  inlet ratio of the AS reactor. For high  
341  $\text{COD}_f/\text{S}_{\text{NH}_4}$  ratios, the growth rate of  $X_H$  is high enough (Lee and Park, 2007), and  
342  $X_{\text{Aut}}$  does not coexist with  $X_H$ ; conversely, for low  $\text{COD}_f/\text{S}_{\text{NH}_4}$  ratios,  $X_{\text{Aut}}$  coexists  
343 with  $X_H$  (Bassin et al., 2015).

344 As a summary of the microorganisms distribution of the BAS process, it is observed  
345 that the first reactor of the MBBR is the bacterial stage, the second reactor of the MBBR  
346 is the bacterial-predator stage and the AS reactor is the predator stage.

#### 347 *4.3. Nutrient dosage in the BAS process*

348 A ratio of 100:5:1 ( $\text{COD}_f:\text{N}:\text{P}$ ) has traditionally been used as a “rule of thumb” for  
349 setting nutrient levels in biological processes (Ammary, 2004). However, studies of  
350 BAS processes treating wastewater from the pulp and paper industry indicate that  
351 nitrogen and phosphorus requirements in relation to  $\text{COD}_f$  are not always as high as the  
352 above ratio (Rankin et al., 2007). In this work, the  $\text{COD}_f:\text{N}:\text{P}$  ratios used are much  
353 lower than the “rule of thumb” (Slade et al., 2004), as shown in Table 3. The large  
354 percentage of  $\text{COD}_f$  removed in the BAS process confirms that the ratio can be much  
355 lower than the ratio indicated by the “rule of thumb”, with a positive economic effect on  
356 the overall process due to the high cost of nutrients (Revilla et al., 2014).

357 To illustrate why this low level of  $COD_f:N:P$  is sufficient in the BAS process, the  
358 simulation results under a steady state of nutrients were obtained for MBBR and AS  
359 reactors in Table 5. It is observed that the simulation results for  $S_{PO4}$  and  $S_{NO3}$  in the AS  
360 reactor are much higher than in MBBR reactors, but the simulation result for  $S_{NH4}$  in the  
361 AS reactor is much lower. The unexpected increase in  $S_{PO4}$  after running the simulation  
362 in the activated sludge reactor is due to two biological processes: predation and  
363 inactivation (Hao et al, 2011). During these processes, phosphorous compounds inside  
364 heterotrophic microorganisms are released into the water. However, the simulation  
365 result for  $S_{NH4}$  in the AS reactor is very low because  $S_{NH4}$  recovered due to predation  
366 results in a low  $COD_f/S_{NH4}$  ratio, and  $S_{NH4}$  is oxidized to  $S_{NO3}$  by autotrophic  
367 microorganisms (Lee and Park, 2007). As a result, the simulation result for  $S_{NO3}$  is high,  
368 and the  $S_{NH4}$  concentration is low in the AS reactor of the BAS process.

369 To confirm the influence of predation on the concentrations of phosphorus and nitrogen  
370 forms in the AS reactor of a BAS process, the proposed mathematical model was used  
371 to switch predation on and off (Moussa et al., 2005). The simulation of  $S_{NH4}$ ,  $S_{NO3}$  and  
372  $S_{PO4}$  at steady state when predation is switched on and off are shown in Table 6. These  
373 values are all lower in absence of predators than in the presence of predators,  
374 reinforcing the importance of predator microorganisms.

375 These results demonstrate the importance of predation in the AS reactors of the BAS  
376 process for nutrient dosage. The increase in phosphorus and nitrogen concentrations in  
377 the AS reactor due to predation enables the use of low doses of nutrients in the inlet  
378 stream of the BAS process without decreasing  $COD_f$  removal efficiency. This is a great  
379 advantage for the overall process (Rankin et al., 2007).

380 *4.4. Sludge production in the BAS process.*



381 The treatment and disposal of sludge from a wastewater treatment plant is expensive  
382 and can account for up to 60% of the total operating costs of wastewater treatment  
383 (Ramdani et al., 2010). Reducing sludge production thus presents an obvious economic  
384 interest. A main characteristic of the BAS process is that the production of sludge is  
385 much lower than in conventional AS processes (Rankin et al., 2007; Malmqvist et al.,  
386 2008).

387 In this section, the influence of predation is analysed by comparison of the fraction of  
388 particulate compounds and concentration of TSS in the AS reactor using the proposed  
389 model. The comparison is performed at steady state under the same operational  
390 conditions, but switching predation processes on and off. Table 6 shows the simulated  
391 results with and without predators. It is observed decreases in TSS concentration of  
392 42% and 44% in case study A and B, respectively, when predation was on (Wei et al.,  
393 2003; Malmqvist et al., 2008). These results are explained by the large decrease in the  
394 fraction of  $X_H$  when predators are activated, since the main food source in the AS  
395 reactor of BAS for predator microorganisms are the heterotrophic microorganisms that  
396 leave the second MBBR reactor (Sointio et al., 2006). As shown in Table 6, the  
397 presence of high fractions of predator leads to an increase in the inert fraction.

#### 398 *4.5. Influence of the SRT on biomass content in the BAS process*

399 Another option for decreasing sludge production is to extend the SRT (Liu and Wang,  
400 2015). However, an increase in SRT results in an increase in the inactivation processes,  
401 which may lead to a higher concentration of inert matter. As a consequence, biological  
402 wastewater treatment could lose efficiency (Hreiz et al., 2015). The level of inert matter  
403 in the AS reactor of the full-scale BAS plant under study is high (Figure 5) due to  
404 inactivation and predation mechanisms (observed previously by Hao et al., 2011).

405 Therefore, it is especially important to control SRT to avoid efficiency losses in the  
406 treatment and accumulation of inert matter.

407 Case studies A and B operate under different SRT conditions suited to different  
408 industrial wastewaters (Table 3). An analysis of both case studies allows observation of  
409 the effect of SRT on the fraction of particulate compounds and biomass content in the  
410 AS reactor. Figure 6 shows the dynamic behaviour of the simulated fraction of  
411 particulate compounds in both case studies until they reach a steady state after 150 days.  
412 This allows comparison of the behaviour of all biomass content in the AS reactor for  
413 two different SRTs and industrial wastewaters at the steady state. Case study B operates  
414 with a higher SRT (30 days) than case study A (19 days), resulting in similar  
415 concentrations of TSS in both case studies at the steady state ( $8.5\text{ g/m}^3$  in case study A  
416 and  $8.6\text{ g/m}^3$  in case study B), namely, the inert material ( $X_I$ ) that is the main fraction  
417 of TSS.

418 For wastewater from the cellulose industry (case study B), it is possible to operate using  
419 high SRT values because the increase in  $X_I$  is compensated by a reduction in the amount  
420 of predators ( $X_{\text{Predators}}$ ), heterotrophic microorganisms ( $X_H$ ) and autotrophic  
421 microorganisms ( $X_{\text{Aut}}$ ) (Moussa et al., 2005) resulting in similar concentrations of TSS  
422 in both case studies. Therefore, the mathematical model can be used to determine the  
423 fraction of particulate compounds at various operating conditions of SRT and thus avoid  
424 the accumulation of high amounts of inert material (Moussa et al., 2005; Ni et al., 2009,  
425 2011) in the AS reactor during a BAS process.

## 426 **5. Conclusions**

427 A novel unified model for the BAS process is proposed to study microbial behaviour in  
428 the biofilm (MBBR) and AS stages and to evaluate the influence of predation

429 mechanisms on nutrient dosage, sludge production and microbial distribution. The first  
430 MBBR reactor is the bacterial stage, the second MBBR reactor is the bacterial-predator  
431 stage and the AS reactor is the predator stage. The results demonstrate that predation is  
432 the main cause of reductions in nutrient requirements (up to 44%) and sludge  
433 production (up to 46%) compared to the conventional AS process.

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