

(1) and (2) as follows,

$$E_{out} = \int P_{sm} dt \cdot S_{sm,base}, \quad (1)$$

$$I_{sm} = \sqrt{I_{sm0}^2 - 2E_{out} / (L_{sm} \cdot I_{sm,base}^2)}, \quad (2)$$

where, L_{sm} is the SMES coil inductance, (H); E_{out} is the SMES energy output, (J); $I_{sm,base}$ is the SMES current base, (A); and $S_{sm,base}$ is the SMES MVAbase, (MVA). Subsequently, the energy stored in the SMES unit (E_{sm}) and the initial E_{sm} (E_{sm0}) can be determined by (3) and (4) as follows,

$$E_{sm} = E_{sm0} - E_{out}, \quad (3)$$

$$E_{sm0} = 0.5 L_{sm} I_{sm0}^2 \cdot I_{sm,base}^2, \quad (4)$$

The desired SMES output active and reactive power (P_d and Q_d) can be expressed as

$$P_d = V_{ts} I_{sm} AP, \quad (5)$$

$$Q_d = V_{ts} I_{sm} AQ, \quad (6)$$

where, AP and AQ are the active and reactive power fractions, respectively. For simplicity, V_{ts} is a steady state bus voltage of SMES unit, (pu). The SMES output active and reactive power, i.e., P_{sm} and Q_{sm} are the output of the SMES controlled converter (CONV), which is represented by a first order time-lag compensator as follows,

$$P_{sm} = 1/(1 + 0.01s)P_d, \quad (7)$$

$$Q_{sm} = 1/(1 + 0.01s)Q_d. \quad (8)$$

In this paper, it is assumed that for a nominal condition the SMES unit should not supply/receive active and reactive power to/from the power system. On the other hand, the SMES unit should alleviate power system oscillations when being subjected to system disturbances.

III. ROBUST CONTROLLER DESIGN

To enhance the power system stabilization, the structure of 2nd order lead/lag compensator is used in the design of $K_P(s)$ and $K_Q(s)$ controllers as

$$\Delta u_{CTL} = K_C \frac{sT_W}{1 + sT_W} \left[\frac{1 + sT_1}{1 + sT_2} \right] \left[\frac{1 + sT_3}{1 + sT_4} \right] \cdot \Delta u_{IN}, \quad (9)$$

where, Δu_{CTL} is the control output signal of controller; Δu_{IN} is the feedback input signal of controller; K_C is a controller gain; T_W is a washout time constant (s); and, T_1 , T_2 , T_3 and T_4 are time constants (s). Note that Δu_{IN} for $K_P(s)$ is the tie-line active power deviation (ΔP_{tie}), and Δu_{IN} for $K_Q(s)$ is the tie-line reactive power deviation (ΔQ_{tie}).

In this paper, T_W is set to 10s. The control parameters K_C , T_1 , T_2 , T_3 and T_4 are optimized using Hybrid TS/EP [5] based on the following objective function F ,

$$\begin{aligned} \text{Min} \quad & F(K_C, T_i) = \varphi + \gamma, \\ \text{St.} \quad & K_{\min} \leq K_C \leq K_{\max}, \\ & T_{\min} \leq T_i \leq T_{\max}, \quad i = 1, \dots, 4 \end{aligned} \quad (10)$$

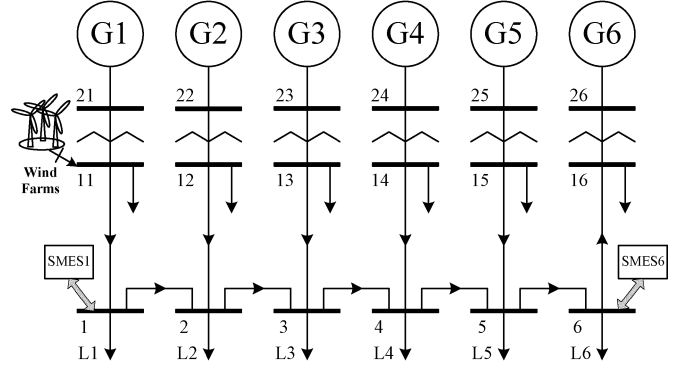


Fig. 2. Six-area interconnected power system with wind farms and SMES.

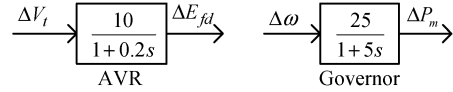


Fig. 3. AVR and Governor systems.

where, K_{\min} , K_{\max} , T_{\min} and T_{\max} are the minimum and maximum values of a controller gain and a time constant, respectively. φ is the difference between the actual and the desired damping ratios of the dominant power oscillation mode. γ is the normalized robustness index in terms of a multiplicative stability margin (MSM) [5]. It should be noted that the larger the MSM, the better the robust stability margin will be.

IV. APPLICATION TO INTERCONNECTED POWER SYSTEM WITH WIND FARMS

A. Study System

The interconnected power system as shown in Fig. 2 is employed in the study. The power system consists of six areas connected in a longitudinal configuration. Each area is represented by a 5th order generator model [6]. Fig. 3 depicts an automatic voltage regulator (AVR) and a governing system. It should be noted that the characteristic of a simple governor is used, since the tie-line power compensation by the SMES is apparently faster than that by the governor. This also implies that SMES and governing system can be coordinated properly. In addition, the dynamic of governor can be neglected in the design of RSMES. The area capacity ratio for areas 1 to 6 is 20:13.5:6.75:40:6.75:33 with a 1,000 MVA base. For study purpose, the electric power is transferred from areas 1 to 6. The wind farms are located in area 1 and have the maximum generation capacity of 500 MW. Based on the residue method [7], areas 1 and 6 are equipped with SMES for power system stabilization. The SMES has a specification of 800 MJ, 40 kA, 1,000 MVA.

B. Simulation Results and Evaluations

In this study, the RSMES are designed at the design operating condition (DOC). By using Hybrid TS/EP, the control parameters of $K_P(s)$ and $K_Q(s)$ controllers are optimized successfully based on the objective function (10) to yield the desired damping ratio of 0.055 and achieve the best obtainable MSM. Consequently, the robust control parameters are obtained

TABLE I
 OPERATING CONDITIONS

	1.DOC ($P_{tie} = 2.3$)	2.LL ($P_{tie} = 1.5$)	3.HL ($P_{tie} = 3.0$)
G1	PG: 12, L1: 2.2 L11: 7+j0.7	PG: 8, L1: 1.5 L11: 5+j0.5	PG: 16, L1: 3.0 L11: 10+j1.0
G2	PG: 8.1, L2: 1.5 L12: 6.3+j0.6	PG: 5.4, L2: 1.0 L12: 4.2+j0.4	PG: 10.8, L2: 2.0 L12: 8.4+j0.8
G3	PG: 4.05, L3: 0.9 L13: 3.2+j0.3	PG: 2.7, L3: 0.6 L13: 2.1+j0.2	PG: 5.4, L3: 1.2 L13: 4.2+j0.4
G4	PG: 24, L4: 4.5 L14: 18.5+j1.8	PG: 16, L4: 3.0 L14: 13+j1.3	PG: 32, L4: 6.0 L14: 26+j2.6
G5	PG: 4.05, L5: 0.9 L15: 3.2+j0.3	PG: 2.7, L5: 0.6 L15: 2.1+j0.2	PG: 5.4, L5: 1.2 L15: 4.2+j0.4
G6	PG: 16.4, L6: 4.5 L16: 15.3+j1.5	PG: 11.55, L6: 3.0 L16: 10.2+j1.0	PG: 23.2, L6: 6.0 L16: 20.4+j2.0

PG: Generation (pu), L: Load (pu), Base: 1,000 MVA

 TABLE II
 DOMINANT MODES AND DAMPING RATIOS

Case	1.DOC ($P_{tie} = 2.3$)	2.LL ($P_{tie} = 1.5$)	3.HL ($P_{tie} = 3.0$)
No SMES	-0.074+j2.713; +0.027	-0.114+j2.914; +0.039	0.100+j2.387; -0.042
CSMES	-0.104+j3.679; +0.028	-0.154+j3.894; +0.040	-0.036+j3.413; +0.011
RSMES	-0.525+j3.299; +0.157	-0.688+j3.763; +0.180	-0.164+j2.744; +0.060
	-0.366+j6.673; +0.055	-0.438+j6.296; +0.069	-0.095+j3.654; +0.026
	-0.400+j3.237; +0.123	-0.471+j3.535; +0.132	-0.106+j2.756; +0.039
	-0.365+j6.651; +0.055	-0.435+j6.278; +0.069	-0.116+j3.740; +0.031

as follows.

SMES1 :

$$K_P(s) = 1.02 \frac{10s}{1+10s} \left[\frac{1+0.323s}{1+0.042s} \right] \left[\frac{1+0.287s}{1+0.068s} \right] \quad (11)$$

SMES1 :

$$K_Q(s) = 2.00 \frac{10s}{1+10s} \left[\frac{1+0.204s}{1+0.281s} \right] \left[\frac{1+0.620s}{1+0.180s} \right] \quad (12)$$

SMES6 :

$$K_P(s) = 1.00 \frac{10s}{1+10s} \left[\frac{1+0.425s}{1+0.233s} \right] \left[\frac{1+0.010s}{1+0.114s} \right] \quad (13)$$

SMES6 :

$$K_Q(s) = 26.48 \frac{10s}{1+10s} \left[\frac{1+0.097s}{1+0.019s} \right] \left[\frac{1+0.341s}{1+0.217s} \right] \quad (14)$$

For comparison purpose, the conventional SMES controllers (CSMES) are designed using the same method but the MSM is not considered in the design. In particular, the CSMES are also designed to yield the desired damping ratio of 0.055.

To evaluate the designed controller, three different operating conditions are employed as given in Table I, i.e., 1.DOC, 2.Light Load (LL) and 3.Heavy Load (HL). In particular, the tie-line power flows (P_{tie}) in all operating conditions are also different. In each case the eigenvalues of the power oscillation modes are evaluated as shown in Table II, however, only two dominant modes are given. This system has a dominant power oscillation mode with a long period which becomes unstable as the power flow becomes heavier.

 TABLE III
 MULTIPLICATIVE STABILITY MARGINS

Case	1.DOC ($P_{tie} = 2.3$)	2.LL ($P_{tie} = 1.5$)	3.HL ($P_{tie} = 3.0$)
CSMES	0.604	0.836	0.335
RSMES	0.858	1.202	0.403

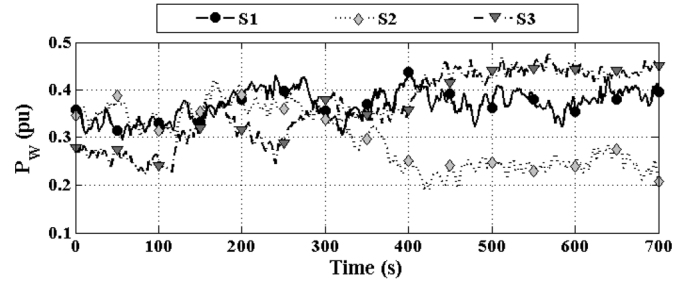


Fig. 4. Wind power generations [Base: 1000 MVA].

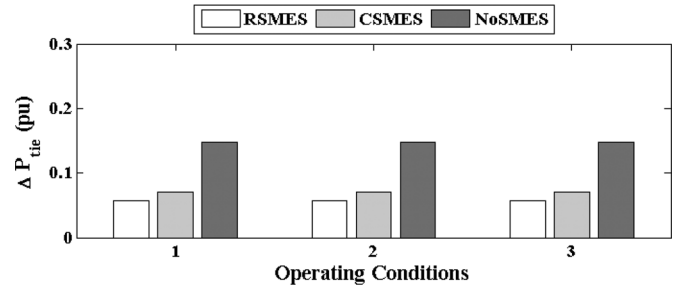


Fig. 5. Maximum deviations of P_{tie} with wind power S1 [Base: 1000 MVA].

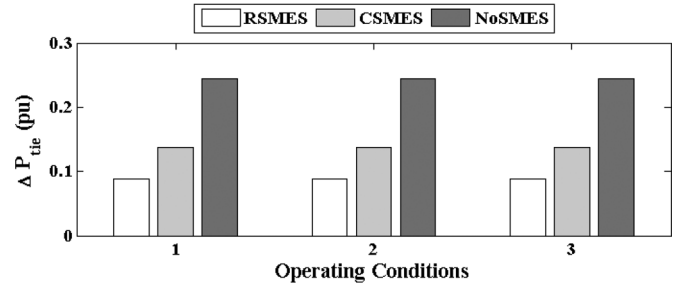


Fig. 6. Maximum deviations of P_{tie} with wind power S2 [Base: 1000 MVA].

As results, both RSMES and CSMES can significantly improve the system damping performance in all cases. In addition, MSMs are shown in Table III. In comparison with CSMES, the system with RSMES has higher MSMs. The higher MSM indicates the higher degree of system variations at which the system can persist without destabilized by unexpected disturbances.

Subsequently, nonlinear simulation studies are carried out to evaluate the effectiveness and robustness of tie-line power stabilization when the system is subjected to wind power fluctuations. The data of wind power (P_W) measured and collected from site are modified and employed to represent the wind power attached to area 1 at different situations as shown in Fig. 4. In particular, S1 represents the wind power with slightly changed generation. S2 represents the wind power with sudden decrease, and S3 represents the wind power with sudden increase.

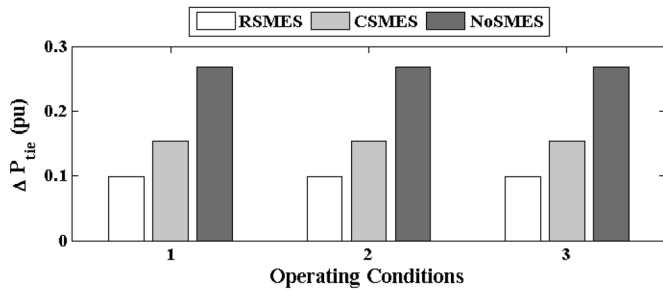


Fig. 7. Maximum deviations of P_{tie} with wind power S3 [Base: 1000 MVA].

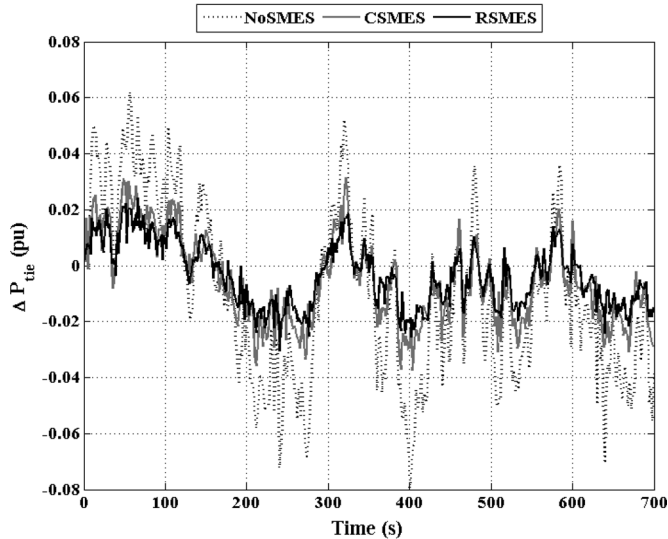


Fig. 8. System responses of P_{tie} in case HL with wind power S1.

As shown in Figs. 5–7, the maximum deviations of P_{tie} in different cases and wind power situations are presented. Fig. 5 shows the comparison when the wind power S1 is applied. The power system with CSMES and RSMES shows significantly the improvement of tie-line power flow. On the other hand, in case without SMES (NoSMES) fluctuations of P_{tie} are high, although the power system is still stable. Figs. 6 and 7 show the comparison when the wind powers S2 and S3 are applied, respectively. It is obvious that RSMES yield effectively the best performance in comparison with CSMES and NoSMES. This also implies that RSMES can retain satisfactorily the robust performance. Next, some nonlinear time-domain simulation results are illustrated to show the effectiveness and robustness of the designed controller. Fig. 8 shows the system responses of P_{tie} in case HL when the wind power S1 is applied. In comparison with NoSMES, the maximum deviations of P_{tie} in case of RSMES can be reduced by 62%, whereas in case of CSMES can be reduced by 53%. It should be noted that the dynamic of governor is also included in the time-domain simulation to show that SMES and governing system can properly work together.

Fig. 9 shows the system responses of I_{sm} of SMES1 and SMES6 in case HL when the wind power S1 is applied. Apparently, both I_{sm} of RSMES and CSMES can properly remain within the allowable limits. However, the fluctuation of I_{sm} in case of RSMES is larger. This is due to the fact that RSMES can appropriately supply and receive the larger amount of electrical

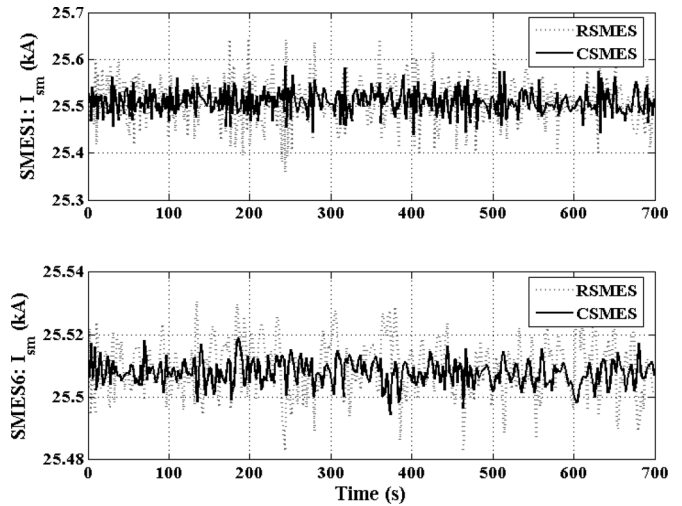


Fig. 9. System responses of I_{sm} in case HL with wind power S1.

energy with the power system. Accordingly, the stabilization of tie-line power flow by RSMES is superior to that by CSMES. In addition, it should be noted that the electrical energy stored in the SMES is also appropriately utilized due to the close correlation between E_{sm} and I_{sm} .

V. CONCLUSION

In this paper, the use of robust SMES controller for stabilization of tie-line power flow in a longitudinally interconnected power system is presented. SMES is an effective device and can be applied to various applications in power systems. With proper controller design, SMES can be a promising solution for mitigating problems of tie-line power fluctuations due to adverse effects of wind farms in a power system. Moreover, by considering the robustness in the controller design, the robust SMES controller can robustly operate and maintain the effective use of transmission lines. Finally, simulation results exhibit and confirm the effectiveness and robustness in case of a power system with wind farms under various situations.

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