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# Earthquake-induced rotational ground motions from G-Pisa ring laser gyroscope 

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## Chapter 1

## Introduction and aim

Seismologists have measured for decades the translational components of ground motion due to different kind of sources (both natural and artificial). These components are usually referred as N (north-south) E (east-west) and Z (vertical) or R (radial), T (tangential) and Z (vertical). A complete representation of ground motion induced by earthquakes needs not only these three translational components but also six components of strain and three components of rotational motion (Aki and Richards, 2002). The latter has always been very difficult to measure, because of the small amplitudes even in the vicinity of the source. Various attempts to measure rotational motion induced by earthquakes have been made in the history of seismology. Pioneering studies in this sense are those carried out by Cecchi (1876) and Galitzin (1912), who proposed different ways to perform such measurements. Despite these first attempts, the widespread belief that rotational motions were insignificant had continued for many years later. For example Richter himself 1958 in one of his footnotes wrote: "Theory indicates, and observation confirms, that such rotations are negligible". But at that time, as we said, there were no instrument sensitive enough to measure rotational motions with a resolution better than few microradians per second. More recently, using an azimuthal array of seismographs, Droste and Teisseyre (1976) derived rotational seismograms of rock bursts from a nearby mine. Nigbor (1994) studied rotational effects recorded in the near-field of explosions using a triaxial translational accelerometer and a solid-state rotational velocity sensor. The same sensor has been used by Takeo (1998) for recording an earthquake swarm on Izu peninsula, Japan. However,
because of the limitation of the instrument sensitivity, this kind of sensor was only able to sense the rotational ground motion near the earthquake sources or other artificial sources. This explains why Aki and Richards (2002) stated "...as of this writing seismology still awaits a suitable instrument for making such measurements".

In the last years, thanks to the development of laser technology, a new kind of instrument began to be available. Ring-laser gyroscopes, working on Sagnac effect are providing an interesting tool to investigate rotational ground motion (Schreiber, 2006; Stedman, 1997). Several observations have been made with this instruments, starting from Stedman et al. (1995), McLeod et al. (2009) and Pancha et al. (2000) that have reported a sufficient sensor sensitivity to record rotational motion for seismology. Rotational motion induced by earthquakes has been measured intensively with the ring-laser gyroscope installed at the fundamental station Wettzell, Germany (Cochard et al., 2006; Gebauer et al., 2012; Igel et al., 2005, 2007). These authors showed the great correlation between gyrolaser (rotational motion) and collocated seismic sensor (translational motion) recordings, both in amplitude and in phase, as predicted by theory. Phase velocity and direction of propagation of the seismic wavefield have also been investigated (Gaebler, 2010; Igel et al., 2005, 2007; Kurrle et al., 2010; Suryanto, 2006) using collocated measurement of rotation and translation. Another way to estimate rotations have been proposed by some authors using array of seismic sensors (Bodin, 1997; Huang, 2003; Spudich and Fletcher, 2008; Spudich et al., 1995), comparisons between this kind of estimations and direct measurement of rotation from Wettzell gyrolaser has also been carried out by Suryanto et al. (2006) and have shown good agreement, but with important limitations due to the assumptions behind the array-derived rotation rate method.

This thesis focuses on the data collected by the G-Pisa ring-laser gyroscope, developed by the University of Pisa (Department of Physics) and INFN (Belfi et al., 2011, 2012b; Di Virgilio et al., 2010). This instrument has been operating for almost 2 years at the European Gravitational Observatory in Cascina (Pisa), in the framework of the VIRGO project. In particular, I report the very first seismic analysis of the rotational data from a gyrolaser lying in the vertical plane, which is sensitive to rotation about a horizontal axis (tilt). The main part of the thesis is dedicated to the analysis of the Mw=9.0, March 11th, 2011, Japan earthquake; in addition, I also account for recordings from some events
occurred at regional distances.
The first objective of this work is to characterize the performance of G-Pisa in relation to a collocated accelerometer and to verify the ground-coupling of the instrument. By calculating the power spectral density (PSD) of rotation rate and acceleration I first identify the signal to noise ratio as a function of frequency and, by computing time-frequency transforms (spectrograms), I individuate the most energetic frequency bands as a function of time for both the instruments during several selected earthquakes. Then, rotation rates and accelerations are correlated within subsequent frequency bands, in order to quantify similarity between the signals. The second objective of the thesis is to compare the recorded rotation rates with those obtained through an array-based analysis. Applying the seismo-geodetic method by Spudich et al. (1995), I derive the rotation rate from a tripartite array of three-components accelerometers. This method provides an independent estimation of ground rotations that should be in agreement with that directly recorded by the gyrolaser. Results from this analysis show that the two measurements are in general agreement; I attribute the discrepancies to both the geometrical setting of the array and the band limitations of its sensors. The third objective concerns phase velocities estimation and derivation of surface waves dispersion curves from collocated measurements of rotation and translation. Following Igel et al. $(2005,2007)$ and Kurrle et al. $(2010)$, I address this issue by calculating the zero-lag correlation coefficient between translational and rotational traces. When the correlation coefficient is above an arbitrary threshold, phase velocity is obtained through a linear regression within overlapping sliding time windows. Iterating the procedure after a narrow band-pass filtering of both traces, it is possible to derive a dispersion curve for the selected wave packet. A theoretically equivalent dispersion curve could be derived in frequency domain as shown by Suryanto (2006), both for Loveand Rayleigh-waves, simply by calculating the spectral ratios between translation and rotation. I implemented this second procedure using a multitaper method (MTM, Thomson (1982)), in order to reduce variance and bias by averaging periodograms obtained using a properly-designed taper. The dispersion curves calculated in this manner are compared to those obtained with a multi-frequency Plane Wave Fit (PWF) analysis (Del Pezzo and Giudicepietro, 2002). This method, that consists in estimating wavefield slowness for an array of sensors, provides independent information about velocities and direction
of propagation (azimuth) for plane waves crossing the array. Rayleigh-waves dispersion curves derived from the Japan earthquake, are then compared against the theoretical phase velocities derived from a standard (AK135) Earth Model (Kennett et al., 1995). Since Rayleigh-waves are fully recorded by the gyrolaser only when their direction of propagation is perpendicular to G-Pisa area vector, I implemented a rotation rate signal correction method that takes into account the different directions of propagation of Rayleigh-waves (as estimated from PWF inversion) with respect to G-Pisa axis of sensitivity. This correction leads to a more reliable result in estimating phase velocities, that otherwise would be overestimated. Collocated measurements of rotation about vertical axis and transverse acceleration for horizontally-polarized seismic waves (SH- and Love-waves) allow estimating direction of propagation and azimuth of the incoming wavefield. Following Igel et al. (2007) and Hadziioannou et al. (2012) I conducted these estimates for Love waves recorded when G-Pisa was configured with the area vector oriented vertically.

This thesis is organised into five chapters. In the first chapter, I briefly report the general theory behind rotational motions, and present the relationships between rotation and translation in the context of classical elasticity. Here I show that surface-waves phase velocities and thus dispersion curves can be obtained from collocated measurements or rotation and translation. In the second chapter I present the instrumentation and data, with particular reference to G-Pisa and its ability to investigate both Rayleigh-and Lovewaves with a sensitivity on the order of a few $\mathrm{nrad} / \mathrm{s} / \sqrt{\mathrm{Hz}}$ over the $0.02-1 \mathrm{~Hz}$ frequency band. In the third chapter I describe the data analysis methods, and their practical implementation in terms of Matlab scripts. In the fourth chapter I present and critically comment the results from the analysis. This chapter is divided into two sections, dedicated respectively to the Love- and Rayleigh-waves results. The last chapter is dedicated to the general discussion and conclusions.

## Chapter 2

## Basic theory

### 2.1 Introduction

Here I briefly describe the background theory of seismic rotations. All the discussion is based on classical elasticity for which the stress and strain tensors are symmetric. As pointed out by Lee et al. (2009) near field observations report rotational motions which are from 10 to 100 times larger than what expected from classical elasticity theory. Theoretical work suggests that in granular materials or cracked continua asymmetries of the stress and strain tensors can create rotations separate from those predicted by classical elastodynamic theory (Pujol, 2009; Teisseyre, 2009, 2012; Teisseyre et al., 2006).

In the framework of classical elasticity and assuming infinitesimal deformations, following Cochard et al. (2006) the displacement of a point at $\mathbf{x}$ is related to that of a neighbouring point $\mathbf{x}+\delta \mathbf{x}$ by (Aki and Richards, 2002):

$$
\begin{align*}
\mathbf{u}(\mathbf{x}+\delta \mathbf{x}) & =\mathbf{u}(\mathbf{x})+\mathbf{G} \delta \mathbf{x} \\
& =\mathbf{u}(\mathbf{x})+\boldsymbol{\varepsilon} \delta \mathbf{x}+\mathbf{\Theta} \delta \mathbf{x}  \tag{2.1}\\
& =\mathbf{u}(\mathbf{x})+\boldsymbol{\varepsilon} \delta \mathbf{x}+\boldsymbol{\theta} \times \delta \mathbf{x}
\end{align*}
$$

where $\mathbf{G}, \boldsymbol{\varepsilon}, \boldsymbol{\Theta}$ are the gradient, strain, and rotation second order tensors, respectively,
and

$$
\boldsymbol{\theta}=\left(\begin{array}{c}
\theta_{x}  \tag{2.2}\\
\theta_{y} \\
\theta_{z}
\end{array}\right)=\frac{1}{2} \nabla \times \mathbf{u}(\mathbf{x})=\left(\begin{array}{c}
\frac{\partial u_{z}}{\partial y}-\frac{\partial u_{y}}{\partial z} \\
\frac{\partial u_{x}}{\partial z}-\frac{\partial u_{z}}{\partial x} \\
\frac{\partial u_{y}}{\partial x}-\frac{\partial u_{x}}{\partial y}
\end{array}\right)
$$

is a (pseudo-) vector which does not enter Hooke's law and represents the angle of rigid rotation generated by the disturbance. This illustrates that one needs three components of translation, six components of strain and three components of rotation to fully characterize the change in the medium around point x .

Starting from Hooke's Law

$$
\begin{equation*}
\sigma_{i j}=\lambda \delta_{i j} \sum_{k=1}^{3} \varepsilon_{k k}+2 \mu \varepsilon_{i j} \tag{2.3}
\end{equation*}
$$

where $\sigma_{i j}$ and $\varepsilon_{i j}$ are generic component of the stress and strain tensors respectively, $\sum_{k=1}^{3} \varepsilon_{k k}=\frac{\partial u_{x}}{\partial x}+\frac{\partial u_{y}}{\partial y}+\frac{\partial u_{z}}{\partial z}=\nabla \mathbf{u}, \lambda, \mu$ are the Lamè constants and $\delta_{i j}$ is the Kronecker delta that assumes value 1 when $i=j$ and 0 otherwise. If we consider the free surface lying on the xy plane and under the zero traction boundary condition (e.g. $\left.\sigma_{i z}=0 \quad(i=x, y, z)\right)$, direct application of Eq.2.3 in a homogeneous, isotropic medium leads to

$$
\begin{align*}
\frac{\partial u_{x}}{\partial z} & =-\frac{\partial u_{z}}{\partial x} \\
\frac{\partial u_{y}}{\partial z} & =-\frac{\partial u_{z}}{\partial y}  \tag{2.4}\\
\frac{\partial u_{z}}{\partial z} & =-\frac{\lambda}{\lambda+2 \mu}\left(\frac{\partial u_{x}}{\partial x}+\frac{\partial u_{y}}{\partial y}\right)
\end{align*}
$$

and from 2.2 we get:

$$
\begin{align*}
\theta_{x} & =\frac{\partial u_{z}}{\partial y} \\
\theta_{y} & =-\frac{\partial u_{z}}{\partial x}  \tag{2.5}\\
\theta_{z} & =\frac{1}{2}\left(\frac{\partial u_{y}}{\partial x}-\frac{\partial u_{x}}{\partial y}\right)
\end{align*}
$$

The above equations give us the expression for rotation angles with respect to displacement gradient elements, under the assumptions of plane wave propagation, and zero traction boundary condition, in the next sections we are going to look at the relationship between these angles and translational components of motion for the two main types of surface waves, Love and Rayleigh-waves, to derive simple formulas that link rotation and translation. We will see that in both cases, these two quantities are scaled by phase velocity, and that in principle, one can extract it by collocated measurement of rotation and translation.

### 2.2 Love-waves

Love-waves are horizontally polarized surface waves generated by interaction of SH-waves with the free surface (Fig. 2.1).

Being transversely polarized, the displacement for a wave propagating along X -axis can be expressed by

$$
\begin{equation*}
\mathbf{u}(x, y, z, t)=\left(0, u_{y}\left(t-x / C_{L}\right), 0\right) \tag{2.6}
\end{equation*}
$$

with $C_{L}$ being horizontal phase velocity. Love-waves induce rotations about Z-axis that using 2.2 can be expressed by

$$
\begin{equation*}
\theta_{z}=\frac{1}{2} \frac{\partial \dot{u}_{y}}{\partial x}=-\frac{\dot{u}_{y}\left(t-x / C_{L}\right)}{2 C_{L}} \tag{2.7}
\end{equation*}
$$

## Love Wave



Figure 2.1: The particle motion of Love-waves
and for rotation rate

$$
\begin{equation*}
\Omega_{z}=\frac{\partial \theta_{z}}{\partial t}=-\frac{\ddot{u}_{y}\left(t-x / C_{L}\right)}{2 C_{L}} \tag{2.8}
\end{equation*}
$$

this means that transverse acceleration and rotation rate about Z-axis are in phase and scaled by a factor $-\frac{1}{2 C_{L}}$. A ring-laser set in horizontal configuration is sensitive, in principle, only to rotation about vertical axis, that means, only to Love and SH waves that are horizontally polarized.

### 2.3 Rayleigh-waves

Rayleigh-waves are effectively surface waves characterized by a retrograde elliptic motion confined in the vertical plane containing the direction of propagation (Fig. 2.2). Rayleighwaves can therefore be recorded both by the vertical component and by the horizontal
component of a seismic sensor.

## Rayleigh Wave



Figure 2.2: The particle motion of Rayleigh-waves

For a simple half-space Poisson solid, the Rayleigh-waves displacements propagating along X-axis at zero depth are given by Lay and Wallace (1995) as:

$$
\begin{align*}
& u_{x}=-\alpha A k \sin (\omega t-k x)  \tag{2.9}\\
& u_{z}=\beta A k \cos (\omega t-k x)
\end{align*}
$$

where A is the P -wave amplitude, $\omega$ is the angular frequency, $x$ is distance, $k$ is the Rayleigh wavenumber and $\alpha=0.42$ and $\beta=0.62$ are constants for the Poisson solid. Following Lin et al. (2011) we refer to X and Z directions as radial and vertical. In addition, Z direction is positive down. The velocity and acceleration of the particle motions along the X -axis and Z -axis are then:

$$
\text { Velocity }\left\{\begin{array}{l}
\dot{u}_{x}=-\alpha A k \omega \cos (\omega t-k x)  \tag{2.10}\\
\dot{u}_{z}=-\beta A k \omega \sin (\omega t-k x)
\end{array}\right.
$$

$$
\text { Acceleration }\left\{\begin{array}{l}
\ddot{u}_{x}=\alpha A k \omega^{2} \sin (\omega t-k x) \\
\ddot{u}_{z}=-\beta A k \omega^{2} \cos (\omega t-k x)
\end{array}\right.
$$

Using 2.5, we can obtain the rotation angle around Y-axis for Rayleigh-waves:

$$
\begin{equation*}
\theta_{y}=-\beta A k^{2} \sin (\omega t-k x) \tag{2.11}
\end{equation*}
$$

and differentiating with respect to time we get rotation rate as:

$$
\begin{equation*}
\Omega_{y}=\dot{\theta_{y}}=-\beta A k^{2} \omega \cos (\omega t-k x) \tag{2.12}
\end{equation*}
$$

If we now look at the relationship between translations along X-axis ( $\dot{u}_{x}, \ddot{u}_{x}$ ) and rotations about Y-axis $\left(\theta_{y}, \Omega_{y}\right)$

$$
\begin{align*}
& \frac{\ddot{u_{x}}}{\Omega_{y}}=-\frac{\alpha}{\beta} \frac{\omega}{k} \frac{\sin (\omega t-k x)}{\cos (\omega t-k x)}  \tag{2.13}\\
& \frac{\ddot{u_{x}}}{\theta_{y}}=-\frac{\alpha}{\beta} \frac{\omega^{2}}{k}=-\frac{\alpha}{\beta} C_{R} \omega  \tag{2.14}\\
& \frac{u_{x}}{\Omega_{y}}=\frac{\alpha}{\beta} \frac{1}{k} \tag{2.15}
\end{align*}
$$

We can see from 2.13 that X -axis acceleration and Y -axis rotation rate are phase shifted by $90^{\circ}$ and scaled by the phase velocity, 2.14 shows that X -axis acceleration and Y-axis rotation angle are in phase and scaled by phase velocity multiplied by frequency.

Equation 2.15 tells us that X-axis velocity and Y-axis rotation rate are in phase and scaled by the inverse of wavenumber.

Instead by comparing translation along Z-axis and rotation about Y-axis

$$
\begin{equation*}
\frac{\ddot{u_{z}}}{\Omega_{y}}=\frac{\omega}{k}=C_{R} \tag{2.16}
\end{equation*}
$$

we can observe that the two quantities are in phase and amplitude are scaled by a factor $C_{R}$ that is Rayleigh-waves phase velocity.

### 2.4 Applications

In the previous sections we showed that collocated measurements of rotation and translation can provide additional information about seismic wavefield. Here we briefly discuss some possible application of this method. First of all, the possibility of examining seismic wave phase velocities, as described by Igel et al. (2005, 2007) and Suryanto (2006) from collocated measurements, remains one of the most interesting application that could allow to derive surface waves dispersion curve (Kurrle et al., 2010) without relying on multichannel analysis. This possibility is examined more in deep in this thesis both for Love and Rayleigh-waves. Furthermore, exploiting the phase relationship between transverse acceleration and rotation rate about the vertical axis it is possible to use collocated measurements to estimate directions of propagation of Love-waves (Gaebler, 2010; Hadziioannou et al., 2012), that until today is indirectly estimated with array techniques. Another possible fields of application regards earthquake engineering where rotational (or torsional) motions play an important role, especially in connection with the building response and in the calculation of site effects (Ghayamghamian and Matosaka, 2003). Historical examples of rotation of buildings (Fig. 2.3) are well summarized in Kozák (2009) and Sargeant and Musson (2009) and used in order to develop numerical models of earthquake rotated object by Hinzen (2012). Here we just recall these works for a deeper discussion on this matter.

Another possible application of rotational measurements has been pointed out by


Figure 2.3: Rotation of obelisk segments from the 1897 Assam earthquake (Oldham, 1899).

Legrand (2003) showing that the representation of a finite source in the earthquake source modelling is more informative by including the rotational part that may derived from rotational motions. He also mentioned that the description of the finite source via seismic moment tensor is neglecting the rotational part that actually must be taking into account. Lastly, Bernauer et al. (2009) introduced a new technique to seismic tomography of incorporating rotational motions into the seismic inverse problems with the goal to resolve better and more realistic tomographic images.

All this possible applications require as said, an high sensitive rotational sensor that should be capable to detect rotations in a large frequencies and amplitudes range. In the next chapter we briefly describe ring-laser gyroscopes, that over the last few years are representing the most suitable instrument to achieve this task.

## Chapter 3

## Instrumentation and data

This chapter describes the instrumentation used for the experiments and the features of the collected data. To perform collocated measurements of rotation and translation the distance between the two different type of sensors must be considered small with respect to the analyzed wavelengths. This has been achieved comparing data from G-Pisa ring-laser gyroscope with seismic sensors already present at the VIRGO site (Fig. 3.1).

When possible, data from a Guralp CMG40-T broadband seismometer were used because of the high sensitivity of the instrument. Otherwise we used signals recorded by a triaxial EpiSensor ES-T, force balance accelerometer located at VIRGO's central building, some 10 m apart from the ring-laser apparatus. This accelerometer, together with other two identical instruments located at the VIRGO North-end and West-end, has been used also to collect data for array analysis. The array set up is shown in Fig. 3.2. In this work, all the instruments recording ground translation have one of the sensitivity axes oriented along VIRGO's arms thus the N-S components of translation are misaligned with respect to the geographical N of an angle of about $19^{\circ}$ measured clockwise.

### 3.1 Gyrolaser

In this thesis a ring-laser gyroscope was used so the main attention is pointed to this kind of instrument. A complete description of other types of rotational sensors and their possible applications in the field of seismology can be found in literature (Bernauer et al.,


Figure 3.1: Location of the VIRGO gravitational wave antenna, Cascina (Pisa). The ring-laser gyroscope G-Pisa, a Guralp CMG40-T broadband seismometer and a tri-axial EpiSensor ES-T accelerometers are located in VIRGO's central building. VIRGO's North arm has an azimuth of $19^{\circ}$ with respect to the geographical North.

2012; Graizer, 2009; Jaroszewicz et al., 2011; Knejzlík et al., 2012; Velikoseltsev et al., 2012) and goes beyond the scope of this work.

The rotation rates thus far observed in seismology range from $10^{-1} \mathrm{rad} / \mathrm{s}$ (Nigbor, 1994) close to seismic sources to $10^{-11} \mathrm{rad} / \mathrm{s}$ for large earthquakes at teleseismic distances (Igel et al., 2005, 2007). Ring laser gyroscopes represents powerful tools to measure small amplitude rotations induced by earthquakes because of their insensitivity to translational and cross-rotational motions. Ring lasers detect the Sagnac beat frequency of two counter-propagating laser beams (Stedman, 1997) as sketched in Fig3.3. These active interferometers are composed by triangular or square optical cavities under vacuum in which the light beams interfere. If the reference frame of the instrument rotates, the effective cavity length between the co-rotating and the counter-rotating lightbeams differs, and the two beams are frequency split. Such frequency splitting is then measured as the


Figure 3.2: Array setup. EpiSensor accelerometers used for the array experiments are indicated by blue arrows.
beat frequency of the two beams outside the cavity. This beat frequency (Sagnac frequency $\left.f_{S}\right)$ is related to the rotation rate by a scale factor. For a ring-laser with perimeter $P$, area vector $\mathbf{A}=A \hat{\mathbf{n}}$, and laser wavelength $\lambda$, the angular velocity $\boldsymbol{\Omega}$ of its reference frame induces a Sagnac frequency given by:

$$
\begin{equation*}
f_{S}=\frac{4 A}{P \lambda} \boldsymbol{\Omega} \cdot \hat{\mathbf{n}} \tag{3.1}
\end{equation*}
$$

$f_{S}$ depends on the geometrical scale factor $\frac{4 A}{P \lambda}$, on $\hat{\mathbf{n}}$ (changing in orientation of the instrument) and finally on $\boldsymbol{\Omega}$ (due to changes in Earth's rotation rate, or seismically induced rotations) that represents the most dominant contributions to $f_{S}$. In seismic application the Earth's rotation rate plays the role of a constant bias for the sensor. On the other hand, very sensitive ring-laser are able to detect Earth rotation rate variations such as the one induced by polar motion or the free oscillation of the Earth rotation axis known as Chandler Wobble (Igel et al., 2011; Schreiber et al., 2004, 2011).

G-Pisa is a He-Ne based gyrolaser with $\lambda=632.8 \mathrm{~nm}$. It operates in a squared cavity with $A=1.82 m^{2}$ (Belfi et al., 2010, 2011; Di Virgilio et al., 2010). The instrument has been


Figure 3.3: Ring laser gyroscope diagram. $\Omega$ leads the ring-laser to rotate with respect to an inertial frame, the cavity length for the two counter-propagating laser beams becomes different and one observes a beat frequency (Sagnac frequency).
working since July 2010 at the VIRGO site (latitude $\phi=43^{\circ} 37^{\prime} 53^{\prime \prime}$, and expected mean value for the Sagnac frequency due to the Earth rotation bias of about 106.2 Hz ) with a sensitivity of some $(\mathrm{nrad} / \mathrm{s}) / \sqrt{\mathrm{Hz}}$ in the range $10-100 \mathrm{mHz}$ as reported by Di Virgilio et al. (2010) and Belfi et al. (2012b) and shown in Fig. 3.4.

The beat frequency between the two counter-propagating gyrolaser beams is detected by a photodetector and acquired by the VIRGO data acquisition system at the rate of 5 kHz . The rotation rate signal is then reconstructed up to the frequency of 50 Hz by using the following procedure:

- The optical beat signal $v(t)$ is bandpass- filtered (with a digital first-order Chebyshev filter) around the nominal Sagnac frequency within a bandwidth of about 90 Hz .
- The filtered signal and its Hilbert transform $w(t)$ are combined to form the analytic signal $z(t)=v(t)+j w(t)$.
- By expressing the analytic signal in the form $z(t)=|z(t)| \exp [j \phi(t)]$, the instantaneous phase is estimated as $\phi(t)=2 \pi f_{S} t$


Figure 3.4: (Belfi et al., 2012b). Typical angular velocity sensitivity of the gyroscope operating in the vertical plane configuration

- The instantaneous frequency $f_{S}$, connected to the rotation rate by the Eq.3.1, is finally estimated by calculating the derivative of the unwrapped instantaneous phase $\phi$.
- The instantaneous frequency is down-sampled down to the final sampling frequency of 50 Hz and converted to rad/s.

The possibility of changing G-Pisa configuration between horizontal and vertical allows to study rotations, around vertical and horizontal axis (Fig. 3.5). From a seismological point of view this means that assuming plane polarized waves propagation, it is possible to measure rotation induced by different kind of seismic waves. When G-Pisa is placed in horizontal configuration is sensitive to rotation about Z-axis that are induced by horizontally polarized waves (SH- and Love-waves). On the other hand a vertical configuration of G-Pisa allows to measure rotation about one of the two horizontal axis (e.g. X-axis)
induced by waves propagating along and transversely polarized on the vertical plane (Y-Z plane). These are (a) P-wave, as a consequence of wave reflection-conversion at the free surface, (b) SV-waves, and (c) Rayleigh-waves. In this thesis data from both types of configurations have been analyzed and major attention has been given to surface waves (Love and Rayleigh-waves), exploiting the relationships between translation and rotation discussed in chapter 2.


Figure 3.5: The two possible G-Pisa configurations. On the left, horizontal configuration is sensitive to rotation about Z-axis. On the right, vertical configuration records rotation about an horizontal axis.

### 3.2 Guralp seismometer

For the acquisition of the translational ground motions a three-component Guralp CMG40T broadband seismometer was used (Fig. 3.6). The seismometer, already present at the


Figure 3.6: Guralp CMG40-T broadband seismometer

VIRGO site, is located at a distance less than 10 m from the ring-laser and in the same building, so the two instruments are considered collocated with respect to the analyzed frequency range (from 0.005 to 5 Hz ) which implies wavelengths spanning the $10^{5}-10^{2}$ m range. Mechanically, the vertical and horizontal sensor constructions are very similar. The vertical component sensor boom is supported horizontally with a leaf spring. The horizontal sensor is based on an inverted pendulum which is supported with two parallel leaf springs. The vertical and horizontal sensors are orthogonal to each other. The three sensors are controlled by a force feedback system to give velocity and mass position electrical outputs. The relative motion of the mass to the frame is detected by a differential capacitor which provides the basic signal from the device. The basic response of the system (velocity output) is flat to velocity from a specified corner frequency of $f_{n}$ to 50 Hz ( f is
the long period corner frequency). The damping coefficient of the sensor transfer function is $\eta=0.707$. Here is a table of specifications

| FLAT-RESPONSE (VELOCITY) | $30 \mathrm{~s}-50 \mathrm{~Hz}$ |
| :---: | :---: |
| SENSITIVITY | $800 \mathrm{~V} / \mathrm{m} / \mathrm{s}$ |
| DIFFERENTIAL OUTPUT | $\pm 10 \mathrm{~V}$ |

Table 3.1: Technical specification of the Guralp CMG40-T broadband seismometer

### 3.3 EpiSensors

Unfortunately, as in the case of the $M_{W}=9.0$, March 11th, Japan earthquake, it happened that some records coming from the Guralp CMG40-T broadband seismometer were not usable, indeed, because of VIRGO's experiments necessity, it was operating with a high gain level in order to monitor the microseismic activity with high sensitivity, and thus, earthquakes signals resulted severely clipped. In this cases, translational measurements have been carried out with an EpiSensor FBA ES-T Kinemetrics force balance accelerometer (Fig. 3.7). An array of three of these accelerometers has also been used as discussed in the introduction (Fig. 3.2).
The EpiSensor is a triaxial accelerometer optimized for earthquake recording applications.


Figure 3.7: EpiSensor FBA ES-T force balance accelerometer

Inside the waterproof, anodized-aluminum housing are three orthogonally mounted lownoise EpiSensor force balance accelerometer modules.

| DYNAMIC RANGE | $155 \mathrm{~dB}+$ (EpiSensor noise model <br> available from Kinemetrics) |
| :---: | :---: |
| BANDWIDTH | DC to 200 Hz |
| FULL-SCALE OUTPUT | User-selectable at: $\pm 2.5 \mathrm{~V}$ single-ended; <br> $\pm 10 \mathrm{~V}$ single-ended; $\pm 5 \mathrm{~V}, \pm 20 \mathrm{~V}$ differential |

Table 3.2: Technical specification of the EpiSensor FBA ES-T accelerometer

### 3.4 Data

Table 3.3 reports reports a list of the analyzed earthquakes. For each event is specified the G-Pisa configuration and the translational sensor used.

| DATE | TIME <br> $(\mathrm{UTC})$ | LAT <br> $(\mathrm{deg})$ | LONG <br> $(\mathrm{deg})$ | $M_{\omega}$ <br> $(\mathrm{deg})$ | LOCATION | G-Pisa | TRANSL. <br> SENSOR |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2010-Oct-13 | $22: 43: 14$ | 44.14 | 12.37 | 4.1 | Rimini | horiz. | Gur. |
| 2010-Nov-03 | $00: 55: 42$ | 43.76 | 20.73 | 5.5 | Serbia | horiz. | Gur. |
| 2010-Nov-03 | $18: 13: 05$ | 40.00 | 13.16 | 4.9 | Tyrrhenian | horiz. | Gur. |
| 2011-Mar-11 | $05: 46: 24$ | 38.29 | 142.373 | 9.0 | Japan | vert. | EpiS. |
| 2011-Jul-07 | $19: 21: 48$ | 42.03 | 7.72 | 5.3 | Tyrrhenian | vert. | EpiS. |
| 2011-Jul-17 | $18: 30: 28$ | 45.00 | 11.29 | 4.9 | Po plain | vert. | EpiS. |
| 2010-Jul-25 | $12: 31: 20$ | 44.98 | 7.284 | 4.4 | Hautes- <br> Alpes | vert. | EpiS. |

Table 3.3: Parameters of the observed events. G-Pisa configuration and the type of translational sensor used are reported for each event in the last two columns.

## Chapter 4

## Methods

This chapter summarizes the processing methods used through the whole data analysis. As most of the work is based on data collected by G-Pisa in vertical configuration, methods must be considered valid only for this kind of analysis, I will explicitly mention when the methods were used both for Love and Rayleigh-waves analysis or only for Love-waves (G-Pisa in horizontal configuration). For the whole data processing MATLAB software was used. For each of the next sections it will be given a brief review of the the theory behind each method used and a description of how it has been implemented. Results obtained with the described methods will be presented and commented in the next chapter.

### 4.1 Preprocessing

Data coming from G-Pisa comes in unit of $\mathrm{rad} / \mathrm{s}$, that means rotation rate. EpiSensors measure acceleration and so are in unit of $m / \mathrm{s}^{2}$, while data from seismometer are velocity expressed in $\mathrm{m} / \mathrm{s}$. When it was necessary signals have been integrated or differentiated to obtain the desired output. It will be told in the next sections when these operation have been carried out. This preprocessing section will describe the basic operations that have preceded the analysis of the data. First, for each seismic event, traces were cut to isolate earthquakes starting from origin time up to an adequate ending time. The selected portion of the record has been demeaned, simply by removing the mean value from the
entire portion, detrended, to remove linear trend affecting the record, and tapered with a Tukey window of the same length of the analyzed portion. For each event a different linear range of periods has been chosen according to the frequency content. A narrow-bandpass filtering around the selected periods has been done, to investigate the properties of traces in frequency domain. Filtering has always been performed with a 4th order Butterworth bandpass filter, chosen for its flat response in the passband. The filter was applied forward and backward to avoid a phase shift in the resulting filter trace. In the case of the aforementioned narrow-band filtering, for each period $T$, the associated corner frequencies have been selected to be $0.9 * 1 / T \mathrm{~Hz}$ and $1.1 * 1 / T \mathrm{~Hz}$.

### 4.2 Power Spectral Densities and MulTitaper Method

Power Spectral Density (PSD) represents the power in units of power per $H z^{-1}$ as a real function of frequency. As expressed by the Wiener-Khinchin theorem it represents the Fourier transform of the autocorrelation of a signal $x(t)$ :

$$
\begin{equation*}
P_{x}(f)=\int_{-\infty}^{\infty} R_{x}(\tau) e^{-j 2 \pi f \tau} d t \tag{4.1}
\end{equation*}
$$

where $R_{x}(\tau)=\int_{-\infty}^{\infty} x(t) x(t-\tau) d t$ is the autocorrelation function of $x(t)$ Standard method to compute PSD are based exactly upon the previous expressions. Unfortunately this kind of estimations called periodograms, suffers from unacceptable bias and variance. To overcome this kind of side-effects multitaper method has been developed by Thomson (1982) Briefly, multitaper method (mtm), is based on the following algorithm:

- Construct $K$ different tapers of size N
- Ensure that the tapers are properly designed orthogonal functions
- Produce modified periodograms using each taper (with low bias) following:

$$
P_{x x}^{(k)}(\omega)=\frac{1}{N}\left|\sum_{n=0}^{N-1} x(n) w_{k}(n) e^{j \omega n}\right|^{2}
$$

- Average (with or without weighting) to reduce variance following:

$$
\hat{P}_{x x}(\omega)=\frac{1}{K} \sum_{k=0}^{K-1} P_{x x}^{(k)}(\omega)
$$

This operations are implemented in Matlab through dpss and pmtm function. The former is used to compute the Discrete Prolate Spheroidal Sequences (DPSS) used as tapers, the first 4 of these are represented in Fig. 4.1 for $N=1000$.


Figure 4.1: First 4 Discrete Prolate Spheroidal Sequences used as tapers for multitaper analysis. $N=1000$

### 4.3 Spectrograms

To investigate spectral density within a certain frequency range, and to observe its variations with time, spectrograms were calculated using Matlab function spectrogram, that
performs a short-time Fourier transform (STFT) within Hamming sliding windows.

$$
\begin{equation*}
S T F T_{x}(\tau, f)=\int_{-\infty}^{\infty} x(t) g^{*}(t-\tau) e^{-j 2 \pi f t} d t \tag{4.2}
\end{equation*}
$$

where $g(t-\tau)$ defines the time window (Hamming window in this case). The STFT allow us to obtain spectral information in the neighbourhood of $\tau$. By sliding overlapping Hamming windows a STFT is performed in each segment.

### 4.4 Correlation of traces

Almost every analysis carried out in this work is strongly based upon correlation of time series. As shown by theory (Eqs.2.8 and 2.16) rotation rate about vertical and horizontal axis is expected to be in phase with transverse and vertical acceleration respectively, so comparisons between recorded signals are necessary in order to verify theory and to go further into more detailed analysis. Different ways to perform this kind of comparisons have been used in this thesis. Mainly normalized zero-lag correlation coefficient (ZLCC) was used to quantify similarities between different signals with Matlab function corrcoef. The ZLCC is defined between 1 and -1 where 1 represents perfect match. In order to get a correlation coefficient estimation for the entire records, ZLCC is often calculated within overlapping time windows of appropriate length.

### 4.5 Azimuth estimation (Love-waves)

Exploiting the simple relationship between transverse acceleration and rotation rate about a vertical axis, that has been shown before, we compare translation and rotation to obtain azimuth and phase velocities of the propagating Love-waves. As already mentioned, assuming a plane wave propagation and transverse polarization, we do expect that correlation between rotation about Z axis and translational motion is maximum when this latter one is measured along a direction transverse with respect to wave propagation.

The coordinate system is shown in Fig. 4.2


Figure 4.2: Coordinate system for rotation of $E-W$ and $N-S$ components. Backazimuth (BAZ) is defined as the angle between the incoming seismic wave and the geographical North measured clockwise at the receiver station. Here azimuth means just $B A Z+180^{\circ}$.

We can perform clockwise rotation using a matrix multiplication of a vector consisting of the north and east components with a "rotation matrix" given by

$$
A=\left[\begin{array}{cc}
\cos (\theta) & \sin (\theta) \\
-\sin (\theta) & \cos (\theta)
\end{array}\right]
$$

Then we have

$$
\left[\begin{array}{l}
R \\
T
\end{array}\right]=A\left[\begin{array}{c}
N \\
E
\end{array}\right]
$$

where $T$ and $R$ are the transverse and radial components respectively, computed from the recorded $\mathrm{N}-\mathrm{S}(N)$ and E-W $(E)$ components, and $\theta$ is the azimuth.

In this section we first applied a preprocessing step to the horizontal components coming from the seismometer, consisting of demeaning, detrending and tapering. Then a differentiation has been performed to obtain acceleration from velocity and finally traces were narrow-bandpass filtered, as discussed before. Subsequently, the resulting traces have been rotated first to account for the instrument orientation that is the same of VIRGO, so an anticlockwise angle rotation of $19^{\circ}$ gave the true N-S and E-W components. Then for each frequency band taken into account, and in sliding time windows of length three times the central period with $50 \%$ overlap, the corrected horizontal components are rotated for every angle that span the whole $0-360^{\circ}$ interval. For each azimuth of rotation, the similarity between transverse acceleration and rotation rate is computed within each windows through ZLCC. When the correlation coefficient is above a certain threshold ( 0.95 in this case), the azimuth to the source has been found. In this way, the result consists of a complete estimation of azimuth as a function of frequency and time. In addition, windows with high values of correlation coefficient, for different frequencies and azimuths, were selected to compute phase velocities through a least squares method that will be discussed later.

### 4.6 Array analysis

Data from the array described in chapter 3 (Fig. 3.2) has been used in this thesis for two main purposes. First, local phase velocities and azimuths are estimated with a Plane Wave Fit (PWF) analysis. Second, rotation rate is derived through spatial derivatives according to the seismo-geodetic method. What follows is a description of the two methods. Results and comments are reported in the next chapter.

### 4.6.1 Plane Wave Fit

The PWF method is briefly described following Del Pezzo and Giudicepietro (2002). For a plane wave of slowness $\mathbf{S}=\left(S_{x}, S_{y}\right)$ crossing the array, whose stations are located at $x_{i}$, $y_{i}$, the travel time differences between station i and j are given by the scalar product

$$
\begin{equation*}
\Delta t_{i j}=\mathbf{S} \cdot \Delta \mathbf{r}_{i j} \tag{4.3}
\end{equation*}
$$

where $\Delta \mathbf{r}_{i j}$ is the two-element vector of the differences between the coordinates of station $i$ and $j$ that is $\boldsymbol{\Delta} \mathbf{r}_{i j}=\left(x_{i}-x_{j}, y_{i}-y_{j}\right)$. If the inter-station distance is sufficiently small that array channels are coherent, then $\Delta t_{i j}$ can be estimated through the crosscorrelation function between the signal pairs $a_{i}(t)$ and $a_{j}(t)$ :

$$
\begin{equation*}
C_{i j}(\tau)=\int_{-\infty}^{\infty} a_{i}(t) a_{j}(t+\tau) d t \tag{4.4}
\end{equation*}
$$

whose first maximum occurs at a time, $t_{\max }$, which corresponds to the phase delay between the two signals. For a $N$ stations array we can build our overdetermined system of $N(N-1) / 2$ linear equations as

$$
\begin{equation*}
\Delta \mathrm{t}=\mathrm{S} \cdot \Delta \mathrm{r} \tag{4.5}
\end{equation*}
$$

where $\boldsymbol{\Delta} \mathbf{t}$ is the vector containing the $N(N-1) / 2$ travel time differences between all the possible independent station pairs $\left(t_{i j}=-t_{j i}\right)$.
We can write the 4.5 in explicit way for a $N=3$ stations array (like in VIRGO site) to obtain

$$
\left[\begin{array}{l}
\Delta t_{12}  \tag{4.6}\\
\Delta t_{13} \\
\Delta t_{23}
\end{array}\right]=\left[\begin{array}{ll}
x_{1}-x_{2} & y_{1}-y_{2} \\
x_{1}-x_{3} & y_{1}-y_{3} \\
x_{2}-x_{3} & y_{2}-y_{3}
\end{array}\right]\left[\begin{array}{c}
S_{x} \\
S_{y}
\end{array}\right]
$$

and solve using a least square approach (Menke, 1984)

$$
\begin{equation*}
\mathrm{S}=\left(\Delta \mathrm{r}^{\mathrm{T}} \Delta \mathrm{r}\right)^{-1} \Delta \mathrm{r}^{\mathrm{T}} \Delta \mathrm{t} \tag{4.7}
\end{equation*}
$$

where superscript $T$ indicates the transpose of a matrix.

Finally, apparent velocity $v=1 /|\mathbf{S}|$ and azimuth $\phi$ can be obtained through

$$
\begin{align*}
& v=\left(S_{x}^{2}+S_{y}^{2}\right)^{-1 / 2}  \tag{4.8}\\
& \phi=\tan ^{-1}\left(S_{x} / S_{y}\right) \tag{4.9}
\end{align*}
$$

### 4.6.2 Array-derived rotation rate

From Eq.2.2 in Chapter 2 it is clear that one, in principle, could determine rotations finding the spatial derivatives of displacements from a seismic array. Such spatial derivatives can be found trough a finite-differences of ground displacement. In particular I use the seismo-geodetic method proposed by Spudich and Fletcher (2008); Spudich et al. (1995) that is briefly described in the follows.

Let $\mathbf{r}^{i}=\left(x^{i}, y^{i}, z^{i}\right)^{T}, \quad i=0,1, \ldots, N$, be the coordinates of $N+1$ seismic stations before any seismic disturbances, and $T$ is the transpose. Let $\mathbf{R}^{i}=\mathbf{r}^{i}-\mathbf{r}^{0}$ be the predisturbance offset of station $i=1, \ldots, N$ from station 0 . Suppose that at time $t$ each station has moved by a quantity $\mathbf{u}^{i}=\left(\begin{array}{lll}u_{x}^{i} & u_{y}^{i} & u_{z}^{i}\end{array}\right)^{T}$ away from $\mathbf{r}^{i}$. The displacement field $\mathbf{u}$ is approximated to have resulted from a uniform strain and a rigid body rotation about $\mathbf{r}^{0}+\mathbf{u}^{0}$. The strain and rotation together can be characterized by a $3 \times 3$ displacement gradient matrix $G$ whose elements $G_{i j}=\frac{\partial u_{i}}{\partial j}$ are the unknowns. Under the assumption of spatially uniform displacement gradients it can be shown that

$$
\begin{equation*}
\mathbf{d}^{i}=G \mathbf{R}^{i} \tag{4.11}
\end{equation*}
$$

where $\mathbf{d}^{i}=\mathbf{u}^{i}-\mathbf{u}^{0}$. Here I recall the free surface boundary condition and the Eqs.2.3, 2.5, and put this results in 4.11 to obtain

$$
\mathbf{d}^{i}=\left[\begin{array}{ccc}
\frac{\partial u_{x}}{\partial x} & \frac{\partial u_{x}}{\partial y} & \frac{\partial u_{x}}{\partial z}  \tag{4.12}\\
\frac{\partial u_{y}}{\partial x} & \frac{\partial u_{y}}{\partial y} & \frac{\partial u_{y}}{\partial z} \\
-\frac{\partial u_{x}}{\partial z} & -\frac{\partial u_{y}}{\partial z} & -\eta\left(\frac{\partial u_{x}}{\partial x}+\frac{\partial u_{y}}{\partial y}\right.
\end{array}\right] \mathbf{R}^{i}
$$

where $\eta=\frac{\lambda}{(\lambda+2 \mu)}$. Placing the unknown displacement gradient in a column vector $\mathbf{p}=\left(\frac{\partial u_{x}}{\partial x} \frac{\partial u_{x}}{\partial y} \frac{\partial u_{x}}{\partial z} \frac{\partial u_{y}}{\partial x} \frac{\partial u_{y}}{\partial y} \frac{\partial u_{y}}{\partial z}\right)^{T}$ the previous system is rewritten as

$$
\mathbf{d}^{i}=\left[\begin{array}{cccccc}
R_{x}^{i} & R_{y}^{i} & R_{z}^{i} & 0 & 0 & 0  \tag{4.13}\\
0 & 0 & 0 & R_{x}^{i} & R_{y}^{i} & R_{z}^{i} \\
-\eta R_{z}^{i} & 0 & -R_{x}^{i} & 0 & -\eta R_{z}^{i} & -R_{y}^{i}
\end{array}\right] \mathbf{p}
$$

and solving it with a least square method. Finally, from the obtained solution of the problem the rotation angles about the three Cartesian axis are given by:

$$
\begin{aligned}
\theta_{x} & =-p_{6} \\
\theta_{y} & =p_{3} \\
\theta_{z} & =\left(p_{4}-p_{2}\right) / 2
\end{aligned}
$$

For the Japan earthquake the major interest is focused on $\theta_{y}$ as it is the component of rotation that the gyrolaser is measuring for a propagating wave along x -axis. The package used in this work is strainz17 Matlab function developed by Spudich and Fletcher (2008); Spudich et al. (1995) and free-downloadable from USGS website (http://earthquake.usgs.gov/research/software/strainz17/). To obtain rotation rate in
$\mathrm{rad} / \mathrm{s}$ as output, we had to input velocities instead of accelerations. Thus all traces from accelerometers have to be integrated before using the function.

### 4.7 Azimuthal correction

In this section I describe a method for correcting signal from G-Pisa for both the misalignment of the instrument with respect to the N and for the azimuth variation of the incoming wavefield. This is the major problem when analyzing data from a ring-laser in the vertical configuration. In fact, the recorded rotation rate correspond to the true ground rotation only for a vertically polarized Rayleigh-wave that propagates along the direction perpendicular to the ring-laser area vector. Conversely, if the direction of propagation coincides with the area vector, theoretically no signal should be detected by the ring-laser. Between these two end-terms, what is actually recorded consist basically of the projection of the true rotation rate induced by Rayleigh-waves on the G-Pisa axis of sensibility (Fig. 4.3).

Trough the PWF analysis we obtained an estimate of the propagation azimuths as a function of frequency and time. We will use these azimuthal values to correct the rotational signal from G-Pisa, simply dividing it by a factor $\cos [90-(B A Z(i)-\alpha)]$ with $\alpha=19^{\circ}$.

### 4.8 Phase velocity from collocated measurements

Once established correlation between rotation rate and acceleration and using Eq.2.16 or Eq. 2.8 for Rayleigh-waves and Love-waves, respectively, it is possible to estimate phase velocities for these two types of surface waves. Two methods were developed in order to obtain phase velocities and dispersion curves. The first concerns analysis in time domain, the second in frequency domain. What follows is a brief description of these two methods, and the different procedures used for each of them.

### 4.8.1 Time domain

After narrow-bandpass filtering translation and rotation signals, they are correlated within sliding time-windows of length twice the central period with $50 \%$ overlap. For each


Figure 4.3: Scheme used for azimuthal correction. $\Omega_{T}$ represent rotation of Rayleigh-waves about an axis perpendicular to the direction of propagation of the seismic wave. Ring laser mainly records projection, $\Omega_{y}$, on its axis of sensibility.
window that shows a ZLCC value above a fixed and arbitrary threshold and for a given frequency band, phase velocities are derived from a least squares, using $\mathbf{d}=\mathbf{G m}$ where $\mathbf{d}$ is acceleration (vertical for Rayleigh-waves and transverse for Love-waves) $\mathbf{G}$ is the rotation rate and $\mathbf{m}$ represents the only unknown ( $C_{R}$ for Rayleigh-waves $C_{L}$ for Love-waves) that is phase velocity. The simple formula is solved in a least squares sense through $\mathbf{m}=\left(\mathbf{G}^{T} \mathbf{G}\right)^{-1} \mathbf{G}^{T} \mathbf{d}$ (Menke, 1984). The above expression is a simple fit of a straight line starting from the origin and gives a value of velocity for each time window. Dispersion curves are then calculated by mediating velocities for each frequency, within a certain time interval that usually corresponds to the surface waves packet. Doing this allow to obtain an average representative velocity for each considered frequency.

### 4.8.2 Frequency domain

By looking again at the relationships that link rotation and translation, one could in principle, obtain velocities in frequency domain, simply through spectral ratios of rotation and translation. This has been carried out after calculating the respective spectra with a multitaper method. This method has been chosen to avoid individual spectral oscillation, because, as explained before, the output consists of a mean between different modified spectra each of them obtained with a different taper. In addition phase velocities estimation in frequency domain, gives additional and immediate information about dispersion properties of the analyzed waves. In this work dispersion curves in frequency domain are calculated by mediating the ratios of the multitaperd spectra of translation and rotation within overlapping frequency windows of appropriate lengths.

## Chapter 5

## Results

### 5.1 Introduction

This chapter illustrates the results obtained from the application of the methods results and comments obtained with the methods described in chapter 4 . The present chapter is divided into two sections, that correspond to the analysis of Love and Rayleigh waves for horizontal and vertical ring-laser configuration, respectively.

### 5.2 Love-waves

This section illustrates the results for the three regional events listed in table 3.3. Data are from collocated measurements of translation (Guralp CMG40-T seismometer) and rotation (G-Pisa ring-laser). Before starting the analysis, translational signals are detrended, demeaned, tapered and differentiated to obtain ground acceleration. Then horizontal components of ground motion are rotated anticlockwise of an angle of $19^{\circ}$ in order to correct the misalignment of VIRGO's arms with respect to the geographical coordinates. Rotation rate and rotated horizontal components of acceleration for the the $M_{w}=5.5$ Serbia earthquake are shown in Fig. 5.1. Peak ground acceleration is in the order of $2.6 * 10^{-4} \mathrm{~m} / \mathrm{s}^{2}$ while peak rotation rate is about $2 * 10^{-7} \mathrm{rad} / \mathrm{s}$. Spectrograms are shown in Fig. 5.2 for acceleration and rotation rate.

Most of the energy is in the range of frequencies between 0.2 and 3 Hz . Body-waves


Figure 5.1: Rotation rate (top), E-W (middle) and N-S (bottom) acceleration components of the $M_{w}=5.5$ Serbia earthquake. Horizontal components of acceleration are rotated to the geographical coordinates. Traces are filtered between 0.1 and 5 Hz . Time starts at $T_{0}=00: 55$ : 42.
arrivals are detectable in both records at 180 and 250 s, at frequencies between 0.8 and 4 Hz. Rotational signal in the P-waves train is probably related to the rotational component of the P-coda mainly made up of scattered waves at the surface. On the other hand SH-waves are detected between 250 and 300s. Surface waves, that show the highest energy, span the interval of frequencies between 0.8 and 0.2 Hz .


Figure 5.2: Spectrograms of $E-W$ acceleration (top) and rotation rate (bottom) for the $M_{w}=5.5$ Serbia earthquake. Bottom traces are filtered between 0.1 and 5 Hz . Time starts at $T_{0}=00: 56: 55$

### 5.2.1 Azimuth and phase velocity determination

Backazimuth and Love-waves velocities are obtained with the method described in sections 4.6 and 4.9 for the frequency range of $0.2-0.8 \mathrm{~Hz}$. The analysis is carried out by sliding a time window of length twice the dominant period with $75 \%$ overlap. At each window the horizontal components of acceleration are rotated for a range of 180 azimuthal values, spanning the 0-360 angular interval. For each step the correlation between rotational and translational signal is then calculated. For Love-waves the two types of signals should be in phase, so for every window the azimuth that gives the highest value of the zero-lag correlation coefficient is stored and velocity is obtained through a least square fit between rotation rate and best fitting transversal acceleration that corresponds to that azimuth. Fig. 5.3 shows an example of the method used to compute velocity for a single time window.


Figure 5.3: Example of a single time window phase velocity and azimuth estimation. Black trace is the best fitting transverse acceleration obtained with an azimuth of $276^{\circ}$. Red trace is rotation rate scaled with two times the calculated phase velocity for that window ( $713 \mathrm{~m} / \mathrm{s}$ ). Correlation coefficient is 0.91 . This window represent the points located at 181s in the previous figure.

Results are shown in Fig. 5.4. The expected azimuth (265.5 $)$ is well estimated especially in the Love-waves time interval after 150s. Correlation above 0.7 is obtained also in the first part of the record between 30 and 100 s connected with P -wave coda and SH-waves. Azimuth in this interval is still in good agreement with the expected one. Love-waves velocities span the range of values between 1000 and $400 \mathrm{~m} / \mathrm{s}$ with a general trend towards lower values with increasing time.

The same method was applied to the $M_{w}=4.9$ Tyrrhenian earthquake in a frequency band of $0.2-0.6 \mathrm{~Hz}$ because of the low $\mathrm{S} / \mathrm{N}$ ratio of the records above 0.6 Hz . The expected azimuth of $330^{\circ}$ is somewhat underestimated with a mean value of $300^{\circ}$ in the Lovewaves interval. The most coherent values are obtained at the SH -arrival ( $\pm 25 \mathrm{~s}$ ) and in correspondence of the Love-waves peak ( $\pm 100 \mathrm{~s}$ and soon after). Love-waves velocities again show values between 1000 and $400 \mathrm{~m} / \mathrm{s}$ after 80 s .

In order to investigate dispersion properties of Love-waves, the same procedure described above is iterated for 40 periods spanning the $10-0.2 \mathrm{~s}$ interval for the Serbia earthquake that shows a broader frequency content once compared to the Thyrrenian earthquake. Phase velocity for every central period is obtained by averaging velocity values within the Love-waves time interval for correlation coefficient higher than 0.9.

As pointed out by some authors (Igel et al., 2007; Suryanto, 2006) the same dispersion relationship can be obtained in the frequency domain by dividing acceleration and rotation rate spectra. In this work, spectra for both acceleration and rotation rate have been computed with a multitaper method as described before. In this case horizontal components of acceleration are rotated to the expected azimuth to the epicenter $\left(265.5^{\circ}\right)$. Ratios between acceleration and rotation rate spectra were calculated by sliding a window of length 20 spectral coefficient with $50 \%$ overlap and dividing by a factor of 2 following Eq.2.8. Dispersion curves are plotted in Fig. 5.6.
 uolpeyoy

응

$=$


Figure 5.4: Azimuth and Love-waves velocities estimation for the $M_{w}=5.5$ Serbia earthquake. 1) Rotation rate. 2) Azimuth values corresponding to the max correlation coefficient for each window. The background map is the correlation coefficient for every azimuth and black dots correspond to the values with a correlation coefficient above 0.7 . The blue line is the expected azimuth. 3) Love-waves velocity for which the correlation coefficient is above 0.7. 4) Max correlation coefficient for each window. Time starts at $P$-wave first arrival



Figure 5.6: Love-waves dispersion curves for the $M_{w}=5.5$ Serbia earthquake. Top) Calculated in time domain, with error bounds. Bottom) Calculated in frequency domain through spectral ratios, with error bounds.

### 5.3 Rayleigh-waves

### 5.3.1 Japan earthquake

For the $M_{W}=9.0$, March, 11th, 2011, Japan earthquake translational ground motion comes from EpiSensors records, because seismometer signal was saturated. Array data were available for the entire records. Collocated measurements of rotation and translation refer to the ring-laser and an EpiSensor located in VIRGO central building. In Fig. 5.7 are shown the 2-hours long records coming from ring-laser and the collocated EpiSensor vertical component of ground motion after demeaning, detrending, tapering and bandpass filtering with corner frequencies of 0.005 and 1 Hz .

As expected, amplitudes of rotation rate are much smaller than those of vertical acceleration. Peak amplitudes of rotation rate are on the order of $6 * 10^{-8} \mathrm{rad} / \mathrm{s}$ while those of acceleration are at least 4 orders of magnitude larger $\left(6.5-7 * 10^{-4} \mathrm{~m} / \mathrm{s}^{2}\right)$.

## Spectral properties

In order to investigate energy carried on by each frequency, PSD estimations were performed along each of the two unfiltered signals. Using multitaper method, described in chapter 4, P-wave and Rayleigh-waves were individually analyzed taking time windows of length 600s and 2000s respectively starting at the expected arrival time for each phase. Then, in order to evaluate signal to noise ratio, PSD was evaluated over a 5 hours-long record preceding the earthquake was taken and. Results are shown in Fig. 5.8. For EpiSensor, acceleration spectra for both P- and Rayleigh-waves are always above background noise up to 2 Hz and their energy is from 1 to 5 orders of magnitude larger than that of noise. For the ring-laser gyroscope amplitudes are generally weaker. They reach values about 2 orders of magnitude greater than that of noise, in the band of frequency between 0.02 and 0.1 Hz for Rayleigh-waves and between 0.2 and 2 Hz for P-wave. P-wave is under the background noise level for frequencies less than 0.2 Hz while Rayleigh-waves for frequencies grater than 0.1 Hz and less than 0.01 Hz . Noise peaks at 2 and 4 Hz are a constant feature at both instruments. Belfi et al. (2012a) interpret this observation in terms of a site effect and/or resonance of the building, inducing narrow-band amplification
of the earthquake signal or the anthropogenic noise.

To better understand the evolution of the frequency content as a function of time for both rotation and translation, spectrograms were calculated and traveltimes for the main seismic phases are reported in table 5.1

| PHASE | TRAVELTIME (sec) |
| :---: | :---: |
| P | 764.53 |
| S | 1403.75 |
| LQ (Love) @ 40s | 2221.16 |
| LR (Rayleigh) @ 40s | 2465.18 |

Table 5.1: Traveltimes for the main seismic phases

By looking at Fig. 5.9, most of the energy is concentrated in the interval between 3000 and 4000 s after $T_{0}$ and in a frequency band of 0.03 and 0.1 Hz , that correspond to surface waves packet. Rayleigh-waves dispersion is clearly visible down to 0.005 Hz in both figures although it is more pronounced, showing higher energy, in the acceleration spectrogram. Above 0.1 Hz P- S-waves are observed clearly especially for acceleration where $\mathrm{S} / \mathrm{N}$ ratio is higher in that frequency band. Other rotational signals are observed in Fig. 5.9b). The first starting around 800 s for frequency $1-0.1 \mathrm{~Hz}$ is related to P-wave coda, where scattered waves are present. The second is in the same frequency range of Rayleigh-waves but it is located before, starting at about 1500s, where S-waves are expected. This could be explained by the presence of vertically polarized SV-waves that could in principle be responsible of such rotational signal. In this work most of the attention is focused on Rayleigh-waves because they show the largest amplitude and so the best S/N ratio. Pand S-waves induced rotations are observed but not investigated in this study.


Figure 5.7: 2 hours-long records of the Japan earthquake starting from origin time ( $T_{0}$ ) after bandpass filter with corner frequencies of 0.005 and 1 Hz . Red dots are the expected traveltimes for 4 major seismic phases ( $P$-, $S$-, Love- and Rayleigh-waves). Top) vertical acceleration from EpiSensor. Bottom) rotation rate from ring-laser.


Figure 5.8: PSD estimation for EpiSensor (top) and ring-laser (bottom) using pmtm Matlab function. For $P$ - and Rayleigh-waves windows of length $\sim 600$ s and $\sim 2000$ s respectively were chosen starting at the expected traveltimes and encompassing the whole wave train. 5 hours-long record preceding the earthquake was used to evaluate PSD for noise.


Figure 5.9: Spectrograms of vertical acceleration (top) and rotation rate (bottom) for the $M_{w}=9.0$ Japan earthquake. Bottom traces are filtered between 0.005 and 1 Hz . Time starts at $T_{0}=05: 46: 23$

## Correlation of traces

A first comparison between rotation rate and vertical acceleration is made after a bandpass filtering with corner frequencies 0.005 an 1 Hz . ZLCC is calculated within overlapping time windows of length 30s. Fig. 5.10 shows 6 hours long records starting 2 hours before $T_{0}$ of vertical acceleration and rotation rate. Before the earthquake first break $(t \approx 8000 s)$ ZLCC is always less than 0.2-0.3 indicating absence of waveform correlation. A slight increase in correlation coefficient is observed soon after with values reaching 0.4 that suddenly drop again to lower values in the interval between $\approx 8700 s$ and $\approx 9000 s$. This feature indicates a correlation in the interval encompassing the P-coda where scattered waves are present. Starting from $t \approx 9000 \mathrm{~s}$ an increase of ZLCC is observed until it reach its maximum values between $\approx 10300 \mathrm{~s}$ and $\approx 11300 \mathrm{~s}$. This interval corresponds to the maximum amplitude interval of surface waves. Rayleigh-waves onset is expected at $\approx 9600 s$ where ZLCC is about 0.65 , thus correlation reach its maximum values after the main phase is arrived.




Figure 5.10: ZLCC (smoothed average in red) between vertical acceleration and rotation rate as functions of time by sliding overlapping time windows of length 30s. Traces are filtered between 0.005 and $1 \mathrm{~Hz} . T_{0}$ is at 7200s

To analyze more in detail amplitude relationship between rotation rate and vertical
acceleration, traces were superimposed, with rotation rate scaled by a factor obtained simply dividing peak ground acceleration (PGA) by peak ground rotation (PGR). Vertical acceleration and rotation rate are compared in a time interval of length 2500 s starting at $t=2000 s$ after $T_{0}$, just before Rayleigh-waves arrival. By sliding overlapping time windows of length 20s, ZLCC is computed and velocities obtained with a least squares fit when ZLCC is above 0.75 . Fig. 5.11 shows results after a bandpass filter with corner frequencies of 0.005 and 0.1 Hz . A general trend of decreasing period with time is observed, as expected for dispersive Rayleigh-waves. This is confirmed also by the same decreasing trend of velocities values that vary between 10000 and $5000 \mathrm{~m} / \mathrm{s}$. These values, however, are higher than expected as already reported by Belfi et al. (2012a).

To further illustrate the frequency-dependent performance of the rotational sensor compared with the accelerometer, vertical acceleration and rotation rate were superimposed after filtering with a narrow bandpass (zero-phase Butterworth with corner frequencies $0.9 * 1 / T$ and $1.1 * 1 / T \mathrm{~Hz}$, where $T$ is the period in seconds). The procedure is iterated for 50 center periods spanning the $200-1$ s period range and centered on the Rayleigh-waves train.

Traces were individually normalized so the maximum value is set to 1 . Superposition of such normalized traces is shown in Fig. 5.12a). As predicted by theory these two components of ground motion seem to be in phase especially at periods longer than 100s. The expected dispersive behavior is clearly observed in both records. To quantify similarity between rotation rate and vertical acceleration ZLCC is computed at the same frequency bands and in the same time interval, by sliding a time window of length twice the dominant period with $50 \%$ overlap (Fig. 5.12b)). Again, higher values of ZLCC are associated with Rayleigh-waves and the dispersion is clearly visible. Altough Rayleigh-waves expected arrival is located at 2460 s, high values of ZLCC are observed just before, between 1400 and 2400 s in the $20-60$ s range of periods, and could be connected with vertical polarized SV waves.


Figure 5.11: ZLCC (smoothed average in red) between vertical acceleration and rotation rate and calculated velocities as
functions of time by sliding overlapping time windows of length 20s. Dashed gray line represents the best fit of calculated
velocities. Displayed rotation rate is scaled by a factor $=P G A / P G R$. Traces are filtered between 0.005 and 0.1 Hz . Time
starts at Rayleigh-waves arrival ( $\approx 2400 \mathrm{~s}$ after $T_{0}$ ).


Figure 5.12: Top. Superposition of vertical acceleration (black) and rotation rate (red) after narrow-bandpass filtering. Traces are individually normalized. Bottom. Normalized zero-lag correlation coefficient between vertical acceleration and rotation rate after narrow-bandpass filtering. Bottom trace represents vertical acceleration filtered between 0.005 and 0.1 Hz . Time is from $T_{0}$.

## Array measurements

This section reports the results coming from two different kind of analysis performed on the array data. The array set up and configuration has already been described in chapter 3. Signals are from three triaxial accelerometers arranged in a triangular configuration with an interdistance of about 3 km . First, array-derived rotation rate is calculated from array and then compared with the recorded rotational signal from G-Pisa. Second, a multifrequency Plane Wave Fit (PWF) analysis is performed in order to estimate phase velocities and directions of propagation.

As discussed in chapter 4, array-derived rotation rate is calculated using stainz17, acceleration traces are first integrated to obtain velocity that is used as input, to directly get rotation rate as result. Again ZLCC is used to quantify similarity between array-derived rotation rate and rotation rate directly recorded by G-Pisa. Traces match surprisingly well for the entire duration, when filtered between 0.01 and 0.05 Hz as it can be observed in Fig. 5.13 for array-derived and measured rotation rate. Good fit is observed especially in the Rayleigh-waves train but also before and after. Fig. 5.14 shows the portion of traces from 2400s to 4000s corresponding to the Rayleigh-waves train. Minor differences in amplitudes are observed, array-derived rotation rate indeed seems to have a slightly higher amplitude than the recorded signal. This discrepancy can be explained considering that stainz17 was applied to the minimum required numbers of stations (three) and as reported by Suryanto et al. (2006) this could lead to non negligible errors, that in this case, however, are surprisingly small. We also compared array-derived rotation rate with vertical acceleration recorded by the station placed in VIRGO's central building in the same way (Fig. 5.15). In addition velocities are estimated through the ratio $a_{z}(t) / \Omega(t)$ in a least square sense when ZLCC was above 0.75. Again a good match is observed although velocities continue to be overestimated as they span the $10000-5000 \mathrm{~m} / \mathrm{s}$ range.





$\begin{array}{llll}4000 & 5000 & 6000 & 7000\end{array}$
Time [s]
Figure 5.13: Array-derived rotation rate against G-Pisa recorded signal. From top to bottom, a) array-derived rotation rate for a three-sensor array. b) Rotation rate directly recorded by G-Pisa. c) Superposition of traces. d) Zero-lag correlation coefficient as a function of time calculated in sliding and overlapping time windows. Traces are filtered between 0.01 and 0.05 Hz.
(T)
, - G-Pisa

Figure 5.14: The same as in Fig. 5.13 but zoomed in around the Rayleigh-waves train.

Figure 5.15: Array-derived rotation rate against vertical acceleration recorded by the accelerometer located in VIRGO's central building. From top to bottom, a) superposition of traces with array-derived rotation rate scaled by a factor PGA/PGR. b) $Z L C C$ as a function of time, red dots mark values above 0.75. c) Velocities obtained through the ratio $a_{z}(t) / \Omega(t)$ in a lest square sense when ZLCC was above 0.75.

Array data from three triaxial EpiSensors were processed using a PWF analysis for periods spanning the $100-1 \mathrm{~s}$ interval. This method allows an estimation of azimuth and phase velocities of the incoming wavefield. To obtain such quantities as a function of frequency and time the procedure was iterated for every central period after a narrowbandpass filtering and in sliding time windows. Results are shown in Fig. 5.16 and in Fig. 5.17 The expected azimuth for the Japan earthquake was $216^{\circ}$ and in general it is in


Figure 5.16: Estimated azimuth ( $\Phi$ ) as a function of period and time from PWF analysis
agreement with those obtained by the PWF analysis. It has to be said that the energy content varies along frequencies and time as shown by the PSD analysis and spectrograms and this will affect results obtained with a multi-frequency PWF analysis, so Fig. 5.16 and Fig. 5.17 should be read together with Fig. 5.8 and Fig. 5.9. Data matrices of calculated velocities and azimuth will be used for two different aims. First of all it is possible to build a Rayleigh-waves dispersion curve from array-derived velocities data by mediating obtained values in the Rayleigh-waves train. Azimuth will be used to correct G-Pisa recorded rotation rate. In the next step the attention is focused on obtaining a dispersion curve, azimuthal correction will be discussed later. Fig. 5.17 shows the expected traveltimes for Rayleigh-waves at different frequencies calculated for group velocity with matdisperse from Lai (1998) for the spherically symmetric AK135 Earth model (Kennett


Figure 5.17: Estimated velocity as a function of period and time from PWF analysis
et al., 1995). For each frequency a time interval of fixed length $\delta t=200 \mathrm{~s}$ is taken, centered at the expected traveltime. For every window a representative Rayleigh-waves phase velocity at that frequency is obtained mediating the array-derived velocities included in $\delta t$.

Looking at Fig. 5.19top a general match between theoretical and calculated dispersion curves is observed except for periods longer than 90 s and less than 15 s . The latter discrepancy could be explained by considering that, for decreasing wavelengths, the coherency between array channels decreases, resulting in unreliable slowness estimates.

## Dispersion curve from collocated measurements of rotation and translation

The next step is to correct rotation rate recorded by G-Pisa for azimuth calculated with the PWF analysis, using the procedure described in chapter 4. The correction is applied to the Rayleigh-waves train, so only a portion of the recorded signal is analyzed. A time window of length 2000s starting at the expected Rayleigh-waves arrival ( 2460 s after $T_{0}$ ) is selected both for the rotation rate and for the array-derived azimuth. For every frequency rotation rate is corrected with the proper value within sliding time-windows of length twice the dominant period and with $50 \%$ overlap. At each window position, the corrected rotation rate is cross-correlated with vertical acceleration and ZLCC is obtained. When ZLCC is above a threshold of 0.75 , phase velocity is calculated through a linear regression. Results are shown in Fig. 5.18.


Figure 5.18: Rayleigh-waves phase velocities estimation from collocated measurements of rotation and translation after azimuthal correction of G-Pisa signal. ZLCC between vertical acceleration and rotation rate is calculated within sliding time-windows of length twice the dominant period with $50 \%$ overlap. When ZLCC is above 0.75 velocities are obtained through a linear regression. White areas indicate where correlation is under the threshold. Values of velocities are in $\mathrm{m} / \mathrm{s}$. Black dots are the Rayleigh-waves group traveltimes

To obtain a more readable Rayleigh-waves dispersion curve from collocated measurements of rotation and translation, we mediate the obtained velocities from the above data matrix in an interval of time that starts at the theoretical traveltimes and last 1000s (Fig. 5.19middle). The so calculated dispersion curve show variations with respect to those obtained from AK135 Earth model. A comparable trend is observed in the $60-10 \mathrm{~s}$ periods range but velocities are in general underestimated. These two features are connected first with the accelerometer response under 50s that probably is not so accurate in amplitude and phase and second with the observation that, in general, the highest values of correlation are always delayed with respect to the main phase arrival thus leading to an underestimation of velocity. Between 60 and 10s indeed, the upper error bound seems to be a better velocities estimator, especially between 30 and 10s, where most of the energy is concentrated. Below 10s local geology strongly influences velocities and takes them away from the model and in addition results are influenced by the low $\mathrm{S} / \mathrm{N}$ ratio for rotation rate.

Dispersion curve was also estimated in frequency domain by dividing spectra from vertical acceleration and rotation rate (Fig. 5.19bottom). This time, rotation rate trace has been corrected for a constant azimuth for every frequency that correspond to the theoretical one.
(


Figure 5.19: Rayleigh-waves dispersion curves for the $M_{W}=9.0$, March 11th, Japan earthquake. Top) Obtained through a multi-frequency PWF analysis of array data. For every period phase velocity is estimated by mediating the array-derived velocities within a time interval of 200s centered at the Rayleigh-waves group arrival. Middle) From collocated measurements of rotation and translation in time domain. Phase velocities are obtained through a linear regression of azimuth-corrected rotation rate and vertical acceleration and then mediated in a 1000s time window starting at the theoretical traveltimes. Bottom) From collocated measurements of rotation and translation in frequency domain by multitapered spectral ratios in overlapping frequency windows. Red and black dots are the upper and lower bounds, respectively. In green theoretical Rayleigh-waves dispersion curve from AK135 Earth model

### 5.3.2 Regional earthquakes

This section is mainly focused on the analysis of the $M_{W}=4.9$, July 17th, 2011, Po-Plain, earthquake. Great circle path epicentral distance is about 169.4 km .

PSD of rotation rate (Fig. 5.20) show a good signal to noise ratio (up to 4 orders of magnitude) in the range between 0.5 and 5 Hz for what concerns Rayleigh-waves. In addition, it is possible to observe again the effect of scattered waves in the P-wave coda, that takes the relative spectra above that of Rayleigh-waves starting from 4 Hz . On the other hand, PSD computed for vertical acceleration (Fig. 5.20) exhibits a slightly different pattern, although the general trend is the same. P-wave and Rayleigh-waves spectra are always above background noise level and Rayleigh-waves seem visible also under 0.5 Hz and above 5 Hz however with a poor signal to noise ratio. Thus as expected, regional earthquakes should provide a piece of information about Rayleigh-waves within a different and higher frequency band with respect to large teleseismic earthquakes. This means that by applying the same methods used for the Japan earthquake, it is possible to retrieve additional information on Rayleigh-waves phase velocities in the frequency band that should account for local geology. Rayleigh-waves dispersion curves are so calculated in time domain, using the method described before. Results are shown in Fig. 5.21 and compared with those obtained by Saccorotti et al. (2011) from an array noise analysis at the VIRGO site.

The calculated velocities are in good agreement and show values greater than $1000 \mathrm{~m} / \mathrm{s}$ under 1 Hz and between 600 and $100 \mathrm{~m} / \mathrm{s}$ above 1 Hz . As the results of Saccorotti et al. (2011) derive from ambient seismic noise, I also test the possibility to retrieve Rayleighwaves dispersion curves, from collocated measurements of rotation and translation with this particular source of seismic waves. To do so, I isolated a portion of signal of length 5 hours preceding the earthquake and applied the time domain method to estimate phase velocities.

Results show that it seem possible to extract information on surface waves velocities just from collocated measurements of rotation and translation.


Figure 5.20: PSD estimation for the the $M_{W}=4.9$, July 17th, 20011, Po-plain, earthquake.

(b)

Figure 5.21: Comparison between a) Rayleighwaves dispersion curve for the $M_{W}=4.9$, July 17th, 20011, Poplain, earthquake and b) Rayleigh-waves dispersion curve from ambient seismic noise (Saccorotti et al., 2011). a) Velocities are obtained through a linear regression between vertical acceleration and rotation rate in sliding and overlapping time windows of length twice the dominant period when ZLCC was above 0.75 . Error bounds refer to the average carried out along the Rayleigh-waves train. b) Slowness data are obtained from 24 consecutive, nonoverlapping, 600s long time windows. The inset shows the configuration of the array used for slowness estimates (circles), with respect to the wind farm (stars) source of seismic noise.


Figure 5.22: Rayleigh-waves dispersion curve from collocated measurements of rotation and translation for a 5 hours long ambient seismic noise signal. Velocities are obtained through a linear regression between vertical acceleration and rotation rate in sliding and overlapping time windows of length twice the dominant period when ZLCC was above 0.75 . Error bounds refer to the average carried out along the whole signal.

## Chapter 6

## Conclusions

In this thesis collocated measurements of rotation and translation induced by earthquakes are used to estimate local seismic phase velocities, dispersion curves and directions of propagation of surface waves. Rotational data were recorded by a ring-laser gyroscope (G-Pisa) at European Gravitational Observatory at Cascina (Pisa). G-Pisa can be operated with the laser plane in the vertical or in the horizontal orientation. In the two cases it detects rotations respectively around the horizontal axis (Rayleigh-waves) or the vertical axis (Love-waves).

Results coming from collocated measurements of rotation (G-Pisa) and translation (Guralp CMG40-T broadband seismometer) for Love-waves, show that it is possible to determine local phase velocities and direction of propagation of the seismic waves, thus confirming what have already been reported by many authors (Cochard et al., 2006; Igel et al., 2005, 2007).

This work reports the very first analysis of seismic rotations detected with a gyrolaser lying in the vertical plane. Results of this analysis for the $M_{W}=9.0$, March 11th, 2011, Japan earthquake, confirmed the Rayleigh-waves theoretical relationship between vertical acceleration and rotation rate at least for what concerns phase matching, especially at periods longer that 100s. Since amplitude relationships are strongly influenced by the directions of propagation of the Rayleigh-waves with respect to gyrolaser axis, a method to correct rotation rate signal is proposed. This method, which is based on a multifrequency PWF array analysis, leads to more reliable estimates of phase velocity from the ratio
$a_{z}(t) / \Omega(t)$. After this correction, dispersion curves are derived both in time and in frequency domain from collocated measurements of rotation and translation. Results are in good agreement with those provided by a standard (AK135) Earth model in the period range between 60 and 10s. Out of these bounds discrepancies can be attributed to the accelerometer response for periods longer than 60s, and to the local geology for periods shorter than 10s.

In order to investigate Rayleigh-waves phase velocities at shorter wavelengths (frequencies between 0.5 and 5 Hz ), some regional earthquakes and ambient noise signals have been analyzed, by applying the same methods used for the Japan earthquake. Results match quite well with those obtained by Saccorotti et al. (2011) using a multichannel array analysis of ambient seismic noise. This confirms the possibility to use collocated measurements of rotation and translation to derive dispersion properties of surface waves and so information about local geology even for ambient seismic noise signals.

In summary, collocated measurements of rotations and translations induced by earthquakes or by ambient seismic noise might become a reasonable alternative to array measurements for estimating local seismic phase velocities and directions of propagation.

This results open new perspectives for a wide range of applications for which highsensitivity measurements of ground tilt are required. These include the surveillance of volcanic and geothermal areas, the monitoring of carbon dioxide capture and storage in geological structures, the control of oil and gas production plants and ground motions characterization for earthquake engineering.

Although these first results seem to be very promising, further observations are needed, and improvements in ring-laser sensitivity should be combined with the use of very sensitive broadband seismic sensor. For this reason, G-Pisa is currently working in the INFN laboratory at San Piero a Grado (Pisa), together with a STS-2 Streckeisen broadband sensor.

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