Coherent diffractive phot oproduction of $\rho 0$ mesons on gol d nucl ei at $200 \mathrm{GeV} /$ nucl eon－pai $r$ at the Rel ativistic Heavy I on Collider

| 著者 | STAR Col I abor at i on，Esumi S |
| :--- | :--- |
| j our nal or <br> publ i cat i on titl e | Physi cal revi ew C |
| vol une | 96 |
| nunber | 5 |
| page range | 054904 |
| year | $2017-11$ |
| 権利 | （C）2017 Aner i can Physi cal Soci et y |
| URL | ht t p：／／hdl ．handl e．net／2241／00149210 |

# Coherent diffractive photoproduction of $\rho^{0}$ mesons on gold nuclei at 200 GeV /nucleon-pair at the Relativistic Heavy Ion Collider 

L. Adamczyk, ${ }^{1}$ J. K. Adkins, ${ }^{2}$ G. Agakishiev, ${ }^{3}$ M. M. Aggarwal, ${ }^{4}$ Z. Ahammed, ${ }^{5}$ N. N. Ajitanand, ${ }^{6}$ I. Alekseev, ${ }^{7,8}$ D. M. Anderson, ${ }^{9}$ R. Aoyama, ${ }^{10}$ A. Aparin, ${ }^{3}$ D. Arkhipkin, ${ }^{11}$ E. C. Aschenauer, ${ }^{11}$ M. U. Ashraf, ${ }^{12}$ A. Attri, ${ }^{4}$ G. S. Averichev, ${ }^{3}$ X. Bai, ${ }^{13}$ V. Bairathi, ${ }^{14}$ A. Behera, ${ }^{6}$ R. Bellwied, ${ }^{15}$ A. Bhasin, ${ }^{16}$ A. K. Bhati, ${ }^{4}$ P. Bhattarai, ${ }^{17}$ J. Bielcik, ${ }^{18}$ J. Bielcikova, ${ }^{19}$ L. C. Bland, ${ }^{11}$ I. G. Bordyuzhin, ${ }^{7}$ J. Bouchet, ${ }^{20}$ J. D. Brandenburg, ${ }^{21}$ A. V. Brandin,,${ }^{8}$ D. Brown, ${ }^{22}$ I. Bunzarov, ${ }^{3}$ J. Butterworth, ${ }^{21}$ H. Caines, ${ }^{23}$ M. Calderón de la Barca Sánchez, ${ }^{24}$ J. M. Campbell, ${ }^{25}$ D. Cebra, ${ }^{24}$ I. Chakaberia, ${ }^{11}$ P. Chaloupka, ${ }^{18}$ Z. Chang, ${ }^{9}$ N. Chankova-Bunzarova, ${ }^{3}$ A. Chatterjee, ${ }^{5}$ S. Chattopadhyay, ${ }^{5}$ X. Chen, ${ }^{26}$ J. H. Chen, ${ }^{27}$ X. Chen, ${ }^{28}$ J. Cheng, ${ }^{12}$ M. Cherney, ${ }^{29}$ W. Christie, ${ }^{11}$ G. Contin, ${ }^{30}$ H. J. Crawford, ${ }^{31}$ S. Das, ${ }^{13}$ L. C. De Silva, ${ }^{29}$ R. R. Debbe, ${ }^{11}$ T. G. Dedovich, ${ }^{3}$ J. Deng, ${ }^{32}$ A. A. Derevschikov, ${ }^{33}$ L. Didenko, ${ }^{11}$ C. Dilks, ${ }^{34}$ X. Dong, ${ }^{30}$ J. L. Drachenberg, ${ }^{35}$ J. E. Draper, ${ }^{24}$ L. E. Dunkelberger, ${ }^{36}$ J. C. Dunlop, ${ }^{11}$ L. G. Efimov, ${ }^{3}$ N. Elsey, ${ }^{37}$ J. Engelage, ${ }^{31}$ G. Eppley, ${ }^{21}$ R. Esha, ${ }^{36}$ S. Esumi, ${ }^{10}$ O. Evdokimov, ${ }^{38}$ J. Ewigleben, ${ }^{22}$ O. Eyser, ${ }^{11}$ R. Fatemi, ${ }^{2}$ S. Fazio, ${ }^{11}$ P. Federic, ${ }^{19}$ P. Federicova, ${ }^{18}$ J. Fedorisin, ${ }^{3}$ Z. Feng, ${ }^{13}$ P. Filip, ${ }^{3}$ E. Finch,,${ }^{39}$ Y. Fisyak, ${ }^{11}$ C. E. Flores, ${ }^{24}$ L. Fulek, ${ }^{1}$ C. A. Gagliardi, ${ }^{9}$ D. Garand, ${ }^{40}$ F. Geurts, ${ }^{21}$ A. Gibson, ${ }^{41}$ M. Girard, ${ }^{42}$ D. Grosnick, ${ }^{41}$ D. S. Gunarathne, ${ }^{43}$ Y. Guo, ${ }^{20}$ A. Gupta, ${ }^{16}$ S. Gupta, ${ }^{16}$ W. Guryn, ${ }^{11}$ A. I. Hamad, ${ }^{20}$ A. Hamed, ${ }^{9}$ A. Harlenderova, ${ }^{18}$ J. W. Harris, ${ }^{23}$ L. He, ${ }^{40}$ S. Heppelmann, ${ }^{34}$ S. Heppelmann, ${ }^{24}$ A. Hirsch, ${ }^{40}$ G. W. Hoffmann, ${ }^{17}$ S. Horvat, ${ }^{23}$ T. Huang, ${ }^{44}$ B. Huang, ${ }^{38}$ X. Huang, ${ }^{12}$ H. Z. Huang, ${ }^{36}$ T. J. Humanic, ${ }^{25}$ P. Huo, ${ }^{6}$ G. Igo, ${ }^{36}$ W. W. Jacobs, ${ }^{45}$ A. Jentsch, ${ }^{17}$ J. Jia, ${ }^{6,11}$ K. Jiang,,$^{26}$ S. Jowzaee, ${ }^{37}$ E. G. Judd, ${ }^{31}$ S. Kabana, ${ }^{20}$ D. Kalinkin, ${ }^{45}$ K. Kang, ${ }^{12}$ K. Kauder, ${ }^{37}$ H. W. Ke, ${ }^{11}$ D. Keane, ${ }^{20}$

A. Kechechyan, ${ }^{3}$ Z. Khan, ${ }^{38}$ D. P. Kikoła, ${ }^{42}$ I. Kisel, ${ }^{46}$ A. Kisiel, ${ }^{42}$ S. R. Klein, ${ }^{30}$ L. Kochenda, ${ }^{8}$ M. Kocmanek, ${ }^{19}$ T. Kollegger, ${ }^{46}$ L. K. Kosarzewski, ${ }^{42}$ A. F. Kraishan, ${ }^{43}$ P. Kravtsov, ${ }^{8}$ K. Krueger, ${ }^{47}$ N. Kulathunga, ${ }^{15}$ L. Kumar, ${ }^{4}$ J. Kvapil, ${ }^{18}$ J. H. Kwasizur, ${ }^{45}$ R. Lacey, ${ }^{6}$ J. M. Landgraf, ${ }^{11}$ K. D. Landry, ${ }^{36}$ J. Lauret, ${ }^{11}$ A. Lebedev, ${ }^{11}$ R. Lednicky, ${ }^{3}$ J. H. Lee, ${ }^{11}$ X. Li, ${ }^{26}$ C. Li, ${ }^{26}$ W. Li, ${ }^{27}$ Y. Li, ${ }^{12}$ J. Lidrych, ${ }^{18}$ T. Lin, ${ }^{45}$ M. A. Lisa, ${ }^{25}$ H. Liu, ${ }^{45}$ P. Liu, ${ }^{6}$ Y. Liu, ${ }^{9}$ F. Liu, ${ }^{13}$ T. Ljubicic,,${ }^{11}$ W. J. Llope, ${ }^{37}$ M. Lomnitz, ${ }^{30}$ R. S. Longacre, ${ }^{11}$ S. Luo, ${ }^{38}$ X. Luo, ${ }^{13}$ G. L. Ma, ${ }^{27}$ L. Ma, ${ }^{27}$ Y. G. Ma, ${ }^{27}$ R. Ma, ${ }^{11}$ N. Magdy, ${ }^{6}$ R. Majka, ${ }^{23}$ D. Mallick, ${ }^{14}$ S. Margetis, ${ }^{20}$ C. Markert, ${ }^{17}$ H. S. Matis, ${ }^{30}$ K. Meehan, ${ }^{24}$ J. C. Mei, ${ }^{32}$ Z. W. Miller, ${ }^{38}$ N. G. Minaev, ${ }^{33}$ S. Mioduszewski, ${ }^{9}$ D. Mishra, ${ }^{14}$ S. Mizuno, ${ }^{30}$ B. Mohanty, ${ }^{14}$ M. M. Mondal, ${ }^{48}$ D. A. Morozov, ${ }^{33}$ M. K. Mustafa, ${ }^{30}$ Md. Nasim, ${ }^{36}$ T. K. Nayak, ${ }^{5}$ J. M. Nelson, ${ }^{31}$ M. Nie, ${ }^{27}$ G. Nigmatkulov, ${ }^{8}$ T. Niida, ${ }^{37}$ L. V. Nogach, ${ }^{33}$ T. Nonaka, ${ }^{10}$ S. B. Nurushev, ${ }^{33}$ G. Odyniec, ${ }^{30}$ A. Ogawa, ${ }^{11}$ K. Oh, ${ }^{49}$ V. A. Okorokov, ${ }^{8}$ D. Olvitt Jr., ${ }^{43}$ B. S. Page, ${ }^{11}$ R. Pak, ${ }^{11}$ Y. Pandit, ${ }^{38}$ Y. Panebratsev, ${ }^{3}$ B. Pawlik, ${ }^{50}$ H. Pei, ${ }^{13}$ C. Perkins, ${ }^{31}$ P. Pile,,${ }^{11}$ J. Pluta, ${ }^{42}$ K. Poniatowska, ${ }^{42}$ J. Porter, ${ }^{30}$ M. Posik, ${ }^{43}$ A. M. Poskanzer, ${ }^{30}$ N. K. Pruthi, ${ }^{4}$ M. Przybycien, ${ }^{1}$ J. Putschke, ${ }^{37}$ H. Qiu, ${ }^{40}$ A. Quintero, ${ }^{43}$ S. Ramachandran, ${ }^{2}$ R. L. Ray, ${ }^{17}$ R. Reed, ${ }^{22}$ M. J. Rehbein, ${ }^{29}$ H. G. Ritter, ${ }^{30}$ J. B. Roberts, ${ }^{21}$ O. V. Rogachevskiy, ${ }^{3}$ J. L. Romero, ${ }^{24}$ J. D. Roth, ${ }^{29}$ L. Ruan, ${ }^{11}$ J. Rusnak, ${ }^{19}$ O. Rusnakova, ${ }^{18}$ N. R. Sahoo, ${ }^{9}$ P. K. Sahu, ${ }^{48}$ S. Salur, ${ }^{30}$ J. Sandweiss, ${ }^{23}$ M. Saur, ${ }^{19}$ J. Schambach, ${ }^{17}$ A. M. Schmah, ${ }^{30}$ W. B. Schmidke, ${ }^{11}$ N. Schmitz, ${ }^{51}$ B. R. Schweid, ${ }^{6}$ J. Seger, ${ }^{29}$ M. Sergeeva, ${ }^{36}$ P. Seyboth, ${ }^{51}$ N. Shah,,${ }^{27}$ E. Shahaliev, ${ }^{3}$ P. V. Shanmuganathan, ${ }^{22}$ M. Shao, ${ }^{26}$ A. Sharma, ${ }^{16}$ M. K. Sharma, ${ }^{16}$ W. Q. Shen, ${ }^{27}$ Z. Shi, ${ }^{30}$ S. S. Shi, ${ }^{13}$ Q. Y. Shou, ${ }^{27}$ E. P. Sichtermann, ${ }^{30}$ R. Sikora, ${ }^{1}$ M. Simko, ${ }^{19}$ S. Singha, ${ }^{20}$ M. J. Skoby, ${ }^{45}$ N. Smirnov, ${ }^{23}$ D. Smirnov, ${ }^{11}$ W. Solyst, ${ }^{45}$ L. Song, ${ }^{15}$ P. Sorensen, ${ }^{11}$ H. M. Spinka, ${ }^{47}$ B. Srivastava, ${ }^{40}$ T. D. S. Stanislaus, ${ }^{41}$ M. Strikhanov, ${ }^{8}$ B. Stringfellow, ${ }^{40}$ T. Sugiura, ${ }^{10}$ M. Sumbera, ${ }^{19}$ B. Summa, ${ }^{34}$ Y. Sun, ${ }^{26}$ X. M. Sun, ${ }^{13}$ X. Sun, ${ }^{13}$ B. Surrow, ${ }^{43}$ D. N. Svirida, ${ }^{7}$ A. H. Tang, ${ }^{11}$ Z. Tang, ${ }^{26}$ A. Taranenko, ${ }^{8}$ T. Tarnowsky, ${ }^{52}$ A. Tawfik, ${ }^{53}$ J. Thäder, ${ }^{30}$ J. H. Thomas, ${ }^{30}$ A. R. Timmins, ${ }^{15}$ D. Tlusty, ${ }^{21}$ T. Todoroki, ${ }^{11}$ M. Tokarev, ${ }^{3}$ S. Trentalange, ${ }^{36}$ R. E. Tribble, ${ }^{9}$ P. Tribedy, ${ }^{11}$ S. K. Tripathy, ${ }^{48}$ B. A. Trzeciak, ${ }^{18}$ O. D. Tsai, ${ }^{36}$ T. Ullrich, ${ }^{11}$ D. G. Underwood, ${ }^{47}$ I. Upsal, ${ }^{25}$ G. Van Buren, ${ }^{11}$ G. van Nieuwenhuizen, ${ }^{11}$ A. N. Vasiliev, ${ }^{33}$ F. Videbæk, ${ }^{11}$ S. Vokal, ${ }^{3}$ S. A. Voloshin, ${ }^{37}$ A. Vossen, ${ }^{45}$ G. Wang, ${ }^{36}$ Y. Wang, ${ }^{13}$ F. Wang, ${ }^{40}$ Y. Wang, ${ }^{12}$ J. C. Webb, ${ }^{11}$ G. Webb, ${ }^{11}$ L. Wen, ${ }^{36}$ G. D. Westfall, ${ }^{52}$ H. Wieman, ${ }^{30}$ S. W. Wissink, ${ }^{45}$ R. Witt, ${ }^{54}$ Y. Wu, ${ }^{2}$ Z. G. Xiao, ${ }^{12}$ W. Xie, ${ }^{40}$ G. Xie, ${ }^{26}$ J. Xu, ${ }^{13}$ N. Xu, ${ }^{30}$ Q. H. Xu, ${ }^{32}$ Y. F. Xu, ${ }^{27}$ Z. Xu, ${ }^{11}$ Y. Yang, ${ }^{44}$ Q. Yang, ${ }^{26}$ C. Yang,,${ }^{32}$ S. Yang, ${ }^{11}$ Z. Ye, ${ }^{38}$ Z. Ye, ${ }^{38}$ L. Yi, ${ }^{23}$ K. Yip, ${ }^{11}$ I.-K. Yoo, ${ }^{49}$ N. Yu, ${ }^{13}$ H. Zbroszczyk, ${ }^{42}$ W. Zha, ${ }^{26}$ Z. Zhang, ${ }^{27}$ X. P. Zhang, ${ }^{12}$ J. B. Zhang, ${ }^{13}$ S. Zhang, ${ }^{26}$ J. Zhang, ${ }^{28}$ Y. Zhang, ${ }^{26}$ J. Zhang, ${ }^{30}$ S. Zhang, ${ }^{27}$ J. Zhao, ${ }^{40}$ C. Zhong, ${ }^{27}$ L. Zhou, ${ }^{26}$ C. Zhou, ${ }^{27}$ X. Zhu, ${ }^{12}$ Z. Zhu, ${ }^{32}$ and M. Zyzak ${ }^{46}$
(STAR Collaboration)
${ }^{1}$ AGH University of Science and Technology, FPACS, Cracow 30-059, Poland
${ }^{2}$ University of Kentucky, Lexington, Kentucky 40506-0055
${ }^{3}$ Joint Institute for Nuclear Research, Dubna, 141 980, Russia
${ }^{4}$ Panjab University, Chandigarh 160014, India
${ }^{5}$ Variable Energy Cyclotron Centre, Kolkata 700064, India
${ }^{6}$ State University of New York, Stony Brook, New York 11794
${ }^{7}$ Alikhanov Institute for Theoretical and Experimental Physics, Moscow 117218, Russia
${ }^{8}$ National Research Nuclear University MEPhI, Moscow 115409, Russia
${ }^{9}$ Texas A\&M University, College Station, Texas 77843
${ }^{10}$ University of Tsukuba, Tsukuba, Ibaraki, Japan
${ }^{11}$ Brookhaven National Laboratory, Upton, New York 11973

${ }^{12}$ Tsinghua University, Beijing 100084<br>${ }^{13}$ Central China Normal University, Wuhan, Hubei 430079<br>${ }^{14}$ National Institute of Science Education and Research, Bhubaneswar 751005, India<br>${ }^{15}$ University of Houston, Houston, Texas 77204<br>${ }^{16}$ University of Jammu, Jammu 180001, India<br>${ }^{17}$ University of Texas, Austin, Texas 78712<br>${ }^{18}$ Czech Technical University in Prague, FNSPE, Prague, 115 19, Czech Republic<br>${ }^{19}$ Nuclear Physics Institute AS CR, 25068 Prague, Czech Republic<br>${ }^{20}$ Kent State University, Kent, Ohio 44242<br>${ }^{21}$ Rice University, Houston, Texas 77251<br>${ }^{22}$ Lehigh University, Bethlehem, Pennsylvania 18015<br>${ }^{23}$ Yale University, New Haven, Connecticut 06520<br>${ }^{24}$ University of California, Davis, California 95616<br>${ }^{25}$ Ohio State University, Columbus, Ohio 43210<br>${ }^{26}$ University of Science and Technology of China, Hefei, Anhui 230026<br>${ }^{27}$ Shanghai Institute of Applied Physics, Chinese Academy of Sciences, Shanghai 201800<br>${ }^{28}$ Institute of Modern Physics, Chinese Academy of Sciences, Lanzhou, Gansu 730000<br>${ }^{29}$ Creighton University, Omaha, Nebraska 68178<br>${ }^{30}$ Lawrence Berkeley National Laboratory, Berkeley, California 94720<br>${ }^{31}$ University of California, Berkeley, California 94720<br>${ }^{32}$ Shandong University, Jinan, Shandong 250100<br>${ }^{33}$ Institute of High Energy Physics, Protvino 142281, Russia<br>${ }^{34}$ Pennsylvania State University, University Park, Pennsylvania 16802<br>${ }^{35}$ Lamar University, Physics Department, Beaumont, Texas 77710<br>${ }^{36}$ University of California, Los Angeles, California 90095<br>${ }^{37}$ Wayne State University, Detroit, Michigan 48201<br>${ }^{38}$ University of Illinois at Chicago, Chicago, Illinois 60607<br>${ }^{39}$ Southern Connecticut State University, New Haven, Connecticut 06515<br>${ }^{40}$ Purdue University, West Lafayette, Indiana 47907<br>${ }^{41}$ Valparaiso University, Valparaiso, Indiana 46383<br>${ }^{42}$ Warsaw University of Technology, Warsaw 00-661, Poland<br>${ }^{43}$ Temple University, Philadelphia, Pennsylvania 19122<br>${ }^{44}$ National Cheng Kung University, Tainan 70101<br>${ }^{45}$ Indiana University, Bloomington, Indiana 47408<br>${ }^{46}$ Frankfurt Institute for Advanced Studies FIAS, Frankfurt 60438, Germany<br>${ }^{47}$ Argonne National Laboratory, Argonne, Illinois 60439<br>${ }^{48}$ Institute of Physics, Bhubaneswar 751005, India<br>${ }^{49}$ Pusan National University, Pusan 46241, Korea<br>${ }^{50}$ Institute of Nuclear Physics PAN, Cracow 31-342, Poland<br>${ }^{51}$ Max-Planck-Institut fur Physik, Munich 80805, Germany<br>${ }^{52}$ Michigan State University, East Lansing, Michigan 48824<br>${ }^{53}$ World Laboratory for Cosmology and Particle Physics (WLCAPP), Cairo 11571, Egypt<br>${ }^{54}$ United States Naval Academy, Annapolis, Maryland, 21402<br>(Received 18 May 2017; published 13 November 2017)

The STAR Collaboration reports on the photoproduction of $\pi^{+} \pi^{-}$pairs in gold-gold collisions at a center-ofmass energy of 200 GeV /nucleon-pair. These pion pairs are produced when a nearly real photon emitted by one ion scatters from the other ion.

We fit the $\pi^{+} \pi^{-}$invariant-mass spectrum with a combination of $\rho^{0}$ and $\omega$ resonances and a direct $\pi^{+} \pi^{-}$ continuum. This is the first observation of the $\omega$ in ultraperipheral collisions, and the first measurement of $\rho-\omega$ interference at energies where photoproduction is dominated by Pomeron exchange. The $\omega$ amplitude is consistent with the measured $\gamma p \rightarrow \omega p$ cross section, a classical Glauber calculation, and the $\omega \rightarrow \pi^{+} \pi^{-}$branching ratio. The $\omega$ phase angle is similar to that observed at much lower energies, showing that the $\rho-\omega$ phase difference does not depend significantly on photon energy.

The $\rho^{0}$ differential cross section $d \sigma / d t$ exhibits a clear diffraction pattern, compatible with scattering from a gold nucleus, with two minima visible. The positions of the diffractive minima agree better with the predictions of a quantum Glauber calculation that does not include nuclear shadowing than with a calculation that does include shadowing.

## I. INTRODUCTION

Relativistic heavy ions are accompanied by high photon fluxes due to their large electric charge and the strongly Lorentz-contracted electric fields. In relativistic heavy ion collisions, these fields can produce photonuclear interactions. When the nuclei collide and interact hadronically, strong interactions obscure these electromagnetic interactions. However, at impact parameters large enough so that no hadronic interactions occur, the photonuclear interactions can be seen; these are ultraperipheral collisions (UPCs). The photon flux is well described within the Weizsäcker-Williams formalism [1,2]. Since they come from nuclei, these photons are nearly real, with virtuality set by the nuclear radius $R_{A}$. For gold, $\left\langle Q^{2}\right\rangle \sim\left(\hbar / R_{A}\right)^{2} \sim 10^{-3} \mathrm{GeV} / c^{2}$.

Vector-meson photoproduction may be modeled by the photon fluctuating to a quark-antiquark pair which then scatters from the target nucleus, emerging as a real vector meson. A more detailed model treats the photon as a combination of Fock states: a bare photon with virtual $q \bar{q}$ pairs, plus higher virtual states. This model described the photoproduction measurements performed at the Hadron-Electron Ring Accelerator (HERA) at DESY [3] and is also applicable in the UPC environment. The cross-section for UPC photoproduction can be found by convoluting the photon flux (with the constraint that there be no hadronic interactions) with the photon-nucleon cross section. For nuclear targets, one needs to account for the possibility of multiple dipole-target interactions, usually via a Glauber calculation.

The first calculation of UPC photoproduction cross sections used HERA data on $\gamma p \rightarrow \rho^{0} p$ as input to a classical Glauber calculation to predict the cross section with heavy ion targets [4]. It correctly predicted the $\rho^{0}$ photoproduction cross section at the Relativistic Heavy Ion Collider (RHIC), at energies of $62 \mathrm{GeV} /$ nucleon-pair [5], 130 [6] and $200 \mathrm{GeV} /$ nucleon-pair [7], and up to $2.76 \mathrm{TeV} /$ nucleon-pair at the Large Hadron Collider (LHC) [8]. A later calculation treated the $q \bar{q}$ pair as a dipole in a quantum Glauber calculation, which found a cross section about $50 \%$ higher, in tension with the data [9]. In a modified quantum Glauber calculation, nuclear shadowing reduces the calculated $\rho^{0}$ cross section [10], in agreement with the data. Other calculations include nuclear saturation mechanisms, including the color glass condensate [11,12]. Twophoton production of $\pi^{+} \pi^{-}$pairs also occurs, but the cross section is much smaller than for photonuclear interactions [13].

For photoproduction of $\rho^{0}$ mesons in gold-gold collisions at a center-of-mass energy of $200 \mathrm{GeV} /$ nucleon-pair at RHIC, the $\rho^{0}$ rapidity range $|y|<0.7$ corresponds to photon-nucleon center-of-mass energies from 9 to 18 GeV , depending on the rapidity and final-state transverse momentum. In this region, the $\rho^{0}$ photoproduction cross section increases slowly with collision energy and the $\gamma p \rightarrow \rho^{0} p$ cross section is well described by the soft-Pomeron model [14]; the $\gamma A$ cross section is almost independent of energy [4].

Because of the high photon flux, these UPC events have a high probability to be accompanied by additional photon exchanges that excite one or both of the ions into giant dipole
resonances (GDRs) or higher excitations. The GDRs typically decay by emitting a single neutron, while higher resonances usually decay by emitting two or more neutrons [15]. These neutrons have low momentum with respect to their parent ion, so largely retain the beam rapidity. For heavy nuclei, the cross section for multiphoton interactions nearly factorizes [16], with the combined cross section given by an integral over impact parameter space:

$$
\begin{align*}
\sigma\left(A_{1} A_{2} \rightarrow A_{1}^{*} A_{2}^{*} \rho^{0}\right)= & \int d^{2} b\left[1-P_{\mathrm{Had}}(b)\right] P_{1}\left(b, A^{*}\right) \\
& \times P_{2}\left(b, A^{*}\right) P\left(b, \rho^{0}\right) \tag{1}
\end{align*}
$$

where $P_{\text {Had }}(b), P_{1}\left(b, A^{*}\right), P_{2}\left(b, A^{*}\right)$, and $P\left(b, \rho^{0}\right)$ are the respective probabilities for having a hadronic interaction, exciting each of the ions and producing a $\rho^{0}$. Each photonmediated reaction occurs via independent photon exchange, so all four probabilities are tied together only through a common impact parameter [17]. The photonuclear cross sections are based on a parametrization of data [18]. Because the cross sections are large, we must account for the possibility of multiple photons exciting a single nucleus. This is included in our simulations via a unitarization process, as discussed in Refs. [17,18]. Experimentally, requiring mutual Coulomb excitation along with dipion production leads to a trigger with a higher purity, allowing more events to be collected than for the dipion state by itself.

This paper reports on the measurement of exclusive $\rho^{0}$ and $\omega$ meson and direct $\pi^{+} \pi^{-}$photoproduction in UPCs between gold ions using the Solenoidal Tracker at RHIC (STAR) detector at a center-of-mass energy of $200 \mathrm{GeV} /$ nucleon-pair. The current data sample is about 100 times larger than in previous RHIC measurements [7], allowing for much-higher-precision studies and two main new results. First, the $\pi \pi$ invariant-mass distribution cannot be fit with just $\rho^{0}$ and direct $\pi^{+} \pi^{-}$ components; an additional contribution from photoproduction of $\omega$, with $\omega \rightarrow \pi^{+} \pi^{-}$is required for an acceptable fit. The second result is the observation of a diffraction pattern, clearly showing the first and second minima, with a possible third. This diffraction pattern can be used to determine the distribution of the hadronic interactions in gold nuclei.

## II. EXPERIMENTAL SETUP AND ANALYSIS

This analysis uses an integrated luminosity of $1100 \pm$ $100 \mu \mathrm{~b}^{-1}$ of data collected in 2010. Four types of STAR subsystems were used for triggering and event reconstruction in the analysis: the time projection chamber (TPC), time-offlight system (TOF), beam beam counters (BBCs), and east and west zero degree calorimeters (ZDCs).

The STAR TPC [19] efficiently detects charged tracks from midrapidity to pseudorapidities beyond $|\eta|=1.0$, using 45 layers of pad rows in a $2-\mathrm{m}$-long cylinder. In the 0.5 T solenoidal magnetic field, the momentum resolution is $\Delta p / p=0.005+0.004 p$ where $p$ is in $\mathrm{GeV} / c$ [19]. The TPC can also identify charged particles by their specific ionization energy loss $(d E / d x)$ in the TPC gas. The $d E / d x$ resolution is $8 \%$ for a track that crosses 40 pad rows. This gives good pion separation up to a momentum comparable to the kaon mass.

The TOF surrounds the TPC, covering the pseudorapidity region $|\eta|<1$ [20]. In this analysis, the TOF was used to reject tracks that are out of time with the beam crossing.

The other detector components were used solely for triggering. Charged particles with pseudorapidity $2<|\eta|<5$ are detected by using the two BBCs, one on each side of the nominal interaction point. Each is formed with 18 scintillator tiles arranged around the beam pipe [21]. The ZDCs are small hadron calorimeters installed downstream of the collision region to detect neutrons at or near beam rapidity [22].

The trigger [23] selected 38 million events with low multiplicity in the central detector, along with one to roughly four neutrons in each ZDC, along the lines described in Ref. [7]. It required low activity in the TOF detector (at least two and no more than six hits), no charged particles detected in the BBC detectors, and, finally, showers in both ZDC detectors. The ZDC signals were required to be between 50 and 1200 analog to digital converter (ADC) counts, corresponding to an energy deposition between $1 / 4$ and about 4 beam-energy neutrons. The one-neutron peak was centered at 198 counts, with a width $(1 \sigma)$ of about 55 counts, making the ZDCs almost fully efficient for single neutrons.

The analysis selected events containing a pair of oppositely charged tracks that were consistent with originating from a single vertex, located within 50 cm longitudinally of the nominal interaction point. The tracks were required to have at least 14 hits in the TPC (out of a possible 45), to have $d E / d x$ values within $3 \sigma$ of the expected $d E / d x$ for a pion, and to have a valid hit in the TOF system to reject tracks from other beam crossings. This requirement also limited the track acceptance to the region $|\eta|<1.0$. The 384000 events with a $\pi^{+} \pi^{-}$pair invariant mass in the range $0.25<M_{\pi \pi}<1.5 \mathrm{GeV} / c^{2}$ and $|y|<1$ were saved for further evaluation.

The largest backgrounds for this analysis are lowmultiplicity hadronic interactions (peripheral ion-ion collisions). Other backgrounds come from other UPC reactions or from cosmic rays accompanied by in-time mutual Coulomb excitation. Pure electromagnetic production of $e^{+} e^{-}$pairs contribute less than $4 \%$ to the $\rho^{0}$ peak [6]. The decay $\omega \rightarrow \pi^{+} \pi^{-} \pi^{0}$ produces a $\pi^{+} \pi^{-}$pair with a larger $p_{T}$ than for coherent photoproduction, and a pair invariant mass that is usually below 600 MeV . It was a $2.7 \%$ background in a previous analysis [7] and, due to a higher cut on the pair invariant mass, should be smaller here. We neglect these minor backgrounds which are well within the overall systematic errors.

The hadronic background is estimated from the like-sign pion pairs. Figure 1 compares the transverse momentum $\left(p_{T}\right)$ distribution of the $\pi^{+} \pi^{-}$pairs (black histogram) with the corresponding distribution for like-sign pairs (red histogram) in two-track vertices. The signal has a prominent peak at $p_{T}<$ $100 \mathrm{MeV} / c$, from coherent photoproduction of pion pairs on the gold nucleus.

The reconstructed events are corrected for acceptance and detection efficiency by using a detailed simulation of the STAR detector. A mix of $\rho^{0}$ mesons and nonresonant $\pi^{+} \pi^{-}$ events are generated by using the STARlight Monte Carlo [4,24] which reproduces the kinematics of the processes, including the dipion mass and rapidity distributions. The generated events are passed through a complete GEANT [25]


FIG. 1. The unlike-sign (black-filled squares) pion-pair transverse momentum distribution. The peak below $100 \mathrm{MeV} / c$ is from coherently produced $\pi^{+} \pi^{-}$pairs. The red open squares show the pair momentum for same-sign pion pairs. Both histograms show pairs that come from vertices with only two tracks.
simulation of the detector and then embedded in "zero-bias" STAR events, data from randomly selected beam crossings. This embedding procedure accurately accounts for the detector noise and backgrounds, including overlapping events recorded in the STAR TPC during its sizable active time windows. As Fig. 2 shows, the agreement between the Monte Carlo and data is very good. The agreement in pair mass and rapidity and other kinematic distributions (not shown) gives us confidence that the Monte Carlo will correctly predict the experimental acceptance.


FIG. 2. Plots comparing data and the simulations used for efficiency determination, after all cuts. Comparison of uncorrected data (blue points) with embedded simulated $\rho^{0}$ and direct $\pi^{+} \pi^{-}$ events (yellow histogram). The simulated UPCs were run through a GEANT simulation of the detector, embedded in randomly triggered (zero-bias) events, and subject to the same reconstruction programs as the data.


FIG. 3. The shower energy in the west ZDC from neutrons produced by mutual dissociation is shown as a distribution of ADC channels. These events have a single neutron detected on the east ZDC. The peaks corresponding to one to four neutrons are fit with Gaussian distributions with standard deviations that grow as $n \sigma$, where $n$ is the number of neutrons and $\sigma$ is the standard deviation of the one-neutron Gaussian. The red curve is the sum of all Gaussians which are also displayed individually.

The event reconstruction efficiency depends only weakly on the pair mass and pair $p_{T}$, but depends fairly strongly on rapidity. The rapidity dependence has a bell shape with a maximum of $13 \%$ efficiency at $y \approx 0.1$. It is slightly asymmetric because of inefficiencies in one of the TPC east (rapidity $<0$ ) sectors. One uncertainty in the reconstruction efficiency stems from uncertainties in the actual ("as-built") positions of the TOF slats, which may not be completely accurately reflected in the simulations. While this uncertainty may affect the measured $d \sigma / d y$, particularly at large rapidity, it does not significantly affect the pair $p_{T}$ or mass acceptance uncertainties.

This analysis considers two classes of nuclear breakup: single neutrons ( $1 n$ ), associated with giant dipole resonances, or more than one neutron ( Xn ), from a broad range of photonuclear interactions including, as previously noted, multiphoton interactions. Figure 3 shows the ADC distribution from the west ZDC for events that satisfy a cut which selects events with a single neutron in the east ZDC and a photoproduced $\rho^{0}$ with $|y|<1$ and $p_{T}<100 \mathrm{MeV} / c$. Table I shows the

TABLE I. Mutual dissociation cross sections for events with exclusive coherent $\rho^{0}$ photoproduction within $|y|<1$, broken down by the number of neutrons in the east (rows) and west (columns) ZDCs.

| East ZDC | West ZDC |  |  |
| :--- | :---: | :---: | :---: |
|  | $1 n$ | $2 n$ | $3 n$ |
| $1 n$ | $1.38 \pm 0.24 \mathrm{mb}$ | $0.57 \pm 0.11 \mathrm{mb}$ | $0.39 \pm 0.07 \mathrm{mb}$ |
| $2 n$ | $0.57 \pm 0.11 \mathrm{mb}$ | $0.23 \pm 0.04 \mathrm{mb}$ | $0.18 \pm 0.03 \mathrm{mb}$ |
| $3 n$ | $0.40 \pm 0.07 \mathrm{mb}$ | $0.19 \pm 0.03 \mathrm{mb}$ | $0.15 \pm 0.03 \mathrm{mb}$ |

cross sections for coherent $\rho^{0}$ photoproduction accompanied by different numbers of neutrons. There is some nonlinearity in the system. The cross sections are determined by applying a window to one ZDC spectrum and fitting the neutron spectrum in the other, and then reversing the procedure. The fits included events with one, two, three, or four neutrons in each ZDC. The one- and two-neutron peaks are very clear, but the higher peaks are less obvious. The two results are averaged, and the difference is used as an estimate of the systematic error. Statistical errors are $<1 \%$ and are not listed. Systematic errors arising from the event-selection cuts were added in quadrature to the quadrature sum of the relevant common uncertainties listed in Table IV (17\%).

The limited ZDC window led to a relatively high yield of photoproduced $\rho^{0}$ per trigger, but the cost was that it did not cover the full neutron number spectrum. So, we used the $1 n 1 n$ events to normalize the $X n X n$ cross section, based on the STARlight [24] calculation of the cross-section ratio. We find the ratio of triggered events to those with single neutrons in each ZDC, using the fit results in Table I, and use the STARlight ratio of $X n X n$ to $1 n 1 n$ events to normalize the overall cross-section scale.

The cross sections in Table I decrease slowly with increasing total neutron number. The summed cross section for $2 n 1 n+1 n 2 n$ (i.e., the two combinations with one neutron in one direction) is $83 \%$ of the $1 n 1 n$ cross section. This fraction is larger than is seen for mutual Coulomb dissociation, where one calculation has the $(2 n 1 n+1 n 2 n): 1 n 1 n$ ratio around 0.6 [26] and another finds a ratio around 0.4 , albeit at a slightly lower beam energy [27]. Some of this difference is because requiring $\rho^{0}$ photoproduction selects events with smaller impact parameters, where the photon spectrum is harder [16].

## III. THE $\pi^{+} \pi^{-}$MASS SPECTRUM

Figure 4 shows the efficiency-corrected, like-sign-pair (background) subtracted invariant mass of the pion pairs with $p_{T}<100 \mathrm{MeV} / c$. Events with $M_{\pi \pi}>600 \mathrm{MeV} / c^{2}$ were initially fit with a modified Söding parametrization [28], with a relativistic Breit-Wigner resonance for the $\rho^{0}$ plus a flat direct $\pi^{+} \pi^{-}$continuum. This two-component model was a poor fit to the data, so an additional relativistic Breit-Wigner component was added, to account for $\omega$ photoproduction, followed by its decay $\omega \rightarrow \pi^{+} \pi^{-}$. The full fit function is

$$
\begin{align*}
\frac{d \sigma}{d M_{\pi^{+} \pi^{-}}} \propto & \left\lvert\, A_{\rho} \frac{\sqrt{M_{\pi \pi} M_{\rho} \Gamma_{\rho}}}{M_{\pi \pi}^{2}-M_{\rho}^{2}+i M_{\rho} \Gamma_{\rho}}+B_{\pi \pi}\right. \\
& +\left.C_{\omega} e^{i \phi_{\omega}} \frac{\sqrt{M_{\pi \pi} M_{\omega} \Gamma_{\omega \rightarrow \pi \pi}}}{M_{\pi \pi}^{2}-M_{\omega}^{2}+i M_{\omega} \Gamma_{\omega}}\right|^{2}+f_{p} \tag{2}
\end{align*}
$$

where $A_{\rho}$ is the $\rho$ amplitude, $B_{\pi \pi}$ is the amplitude for the direct pions, $C_{\omega}$ is the amplitude for the $\omega$, and $f_{p}$ is a linear polynomial that accounts for the remaining background. The momentum-dependent widths in Eqs. (3) and (4) below are motivated by the forms proposed in Ref. [29], where $\Gamma_{0}$ is the pole width for each meson. Several variations of the dipionmass dependence on the $\omega$ width were tried, but none differed


FIG. 4. The $\pi^{+} \pi^{-}$invariant-mass distribution for all selected $\pi \pi$ candidates with $p_{T}<100 \mathrm{MeV} / c$. The black markers show the data (in $2.5 \mathrm{MeV} / c^{2}$ bins). The magenta curve is the modified Söding fit to the data in the range $0.6<M_{\pi \pi}<1.3 \mathrm{GeV} / c^{2}$. Also shown are the $\rho^{0}$ Breit-Wigner component of the fit (brown curve), constant nonresonant pion-pair component (brown-dashed curve), interference between nonresonant pion pairs and the $\rho^{0}$ (blue-dashed curve), Breit-Wigner distribution for the $\omega$ mesons (blue solid curve), interference between $\rho^{0}$ and $\omega$ (red-dashed curve), and a small contribution from the remnant background, fit by a linear polynomial (cyan-dashed curve).
significantly from a constant, reflecting the fact that the $\omega$ width is small, and the width does not change significantly in that mass range. The momentum-dependent widths are taken to be

$$
\begin{equation*}
\Gamma_{\rho}=\Gamma_{0} \frac{M_{\rho}}{M_{\pi \pi}}\left(\frac{M_{\pi \pi}^{2}-4 m_{\pi}^{2}}{M_{\rho}^{2}-4 m_{\pi}^{2}}\right)^{3 / 2} \tag{3}
\end{equation*}
$$

and

$$
\begin{equation*}
\Gamma_{\omega}=\Gamma_{0} \frac{M_{\omega}}{M_{\pi \pi}}\left(\frac{M_{\pi \pi}^{2}-9 m_{\pi}^{2}}{M_{\omega}^{2}-9 m_{\pi}^{2}}\right)^{n} \tag{4}
\end{equation*}
$$

where $\Gamma_{0}$ is the pole width for each meson. For the $\omega$, the $9 m_{\pi}^{2}$ term reflects the fact that the $\omega$ decay is dominated by the three-pion channel, $n=3 / 2$ for a quasi-two-body decay [29] and $n=4$ for a free-space three-body decay $[30,31]$. We have tested $\Gamma$ as constant, and the $n=3 / 2$ and $n=4$ boundary cases. All three fits result in negligible difference due to the narrow width of $\omega$ decay, and we choose a default $\Gamma$ with $n=3 / 2$ for all the fits shown in the figures and extracted values. The branching ratio for $\omega \rightarrow \pi^{+} \pi^{-}$is small, so we use

$$
\begin{equation*}
\Gamma_{\omega \rightarrow \pi \pi}=\operatorname{Br}(\omega \rightarrow \pi \pi) \Gamma_{0} \frac{M_{\omega}}{M_{\pi \pi}}\left(\frac{M_{\pi \pi}^{2}-4 m_{\pi}^{2}}{M_{\omega}^{2}-4 m_{\pi}^{2}}\right)^{3 / 2} \tag{5}
\end{equation*}
$$

with $\operatorname{Br}(\omega \rightarrow \pi \pi)=0.0153_{-0.0013}^{+0.0011}$ [32].
In Eq. (2), $f_{p}$ is a linear function that describes the remaining remnant background. The masses and widths of the $\rho^{0}$ and $\omega$ were allowed to float, giving a total of ten parameters: two masses, two widths, three amplitudes, the phase of the $\omega$ meson, and two parameters for the background.

TABLE II. The results of fitting Eq. (2) to the data. The parameters $p_{0}$ and $p_{1}$ are for the polynomial background.

| Fit parameter | Value | Units |
| :--- | :---: | :---: |
| $M_{\rho}$ | $0.7762 \pm 0.0006$ | $\mathrm{GeV} / c^{2}$ |
| $\Gamma_{\rho}$ | $0.156 \pm 0.001$ | $\mathrm{GeV} / c^{2}$ |
| $A_{\rho}$ | $1.538 \pm 0.005$ |  |
| $B_{\pi \pi}$ | $-1.21 \pm 0.01$ | $\left(\mathrm{GeV} / c^{2}\right)^{-1 / 2}$ |
| $C_{\omega}$ | $0.55 \pm 0.04$ |  |
| $M_{\omega}$ | $0.7824 \pm 0.0008$ | $\mathrm{GeV} / c^{2}$ |
| $\Gamma_{\omega}$ | $0.017 \pm 0.002$ | $\mathrm{GeV} / c^{2}$ |
| $\phi_{\omega}$ | $1.46 \pm 0.11$ | Radians |
| $f_{p} p_{0}$ | $0.99 \pm 0.07$ | $\left(\mathrm{GeV} / c^{2}\right)^{-1}$ |
| $f_{p} p_{1}$ | $-0.86 \pm 0.06$ | $\left(\mathrm{GeV} / c^{2}\right)^{-2}$ |

Figure 4 shows the data and fit result, with several fit components, while Table II shows the fit results. The $\rho^{0}$ and $\omega$ masses and the $\rho^{0}$ width are in good agreement with their Particle Data Group values [32]. The $\omega$ is considerably wider than the standard value, because it is broadened by the detector resolution, which is comparable to the $\omega$ width. The fit $\chi^{2} / \mathrm{DOF}=255 / 270$ shows that the data and model are consistent in the fit region.

The ratio of direct $\pi^{+} \pi^{-}$to $\rho^{0}$ amplitudes, $|B / A|=$ $0.79 \pm 0.01$ (stat.) $\pm 0.08$ (syst.) $\quad\left(\mathrm{GeV} / c^{2}\right)^{-1 / 2}, \quad$ agrees within the $1 \sigma$ uncertainty with the value reported in the previous STAR publication [7]: $0.89 \pm 0.08$ (stat.) $\pm$ 0.09 (syst.) $\left(\mathrm{GeV} / c^{2}\right)^{-1 / 2}$. At $2.76 \mathrm{TeV} /$ nucleon-pair, the ALICE collaboration measured a smaller ratio, $|B / A|=$ $0.50 \pm 0.04$ (stat.) ${ }_{-0.04}^{+0.10}$ (syst.) $\left(\mathrm{GeV} / c^{2}\right)^{-1 / 2}$ [8].

The measured ratio of $\omega$ to $\rho^{0}$ amplitude was $C / A=$ $0.36 \pm 0.03$ (stat.) $\pm 0.04$ (syst.). The $\omega$ amplitude is small, but is clearly visible through its interference with the $\rho^{0}$ which produces a small kink in the spectrum near $800 \mathrm{MeV} / c^{2}$. The $\omega$ amplitude agrees with a prediction from STARlight [24], $C / A=0.32$, which uses the $\gamma p \rightarrow \omega p$ cross section and a classical Glauber calculation.

The only previous measurement of $\rho^{0}-\omega$ interference in the $\pi^{+} \pi^{-}$channel was made by a DESY-MIT group, using $5-7 \mathrm{GeV}$ photon beams [29]. That fit used a similar but not identical fit function. Neglecting some differences in the treatment of the $\omega$ width, that result was, in our terminology, $|C / A|=0.36 \pm 0.04$. In the terminology of Ref. [29] $|C / A|=\zeta \sqrt{M_{\rho} \Gamma_{\rho} / M_{\omega} \Gamma_{\omega}} / \sqrt{B r(\omega \rightarrow \pi \pi)}$, where $\zeta$ is their $\omega$ amplitude.

Our fit finds a nonzero $\omega$ phase angle, $\phi_{\omega}=1.46 \pm$ 0.11 (stat.) $\pm 0.07$ (syst.). The systematic error was estimated from fits using slightly different fit functions. This phase angle result is a bit lower than, but consistent within experimental uncertainties with the DESY-MIT measurement of $1.68 \pm$ 0.26. The DESY-MIT experiment used much lower energy photons, in a regime where $\omega$ production proceeds via both meson and Pomeron exchange. This shows that the $\rho$ and $\omega$ phases are either relatively constant, or change in tandem over a fairly wide range of photon energy. Other experiments have studied $\rho^{0}-\omega$ interference using photoproduction to the $e^{+} e^{-}$ final state (where the $\omega$ is more visible but the branching ratios

TABLE III. Photon energy (laboratory frame) and $\gamma N$ center-ofmass energy for different rapidities. There are two rows per rapidity: one for the higher energy photon solution, and one for the lower one.

| Rapidity | Photon energy <br> (laboratory frame) <br> $(\mathrm{MeV})$ | $\gamma N$ center-of-mass energy <br> $(\mathrm{GeV})$ |
| :--- | :---: | :---: |
| 0 | 380 | 12.4 |
| 0.15 | 327 | 11.5 |
|  | 441 | 13.4 |
| 0.4 | 255 | 10.2 |
|  | 488 | 14.1 |
| 0.63 | 202 | 9.1 |
|  | 713 | 17.0 |

are much smaller), or via the reaction $e^{+} e^{-} \rightarrow \pi^{+} \pi^{-}$, and found similar phase angles [33,34].

An alternate fit was performed, where $B_{\pi \pi}$ was multiplied by a mass-dependent term, $\left(M_{\rho} / M_{\pi \pi}\right)^{2}\left[\left(M_{\pi \pi}^{2} / 4-\right.\right.$ $\left.\left.m_{\pi}^{2}\right) /\left(M_{\rho}^{2} / 4-m_{\pi}^{2}\right)\right]^{3 / 4}[35]$ to account for the possibility that the continuum $\pi \pi$ pairs do not completely interfere with the $\rho^{0}$ or $\omega$. This fit produced similar results, with a comparable $\chi^{2} /$ DOF .

To study the photon energy dependence of the amplitude ratios, we performed the fit in five bins of rapidity: $y<-0.35$, $-0.35<y<-0.15,-0.15<y<0.15,0.15<y<0.35$, and $y>0.35$. These bins were chosen so that each of the three $|y|$ ranges included about 100000 pion pairs. The amplitudes should be symmetric around $y=0$; pairing by $|y|$ provides a check on rapidity-dependent systematic errors. To ensure the fits were stable, the values of $M_{\omega}$ and $\Gamma_{\omega}$ were fixed to the values extracted from the fit to the rapidity-integrated pion-pair mass distribution.

In the laboratory frame, at low $p_{T}$, the rapidity is related to photon energy $k$ by

$$
\begin{equation*}
k=M_{\pi \pi} / 2 \exp ( \pm y) \tag{6}
\end{equation*}
$$

The $\pm$ sign reflects the twofold ambiguity as to which nucleus emitted the photon. Table III gives the laboratory-frame photon energies and the $\gamma N$ center-of-mass energies for the two solutions to Eq. (6) for the centers of the rapidity bins when $M_{\pi \pi}=M_{\rho}$. The photon flux drops rapidly with increasing energy, so away from $y=0$, the cross section is dominated by the lower photon energy; the relative fractions scale roughly as the ratio of the laboratory-frame photon energies.

Figure 5 shows the direct $\pi^{+} \pi^{-}$to $\rho^{0}(|B / A|)$ and $\omega$ to $\rho^{0}$ $(C / A)$ ratios in the five rapidity bins. Both $|B / A|$ and $C / A$ are unchanged as rapidity varies, showing that these ratios do not have a large dependence on the photon energy. Also shown are the STARlight predictions and, for $C / A$, the DESY-MIT result. The DESY-MIT result is at a much lower beam energy, which would correspond to an effective rapidity of -2.5 with the lower photon energy solution of Eq. (6).

To determine the $\rho^{0}$ cross section as a function of rapidity, we integrate the $\rho^{0}$ Breit-Wigner function over the mass range from $2 M_{\pi}$ to $M_{\rho}+5 \Gamma_{\rho}$.



FIG. 5. (top) The ratio $|B / A|$ of amplitudes of nonresonant $\pi^{+} \pi^{-}$ and $\rho^{0}$ mesons. The black points (with shaded blue systematic error band) are from the current analysis, while the previous STAR results are shown with open blue squares. The red line shows the rapidityaveraged result. In the bottom panel, the black points show the ratio $|C / A|$ of the $\omega$-to- $\rho^{0}$ amplitude. The red band shows the systematic errors, while the horizontal blue line shows the STARlight prediction with the most recent branching ratio for $\omega \rightarrow \pi^{+} \pi^{-}$decay [32]. The green dashed band shows the DESY-MIT result for $|C / A|[29]$. Their result was at much lower photon energies, equivalent to a large effective rapidity. For the lower energy photon solution of the twofold ambiguity, the effective rapidity is about -2.5 .

Figure 6 shows the acceptance-corrected $d \sigma / d y$ for $\rho^{0}$. The asymmetry between positive and negative rapidity gives a measure of the rapidity-dependent systematic uncertainties in the cross section. This is likely due to asymmetries in the as-built longitudinal position of the TOF counters. The magnitude of this uncertainty grows slowly with increasing rapidity, reaching $4 \%$ at $y=0.7$. Since the actual lengths of the TOF slats are known, this uncertainty does not apply to rapidity-integrated measurements.

The systematic uncertainties in these measurements fall into two classes, either an overall scale for the cross section, or uncertainties that vary point to point. The former is usually dominant.

The uncertainty in the integrated luminosity is $10 \%$. As with previous measurements [7], this uncertainty is mainly driven by the fraction of the total $\mathrm{Au}+\mathrm{Au}$ cross section accessible with the trigger used to collect this data. The


FIG. 6. $d \sigma / d y$ for exclusively photoproduced $\rho^{0}$ mesons in (top) $X n X n$ events and (bottom) $1 n 1 n$ events. The data are shown with red markers. The statistical errors are smaller than the symbols, the orange band shows the quadrature sum of the point-to-point systematic uncertainties. The red boxes at $y \approx-0.9$ show the quadrature sum of the common systematic uncertainties. The black histograms are the STARlight calculation for $\rho^{0}$ mesons with mutual dissociation. The blue markers in the top panel show the previous STAR measurement [7].
selection of the number of neutrons produced in mutual electromagnetic dissociation depends on the response of the ZDC calorimeters. We allocate a $5 \%$ uncertainty to this neutron counting due to small nonlinearities in the calorimeters and overlaps between one and many neutron distributions. We assign a $7 \%$ uncertainty due to modeling of the TOF system in the simulation, based on studies of the TOF response in more central collisions. The uncertainty in the track reconstruction efficiency for the STAR TPC is 3\% per track [19] ( $6 \%$ for two tracks), while the efficiency of the vertex finder is known within a $5 \%$ uncertainty, driven by the effect of backgrounds. The uncertainty in how often the BBC detectors will veto good UPC events is due to fluctuating backgrounds. Even with use of embedding techniques, we estimate that these veto conditions introduce a $2 \%$ uncertainty to the results.

The same-sign pion-pair distributions are the best estimators for the hadronic backgrounds for these two-track events. The background subtraction was done at the level of raw histograms and also after a fit to the background to eliminate statistical fluctuations. These two procedures lead to final results that agree within $1.5 \%$.

The scaling from the rapidity distribution extracted from $1 n 1 n$ events to the previously measured $X n X n$ distribution uses a correction extracted from the event generator STARlight. There is a $6 \% \mathrm{XnXn}$ cross-section uncertainty from the uncertainty in the neutron data used as input to STARlight. This uncertainty is squared because we detect neutrons in both beams but applies only to the $X n X n$ results.

Table IV summarizes these common systematic uncertainties. They are summed in quadrature to find the $18.2 \%$ overall common uncertainty. This uncertainty is a bit higher than in our comparable previous publication [7], largely because of additional uncertainties associated with the pileup and the more complex trigger that is required to deal with the higher luminosities.

The main point-to-point systematic uncertainties in the rapidity and $p_{T}$ distributions come from the track selection and particle identification. The systematic uncertainties were evaluated by varying the track quality cuts and PID cuts around their central value in both the data and simulation and seeing

TABLE IV. The common systematic uncertainties present in the rapidity distribution in Fig. 6 and the $-t$ distributions in Figs. 7 and 8. These uncertainties are given as a percentage of the measured quantities.

| Name | Value | Comment |
| :--- | :---: | :---: |
| Luminosity | $10.0 \%$ |  |
| ZDC | $5.0 \%$ | ADC ch. to num. neutrons |
| TOF geometry modeling | $7.0 \%$ |  |
| TPC tracking efficiency | $6.0 \%$ | $3.0 \%$ per track [19] |
| Vertex finder efficiency | $5.0 \%$ | Background driven |
| BBC veto in trigger | $2.0 \%$ | Background driven |
| Efficiency determination | $7.0 \%$ |  |
| Conversion from $\pi^{+} \pi^{-}$pairs to $\rho^{0}$ yield | $2.2 \%$ | Varying mass fit range |
| Background subtraction | $1.5 \%$ |  |
| STARlight model | $6.0 \%$ | only for $X n X n$ results |
| Quadrature sum | $18.2 \%$ |  |

TABLE V. Point-to-point systematic uncertainties on $d \sigma / d y$ (Fig. 6) as a percentage of the measured cross section in four rapidity ranges. PID cut refers to uncertainty in the efficiency for $\pi$ identification via the truncated $d E / d x$ [36]. Those cuts were varied simultaneously in the data and simulation to determine the uncertainty in particle identification efficiency. The fit to efficiency is the uncertainty in the efficiency parametrization, while the number of track hits is the minimum number of points used for fitting the track. The TOF asymmetry is the uncertainty due to the positions of the TOF slats.

| Rapidity | PID <br> cut | Fit to <br> eff. | Number of <br> track hits | TOF <br> asymmetry |
| :--- | :---: | :---: | :---: | :---: |
| $-0.7-0.5$ | $8 . \%$ | $0.25 \%$ | $0.2 \%$ | $5 \%$ |
| $-0.5-0.0$ | $5 . \%$ | $0.25 \%$ | $0.05 \%$ | $3.6 \%$ |
| $0.0-0.5$ | $5 . \%$ | $0.25 \%$ | $0.05 \%$ | $3.6 \%$ |
| $0.5-0.7$ | $8 . \%$ | $0.25 \%$ | $0.2 \%$ | $5 \%$ |

how the final result varies. Table V lists the point-to-point uncertainties in the rapidity distribution while Table VI lists the point-to-point uncertainties for the $p_{T}$ distribution.

The ALICE collaboration has studied dipion photoproduction, in lead-lead collisions at the LHC [8]. They fit their dipion mass distribution in the range from 0.6 to $1.5 \mathrm{GeV} / c^{2}$ to a function like Eq. (2), but without the $\omega$ component, finding masses and widths consistent with the standard values. Their cross-section values were about $10 \%$ above the STARlight prediction.

## IV. MEASUREMENT OF $\boldsymbol{d} \sigma / \boldsymbol{d} \boldsymbol{t}$

Figure 7 shows the efficiency-corrected differential cross section $d \sigma / d t$ for $\rho^{0}$ mesons within the measured range $|y|<$ 1 , after like-sign background subtraction. The Mandelstam variable $t$ is expressed as $t=t_{\|}+t_{\perp}$ with $t_{\|}=-M_{\rho}^{2} /\left(\gamma^{2} e^{ \pm y}\right)$ and $t_{\perp}=-\left(p_{T}^{\text {pair }}\right)^{2}$. Here, $\gamma$ is the Lorentz boost of the ions. At RHIC energies, $t_{\|}$is almost negligible. The cross section $d \sigma / d t$ for $\rho^{0}$ mesons is obtained by scaling the total dipion cross section by a factor of 0.75 . This factor was extracted from comparisons between the number of pion pairs with invariant masses ranging from $500 \mathrm{MeV} / c^{2}$ to $1.5 \mathrm{GeV} / c^{2}$ and the integral of the $\rho^{0}$ Breit-Wigner function extracted from fits

TABLE VI. Point-to-point systematic uncertainties for the $-t$ distribution shown in Fig. 8, as a percentage of the measured cross section in three $-t$ ranges. The PID and track selection uncertainties are described in the text. The uncertainty in the incoherent component subtraction was estimated by selecting the largest relative deviation from the default value and cross sections extracted by changing the value of the fit parameters by one standard deviation while the other parameters remain at the default fit value.

| $-t\left[(\mathrm{GeV} / c)^{2}\right]$ | Track sel. | Pion PID | Incoher. subtr. |
| :--- | :---: | :---: | :---: |
| $0.00-0.02$ | $0.2 \%$ | $8 \%$ | $0.5 \%$ |
| $0.02-0.04$ | $0.2 \%$ | $8 \%$ | $3.0 \%$ |
| $0.04-0.10$ | $0.2 \%$ | $8 \%$ | $8.5 \%$ |



FIG. 7. The $-t$ distribution for exclusive $\rho^{0}$ mesons in events with $1 n 1 n$ mutual dissociation (open blue circles) and $X n X n$ (filled red circles). The statistical errors are smaller than the points, and the colored bands show the total systematic uncertainties. The dipole fits are shown by solid black lines. For $X n X n$, the dipole form factors are shown extrapolated to low $|t|$ (dotted black line line), along with the STARlight prediction for the incoherent contribution (dashed blue line).
in rapidity and $-t$ bins. In all comparisons, the integrals are performed from $2 M_{\pi}$ to $M_{\rho}+5 \Gamma_{\rho}$.

We separate the $\rho^{0} t$ spectrum into coherent and incoherent components based on the shape of the distribution in Fig. 7. Because of the ZDC requirement in the trigger, and the presence of Coulomb excitation, we cannot use the presence of neutrons from nuclear breakup as an event-by-event signature of incoherence [37].

The incoherent components for the $1 n 1 n$ and $X n X n$ distributions are fit with a dipole form factor:

$$
\begin{equation*}
\frac{d \sigma}{d t}=\frac{A / Q_{0}^{2}}{\left(1+|t| / Q_{0}^{2}\right)^{2}} \tag{7}
\end{equation*}
$$

which has been used to describe low- $Q^{2}$ photon-nucleon interactions [38]. The fit is done in the range from $-t=$ $0.2(\mathrm{GeV} / c)^{2}$ (above the coherent production region) to $-t=0.45(\mathrm{GeV} / c)^{2}$. The upper limit for $-t$ is chosen to reduce the contamination from hadronic interactions. For the events with mutual dissociation into any number of neutrons ( $X n X n$ ), the fit finds $A=3.46 \pm 0.02 \mathrm{mb}$ and $Q_{0}^{2}=$ $0.099 \pm 0.015(\mathrm{GeV} / c)^{2}$, with $\chi^{2} / \mathrm{NDF}=19 / 9$. For events with mutual dissociation into single neutrons $(1 n 1 n), Q_{0}^{2}$ is fixed at $0.099 \mathrm{GeV} / c^{2}$. The fit finds $A=0.191 \pm 0.003 \mathrm{mb}$, with $\chi^{2} / \mathrm{NDF}=15.8 / 10$. The integrals of these fits lead to the incoherent cross sections shown in Table VII. The coherent component of the $t$ distribution is then extracted by subtracting the incoherent-component fit from the total $d \sigma / d t$.

TABLE VII. The coherent and incoherent cross sections for $\rho^{0}$ photoproduction within $|y|<1$ with $X n X n$ and $1 n 1 n$ mutual excitation, and their ratios.

| Parameter | XnXn | $1 n 1 n$ |
| :--- | :---: | :---: |
| $\sigma_{\text {coh. }}$ | $6.49 \pm 0.01$ (stat.) $\pm 1.18$ (syst.) mb | $0.770 \pm 0.004$ (stat.) $\pm 0.140$ (syst.) mb |
| $\sigma_{\text {incoh. }}$ | $2.89 \pm 0.02$ (stat.) $\pm 0.54$ (syst.) mb | $0.162 \pm 0.010$ (stat.) $\pm 0.029$ (syst.) mb |
| $\sigma_{\text {incoh. } . ~}^{\text {coh. }}$ | $0.445 \pm 0.015$ (stat.) $\pm 0.005$ (syst.) | $0.233 \pm 0.007$ (stat.) $\pm 0.007$ (syst.) |

If the nuclear excitation was completely independent of $\rho$ photoproduction, then the cross-section ratio for incoherent to coherent production should not depend on the type of nuclear excitation studied. It is not; the difference could signal the breakdown of factorization, for a couple of reasons. One possibility is that unitarity corrections play a role by changing the impact parameter distributions for $1 n 1 n$ and $X n X n$ interactions. When $b \gtrsim 2 R_{A}$, the cost of introducing another low-energy photon into the reaction is small. So one photon can excite a nucleus to a GDR, while a second photon can further excite the nucleus, leading to $X n$ emission rather than $1 n$ [18]. The additional photon alters the impact parameter distributions for the $1 n 1 n$ and $X n X n$ channels. The $X n X n$ channel will experience a slightly larger reduction at small $|t|$ due to interference from the two production sites. This may slightly alter the measured slopes and coherent-to-incoherent ratios. Alternately, at large $|t|$, a single photon can both produce a $\rho^{0}$ and leave the target nucleus excited, breaking the assumed factorization paradigm. The rate has not been calculated for $\rho^{0}$, but the cross section for $J / \psi$ photoproduction accompanied by neutron emission is significant [39]. This calculated $J / \psi$ cross section is noticeably less for single neutron emission than for multineutron emission, so $\rho^{0}$ photoproduction accompanied by neutron emission might alter the $X n X n$ incoherent-tocoherent cross-section ratio more than that of $1 n 1 n$. The difference between the ratios for $1 n 1 n$ and $X n X n$ collisions is somewhat larger than was found in a previous STAR analysis [7].

The $d \sigma / d t$ for coherent $\rho^{0}$ photoproduction accompanied with mutual dissociation of the nuclei into any number of neutrons ( $X n X n$ ) and only one neutron ( $1 n 1 n$ ) is shown in Fig. 8 with red and blue markers, respectively. In both $1 n 1 n$ and $X n X n$ events, two well-defined minima can clearly be seen. In both spectra, the first minima are at $-t=0.018 \pm 0.005(\mathrm{GeV} / c)^{2}$. Second minima are visible at $0.043 \pm 0.01(\mathrm{GeV} / c)^{2}$. To first order, the gold nuclei appear to be acting like black disks, with similar behavior for $1 n 1 n$ and $X n X n$ interactions.

A similar first minimum may be visible in ALICE data for lead-lead collisions. Figure 3 of Ref. [8] shows an apparent dip in $d N / d p_{T}$ for $\rho^{0}$ photoproduction, around $p_{T}=0.12 \mathrm{GeV} / c$ $\left[-t=0.014(\mathrm{GeV} / c)^{2}\right]$. Lead nuclei are slightly larger than gold nuclei, so the dip should be at smaller $|t|$.

These minima are shallower than would be expected for $\gamma-A$ scattering, because the photon $p_{T}$ partly fills in the dips in the $\gamma-A p_{T}$ spectrum. There are several theoretical predictions for the locations and depths of these dips. A classical Glauber calculation found the correct depths, but slightly different locations [40]. A quantum Glauber calculation did a better job of predicting the locations of the first minimum [10], although that calculation did not include the photon $p_{T}$, so
missed the depth of the minimum. However, quantum Glauber calculations which included nuclear shadowing predict that, because of the emphasis on peripheral interactions, the nuclei should be larger, so the diffractive minima are shifted to lower $|t|$ [41]. For $\rho$ photoproduction with lead at LHC energies, this calculation predicted that the first minima should be at about $0.0165(\mathrm{GeV} / c)^{2}$ without the shadowing correction, and $0.012(\mathrm{GeV} / c)^{2}$ with the correction. These values are almost independent of collision energy but depend on the nuclear radii. Scaling by the ratio of the squares of the nuclear radii, 1.078 , the predictions are about $0.0177(\mathrm{GeV} / c)^{2}$ without the shadowing correction, and $0.0130(\mathrm{GeV} / c)^{2}$ with the shadowing. The data are in better agreement with the prediction that does not include the shadowing correction.

The Sartre event generator run in UPC mode at RHIC energies [42] produces a Au nucleus recoil after $\rho^{0}$ elastic scattering with a very good agreement with the $\rho^{0} t$ distribution presented here. That is not surprising, since it includes


FIG. 8. $d \sigma / d t$ for coherent $\rho^{0}$ photoproduction in $X n X n$ events (filled red circles) and $1 n 1 n$ events (open blue circles). The filled bands show the sum in quadrature of all systematic uncertainties listed in Table V and the statistical errors, which are shown as vertical lines. The red and blue lines show an exponential fit at low $t$, as discussed in the text. The inset shows, with finer binning at low $p_{T}$, the effects of the destructive interference between photoproduction with the photon emitted by any of the two ions.
a physics model that is similar to the quantum Glauber calculation that does not include nuclear shadowing.

An exponential function is used to characterize the spectrum below the first peak $\left[0.0024<|t|<0.0098(\mathrm{GeV} /)^{2}\right)^{2}$. The measured slope is $426.4 \pm 1.8(\mathrm{GeV} / c)^{-2}$ for the XnXn events and $407.8 \pm 3.2(\mathrm{GeV} / c)^{-2}$ for the $1 n 1 n$ events. The $X n X n$ slope is very similar to the ALICE measurement of $426 \pm 6 \pm 15(\mathrm{GeV} / c)^{-2}$ [8]; there is no evidence for an increase in effective nuclear size with increasing photon energy.

At very small $-t,|t|<10^{-3}(\mathrm{GeV} / c)^{2}$, both cross sections flatten out and turn downward, as can be seen in the insert in Fig. 8. This is expected due to destructive interference between $\rho^{0}$ production on the two nuclear targets [40,43].

These results are subject to the common uncertainties from Table IV, in addition to the point-to-point uncertainties described above and listed in Table VI. The yellow and pink bands in Fig. 8 are the sum in quadrature of all systematic uncertainties and statistical errors.

The shape of $d \sigma / d t$ for coherent photoproduction is determined by the position of the interaction sites within the target. One can, in principle, determine the density distribution of the gold nucleus via a two-dimensional Fourier transform of $d \sigma / d t$. RHIC beam energies are high enough that, for $\rho^{0}$ photoproduction at midrapidity, the longitudinal density distribution may be neglected and the ions may be treated as discs. Nuclei are azimuthally symmetric, so the radial distribution can be determined with a Fourier-Bessel (Hankel) transformation:

$$
\begin{equation*}
F(b) \propto \frac{1}{2 \pi} \int_{0}^{\infty} d p_{T} p_{T} J_{0}\left(b p_{T}\right) \sqrt{\frac{d \sigma}{d t}} . \tag{8}
\end{equation*}
$$

Figure 9 shows the result of this transform in the region $|t|<0.06(\mathrm{GeV} / c)^{2}$. Several features are visible. The tails of $F(b)$ are negative around $|b|=10 \mathrm{fm}$. This may be due to interference between the two nuclei, since the drop in $d \sigma / d t$ for $|t|<0.0002(\mathrm{GeV} / c)^{2}$ is due to what is effectively a negative amplitude for photoproduction on the "other" nucleus [43].

We varied the maximum $|t|$ used for the transform over the range 0.05 to $0.09(\mathrm{GeV} / c)^{2}$. This led to substantial variation at small $b$, shown by the cyan region in Fig. 9. The origin of this variation is not completely clear, but it may be related to aliasing due to the lack of a windowing function [44], or because of the limited statistics at large $|t|$. There is much less variation at the edges of the distribution, showing that the transform is stable in the region $4<b<7 \mathrm{fm}$. The full-width half-maximum (FWHM) of the distribution is 2(6.17 $\pm 0.12$ ) fm . This FWHM is a measure of the hadronic size of the gold nucleus. With theoretical input, it could be compared with the electromagnetic (proton) radius of gold, as determined by electromagnetic scattering. The difference would be a measure of the neutron skin thickness of gold, something that is the subject of considerable experimental interest [45,46].

There are a few effects that need to be considered in comparing the distribution in Fig. 9 with nuclear data. Because of the significant $q \bar{q}$ dipole size, $\rho^{0}$ production occurs preferentially on the front side of the nucleus, and the contribution of the central region is reduced. Since the photons come from the fields of the other nucleus, the photon field is not uniform across the target; it is stronger on the "near" side.


FIG. 9. The target distribution in the transverse plane, the result of a two-dimensional Fourier transform (Hankel transform) of the $X n X n$ and $1 n 1 n$ diffraction patterns shown in Fig. 8. The integration is limited to the region $|t|<0.06(\mathrm{GeV} / c)^{2}$. The uncertainty is estimated by changing the maximum $-t$ to $0.05,0.07$, and 0.09 $(\mathrm{GeV} / c)^{2}$. The cyan band shows the region encompassed by these $-t$ values. To highlight the similarity of both results at their falling edges, the resulting histograms are scaled by their integrals from -12 to 12 fm . The FWHM of both transforms is $2(6.17 \pm 0.12) \mathrm{fm}$, consistent with the coherent diffraction of $\rho^{0}$ mesons off an object as big as the Au nuclei.

Finally, the interference between production on the two targets alters the distributions at large $|b|$.

## V. SUMMARY AND CONCLUSIONS

STAR has made a high-statistics study of $\rho^{0}, \omega$, and direct $\pi^{+} \pi^{-}$photoproduction in $200 \mathrm{GeV} /$ nucleon-pair gold-ongold ultraperipheral collisions, using $384000 \pi^{+} \pi^{-}$pairs.

We fit the invariant-mass spectrum to a mixture of $\rho^{0}$, $\omega$, direct $\pi^{+} \pi^{-}$, and interference terms. The ratio of direct $\pi^{+} \pi^{-}$to $\rho^{0}$ is similar to that in previous measurements, while the newly measured $\omega$ contribution is comparable with predictions based on the previously measured $\gamma p \rightarrow \omega p$ cross section and the $\omega \rightarrow \pi^{+} \pi^{-}$branching ratio. The relative fractions of $\rho^{0}, \omega$, and direct $\pi^{+} \pi^{-}$do not vary significantly with rapidity, indicating that they all have a similar dependence on photon energy.

We also measure the cross section $d \sigma / d t$ over a wide range and separate out coherent and incoherent components. The coherent contribution exhibits multiple diffractive minima, indicating that the nucleus is beginning to act like a black disk.

This measurement provides a nice lead-in to future studies of photo- and electroproduction at an electron-ion collider (EIC) [47], where nuclei may be probed with photons at a wide range of $Q^{2}$ [48].

## ACKNOWLEDGMENTS

We thank the RHIC Operations Group and RCF at BNL, the NERSC Center at LBNL, and the Open Science Grid
consortium for providing resources and support. This work was supported in part by the Office of Nuclear Physics within the U.S. DOE Office of Science, the U.S. National Science Foundation, the Ministry of Education and Science of the Russian Federation, National Natural Science Foundation of China, Chinese Academy of Science, the Ministry of Science and Technology of China and the Chinese Ministry of Education, the National Research Foundation of Korea, GA
and MSMT of the Czech Republic, Department of Atomic Energy and Department of Science and Technology of the Government of India; the National Science Centre of Poland, National Research Foundation of Croatia, the Ministry of Science, Education and Sports of the Republic of Croatia, RosAtom of Russia and German Bundesministerium fur Bildung, Wissenschaft, Forschung and Technologie (BMBF), and the Helmholtz Association.
[1] G. Baur, K. Hencken, D. Trautmann, S. Sadovsky, and Y. Kharlov, Phys. Rep. 364, 359 (2002).
[2] C. A. Bertulani, S. R. Klein, and J. Nystrand, Annu. Rev. Nucl. Part. Sci. 55, 271 (2005).
[3] J. Bartels, K. J. Golec-Biernat, and H. Kowalski, Phys. Rev. D 66, 014001 (2002).
[4] S. R. Klein and J. Nystrand, Phys. Rev. C 60, 014903 (1999).
[5] G. Agakishiev et al. (STAR Collaboration), Phys. Rev. C 85, 014910 (2012).
[6] C. Adler et al. (STAR Collaboration), Phys. Rev. Lett. 89, 272302 (2002).
[7] B. I. Abelev et al. (STAR Collaboration), Phys. Rev. C 77, 034910 (2008).
[8] J. Adam et al. (ALICE Collaboration), J. High Energy Phys. 1509 (2015) 095.
[9] L. Frankfurt, M. Strikman, and M. Zhalov, Phys. Rev. C 67, 034901 (2003).
[10] L. Frankfurt, V. Guzey, M. Strikman, and M. Zhalov, Phys. Lett. B 752, 51 (2016).
[11] V. P. Goncalves and M. V. T. Machado, Phys. Rev. C 80, 054901 (2009).
[12] G. Sampaio dos Santos and M. V. T. Machado, Phys. Rev. C 91, 025203 (2015).
[13] M. Klusek-Gawenda and A. Szczurek, Phys. Rev. C 87, 054908 (2013).
[14] J. A. Crittenden, Exclusive Production of Neutral Vector Mesons at the Electron-Proton Collider HERA, Springer Tracts in Modern Physics (Springer, Berlin, Heidelberg, 1997), Vol. 140.
[15] B. L. Berman and S. C. Fultz, Rev. Mod. Phys. 47, 713 (1975).
[16] G. Baur, K. Hencken, A. Aste, D. Trautmann, and S. R. Klein, Nucl. Phys. A 729, 787 (2003).
[17] A. J. Baltz, S. R. Klein, and J. Nystrand, Phys. Rev. Lett. 89, 012301 (2002).
[18] A. J. Baltz, M. J. Rhoades-Brown, and J. Weneser, Phys. Rev. E 54, 4233 (1996).
[19] M. Anderson et al., Nucl. Instrum. Methods Phys. Res., Sect. A 499, 659 (2003).
[20] W. J. Llope, Nucl. Instrum. Methods Phys. Res., Sect. B 241, 306 (2005).
[21] J. Kiryluk (STAR Collaboration), hep-ex/0501072.
[22] C. Adler, A. Denisov, E. Garcia, M. Murray, H. Strobele, and S. White, Nucl. Instrum. Methods Phys. Res., Sect. A 499, 433 (2003).
[23] F. S. Bieser et al., Nucl. Instrum. Methods Phys. Res., Sect. A 499, 766 (2003).
[24] S. R. Klein, J. Nystrand, J. Seger, Y. Gorbunov, and J. Butterworth, Comput. Phys. Commun. 212, 258 (2017).
[25] R. Brun, F. Bruyant, F. Carminati, S. Giani, M. Maire, A. McPherson, G. Patrick, and L. Urban, CERN-W5013 (1994).
[26] I. A. Pshenichnov, J. P. Bondorf, I. N. Mishustin, A. Ventura, and S. Masetti, Phys. Rev. C 64, 024903 (2001).
[27] M. Klusek-Gawenda, M. Ciemala, W. Schafer, and A. Szczurek, Phys. Rev. C 89, 054907 (2014).
[28] P. Söding, Phys. Lett. 19, 702 (1966).
[29] H. Alvensleben et al., Phys. Rev. Lett. 27, 888 (1971).
[30] E. A. Kuraev and Z. K. Silagadze, Yad. Fiz. 58, 1843 (1995) [Phys. Atom. Nucl. 58, 1741 (1995)].
[31] R. R. Akhmetshin et al. (CMD-2 Collaboration), Phys. Lett. B 476, 33 (2000).
[32] K. A. Olive et al. (Particle Data Group Collaboration), Chin. Phys. C 38, 090001 (2014).
[33] J. L. Lemke and R. G. Sachs, Phys. Rev. D 5, 590 (1972).
[34] P. Langacker, Phys. Rev. D 20, 2983 (1979).
[35] J. Pumplin, Phys. Rev. D 2, 1859 (1970).
[36] Y. Xu et al., Nucl. Instrum. Methods Phys. Res., Sect. A 614, 28 (2010).
[37] V. Rebyakova, M. Strikman, and M. Zhalov, Phys. Lett. B 710, 647 (2012).
[38] M. Drees and D. Zeppenfeld, Phys. Rev. D 39, 2536 (1989).
[39] M. Strikman, M. Tverskoy, and M. Zhalov, Phys. Lett. B 626, 72 (2005).
[40] S. R. Klein and J. Nystrand, Phys. Rev. Lett. 84, 2330 (2000).
[41] V. Guzey, M. Strikman, and M. Zhalov, Phys. Rev. C 95, 025204 (2017).
[42] T. Toll and T. Ullrich, Comput. Phys. Commun. 185, 1835 (2014).
[43] B. I. Abelev et al. (STAR Collaboration), Phys. Rev. Lett. 102, 112301 (2009).
[44] https://en.wikipedia.org/wiki/Window_function (Dec., 2016).
[45] C. M. Tarbert et al., Phys. Rev. Lett. 112, 242502 (2014).
[46] A. Gardestig, C. J. Horowitz, and G. A. Miller, arXiv:1504.08347.
[47] A. Accardi et al., Eur. Phys. J. A 52, 268 (2016).
[48] T. Toll and T. Ullrich, Phys. Rev. C 87, 024913 (2013).

