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# Next generation energy modelling – Benefits of applying parallel optimization and high performance computing

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Frieder Borggrefe

System Analysis and Technology Assessment

DLR - German Aerospace Center

Stuttgart

A PROJECT BY



H L R I S



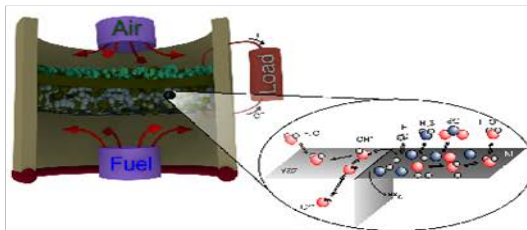
Deutsches Zentrum  
für Luft- und Raumfahrt  
German Aerospace Center

1. Introduction – energy system Modelling and constraints
2. The project BEAM-ME
3. Decomposition
4. Model annotation and PIPS-IPM

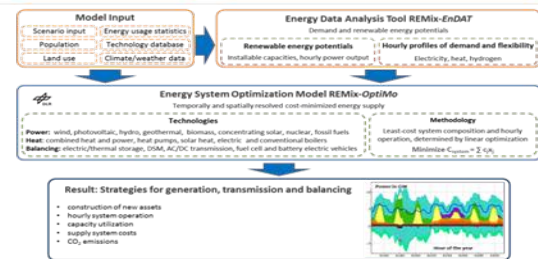
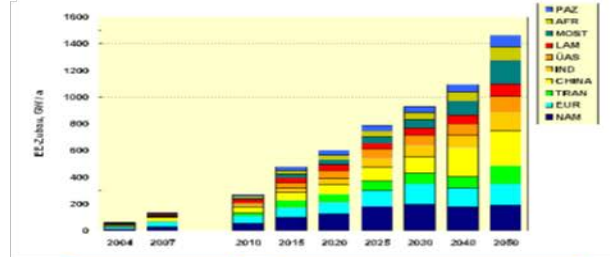
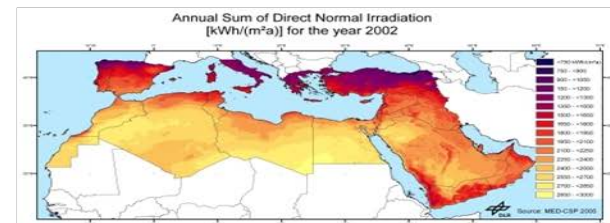
DLR



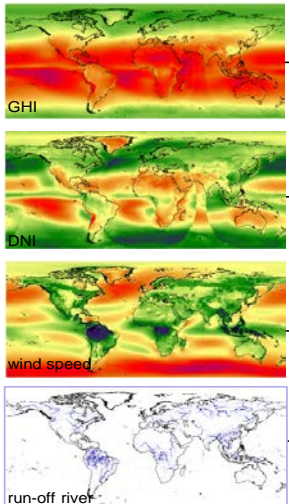
Institute of Engineering Thermodynamics



Systems Analysis and Technology Assessment



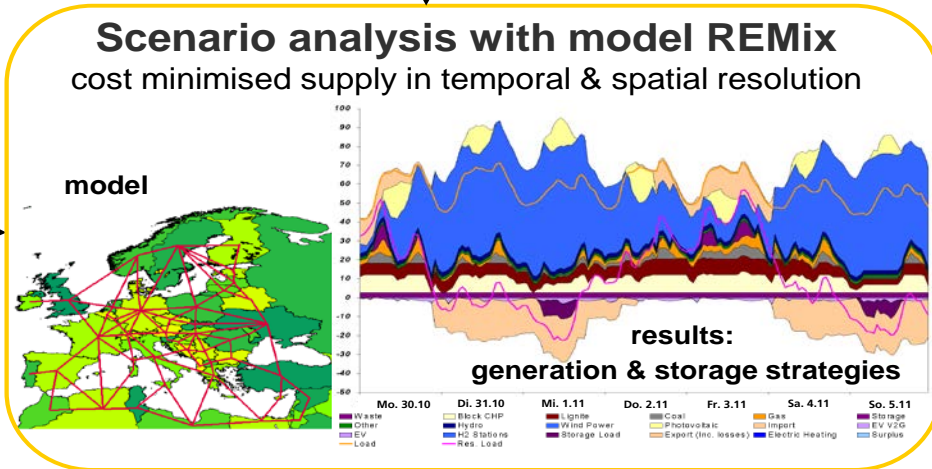
**Installed capacities and power generation profiles from renewables**



**HVDC lines**  
long-range power exchange and imports

**Transmission grid**  
based on current European AC grid

**Scenario analysis with model REMix**  
cost minimised supply in temporal & spatial resolution



**Electricity demand**



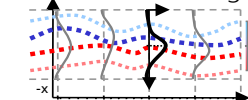
**Heat demand**

**Flexible operation of CHP with:**

- heat storages
- peak boiler & electric heaters

**Electric vehicles (EV)**

**BEV/hybrids:** charging strategies, hourly battery capacities of the fleet connected to the grid



**FCEV:** flexible on-site H<sub>2</sub> generation

**Conventional generation**  
nuclear, coal, gas power plants

**Storages**  
pumped hydro, compressed air, hydrogen

**Demand side management**  
industry & households, increases system efficiency

Installed capacities and power generation profiles: **Energy system models:** renew

**HVDC lines**  
long-range power exchange and imports

**Transmission grid**  
based on current European AC grid

Electricity demand



and generation of  
fossil fuels & electric

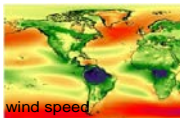
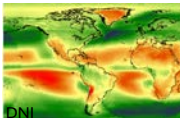
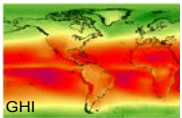
vehicles (EV)

EVs: charging daily battery, the fleet, the grid



**FCEV:** flexible on-site H<sub>2</sub> generation

- Simulate
  - policy and technology choices
  - influence on future energy demand and supply, and investments
- > are mostly used in an exploratory manner
- Depend on external assumptions/boundary conditions:
  - Development of economic activities,
  - demographic development,
  - or energy prices on world markets.



....

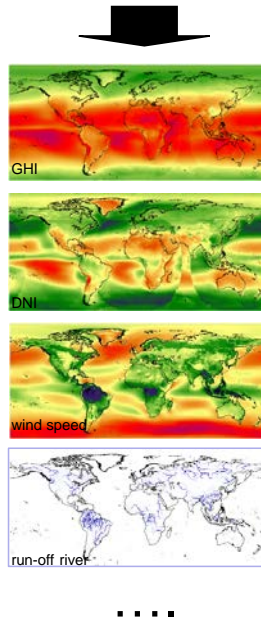
**generation**  
nuclear, coal, gas power plants

pumped hydro  
compressed air  
hydrogen

**management**  
industry & households, increases system efficiency

# The Energy System Model REMix

Installed capacities and power generation profiles from renewables



**HVDC lines**  
long-range power exchange and imports

**Transmission grid**  
based on current European AC grid

$$\min c^T \lambda$$

$$\text{s.t. } A \lambda \geq \tilde{b}$$

**Electricity demand**



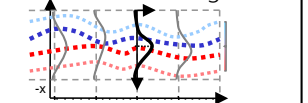
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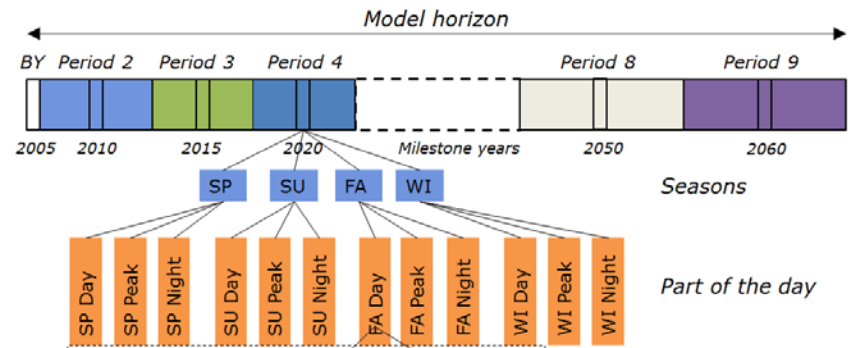




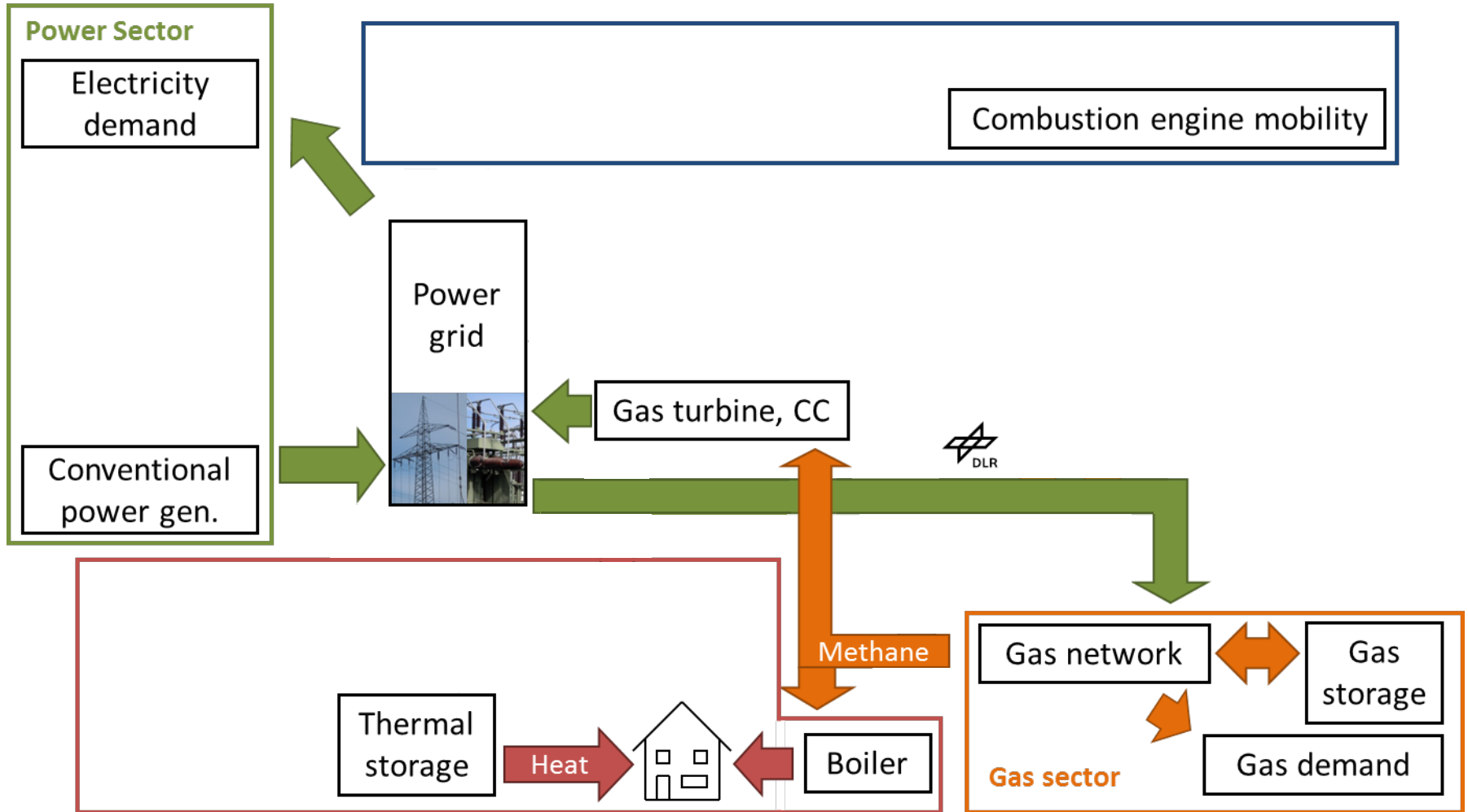
## Modelling comes at a cost:

- Small number of time steps
- Or small number of regions
- Or small number of technologies

## JRC Times model:



# Energy Sector Integration





OMaT 0.2.1.52 - ZIB

File Sync AutoCode Options

Name: ZIB  
User: cao\_ka  
CodeBase: D:/REMix\_OaM/OptMo

Project Modules / Scenario

- Project
- CodeBase
- Find Items

ModuleInfo ScenarioInfo Options Parameter Sets TimeSeries

Module: convBase

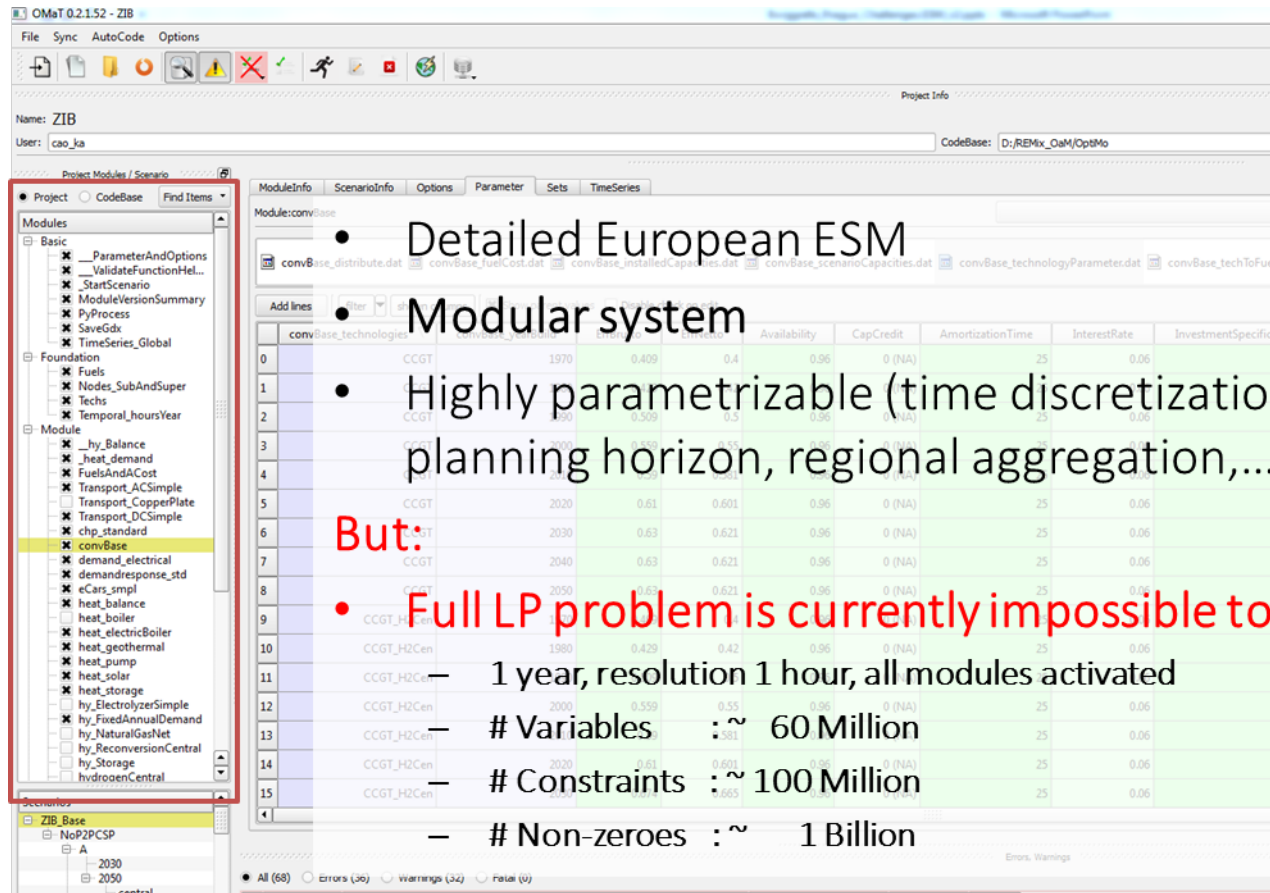
convBase\_distribute.dat convBase\_fuelCost.dat convBase\_installedCapacities.dat convBase\_scenarioCapacities.dat convBase\_technologyParameter.dat convBase\_techToFuel

Add lines filter shown columns Show parent values Disable check on edit

	convBase_technologies	convBase_yearBuild	EffBrutto	EffNetto	Availability	CapCredit	AmortizationTime	InterestRate	InvestmentSpecific
0	CCGT	1970	0.409	0.4	0.96	0 (NA)	25	0.06	70
1	CCGT	1980	0.429	0.42	0.96	0 (NA)	25	0.06	70
2	CCGT	1990	0.509	0.5	0.96	0 (NA)	25	0.06	70
3	CCGT	2000	0.559	0.55	0.96	0 (NA)	25	0.06	70
4	CCGT	2010	0.59	0.581	0.96	0 (NA)	25	0.06	70
5	CCGT	2020	0.61	0.601	0.96	0 (NA)	25	0.06	70
6	CCGT	2030	0.63	0.621	0.96	0 (NA)	25	0.06	70
7	CCGT	2040	0.63	0.621	0.96	0 (NA)	25	0.06	70
8	CCGT	2050	0.63	0.621	0.96	0 (NA)	25	0.06	70
9	CCGT_H2Cen	1970	0.409	0.4	0.96	0 (NA)	25	0.06	70
10	CCGT_H2Cen	1980	0.429	0.42	0.96	0 (NA)	25	0.06	70
11	CCGT_H2Cen	1990	0.509	0.5	0.96	0 (NA)	25	0.06	70
12	CCGT_H2Cen	2000	0.559	0.55	0.96	0 (NA)	25	0.06	70
13	CCGT_H2Cen	2010	0.59	0.581	0.96	0 (NA)	25	0.06	70
14	CCGT_H2Cen	2020	0.61	0.601	0.96	0 (NA)	25	0.06	70
15	CCGT_H2Cen	2030	0.674	0.665	0.96	0 (NA)	25	0.06	70

Errors, Warnings

All (68) Errors (36) Warnings (32) Fatal (0)



Project Name: ZIB  
User: cao\_jia  
CodeBase: D:\REMix\_OaM\OptMo

Module: convBase

- Detailed European ESM
- Modular system
- Highly parametrizable (time discretization, planning horizon, regional aggregation,...)

**But:**

- Full LP problem is currently impossible to solve:
  - 1 year, resolution 1 hour, all modules activated
  - # Variables : ~ 60 Million
  - # Constraints : ~ 100 Million
  - # Non-zeros : ~ 1 Billion

convbase_technologies	convbase_year	Energy	Efficiency	Availability	CapCredit	AmortizationTime	InterestRate	InvestmentSpecific
0	CCGT	1970	0.409	0.4	0.96	0 (NA)	0.06	70
1	CCGT	1990	0.509	0.5	0.96	(NA)	0.06	70
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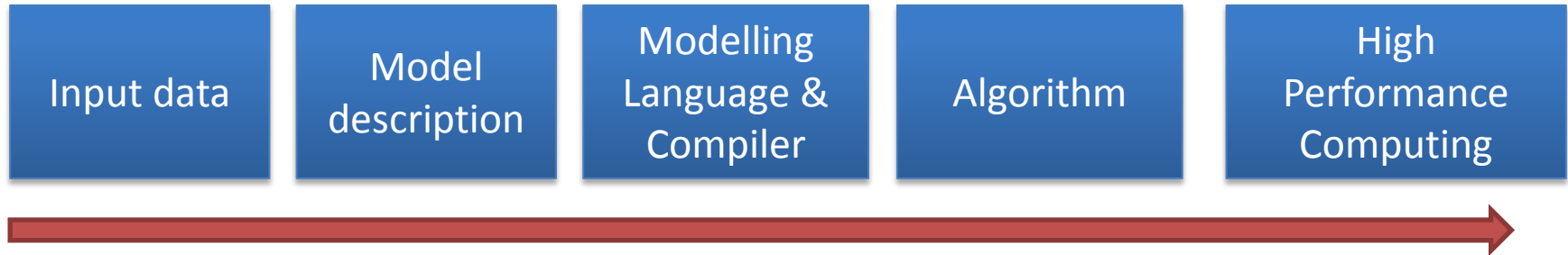
1. Introduction – energy system Modelling and constraints
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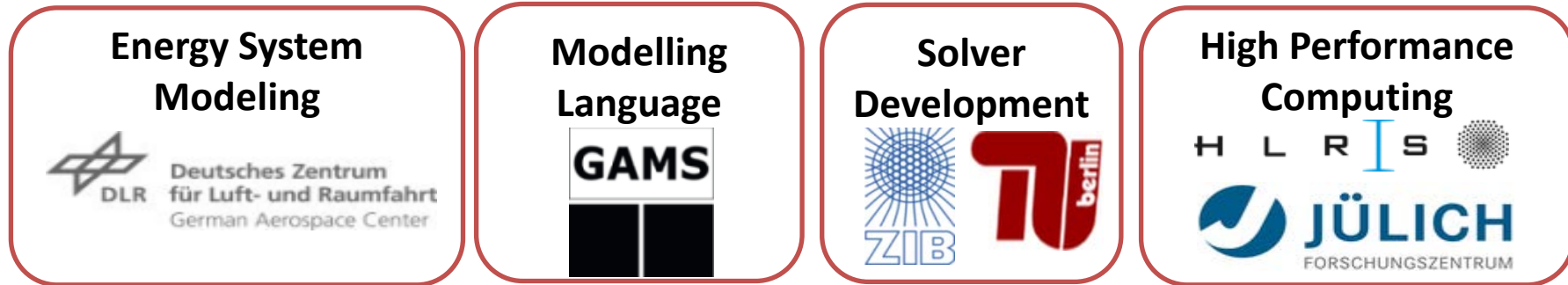
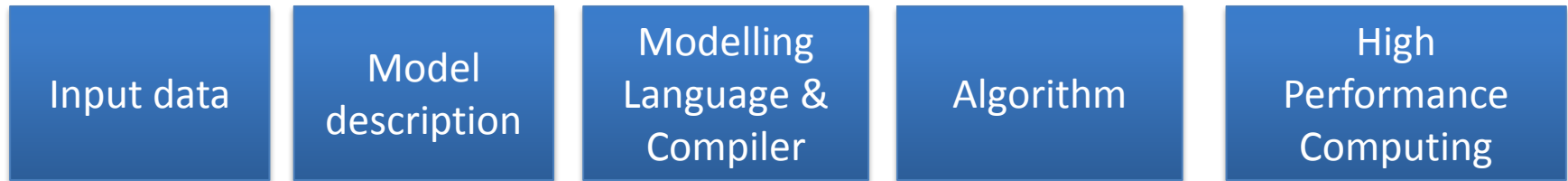


Reduction of solution times urgently needed to enable the reflection of energy system complexity in state-of-the-art models

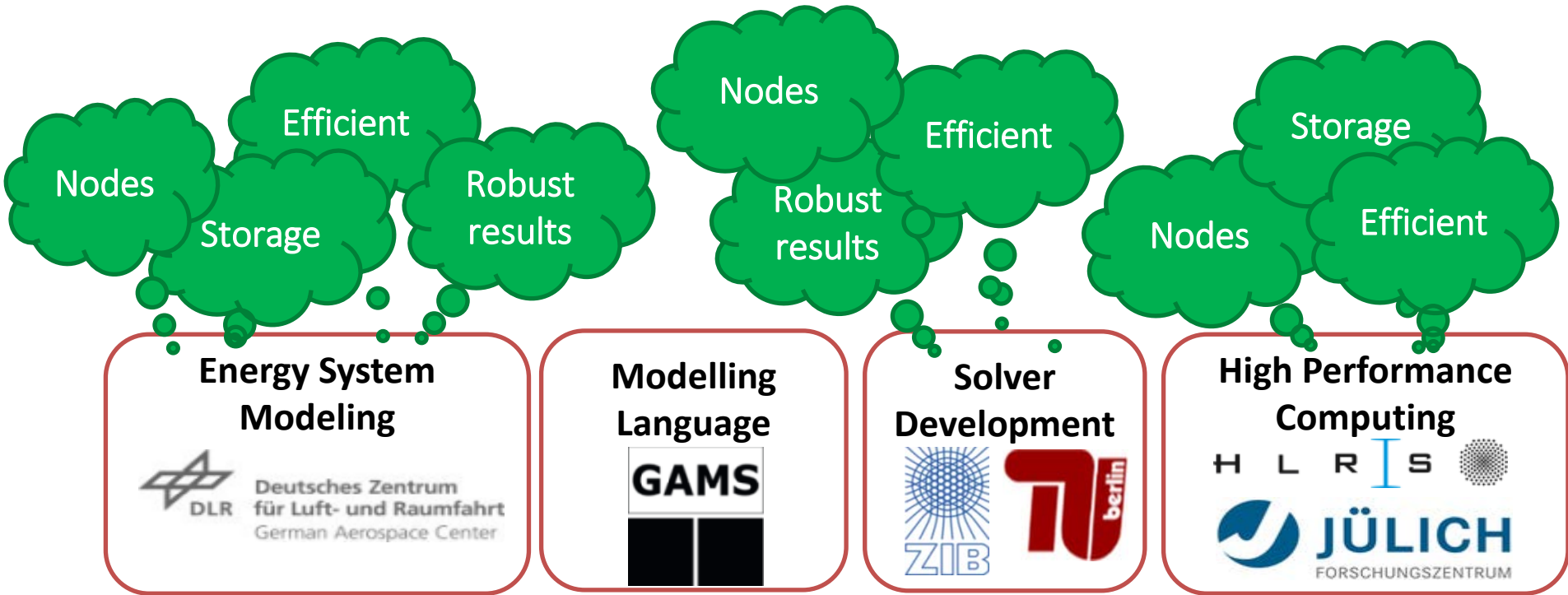


- Evaluation of different approaches to reduce model solution times
  - Increased Modelling efficiency
  - Higher computing power
- Implementation of selected approaches into REMix
- Assessment of the transferability to other models
- Definition of best-practice strategies

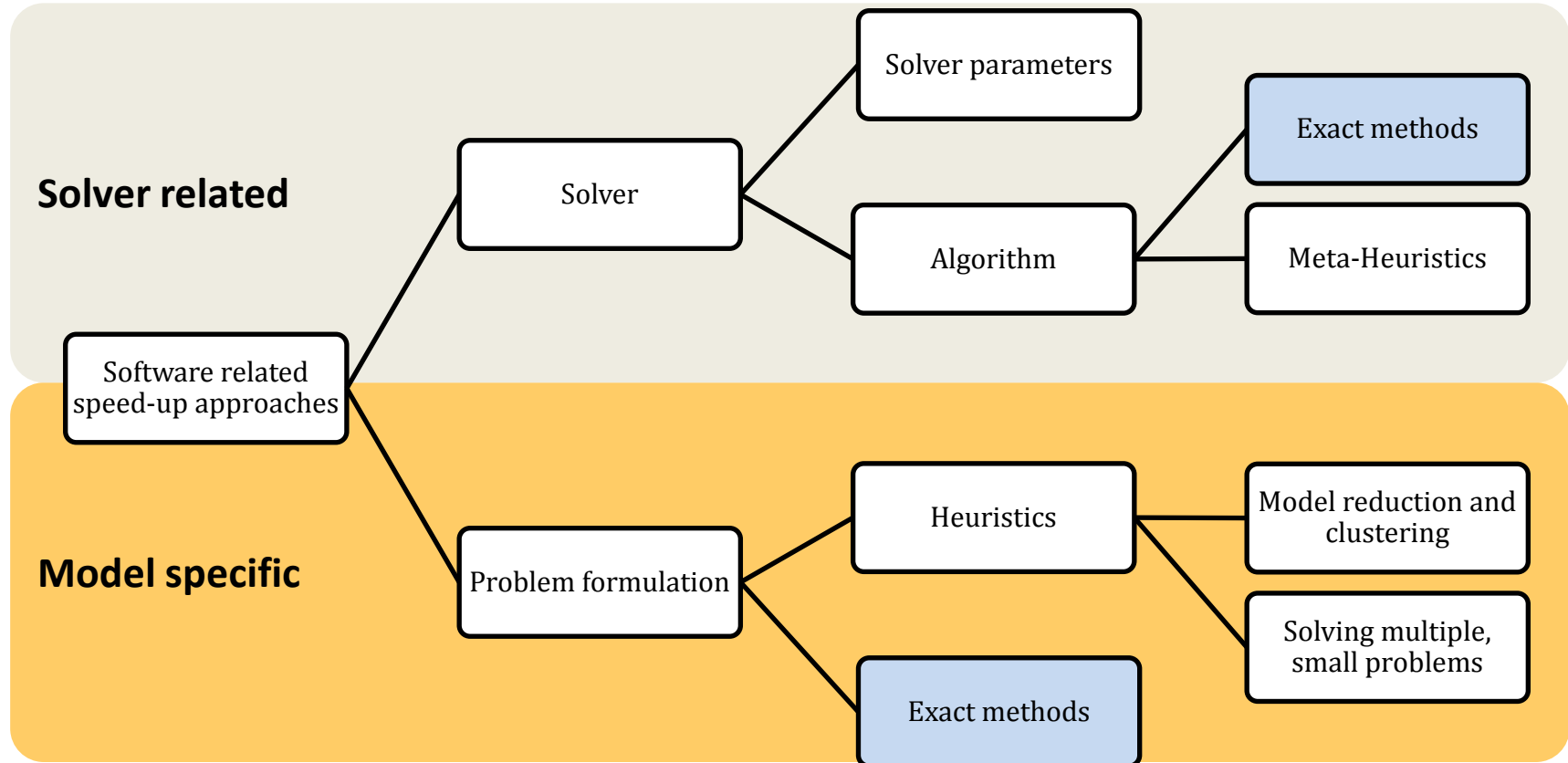








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## Benders decomposition for two-stage stochastic optimization

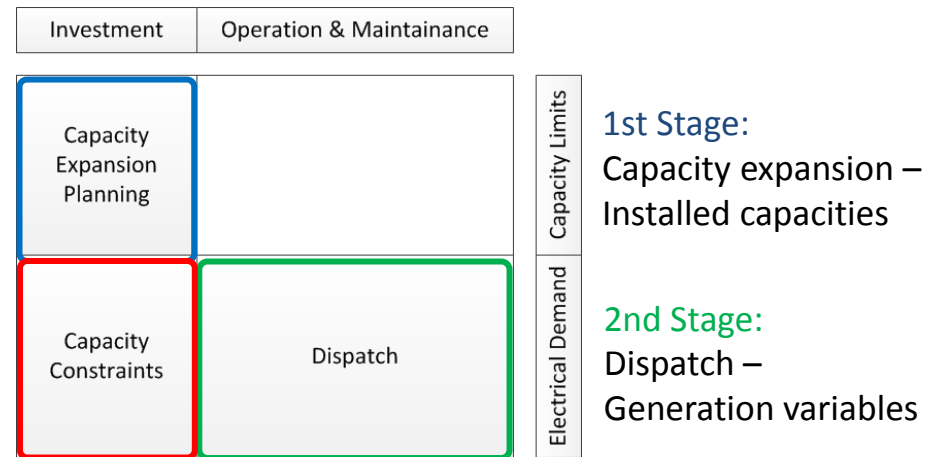
### Investment -> Master problem:

- Decide now which capacities should be expanded

### Dispatch -> Sub problem:

- Decide later on economic dispatch to satisfy electrical demand with capacities given by master problem

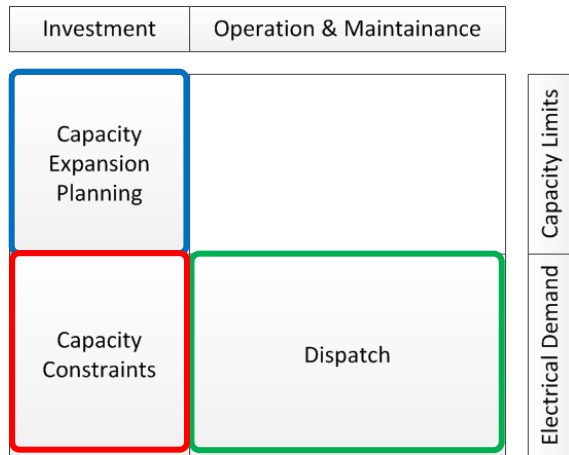
## Mathematical formulation in LP table



### Linking variables:

Installed capacities, connecting the capacity expansion problem and the dispatch problem

## Deterministic Model



1st Stage:  
Capacity expansion –  
Installed capacities



## Benders Decomposition

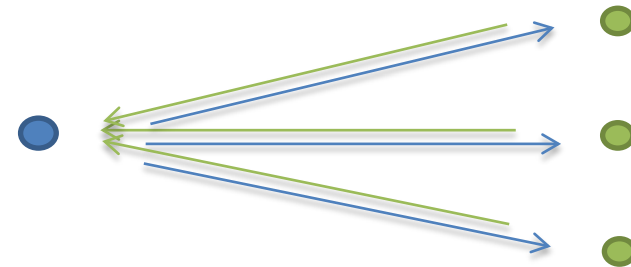
### Master



### Subproblem



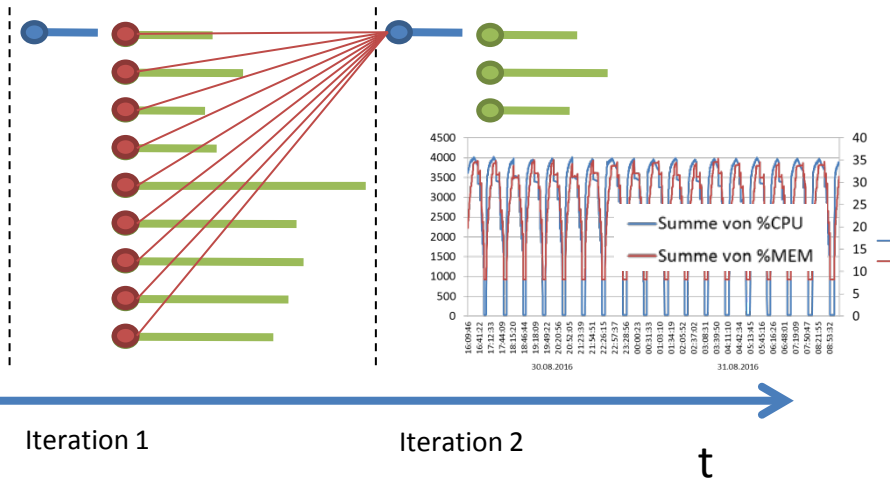
2nd Stage:  
Dispatch –  
Generation variables



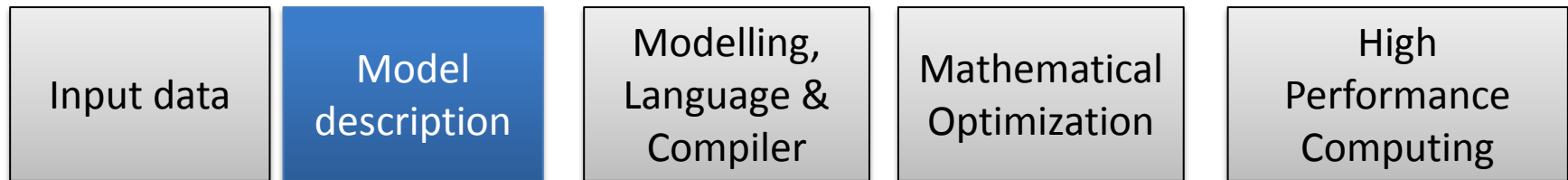
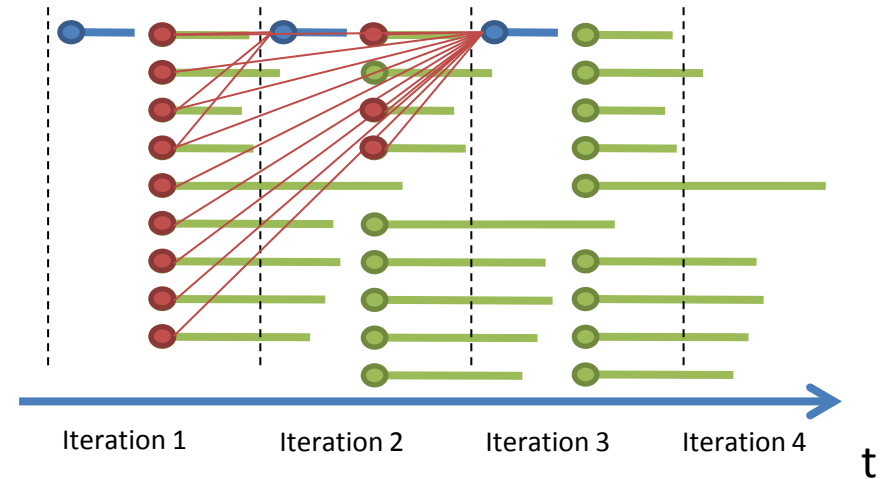
- Size of LP increases with number of scenarios, solved by SIMPLEX / Barrier
- **Out of memory** for typical REMix problems with scenario dimension

- Subproblems can be **solved in parallel**
- Memory demand **scales** with number of parallel solve processes

## Synchronous Model



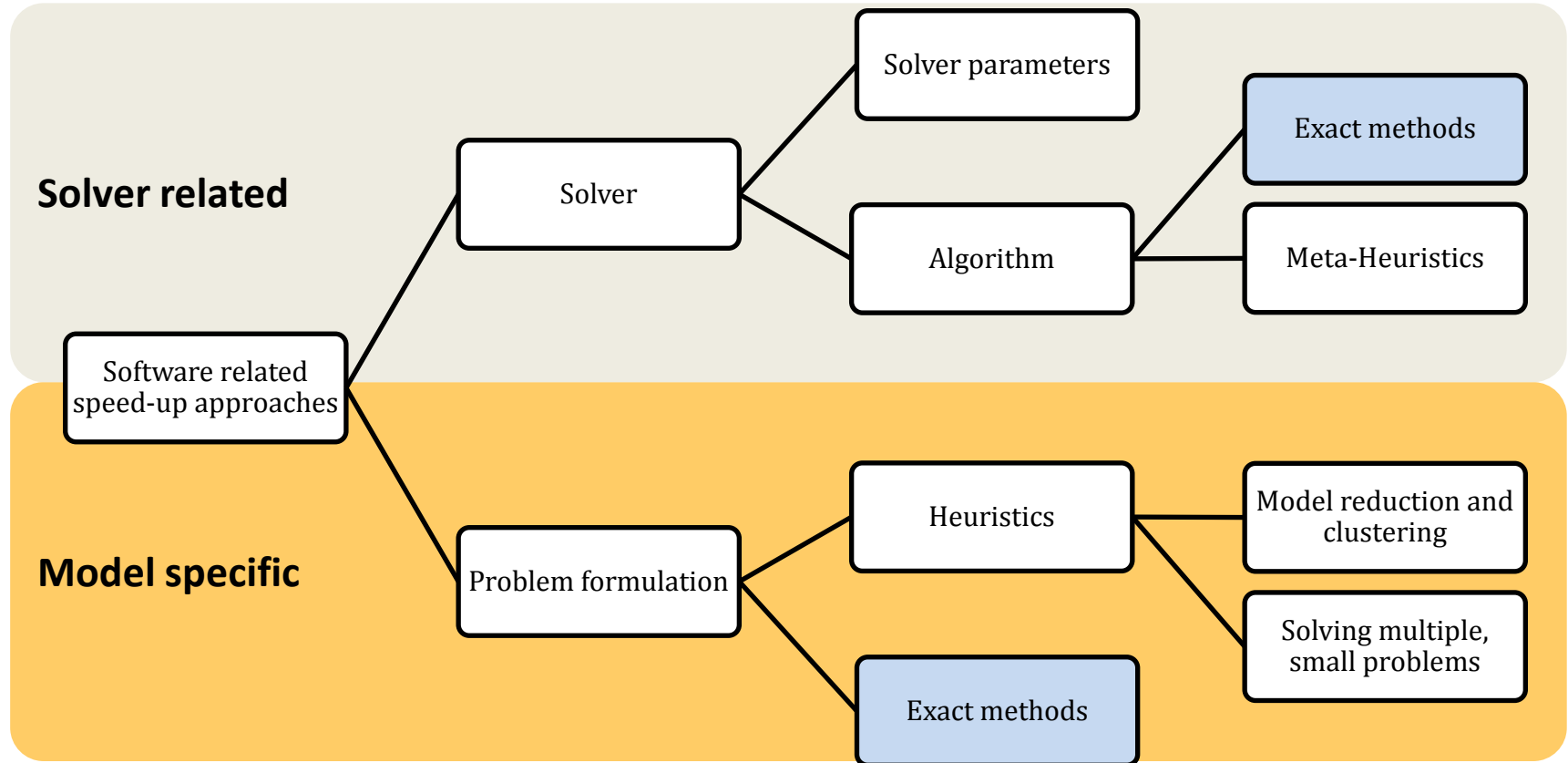
## Asynchronous Model

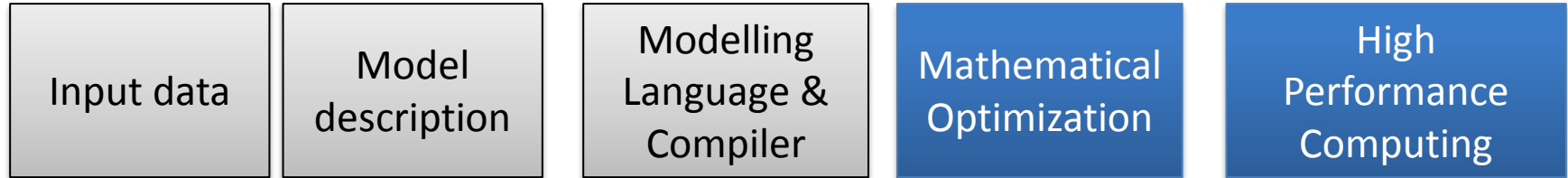




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# Categorization of speed-up approaches

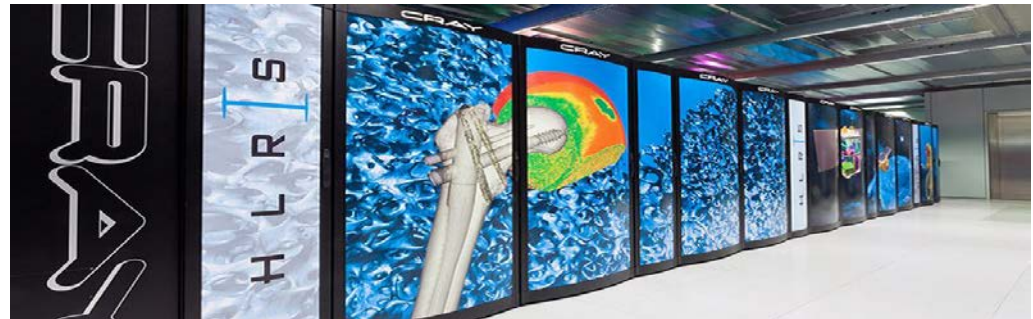




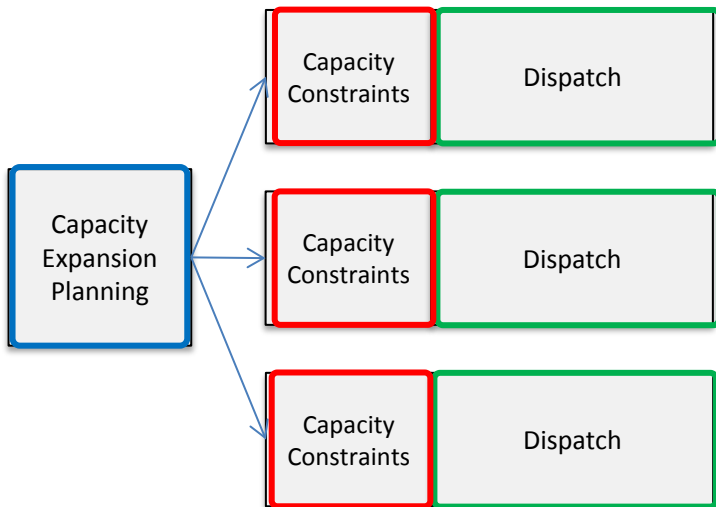
IBM Blue Gene/Q @ JSC:  
28,672 nodes / 458,752 cores

- Efficient HPC implementation
- Benchmarking and profiling
- Distributed storage for large ESMs
- Apply new concepts for assigning tasks to cores

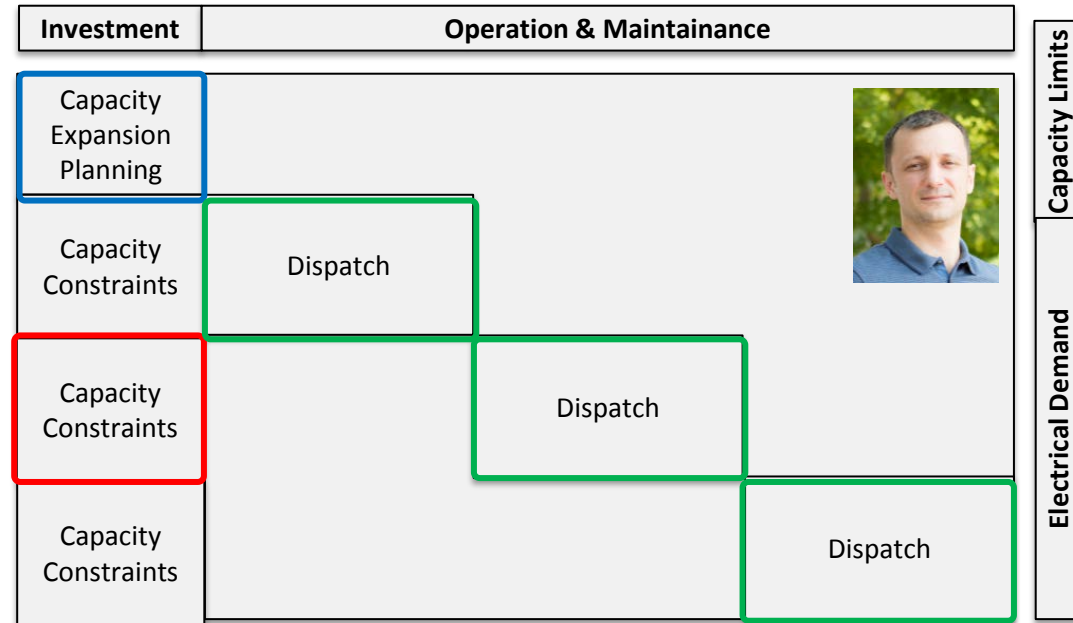
CRAY XC40 @ HLRS:  
3,944 nodes / 94,656  
cores



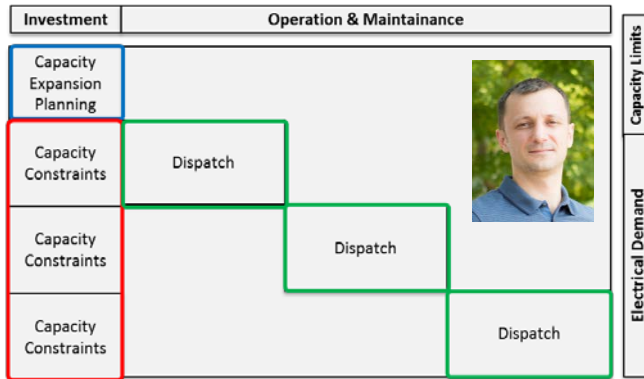
## Decomposition Approach



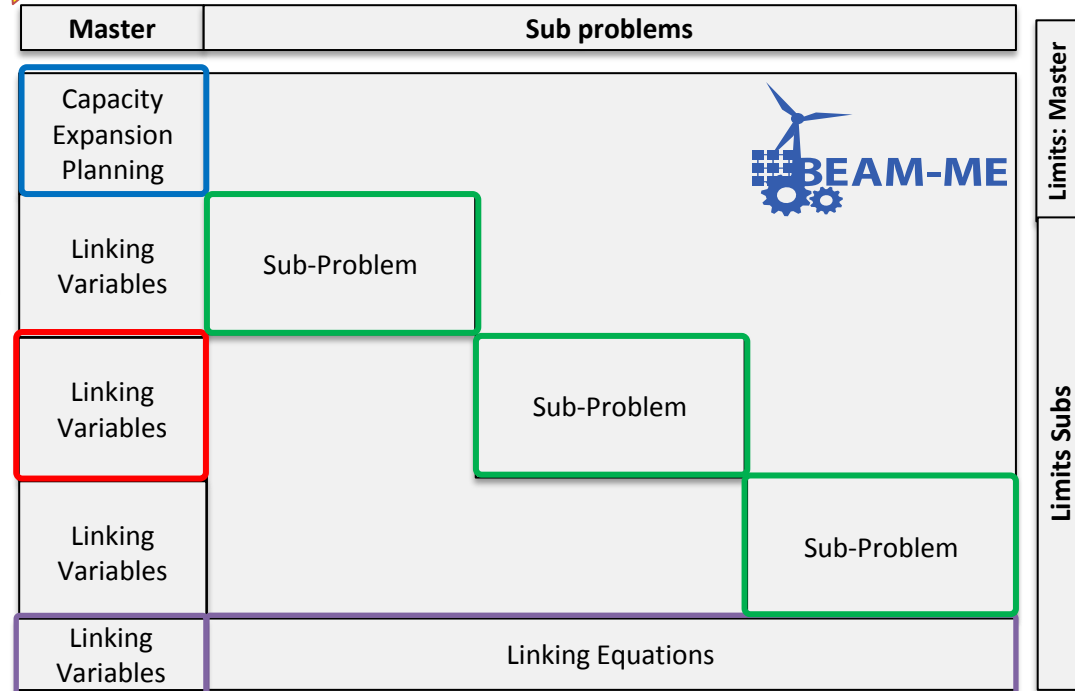
## PIPS-Solver (Argonne National Lab)



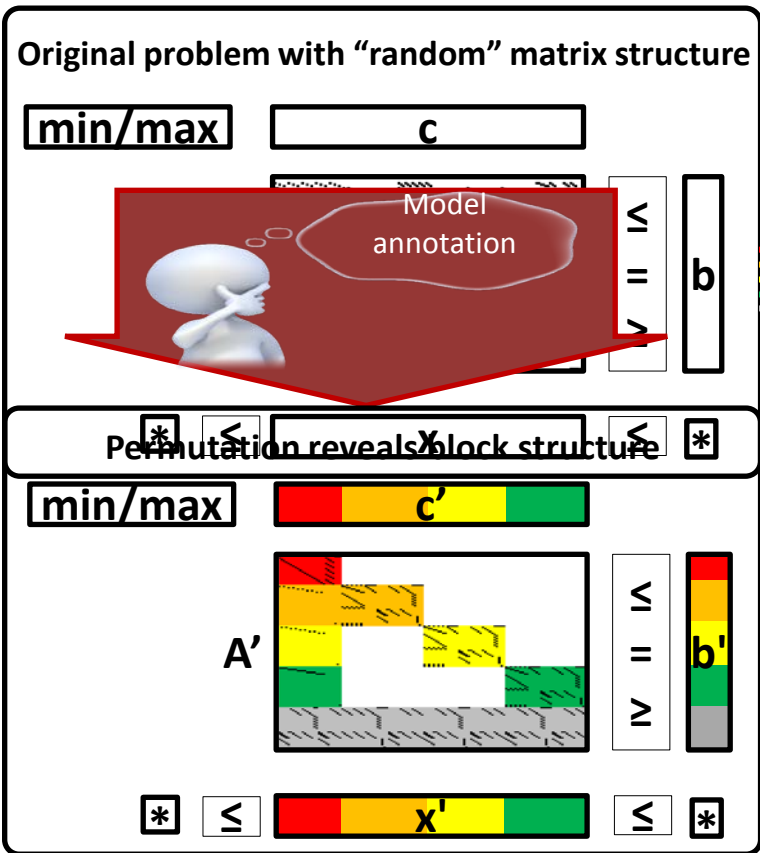
## PIPS-Solver



## New PIPS-IPM-Solver under development

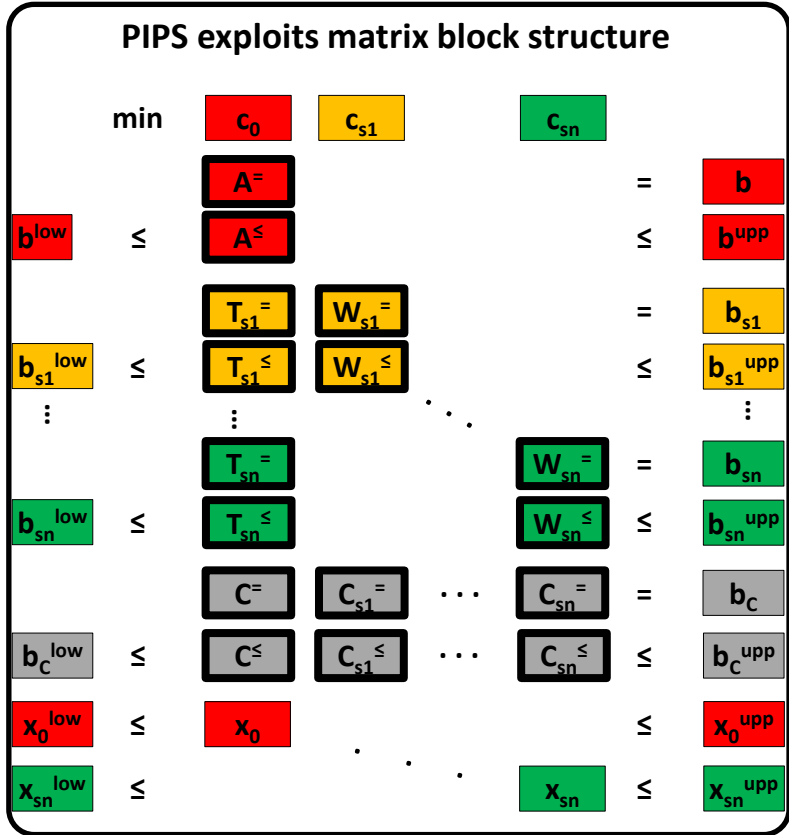


- New developed PIPS-IPM can be used for non stochastic models
- PIPS-IPM will also bring benefits to stochastic Modelling



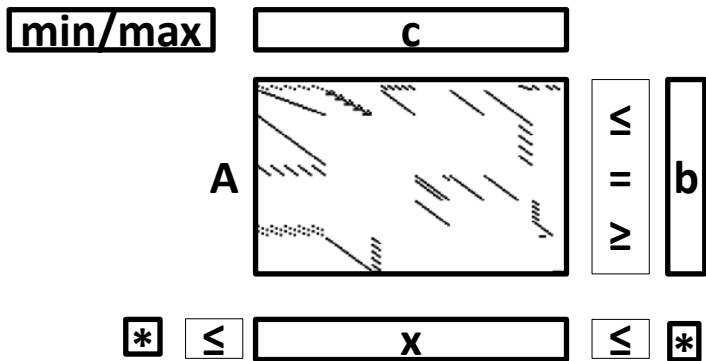
How to get there?

Model generation

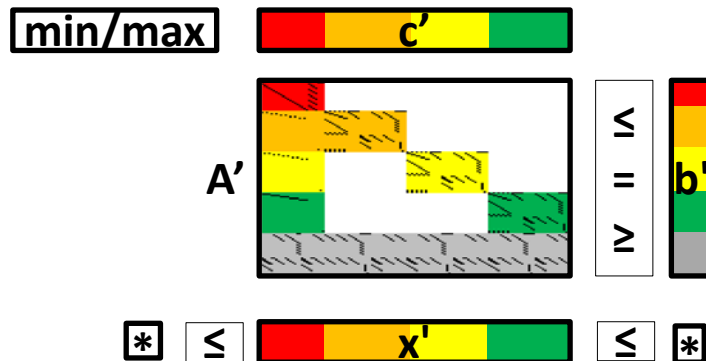




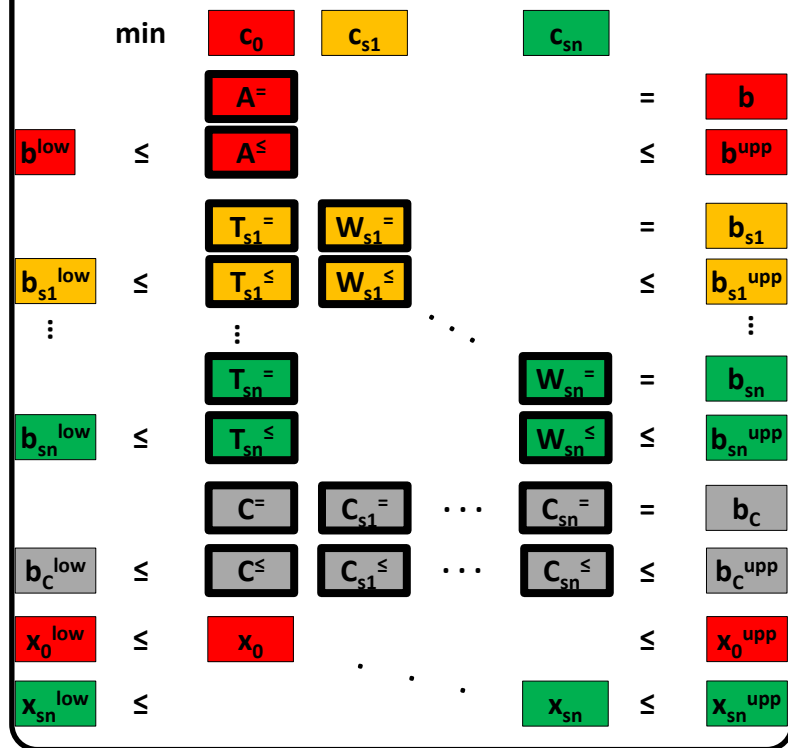
Original problem with "random" matrix structure



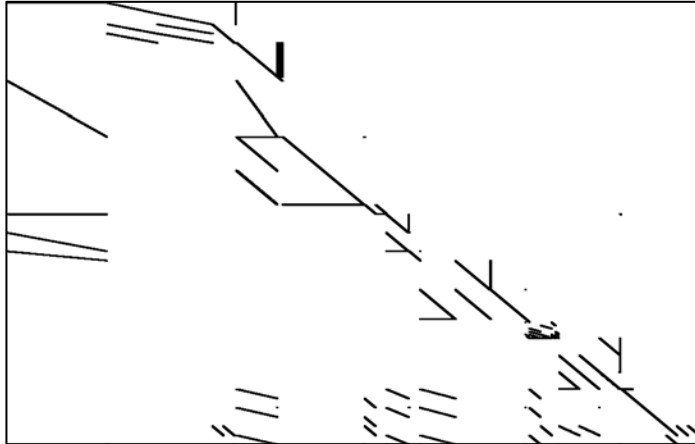
Permutation reveals block structure



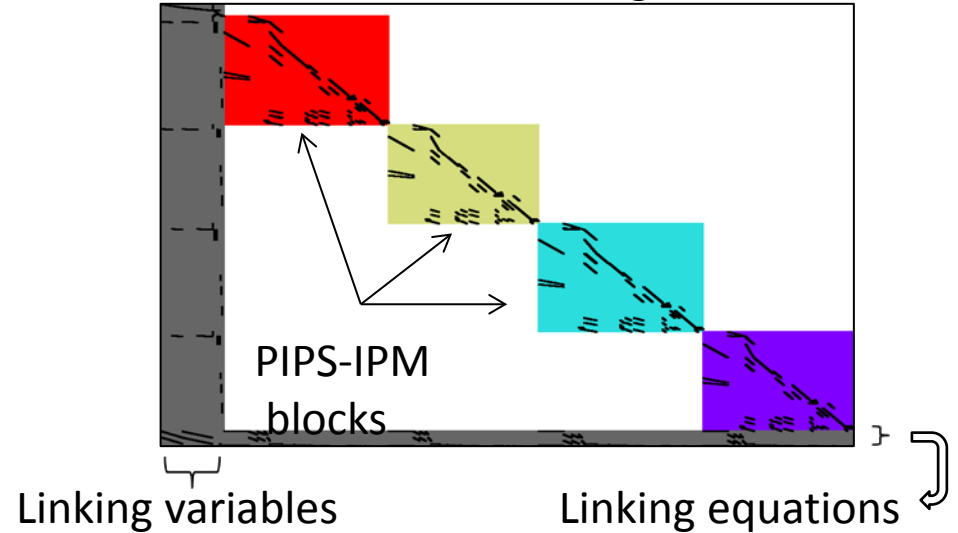
PIPS exploits matrix block structure



Matrix of **non-zero entries** of REMix LP



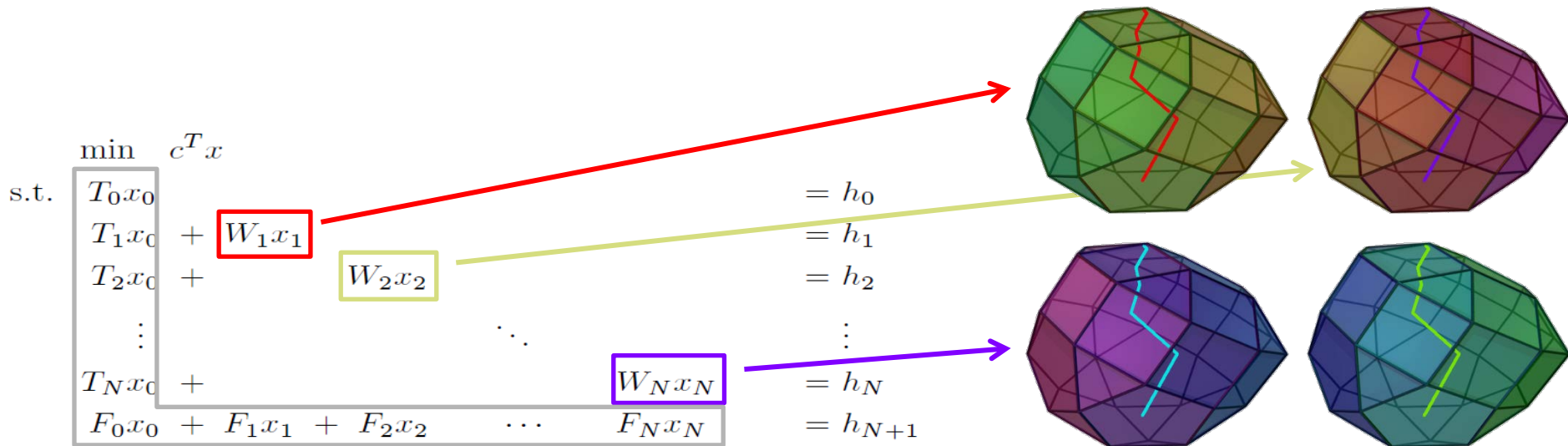
Permuted matrix revealing **block structure**



Annotation can be implemented directly in GAMS  
Modellers provide knowledge about problem and decompositions

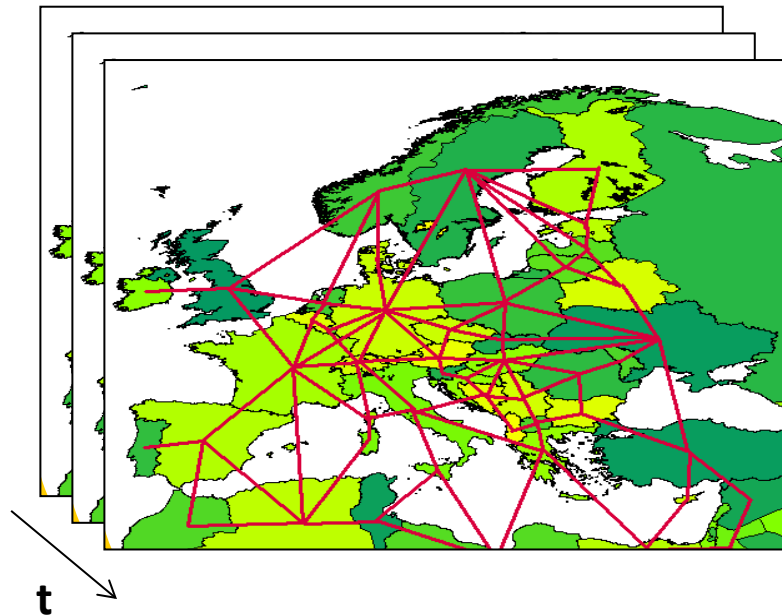
## Parallel Interior Point Solver – Interior Point Method (PIPS-IPM)

- Petra et al. 2014: *“Real-Time Stochastic Optimization of Complex Energy Systems on High-Performance Computers”*
- Wind feed-in planning in electrical power systems under uncertainty

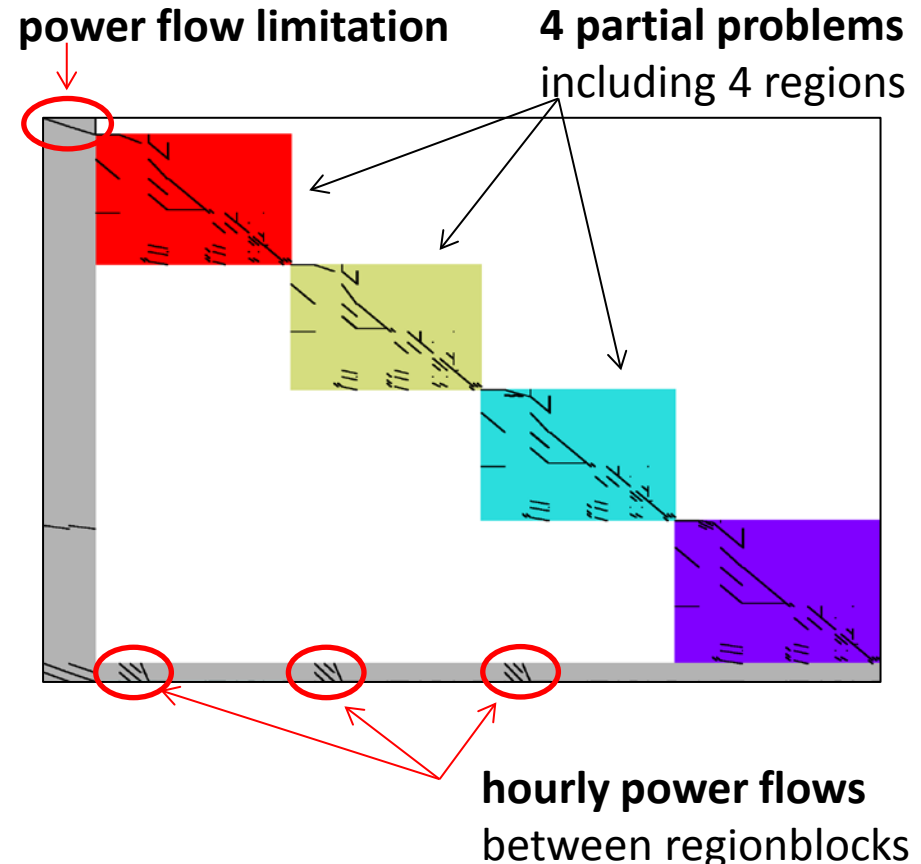


➔ OR 2017: D. Rehfeldt *“Optimizing large-scale linear energy problems with block diagonal structure by using parallel interior-point methods”*

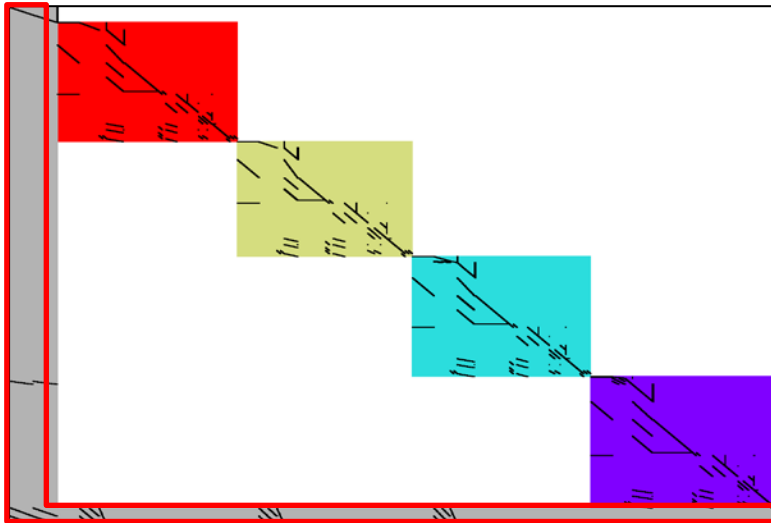
Linking by region: electricity transports, fuel transports, global constraints ( $\text{CO}_2$ )



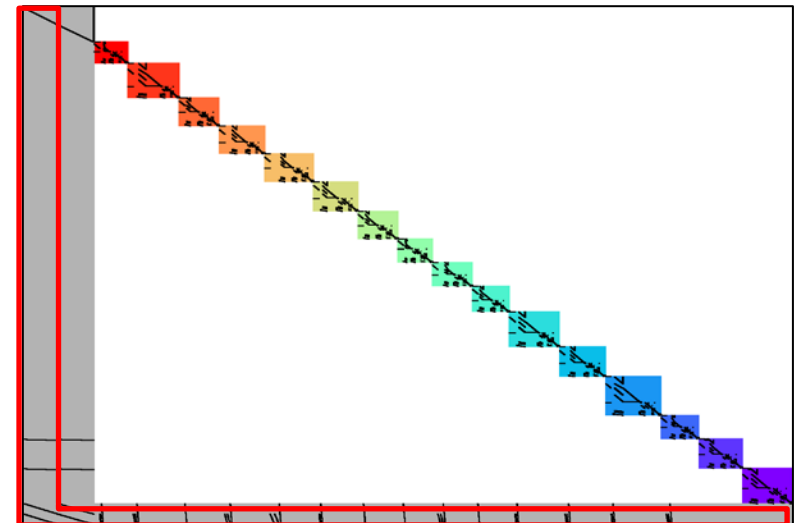
Temporal dimension of transport decisions leads to the largest number of linking variables



**4 partial problems**  
including 4 regions



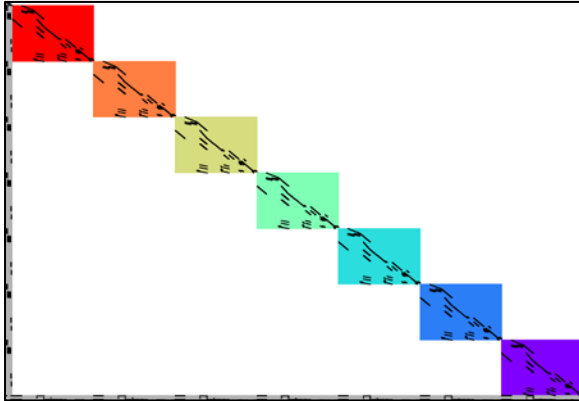
**16 partial problems**  
including 1 region



**low increase** in linking variables and constraints  
due to **sparsely connected** regions

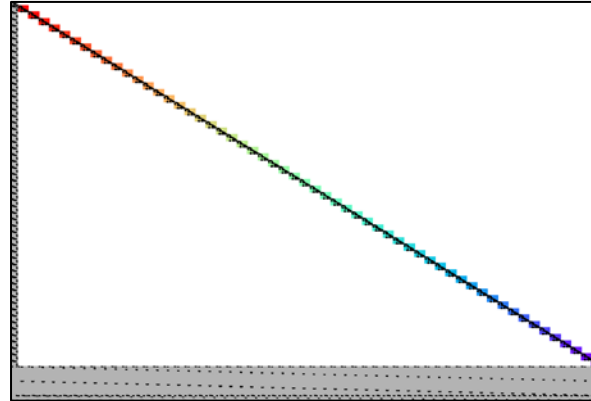
Target: Find **maximum number** of regionblocks of **similar size** which are **sparsely linked** to other regionblocks

**7 partial problems**  
including 24 time steps



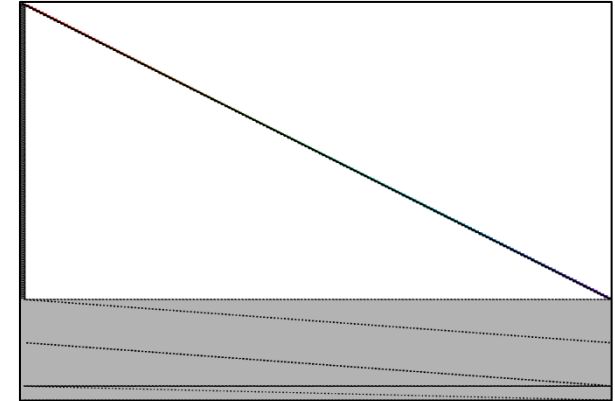
**1 out of 24** storage  
constraints linking

**56 partial problems**  
including 3 time steps



**3 out of 8** storage  
constraints linking

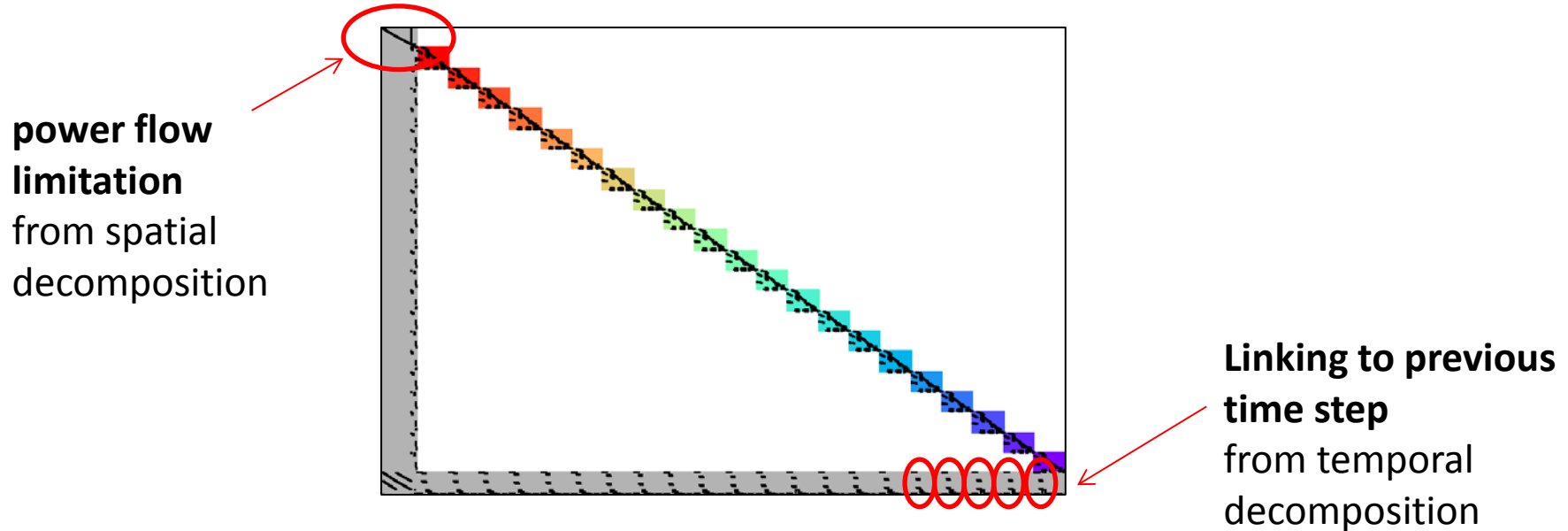
**168 partial problems**  
including 1 time step



**Every** storage  
constraint linking

Target: Find good **trade-off** between **number of time blocks** and  
**number of linking constraints**

Decomposition by **time and region** can be applied at the same time



All previously shown annotation plots describe exactly the **same ESM problem**  
→ **Systematic evaluation** of promising annotations required

Current state of extended PIPS-IPM for BEAM-ME test problems:

- sequentially 10 times slower than CPLEX 12.7.1.0 (latest version) barrier.
- can solve problems with few ( $< 1000$ ) linking constraints and variables faster than CPLEX (multi-threaded) when enough CPU-cores can be used (on several compute nodes).
- biggest problem solved so far has  $> 10$  million variables and constraints

Current challenges:

- LPs with many ( $> 100000$ ) linking constraints and variables hard to solve due to factorization of large dense matrix in solving process



- How to cut the model to allow for efficient application of solvers?
- How can PIPS-IPM use salient features of the problem?
- Identify options for „model tuning“ that work?
  
- algorithmic and implementation improvements, e.g. (parallel, structure-preserving) preprocessing, scaling, adaptation of interior-point algorithm
- handle dense (symmetric indefinite) matrix more efficiently:
  - try GPUs (e.g., MAGMA, cuSolver) for problems with not too many (< 10000) linking constraints and variables
  - try distributed linear algebra (e.g., Elemental, DPLASMA) for bigger problems

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**Benchmark: PIPS-IPM and PIPS must beat SIMPLEX in the first place**

- Model new markets and market design
- Increase spacial and temporal resolution
- Answer **new questions**
  - Improved market analysis
  - Regional potential of specific technologies
- Address **uncertainty** with **stochastic models**
  - Exploring solution space
  - Identifying tipping points between subsities
- Modelling sectors and **sector integration**

