

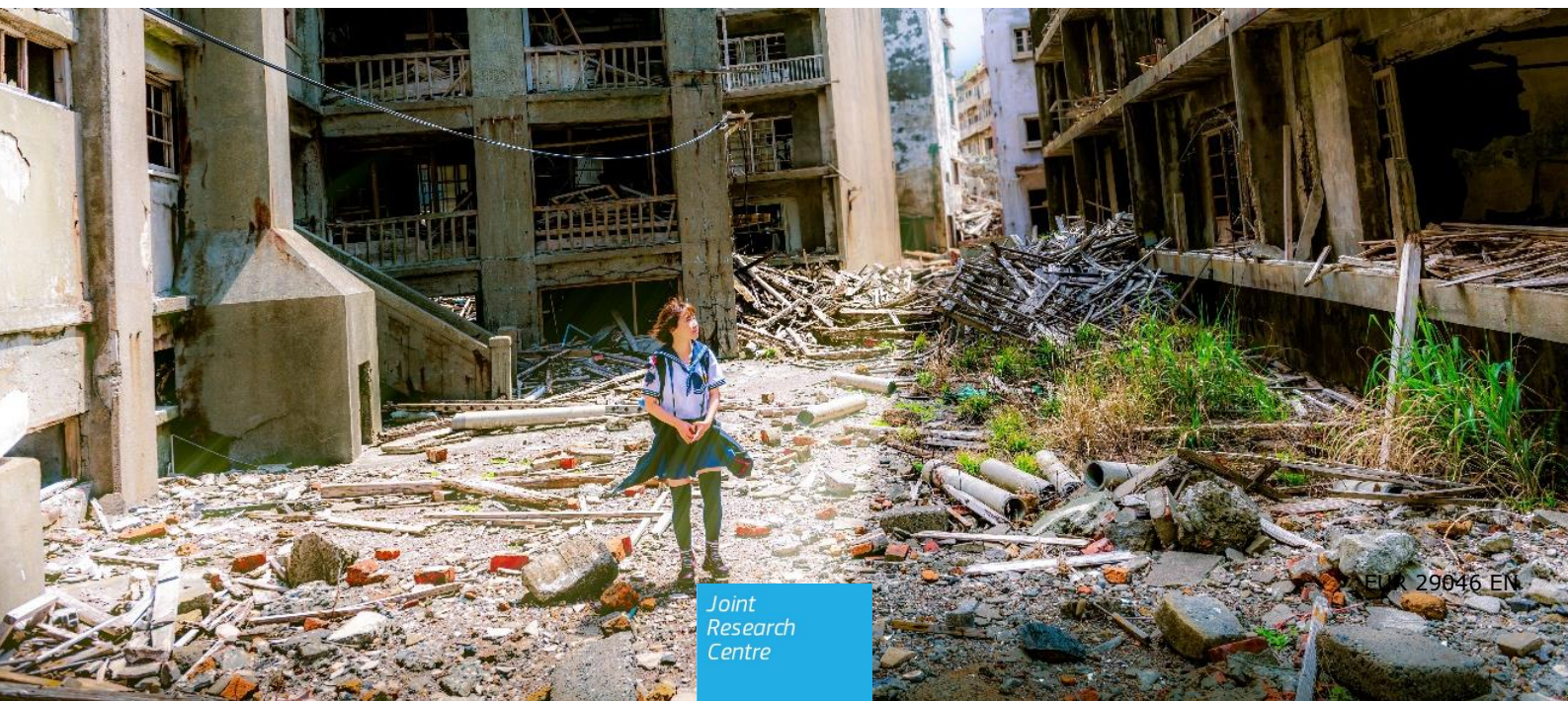
## JRC TECHNICAL REPORTS

# The Global Conflict Risk Index (GCRI) Regression model: data ingestion, processing, and output methods



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The Global Conflict Risk Index (GCRI)  
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## **Abstract**

The GCRI is a quantitative conflict risk model, developed by the JRC and based solely on open source data, providing quantitative input to the EU early warning framework, one input to the EU Conflict Early Warning System (EWS), developed by the European External Action Service (EEAS) in close partnership with the European Commission to enhance the EU's conflict prevention capacities. The GCRI distinguishes between three types of violent conflict a state may experience: civil war over national power, subnational conflicts over secession, autonomy, or resources, and conflicts in the international sphere. While the latter are not currently modelled by GCRI, for the first two the index quantifies the probability and the intensity respectively of national and subnational conflicts occurring in the next one to four years. Relying on historical data and a statistical model that includes political, socio-economic, environmental and security variables, it assesses the level and likelihood of future conflicts

The GCRI is composed of two statistical models: the regression model and the composite model. Both models are based on twenty-four individual variables. This report presents the work done between February 2017 and September 2017, specifically focused on improving the documentation on the regression model.

The present report describes on the one hand the regression model, including the input data and the model itself. On the other hand, it presents the statistical significance test, and the matrix of confusion, performed in order to get a highly detailed analysis of the performances of the model. The results of these analyses are presented in chapter 4 and 5.

This report is part of a series of technical documents produced in 2017 aiming at improving the GCRI models with greater transparency and robustness. It is not a validation of the GCRI, but a contribution to exploit its potential.

## 1. Introduction

The Global Conflict Risk Index (GCRI) has been designed to give policy makers a global risk assessment based on quantitative data. It quantifies the probability and the intensity of national and subnational conflicts occurring in the next one to four years.

The GCRI, inspired by quantitative conflict risk models, is made of two statistical models: the regression model and the composite model. Both models are based on twenty-four individual variables, all relatively stable, in that little change is to be expected from year to year. The data used are all freely accessible by any user on the Internet.

While the composite model assesses the risk-of-conflict at country level using weighted average method, the regression model applies to the twenty-four variables logistic and linear equations. The logistic equations are used to calculate the probability of a conflict whereas the linear ones are used to predict its intensity. The variables and the composite model are described in detail in the technical report "*Conflict Risk Indicators: Significance and Data Management in the GCRI*" (doi. 10.2760/44005).

This report describes the regression model, dividing it in four parts. The first section provides an overview on the input data (2), the second presents in detail how the predictions are obtained and the output data (3), the third shows the statistical significance test and its application to the model (4), and the last one describes the confusion matrix and its application to the model (5).

This report refers to the work done between February 2017 and September 2017 specifically focused on improving the documentation of the regression model. While the work presented here shows great advances in reliability and reproducibility, there is still great potential for improvements.

## 2. Input Data

This section provides all the relevant information on the variables used in the regression model.

The risk assessment is based on economic, social, political, geographical and environmental factors, studied through 24 variables. The data used are extracted from 14 different datasets, which are all freely accessible by any user on the Internet. Table 2 provides details about the data provider, the dataset used, and the URL where on can download the data. Table 3 presents some descriptive statistics: the original range of the data distribution, the thresholds imposed, the transformation done and years covered by each original dataset. While some of the datasets used are complete, others contain

missing data for specific years and/or specific countries. In order to overcome the lack of data and be able to compute the model, the missing data are imputed (replacing missing data with substituted values). In the imputation system adopted, data is taken from either the closest known historical data (desk research is conducted for finding precise information which would then justify the substituted value), or, if not possible, from regional averages, or from similar countries. The imputation is included in the data construction phase, making the data a single and complete dataset ready for statistical analysis. For more information on the data management, please refer to the technical report "*Conflict Risk Indicators: Significance and Data Management in the GCRI*" (doi. 10.2760/44005).



Indicator	Source	Name of dataset	Name of original indicator(s)	URL
Regime type	Center for Systemic Peace	Polity IV Annual Time-Series, 1800-2015	PARCOM, EXREC	<a href="http://www.systemicpeace.org/inscrdata.html">http://www.systemicpeace.org/inscrdata.html</a>
Lack of democracy	Center for Systemic Peace	Polity IV Annual Time-Series, 1800-2015	POLITY2	<a href="http://www.systemicpeace.org/inscrdata.html">http://www.systemicpeace.org/inscrdata.html</a>
Government effectiveness	World Bank	Government Effectiveness: Estimate	GE.EST	<a href="http://databank.worldbank.org/data/reports.aspx?source=worldwide-governance-indicators">http://databank.worldbank.org/data/reports.aspx?source=worldwide-governance-indicators</a>
Level of repression	Political Terror Scale Project	PTS Data	Highest of the three indicators in the set (PTS_A, PTS_H, PTS_S)	<a href="http://www.politicalterrorsscale.org/Data/Download.html">http://www.politicalterrorsscale.org/Data/Download.html</a>
Empowerment rights	CIRI Human Rights Data Project	CIRI Data	NEW_EMPINX	<a href="http://www.humanrightsdata.com/p/data-documentation.html">http://www.humanrightsdata.com/p/data-documentation.html</a>
Recent internal conflict	HIIK; UCDP/PRIO	Battle related deaths, One-sided violence, Non-state conflict, Conflict Barometer 2016	Highest casualty estimates	<a href="http://ucdp.uu.se/downloads/">http://ucdp.uu.se/downloads/</a> <a href="http://hiik.de/de/daten/">http://hiik.de/de/daten/</a>
Neighbours with HVC	HIIK; UCDP/PRIO	Battle related deaths, One-sided violence, Non-state conflict, Conflict Barometer 2016	Highest casualty estimates	
Years since HVC	HIIK; UCDP/PRIO	Armed Conflict Dataset, Conflict Barometer 2016	Conflicts of intensity level 2	
Corruption	World Bank	Control of Corruption: Estimate	CC.EST	<a href="http://databank.worldbank.org/data/reports.aspx?source=worldwide-governance-indicators">http://databank.worldbank.org/data/reports.aspx?source=worldwide-governance-indicators</a>
Ethnic Power Change	ETH Zurich	EPR Core Dataset	Recording of dataset, see variable page	<a href="http://www.icr.ethz.ch/data/epr">http://www.icr.ethz.ch/data/epr</a>

Table 1 - Variable sources (first part)<sup>1</sup>

<sup>1</sup> All datasets have been accessed on September 15<sup>th</sup>, 2017.

<b>Ethnic compilation</b>	ETH Zurich	EPR Core Dataset	Recording of dataset, see variable page	<a href="http://www.icr.ethz.ch/data/epr">http://www.icr.ethz.ch/data/epr</a>
<b>Transnational ethnic bonds</b>	CIDCM Center for International Development & Conflict Management	Marupdate_20042006	GC10	<a href="http://www.mar.umd.edu/mar_data.asp">http://www.mar.umd.edu/mar_data.asp</a>
<b>Homicide rate</b>	World Bank	World Development Indicators	Intentional homicides (per 100,000 people)	<a href="http://data.worldbank.org/indicator/VC.IHR.PSRC.P5">http://data.worldbank.org/indicator/VC.IHR.PSRC.P5</a>
<b>Infant mortality</b>	World Bank	World Development Indicators	Mortality rate, under-5 (per 1,000 live births)	<a href="http://data.worldbank.org/indicator/SH.DYN.MORT">http://data.worldbank.org/indicator/SH.DYN.MORT</a>

Indicator	Source	Name of dataset	Name of original indicator(s)	URL
GDP per capita	World Bank	World Development Indicators	GDP per capita, PPP (constant 2011 international \$)	<a href="http://data.worldbank.org/indicator/NY.GDP.PCAP.PP.KD">http://data.worldbank.org/indicator/NY.GDP.PCAP.PP.KD</a>
Income inequality	Harvard Dataverse Network	The Standardized World Income Inequality Database	Net inequality	<a href="https://dataverse.harvard.edu/dataset.xhtml?persistentId=hdl:1902.1/11992">https://dataverse.harvard.edu/dataset.xhtml?persistentId=hdl:1902.1/11992</a>
Openness	World Bank	World Development Indicators	Foreign direct investment, net inflows (BoP, current US\$)	<a href="http://data.worldbank.org/indicator/BX.KLT.DINV.CD.WD">http://data.worldbank.org/indicator/BX.KLT.DINV.CD.WD</a>
			Foreign direct investment, net inflows (% of GDP)	<a href="http://data.worldbank.org/indicator/BX.KLT.DINV.WD.GD.ZS">http://data.worldbank.org/indicator/BX.KLT.DINV.WD.GD.ZS</a>
			Exports of goods and services (% of GDP)	<a href="http://data.worldbank.org/indicator/NE.EXP.GNFS.ZS">http://data.worldbank.org/indicator/NE.EXP.GNFS.ZS</a>
Food security	FAO	Food security indicators	Average dietary energy supply adequacy	<a href="http://www.fao.org/economic/ess/ess-fs/ess-fadata/en/">http://www.fao.org/economic/ess/ess-fs/ess-fadata/en/</a>
			Domestic food price index	
			Prevalence of undernourishment	
			Domestic food price volatility	
Unemployment	World Bank	World Development Indicators	Unemployment, total (% of total labour force) (modelled ILO estimate)	<a href="http://data.worldbank.org/indicator/SL.UEM.TOTL.ZS">http://data.worldbank.org/indicator/SL.UEM.TOTL.ZS</a>
Water stress	World Resources Institute	Aqueduct Country and River Basin Rankings (Raw country scores)	tdefm	<a href="http://www.wri.org/resources/data-sets/aqueduct-country-and-river-basin-rankings">http://www.wri.org/resources/data-sets/aqueduct-country-and-river-basin-rankings</a>
Oil producer	World Bank	World Development Indicators	Fuel exports (% of merchandise exports)	<a href="http://data.worldbank.org/indicator/TX.VAL.FUEL.ZS.UN">http://data.worldbank.org/indicator/TX.VAL.FUEL.ZS.UN</a>
Structural constraints	BTI: The Bertelsmann Stiftung	BTI 2016	Structural constraints (Q13.1)	<a href="http://www.bti-project.org/en/index/">http://www.bti-project.org/en/index/</a>

<b>Population size</b>	UN DESA/ Population Division	Annual population by single age - Both Sexes.	Sum of all ages	<a href="http://esa.un.org/unpd/wpp/Download/Standard/Interpolated/">http://esa.un.org/unpd/wpp/Download/Standard/Interpolated/</a>
<b>Youth bulge</b>	UN DESA/ Population Division	Annual population by single age - Both Sexes.	Sum of ages 15-24 divided by sum of ages 25+	<a href="http://esa.un.org/unpd/wpp/Download/Standard/Interpolated/">http://esa.un.org/unpd/wpp/Download/Standard/Interpolated/</a>

*Table 2 - Variable sources (second part)<sup>2</sup>*

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<sup>2</sup> All datasets have been accessed on September 15<sup>th</sup>, 2017.

Indicator	Original range	Threshold Min	Threshold Max	Transformation (Before rescaling)	Years covered
Regime type	Parcomp -88 to 5	NA	NA	See variable details.	1800-2015
	Exec -88 to 8	NA	NA		1800-2015
Lack of democracy	-10 to 10	-	-	None	1800-2015
Government effectiveness	-2.49 to 2.43	-	-	None	1996-2015
Level of repression	1 to 5	-	-	None	1976-2015
Empowerment rights	0 to 14	-	-	None	1981-2011
Recent internal conflict	NA	NA	NA	None	1989-2015 (PRIO), 2016 (HIIK)
Neighbours with HVC	NA	NA	NA	None	1989-2015 (PRIO), 2016 (HIIK)
Years since HVC	NA	NA	NA	None	1946-2015 (PRIO), 2016 (HIIK)
Corruption	-2.06 to 2.58	-2	2	None	1996-2015
Ethnic power change	-	-	-	See variable details.	1946-2013
Ethnic compilation	-	-	-	See Table XX	1946-2013
Transnational ethnic bonds	0 to 3	-	-	None	2004-2006
Homicide rate	0 to 139.13	1	50	Log	1995-2014
Infant mortality	1.9 to 332.9	-	-	Log	1989-2015
GDP per capita	246.7 to 137164	-	-	Log	1990-2015
Income inequality	14.06 to 67.21	-	-	None	1960-2015
Openness	Foreign: -29679425810 to 3.065354e+12	100k	15billion	Log	1989-2015
	Foreign 2: -82.89 to 466.6	1	15	Log	1989-2015
	Export: 0.005 to 230	3	200	Log	1989-2015
Food security	Nourishment: 5 to 80.8	5	35	None	1990-2014
	Volatility: 0 to 210.4	-	20	None	1990-2014
	Diet: 68 to 165	75	150	None	1990-2014
	Price level: 1 to 11.69	-	10	None	1990-2014
Unemployment	0.1 to 39.3	2	-	None	1991-2014

Water stress	0.58 to 4.43	0.58	4.44	None	NA
Oil producer	0 to 99.97	1	-	Log	1989-2015
Structural constraints	1 to 10	-	-	None	2006-2016
Population size	0 to 1.38 billion	6	12.5	Log	1989-2016
Youth bulge	0.10 to 0.42	0.12	0.39	None	1989-2016

*Table 3 - Descriptive statistics*

### 3. Regression model

Conflict studies use mostly regression analysis when they want to find a casual relation between the risk of conflict and structural indicators (see e.g. Beck et al., 2000; Bennett and Stam, 2000; Goldstone et al., 2000; Elbadawi and Sambanis, 2002). Based on economic, social, environmental and political data, the regression model used for the GCRI gives an insight into the probability and intensity of conflict at country level. The present chapter describes the model and its outputs.

The regression models described in this chapter are the same generalized linear model (glm) and linear model (lm) described in the two previous JRC technical reports on the GCRI<sup>3</sup>, as well as for the model assumption, the dimension and the related notation.

The regression model is based on equations composed of the variables and respective coefficients. This chapter contributes to the detailed description of the GCRI regression model by explaining how the regression model operates (3.1), what the equations are (3.2), and how the coefficients are calculated (3.3).

#### 3.1. The three phases of the regression model

Figure 1 presents the three different phases that characterize the regression model. Specific statistical methods, i.e. linear and logistic regression, are applied on the input data in order to obtain the output in the form of 8 different scores.

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<sup>3</sup> "The Global Conflict Risk Index (GCRI) A Quantitative Model, Concept and Methodology" (2014), and "The Global Conflict Risk Index (GCRI) Manual for data management and product output, Version 5, Code documentation and methodology summary" (2016).

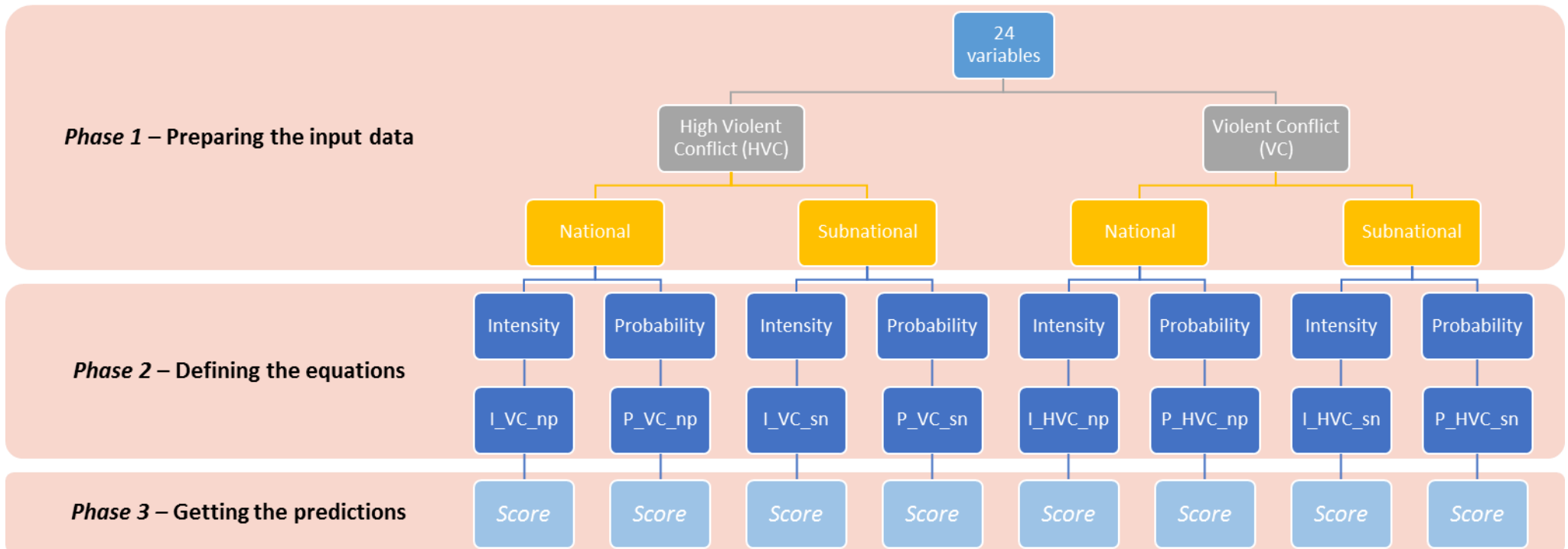


Figure 1 - The regression model



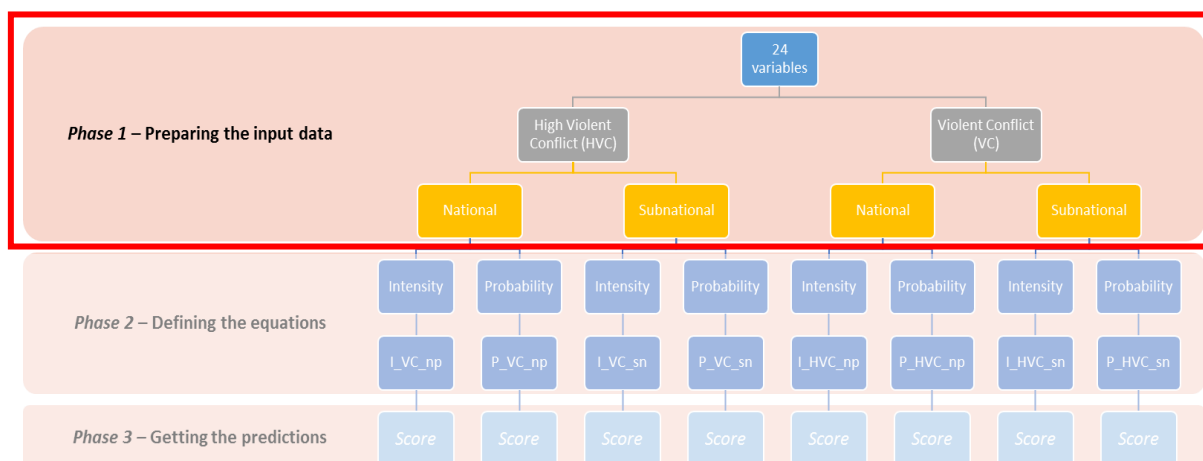


Figure 2 - The regression model, Phase 1

### **Phase 1 – Preparing the input data**

The input data for the regression model are the 24 variables described in Table 1 and Table 2 (p.4 and p.7). The preparation of the input data involves several steps. First of all, the raw data are computed, by imputing data (if necessary) and rescaling the values from 0 to 10 (the meaning of the rescaled values differs according to the variable<sup>4</sup>). Once the first step of the preparation is completed, the second step can start, which consist in further categorisations (Highly violent and violent conflicts; National and subnational conflicts), as described below.

#### **Type of conflict**

Conflicts are categorized according to their type: High Violent Conflict (HVC) or Violent Conflict (VC). This differentiation is made by applying threshold on the variable “Recent Internal Conflict” whose values scale from 0 to 10 (no conflict to high violent conflict). A conflict is classified in the “High Violent Conflict (HVC)” category, if the country/year score for this specific variable is equal or higher than 8. On the other hand, a conflict is classified in the “Violent Conflict (VC)” category when the threshold applied is of 5. Then a lag<sup>5</sup> is calculated, in order to analyse the change of the conflict situation in the next 4 years. More specifically, given a country/year, the highest value among the scores of the 4 following years is taken.

<sup>4</sup> The meanings of the rescaled values are described in the technical report “*Conflict Risk Indicators: Significance and Data Management in the GCRI*” (doi. 10.2760/44005).

<sup>5</sup> A lag refers to a difference in time between an observation and a previous observation. (Eurostat Statistics Explained, Glossary. Available at: <http://ec.europa.eu/eurostat/statistics-explained/index.php/Glossary:Lag>. Retrieved on 26/07/2017)

## Dimension

For each type of conflict (HVC and VC), we look at the two different dimensions of conflict: national and subnational, based on the input data.

## Dataset

As a result of the previous calculations, other variables are added into the dataset used:

- the lag of conflict intensity at the national level (based on the variable "Recent internal conflict");
- the lag of conflict intensity at the subnational level (based on the variable "Recent internal conflict");
- the maximum value between the intensity at the national and subnational levels (based on the variable "Recent internal conflict");
- the value of the variable "Neighbouring with HVC";
- the value of the variable "Years since HVC".

The dataset for running the regression model is complete after applying all these calculations to the raw data. The table below provides an overview on all variables used in the regression model once the preparation of the input data is completed.

Economic, social, political, geographical and environmental factors	Regime Type	REG_U
	Lack of Democracy	REG_P2
	Government Effectiveness	GOV_EFF
	Level of Repression	REPRESS
	Empowerment Rights	EMPOWER
	Corruption	CORRUPT
	Ethnic Power Change	ETHNIC_NP
	Ethnic Compilation	ETHNIC_SN
	Transnational Ethnic Bonds	DISPER
	Homicide Rate	HOMIC
	Infant Mortality	MORT
	GDP per capita	GDP
	Income Inequality	INEQ_SWIID
	Openness	ECON_ISO
	Food Security	FOOD
	Unemployment	UNEMP
	Water Stress	WATER
	Oil Production	FUEL_EXP
	Structural Constraints	STRUCT
	Population Size	POP

	Youth Bulge	YOUTHBOTH	
Maximum value between the intensity at the national and subnational levels	CON_INT		
Value of the intensity in neighbouring countries in HVC	CON_NB		
Value of years since HVC	YRS_HVC		
Intensity at the National level	Intensity_Y_NP		
Lag applied on the intensity at the National level	Intensity_Y4_NP		
Intensity at the Subnational level	Intensity_Y_SN		
Lag applied on the intensity at the Subnational level	Intensity_Y4_SN		
	<b>Applied threshold of:</b>		
Boolean conditions HVC	<b>8</b>	Intensity National (Boolean)	HVC_Y_NP
	<b>8</b>	Lag of Intensity National (Boolean)	HVC_Y4_NP
	<b>8</b>	Intensity Subnational (Boolean)	HVC_Y_SN
	<b>8</b>	Lag of Intensity Subnational (Boolean)	HVC_Y4_SN
Boolean conditions VC	<b>5</b>	Intensity National (Boolean)	VC_Y_NP
	<b>5</b>	Lag of Intensity National (Boolean)	VC_Y4_NP
	<b>5</b>	Intensity Subnational (Boolean)	VC_Y_SN
	<b>5</b>	Lag of Intensity Subnational (Boolean)	VC_Y4_SN

Table 4 - Variables used in the regression model

## Phase 2 – Defining the equations

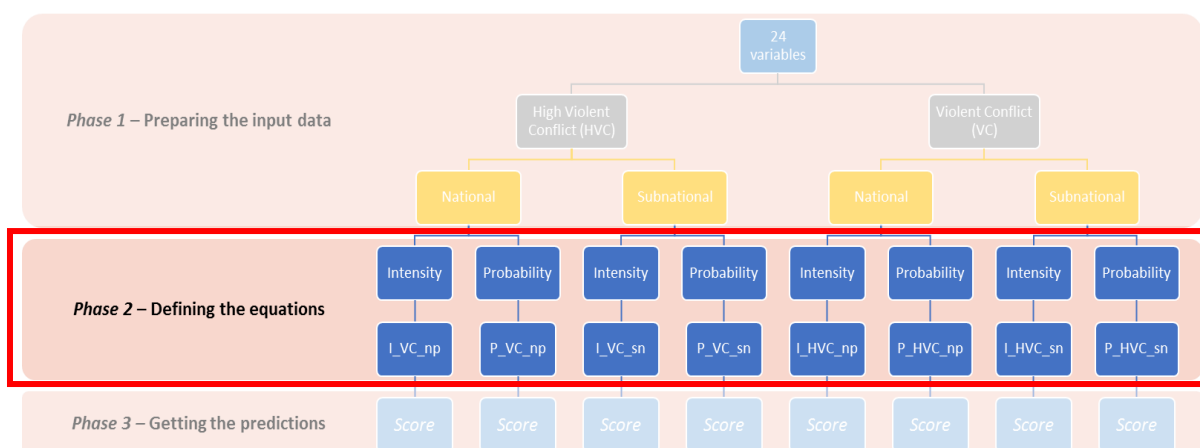


Figure 3 - The regression model, Phase 2

Based on the two categorisations, HVC and VC, National and Subnational, the scope of the assessment is therefore on the four cases listed below:

- 1) Probability and intensity of conflict in HVC at the subnational level;

- 2) Probability and intensity of conflict in HVC at the national level;
- 3) Probability and intensity of conflict in VC at the subnational level;
- 4) Probability and intensity of conflict in VC at the national level.

Two different equations are used to calculate the probability and the intensity, which means that, for each of the four cases presented above, two equations are hence needed. Therefore, 8 equations in total are required to assess the probability and intensity of conflict, and describe the full conflict panorama.

- The **intensity** of a conflict is predicted using a linear model  $l_m$ , which has the following mathematical notation:

$$I = a_0 + a_1X_1 + \dots + a_nX_n$$

Where I is the intensity of the conflict,  $a_0, a_1, a_2, \dots, a_n$  are the coefficients and  $X_1, X_2, \dots, X_n$  are the variables we consider in the model.

- The **probability** of a conflict is predicted using a logistic regression, which uses the generalized linear model  $g_l_m$  and is mathematically defined as follows:

$$p = \frac{e^\gamma}{1 + e^\gamma} ; \quad \gamma = a_0 + a_1x_1 + \dots + a_nx_n$$

Where p is the probability of a conflict,  $a_0, a_1, a_2, \dots, a_n$  are the coefficients and  $X_1, X_2, \dots, X_n$  are the variables we consider in the model.

A schematic overview of the 8 equations, used to run the models, is presented in Table 5.

Name of the equation	Type of conflict	Dimension	Probability or Intensity
P_HVC_NP	HVC	NP	PROBABILITY
P_HVC_SN	HVC	SN	PROBABILITY
P_VC_NP	VC	NP	PROBABILITY
P_VC_SN	VC	SN	PROBABILITY
I_HVC_NP	HVC	NP	INTENSITY

I_HVC_SN	HVC	SN	INTENSITY
I_VC_NP	VC	NP	INTENSITY
I_VC_SN	VC	SN	INTENSITY

Table 5 - The eight equations of the regression model

### Phase 3 – Getting the predictions

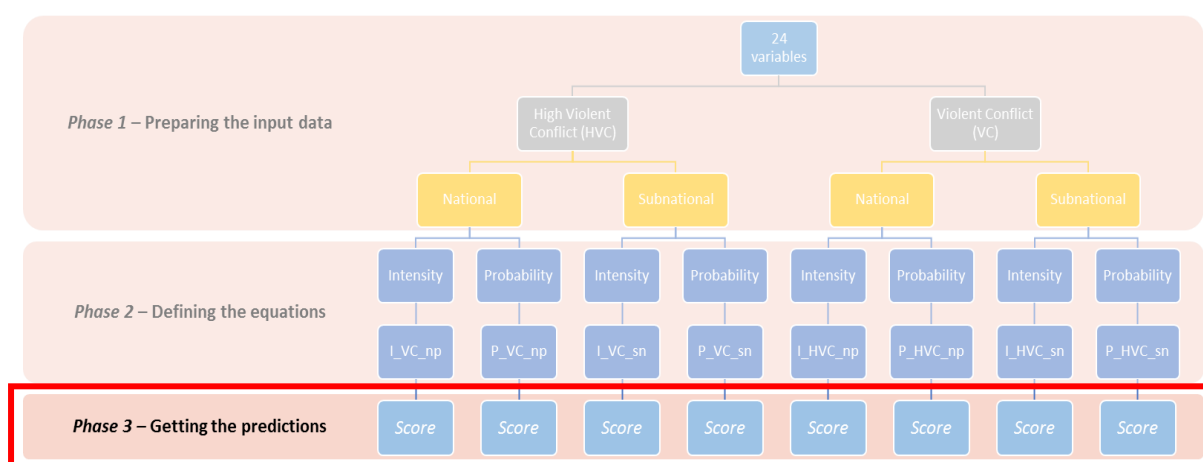


Figure 4 - The regression model, Phase 3

A “fitting” of the regression model is conducted so as to obtain the coefficients and intercept of the equations. For this, we use the two models (glm and lm) that consist of equations, while the quantities appearing in the equations are classified as variables. The fitting uses selected series of data from 1989 to 2011, named the “Dataset for fitting”, which was inherited from previous phase of development. In order to ensure comparability throughout the years, this series is still being used. While all data from 1989 to 2011 are used for calculating the probability, a selection is made for calculating the intensity. In fact, a filter is applied on the dataset (equal to 1, as presented in the column “Filter” in the table below), in order to analyse only the cases experiencing a conflict. The output of the process is a statistical set of information which includes the coefficients and the intercept.

Name of the equation	Filter	Probability or Intensity
P_HVC_NP	None	PROBABILITY
P_HVC_SN	None	PROBABILITY

P_VC_NP	None	PROBABILIY
P_VC_SN	None	PROBABILIY
I_HVC_NP	HVC_Y4_NP==1	INTENSITY
I_HVC_SN	HVC_Y4_SN==1	INTENSITY
I_VC_NP	VC_Y4_NP==1	INTENSITY
I_VC_SN	VC_Y4_SN==1	INTENSITY

Table 6 - Filters applied on the dataset

The calculations to obtain the predictions are performed using the equations and the coefficients and intercept obtained thanks to the “fitting” process. The outputs are scores of the intensity and probability. The following sections describe in detail the equations and the elements composing it.

## 3.2. Equations

All the 8 equations are composed of the same variables, except for *ETHNIC\_NP* that is used only for the National dimension and *ETHNIC\_SN* that is used only for the subnational one. We present in the sub-sections below the explicit equations and the associated coefficients. As described in section 3.1 (p.10) on input data preparation, conflicts are categorized according to their type (high violent conflict or violent conflict) and dimension (national and subnational). The first sub-section describes the equations associated with the conflict type “High Violent Conflict”, whereas the second sub-section describes the equations associated with the conflict type “Violent Conflict”.

### 3.2.1. High Violent Model Equations

This sub-section introduces the equations for calculating the probability and intensity of conflict, and the quantities appearing in the equations. In this sub-section, it applies specifically to each of the two dimensions “National” and “Subnational”, inside the conflict type “High Violent Conflict”. The quantities appearing in the equations presented below are the variables (in black) and associated coefficients (in orange). The coefficients are described in detailed in section 3.3 (p.20).

#### **High Violent Conflict (HVC), National Dimension, Intensity (I\_HVC\_NP)**

To calculate the Intensity for *National Conflict* (I\_HVC\_NP), the equation is:

$$I\_HVC\_NP = -1.108*REG\_U+ -0.358*INEQ\_SWIID+ -0.399*GDP\_CAP+ 0.203*REG\_U*INEQ\_SWIID+ 0.036*INEQ\_SWIID*GDP\_CAP+ 0.158*REG\_U*GDP\_CAP + -0.029*REG\_U*INEQ\_SWIID*GDP\_CAP+ 0.054*REG\_P2+ -0.205*GOV\_EFF+ -0.094*EMPOWER+ 0.027*REPRESS+ 0.033*CON\_NB+ -0.003*YRS\_HVC+ 0.031*CON\_INT+ -0.144 *MORT+ -0.036 *DISPER+ -0.101 *HOMIC+ -0.056 *ETHNIC\_NP+ 0.185 *FOOD+ 0.059*POP+ -0.094*WATER+ -0.051 *ECON\_ISO+ 0.006 *FUEL\_EXP+ 0.122*STRUCT+ -0.007*UNEMP+ 0.312*YOUTHBBOTH+ 0.275*CORRUPT+ 9.574$$

### High Violent Conflict (HVC), National Dimension, Probability (P\_HVC\_NP)

To calculate the Probability for *National Conflicts* (P\_HVC\_NP):

$$P\_HVC\_NP = \text{EXP}(\gamma) / (1+\text{EXP}(\gamma))$$

$$\gamma = -1.166*REG\_U+ -1.685*INEQ\_SWIID+ -1.302*GDP\_CAP+ 0.219*REG\_U*INEQ\_SWIID+ 0.181*INEQ\_SWIID*GDP\_CAP+ -0.134*REG\_U*GDP\_CAP + -0.026*REG\_U*INEQ\_SWIID*GDP\_CAP + 0.024*REG\_P2+ 0.310*GOV\_EFF+ -0.105*EMPOWER+ 0.152*REPRESS+ 0.069*CON\_NB+ 0.171*YRS\_HVC+ 0.229*CON\_INT+ 0.214*MORT+ -0.075*DISPER+ 0.104*HOMIC+ -0.037*ETHNIC\_NP+ -0.089*FOOD+ 0.110*POP+ 0.052*WATER+ 0.110*ECON\_ISO+ 0.067*FUEL\_EXP+ 0.448*STRUCT+ -0.098*UNEMP+ 0.468*YOUTHBBOTH+ 0.034*CORRUPT+ -4.881$$

### High Violent Conflict (HVC), Sub National Dimension, Intensity (I\_HVC\_SN)

To calculate the Intensity for *Subnational Conflict* (I\_HVC\_SN):

$$I\_HVC\_SN = -0.016*REG\_U+ -0.132*INEQ\_SWIID+ 0.078*GDP\_CAP+ 0.001*REG\_U*INEQ\_SWIID+ -0.006*INEQ\_SWIID*GDP\_CAP+ -0.009*REG\_U*GDP\_CAP+ 0.002*REG\_U*INEQ\_SWIID*GDP\_CAP + -0.006*REG\_P2+ 0.039*GOV\_EFF+ 0.022*EMPOWER+ -0.009*REPRESS+ -0.008 *CON\_NB+ 0.026*YRS\_HVC+ -0.009*CON\_INT+ 0.136*MORT+ -0.041*DISPER+ 0.014*HOMIC+ 0.053*ETHNIC\_SN+ 0.063*FOOD+ 0.056*POP+ 0.018*WATER+ -0.015*ECON\_ISO+ 0.004*FUEL\_EXP+ -0.128*STRUCT+ 0.052*UNEMP+ -0.043*YOUTHBBOTH+ 0.037*CORRUPT+ 8.435$$

### High Violent Conflict (HVC), Sub National Dimension, Probability (P\_HVC\_SN)

To calculate the Probability for *Subnational Conflicts* (P\_HVC\_SN):

$$P\_HVC\_SN = \text{EXP}(\gamma) / (1+\text{EXP}(\gamma))$$

$$\begin{aligned} \gamma = & 1.010*REG\_U+ 0.477*INEQ\_SWIID+ 0.647*GDP\_CAP+ -0.198*REG\_U*INEQ\_SWIID+ - \\ & 0.146*INEQ\_SWIID*GDP\_CAP+ \quad \quad \quad - \quad \quad \quad 0.194*REG\_U*GDP\_CAP \quad \quad \quad + \\ & 0.038*REG\_U*INEQ\_SWIID*GDP\_CAP + 0.008*REG\_P2+ 0.439*GOV\_EFF+ 0.06*EMPOWER+ \\ & 0.221*REPRESS+ -0.008*CON\_NB+ -0.050*YRS\_HVC+ 0.308*CON\_INT+ 0.281*MORT+ - \\ & 0.065*DISPER+ 0.147*HOMIC+ 0.257*ETHNIC\_SN+ 0.062*FOOD+ 0.478*POP+ - \\ & 0.125*WATER+ -0.053*ECON\_ISO+ -0.144*FUEL\_EXP+ -0.221*STRUCT+ 0.241*UNEMP+ - \\ & 0.231*YOUTHBBOTH+ -0.139*CORRUPT+ -11.738 \end{aligned}$$

### 3.2.2. Violent Model Equations

This sub-section introduces the equations for calculating the probability and intensity of conflict, and the quantities appearing in the equations. In this sub-section, it applies specifically to each of the two dimensions “National” and “Subnational”, inside the conflict type “Violent Conflict”. The quantities appearing in the equations presented below are the variables (in black) and associated coefficients (in orange).

#### Violent Conflict (VC), National Dimension, Intensity (I\_VC\_NP)

To calculate the Intensity for *National Conflict* (I\_VC\_NP):

$$\begin{aligned} I\_VC\_NP = & -1.238*REG\_U+ \quad \quad \quad -1.088*INEQ\_SWIID+ \quad \quad \quad -1.009*GDP\_CAP+ \\ & 0.189*REG\_U*INEQ\_SWIID+ 0.119*INEQ\_SWIID*GDP\_CAP+ 0.171*REG\_U*GDP\_CAP+ - \\ & 0.026*REG\_U*INEQ\_SWIID*GDP\_CAP + 0.073*REG\_P2+ -0.057*GOV\_EFF+ -0.092*EMPOWER+ \\ & 0.015*REPRESS+ \quad \quad \quad -0.022*CON\_NB+0.112*YRS\_HVC+0.123*CON\_INT+0.084*MORT+ \quad \quad \quad - \\ & 0.032*DISPER+ 0.020*HOMIC+ -0.042*ETHNIC\_NP+ -0.030*FOOD+ 0.024*POP+ - \\ & 0.140*WATER+ 0.015*ECON\_ISO+ 0.065*FUEL\_EXP+ 0.266*STRUCT+ -0.076*UNEMP+ \\ & 0.330*YOUTHBBOTH+ 0.353*CORRUPT+8.331 \end{aligned}$$

#### Violent Conflict (VC), National Dimension, Probability (P\_VC\_NP)

To calculate the Probability for *National Conflicts* (P\_VC\_NP):

$$P\_VC\_NP = \text{EXP}(\gamma) / (1+\text{EXP}(\gamma))$$

$$\begin{aligned} \gamma = & 0.324*REG\_U+ -0.538*INEQ\_SWIID+ -0.192*GDP\_CAP+ 0.016*REG\_U*INEQ\_SWIID+ \\ & 0.028*INEQ\_SWIID*GDP\_CAP+ \quad \quad \quad - \quad \quad \quad 0.093*REG\_U*GDP\_CAP \quad \quad \quad + \\ & 0.006*REG\_U*INEQ\_SWIID*GDP\_CAP + -0.025*REG\_P2+ 0.587*GOV\_EFF+ -0.126*EMPOWER+ \\ & 0.155*REPRESS+ 0.164*CON\_NB+ 0.125*YRS\_HVC+ 0.210*CON\_INT+ 0.239*MORT+ - \\ & 0.075*DISPER+ 0.042*HOMIC+ -0.012*ETHNIC\_NP+ -0.066*FOOD+ 0.181*POP+ \\ & 0.211*WATER+ 0.003*ECON\_ISO+ 0.053*FUEL\_EXP+ 0.420*STRUCT+ 0.002*UNEMP+ \\ & 0.196*YOUTHBBOTH+ -0.263*CORRUPT+ -10.06 \end{aligned}$$



### Violent Conflict (VC), Sub National Dimension, Intensity (I\_VC\_SN)

To calculate the Intensity for *Subnational Conflict* (I\_VC\_SN):

$$\begin{aligned} I\_VC\_NP = & 0.872*REG\_U+ 0.446*INEQ\_SWIID+ 0.777*GDP\_CAP+ - \\ & 0.175*REG\_U*INEQ\_SWIID+ -0.110*INEQ\_SWIID*GDP\_CAP+ -0.157*REG\_U*GDP\_CAP+ 0.032 \\ & REG\_U*INEQ\_SWIID*GDP\_CAP + 0.021*REG\_P2+ 0.238*GOV\_EFF+ 0.059*EMPOWER+ \\ & 0.040*REPRESS+ -0.025*CON\_NB+ 0.001*YRS\_HVC+ 0.151*CON\_INT+ -0.036*MORT+ - \\ & 0.057*DISPER+ 0.051*HOMIC+ 0.098*ETHNIC\_SN+ -0.017*FOOD+ 0.310*POP+ - \\ & 0.075*WATER+ -0.070*ECON\_ISO+ -0.075*FUEL\_EXP+ -0.112*STRUCT+ 0.217*UNEMP+ - \\ & 0.160*YOUTHBBOTH+ 0.076*CORRUPT+0.275 \end{aligned}$$

### Violent Conflict (VC), Sub National Dimension, Probability (P\_VC\_SN)

To calculate the Probability for *Subnational Conflicts* (P\_VC\_SN):

$$P\_VC\_SN = \text{EXP}(\gamma) / (1+\text{EXP}(\gamma))$$

$$\begin{aligned} \gamma = & 1.074*REG\_U+ 0.114*INEQ\_SWIID+ -0.007*GDP\_CAP+ -0.064*REG\_U*INEQ\_SWIID+ - \\ & 0.004*INEQ\_SWIID*GDP\_CAP+ - 0.148*REG\_U*GDP\_CAP + \\ & 0.020*REG\_U*INEQ\_SWIID*GDP\_CAP + -0.081*REG\_P2+ 0.052*GOV\_EFF+ -0.084*EMPOWER+ \\ & 0.178*REPRESS+ -0.009*CON\_NB+ -0.035*YRS\_HVC+ 0.285*CON\_INT+ 0.396*MORT+ \\ & 0.072*DISPER+ 0.033*HOMIC+ 0.244*ETHNIC\_SN+ 0.002*FOOD+ 0.289*POP+ 0.018*WATER+ \\ & -0.039*ECON\_ISO+ 0.009*FUEL\_EXP+ 0.025*STRUCT+ -0.100*UNEMP+ 0.091*YOUTHBBOTH+ \\ & 0.164*CORRUPT+ -8.547 \end{aligned}$$

## 3.3. Coefficients

The coefficients give a specific weight to the variables they are associated to. The coefficients are either positive (it corresponds to a reinforcing effect) or negative (it corresponds to a hindering effect). As described in the section 3.2 (p.17) presenting the equations, the coefficients are one of the two quantities appearing in the equations for calculating the probability and intensity of conflict, together with the variables. The following sub-sections list the coefficients used in the equations. The coefficients used for the conflict type "High violent conflict" are presented in the first sub-section whereas the coefficients used for the conflict type "Violent conflict" are presented in the second sub-section.

### 3.3.1. High Violent Model Coefficients

This sub-section introduces the coefficients used for calculating the probability and intensity of conflict. As shown in the tables below, the coefficients are associated to specific variables. In this sub-section, it applies specifically to each of the two dimensions "National" and "Subnational", inside the conflict type "High Violent Conflict".

#### High Violent Model Coefficients National Dimension

The coefficients used for calculating the probability of conflict are listed on the left side of the tables (*NP HVC Prob*), and the coefficients used for calculating the intensity of conflict are listed on the right side of the tables (*NP HVC Intensity*).

NP HVC Prob		NP HVC Intensity	
(Intercept)	-4.8815	(Intercept)	9.5742
REG_U	-1.1670	REG_U	-1.1083
INEQ_SWIID	-1.6856	INEQ_SWIID	-0.3588
GDP_CAP	-1.3024	GDP_CAP	-0.3992
REG_P2	0.0246	REG_P2	0.0540
GOV_EFF	0.3109	GOV_EFF	-0.2060
EMPOWER	-0.1053	EMPOWER	-0.0944
REPRESS	0.1526	REPRESS	0.0273
CON_NB	0.0694	CON_NB	0.0333
YRS_HVC	0.1717	YRS_HVC	-0.0032
CON_INT	0.2291	CON_INT	0.0312
MORT	0.2148	MORT	-0.1444
DISPER	-0.0758	DISPER	-0.0367
HOMIC	0.1047	HOMIC	-0.1014
ETHNIC_NP	-0.0374	ETHNIC_NP	-0.0566
FOOD	-0.0898	FOOD	0.1851
POP	0.1102	POP	0.0600
WATER	0.0530	WATER	-0.0941
ECON_ISO	0.1108	ECON_ISO	-0.0514
FUEL_EXP	0.0677	FUEL_EXP	0.0061
STRUCT	0.4485	STRUCT	0.1225
UNEMP	-0.0985	UNEMP	-0.0079
YOUTHBBOTH	0.4688	YOUTHBBOTH	0.3122
CORRUPT	0.0340	CORRUPT	0.2759

REG_U:INEQ_SWIID	0.2192	REG_U:INEQ_SWIID	0.2040
REG_U:GDP_CAP	0.1348	REG_U:GDP_CAP	0.1585
INEQ_SWIID:GDP_CAP	0.1818	INEQ_SWIID:GDP_CAP	0.0361
REG_U:INEQ_SWIID:GDP_CAP	-0.0263	REG_U:INEQ_SWIID:GDP_CAP	-0.0293

Table 7 - High Violent Model Coefficients National Dimension

### High Violent Model Coefficients Sub National Dimension

The coefficients used for calculating the probability of conflict are listed on the left side of the tables (*SN HVC Prob*), and the coefficients used for calculating the intensity of conflict are listed on the right side of the tables (*SN HVC Intensity*).

SN HVC Prob		SN HVC Intensity	
(Intercept)	-11.7387	(Intercept)	8.4356
REG_U	1.0105	REG_U	-0.0168
INEQ_SWIID	0.4779	INEQ_SWIID	-0.1322
GDP_CAP	0.6470	GDP_CAP	0.0788
REG_P2	0.0081	REG_P2	-0.0063
GOV_EFF	0.4392	GOV_EFF	0.0392
EMPOWER	0.0620	EMPOWER	0.0226
REPRESS	0.2214	REPRESS	-0.0097
CON_NB	-0.0088	CON_NB	-0.0089
YRS_HVC	-0.0509	YRS_HVC	0.0262
CON_INT	0.3080	CON_INT	-0.0091
MORT	0.2813	MORT	0.1364
DISPER	-0.0658	DISPER	-0.0416
HOMIC	0.1479	HOMIC	0.0145
ETHNIC_SN	0.2573	ETHNIC_SN	0.0538
FOOD	0.0621	FOOD	0.0635
POP	0.4784	POP	0.0569
WATER	-0.1255	WATER	0.0181
ECON_ISO	-0.0532	ECON_ISO	-0.0155
FUEL_EXP	-0.1443	FUEL_EXP	0.0048
STRUCT	-0.2211	STRUCT	-0.1288
UNEMP	0.2417	UNEMP	0.0522
YOUTHBBOTH	-0.2312	YOUTHBBOTH	-0.0435
CORRUPT	-0.1391	CORRUPT	0.0372

REG_U:INEQ_SWIID	-0.1987	REG_U:INEQ_SWIID	0.0014
REG_U:GDP_CAP	-0.1950	REG_U:GDP_CAP	-0.0092
INEQ_SWIID:GDP_CAP	-0.1463	INEQ_SWIID:GDP_CAP	-0.0067
REG_U:INEQ_SWIID:GDP_CAP	0.0387	REG_U:INEQ_SWIID:GDP_CAP	0.0028

Table 8 - High Violent Model Coefficients Sub National Dimension

### 3.3.2. Violent Model Coefficients

This sub-section introduces the coefficients used for calculating the probability and intensity of conflict. As shown in the tables below, the coefficients are associated to specific variables. In this sub-section, it applies specifically to each of the two dimensions "National" and "Subnational", inside the conflict type "Violent Conflict".

#### Violent Model Coefficients National Dimension

The coefficients used for calculating the probability of conflict are listed on the left side of the tables (*NP VC Prob*), and the coefficients used for calculating the intensity of conflict are listed on the right side of the tables (*NP VC Intensity*).

NP VC Prob		NP VC Intensity	
(Intercept)	-10.0602	(Intercept)	8.3311
REG_U	0.3250	REG_U	-1.2381
INEQ_SWIID	-0.5386	INEQ_SWIID	-1.0888
GDP_CAP	-0.1929	GDP_CAP	-1.0095
REG_P2	-0.0250	REG_P2	0.0734
GOV_EFF	0.5877	GOV_EFF	-0.0577
EMPOWER	-0.1265	EMPOWER	-0.0924
REPRESS	0.1550	REPRESS	0.0159
CON_NB	0.1640	CON_NB	-0.0225
YRS_HVC	0.1257	YRS_HVC	0.1126
CON_INT	0.2106	CON_INT	0.1238
MORT	0.2400	MORT	0.0841
DISPER	-0.0759	DISPER	-0.0323
HOMIC	0.0424	HOMIC	0.0203
ETHNIC_NP	-0.0126	ETHNIC_NP	-0.0426
FOOD	-0.0661	FOOD	-0.0301
POP	0.1814	POP	0.0250

WATER	0.2120	WATER	-0.1402
ECON_ISO	0.0039	ECON_ISO	0.0160
FUEL_EXP	0.0530	FUEL_EXP	0.0656
STRUCT	0.4203	STRUCT	0.2664
UNEMP	0.0029	UNEMP	-0.0763
YOUTHBBOTH	0.1969	YOUTHBBOTH	0.3305
CORRUPT	-0.2631	CORRUPT	0.3531
REG_U:INEQ_SWIID	0.0166	REG_U:INEQ_SWIID	0.1891
REG_U:GDP_CAP	-0.0930	REG_U:GDP_CAP	0.1718
INEQ_SWIID:GDP_CAP	0.0280	INEQ_SWIID:GDP_CAP	0.1199
REG_U:INEQ_SWIID:GDP_CAP	0.0063	REG_U:INEQ_SWIID:GDP_CAP	-0.0269

Table 9 - Violent Model Coefficients National Dimension

### Violent Model Coefficients Sub National Dimension

The coefficients used for calculating the probability of conflict are listed on the left side of the tables (*SN VC Prob*), and the coefficients used for calculating the intensity of conflict are listed on the right side of the tables (*SN VC Intensity*).

SN VC Prob		SN VC Intensity	
(Intercept)	-8.5473	(Intercept)	0.2752
REG_U	1.0750	REG_U	0.8728
INEQ_SWIID	0.1146	INEQ_SWIID	0.4468
GDP_CAP	-0.0076	GDP_CAP	0.7776
REG_P2	-0.0814	REG_P2	0.0214
GOV_EFF	-0.0523	GOV_EFF	0.2382
EMPOWER	-0.0846	EMPOWER	0.0595
REPRESS	0.1784	REPRESS	0.0407
CON_NB	-0.0091	CON_NB	-0.0251
YRS_HVC	-0.0356	YRS_HVC	0.0016
CON_INT	0.2855	CON_INT	0.1519
MORT	0.3964	MORT	-0.0362
DISPER	0.0722	DISPER	-0.0572
HOMIC	0.0340	HOMIC	0.0512
ETHNIC_SN	0.2446	ETHNIC_SN	0.0985
FOOD	0.0027	FOOD	-0.0178
POP	0.2896	POP	0.3101
WATER	0.0187	WATER	-0.0751

ECON_ISO	-0.0399	ECON_ISO	-0.0708
FUEL_EXP	0.0099	FUEL_EXP	-0.0754
STRUCT	0.0256	STRUCT	-0.1127
UNEMP	-0.1009	UNEMP	0.2180
YOUTHBBOTH	0.0917	YOUTHBBOTH	-0.1603
CORRUPT	0.1649	CORRUPT	0.0765
REG_U:INEQ_SWIID	-0.1650	REG_U:INEQ_SWIID	-0.1754
REG_U:GDP_CAP	-0.1488	REG_U:GDP_CAP	-0.1576
INEQ_SWIID:GDP_CAP	-0.0044	INEQ_SWIID:GDP_CAP	-0.1103
REG_U:INEQ_SWIID:GDP_CAP	0.0204	REG_U:INEQ_SWIID:GDP_CAP	0.0323

Table 10 - Violent Model Coefficients Sub National Dimension

#### 4. Statistical significance test

In a multiple linear regression with  $p$  variables and  $n$  observations, we do have the dependent (or “predicted”) variable  $y$  modelled as a linear combination of the  $x$  variables (covariates) and the  $\beta$  parameters (coefficients of the linear equation)<sup>6</sup>. The corresponding equation is as follows:

$$y_i = \beta_0 + \beta_1 x_{i1} + \beta_2 x_{i2} + \dots + \beta_p x_{ip} + \varepsilon_i \text{ for } i = 1, 2, \dots, n \text{ (Equation 1)}$$

The t-test (or Student test) allows us to test the following null hypothesis for any parameter  $\beta_j$  :

$$H_0: \beta_j = 0$$

The alternative hypothesis is

$$H_1: \beta_j \neq 0$$

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<sup>6</sup> For a deeper introduction to the use of the linear model in the study of armed conflicts, see Kauffmann, Mayeul. *Méthodes statistiques appliquées aux questions internationales*, March 2009, 197 p., L’Harmattan, Paris

The null hypothesis is the hypothesis that the coefficient equals zero. The ability to assess this hypothesis and the alternative hypothesis contributes to the model's falsifiability and is a significant element of the scientificity of the approach<sup>7</sup>.

It should be noted here that we do not know the true value of the  $\beta_j$  coefficient

(because of, inter alia, measurement errors); we only have an estimate  $\tilde{\beta}_j$  of the  $j^{\text{th}}$

coefficient of equation  $y_i = \beta_0 + \beta_1 x_{i1} + \beta_2 x_{i2} + \dots + \beta_p x_{ip} + \varepsilon_i$  for  $i = 1, 2, \dots, n$  (Equation 1).

The estimates  $\tilde{\beta}_j$  are reported in the first numeric column of the tables showing the estimated models below; the first row ("Intercept") corresponds to  $\tilde{\beta}_0$  (the constant part of the equation), while the following rows correspond to the  $\beta_j$  coefficients relevant to each covariate  $j$ .

Small random variations in the dataset may lead to an estimate of the coefficient  $\tilde{\beta}_j$  which is slightly different from zero, but not significantly different enough to allow us to reject the null hypothesis that the true (unknown)  $\beta_j$  coefficient is indeed zero ; in this case, this is equivalent to saying that the  $x_j$  covariate has no significant impact on  $y$  (in our case, that a given GCRI component has no significant impact on the intensity of conflict in a particular model, assuming that this model is appropriate). If  $H_0$  is rejected, we then keep the alternative hypothesis that the parameter is most likely different from zero.

In the case of the linear models used to model the intensity of conflict, the test statistic is the t statistic, defined as the estimate of the parameter divided by its standard deviation (this is shown in tables below in the column "t value"). Under appropriate hypotheses, the test statistic t follows a Student's distribution with  $n - (p+1)$  degrees of freedom. If there was no uncertainty and if the covariates had no impact on  $y$ , then the t

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<sup>7</sup> For a more thorough discussion of these concepts in view of Popper's epistemology, see Kauffmann, Mayeul, "Introduction" in Kauffmann, Mayeul (ed.) *Building and Using Datasets on Armed Conflicts*, May 2008, Amsterdam: IOS Press, 204 p. ISBN: 978-1586038472 <http://ebooks.iospress.nl/volume/building-and-using-datasets-on-armed-conflicts>

values would all be equal to zero. Because of uncertainty, a t value different from zero might still be compatible with the null hypothesis. The last column of the table,  $\Pr(>|t|)$ , also named the “p-value”, measures the probability that we get a t value that far from zero (or even further from zero than the t value), given that the null hypothesis is assumed to be true. If this probability is very low (often, below 5% or 0.05) we use a decision rule which says that the null hypothesis should be rejected. If the p-value is higher than the threshold, then the null hypothesis cannot be rejected.

It should be emphasised that the p-value associated with the t-test is only a hint on the likelihood of the impact of a covariate on the dependent variable. In no way can a p-value of 0.05 be interpreted as: “the probability of incorrectly rejecting a true null hypothesis is 5 %” (such a probability has been measured to be greater than 23 % and typically close to 50 % by Sellke et al. (2001))<sup>8</sup> .

The interpretation of the four logistic models<sup>9</sup> below (modelling the probability of conflict) is similar to that of the linear models (for conflict intensity) if we look at the p-value. The test statistic, however, is different. In effect, it can be demonstrated that the estimate divided by its standard errors follows (under the null hypothesis) a normal distribution (not a Student distribution); in this case, the test statistic is named z. Hence, the p-value is  $\Pr(>|z|)$  as shown in the last column of the tables related to the logistic models.

### Probability of VC\_NP logistic model

	Estimate	Std. Error	z value	$\Pr(> z )$
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<sup>8</sup> Thomas SELLKE, M. J. BAYARRI, and James O. BERGER, “Calibration of p Values for Testing Precise Null Hypotheses”, *The American Statistician*, February 2001, Vol. 55, No. 1, pp. 63-64. Available at [http://www.cems.uvm.edu/~jbuzas/buzas/calibrating\\_p\\_values.pdf](http://www.cems.uvm.edu/~jbuzas/buzas/calibrating_p_values.pdf)

<sup>9</sup> For a presentation of the Generalized Linear Model (of which the logistic model is a particular case) in the context of conflict modelling, and a review of several GLMs, see: Kauffmann, Mayeul, “Short Term and Event Interdependence Matter: A Political Economy Continuous Model of Civil War”, in *Peace Economics, Peace Science and Public Policy*, Vol. 13, Issue 1, 2007, BE-Press (Berkeley), 19 p. See also: Kucera Jan; Kauffmann Mayeul; Duta Ana-Maria; Soler Ivette Tarrida; Tenerelli Patrizia; Trianni Giovanna; Hale Catherine; Rizzo Lauren; Ferri Stefano. *Armed conflicts and natural resources - Scientific report on Global Atlas and Information Centre for Conflicts and Natural Resources*. 2011. European Commission - Scientific and Technical Research Reports. ISBN 978-92-79-20498-2, pp. 23-28. Kauffmann, Mayeul, *Gouvernance économique mondiale et conflits armés*. Banque mondiale, FMI et GATT-OMC, Paris: l’Harmattan, May 2006, 330 p.



(Intercept)	-10.0602	2.2051	-4.56	0.0000
REG_U	0.3250	0.3691	0.88	0.3787
INEQ_SWIID	-0.5386	0.3885	-1.39	0.1656
GDP_CAP	-0.1929	0.3489	-0.55	0.5804
REG_P2	-0.0250	0.0359	-0.70	0.4869
GOV_EFF	0.5877	0.1122	5.24	0.0000
EMPOWER	-0.1265	0.0419	-3.02	0.0026
REPRESS	0.1550	0.0387	4.01	0.0001
CON_NB	0.1640	0.0200	8.22	0.0000
YRS_HVC	0.1257	0.0235	5.34	0.0000
CON_INT	0.2106	0.0245	8.61	0.0000
MORT	0.2400	0.0838	2.86	0.0042
DISPER	-0.0759	0.0192	-3.95	0.0001
HOMIC	0.0424	0.0355	1.19	0.2333
ETHNIC_NP	-0.0126	0.0350	-0.36	0.7180
FOOD	-0.0661	0.0443	-1.49	0.1355
POP	0.1814	0.0430	4.22	0.0000
WATER	0.2120	0.0427	4.97	0.0000
ECON_ISO	0.0039	0.0565	0.07	0.9452
FUEL_EXP	0.0530	0.0229	2.31	0.0207
STRUCT	0.4203	0.0607	6.92	0.0000
UNEMP	0.0029	0.0360	0.08	0.9348

YOUTHBOTH	0.1969	0.0665	2.96	0.0031
CORRUPT	-0.2631	0.0965	-2.73	0.0064
REG_U:INEQ_SWIID	0.0166	0.0678	0.25	0.8060
REG_U:GDP_CAP	-0.0930	0.0577	-1.61	0.1068
INEQ_SWIID:GDP_CAP	0.0280	0.0631	0.44	0.6572
REG_U:INEQ_SWIID:GDP_CAP	0.0063	0.0107	0.59	0.5557

Table 11- Probability of VC\_NP logistic model

### Intensity of VC\_NP linear model

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	8.3311	2.9236	2.85	0.0045
REG_U	-1.2381	0.4856	-2.55	0.0110
INEQ_SWIID	-1.0888	0.5332	-2.04	0.0416
GDP_CAP	-1.0095	0.4492	-2.25	0.0250
REG_P2	0.0734	0.0491	1.49	0.1355
GOV_EFF	-0.0577	0.1540	-0.37	0.7082
EMPOWER	-0.0924	0.0527	-1.75	0.0801
REPRESS	0.0159	0.0527	0.30	0.7634
CON_NB	-0.0225	0.0281	-0.80	0.4237
YRS_HVC	0.1126	0.0273	4.12	0.0000
CON_INT	0.1238	0.0322	3.84	0.0001
MORT	0.0841	0.1207	0.70	0.4861
DISPER	-0.0323	0.0254	-1.27	0.2033

HOMIC	0.0203	0.0533	0.38	0.7030
ETHNIC_NP	-0.0426	0.0402	-1.06	0.2895
FOOD	-0.0301	0.0714	-0.42	0.6737
POP	0.0250	0.0691	0.36	0.7177
WATER	-0.1402	0.0588	-2.38	0.0175
ECON_ISO	0.0160	0.0747	0.21	0.8309
FUEL_EXP	0.0656	0.0315	2.08	0.0375
STRUCT	0.2664	0.0849	3.14	0.0018
UNEMP	-0.0763	0.0530	-1.44	0.1501
YOUTHBOTH	0.3305	0.1016	3.25	0.0012
CORRUPT	0.3531	0.1336	2.64	0.0085
REG_U:INEQ_SWIID	0.1891	0.0867	2.18	0.0295
REG_U:GDP_CAP	0.1718	0.0731	2.35	0.0190
INEQ_SWIID:GDP_CAP	0.1199	0.0822	1.46	0.1456
REG_U:INEQ_SWIID:GDP_CAP	-0.0269	0.0134	-2.01	0.0445

Table 12 – Intensity of VC\_NP linear model

### Probability of VC\_SN logistic model

	Estimate	Std. Error	z value	Pr(> z )
(Intercept)	-8.5473	1.4543	-5.88	0.0000
REG_U	1.0750	0.2613	4.11	0.0000
INEQ_SWIID	0.1146	0.2829	0.41	0.6853
GDP_CAP	-0.0076	0.2598	-0.03	0.9765

REG_P2	-0.0814	0.0327	-2.49	0.0128
GOV_EFF	-0.0523	0.0973	-0.54	0.5910
EMPOWER	-0.0846	0.0369	-2.29	0.0221
REPRESS	0.1784	0.0345	5.18	0.0000
CON_NB	-0.0091	0.0159	-0.58	0.5645
YRS_HVC	-0.0356	0.0244	-1.45	0.1457
CON_INT	0.2855	0.0232	12.33	0.0000
MORT	0.3964	0.0777	5.10	0.0000
DISPER	0.0722	0.0168	4.30	0.0000
HOMIC	0.0340	0.0312	1.09	0.2755
ETHNIC_SN	0.2446	0.0258	9.48	0.0000
FOOD	0.0027	0.0422	0.06	0.9497
POP	0.2896	0.0353	8.20	0.0000
WATER	0.0187	0.0371	0.50	0.6151
ECON_ISO	-0.0399	0.0505	-0.79	0.4288
FUEL_EXP	0.0099	0.0201	0.50	0.6204
STRUCT	0.0256	0.0498	0.51	0.6070
UNEMP	-0.1009	0.0284	-3.55	0.0004
YOUTHBOTH	0.0917	0.0533	1.72	0.0852
CORRUPT	0.1649	0.0854	1.93	0.0535
REG_U:INEQ_SWIID	-0.1650	0.0527	-3.13	0.0017
REG_U:GDP_CAP	-0.1488	0.0451	-3.30	0.0010

INEQ_SWIID:GDP_CAP	-0.0044	0.0488	-0.09	0.9276
REG_U:INEQ_SWIID:GDP_CAP	0.0204	0.0090	2.26	0.0240

Table 13 – Probability of VC\_SN logistic model

### Intensity of VC\_SN linear model

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	0.2752	1.5629	0.18	0.8603
REG_U	0.8728	0.2510	3.48	0.0005
INEQ_SWIID	0.4468	0.3077	1.45	0.1469
GDP_CAP	0.7776	0.2668	2.91	0.0036
REG_P2	0.0214	0.0338	0.63	0.5277
GOV_EFF	0.2382	0.1071	2.22	0.0264
EMPOWER	0.0595	0.0371	1.61	0.1084
REPRESS	0.0407	0.0382	1.06	0.2879
CON_NB	-0.0251	0.0175	-1.44	0.1513
YRS_HVC	0.0016	0.0190	0.08	0.9332
CON_INT	0.1519	0.0208	7.29	0.0000
MORT	-0.0362	0.0793	-0.46	0.6483
DISPER	-0.0572	0.0188	-3.04	0.0024
HOMIC	0.0512	0.0366	1.40	0.1626
ETHNIC_SN	0.0985	0.0258	3.82	0.0001
FOOD	-0.0178	0.0441	-0.40	0.6871
POP	0.3101	0.0393	7.88	0.0000

WATER	-0.0751	0.0421	-1.78	0.0749
ECON_ISO	-0.0708	0.0540	-1.31	0.1901
FUEL_EXP	-0.0754	0.0216	-3.49	0.0005
STRUCT	-0.1127	0.0573	-1.97	0.0494
UNEMP	0.2180	0.0361	6.03	0.0000
YOUTHBBOTH	-0.1603	0.0638	-2.51	0.0122
CORRUPT	0.0765	0.1007	0.76	0.4479
REG_U:INEQ_SWIID	-0.1754	0.0505	-3.48	0.0005
REG_U:GDP_CAP	-0.1576	0.0396	-3.98	0.0001
INEQ_SWIID:GDP_CAP	-0.1103	0.0509	-2.17	0.0304
REG_U:INEQ_SWIID:GDP_CAP	0.0323	0.0081	3.97	0.0001

Table 14 –Intensity of VC\_SN linear model

### Probability of HVC\_NP logistic model

	Estimate	Std. Error	z value	Pr(> z )
(Intercept)	-4.8815	2.8445	-1.72	0.0861
REG_U	-1.1670	0.5321	-2.19	0.0283
INEQ_SWIID	-1.6856	0.5443	-3.10	0.0020
GDP_CAP	-1.3024	0.4818	-2.70	0.0069
REG_P2	0.0246	0.0481	0.51	0.6090
GOV_EFF	0.3109	0.1579	1.97	0.0490
EMPOWER	-0.1053	0.0557	-1.89	0.0589
REPRESS	0.1526	0.0526	2.90	0.0037

CON_NB	0.0694	0.0264	2.63	0.0087
YRS_HVC	0.1717	0.0261	6.58	0.0000
CON_INT	0.2291	0.0319	7.19	0.0000
MORT	0.2148	0.1111	1.93	0.0533
DISPER	-0.0758	0.0261	-2.90	0.0037
HOMIC	0.1047	0.0519	2.02	0.0436
ETHNIC_NP	-0.0374	0.0413	-0.91	0.3645
FOOD	-0.0898	0.0652	-1.38	0.1683
POP	0.1102	0.0621	1.77	0.0761
WATER	0.0530	0.0614	0.86	0.3880
ECON_ISO	0.1108	0.0748	1.48	0.1387
FUEL_EXP	0.0677	0.0312	2.17	0.0297
STRUCT	0.4485	0.0833	5.39	0.0000
UNEMP	-0.0985	0.0531	-1.85	0.0636
YOUTHBOTH	0.4688	0.0955	4.91	0.0000
CORRUPT	0.0340	0.1424	0.24	0.8111
REG_U:INEQ_SWIID	0.2192	0.0936	2.34	0.0192
REG_U:GDP_CAP	0.1348	0.0796	1.69	0.0902
INEQ_SWIID:GDP_CAP	0.1818	0.0862	2.11	0.0350
REG_U:INEQ_SWIID:GDP_CAP	-0.0263	0.0144	-1.83	0.0677

Table 15 – Probability of HVC\_NP logistic model

### Intensity of HVC\_NP linear model

	<b>Estimate</b>	<b>Std. Error</b>	<b>t value</b>	<b>Pr(&gt; t )</b>
(Intercept)	9.5742	1.6529	5.79	0.0000
REG_U	-1.1083	0.3092	-3.58	0.0004
INEQ_SWIID	-0.3588	0.3001	-1.20	0.2327
GDP_CAP	-0.3992	0.2596	-1.54	0.1251
REG_P2	0.0540	0.0279	1.93	0.0540
GOV_EFF	-0.2060	0.0955	-2.16	0.0319
EMPOWER	-0.0944	0.0291	-3.25	0.0013
REPRESS	0.0273	0.0316	0.87	0.3874
CON_NB	0.0333	0.0148	2.24	0.0257
YRS_HVC	-0.0032	0.0143	-0.23	0.8217
CON_INT	0.0312	0.0179	1.74	0.0823
MORT	-0.1444	0.0737	-1.96	0.0512
DISPER	-0.0367	0.0160	-2.30	0.0223
HOMIC	-0.1014	0.0396	-2.56	0.0110
ETHNIC_NP	-0.0566	0.0192	-2.95	0.0034
FOOD	0.1851	0.0449	4.12	0.0000
POP	0.0600	0.0420	1.43	0.1547
WATER	-0.0941	0.0415	-2.27	0.0241
ECON_ISO	-0.0514	0.0430	-1.20	0.2327
FUEL_EXP	0.0061	0.0172	0.35	0.7239
STRUCT	0.1225	0.0514	2.38	0.0179



UNEMP	-0.0079	0.0329	-0.24	0.8097
YOUTHBBOTH	0.3122	0.0695	4.49	0.0000
CORRUPT	0.2759	0.1055	2.62	0.0094
REG_U:INEQ_SWIID	0.2040	0.0524	3.89	0.0001
REG_U:GDP_CAP	0.1585	0.0441	3.60	0.0004
INEQ_SWIID:GDP_CAP	0.0361	0.0452	0.80	0.4250
REG_U:INEQ_SWIID:GDP_CAP	-0.0293	0.0077	-3.81	0.0002

Table 16 – Intensity of HVC\_NP linear model

### Probability of HVC\_SN logistic model

	Estimate	Std. Error	z value	Pr(> z )
(Intercept)	-8.5473	1.4543	-5.88	0.0000
REG_U	1.0750	0.2613	4.11	0.0000
INEQ_SWIID	0.1146	0.2829	0.41	0.6853
GDP_CAP	-0.0076	0.2598	-0.03	0.9765
REG_P2	-0.0814	0.0327	-2.49	0.0128
GOV_EFF	-0.0523	0.0973	-0.54	0.5910
EMPOWER	-0.0846	0.0369	-2.29	0.0221
REPRESS	0.1784	0.0345	5.18	0.0000
CON_NB	-0.0091	0.0159	-0.58	0.5645
YRS_HVC	-0.0356	0.0244	-1.45	0.1457
CON_INT	0.2855	0.0232	12.33	0.0000
MORT	0.3964	0.0777	5.10	0.0000

DISPER	0.0722	0.0168	4.30	0.0000
HOMIC	0.0340	0.0312	1.09	0.2755
ETHNIC_SN	0.2446	0.0258	9.48	0.0000
FOOD	0.0027	0.0422	0.06	0.9497
POP	0.2896	0.0353	8.20	0.0000
WATER	0.0187	0.0371	0.50	0.6151
ECON_ISO	-0.0399	0.0505	-0.79	0.4288
FUEL_EXP	0.0099	0.0201	0.50	0.6204
STRUCT	0.0256	0.0498	0.51	0.6070
UNEMP	-0.1009	0.0284	-3.55	0.0004
YOUTHBBOTH	0.0917	0.0533	1.72	0.0852
CORRUPT	0.1649	0.0854	1.93	0.0535
REG_U:INEQ_SWIID	-0.1650	0.0527	-3.13	0.0017
REG_U:GDP_CAP	-0.1488	0.0451	-3.30	0.0010
INEQ_SWIID:GDP_CAP	-0.0044	0.0488	-0.09	0.9276
REG_U:INEQ_SWIID:GDP_CAP	0.0204	0.0090	2.26	0.0240

Table 17 – Probability of HVC\_SN logistic model

### Intensity of HVC\_SN linear model

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	0.2752	1.5629	0.18	0.8603
REG_U	0.8728	0.2510	3.48	0.0005
INEQ_SWIID	0.4468	0.3077	1.45	0.1469

GDP_CAP	0.7776	0.2668	2.91	0.0036
REG_P2	0.0214	0.0338	0.63	0.5277
GOV_EFF	0.2382	0.1071	2.22	0.0264
EMPOWER	0.0595	0.0371	1.61	0.1084
REPRESS	0.0407	0.0382	1.06	0.2879
CON_NB	-0.0251	0.0175	-1.44	0.1513
YRS_HVC	0.0016	0.0190	0.08	0.9332
CON_INT	0.1519	0.0208	7.29	0.0000
MORT	-0.0362	0.0793	-0.46	0.6483
DISPER	-0.0572	0.0188	-3.04	0.0024
HOMIC	0.0512	0.0366	1.40	0.1626
ETHNIC_SN	0.0985	0.0258	3.82	0.0001
FOOD	-0.0178	0.0441	-0.40	0.6871
POP	0.3101	0.0393	7.88	0.0000
WATER	-0.0751	0.0421	-1.78	0.0749
ECON_ISO	-0.0708	0.0540	-1.31	0.1901
FUEL_EXP	-0.0754	0.0216	-3.49	0.0005
STRUCT	-0.1127	0.0573	-1.97	0.0494
UNEMP	0.2180	0.0361	6.03	0.0000
YOUTHBBOTH	-0.1603	0.0638	-2.51	0.0122
CORRUPT	0.0765	0.1007	0.76	0.4479
REG_U:INEQ_SWIID	-0.1754	0.0505	-3.48	0.0005

REG_U:GDP_CAP	-0.1576	0.0396	-3.98	0.0001
INEQ_SWIID:GDP_CAP	-0.1103	0.0509	-2.17	0.0304
REG_U:INEQ_SWIID:GDP_CAP	0.0323	0.0081	3.97	0.0001

Table 18 – Intensity of HVC\_SN linear model

## 5. Statistical Metrics

In predictive analytics, a table of confusion (also called a confusion matrix) is a table with two rows and two columns that reports the number of false positives, false negatives, true positives and true negatives. This allows more detailed analysis than mere proportion of correct classifications (accuracy). Accuracy is not a reliable metric for the real performance of a classifier, because it will yield misleading results if the data set is unbalanced (that is, when the numbers of observations in different classes vary greatly).

Assuming the confusion matrix mentioned above, its corresponding table of confusion would be for the conflict class:

		Actual Y4 Conflict situation	
		Conflict	Non-Conflict
Predicted Y4 Conflict situation	Conflict	True Positives (TP)	False Positive (FP)
	Non-Conflict	False Negatives (FN)	True Negatives (TN)

However, since we have 2 models (HVC/VC) in 2 dimensions (NP/SN), we obtain in total 4 confusion matrix, as shown in the tables below.

		Actual Y4 HVC NP Conflict situation	
		Conflict	Non-Conflict
Predicted Y4 HVC	Conflict	True Positives (TP)	False Positive (FP)

NP Conflict situation	Non-Conflict	False Negatives (FN)	True Negatives (TN)
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		Actual Y4 HVC SN Conflict situation	
		Conflict	Non-Conflict
Predicted Y4 HVC SN Conflict situation	Conflict	True Positives (TP)	False Positive (FP)
	Non-Conflict	False Negatives (FN)	True Negatives (TN)

		Actual Y4 VC NP Conflict situation	
		Conflict	Non-Conflict
Predicted Y4 VC NP Conflict situation	Conflict	True Positives (TP)	False Positive (FP)
	Non-Conflict	False Negatives (FN)	True Negatives (TN)

		Actual Y4 VC SN Conflict situation	
		Conflict	Non-Conflict
Predicted Y4 VC SN Conflict situation	Conflict	True Positives (TP)	False Positive (FP)
	Non-Conflict	False Negatives (FN)	True Negatives (TN)

In all the four confusion matrix, the meanings of TP, FP, FN, TN are the following:

- **TP** equivalent with hit. While considering the characteristics of each model, this means that the presence of conflict (Y4) was correctly predicted.
- **TN** equivalent with correct rejection. While considering the characteristics of each model, this means that the non-conflict (Y4) was correctly predicted.

- **FP** equivalent with false alarm. While considering the characteristics of each model, this means that the conflict (Y4) was not correctly predicted; the conflict did not occur.
- **FN** equivalent with miss. While considering the characteristics of each model, this means that the conflict (Y4) was not correctly predicted; the conflict occurred, although it was not predicted.

There are in addition the totals of Actual/real (Y4) situations/cases:

- **P** condition positive. The number of real positive cases in the data.
- **N** condition negatives. The number of real negative cases in the data.

### **Terminology and derivations from a confusion matrix**

Sensitivity, recall, hit rate or true positive rate (TPR) measures the proportion of positives that are correctly identified:

$$TPR = \frac{TP}{P} = \frac{TP}{TP + FN}$$

Specificity or true negative rate (TNR) measures the proportion of negatives that are correctly identified:

$$TNR = \frac{TN}{N} = \frac{TN}{TN + FP}$$

Precision or positive predictive value (PPV) is the fraction of relevant positives instances among the retrieved instances:

$$PPV = \frac{TP}{TP + FP}$$

Negative predictive value (NPV) is the fraction of relevant negatives instances among the retrieved instances:

$$NPV = \frac{TN}{TN + FN}$$

Fall-out or false positive rate (FPR) is calculated as the ratio between the number of negative events wrongly categorized as positive (false positives) and the total number of actual negative events (regardless of classification):

$$FPR = \frac{FP}{N} = \frac{FP}{FP + TN} = 1 - TNR$$

Complementarily, the Miss rate or false negative rate (FNR) is the proportion of positives which yield negative test outcomes with the test, i.e. the conditional probability of a negative test result given that the condition being looked for is present.

$$FNR = \frac{FN}{P} = \frac{FN}{FP + TP} = 1 - TPR$$

Accuracy (ACC) has two definitions:

1. More commonly, it is a description of systematic errors, a measure of statistical bias; as these cause a difference between a result and a "true" value, International Organization for Standardization (ISO) calls this trueness.
2. Alternatively, ISO defines accuracy as describing a combination of both types of observational error above (random and systematic), so high accuracy requires both high precision and high trueness.

In simplest terms, given a set of data points from a series of measurements, the set can be said to be precise if the values are close to the average value of the quantity being measured, while the set can be said to be accurate if the values are close to the true value of the quantity being measured. The two concepts are independent of each other, so a particular set of data can be said to be either accurate, or precise, or both, or neither.

Following a more commonly used definition in the fields of science and engineering, the accuracy of a measurement system is the degree of closeness of measurements of a quantity to that quantity's true value.

$$ACC = \frac{TP + TN}{P + N} = \frac{TP + TN}{TP + TN + FP + FN}$$

### **Mean squared error**

The MSE is a measure of the quality of an estimator—it is always non-negative, and values closer to zero are better.

In statistics, the mean squared error (MSE) or mean squared deviation (MSD) of an estimator (of a procedure for estimating an unobserved quantity) measures the average of the squares of the errors or deviations—that is, the difference between the estimator and what is estimated. MSE is a risk function, corresponding to the expected value of the squared error loss or quadratic loss. The difference occurs because of randomness or

because the estimator doesn't account for information that could produce a more accurate estimate.

The MSE is the second moment (about the origin) of the error, and thus incorporates both the variance of the estimator and its bias. For an unbiased estimator, the MSE is the variance of the estimator. Like the variance, MSE has the same units of measurement as the square of the quantity being estimated. In an analogy to standard deviation, taking the square root of MSE yields the root-mean-square error or root-mean-square deviation (RMSE or RMSD), which has the same units as the quantity being estimated; for an unbiased estimator, the RMSE is the square root of the variance, known as the standard deviation.

### Root mean squared error

The root-mean-square deviation (RMSD) or root-mean-square error (RMSE) is a frequently used measure of the differences between values (sample and population values) predicted by a model or an estimator and the values actually observed. The RMSD represents the sample standard deviation of the differences between predicted values and observed values. These individual differences are called residuals when the calculations are performed over the data sample that was used for estimation, and are called prediction errors when computed out-of-sample. The RMSD serves to aggregate the magnitudes of the errors in predictions for various times into a single measure of predictive power. RMSD is a measure of accuracy, to compare forecasting errors of different models for a particular data and not between datasets, as it is scale-dependent.

Although RMSE is one of the most commonly reported measures of disagreement, some scientists misinterpret RMSD as average error, which RMSD is not. RMSD is the square root of the average of squared errors, thus RMSD confounds information concerning average error with information concerning variation in the errors. The effect of each error on RMSD is proportional to the size of the squared error thus larger errors have a disproportionately large effect on RMSD. Consequently, RMSD is sensitive to outliers.

	METRICS_VC_NP	METRICS_VC_SN	METRICS_HVC_NP	METRICS_HVC_SN
MSE	25.09	22.78	60.66	65.37
RMSE	5.01	4.77	7.79	8.08
Sensitivity or TPR	0.96	0.93	1	1
Specificity or TNR	0.49	0.40	0.39	0
Precision or PPV	0.26	0.33	0.12	0.09
NPV	0.98	0.94	1	-



fall-out or FPR	0.50	0.59	0.60	1
FNR	0.04	0.07	0	0
accuracy	0.57	0.53	0.44	0.091

## 6. Conclusion

In the present report, we have discussed on the one hand the input data for the regression model, how the predictions are obtained, as well as the output data. Based on the twenty-four variables, all relatively stable and freely accessible by any user the regression model operates through 3 phases so as to obtain the probability and intensity of conflict at the country level. On the other hand, the statistical significance test, as well as the confusion matrix, provides an in-depth analysis of the regression model. Further development should, in fact, focus on conducting an advanced evaluation of the coefficients and assessment of the model (using the step-wise method) in order to select the best possible combination of variables. Furthermore, future development would imply reviewing the dataset for fitting, because of updated datasets, as well as exploring possibilities for automatic and intelligent technics for updating the datasets for fitting.

The present report is part of a documentation work aiming at improving the GCRI models with greater transparency, but in no case at validating it. With this specific report on the regression model, we contribute to document a high-potential conflict risk modelling method. The strength of the GCRI methodological approach lies in the diversity of sources used as input data, as well as the large number of variables included into the index. Thanks to this, we are more likely to get a comprehensive evaluation of conflict risk.

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