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## Microscopic model for the magnetic subsystem in HoNi<sub>2</sub>B<sub>2</sub>C

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We demonstrate that the system of localized magnetic moments in  $HoNi_2B_2C$  can be described by the four-positional clock model. This model, at a proper choice of the coupling constants, yields several metamagnetic phases in magnetic field at zero temperature in full agreement with the experimental phase diagram. The model incorporates couplings between non-nearest neighbors in the direction perpendicular to the ferromagnetic planes. The same model leads to a *c*-modulated magnetic phase near the Curie temperature. The theoretical value of the modulation wave vector agrees surprisingly well with that observed by the neutrondiffraction experiment without new adjustable parameters. [S0163-1829(98)04410-5]

In Refs. 1 and 2 transport and magnetic measurements on HoNi<sub>2</sub>B<sub>2</sub>C for various magnetic fields and low temperatures have been reported. The magnetic phase diagram for HoNi<sub>2</sub>B<sub>2</sub>C with fields in the *a-b* plane is of particular interest. In this compound easy magnetization axes are identified with crystallographic directions  $\langle 110 \rangle$  and  $\langle 110 \rangle$ . The lowtemperature magnetization data show the existence of four meta-magnetic phases. The low-field phase has been identified by neutron-diffraction experiments<sup>3,5</sup> and magnetic measurements<sup>2</sup> with the antiferromagnetic phase, which we denote symbolically  $\uparrow \downarrow$ . The phase boundaries and magnetization in other phases versus magnetic field found in the experiment<sup>2</sup> can be readily explained by assuming that the remaining three phases are as follows: phase  $2 - \uparrow \uparrow \downarrow$ , phase  $3 - \uparrow \uparrow \rightarrow$ , and the high-field phase  $4 - \uparrow$ . It means that  $\frac{2}{3}$  of the spins in the phases 2 and 3 are parallel to one of the easy axes whereas the remaining  $\frac{1}{3}$  is antiparallel and perpendicular, respectively, to the same axis. Note that all metamagnetic phases are stoichiometric, i.e., the concentrations of spins parallel, antiparallel, or perpendicular to the reference axis are rational numbers. The phase diagram of HoNi<sub>2</sub>B<sub>2</sub>C at zero temperature is especially simple if the components of magnetic field  $\mathbf{H}||\langle 110 \rangle$ ,  $\mathbf{H}||\langle 110 \rangle$  are chosen as variables. The phase diagram of HoNi<sub>2</sub>B<sub>2</sub>C which follows from the experiment is shown in Fig. 1.

The structure of Lu and Ho 1:2:2:1 compounds was determined in Refs. 9 and 6 as the body-centered-tetragonal lattice with the space group I4/mmm. The x-ray structure analysis and the neutron-scattering experiments in Refs. 3–7 showed that incommensurate modulated magnetic structures with the wave vectors  $\mathbf{K}_c = 0.915 \mathbf{c}^*$  and  $\mathbf{K}_a = 0.585 \mathbf{a}^*$  occur in the temperature range 4.7-6 K. At temperatures below 4.7 K they vanish and antiferromagnetic reflections corresponding to alternating ferromagnetic a-b planes of Ho<sup>3+</sup> localized moments appear. Though the spatial arrangement of the phases  $\uparrow\uparrow\downarrow$  and  $\uparrow\uparrow\rightarrow$  cannot be directly derived from the magnetization measurements, it is unplausible that the ferro-

magnetic in-plane interaction changes suddenly by switching on of the magnetic field. Therefore, we believe that our symbols  $\uparrow\uparrow\downarrow$  and  $\uparrow\uparrow\rightarrow$  correspond to the real spatial sequences of in-plane magnetic moments.

In this article we present a simple microscopic model for magnetic subsystem in the 1:2:2:1 compound which explains all experimental observations. We accept a model of strong anisotropy in which a single-ion moment is directed presumably along four easy directions  $[\pm(1,1,0),\pm(1,\overline{1},0)]$  for the Ho and Dy compounds. Thus, the initially continuous moment **J** is reduced to a discrete variable taking only four values. This is a kind of the so-called clock model with four positions of the "hand."

The main argument in favor of the clock model is that the saturation magnetization in the range of fields larger than 7–10 T is directed not along the field, but along the closest to the field easy direction. It means that the applied field is still smaller than the anisotropy field  $H_A$ . The latter can be roughly estimated as 60 T. The corresponding anisotropy



FIG. 1. Magnetic phase diagram for HoNi<sub>2</sub>B<sub>2</sub>C.  $H_x$  axis corresponds to  $\langle 110 \rangle$  direction.

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energy for Ho<sup>3+</sup> magnetic moment ~10 $\mu_B$  is about 40 meV~400 K. Nevertheless, a single ion with integer J has no average moment in the ground state in the absence of external magnetic field. Indeed, the tunneling with a small amplitude w between adjacent positions of the "hand" leads to the ground state in which all four positions have equal probabilities. The ground state is separated by a finite energy gap equal to 2|w| from the first excited state. A detailed analysis of the single-ion properties will be published separately. Here we focus on the description of collective effects. For this purpose we introduce an angular variable  $\theta_{\mathbf{r}}$  at any lattice site **r** taking independently four values  $0, \pi/2, \pi, 3\pi/2$ . Neglecting the tunneling, the most general Hamiltonian compatible with the tetragonal symmetry is

$$H = \frac{1}{2} \sum_{\mathbf{r},\mathbf{r}'} \left[ K(\mathbf{r} - \mathbf{r}') \cos(\theta_{\mathbf{r}} - \theta_{\mathbf{r}'}) + L(\mathbf{r} - \mathbf{r}') \cos 2(\theta_{\mathbf{r}} - \theta_{\mathbf{r}'}) \right]$$
$$-h_x \sum \cos \theta_{\mathbf{r}} - h_y \sum \sin \theta_{\mathbf{r}}, \qquad (1)$$

here 
$$K(\mathbf{r})$$
 and  $L(\mathbf{r})$  are coupling constants and  $h_{x,y}$  are  
emponents of the magnetic field. We employ the reference

components of the magnetic field. We employ the reference frame in which axes coincide with the easy-axis directions. The higher harmonic terms are generated by the exchange interaction. Indeed, the operator of two particle permutation for spins *J* contains higher powers of the spin scalar product up to 2*J*. The dipolar interaction, in metamagnetic systems, is proportional to a small factor  $\exp(-2\pi c/a)$ ,<sup>10</sup> where *c* is interplane and *a* is in-plane lattice constants, and can be neglected. For the four-positional spins only the invariants  $\mathbf{S_1S_2} = \cos(\theta_1 - \theta_2)$  and  $(\mathbf{S_1S_2})^2 = [\cos(\theta_1 - \theta_2)]^2$  are independent.

Let us restrict the set of coupling constants to a few independent values. We assume that the in-plane interaction is characterized by one nearest-neighbor negative constant K with all other in-plane  $K_r$  and all in-plane  $L_r$  equal to zero. The in-plane interaction is assumed to be dominant to provide the in-plane ferromagnetic order. The interplane interaction is characterized by several constants  $K_n$ ,  $L_n$ . We shall see that interaction with several neighbors is essential.

All spins in each plane are parallel. Thus, the ground state is determined by minimization of a spin-chain Hamiltonian:

$$H = \sum_{i,=-\infty,n=1}^{\infty} \left[ K_n \cos(\theta_i - \theta_{i+n}) + L_n \cos^2(\theta_i - \theta_{i+n}) \right].$$
(2)

It should be noted that in the absence of an applied magnetic field it is known that the Néel antiferromagnetic state consists of alternating ferromagnetic *a-b* planes. This requirement is satisfied, if  $K_1 > 0$ . A natural desire to simplify the model leaving one or two independent coupling constants cannot be fulfilled. For example, if one leaves nonzero  $K_1$  and  $K_2$  and sets  $L_1, L_2$  and all the rest  $K_n, L_n(n \ge 3)$  to zero, two kinds of phase diagrams occur. The first diagram, Fig. 2(a), corresponds to  $0 < K_2 < K_1/2$  (the latter inequality is necessary to have the antiferromagnetic state in zero field). It contains six different phases. Due to the symmetry only the sector  $0 < h_y < h_x$  must be considered. Figure 2(b) corresponds to  $K_2 < 0$ . It is simpler and contains only three



FIG. 2. Magnetic phase diagrams. All the parameters are the same as in Fig. 1 except: (a)  $L_2=0.05$ ,  $K_3=L_3=0$ , and (b)  $K_2=-0.62$ ,  $K_3=L_3=0$ .

phases. Neither of the phase diagrams fits the experiment which clearly displays four phases as shown in Fig. 1. Other coefficients  $K_n$  and  $L_n$  must be incorporated to describe the experimental situation in HoNi<sub>2</sub>B<sub>2</sub>C. We shall show later that the coefficient  $L_3$  is not zero. Thus, we restrict our model to six nonzero coupling constants  $K_n, L_n, n = 1,2,3$ . This is a generalization of the so-called anisotropic nextnearest-neighbor Ising (ANNNI) model.<sup>11,12</sup> Our model differs from the standard ANNNI one by two features: the thirdneighbor interaction and the four positions of the hand instead of two.

In order to understand why the second- and third-neighbor interaction must be incorporated, one should compare energies of the simplest periodic sequences in the chain. The phases we anticipate to be realized as the ground states at different values of the field **h** are:  $\uparrow \downarrow$  (AF),  $\uparrow$  (F),  $\uparrow \uparrow \downarrow$  and  $\uparrow \uparrow \rightarrow$  (period 3). Others, having rather close energies, are  $\uparrow \rightarrow; \uparrow \uparrow \uparrow \downarrow, \uparrow \uparrow \uparrow \rightarrow, \uparrow \uparrow \downarrow \rightarrow, \text{ and } \uparrow \downarrow \uparrow \rightarrow; \uparrow \uparrow \downarrow \uparrow \downarrow, \uparrow \uparrow \uparrow \uparrow \downarrow,$ and  $\uparrow\uparrow\rightarrow\uparrow\rightarrow$ ;  $\uparrow\uparrow\uparrow\uparrow\downarrow\downarrow$  and  $\uparrow\downarrow\uparrow\rightarrow\leftarrow\rightarrow$ . We have found by numerical sorting that other phases have larger energies and can be omitted. With these 14 phases participating in the competition, a number of inequalities must be satisfied to ensure the existence of the experimentally observed phase diagram. Namely, on the phase boundaries the energies of the phases other than those being in equilibrium must be larger. For the reader's convenience the energies of the competing 14 phases are given in Table I. All are linear functions of the magnetic field. Therefore only their values at the corners of the phase diagram should be compared.

The general investigation of the phase diagram in the eight-dimensional space of  $K_n$ ,  $L_n$  and  $h_x$ ,  $h_y$  is too cumbersome. Instead we assume that the phase diagram has four phase boundaries, separating the experimentally established four phases, and find the constraints imposed by the experiment onto the model. The four phase boundaries found in the experiment are

$$AF \leftrightarrow \uparrow \uparrow \downarrow \leftrightarrow \uparrow \uparrow \rightarrow \leftrightarrow \quad F \leftrightarrow \uparrow \uparrow \downarrow.$$

According to Table I, these lines are described by the following equations, in the same respective order as above:

$$h_x = 2(K_1 - 2K_2 + 3K_3) \equiv H_{c10}, \qquad (3)$$

$$h_x + h_y = 2(K_1 + K_2) - 4(L_1 + L_2) \equiv \sqrt{2}H_{c20}, \qquad (4)$$

TABLE I. Competing phases and their energies.

Phase	Energy of the phase
AF (↑↓)	$-K_1+K_2-K_3+L_1+L_2+L_3$
F (†)	$K_1 + K_2 + K_3 + L_1 + L_2 + L_3 - h_x$
$\uparrow \rightarrow$	$K_2 - L_1 + L_2 - L_3 - (h_x + h_y)/2$
$\uparrow \uparrow \downarrow$	$-(K_1+K_2)/3+K_3+L_1+L_2+L_3-h_x/3$
$\uparrow\!\uparrow\!\rightarrow$	$(K_1+K_2+3K_3-L_1-L_2+3L_3-2h_x-h_y)/3$
↑↑↑↓	$L_1 + L_2 + L_3 - h_x/2$
$\uparrow \uparrow \uparrow \rightarrow$	$(K_1 + K_2 + K_3)/2 - (3h_x + h_y)/4$
$\uparrow \uparrow \downarrow \! \rightarrow$	$-K_2/2 - (h_x + h_y)/4$
$\uparrow\downarrow\uparrow\rightarrow$	$-(K_1-K_2+K_3)/2-(h_x+h_y)/4$
$\uparrow\uparrow\uparrow\uparrow\downarrow$	$(K_1+K_2+K_3)/5+L_1+L_2+L_3-3h_x/5$
$\uparrow \uparrow \downarrow \uparrow \downarrow$	$-(3K_1-K_2-K_3)/5+L_1+L_2+L_3-h_x/5$
$\uparrow\uparrow{\longrightarrow}\uparrow{\longrightarrow}$	$(K_1 + 3K_2 + 3K_3 - 3L_1 + L_2 + L_3 - 3h_x - 2h_y)/5$
↑↑↑↑↑↓	$(K_1+K_2+K_3)/3+L_1+L_2+L_3-2h_x/3$
$\uparrow\!\downarrow\!\uparrow\!\rightarrow\!\leftarrow\!\rightarrow$	$-(2K_1-K_2-L_1+L_2)/3-L_3-(h_x+h_y)/6$

$$h_x - h_y = 2(K_1 + K_2) + 4(L_1 + L_2) \equiv \sqrt{2}H_{c30}, \qquad (5)$$

$$h_x = 2(K_1 + K_2). \tag{6}$$

The latter three lines intersect in the triple point  $h_x^t = 2(K_1$  $+K_2$ ,  $h_v^t = -4(L_1 + L_2)$ . Note that Eqs. (3)-(5) are equivalent to empirical equations for the transition lines found in Ref. 2. Thus, the theory suggests a natural explanation of all functional dependences,  $H_{c1}(\theta)$ ,  $H_{c2}(\theta)$ , and  $H_{c3}(\theta)$ , found in the experiment. Here  $\theta$  is the angle between magnetic field and easy-axis direction. The phase diagram in the plane  $h_x$ ,  $h_y$  has an extremely simple shape (see Fig. 1). Note that all the above discussed functional dependences were derived from purely geometrical considerations. However, the very existence of the phase diagram with the four phases observed in the experiment is highly nontrivial and imposes strong constraints on the coupling constants. These constraints are expressed as a long series of inequalities. We present here the two most important of them with necessary comments on their meaning:

- (i)  $K_1 2K_2 + 3K_3 + 2(L_1 + 2L_2) + 6L_3 < 0$ . The AF and  $\uparrow \uparrow \downarrow$  phases have lower energy than the phase  $\uparrow \downarrow \uparrow$  $\rightarrow \leftarrow \rightarrow$  on the phase boundary  $h_x = H_{c10}$ .
- (ii)  $K_1 2K_2 + 3K_3 + 2(L_1 2L_2) + 6L_3 < 0$ . The phases  $\uparrow \uparrow \downarrow$  and  $\uparrow \uparrow \rightarrow$  have lower energy than the phase  $\uparrow \rightarrow$  on the phase boundary  $h_x + h_y = \sqrt{2}H_{c20}$ .

One can deduce from these inequalities that

$$K_1 - 2K_2 + 3K_3 + 2(L_1 + L_2) + 6L_3 < 0.$$

From Eqs. (3)–(5) we obtain

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$$L_{3} < -\left(\frac{H_{c01}}{12} - \frac{H_{c20} - H_{c30}}{12\sqrt{2}}\right). \tag{7}$$

With the experimental values  $H_{c10}=4.1$  kG,  $H_{c20}=8.4$  kG, and  $H_{c30}=6.6$  kG in inequality (7), we find the upper boundary for  $L_3:L_3<-0.24$  kG. Thus, the coupling constant  $L_3$  cannot be zero. The experimental data imply that the interaction between magnetic planes separated by three half-periods 3c/2 is essential. Taking this interaction into

account, we otherwise follow the principle of minimal interaction; we set as many as possible coupling constants to be zero. In particular, we set  $K_3 = L_2 = 0$ .

In the framework of our rough theory the magnetization in each phase does not depend on the magnetic field. It is equal to zero in the AF ( $\uparrow\downarrow$ ) phase. In the phase  $\uparrow\uparrow\downarrow$  it is directed along an easy axis closest to the direction of the magnetic field, and its absolute value is equal to 1/3 of the easy-axis saturation value. In the phase  $\uparrow \uparrow \rightarrow$  the magnetization is tilted by an angle  $\arctan(1/2) = 26.6^{\circ}$  to the easy axis closest to the magnetic field, and its absolute value is equal to  $\sqrt{5/3}=0.745$  of the easy-axis saturation value. In the ferro-phase  $\uparrow$  it is equal to 1 per site. In the experiment<sup>2</sup> the projection of magnetization onto the field direction was measured. According to the theory it is  $(1/3)\cos\theta$  for phase  $\uparrow\uparrow\downarrow$ (phase 2), 0.745  $\cos(\theta - 26.6^{\circ})$  in phase  $\uparrow \uparrow \rightarrow$  (phase 3), and  $\cos \theta$  in the ferro-phase. While theoretical values of the magnetization in phase 2 and the ferro-phase are in a good agreement with the experimental data, there is a discrepancy between the theoretical and experimental magnetization of phase 3 [see Fig. 5(c), in Ref. 2]. In particular, in the experiment there is no maximum of  $M_{s2}(\theta)$  at  $\theta = 26.6^{\circ}$  as the theory predicts. Instead the saturation magnetization decreases monotonically with the angle in the interval  $15^\circ < \theta$  $<45^{\circ}$ . The reason can be that the determination of the  $M_{s2}$ at a small angle is very unreliable since the plateau is not clearly pronounced. On the other hand, the values of magnetization at orientations closer to the easy axis, where the plateau is well pronounced, are in a good agreement with the theory. Finally, the relative difference of the magnetization at a maximum ( $\theta = 26.6^{\circ}$ ) and at  $\theta = 45^{\circ}$  is only 5% which may be beyond of the precision of the model without the tunneling taken into account (w=0).

From Eqs. (3)-(5) one can find

$$K_1 = 4.22$$
 kG,  $K_2 = 1.08$  kG,  
 $L_1 = -0.32$  kG,  $L_3 = -0.46$  kG. (8)

Thus, we demonstrated that the low-temperature magnetization data and corresponding phase diagram can be naturally described in the framework of the four-position clock model with the values of the constants given by Eq. (8).

Now we consider a vicinity of the Curie temperature. We will show that the modulation along the *c* direction naturally appears in the framework of the same model. The order parameter (magnetization in a plane) is small near this temperature allowing one to neglect the terms with the  $\cos 2(\theta_n - \theta_{n'})$  in Hamiltonian (2), proportional to the fourth power of the order parameter **s**. The chain interaction Hamiltonian becomes

$$H = \sum_{i=-\infty}^{\infty} \sum_{n=1}^{3} K_n \mathbf{s}_i \cdot \mathbf{s}_{i+n} \,. \tag{9}$$

The quadratic Hamiltonian (9) can be represented in terms of Fourier-components  $\mathbf{s}_q = N^{-1/2} \Sigma_{n=1}^N e^{iqn} \mathbf{s}_n$ :

$$H = \sum_{q} K_{q} \mathbf{s}_{q} \cdot \mathbf{s}_{-q} \tag{10}$$

with  $K_q = K_1 \cos q + K_2 \cos 2q$ . The value  $K_q$  has the absolute minimum at  $q = \arccos(-K_1/4K_2)$ , if  $|K_1| < 4|K_2|$ . For

our data  $K_1/(4K_2) = 0.977$  and  $q = 167^\circ = 0.93c^*$ . Comparing the theoretical value to the experimental one  $q = 0.915c^*$ , we find the agreement to be surprisingly good, maybe too good. We can introduce the constant  $K_3$  to compensate a small discrepancy. The value  $K_3$  established in this way is -0.023. Though this value is not reliable, it shows

that our minimal value was close to reality. No modulated magnetic phase has been found for the Dy compound.<sup>13</sup> From our point of view it means that  $K_1/(4K_2) > 1$  in this compound.

An important remark is in order: several phases which do not occur in the phase diagram have energies very close to the ground-state energy. This means that a small perturbation (stress) can change the phase diagram drastically.

The next step toward a more realistic theory would be to incorporate the nonzero tunneling amplitude w. The crystal electric-field spectrum numerical calculations<sup>14</sup> for this amplitude give the magnitude  $w \approx 3$  kG, which is not small, especially in comparison to  $L_1$  and  $L_2$ . The incorporation of the tunneling amplitude, probably weakens the strong limitations imposed by the inequalities. We have performed a variational calculation of the ground state for the extended

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model including w in the Hartree approximation. They will be published elsewhere.

Another important and not yet resolved question is the origin and the behavior of the *a* modulation with the wave vector  $0.585a^*$ . It appears not only in the Ho compound, but also in Er, Tm, and Tb.<sup>15</sup> Its wave vector is very conservative. Therefore, it is tempting to ascribe it to a spin-density wave in the conductivity electrons. This idea is supported by an observation of good nesting on the numerically calculated Fermi surface.<sup>16</sup> However, such a treatment does not agree with the fact that in the Ho compound the a and c modulations appear and disappear in the same temperature interval. Rathnayaka et al.<sup>1,8</sup> have found an additional phase transition in the same temperature interval. It can be considered as an implicit indication of the independence of these order parameters. From a theoretical point of view, there is no reason for them to appear in the same point. However, direct neutron-diffraction measurements do not distinguish the temperature where these modulations appear.

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