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31 tropospheric and other group delays using a hardware signal simulator. When  
32 applying the proposed technique for Global Positioning System (GPS) legacy  
33 signals, mean offsets in the order of 3 ns for satellites and receivers were found  
34 to exist between the estimated DCBs and the IGS published DCBs. It was shown  
35 that these estimated DCBs are fairly stable in time, especially for the legacy  
36 signals. When the proposed technique is applied for the DCBs estimation using  
37 the newer Galileo signals, an agreement at the level of 1 to 2 ns was found  
38 between the estimated DCBs and the manufacturer's measured DCBs, as  
39 published by the European Space Agency, for the three still operational Galileo  
40 In Orbit Validation (IOV) satellites.

41

42 **Keywords: Differential Code Biases, Total Electron Content, hardware**  
43 **delays, STEC, simulator**

44

45 **Introduction:**

46 In the last few decades, specialized GNSS (Global Navigation Satellite System)  
47 Ionospheric Scintillation Monitor Receivers (ISMRS) such as the NovAtel/AJ  
48 Systems GSV4004 and the Septentrio PolaRxS Pro, have been developed with a  
49 view to support continuous ionospheric modeling by estimating Total Electron  
50 Content (TEC) and different scintillation parameters. However, it is not a straight  
51 forward task to derive accurate TEC information from these specialized  
52 receivers because the recorded code based pseudorange measurements are  
53 contaminated by instrumental biases, the so-called Differential Code Biases  
54 (DCBs), existing between the code observations from different frequencies, at  
55 both the satellite and receiver ends. Considering these existing hardware delays  
56 to be stable for reasonable periods of time, the recorded TEC measurements have  
57 been used quite successfully on a relative basis in a number of experiments. Yet,  
58 to enable the calculation of absolute TEC for ionospheric monitoring, these  
59 receivers must be calibrated to account for their respective DCBs. Ignoring the  
60 satellite and receiver DCBs when computing TEC may result in an error of up  
61 to 20 TECU (or 7 ns) for satellites and 40 TECU (or 14 ns) for receivers, and

62 their cumulative effect can reach as much as 100 TECU (or 35 ns) in extreme  
63 cases (Sardón et al., 1994). If not accounted for, these can also sometimes lead  
64 to non-physical negative TEC values (Ma and Maruyama, 2003; Mylnikova,  
65 2015). This could become even worse for the more recent new GNSS signals  
66 and hence cannot be ignored (Montenbruck et al., 2014; Wang et al., 2015).

67 With the advent of modernized GPS, GLONASS and the new Galileo  
68 and Beidou signals in addition to the legacy GPS and GLONASS signals, a  
69 variety of signal pairs is available to compute TEC. However, the associated  
70 DCBs and different available tracking modes such as pilot only and combined,  
71 make the accurate TEC computation even more challenging.

72 Van Dierendonck (1999) and Van Dierendonck and Hua (2001) defined  
73 a calibration procedure for GSV4004 monitors, by comparing their estimated  
74 TEC data with a ‘reference’ TEC, such as that generated by the International  
75 GNSS Service (IGS) or a Space Based Augmentation System (SBAS), an  
76 approach attempted in Dodson et al. (2001). Additionally, different algorithms  
77 for computing these DCBs have also been proposed in the past. For single station  
78 receiver DCB estimate, these can be roughly categorized in two groups (Arikan  
79 et al., 2008; Komjathy et al., 2005; Li et al., 2014, Li et al., 2017). The first group  
80 models Vertical TEC (VTEC) as a polynomial that is a function of ionospheric  
81 pierce point coordinates in a coordinate system referenced to the earth-sun axis.  
82 Both the satellite and receiver DCBs are considered as unknowns along with  
83 other coefficients, and are solved for in a least squares (LSQ) solution (Lanyi  
84 and Roth, 1988; Sardón et al., 1994; Jakowski et al., 1996; Lin, 2001; Otsuka et  
85 al., 2002, Rao, 2007; Yuan et al., 2007; Mayer et al., 2011; Durmaz and  
86 Karslioglu, 2015). The second group uses the method of minimization of the  
87 standard deviation of VTEC using different receiver trial biases and the one that  
88 minimizes the standard deviation of computed VTEC is chosen as the receiver  
89 bias for that particular station (Ma and Maruyama, 2003; Zhang et al., 2003;  
90 Komjathy et al., 2005; Arikan et al., 2008, Montenbruck et al., 2014).

91 The published DCB products are routinely estimated by different  
92 Analysis Centers (ACs) of the IGS as a by-product of their local or global  
93 ionospheric analyses for almost all the available satellites in different

94 constellations and a selected number of IGS or MGEX (Multi GNSS  
95 Experiment) stations. A linear geometric combination of code based  
96 pseudoranges is employed by the ACs to derive the DCBs on a daily basis along  
97 with a set of ionospheric coefficients. However, this is a rank deficient system  
98 and an external constraint must be employed to break the rank deficiency and  
99 separate the satellite DCBs from the receiver DCBs. This is normally achieved  
100 by constraining the mean of the satellites DCBs to zero, in a so-called ‘zero mean  
101 constraint’. Consequently, with the routine changes carried out in the satellite  
102 constellations, frequent jumps can be observed in the estimated DCBs (Zhong et  
103 al., 2015). On the other hand, the problem of rank deficiency can also be resolved  
104 by constraining the solution to a known receiver DCB in the network instead.  
105 The advantage of using this approach is that a more realistic and stable set of  
106 satellite and receiver DCBs are estimated.

107           For global TEC monitoring and other related applications, it would be  
108 straight forward to carry out the analysis provided the receiver with the known  
109 DCB is part of the IGS/MGEX network. However, as in a general situation this  
110 receiver will not be part of the network, its DCB must be obtained from the  
111 manufacturer or otherwise carefully estimated through a technique that can  
112 ensure that it is consistent with the available set of satellite DCBs. We hereby  
113 introduce a technique for satellite and receiver DCB estimation by first  
114 estimating the DCB of an available receiver through simulation and afterwards  
115 ‘inserting’ this receiver in a global network for processing. For carrying out this  
116 technique, a Septentrio PolaRxS Pro ISMR, referred to hereafter as ‘SEPT’, was  
117 used in conjunction with the Spirent GSS8000 hardware simulator, in a  
118 simulation where the state of the ionosphere, troposphere and the other group  
119 delays could be controlled, as demonstrated in Ammar (2011). Once the receiver  
120 DCB has been estimated, it is then used to constrain the solution in a global  
121 network of stations following the strategy implemented by the Centre of Orbit  
122 Determination in Europe (CODE), to ultimately estimate the DCBs of the  
123 satellites and all the other receivers involved in the network (Schaer, 1999). The  
124 final results should produce a consistent set of stable DCBs, which are now  
125 closer to their physical values and therefore more representative to be employed  
126 in any TEC monitoring application. For validation purposes, another Septentrio

127 PolaRxS Pro ISMR and a Javad Triumph – I receiver are also involved. These  
 128 are referred to hereafter as ‘SEP2’ and ‘JAVD’, respectively. Moreover, the idea  
 129 of working with an ISMR as a primary receiver was originally conceived  
 130 because of the specific feature of this receiver to estimate TEC for ionospheric  
 131 monitoring purposes, where the estimation of DCBs is desirable so that absolute  
 132 and calibrated TEC can be obtained. Nevertheless, the proposed technique can  
 133 be applied to any conventional multi-frequency, multi-constellation receiver, as  
 134 long as its capabilities can be reflected in the GNSS simulator.

135 It is important to remember that the calibrated DCBs obtained via  
 136 simulators can vary between simulators based on their ability to generate high  
 137 quality signals and on their intrinsic hardware delays. Further complications can  
 138 arise from the fact that there may exist differences between live and simulated  
 139 signals depending on correlator spacing and multipath mitigation techniques  
 140 (Hauschild and Montenbruck, 2016). This would not be a problem in TEC  
 141 monitoring due to relative time independence of the satellites and receivers  
 142 DCBs but for other precise operations such as time transfer, this must be given  
 143 due consideration.

144

145 **DCB in the context of TEC Estimation:**

146 For a specific GNSS constellation, the difference of two code based pseudorange  
 147 measurements obtained from two signals, in linear units, equals the sum of the  
 148 differential ionospheric path delays and the respective satellite and receiver  
 149 DCBs. If both signals share the same frequency, as in the case of C<sub>1</sub> and P<sub>1</sub>, the  
 150 combined satellite and receiver DCB equals the average difference of the  
 151 respective code measurements (Montenbruck et al., 2013). This can be written  
 152 as follows:

$$153 \quad P_{i,r}^s - P_{j,r}^s = (I_i - I_j) + DCB_{P_i-P_j}^s + DCB_{r, P_i-P_j} \quad (1)$$

154 Here, the superscript ‘s’ and the subscript ‘r’ are used to refer to satellite and  
 155 receiver, respectively. The subscripts ‘i’ and ‘j’ can be 1, 2 or 5 depending upon  
 156 the carrier frequency in use. Also, P<sub>i,r</sub><sup>s</sup> and P<sub>j,r</sub><sup>s</sup> are the code pseudorange  
 157 observables on carrier frequencies L<sub>i</sub> and L<sub>j</sub> with corresponding ionospheric

158 delays as  $I_i$  and  $I_j$ , respectively. The frequency dependent ionospheric delay (in  
 159 meter) can be further written in the generalized form as follows:

$$160 \quad I = \frac{40.3}{f_L^2} \times \text{STEC} \quad (2)$$

161  $f_L$  refers to the frequency (in Hz) of the signal L and STEC is the Slant TEC (in  
 162 meter) between the satellite transmitter and the receiver antenna.

163 Working with GPS, the correction parameter for the satellite DCB  
 164 between P1 and P2 pseudoranges on GPS L1 and L2 signals (or  $\text{DCB}_{P1-P2}^S$ ) is  
 165 referred to as the estimated group delay differential or  $T_{GD}$  and this is provided  
 166 to the users through the broadcast message. The relation between satellite  
 167  $\text{DCB}_{P1-P2}^S$  and  $T_{GD}$  is given as follows:

$$168 \quad T_{GD} = \frac{1}{1-\gamma} \text{DCB}_{P1-P2}^S \quad (3)$$

169 where for GPS L1 and L2 frequencies,

$$170 \quad 1 - \gamma = 1 - \frac{f_{L1}^2}{f_{L2}^2} = 1 - \frac{(1575.42 \times 10^6)^2}{(1227.60 \times 10^6)^2} = -0.647 \quad (4)$$

171 Using (2) to (4) and the definition of 1 TEC Unit (TECU) which is equal to  $10^{16}$   
 172 electrons/ $m^2$ , the standard equation that can be used in any dual frequency  
 173 receiver generating P1 and P2 to compute STEC in TECU can be written as  
 174 follows:

$$175 \quad \text{STEC} = 9.5238 \times [(P_2 - P_1) - 0.647T_{GD} + \text{DCB}_{r, P1-P2}] \quad (5)$$

176 Similarly, working with Galileo E1 and E5a code observables, the STEC  
 177 equation can take the following form:

$$178 \quad \text{STEC} = 7.764 \times [(E_{5a} - E_1) - 0.7933B_{GD} + \text{DCB}_{r, E1-E5a}] \quad (6)$$

179 where  $\text{DCB}_{r, E1-E5a}$  is the differential code bias between Galileo E1 and E5a  
 180 signals and  $B_{GD}$  i.e. the broadcast group delay is the correction parameter for  
 181  $\text{DCB}_{E1-E5a}^S$  as transmitted in the navigation message by the Galileo satellites.

182 For either (5) or (6), if the terms STEC,  $T_{GD}$  and  $B_{GD}$  are controlled in  
 183 simulation by setting them to 0, then the DCB of the receiver can directly be

184 estimated from the observations. Here we assume that the simulator DCB is  
185 negligible and can be ignored.

186

### 187 **M\_DCB Software:**

188 Jin et al. (2012) developed an open source M\_DCB software package in  
189 MATLAB to estimate the global or regional receivers and GPS satellites DCBs.  
190 This is based on the CODE's global ionospheric analysis strategy in which the  
191 VTEC is expressed as a spherical harmonic expansion of a degree and order 15.  
192 Differences of less than 0.7 ns and an RMS of less than 0.4 ns were found to  
193 exist between the M\_DCB software and IGS ACs products (e.g., JPL, CODE  
194 and IGS Combined). We modify this software to not only handle the external  
195 constraint of known receiver DCB but also to handle the newer GPS L5 and  
196 Galileo E1 and E5a signals, which were not covered in the original package.  
197 Hereafter, the revised version of the M\_DCB software with the external  
198 constraint of zero mean condition on the satellites DCBs is referred to as the  
199 'DCB\_ZM', whereas with the external constraint of known receiver DCB, it is  
200 referred to as the 'DCB\_FIX'.

201

### 202 **Receiver DCB Estimation using Simulation (Methodology):**

203 The approach that was followed to estimate the receiver DCB was to use the  
204 Spirent GSS8000 hardware signal simulator to generate all possible GNSS  
205 signals without ionospheric and tropospheric delays, as well as eliminating  
206 simulated satellite signal delays such as  $T_{GD}$  and  $B_{GD}$  by setting them to 0. The  
207 Septentrio PolaRxS (SEPT) receiver was set to track these simulated signals  
208 under default tracking loop parameters with no multipath mitigation as presented  
209 in Table 1. From the recorded RINEX observations, the STEC was computed  
210 based on (5) for GPS and (6) for Galileo depending upon the signal combination,  
211 using all the available satellites. The mean of the computed STEC for all the  
212 satellites essentially gave the DCB of the receiver for a particular signal  
213 combination. The same methodology was followed for the DCB estimation of



214 SEP2 and JAVD receivers and the different tracking parameters applied to these  
 215 receivers are also presented in Table 1.

216

217 **Table 1** Different tracking parameters applied during simulations and real data  
 218 collection for the different receiver systems

Receiver System	Delay Locked Loop (DLL) Tracking Loop		Smoothing Interval (seconds)	Multipath Mitigation
	Bandwidth (Hz)	Order		
SEPT	0.25	2	Not Applied	Off
SEP2	0.25	2	Not Applied	Off
JAVD	3	1	100 (default)	Off

219

220 Cable DCB:

221 The antenna cable is commonly considered a non-dispersive medium (Defraigne  
 222 et al., 2014). However, Dyrud et al. (2008) showed that a small constant variation  
 223 of 0.004 meters or approximately 13 ps (picoseconds) can exist in the absolute  
 224 DCB of the receiver system while working with different cable lengths. Working  
 225 on a similar strategy with different lengths of the RG213 coaxial cables ranging  
 226 from 1 meter to 30 meters, Ammar (2011) also showed variations of up to 35 ps  
 227 in the estimated DCB between P1 and P2 pseudoranges using simulated data.  
 228 These small variations in the absolute DCB of the receiver system with varying  
 229 cable lengths can be explained on the basis of the additional noise that the longer  
 230 cables introduce in the pseudorange measurements in comparison to the shorter  
 231 ones. To rule out any minor effect coming from the cable, the same antenna cable  
 232 of 20 meters length was used with the SEPT receiver both to connect it with the  
 233 simulator and to connect it with the antenna for open sky data collection. On the  
 234 other hand, the same was not possible for the other two receivers, SEP2 and  
 235 JAVD, because of the difficulty in taking existing routed cables out of the

236 building fixtures. Therefore, to keep the noise level to a minimum, the smallest  
237 available 1-meter cable was used to connect them to the simulator during the  
238 estimation of their respective DCBs.

239

240 **Antenna DCB:**

241 The antenna DCB (also referred to as the differential group delay) should also  
242 be given due importance because in an open sky situation it obviously forms part  
243 of the overall DCB of the data recording system comprising the antenna, the  
244 cable and the receiver itself.

245 For the specific NovAtel GPS 702GG antenna that was used initially  
246 with the SEPT receiver, the DCB of -2.7 ns was provided by the manufacturer  
247 between L1 and L2. It was measured at 23°C and with 4.53V power supply  
248 (NovAtel, 2016).

249 For the Leica AR10 antennas that were used initially with the SEP2 and  
250 JAVD receivers, the DCB value of 3 ns between L1 and L2 was provided (Leica,  
251 2016). This is not antenna specific and is just the maximum DCB value as  
252 estimated by the manufacturer at 22°C for all the Leica AR10 antennas. More  
253 recently, to accommodate the newer GPS L5 and Galileo signals, the antenna  
254 used with the SEPT receiver has been upgraded to the NovAtel GPS 703GGG.  
255 For this particular antenna, the DCBs between L1 and L2 and between L1 and  
256 L5, as computed by the manufacturer at 25°C and with 4.5V power supply, are  
257 2.2 ns and 1.3 ns, respectively (NovAtel, 2016). SEP2 antenna has also been  
258 upgraded to Septentrio choke ring antenna but no differential group delay value  
259 has been provided by the manufacturer.

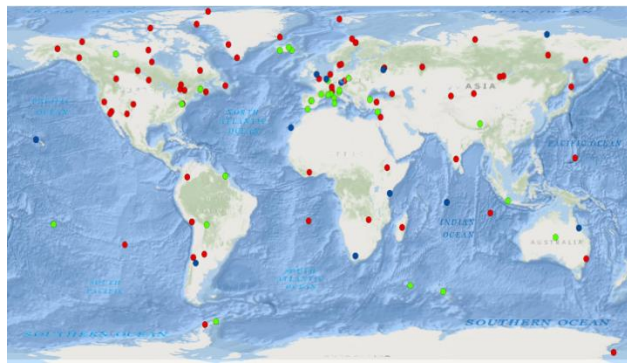
260

261 **Satellites and Receivers DCBs Estimation from Real Data (Methodology):**

262 Initially 'Network A' of 96 stations, comprising of 93 IGS stations and 3  
263 additional stations, namely SEPT, SEP2 and JAVD that were set up at the NGI  
264 (Nottingham Geospatial Institute), was chosen to be part of the global  
265 ionospheric analysis using the DCB\_FIX software. These stations are  
266 represented by red dots in Figure 1. For consistency and compatibility with the

267 original M\_DCB software, these stations were specifically selected to consist of  
268 GPS P1, P2 receiver types only. The estimated DCBs from the DCB\_FIX  
269 software are later compared with the IGS published daily DCB estimates given  
270 in IONEX format. The estimated ionospheric coefficients as part of the LSQ  
271 processing are not analyzed in any way for the generation of global ionospheric  
272 maps (GIMs).

273



274

275

276 **Fig. 1** Red – Network A; Green – Network B; Blue – Common stations in both  
277 the networks.

278

279 To incorporate the modernized GPS L5 signal and the newer Galileo E1  
280 and E5a signals, a new network of 41 stations comprising of 39 IGS or MGEX  
281 stations and 2 NGI stations i.e. SEPT and SEP2, was chosen to be part of the  
282 DCB estimation using the DCB\_FIX software. This network is referred to as  
283 ‘Network B’ and the corresponding stations are represented by green dots in  
284 Figure 1. Also, this network selection was dictated by the fact that the SEPT  
285 receiver incorporates a pilot only tracking technique and limited receivers in the  
286 IGS or MGEX network are currently available with the same tracking technique.  
287 While Li et al. (2016) were able to use a network of 100 plus stations tracking  
288 Galileo based on their localized ionospheric modeling, it can still be a problem  
289 for the research groups working with a global ionospheric model to obtain a good  
290 spread of stations worldwide. Finally, the blue dots in Figure 1 are the stations  
291 that are common in both the networks.

292

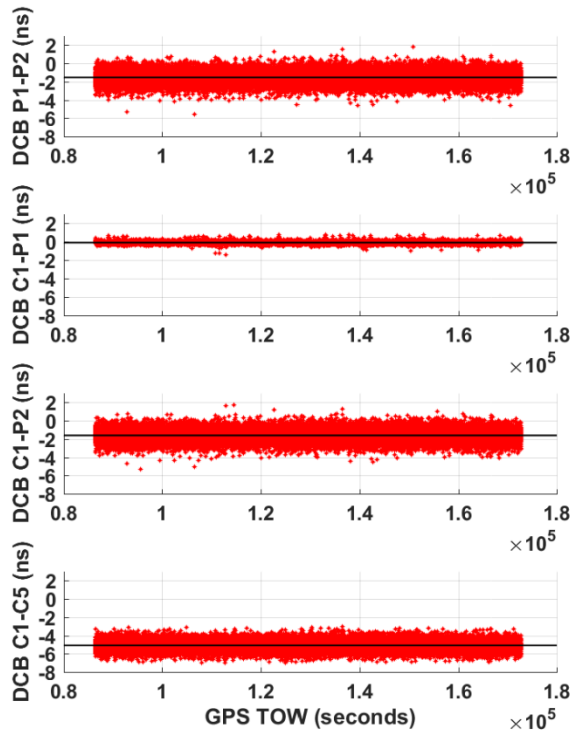
293 **Results for Estimated Receivers DCBs using Simulation:**

294 To estimate the DCB of the SEPT receiver, data from three 26 hours simulations  
295 was captured, where the ionosphere, troposphere and the group delays are set to  
296 0. The simulated signals are recorded by the SEPT receiver using a 20 meters  
297 RG213 coaxial cable. The first two hours of the simulations are discarded to  
298 allow for the simulator and receiver hardware to reach stable operational  
299 temperatures. The DCBs for the desired signal combinations are computed  
300 independently from the code based pseudoranges as recorded in the RINEX files.

301 Figures 2 and 3 show the estimated DCBs for the SEPT receiver between  
302 GPS P1/P2, C1/P1, C1/P2, C1/C5 and Galileo E1/E5a. The mean and one sigma  
303 standard deviation of these DCBs (in ns) across the three simulations were found  
304 to be  $-1.70 \pm 0.53$ ,  $0.03 \pm 0.09$ ,  $-1.67 \pm 0.52$ ,  $-4.97 \pm 0.44$  and  $-5.21 \pm 0.26$ ,  
305 respectively. The consistency between these estimates was confirmed by  
306 verifying the following relation:

307 
$$\text{DCB (C1 - P1)} + \text{DCB (P1 - P2)} = \text{DCB (C1-P2)} \quad (7)$$

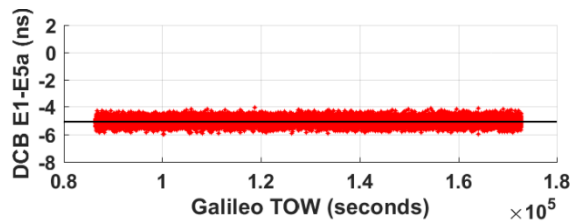
308



309

310 **Fig. 2** Plots showing DCBs between different GPS signal combinations (in ns)  
 311 vs. GPS Time of Week – TOW (in Seconds) as observed by all the satellites in  
 312 one simulation run (SEPT Receiver)

313



314

315

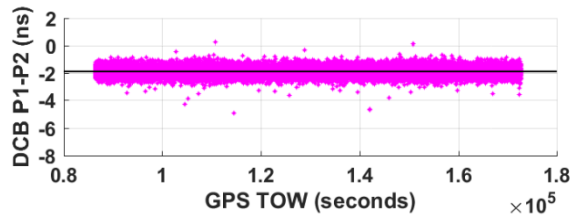
316 **Fig. 3** Plot showing DCB between Galileo E1 and E5a (in ns) vs. Galileo TOW  
 317 (in seconds) as observed by all the satellites in one simulation run (SEPT  
 318 receiver).

319

320 Following the same methodology, Figures 4 and 5 show the DCB  
 321 estimates for SEP2 and JAVD receivers, respectively, for only the GPS P1/P2

322 code combination. The mean and one sigma standard deviation of these DCBs  
323 (in ns) across the three simulations were found to be  $-1.90 \pm 0.31$  and  $6.83 \pm$   
324  $1.35$ , respectively.

325

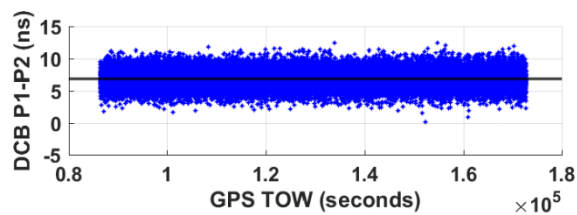


326

327

328 **Fig. 4** Plot showing DCB between GPS P1 and P2 (in ns) vs. GPS TOW (in  
329 Seconds) as observed by all the satellites in one simulation run (SEP2  
330 receiver).

331



332

333

334 **Fig. 5** Plot showing DCB between GPS P1 and P2 (in ns) vs. GPS TOW (in  
335 Seconds) as observed by all the satellites in one simulation run (JAVD  
336 receiver).

337 From Figures 2 to 5, it can be seen that the ISMRs present a lower noise  
338 level than the JAVD receiver even without the application of carrier phase  
339 smoothing. However, keeping in mind that the ISMRs are working under  
340 different tracking parameters (Table 1), a fair comparison would only be possible  
341 by using a consistent set of tracking parameters for all the three receivers.

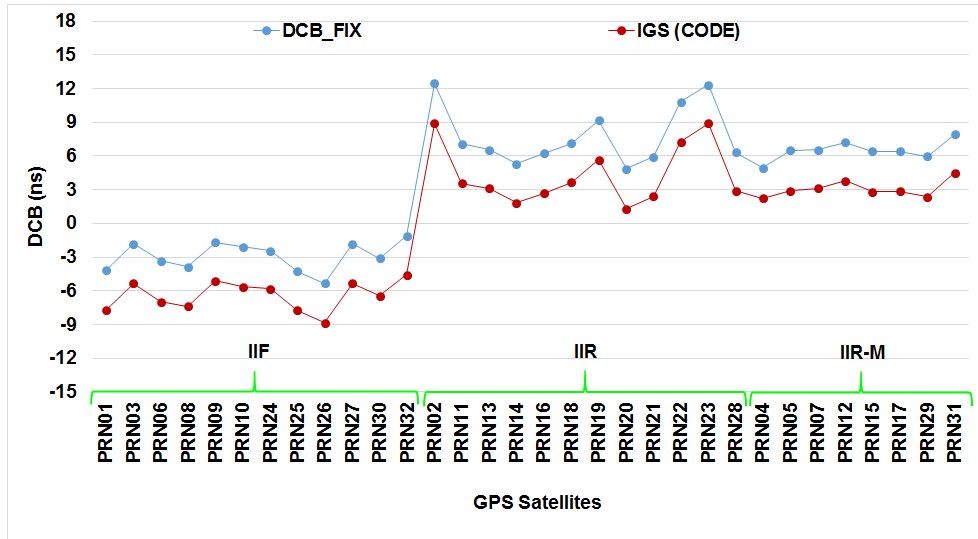
342

343 **Results for Estimated Satellites and Receivers DCBs using Network A**  
344 **(GPS P1/P2 Only):**

345 Using the DCB\_FIX software with the archived RINEX data of 96 stations  
346 (Network A) from Mar 17 to Apr 7, 2016 (22 days) and the spherical harmonics  
347 of degree and order 15, the processing was run on a day to day basis with the  
348 solution constrained to the known DCB value of the SEPT receiver system. A  
349 known DCB value of  $-4.41$  ns was used for the SEPT receiver system which is  
350 the sum of the antenna DCB (see the section on antenna DCB) and the mean  
351 receiver DCB as computed in the previous section. Also, the selection of these  
352 22 days was made on the basis that two additional receivers, i.e. SEP2 and  
353 JAVD, were available during that time to validate the results along with their  
354 antenna DCBs.

355 In Figures 6 and 7, the red curves show the mean DCBs as estimated by  
356 the IGS, whereas, the blue curves show the mean DCBs as estimated by the  
357 DCB\_FIX software. Note that the mean DCB for both the satellites and receivers  
358 is computed over a period of 22 days. Also, in Figure 6, the GPS satellites are  
359 grouped together as per the different family blocks to which they belong. It can  
360 be observed that a similar pattern exists between the IGS computed DCBs and  
361 the DCBs estimated through the DCB\_FIX software. However, stable mean  
362 offsets of  $-3.47$  ns for satellites and  $+3.54$  ns for receivers were found to exist  
363 between the estimated DCBs and the IGS published DCBs. A possible  
364 explanation is that the zero mean satellites DCB constraint, although effective to  
365 break the rank deficiency, imposes an artificial shift on the estimated DCBs. By  
366 using a more realistic constraint in the form of a properly estimated receiver  
367 DCB, the resulting DCBs are closer to their actual values. The more accurate the  
368 known DCB used to constrain the solution, the more accurate the estimated  
369 DCBs for the other receivers and satellites.

370

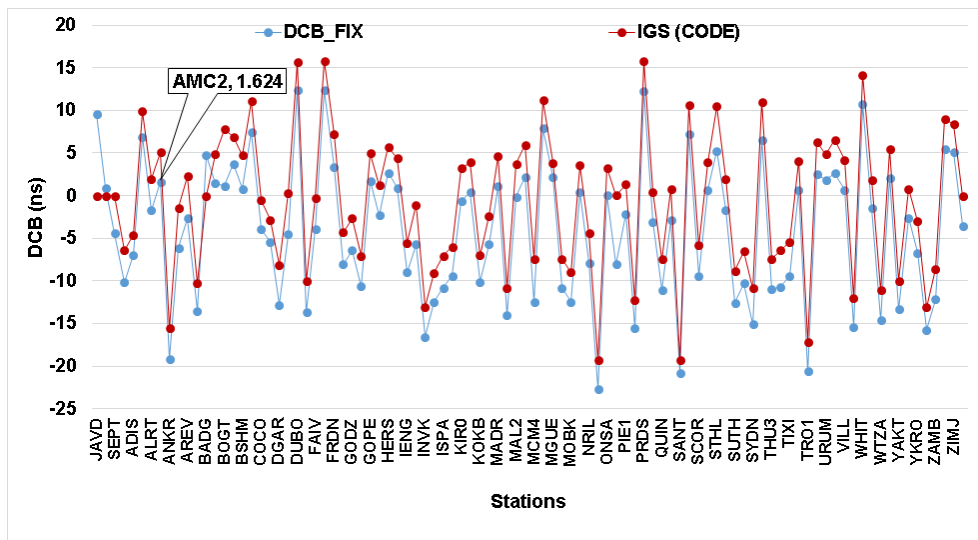


371

372

373 **Fig. 6** Plot showing the average GPS satellite DCBs between P1 and P2  
 374 estimated by the DCB\_FIX software (SEPT = -4.41ns) and IGS (CODE) over  
 375 a period of 22 days (Mar 17 to Apr 7, 2016).

376



377

378

379 **Fig. 7** Plot showing the average receivers' DCBs between P1 and P2 estimated  
 380 by the DCB\_FIX software (SEPT = -4.41 ns) and IGS (CODE) over a period  
 381 of 22 days (Mar 17 to Apr 7, 2016).

382



383 The DCB estimates for SEP2 and JAVD receiver systems from the  
 384 DCB\_FIX software and the DCB\_ZM software are investigated as per in table  
 385 2:

386

387 **Table 2** DCB estimates of SEP2 and JAVD receiver systems from the  
 388 simulator/antenna combination, DCB\_FIX software and DCB\_ZM Software  
 389 (IGS)

Receiver System	DCB P1-P2 Estimates (in ns)		
	Receiver/Cable (Simulator) + Antenna (Manufacturer)	DCB_FIX	DCB_ZM
SEP2	1.10	0.92 ± 0.27	4.40 ± 0.22
JAVD	9.83	9.60 ± 0.53	13.05 ± 0.6

390

391 Since the maximum DCB value of 3 ns for Leica AR10 antenna has been  
 392 used to compute the overall known DCB of the two receiver systems as discussed  
 393 in the earlier section on antenna DCB, it is quite remarkable that the DCB\_FIX  
 394 software has been able to estimate the DCBs for the two receiver systems within  
 395 few tenths of a nanosecond. The accuracy of the DCB estimated by the  
 396 DCB\_FIX is also independent of the fact that the SEP2 receiver is of a relatively  
 397 higher quality in comparison to the geodetic grade JAVD receiver. When  
 398 constrained by the zero mean condition, the DCB\_ZM software produces DCB  
 399 estimates comparable to the IGS DCB solution and it can be seen from table 2  
 400 that the latter are over estimated by about 3.5 ns. On the other hand, the satellite  
 401 DCBs estimated by IGS are under estimated by approximately the same amount  
 402 when compared to those estimated by the DCB\_FIX software (Figure 6).

403 It can also be seen from Figure 6 that the satellite DCBs for the newer  
 404 generation of GPS block IIF satellites are lower than the previous generation of  
 405 satellites. One possible explanation can be that with the advancement in

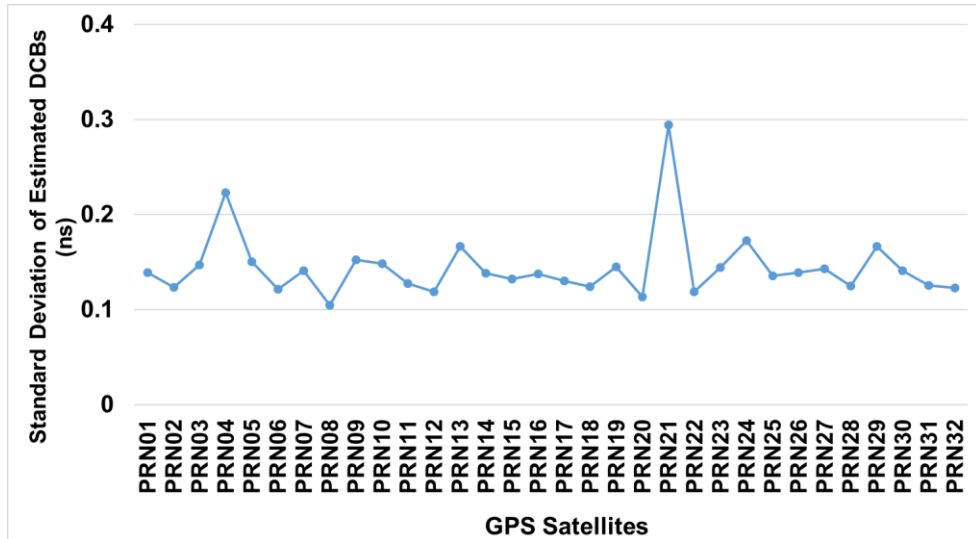
406 technology, the newer satellites are better equipped in terms of quality of  
407 hardware to handle in-orbit temperatures and hence possess lower DCBs. The  
408 temperature sensitivity for signals transmitted by satellites in orbit is discussed  
409 in Coco et al. (1991).

410

411 Stability of Estimated DCBs (GPS P1/P2 Only):

412 To investigate the stability of the estimated DCBs using the DCB\_FIX software,  
413 the standard deviations of both the satellites and the receivers DCBs are plotted  
414 in Figures 8 and 9 respectively. The estimated DCBs are generally stable over  
415 time for both the satellites and the receivers. The average standard deviations of  
416 the estimated satellite and receiver DCBs are found to be 0.15 ns and 0.45 ns,  
417 respectively. Sudden jumps in standard deviations may indicate a possible  
418 replacement of the satellite or receiver or any part of the receiver system, such  
419 as antennas and cables. In some cases, it can also indicate potential hardware  
420 issues within the receiver or receiver architecture. These are however difficult to  
421 investigate because of the independent working of the IGS and MGEX stations.  
422 In Figure 9, a peak can be observed in the standard deviation of 'PALV' receiver  
423 system DCB – this is because the receiver was changed on the 30 March 2016  
424 as published in the station log file ([https://igs.cb.jpl.nasa.gov/igs/cb/station/log/  
425 palv20160329.log](https://igs.cb.jpl.nasa.gov/igs/cb/station/log/palv20160329.log)) and the replacement receiver has a significantly different  
426 DCB. As receivers from the same brand have relatively similar DCBs, it can be  
427 difficult to identify their replacement based on the standard deviations' figures  
428 only.

429

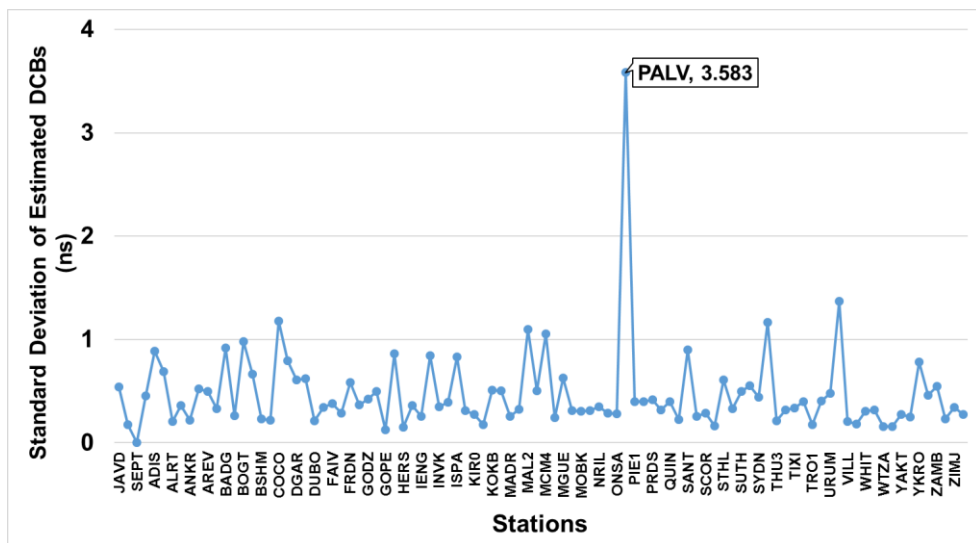


430

431

432 **Fig. 8** Plot showing the standard deviations of the GPS satellites DCBs  
 433 between P1 and P2 estimated by the DCB\_FIX software over a period of 22  
 434 days (Network A – Mar 17 to Apr 7, 2016).

435



436

437

438 **Fig. 9** Plot showing the standard deviations of the receivers DCBs between P1  
 439 and P2 as estimated by the DCB\_FIX software over a period of 22 days  
 440 (Network A – Mar 17 to Apr 7, 2016).

441

442 In all the above data processing with DCB\_FIX or DCB\_ZM software,  
443 the quality of the LSQ solution is analyzed based on the a-posteriori unit variance  
444 or the standard error of observation, which is generally found to be independent  
445 of the external constraints, whether artificial or real. Therefore, the quality of the  
446 LSQ solution can only be improved by using a more refined model in the global  
447 ionospheric analysis.

448

449 **Results for Estimated Satellites and Receivers DCBs using Network B**  
450 **(Galileo E1/E5a Only):**

451 Using the DCB\_FIX software with the archived RINEX data of 41 stations  
452 (Network B) from 4 October 2016 up to 15 November 2016 (43 days) and a  
453 degree and order of 15 for the spherical harmonics, the processing was run on a  
454 day to day basis, constrained by the known DCB value between Galileo E1  
455 (C1C) and E5a (C5Q) signals for the SEPT receiver system. This value was  
456 estimated in simulation using the previously explained strategy as  $-3.91$  ns.

457 From the estimated satellite and receiver DCBs, the results with a  
458 relatively higher average standard deviation of 0.54 ns and 1.24 ns, respectively,  
459 have been observed. Also, the DCB estimates of some of the stations and the  
460 Galileo E24 satellite have been ignored in the computation of these standard  
461 deviations because abnormally high DCBs were estimated on some days of the  
462 processing. One possible explanation for these abnormalities and relatively  
463 higher standard deviations is that the hardware technology that is currently in  
464 place to transmit and process these newer signals is still under test phase and in  
465 the process of refinement. For the sake of conciseness, the figures showing the  
466 estimated satellites and receivers DCBs are not presented. Table 3 compares for  
467 3 Galileo IOV (In Orbit Validation) satellites, the DCBs estimated using the  
468 DCB\_FIX software with the manufacturer measured DCBs that have recently  
469 been published by the European Space Agency (ESA) on its website (Galileo  
470 2016). Note that these published values for IOVs are based on absolute  
471 calibration carried out on ground against a payload verification system.

472

473 **Table 3** Comparison of Galileo IOV Satellite DCBs as estimated from the  
 474 DCB\_FIX Software with the ESA published manufacturer measured on ground  
 475 DCBs.

476

Galileo PRN	DCB E1-E5a Estimates (in ns)			
	ESA Published DCBs (I)	DCB_FIX Software (II)	DCB derived from BGD	Difference between (II) and (I)
E11	9.71 ± 0.38	11.07 ± 0.52	16.62	1.36
E12	6.97 ± 0.41	8.80 ± 0.37	14.77	1.83
E19	2.15 ± 0.48	3.06 ± 0.29	8.12	0.91

477

478 It can be seen from Table 3 that the DCB estimates from the DCB\_FIX software  
 479 agree with the manufacturer measured on ground DCBs at the level of 1 to 2 ns.  
 480 The results obtained by the DCB\_FIX software are expected to improve further  
 481 once the simulator DCB is accounted for in this processing strategy. Minor  
 482 improvements have also been observed in the DCB estimation by increasing the  
 483 degree and order of the spherical harmonics in the global VTEC expression.

484

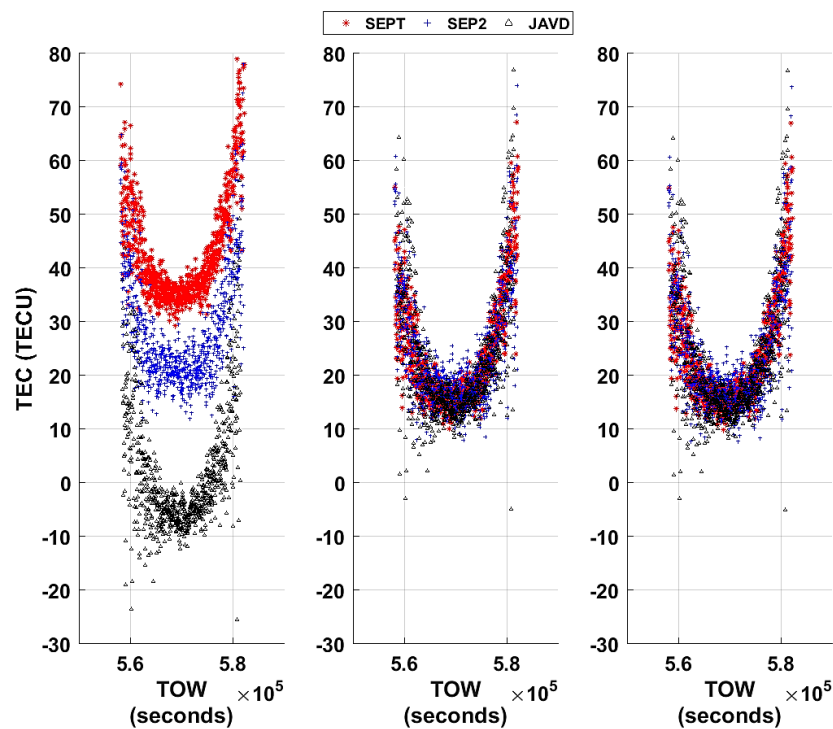
485 **Results for Estimated STEC using different Calibration Strategies (GPS**  
 486 **P1/P2 only):**

487 Based on equation (5) and using daily RINEX datasets, the STEC is estimated  
 488 for different co-located receivers in the network, with the purpose of comparing  
 489 the different STEC estimation strategies. The uncalibrated STEC refers to the  
 490 case where no DCBs were applied and the calibrated STEC refers to the case  
 491 where either IGS published DCBs or DCB\_FIX estimated DCBs were applied.

492 Figure 10 shows the STEC plots constructed on the basis of different  
 493 calibration strategies for PRN 24, as observed by the three NGI receivers, i.e.

494 SEPT, SEP2 and JAVD, on the ionosphericly quiet day of Mar 26, 2016. The  
 495 improvement and consistency in the estimated STEC as observed by three  
 496 different receivers can be clearly seen from these plots between uncalibrated and  
 497 calibrated solutions. It is also apparent that, in comparison to the highly  
 498 specialized ISMRs such as SEPT and SEP2, the geodetic grade receiver, the  
 499 Javad Triumph – 1, can also be used to generate almost similar STEC, if receiver  
 500 and satellite DCBs can be properly estimated. Here, one minor concern would  
 501 be the increased noise level in the JAVD’s TEC measurements even after the  
 502 application of smoothing. However, as previously stated, a fair comparison  
 503 would only be possible by using a consistent set of tracking parameters for all  
 504 three receivers. Note that all three receivers are connected separately to three  
 505 different antennas and were operating under different tracking parameters, as  
 506 presented in Table 1.

507



508

509

510 **Fig. 10** Uncalibrated (left), IGS or DCB\_ZM Calibrated (Center) and  
 511 DCB\_FIX Calibrated (Right) STEC plots for PRN 24 as observed by SEPT,  
 512 SEPT and JAVD receiver systems (Mar 26, 2016)

513

514           From Figure 10, it can also be observed that there is a good agreement  
515 between IGS (or DCB\_ZM) calibrated and DCB\_FIX calibrated STEC plots.  
516 This demonstrates that for all practical purposes of ionospheric modeling, using  
517 the 'known' receiver DCB as an external constraint in comparison to the IGS  
518 strategy, represents a perfectly valid way of resolving the rank deficiency  
519 problem.

520

#### 521 **Estimation of Simulator DCB (For GPS P1/P2 Only):**

522 As contrary to our earlier assumption of negligible simulator DCB, a strategy  
523 was devised to estimate the contribution of the simulator in the DCB estimation  
524 by involving the IGS AMC2 station. From the log file of AMC2 station  
525 ([https://igsceb.jpl.nasa.gov/igsceb/station/log/amc2\\_20140915.log](https://igsceb.jpl.nasa.gov/igsceb/station/log/amc2_20140915.log)), it can be seen  
526 that the individual hardware delays existing between different components of the  
527 system such as antenna, antenna cable, antenna splitter, receiver, etc. have  
528 already been measured and applied to the raw code based pseudoranges.  
529 Although not knowing exactly how these individual delays are measured, it is  
530 considered here that the measurements are done accurately enough. Based on  
531 that assumption, one can expect to get a DCB value close to 0 for this station  
532 when estimating DCBs using a 'known' receiver DCB, provided that the  
533 ionosphere has been correctly modelled. As shown in Figure 7, by using the  
534 DCB\_FIX software, a mean DCB value of + 1.62 ns was estimated for this  
535 station, implying therefore that a value of – 1.62 ns with some uncertainty can  
536 be interpreted to represent the DCB of the simulator itself existing between GPS  
537 P1 and P2 signals. Hence, it can be inferred that the simulator DCB for a certain  
538 signal combination can be measured by exploiting the proposed strategy in  
539 conjunction with a station receiver with accurately known hardware delays and  
540 this would further push the estimated DCBs toward their physical values.

541

#### 542 **Conclusions:**

- 543 1. A hardware signal simulator such as the Spirent GSS8000 can be effectively  
544 used to estimate a consistent set of DCBs between different signal  
545 combinations for any multi frequency, multi constellation receiver. The  
546 proposed technique can be improved further by accounting for the simulator  
547 delays as well.
- 548 2. The receiver DCB is often mistaken as a function of the receiver hardware  
549 only. This is in fact not true because in an open sky situation, the receiver  
550 DCB refers to the DCB of the entire ‘system’ comprising of antenna, cable  
551 and the receiver itself. Therefore, it should be ensured that if a receiver DCB  
552 is to be used to estimate the satellites and receivers DCBs in a regional or  
553 global network, the DCB of the whole system is used to constrain the solution,  
554 otherwise one can expect variations in the estimated DCBs with the changing  
555 system components such as antenna, cable, splitter, etc.
- 556 3. Since the IGS is generating DCBs for only a selected number of terrestrial  
557 stations, the technique proposed offers an alternative way of locally  
558 estimating the DCB of any receiver – satellite system using the DCB\_FIX  
559 software. The advantage would be that the changes in the constellation will  
560 not affect the DCB estimation, unlike when any other constraint is used.
- 561 4. A good agreement at the level of 1 to 2 ns was found to exist between the  
562 estimated DCBs from the DCB\_FIX software and the manufacturer measured  
563 on ground absolute DCBs for the 3 Galileo IOVs satellite as published by the  
564 ESA.
- 565 5. The comparison between calibrated and uncalibrated STEC estimation  
566 clearly shows the improvement and consistency in the estimated STEC  
567 techniques between the different receiver types. Relative to highly specialized  
568 ionospheric scintillation monitor receivers, a geodetic grade receiver like  
569 Javad Triumph – 1 can also be used to compute STEC provided that the  
570 receiver and satellite DCBs are properly estimated and applied.
- 571 6. A good agreement between the IGS (or DCB\_ZM) and DCB\_FIX calibrated  
572 STEC plots was demonstrated. This also demonstrates that for all practical  
573 purposes of ionospheric modeling, using the ‘known’ receiver DCB as an



574 external constraint is a demonstrated valid way of resolving the rank  
575 deficiency problem that arises when computing DCB estimations for  
576 receiver/satellite network.

577

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588

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701

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733