Closed-loop Temperature Control of Friction Stir Welding

by

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R. P. Pothier

Date: 9 January 2015

Abstract

This study develops and presents a friction stir weld (FSW) quality assurance tool based on control of weld zone temperature. Apart from correct tool geometry, tool tilt angle, traverse speed and forge force during welding, one important requirement is that the weld material be sufficiently plasticised (softened). The level of plasticisation is related to weld zone temperature which is primarily dependent on spindle speed, traverse speed and forge force. When all other conditions are correct, sufficiently plasticised material flows around and consolidates behind the tool without the production of voids in the weld. Typically, weld temperature varies along the weld length which may result in variations in weld quality. Weld zone temperature control makes constant weld zone temperature possible. In this study, thermocouple sensors were embedded in the FSW tool and a weld zone temperature control algorithm was developed. Spindle speed was the actuating mechanism for controlling weld temperature. The system was modelled and controllers were designed using Matlab tools. The system was simulated and the performance was compared to the system The control system ensures that the weld zone performance during welding. temperature can be maintained irrespective of the presence of thermal disturbances. Tensile testing was conducted which confirmed a range of temperature in which the welds resulted in consistent strength.

Keywords: Friction Stir Welding (FSW); Closed-loop; Temperature Control; System modelling; Controller design; Controller tuning; PID; Aluminium Alloy 6082

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Abbreviations

AA	Aluminium Alloy
ASTM	American Society for Testing and Materials
EDM	Electric Discharge Machine
FSW	Friction Stir Weld/Friction Stir Welding
HAZ	Heat affected Zone
HMI	Human Machine Interface
PDS	Process Development System
PID	Proportional Integral Derivative (controller)
PLC	Programmable Logic Controller
SID	System Identification (Tool)
TMAZ	Thermo-Mechanically Affected Zone
USB	Universal Serial Bus (connection)
UTS	Ultimate Tensile Strength

Glossary

Backing plate The plate which supports the weld material from the bottom. Bed In the context of this study, the machine's bed is the support area on which the weld is conducted. A critically damped system ($\zeta = 1$) achieves the set-point Critically damped in the shortest amount of time with zero overshoot of the set-point. Damping An effect on the system which limits the rate at which the controlled variable of the process can change. Damping ratio The ratio (ζ) of the amount of actual damping of the system to the amount of damping at the point of critical damping $\left(\frac{\text{damping}}{\text{critical damping}}\right)$. Dry ice Carbon dioxide in its solid form (at a temperature of approximately -78.5°C). Typically in the form of pellets which resemble ice. Dynamic recrystallisation Recrystallisation of the material's grain structure caused by the deformation of the material (not heat treatment). EtherCAT A computer communication network technology. Filter A filter attenuates certain undesired frequencies from a signal. In the case of this study, digital filters are utilised which take the form of mathematical calculations executed by the machine controller.

- Force control A friction stir weld can be programmed to execute in force control mode in which case the forge force (vertical direction) is maintained at the operator set-point. The vertical position of the tool is allowed to vary according to mechanical influences such as machine bed deflection.
- Forge force The downward force applied by the machine which is supported mainly by the tool shoulder. The force consolidates the material exiting from the rear of the tool.
- Fuzzy logic A control strategy based on rules applied to feedback signals. The importance of the rules (or action taken on a specific feedback signal) can be set using weighted coefficients.
- Genetic algorithm A genetic algorithm is given an objective. In control systems the algorithm modifies the input to the system (actuator(s)), measures the output and continually modifies controller gains in the direction of achieving the objective. The algorithm effectively learns the process which it is controlling.
- Linearity A control system is considered linear if a change in the input variable (actuator(s)) has the same effect on the output variable when the system is at any point in the operating range of the system output.
- Load cell A force sensor or transducer.

- Natural frequency A system will tend to oscillate at its natural frequency if a driving force on the system precisely cancels out any damping force on the system.
- Negative damping A negatively damped system ($\zeta < 0$) will begin to oscillate with growing amplitude (caused by the driving force of the system) which increases indefinitely. The system is considered unstable.
- Over aging As the material age hardens, its strength increases to a peak. Aging of the material beyond this point is considered over aging in this study. The process of over aging requires a large amount of time at room temperature. It is possible to drastically accelerate the process by artificially aging the material using heat. This is what occurs in the heat affected zone of the weld for the material used in this study.
- Over damped An over damped control system ($\zeta > 1$) does not overshoot the set-point although the rise time is larger than for a critically damped system.
- Over plunge In the context of this study, over plunging is when the FSW weld material is unable to support the forge force (the temperature of the material or the forge force is too high) and the tool collides with the backing plate.
- Parent material The portion of the weld plate which is unaffected by the heat of the weld and is considered to have approximately

identical mechanical properties after welding as before welding.

- Percentage overshoot As a control system is driven towards the set-point, it often overshoots the set-point value. The amount by which the control system overshoots the set-point as a percentage of the step command size is the percentage overshoot.
- Tilt angle During a FSW, the tool is tilted from the vertical by a few degrees such that the majority of the forge force is applied at the rear of the tool in order to consolidate the material exiting from underneath the rear of the tool shoulder.
- Plunge The plunge stage is at the beginning of the weld. The rotating welding tool is forced downward into the weld material.

Plunge depth The distance from the surface of the weld material to the tip of the tool pin.

- Position control The weld tool position is maintained at the operator set plunge depth. The forge force during the weld is allowed to varying according to influences such as deflection of the machine bed.
- Quality The tensile strength of the weld is a representation of the weld quality in this study.

Ramp up	The initial stage during the weld after the plunge stage is
	complete, in which the weld slowly accelerates up to
	welding speed. The weld is in position control mode in
	this stage prior to the weld going into force control mode
	if the weld is programmed to be a force control weld. For
	this study the ramp up stage is 20 mm in length.

- Rise time The time taken for the control system to drive the output variable from 10% to 90% of the size of the step command applied to the set-point.
- Run-on tab A sacrificial plate placed at the beginning of the weld on which the plunge and ramp up stage can occur before the weld travels onto the weldment. The run-on tab allows for the FSW to be conducted for the full length of the weldment because a FSW cannot be plunged on the edge of the weldment.
- Servo drive The controller which manages the spindle servo motor parameters such as torque and speed regulation according to the requirements received from the machine PLC via an EtherCAT connection. The servo drive also manages spindle motor power supply.
- Settling time The time required for a control system to stabilise to within 5% of the set-point (for the final occurrence) after a step command change is made to the set-point.
- Set-point The desired position of the output of the control system (temperature in the context of this study), programmed by the operator, which the control system strives to achieve.

- Spindle power The product of spindle torque and spindle angular velocity (units of W or kW). Spindle speed The rate at which the spindle rotates (units of rev/min in terms of spindle speed or rad/s in terms of angular velocity).
- Spindle torqueThe rotational force which the spindle applies to the FSWtool.
- Stable zone Theoretically, the stable zone is the area of the weld in which the weld zone temperature is approximately constant. The study shows that typically the temperature continues to rise from the beginning to end of the weld although the temperature rising rate is relatively small after the ramp up stage.
- Steady-state error When a control system is maintaining constant system output, the error between the system output value and the desired set-point is the steady-state error.
- Step command An instantaneous change in control system set-point, programmed by the operator.
- Transfer function A mathematical equation representing the dynamics of the control system. The transfer function of the process is considered a mathematical model of the system in the context of this study.

- Traverse speed The rate at which the weld is travelling along the weld path. Equivalently, traverse speed can be referred to as feed rate or travel speed in FSW studies.
- Ultimate tensile strength The maximum stress (after the yield point) which the tensile sample is able to withstand prior to fracture.
- Undamped An undamped system (damping ratio $\zeta = 0$) has insufficient damping to diminish oscillation amplitude of the output yet the output oscillation amplitude does not increase indefinitely (the system is on the border of stable/unstable).
- Underdamped An underdamped system $(0 < \zeta < 1)$ is stable and percentage overshoot ranges from high to low as ζ moves from zero towards unity. The rise time is shorter than for a critically damped system although overshoot occurs.
- Welding tool The non-consumable tool which applies the frictional and stirring forces to the weld zone during the production of a FSW.

Weldment The work-piece which is welded or undergoing welding.

Weld nuggetThe portion of the weld zone through which the tool pin
traverses.

Weld setup The entire physical setup of backing plate, weld plate(s), welding tool, clamping mechanisms and the FSW welding machine.

Weld zone	The area of the weldment underneath the welding tool during the production of a FSW.
Wind-up	The integral term of the PID controller is a summation over time. Should the error between the set-point and the process feedback be of one sign for a specific amount of time, the integral term will wind-up for that amount of time.
Wind-up limit	In order to prevent excessive wind-up, a wind-up limit is often placed on the integral term.
x-force	The force applied by the x-axis hydraulic cylinder during the production of a FSW (in the welding direction in the context of this study).
y-force	The force applied by the y-axis hydraulic cylinder during the production of a FSW (transverse to the weld direction and is regulated in order to maintain y-axis position in the context of this study).
Yield strength	The stress at the point when the load on the sample causes it to begin plastic deformation.
z-force	The force applied by the z-axis hydraulic cylinder during the production of a FSW (see forge force).

Chapter 1

Introduction

Friction stir welding (FSW) is a solid-state joining process. During process execution, the temperature does not reach the solidus point (or the liquidus point) of the material. Frictional heat is generated between the non-consumable welding tool and the work-piece in order to heat the material to the point of plasticisation. The plasticised material is concurrently stirred and forged by the tool into a joint.

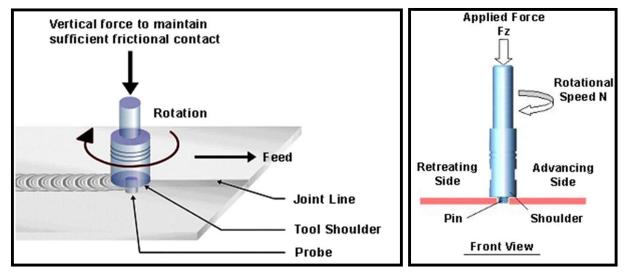


Figure 1.1. Friction stir weld process geometry ^[1]

The friction stir weld tool consists of a shoulder and a pin (see tool design in Section 3.2). The process begins by plunging the rotating tool into the material until the pin reaches the required plunge depth. This depth is usually as close to the backing plate surface as possible. At this point, the tool shoulder comes into contact with the surface of the material. The tool shoulder supports the majority of the forge force (labelled: "Vertical force/Applied force" in Figure 1.1). This force, together with the relative motion between the rotating tool and the weldment generates the frictional heat responsible for plasticising the material. As the material temperature rises, the material plasticises, reducing the spindle torque and hence the spindle power (for

constant spindle speed). The rising rate of the material temperature then decreases because of the reduction of energy input rate and increasing thermal diffusion into the surrounding material. The process stabilises at a specific temperature range. The FSW process is self-regulating in this sense. The weld temperature is typically not constant for the duration of the weld. FSW is an asymmetric process because the rotation of the tool causes the material on one side of the pin to move in the same direction as the welding direction (advancing side) while the material on the opposing side moves in the opposite direction to the welding direction (retreating side).

In order to produce a good quality FSW, which has consistent mechanical properties for the entire length of the weld, certain process conditions need to exist during the execution of the weld. Most of these conditions, such as spindle speed, weld traverse speed, forge force and tool tilt angle can be selected by the operator. During the weld, the machine controls these parameters in order to maintain their values according to the operator's weld program. The temperature of the material in the weld zone is dependent on these parameters as well as process conditions occurring during welding which are specific to the weld setup. The weld temperature is seldom constant because of changes in the amount of heat dissipated from the weld zone at different positions along the weld path. At a specific temperature or temperature range, the material in the weld zone will be optimally plasticised for the process to occur successfully and produce a good quality weld joint. This temperature is referred to as the optimal plasticisation temperature (OPT) in this study. Since the temperature of a typical FSW varies along the weld length, the material in the weld zone is not guaranteed to be at the OPT.

In this study, a temperature control algorithm was developed which was able to control weld zone temperature at various operator set-points. The control system alters spindle speed in order to control the weld zone temperature (which needed to be realistic for the specific weld setup). This control system created the possibility for the operator to conduct a weld with constant weld zone temperature. Selecting the

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weld temperature set-point as the OPT (for the particular weld setup) was therefore made possible.

The control system was developed on aluminium alloy 6082-T6 in this study. The system needed to be able to measure the weld zone temperature in the range of room temperature to approximately the material liquidus temperature (as safe limits). This generated the feedback signal for the control system.

The project produced an integrated temperature control system on an operational friction stir welding platform. The controller performance was tested and compared to the performance of various computer generated controllers in a simulated model.

The controller disturbance rejection was also tested by introducing a heat sink disturbance and then a heat source disturbance. Welds were conducted at constant temperature through the disturbance area. Tensile tests were done to investigate the weld quality consistency of these welds.

1.1. Aim

Develop a closed-loop temperature control system for friction stir welding which alters spindle speed in order to maintain the operator's set-point temperature for the plasticised material in the weld zone. The control system needs to exhibit good disturbance rejection.

Chapter 1 Introduction

1.2. Objective

Develop a prototype temperature control system for friction stir welding which will assist with quality control during welding. Determine the contribution of constant weld temperature to joint quality consistency along the weld length.

1.3. Significance of Research

This study provides industry (as well as eNtsa) with a tool to control the temperature of a FSW. The temperature of the weld can be maintained within a specific range (determined by the response capability of the system) of a specific set-point. Constant weld temperature could improve the consistency of the weld quality along the weld length because the material is maintained at a reasonably consistent plasticised state (optimal or not for the material being processed). Preferably, the operator would then select the OPT for the weld material and the weldment would contain the qualities of optimised strength and consistency along the weld length. The system provides the FSW industry with a tool which assists in the production of consistent quality welds.

1.4. Problem Statement

1.4.1. Temperature Fluctuation

The temperature of a FSW fluctuates as the weld progresses due to various influences which change the heat dissipation from the weld. For the weld setup used in this study, it was found that the weld temperature would continue to rise as the weld progresses; if the temperature control algorithm was not engaged. Temperature variation could affect weld quality if the material is not maintained at the OPT.

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1.4.2. Force and Position Control Effects

The vertical position (z-axis) of the FSW tool is typically controlled by either position control or force control. Either the z-position or the z-force is kept constant and the other varies as the weld progresses. Force control was the strategy used in the experiments conducted in this study. Typically the weld traverse speed and spindle speed are selected and are maintained constant throughout the duration of the weld. Fluctuation of either of these parameters would cause a change in the frictional forces between the tool and the work-piece; causing the machine to alter its spindle torque and/or welding feed force (x-force in this study) in order to maintain constant spindle speed and traverse speed. This could cause a temperature fluctuation in the weld.

1.4.3. Heat Dissipation into the Surrounding Material

In the proximity of a point in the middle of the weldment, the plate material volume (heat sink) is higher than a position closer to the edges of the weldment. Theoretically, the temperature of the weld zone therefore decreases as the tool moves towards the centre of the weldment, and increases as the tool moves away from the centre of the weldment. If the weld is sufficiently long, there exists a stable zone starting from a certain position after the beginning of the weld length and ending at a certain position before the end of the weld length. In this zone, heat dissipation into the surrounding material can be considered approximately constant. Temperature change outside of the stable zone must be compensated for.

1.4.4. Work-piece Clamps

The clamps which hold the weldment to the bed of the machine are fabricated from steel. These clamps are therefore thermally conductive. Heat is dissipated from the weldment, through the clamps. Weld temperature therefore theoretically increases as the weld tool moves away from one clamp and decreases as it approaches the next clamp. This influence is small and could be considered negligible.

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Chapter 1 Introduction

1.5. Sensor Positioning

The sensors which measure the weld zone temperature need to be placed in the optimal position relative to the weld zone. The optimal position is a position anywhere on the tool, work-piece or backing plate which has the least thermal resistance between it and the hottest plasticised material in the weld zone. This position will be at a temperature which represents the temperature of the weld zone. The optimal position will allow a change in temperature to be detected with minimum delay after the moment in which the change occurred. This will allow the system to respond in the minimum amount of time to changes in weld zone temperature in order to achieve minimal temperature fluctuation.

1.6. Hypothesis

Closed-loop temperature control of a friction stir weld can be developed and implemented as a weld quality assurance tool. Upon successful implementation of a closed-loop temperature control system, online process control of weld quality is made possible which will aid in process efficiency regarding cost and quality.

1.7. Delimitations

- This study was intended to develop the temperature control system and show its contribution to weld strength consistency. Once the temperature of the FSW was controllable and the tensile tests were completed, the project was complete. The weld strength consistency was investigated in this study, although the optimisation of the weld quality regarding the influences made by weld zone temperature (determining the OPT of the material) was not within the scope of this study.
- The development of the system was conducted on AA 6082-T6. The reasons for this are that aluminium and the welding tool material (W302 tool steel) are

relatively inexpensive. In addition to this, FSW of aluminium does not require a shielding gas to protect the weld from the atmosphere (oxidation prevention) as would be the case for FSW of steel or titanium. This simplifies the weld setup. Both steel and titanium FSW would require FSW tools manufactured from a material which would not substantially degrade at the welding temperatures of steel or titanium (e.g. Tungsten Rhenium^[2] which is relatively expensive in comparison to tool steel used for welding aluminium).

- The welds conducted in the development process were bead on plate welds.
- A single tool design was used throughout the project. The hottest point in the weld zone was determined from literature and this position was used in the tool thermocouple pocket design.
- Weld length is 585 mm (maximum allowable x-axis stroke on the PDS FSW platform). This allows for investigation of temperature changes induced by spindle speed alterations in as much of the stable zone as possible. In addition to this, the Ziegler Nichols tuning method ^[3] requires that the tuner increase the controller proportional gain term until the system oscillates with constant amplitude. The tuner will therefore require maximum weld length and hence time for completing the task.
- The parameters selected as a starting point for welding aluminium alloy 6082-T6 are:
 - Traverse speed: 200 mm/min [4]
 - Spindle speed: 560 rpm ^[4]
 - Tilt angle: 1°^[4]
- The FSW temperature control system must have good disturbance rejection. Some examples of these disturbances include the heat conductivity between

the weldment and the clamps as well as changes in heat conductivity between the weldment and the backing plate. The significance of such influences is difficult to quantify. Thermal disturbances, including dry ice as well as heated steel blocks, were introduced to the system in order to test the temperature control algorithm's disturbance rejection. The control system is tuned in such a way that if the temperature of the weld zone were to change due to any influence, the system will make appropriate machine spindle speed adjustments to compensate. These adjustments are made according to the predicted manner in which the temperature of the material responds to changes in spindle speed.

- The greater the error between the temperature set-point and the actual process temperature, the more aggressive the changes in spindle speed are in order to compensate for the error. Proportional, Integral and Derivative (PID) control was implemented. Ziegler Nichols PID tuning method ^[3] was conducted in order to tune the control system. Performance of the control algorithm was then tested and compared to the performance of the simulated process model.
- The system components added to the FSW platform include:
 - A telemetry system which allows the sensors to be mounted on the rotating tool and the data transmitted wirelessly to the controller.
 - A tool containing embedded thermocouples.
 - The control algorithm was written and added to the machine control program which executes on the machine's programmable logic controller (PLC). The algorithm tasks include:
 - Acquire sensor data (feedback input)
 - Acquire operator set-point (operator input)
 - Perform necessary control calculations (internal processing)
 - Set the updated machine spindle speed (output)

 Welds were conducted in force control mode in order to maintain approximately constant frictional forces between the tool and the weldment. Undesirable fluctuation of forge force would be experienced in welds conducted in position control mode. Force control mode ensured that the forge force was a control variable for the weld experiments conducted in this study.

1.8. Organisation of Dissertation

Chapter 2 presents relevant scientific documents which support this study in terms of tool design as well as algorithm implementation and tuning.

Chapter 3 details the tool design; explains the research method executed; outlines the FSW machines utilised in the study; explains the method by which temperature data is transmitted from the rotating tool (telemetry system) to the machine controller and discusses the weld setup and geometry.

Chapter 4 discusses the FSW machine control systems which were implemented on the machine prior to the initiation of this study which were utilised in the experiments conducted in this study.

Chapter 5 forms the main body of the dissertation. The chapter includes the design, implementation, tuning and verification of the temperature control system. The performance of the control system regarding response to step command changes as well as disturbance rejection was tested. In addition to this, tensile tests were conducted in order to investigate the influence which weld temperature has on weld quality.

Chapter 6 formulates conclusions from the experimental data generated by this study and provides suggestions for future research which would build on the knowledge generated by this study.

Chapter 1 Introduction

1.9. Summary

This chapter introduced FSW basic concepts and principles necessary for understanding the method by which a typical FSW joint is produced. In addition to this, the concept of the material OPT was introduced. This study is based on optimisation of a control system designed to maintain the weld zone temperature which contributes to good consistency of weld quality. It is thus possible to maintain the material OPT along the weld path using this control system. In addition to this, the control system is able to maintain weld zone temperature in the presence of thermal disturbances. The significance of this study to industry and eNtsa is the possibility of ensuring the consistency of FSW quality through the use of this temperature control tool.

The problem statement outlines causes of weld zone temperature fluctuations. These causes include heat dissipation into the plate being welded (changes according to position on the weld path), heat dissipation into the various physical weld setup components and frictional force changes according to the welding mode (position or force control).

The selection method for the temperature sensor (thermocouple) position relative to the weld zone is described.

The delimitations of the study including project scope; material choice; weld parameters selected as a starting point; weld setup details; tool design; details about the temperature control algorithm development, testing and comparison with simulated models; components added to the existing FSW platform necessary for this study and the reason for the selection of force control mode for this study are clarified.

Chapter 2

Relevant Literature

This chapter highlights relevant knowledge contributions and sections from scientific publications which supports this study. The information from relevant literature made it possible to perform certain tasks in the development of the control system without the need to perform additional experiments to generate the information.

2.1. Temperature Response to Spindle Speed and Traverse Speed Changes

"Towards Process Control of Friction Stir Welding for Different Aluminium Alloys" ^[5] investigated the weld temperature change induced by varying spindle speed (whilst maintaining constant traverse speed) as well as the temperature change induced by varying traverse speed (whilst maintaining constant spindle speed). A thermocouple was placed in the shoulder of the tool as shown in Figure 2.1.

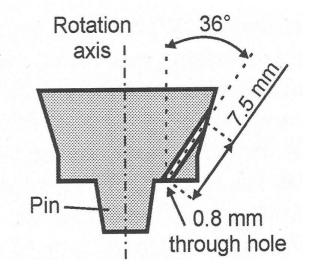


Figure 2.1. Section diagram of the thermocouple pocket in the FSW tool ^[5]

The study was carried out on 2xxx, 5xxx, 6xxx and 7xxx series aluminium alloys. During the experiment, the parameter being varied was changed at a frequency of 0.1 Hz in order to allow sufficient time for the weld temperature to change in reaction to the parameter change. The researcher utilised a nominal spindle speed and traverse speed for each alloy which would have been acquired from previous experimentation. As the varying parameter changed (at 0.1 Hz), the amplitude of the change was a percentage of the nominal value of that parameter.

For each alloy, three experiments were conducted and the weld temperature range logged:

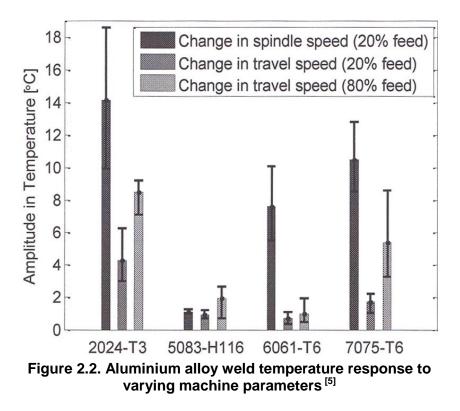
- Maintain constant nominal traverse speed and vary spindle speed (amplitude = 20% of nominal)
- Maintain constant nominal spindle speed and vary traverse speed (amplitude = 20% of nominal)
- Maintain constant nominal spindle speed and vary traverse speed (amplitude = 80% of nominal)

The parameter values used in experiment 1 and experiment 2 are shown in Table 2.1.

Alloy	Nominal		% 20 Amplitude of Nominal		Feed (mm/rev)		
	Spindle Speed (rev/min)	Travel Speed (mm/min)	Spindle Speed (rev/min)	Travel Speed (mm/min)	Varying Spindle Speed	Varying Travel Speed	
2024 722	2024-T3 1100 75 220	15	0.085	0.082	Max		
2024-13		15	220	15	0.057	0.055	Min
5002 1111/	3-H116 1300 150 260	2(0	20	0.144	0.138	Max	
5083-1110		150	200	30	0.096	0.092	Min
(0(1 T)	1300 200	200	260	40	0.192	0.185	Max
6061-T6		200			0.128	0.123	Min
7075 TC	1200	1300 75	260	15	0.072	0.069	Max
7075-T6	1500				0.048	0.046	Min

Table 2.1. Machine parameters for experiment 1 and experiment 2^[5]

The results of the experiments are shown in Figure 2.2.



The results show that varying the spindle speed resulted in the greatest reaction amplitude in the weld temperature with the exception of the 5xxx series aluminium alloys. Therefore it is more desirable to control weld temperature via variation of spindle speed. The project will therefore involve temperature control via spindle speed changes although there is a limit to the amount of change which can be made to spindle speed. This is based on the spindle speed limits for the weld setup. The machine which was used for conducting the preliminary welds was eNtsa's MTS I-stir FSW platform. The machine used for the implementation of the temperature control algorithm was eNtsa's Process Development System (PDS).

2.2. Temperature Control Model

"Investigation of Methods to Control Friction Stir Weld Power with Spindle Speed Changes" ^[6] proposed a closed loop temperature control strategy model. The strategy incorporated an inner and an outer control loop.

The outer loop obtains the operator set-point and the temperature feedback signal. From there the controller calculates the required spindle power. The temperature feedback is measured by means of a thermocouple sensor.

The inner loop uses the calculated power value (the outer loop output) as a set-point for spindle power. This set-point, together with the power feedback, is used to calculate the spindle speed command. The spindle power feedback is calculated by measuring the spindle angular velocity and spindle torque by means of a tachometer and a dynamometer respectively and then performing the calculation of power is equal to the product of torque and angular velocity. The control diagram is shown in Figure 2.3.

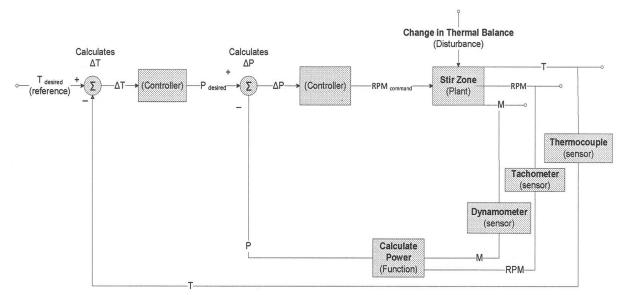


Figure 2.3. Simplified dual loop temperature control block diagram^[6]

The spindle speed and spindle torque sensors are incorporated in the MTS I-stir and PDS FSW platforms. The control system which is implemented on the machine controls the spindle speed. Spindle power output is a result of this control because the spindle drive adjusts the spindle torque in order to control spindle speed. This corresponds to a certain power value and the only importance which this value has is that it is below the capability of the spindle motor and drive setup. The control model for this study therefore differs from the model in Figure 2.3 and is shown in Figure 2.4.

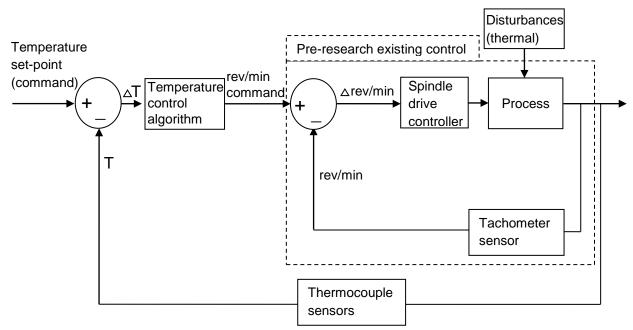


Figure 2.4. Temperature control system block diagram

2.3. Weld Temperature at Various Positions in the Weld Area

"Heat Transfer in Friction Stir Welding-Experimental and Numerical Studies" ^[7] investigated the temperature at various positions relative to the weld zone. In addition to this, a FSW temperature model was developed and the theoretical results obtained from the model (using the same parameters as used for the physical welds conducted). Temperature data from the simulation was plotted together with the data obtained from the physical welds conducted for comparison. The thermocouples were placed at various positions relative to the weld zone as shown in Figure 2.5.

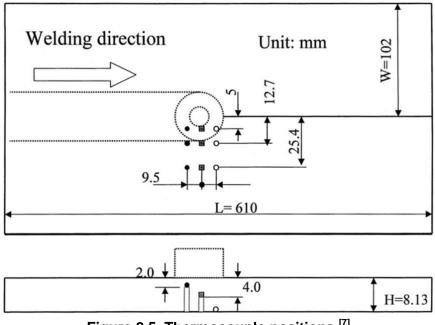


Figure 2.5. Thermocouple positions ^[7]

Figure 2.6, Figure 2.7 and Figure 2.8 show the comparison of the thermocouples at 2 mm (top), 4 mm (middle) and 8.13 mm (bottom) from the weld plate surface respectively.

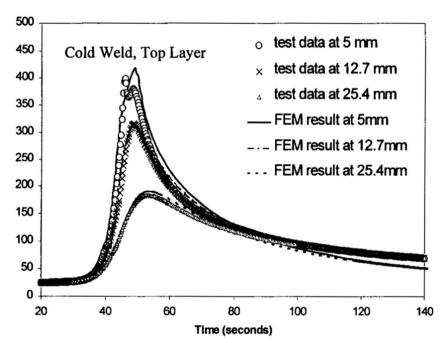


Figure 2.6. Comparison of a FSW temperature model and actual thermocouple experimental results at 2 mm depth ^[7]

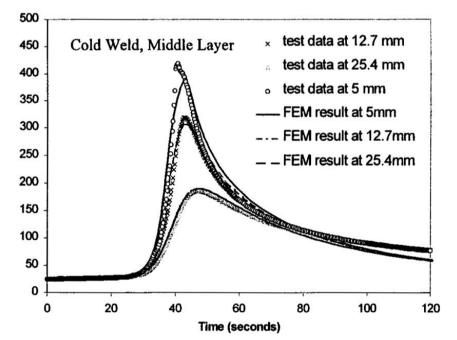


Figure 2.7. Comparison of a FSW temperature model and actual thermocouple experimental results at 4 mm depth ^[7]

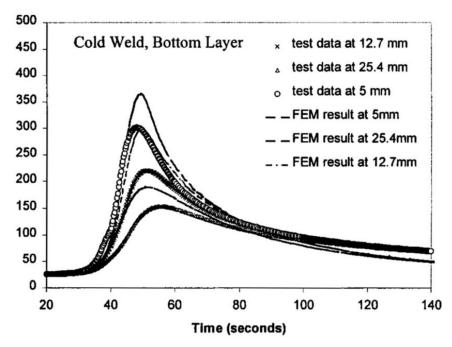


Figure 2.8. Comparison of a FSW temperature model and actual thermocouple experimental results at 8.13 mm depth ^[7]

From the graphs it can be seen that the FSW finite element model (FEM) and experimental results approximately agree.

Within each of the three graphs, it can be seen that the hottest position in the transverse direction is consistently at 5 mm from the weld centreline (nearest to the tool pin) and gets cooler as temperature is measured further from the weld centreline (at 12.7 mm and 25.4 mm). The hottest position regarding depth is the top surface.

It was decided that for this study, the thermocouples embedded in the tool would be located in the pin and nearest to where the shoulder meets the tool pin. This ensures measurement of the hottest area of the weld zone which would induce the fastest thermocouple response.

2.4. Temperature Control of Friction Stir Welding

"Effects of Tool-Workpiece Interference Temperature on Weld Quality and Quality Improvements Through Temperature Control in Friction Stir Welding" ^[8] investigated weld quality dependence on weld tool to weldment interface temperature. The study was conducted on various aluminium alloys including AA 6061 which is similar to the alloy utilised in this study (AA 6082). The study found that a critical temperature of 515°C exists for the AA 6061 plate and the particular weld setup (see Figure 2.9), below which voids begin to form in the weld and failure occurs in the weld area (not in the heat affected zone (HAZ) or the parent material). The graph identified by the circle (---) in Figure 2.9 is constructed from welds which were executed with traverse speed of 200 mm/min which is the same as the traverse speed selected for the welds conducted in this study.

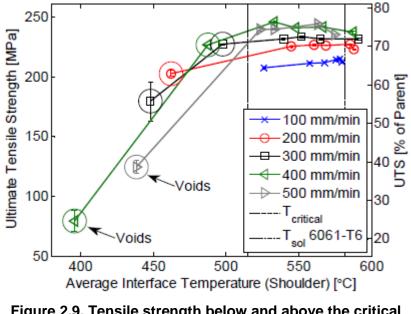


Figure 2.9. Tensile strength below and above the critical temperature ^[8]

An example of the voids which begin to form are shown in the weld cross section of Figure 2.10. The shoulder to weldment average interface temperature was 439°C in this case.

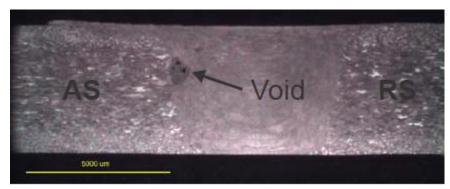
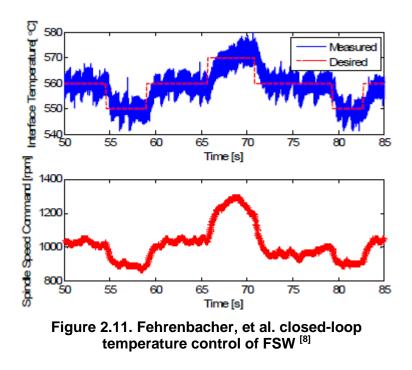


Figure 2.10. Voids ^[8]

Above the critical temperature in Figure 2.9, the weld strength is seen to be approximately constant for a specific traverse speed.

A dynamic process model was generated using the Matlab system identification tool. It was found that a first order model with a time delay was a good representation of the input data (spindle speed) to output data (process temperature) relationship.

A closed loop temperature control system was implemented and tested on 4.76 mm thick AA 6061-T6 plate by introducing step command changes to the controller setpoint. The response obtained is shown in Figure 2.11.



The following statement which is made in the study is important to this study: "The data also shows that for the parameter window chosen, varying the spindle speed results in a larger variation in interface temperature than varying the travel speed, which is an important result for developing closed-loop temperature control for FSW." ^[8]. This compliments the findings in Section 2.1.

2.5. Controller Derivative Filtering

In Section 10.5 of "Feedback Systems An Introduction for Scientists and Engineers" ^[9], a statement is made that the derivative term of a PID controller typically has high gain for high frequency signals. Typically, the high frequency signal is a result of noise introduced into the system on the sensor feedback signal to the controller. This is a drawback of the controller as it could cause the actuating mechanism (controlled by the PID controller), which drives the system, to oscillate unnecessarily. This could possibly lead to undue wear on the system and a waste of energy. A derivative filter design is suggested in Section 10.5 of "Feedback Systems An Introduction for Scientists and Engineers" ^[9]. The filter is designed as a modified calculation for the derivative term of the PID controller which attenuates controller derivative gain for high rates of change of the process variable under control (leading to a high rate of change of the error signal, typically associated with high frequency noise on the feedback signal). The filter is implemented by replacing the equation which calculates the derivative term of the PID controller with Equation 5.12 on page 55.

2.6. Ziegler Nichols Tuning Method

J.G Ziegler and N.B Nichols developed a controller tuning method outlined in "Optimum Settings for Automatic Controllers" ^[3]. The method allows the controller tuner to monitor a number of process characteristics and calculate the approximate optimum controller settings without the need to apply excessively complex mathematic calculations regarding the system dynamics. The method could produce controller settings which are closer to optimum than if excessively complex mathematic calculations regarding the system were carried. The reason for this being that the method takes into account all system properties which are difficult to quantify mathematically in the dynamic model. An example of such a property is bearing friction at various operating speeds.

The method begins by setting P, I and D controller gains to zero. With the system operating and the controller set-point set to the position at which the controller is to be tuned, the proportional gain is increased slowly from zero until the system begins to oscillate with constant amplitude. The proportional gain at this point is considered the ultimate gain. The period of the oscillation is measured. From the ultimate gain and the oscillation period, the approximately optimum controller P, I and D gains can be calculated from the Ziegler Nichols equations (see Section 5.3.3 on page 63).

2.7. Tool Designs

A number of sources were referred to during the design of the FSW tool used in this study and relevant details of each are outlined in the following paragraphs:

For FSW of 6.35 mm thick 6061-T6 aluminium alloy in the study titled: "Tool Forces Developed During Friction Stir Welding" ^[10], the tool consisted of a shoulder diameter of 19.2 mm, a threaded pin with diameter of 6.35 mm and pin length of 5.83 mm. The tool tilt angle utilised during welding was 1° and the tool rotation direction was such that the thread direction displaces the plasticised material downwards. Pushing the plasticised material downwards compliments the data found in Section 2.3 which shows that the material is at a higher temperature near to the tool shoulder. Pushing this material downward would assist in ensuring that the material at the bottom of the weld zone is sufficiently plasticised in order to avoid flaws at the bottom of the weld.

Friction stir welding of 5 mm thick aluminium alloy 6061 plate was reported in literature titled: "Friction Stir Welding of Al 6061 Alloy" ^[11]. The tool consisted of a shoulder diameter of 25 mm, a pin height of 4.8 mm and the tool tilt during welding was 2°.

Friction stir welding of aluminium alloy 6061-T6 plate of thickness 4.95 mm was reported in literature titled: "Tensile Properties and Constitutive Modeling of Friction

Stir Welded AA6061-T6 Butt Joints"^[12]. The tool design utilised in the study is shown in Figure 2.12. A tool tilt angle of 3° was utilised in the study.

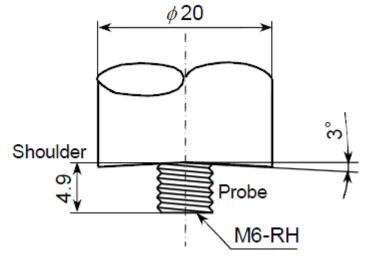


Figure 2.12. Tool design for AA6061-T6 4.95 mm plate ^[12]

Tool geometry was investigated in the study titled: "Study of Tool Geometry in Friction Stir Welding Applications" ^[13]. The study suggested that the material suitable for FSW welding aluminium between 0.5 mm and 50 mm in thickness is a hot worked tool steel which complies with the AISI H13 standard. This material was suggested for its properties of strength, toughness, hardness and wear resistance at the welding temperature of aluminium FSW. W302 tool steel (which was available for this study) complies with the AISI H13 standard. "Study of Tool Geometry in Friction Stir Welding Applications" ^[13] also suggests a tool pin length of 3.85 mm for welding AA6061 plate of 4.00 mm thickness.

"The Influence of Thread Form on Refilling Friction Stir Welding of 2219 Aluminium Alloy Sheets" ^[14] investigates the effects of tool pin thread pitch on material flow velocity by means of simulation. The study investigated thread pitch of 0.6 mm and 1.2 mm. The spindle speed was 83.8 rad/s (approximately 800 rev/min) and the tool traverse speed was 3.33 mm/s (approximately 200 mm/min). The study concluded that the thread pitch can increase the material downward flow by more than 20 percent in order to fill any voids which may begin to form in the weld zone.

FSW of 6 mm thick AA 7039 plate was studied in literature titled: "Tool Design Effects for FSW of AA7039"^[15]. Various tool dimensions were tested including shoulder diameters of 16 mm, 19 mm and 22 mm as well as pin diameters of 6 mm, 7 mm and 8 mm. The study found that increasing the tool pin diameter beyond 7 mm caused a reduction in weld cross-sectional area and tensile strength. The study also found that a shoulder diameter of 19 mm was the most suitable. The study utilised a vertical milling machine which was converted to conduct FSW. The setup produces a FSW which is essentially conducted in position control mode (vertical position of the spindle head determines the plunge depth). A further study was conducted (written by some new authors as well as some of the authors of "Tool Design Effects for FSW of AA7039"^[15]) titled: "Effect of Tool Shoulder and Pin Probe Profiles on Friction Stirred Aluminium Welds – a Comparative Study" ^[16]. The study made the following statement which was valuable in the design of the FSW tool utilised in this study: "Apart from initial high vibration of the machine, the straight cylindrical tool exhibited good weld surface finish and overall acceptable welds." [16]. In the study it was once again found that it was detrimental for weld quality to utilise a FSW tool which exhibits a straight, cylindrical tool exhibiting a pin diameter exceeding 7 mm ^[15].

2.8. Tensile Strength

"Tensile Properties and Constitutive Modeling of Friction Stir Welded AA6061-T6 Butt Joints" ^[12] reported tensile strength of between 72 percent and 74 percent of parent material. The relevance between this information and this study is that both studies were carried out on 6xxx aluminium alloy in the T6 condition (heat generated during welding causes over aging of the heat affected zone) and the results are comparable. Tensile test results obtained from this study are shown in Section 5.7 of this document.

"Heat Transfer in Friction Stir Welding-Experimental and Numerical Studies" ^[7] investigates FSW temperature of AA2195-T8 which is a heat treatable aluminium

alloy (as is the case for AA6082-T6, which is utilised in this study). According to the study, a tensile strength of greater than 66 percent of the parent material is considered a good FSW for heat treatable aluminium alloys^[7].

2.9. Summary

This chapter outlined and discussed information from various literature sources which is of particular relevance to this study. Literature which investigated temperature response to spindle speed and traverse speed changes showed that variation of spindle speed affected weld zone temperature more significantly than variation of traverse speed. A temperature control model for friction stir welding was proposed in the study titled: "Investigation of Methods to Control Friction Stir Weld Power with Spindle Speed Changes" ^[6] and there were similarities between the control system diagram in the study and the control system diagram of the control system developed in this study. The study in which temperature was measured at various positions relative to the weld zone assisted with the selection of the positioning of the thermocouples embedded in the FSW tool utilised in this study.

A study was presented which investigated temperature control of friction stir welding and the effects which weld temperature has on weld quality. A particular type of controller derivative filter was presented in literature which was implemented and modified in this study. The purpose of the filter is to reduce undesirable oscillation of the control system actuator's output variable (spindle speed in this study). The Ziegler Nichols PID tuning method ^[3], which was used to tune the control system in this study, was outlined. The method is a practical procedure used to determine the approximately optimal controller gains for a control system based on recorded system behaviour. Tool design specifications were collected from relevant studies detailing FSW tool geometry for 2xxx, 6xxx and 7xxx series heat-treatable aluminium alloys. The information assisted with the choice of tool geometry utilised in this study. Typical information (collected from two sources) regarding FSW tensile strength for heat treatable aluminium alloys relative to the parent strength was discussed.

Chapter 3

Research Methodology and Experimental Setup

This chapter explains the research method undertaken in order to investigate and produce an acceptable FSW tool design for the material being welded. The principle by which the telemetry system transmits the temperature data from the rotating tool to the machine controller is explained. The MTS FSW platform used for the preliminary welds and the PDS platform used for the main experimental welds in this study are outlined. The chapter also outlines the experimental setup used for conducting the experimental welds. Details regarding the physical weld geometry and weld setup are explained in the final section of this chapter.

3.1. Research Methodology

Initially a literature survey was completed. A foundation of understanding of the FSW process and weld zone temperature was generated. Information from the survey assisted with tool design including geometry and thermocouple pocket design.

The tool was designed and manufactured according to Section 3.2. The temperature measurement hardware (thermocouples and telemetry system) was fitted to the FSW platform and interfaced with the machine controller.

The process window was established (see Section 5.1). The tool tilt angle was selected appropriately to supply adequate forging force to the material at the rear of the tool whilst producing a good surface finish. Forge force, maximum spindle speed and minimum spindle speed were determined. The tool travel speed (after the ramp up stage) was constant for the entire study and all the welding was done in force control mode, except for the position control mode welds conducted during the establishment of the process window.

In the preliminary welds (see Section 5.2), the relationship between spindle speed and temperature was investigated. This work provided the researcher with a better understanding of the process temperature response and provided data which was used in generating the mathematical model of the process. This mathematical model was later used in simulations of various temperature PID controllers (generated through various methods, see Section 5.5) which were compared to the response of the implemented (real) weld temperature controller response.

The temperature control algorithm was developed and tested (See Section 5.3). The control system measures the temperature of the weld zone via thermocouple temperature sensors located in the non-consumable weld tool. If the temperature is below the set-point, the algorithm increases spindle speed to compensate. If the temperature is above the set-point, the controller decreases spindle speed to compensate. Limits were placed on the amount by which the controller was allowed to alter machine spindle speed. If a limit is reached, the spindle speed is set to that limit and if the system does not reach the set-point temperature, the set-point was set to an unsuitable value for the process setup. These limits protect the equipment because insufficient spindle speed introduces the risk of the weld material cooling excessively which could lead to tool seizure and/or fracture. On the opposite limit, excessive spindle speed would lead to excessive plasticising of the weld material which would cause the tool to over plunge and collide with the backing plate, damaging it and/or the weld tool. The system was tuned using the Ziegler Nichols PID tuning method ^[3].

Matlab's system identification tool was used to generate a mathematical relationship (transfer function) between the spindle speed and weld zone temperature. Matlab's controller design tools (ACSYS and Simulink PID tuner) were used to design PID controllers. These controllers were connected to the transfer function in Matlab Simulink and the responses of each were simulated in comparison to the response of the real control system. See Section 5.4 and Section 5.5.

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The disturbance rejection of the system was tested (see Section 5.6). Heat energy sink and heat energy source disturbances were placed on the weld plate. The control system compensated for these disturbances by increasing or decreasing spindle speed in order to maintain the desired weld zone temperature.

Tensile testing was conducted on the welds obtained from the welds completed in Section 5.6 in order to test the weld strength consistency. See Section 5.7 for the discussion about the tensile testing.

3.2. Tool Design

A typical FSW tool consists of a shoulder and a pin. The pin is plunged into the material to the required plunge depth and at this depth; the shoulder comes into contact with the material surface. The shoulder may be concave, flat or consist of some sort of machined pattern intended to improve frictional heat generation and/or material flow. The pin design may consist of a straight or tapered design, flutes, threaded or a combination of these designs. A FSW tool does not typically contain thermocouple pockets unless specifically required for the intended used of the tool.

The FSW tool used in this study was manufactured from W302 tool steel and then through hardened to 54 on the Rockwell C scale. The tool design consists of a 22 mm diameter, 6° concave shoulder, with a straight, threaded (0.8 mm pitch), 7.9 mm diameter pin which is 5.77 mm in length from the lowest point on the shoulder. The FSW tool is shown in Figure 3.1.



Figure 3.1. FSW tool

Two J-type thermocouples of 1.5 mm diameter are located in the tool in order to measure weld zone temperature during the welding process. J-type thermocouples were selected based on their operating range of 0°C to 750°C ^[17] since AA 6082-T6 has a liquidus temperature of approximately 660°C ^[18] and the weld process is executed below this value. These thermocouples provide the sensory feedback necessary for closed-loop temperature control. The thermocouple tips are located with 180° separation, inside the tool pin near the shoulder as shown by the tool mock-up shown in Figure 3.2.



Figure 3.2. FSW tool mock-up

Regarding the weld tool which has the thread machined onto the pin, the thermocouple tip is separated from the weld zone material by approximately 0.2 mm of tool material. The thermocouple pockets are approximately 50 mm in depth. In order to achieve sufficient accuracy of the bottom of the pocket, an Electric Discharge Machine (EDM) die sink with 1.5 mm diameter copper electrodes was used for

machining the pockets. The arc length in the machining process creates the clearance for the thermocouple sheaths.

The thermocouples were calibrated by utilising a furnace and the FSW platform's PLC for the telemetry output signals. The J-type thermocouple specification for temperature versus thermoelectric voltage was plotted and suggests the thermocouples respond linearly in the range achieved by the welds in this study. Refer to **Appendix A** for the calibration data.

The telemetry system provides gain and zero set-point adjustments for each channel. These were adjusted in order to utilise the range of the process and achieve good resolution. Channel 7 and channel 8 of the telemetry system were utilised. The gain and zero set-point for each channel are adjusted by means of turning set screws. The two channels were adjusted to approximately the same setting although it is difficult to set them to the exact identical setting by means of turning a set screw. For this reason there are slightly different calibrations for channel 7 and channel 8. Before welding commenced, it was decided that because the system will never exceed 700°C (which is above the material's liquidus temperature) and the telemetry output is ±10 V, the gain and zero were set such that 700°C measured by the thermocouple generates approximately +10 V output on the telemetry system output. An initial calibration was done over a broad range of temperatures in order to be able to measure weld temperature. Welds were conducted with this calibration in order to log the temperature range of the particular weld setup. The thermocouples were later re-calibrated for the range of temperature which is experienced by the weld setup used in this study. This eliminates error of the calibration data inside of the process temperature range caused by any possible non-linearity of the thermocouples outside of the process temperature range. The operating range of temperature achieved by the welds conducted in this study was found to be between 450°C and 540°C. The thermocouples were re-calibrated in this range. This makes the thermocouple data as accurate as possible for the experiments conducted thereafter. The measured data and resulting calibration curves can be seen in **Appendix A**. The error of the

temperature measurement system, including the thermocouples, telemetry system and PLC data acquisition was calculated. The combined error for channel 7 was calculated as 1.119% (95% confidence) and the combined error for channel 8 was calculated as 1.823% (95% confidence). See **Appendix A, page A-5 and page A-9** for the error calculations executed with Microsoft Excel.

3.3. Telemetry System

The thermocouple temperature data is transmitted from the rotating tool wirelessly via the telemetry system. The telemetry system communicates the temperature data with the machine controller in order to generate the weld zone temperature feedback signal used by the temperature control algorithm.

3.3.1. Power Supply

The circuitry attached to the rotating spindle head (contained in the telemetry rotor) is powered inductively by the antenna coil as the primary coil and the rotor coil as the secondary. The AC power generated in the rotor coil is rectified to DC power in order to power the rotating circuitry.

3.3.2. Sensor Data Transmission

The circuitry in the rotor amplifies the sensor signals and transforms the data by generating a frequency subcarrier for each sensor channel (different frequencies). The mixer then mixes the subcarriers into one signal (this signal thus contains all sensor channel frequencies and is called the subcarrier mixture signal). The radio frequency modulator (RF modulator) uses the subcarrier mixture signal to modulate the main carrier frequency which is transmitted from the rotor to the receiver via the antenna system. This signal is called the RF signal. The telemetry rotor is shown in Figure 3.3.



Figure 3.3. Telemetry rotor

On the receiver side, the reverse process is done in order to obtain voltage signals for each sensor channel. The demodulation unit (see Figure 3.4) is plugged into a 220 V single phase power supply. It in turn powers the compact power generator which in turn powers the telemetry rotor via the antenna. The RF demodulator (contained in the compact power generator) generates the subcarrier mixture signal (combined sensor data) and sends it to the demodulation unit via the coaxial cable seen in the figure.



Figure 3.4. Antenna (left front), compact power unit (left rear) and demodulation unit (right)

The demodulator demodulates the signal into the separated subcarrier signals for each channel and converts the data from frequency defined to voltage defined. The voltage signals are amplified to \pm 10 V analog outputs for each channel shown at the rear of the demodulation unit (see Figure 3.5). These signals are connected to the controller analog input card.



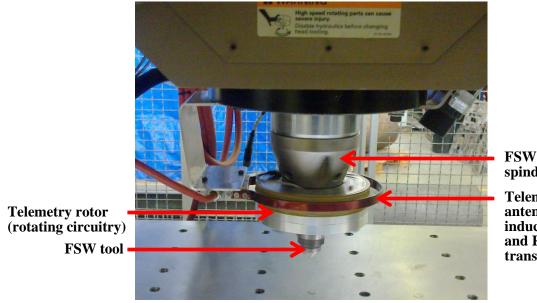
Figure 3.5. Demodulation unit rear

3.4. MTS Platform



Figure 3.6. MTS FSW platform

The preliminary work for this study was carried out on the MTS FSW platform at eNtsa (a technology station at Nelson Mandela Metropolitan University). The FSW machine is shown in Figure 3.6. This work involved establishment of the process parameter window and investigation of weld zone temperature response to spindle speed step changes of 100 rev/min (see Section 5.1 and Section 5.2). The FSW machine spindle setup is shown in Figure 3.7.



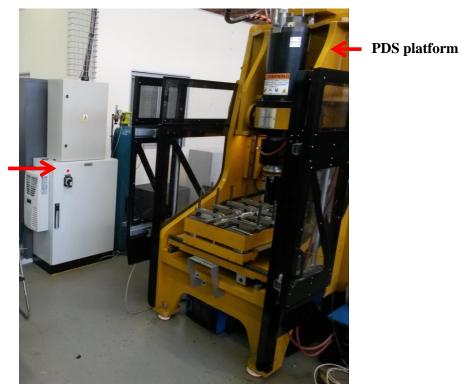
FSW machine spindle head

Telemetry antenna (for inductive power and RF data transmission)

Figure 3.7. MTS FSW machine head with attached telemetry components

3.5. Process Development System (PDS)

The PDS platform (see Figure 3.8) was developed by eNtsa at NMMU. The machine consists of four axes (x, y, z and b which is the tilt axis). The platform is versatile and is capable of performing many types of friction processes such as FSW, friction hydro pillar processing (FHPP) and friction taper stud welding (FTSW). The platform is also able to perform machining operations in a similar manner to a CNC milling machine.



PDS platform power supply and spindle drive cabinet

Figure 3.8. PDS Platform

The researcher has full access to the machine control program. Closed-loop control of temperature using analog inputs for the feedback signals and the spindle motor as the actuator was therefore possible. The closed-loop temperature control algorithm was developed and tested; and the experimental welds investigating weld consistency were conducted on this platform (see Section 5.3 to Section 5.6). The FSW tool setup with telemetry system for the PDS platform is shown in Figure 3.9.

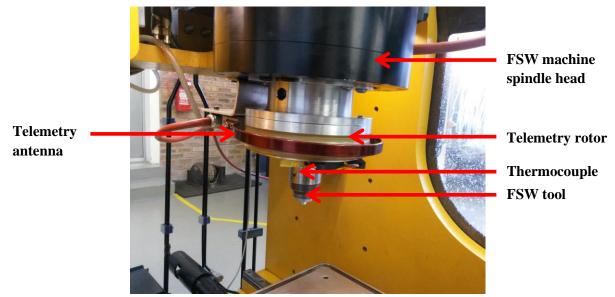


Figure 3.9. PDS spindle head setup

3.6. Weld Geometry and Setup

Experimentation in this study was conducted on Aluminium Alloy 6082-T6 with the following dimensions and backing plate material:

- Plate dimensions: 750 mm x 100 mm x 6.1 mm
- Backing plate material: 17-4 PH stainless steel

The development of the temperature control system was conducted on FSW bead on plate welds as opposed to FSW butt welding. This reduces weld preparation and reduces the number of controlled variables which need to be maintained consistent in order to avoid undesirable influences of the experimental results. For a specific material type and plate thickness, the welding parameters for bead on plate welding and FSW butt welding are approximately identical.

There are three main reasons for the reduction in weld preparation: butt welds require milling of the joining edges in order to ensure that the two edges are perfectly parallel to each other and the joint gap is constant; removal of the aluminium oxide from the

Chapter 3 Experimental Setup

butting edges immediately prior to welding is required because the surface oxide could have a reducing effect on weld quality; a butt weld requires extra clamping in order to prevent the two plates from separating during welding. Controlled variables which are removed from the experiment include: plate gap variation; effectiveness of the aluminium oxide removal procedure; time delay between oxide removal and weld execution during which oxide begins to reform. The weld setup is shown in Figure 3.10.

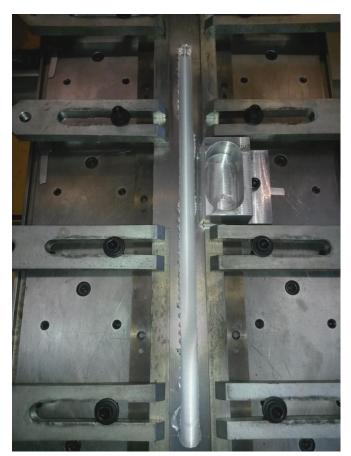


Figure 3.10. Bead on plate FSW

Weld length conducted on the MTS platform was 650 mm. Maximum weld length on the PDS platform was limited by the stroke of the x-axis. The PDS platform allowed for a maximum weld length of 585 mm (which is the length of the weld shown in Figure 3.10).

3.7. Summary

The research methodology followed in conducting this study outlined the steps taken to develop the temperature control system and verify the resultant PID controller. The FSW tool design was explained and thermocouple pocket machining on the tool verified. The verification of the pocket machining process ensured that the thermocouple tips are located correctly relative to the tool geometry.

The telemetry system was outlined in this chapter. The theory behind supplying the rotating circuitry with power and the transmission of the thermocouple data from the rotating tool to the machine controller was explained.

The chapter shows the FSW setup on the MTS platform (used for the process window establishment (see Section 5.1) and the preliminary welds conducted (see Section 5.2)). The chapter shows the FSW setup on the PDS platform (used for temperature control algorithm development and testing (see Section 5.3, Section 5.4 and Section 5.6). The physical weld geometry and setup is explained in the final section of this chapter.

Chapter 4

Machine Control

This chapter discusses the control mechanisms of the PDS platform (existing prior to the initiation of this investigation) which are utilised during; and are necessary for executing the experimental welds conducted in this study. See Section 5.3.1 (page 60) and Section 5.3.2 (page 61) for the discussion about implementation of the temperature control system.

4.1. PDS Platform Systems Control

The PDS platform contains a central PLC (Beckhoff TwinCAT) which performs the majority of the calculations necessary for machine control. A human machine interface (HMI) is connected to the PLC. All weld programs are programmed and executed through this interface. The weld data is viewed and/or extracted from the PLC memory via the HMI and a universal serial bus (USB) port. A servo motor drives the machine spindle. The PLC controls the spindle by generating a spindle speed or spindle torque command which is communicated to the servo motor drive via an EtherCAT connection. The servo motor drive contains internal control loops designed to control spindle torque and spindle speed according to the command which it receives from the PLC.

The x, y, z and b axes are driven by hydraulic cylinders. The hydraulic pressure for each cylinder is regulated by servo-valves which are controlled by the PLC. The positions of the axes are measured by means of MTS Temposonic displacement sensors (R series). A PID control loop (similar to the force control loop in the control system diagram of Figure 4.2) controls each axis.

4.2. Z-force Measurement and Z-force Control

The bed of the PDS platform is mounted on four load cells, one of which is shown in Figure 4.1.



Figure 4.1. One of four of the PDS bed load cells

The load cells measure force along three axes. The force measurements from the four load cells are used to calculate the resultant x-force, y-force and z-force applied to the bed and weldment by the weld tool. All forces are logged by the machine during a weld for the purpose of data analysis. The forge force (z-force) control system diagram (see Figure 4.2) defines the interaction of the system components.

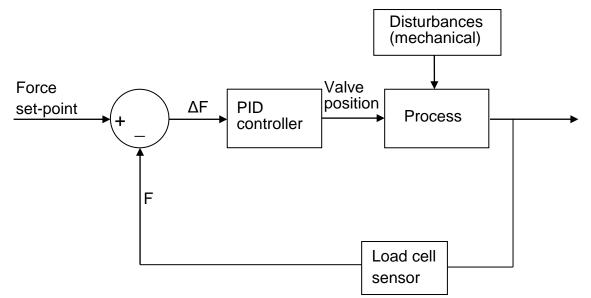


Figure 4.2. Forge force control system diagram

The operator programs a force set-point into the weld program, the load cells provide the forge force feedback signal and the error signal (ΔF) is then used by the PID control algorithm in order to perform necessary control calculations based on the dynamics of the system. The PID output provides a command signal for the z-axis hydraulic servo-valve position. The valve is controlled such that it regulates the hydraulic pressure appropriately in order to maintain the forge force set-point. Mechanical disturbances affecting the process (forge force in this case) such as deflection of the machine bed are accounted for by the PID controller because the controller gains have been set such that the system exhibits good disturbance rejection.

4.3. Feed Rate Control

The control system diagram (see Figure 4.3) for controlling weld traverse speed (x-velocity or feed rate) defines the interaction of the system components.

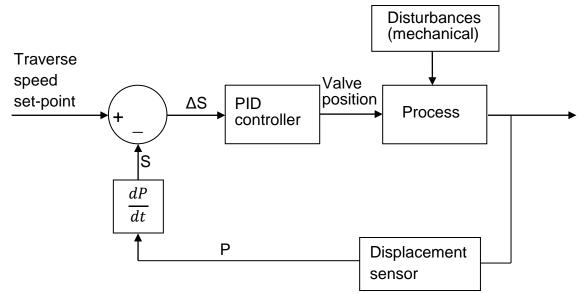


Figure 4.3. Feed-rate control system diagram

The operator programs the traverse speed requirement into the weld program which is the traverse speed set-point. The PLC calculates the derivative of the x-axis displacement position sensor output (P) which results in the x-axis velocity (S) feedback signal. The error signal (Δ S) is then used by the PID controller in order to perform necessary control calculations based on the dynamics of the system. The PID output provides a command signal for the x-axis hydraulic servo-valve position. The valve is controlled such that it adjusts the hydraulic pressure (and hence x-force) appropriately in order to maintain the traverse speed set-point. Mechanical disturbances affecting the process, such as variations in the resistance of the material in front of the tool are accounted for by the PID controller because the controller gains have been set such that the system exhibits good disturbance rejection.

4.4. Summary

This chapter defines various machine control components which were implemented on the machine prior to the initiation of this study. These components include: the main controller for the PDS platform and how it interfaces with the operator; the driving mechanisms for the machine axes and the spindle as well as their respective controlling devices; the force sensors and the manner in which they are laid out on the machine. The control loop for forge force control and the control loop for weld traverse speed control were outlined in this chapter.

Chapter 5

Temperature Control Design and Verification

This chapter explains in detail the manner in which the experiments were conducted and the results of this study acquired. The procedure followed in the development and testing of the temperature control system is covered in detail. A mathematical model of the relationship between FSW temperature and machine spindle speed was generated using Matlab. The weld temperature response was compared to the response of the model; both of which using the PID controller gains determined from the Ziegler Nichols tuning method ^[3] (see Section 5.3.3). In addition to this, alternative PID controllers were generated using two Matlab controller development tools. The response of each controller was simulated (in Matlab Simulink) on the same scope as the model which was simulated with the PID controller gains found from the Ziegler Nichols tuning method ^[3]. A clear comparison can therefore be seen as the responses are on the same set of axes (see Section 5.5). Experimental welds, which introduce a thermal disturbance between the middle work-piece clamps, were conducted. The data from the experiments is analysed and the behaviour of the control system discussed in this chapter. Furthermore, tensile testing was conducted on these experimental welds in order to generate an indication of the weld quality along the weld length. Weld strength consistency is discussed in this chapter.

5.1. Establishment of the Process Window

The initial set of welds conducted in the establishment of the process parameter window consisted of five welds. These welds were conducted on the MTS FSW platform in position control mode because the forge force requirement for the particular weld setup was unknown. Setting the forge force too high (in a force control mode weld) for a particular weld setup would cause the tool to over plunge, into the backing plate. This could cause damage to the tool and/or the backing plate.

The machine sensor data is automatically logged by the machine during a weld. From the data logs of "Weld 3", "Weld 4" and "Weld 5", the process forge force and weld zone temperature was plotted in order to determine the maximum forge force required (and allowed at a given weld zone temperature) for the welds conducted in the remainder of this study (welds which were conducted force control mode). The reactive forge force applied by the machine, which was required to maintain the vertical position of the tool, can be seen from the graphs (see "Weld 5" in Figure 5.2). For the full set of weld graphs, see **Appendix B**.

"Weld 1" and "Weld 2" were conducted with 1° and 2° of tool tilt respectively. As a starting point, spindle speed was 600 rev/min which was slightly above the spindle speed suggested by literature for a weld traverse speed of 200 mm/min ^[4]. "Weld 1" rendered a good surface finish and "Weld 2" rendered a rough surface finish. A higher forge force was experienced by the material in "Weld 2" than the material in "Weld 1" which can be seen in Figure 5.1.

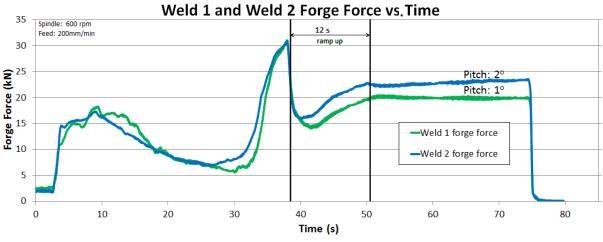
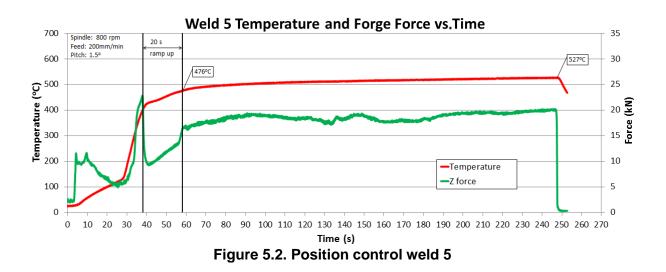


Figure 5.1. Forge forces of weld 1 and weld 2

The researcher thus decided to make a compromise between good surface finish and high forge force by utilising 1.5° of tool tilt for the remaining welds in this study. Various other conditions have an effect on weld surface finish such as temperature

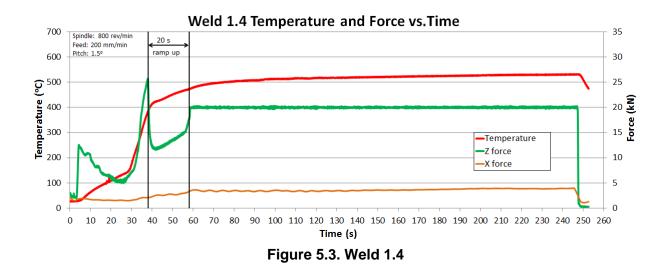
(evident in welds done by the researcher) although investigation of surface finish does not form part of the scope of this study.

"Weld 3" and "Weld 4" introduced spindle speed increases in order to determine the approximate upper limit of the process window regarding spindle speed. "Weld 3" and "Weld 4" were conducted with spindle speed of 700 rev/min and 800 rev/min respectively. Welds conducted with higher spindle speed experienced a lower reactive forge force generated by the machine. The higher spindle speed applies a higher energy input rate to the weld zone which causes the weld zone material temperature to rise, which becomes softer and is therefore displaced by the tool at a lower forge force. "Weld 4" and "Weld 5" (800 rev/min) were the only welds which experienced less than 20 kN forge force for the majority of the weld length after the ramp up stage. The forge force in "Weld 5" reached 20 kN near the end of the weld, which also corresponds to the hottest area of the weld. This suggests that it is safe to run a weld of this particular setup with 800 rev/min spindle speed and 20 kN forge force without the risk of over plunging (into the backing plate). The graph showing temperature and reactive forge force versus time is shown in Figure 5.2.



The researcher thus decided that the forge force of 20 kN would be used for the remaining welds in this study. It was also decided that 800 rev/min would be the preliminary upper limit for the spindle speed. A further six welds were conducted in

force control in order to confirm the maximum spindle speed and determine the minimum spindle speed. See **Appendix C** for the full set of weld graphs. These welds were numbered 1.1 to 1.6 and were force control mode welds (20 kN forge force). The upper limit for spindle speed was confirmed by "Weld 1.4" (800 rev/min spindle speed). For "Weld 1.4", the region where the tool reached its maximum plunge depth, faint tool marks could be observed for a short distance on the backing plate, meaning that the tool skimmed the backing plate lightly in this region. This meant that the spindle speed could not be increased further (confirming the upper spindle speed limit). The graph for this weld can be seen in Figure 5.3.



The next objective was to determine the lower limit for spindle speed. This procedure was the process of most risk in the study. Decreasing spindle speed decreases the plasticised state of the material (lower energy input rate allows cooler weld zone material), causing the machine to apply an increase of x-force (in the traverse direction). The machine does this in order to maintain the weld traverse speed set by the operator (200 mm/min). Decreasing the spindle speed excessively could cause tool seizure or failure (the tool pin may fracture).

A finite element analysis was done on the tool in order to determine the limit of x-force which could be applied to the pin. In reality, the x-force applied by the machine is taken up partially by the tool shoulder (caused by the plunge depth and tool tilt angle)

and the remainder is distributed along the tool pin. In addition to this, the weld zone material is cooler near the bottom (evidenced by Section 2.3) which implies that a greater amount of the x-force (supported by the tool pin) is supported by the lower portion of the tool pin. The proportion of the x-force supported by the pin is unknown for this particular weld setup. For the analysis, the worst case scenario is therefore used and assumes that the entire x-force is supported by the pin tip. See Figure 5.4.

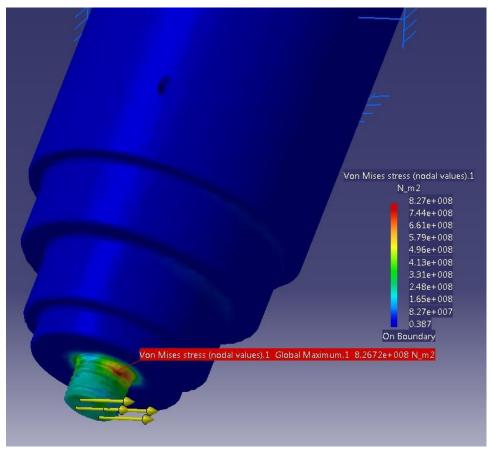


Figure 5.4. FSW tool FEA analysis

The tool analysis showed that for an x-force of 5 kN applied to the pin, the area of maximum bending moment (in combination with a stress concentration caused by the thread) experienced a maximum stress of approximately 827 MPa. A section view revealed that the material at the bottom of the thermocouple pockets experienced approximately 575 MPa as shown in Figure 5.5.

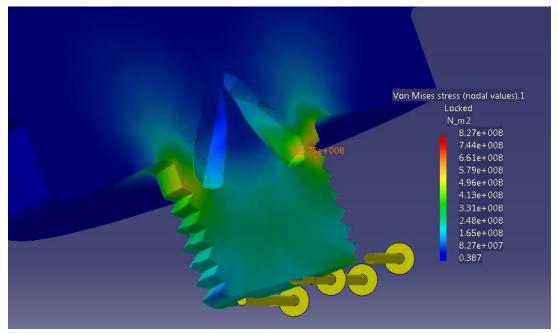


Figure 5.5. FEA thermocouple section view

The Bohler datasheet for W302 tool steel shows material strength after hardening (approximately 54 HRC) for various operating temperatures. Specifically, the 0.2 percent proof stress at 500°C (corresponding to weld temperature in this study) is 900 MPa. The safety factor if the tool were to experience the extreme case modelled in the FEA analysis would be 1.09 which would not be very safe as 1.5 would be desirable. Considering that a portion of the x-force is supported by the tool shoulder and the remaining x-force is distributed along the pin length in reality, it was decided that 5 kN would be a relatively safe limit for x-force when determining the lower spindle speed limit.

For "Weld 1.5", spindle speed was 400 rev/min. The x-force was checked from the weld log data. The graphs of x-force for "Weld 1.1" to "Weld 1.6" in **Appendix C** show smoothed force data by means of a moving average for clarity of the graphs. The oscillation of the x-force could be attributed to the inevitable small amount of runout of the tool. This was evident by the frequency of the force oscillation matching the frequency of the spindle rotation. The z-force graphs, however, are plotted from raw

force data. The maximum x-force recorded in "Weld 1.1", "Weld 1.5" and "Weld 1.6" are as follows:

- "Weld 1.1" (spindle speed: 500 rev/min): 4.55 kN
- "Weld 1.5" (spindle speed: 400 rev/min): 4.97 kN
- "Weld 1.6" (spindle speed: 300 rev/min): 5.57 kN

The spindle speed was not decreased further than 300 rev/min, as it would risk tool failure and the spindle speed lower limit was therefore set at 300 rev/min. The graph of "Weld 1.6" shows that the average x-force is less than 5 kN.

Process parameters for the welds conducted in the remainder of the study:

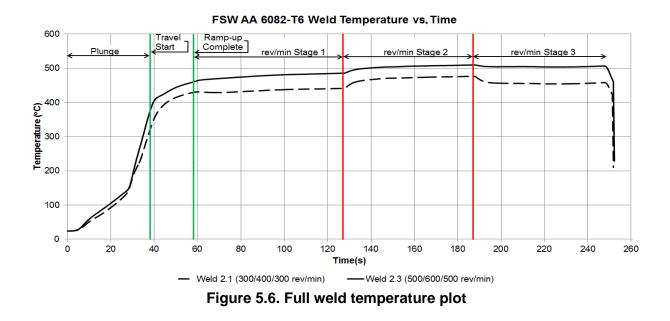
- Forge force: 20 kN
- Traverse speed: 200 mm/min
- Spindle speed range: 300 rev/min to 800 rev/min

5.2. Temperature Response to Spindle Speed Changes

Preliminary work was carried out on the MTS FSW platform (see Section 3.4). The work investigated weld zone temperature response to changes of spindle speed whilst all other weld parameters, including weld traverse speed and weld forge force, were maintained constant. The weld consisted of five regions which include plunge, ramp up, spindle speed stage 1 (referred to as simply stage 1), spindle speed stage 2 (referred to as simply stage 2) and spindle speed stage 3 (referred to as simply stage 3). The plunge region is the portion where the rotating tool pin is plunged into the material until the tool shoulder comes into contact with the surface of the plate to be welded. The ramp up region is the portion of the weld where the tool begins to move in the traverse direction. The tool is in position control until the end of this region. The tool accelerates slowly (to build up the temperature of the weld zone) over 20 mm and reaches the weld traverse speed at the end of this region. The weld then

enters stage 1 where it stops accelerating (traverse speed is constant at 200 mm/min from this point to the end of the weld) and goes into force control mode (set to 20 kN forge force). The spindle speed is the same in all regions except for stage 2. The spindle speed in this stage is either increased or decreased by 100 rev/min relative to the other regions of the weld.

The temperature graphs of two welds are shown in Figure 5.6. The axis limits are set in order to show the temperature of the weld zone from the beginning to the end of the weld. The temperature change in stage 2 is small relative to the range of temperature of the entire weld and Figure 5.6 is shown in order to put this temperature change into perspective. Subsequent figures show smaller axis ranges in order to make the temperature changes of stage 2 clearer. The legend of each graph is labelled with the spindle speed for each of the three spindle speed stages.



The graphs in Figure 5.7 show that for the low average spindle speed welds (e.g. "Weld 2.1"), the spindle speed increase, of 100 rev/min in stage 2, results in a larger temperature increase than for the higher average spindle speed welds (e.g. "Weld 2.3"). There are two reasons for this. The first is because the material which is at a higher temperature is more plasticised (softer) which results in lower torque between

the tool and the weldment. The 100 rev/min increase in spindle speed therefore results in a smaller increase of energy input rate for the higher temperature welds. The second reason is that the weld zone temperature is higher for the high average spindle speed welds which results in a larger temperature gradient between the weld zone material and the surrounding material. The heat is therefore conducted away from the weld zone at a higher rate for the higher temperature welds.

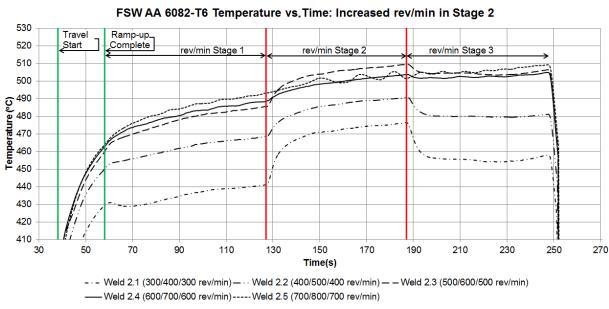


Figure 5.7. Increased spindle speed in stage 2

The graph of "Weld 2.1" (see Figure 5.7 and Figure 5.8) indicates that the increase of spindle speed (300 rev/min to 400 rev/min) in stage 2 causes a weld zone temperature increase, a spindle torque decrease and a spindle energy input rate increase. The total energy input rate of the weld is equal to the sum of spindle power and traverse axis power (rate of work done in the welding direction).

The weld is conducted at constant traverse speed (200 mm/min) which means that in stage 2, when the material temperature rises and the material softens, the traverse force (x-force) decreases, causing a decrease of traverse energy input rate into the weld. In order to quantify this amount, the traverse power decrease from stage 1 to stage 2 was calculated. The x-force average of "Weld 2.1" was taken between 100

seconds and 120 seconds for stage 1 and between 140 seconds and 160 seconds in stage 2. The power for each stage is calculated using Equation 5.1.

$$P_t = f_x \times \frac{t_s}{60}$$
 Equation 5.1

where

$$P_t$$
is the traverse power (J/s) f_x is the force in the welding direction (kN) t_s is the weld traverse speed (mm/min)

Equation 5.1 is derived from the law that energy (work done) is equal to the product of force and displacement. The results of the power calculations are shown in Table 5.1.

Stage	Data range (s)	Average x-force (kN)	Average traverse power (J/s)
1	100 to 120	4.27	14.23
2	140 to 160	3.88	12.93

 Table 5.1. Weld 2.1 traverse power data for stage 1 and stage 2

From stage 1 to stage 2, the traverse energy input rate decreased by 1.3 J/s. This decrease is small relative to the increase of spindle energy input rate in stage 2 of the weld. The change in total energy input rate introduced in stage 2 of weld 2.1 (see Figure 5.8) can therefore be approximated by the change of spindle energy input rate.

The spindle power is equal to the product of spindle torque and spindle angular velocity. In stage 2, the increase of angular velocity outweighs the decrease of torque in the product calculation resulting in an overall increase in spindle power (spindle energy input rate).

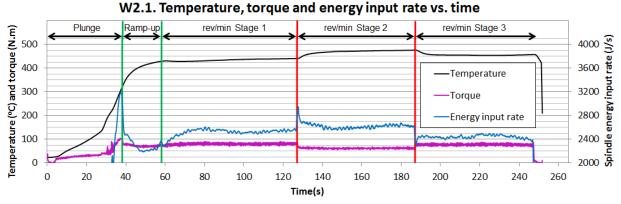
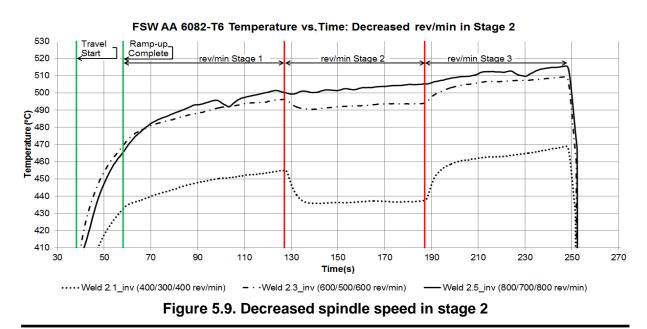


Figure 5.8. W2.1. Spindle energy input rate, torque and temperature versus time

For closer inspection of the weld zone temperature behaviour of "Weld 2.1", refer to Figure 5.7.

The graphs in Figure 5.9 show that for low spindle speed welds, the spindle speed decrease of 100 rev/min in stage 2 results in a larger temperature decrease than for the higher spindle speed welds. The reasoning is the same as for increasing spindle speed in stage 2 (see the discussion around Figure 5.7). The spindle torque at low weld zone temperature is larger than for high weld zone temperature. This results in a larger energy input rate decrease for a set amount of spindle speed decrease (100 rev/min in this case).



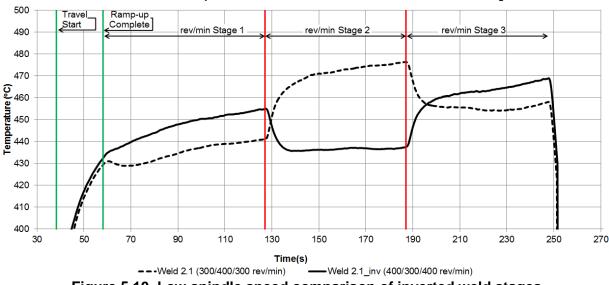
The following two figures (Figure 5.10 and Figure 5.11) show a comparison of welds executed with inverted spindle speed stages as per Table 5.2.

Weld	Spindle speed	Spindle speed	Spindle speed	Figure
number	stage 1	stage 2	stage 3	showing weld
Humber	(rev/min)	(rev/min)	(rev/min)	temperature
2.1	300	400	300	Figure 5.10
2.1_inv	400	300	400	
2.3	500	600	500	Figure 5.11
2.3_inv	600	500	600	

 Table 5.2. Weld stage speeds (inverted welds)

"Weld 2.1" achieved a considerably higher temperature than "Weld 2.1_inv" in stage 2. From the weld graphs it is clear that this would remain the case if "Weld 2.1_inv" did not experience the decrease of spindle speed in stage 2. The effect is explained by the positive energy input rate spike at the beginning of stage 2 of "Weld 2.1" which can be seen in Figure 5.8. At the end of stage 1, the spindle torque is approximately constant. The moment at which the spindle speed is increased, the energy input rate (product of torque and angular velocity) spikes because the spindle torque is high (from stage 1) and the spindle speed suddenly increases (to the value for stage 2). The temperature of the material then increases causing a decrease of spindle torque. The energy input rate therefore decreases as the weld progresses in stage 2.

The same principle applies for "Weld 2.1_inv" which experiences a spike decrease in energy input rate as it enters stage 2. The spindle torque is low due to the higher temperature in stage 1 and the sudden decrease of spindle speed (to the value for stage 2) causes the spike decrease in energy input rate. The material therefore cools dramatically. This causes an increase of spindle torque and the energy input rate therefore increases after the spike decrease.



FSW AA 6082-T6 Temperature vs. Time: 300 and 400 rev/min Inverted Weld Stages

Chapter 5 Temperature Control Design and Verification

Figure 5.10. Low spindle speed comparison of inverted weld stages

"Weld 2.3" and "Weld 2.3_inv" (see Figure 5.11) are conducted at higher spindle speeds than "Weld 2.1" and "Weld 2.1 inv". The effect observed in the comparison of "Weld 2.1" and "Weld 2.1_inv" is evident in the comparison of "Weld 2.3" and "Weld 2.3 inv", although the magnitude of the temperature changes in stage 2 are smaller. The main cause is the smaller spindle torque difference between these two welds due to their higher weld zone temperatures (relative to "Weld 2.1" and "Weld 2.1_inv").

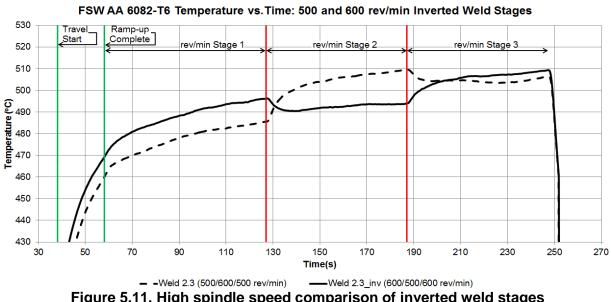


Figure 5.11. High spindle speed comparison of inverted weld stages

The effect observed in Figure 5.10 and Figure 5.11 suggests that the temperature dynamics of FSW are not linear. The full set of weld graphs for this section can be seen in **Appendix D**.

5.3. Algorithm Development

The control architecture implemented in this study for temperature control of FSW consisted of a "Proportional Integral Derivative" (PID) controller. The system was tuned at a certain temperature (492°C). The performance of the control system was assessed at various welding temperatures ranging from 480°C to 530°C. Should the control architecture have been found to be unsuitable for FSW because of non-linearity of FSW temperature dynamics, a modified PID control architecture would have been implemented. This architecture would consist of scheduled gains where the system is tuned at various welding temperatures. The P, I and D gains obtained from the tuning would be placed in a matrix of controller gains versus temperature. According to the operating point of the system, linear interpolation is executed and the appropriate controller gains are selected for the controller as the control algorithm is executed. Should this architecture have been insufficient for FSW, alternative control structures would have been tested such as fuzzy logic and genetic algorithms.

PID control is considered by various researchers as insufficient control for FSW temperature because PID control requires that the dynamics of the system which it is controlling are approximately linear, which is not the case for weld zone temperature of FSW as shown in Section 5.2. Temperature of FSW relies on many process conditions. These conditions include spindle speed, traverse speed, forge force, the specific characteristics of the material being welded, heat dissipation into the backing plate, heat dissipation into the weldment clamps, heat dissipation into the tool and spindle head and other thermal disturbances. For the experiments conducted in this study, the traverse speed was kept constant at 200 mm/min, the forge force was constant at 20 kN, the material being welded originated from one aluminium sheet. The plate and clamp setup was identical for all welds being compared and the tool

geometry was not changed. Variations in external thermal disturbances were eliminated as far as possible and the thermal disturbances in the welds which specifically tested the control algorithm's disturbance rejection were maintained as consistent as possible. For these welds, thermal source and thermal sink disturbances were tested.

5.3.1. Control System Layout

The FSW process and temperature controller are shown in a control system diagram in Figure 5.12. The area demarcated by the dotted outline includes the physical FSW process together with all thermal disturbances, the thermocouple sensors, telemetry rotor and spindle drive (which receives the spindle speed command from the machine PLC and controls the servo motor accordingly). The process output regarding this study is weld zone temperature. The temperature measurements are sent from the rotating tool via the telemetry system which generates a 0 V to 10 V analog signal (for each thermocouple sensor). This analog signal is converted to a digital value via the PLC analog input card. The control algorithm is demarcated by the solid red outline in Figure 5.12. The algorithm was written on the FSW machine's main PLC. The temperature control algorithm uses the operator's temperature set-point (as well as a nominal spindle speed setting) command and the temperature feedback signal to generate a temperature error. This error is used in the PID control calculations (together with the PLC cycle time and various other parameters stored in memory) to calculate the spindle speed command required to drive the system towards zero error between the set-point and the feedback signal.

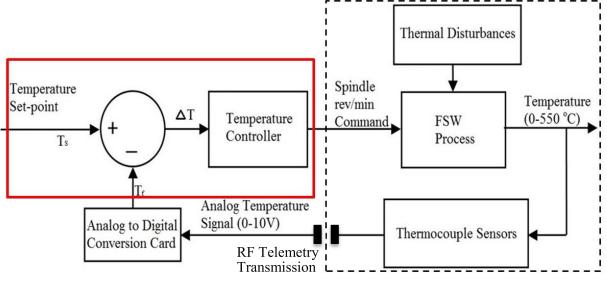


Figure 5.12. Control system diagram

The digital values (generated by the analog to digital conversion cards) representing the temperature feedback signal voltages are converted to temperature values according to their individual curve fit equations found from the thermocouple calibration process (see **Appendix A**).

5.3.2. Control Algorithm

Refer to the PID algorithm flow diagram shown in Figure 5.13, bearing in mind that the procedure is executed every program cycle of the PLC (one millisecond). The temperature control algorithm calculates the error term by subtracting the temperature feedback signal (average of the two thermocouples) from the operator set-point. The proportional term is calculated as the error term multiplied by the proportional gain (Kp). The integral term is a summation over time and is calculated by adding the product of the integral gain (Ki), PLC cycle time (dt) and the error term to the integral sum as it was after the previous program cycle. The derivative term is usually calculated as the rate of change of the error term although a sudden change in set-point will cause a spike in the derivative term. In this study, the derivative term is calculated as the rate of change of the temperature feedback signal. The only difference is that the rate of change of the temperature feedback signal is opposite in

sign to the rate of change of the error term and a sudden change in set-point will not generate a derivative spike. The derivative term is calculated as the difference between the temperature feedback signal and what the temperature feedback signal was in the previous program cycle, divided by the time over which the change took place (which is the PLC cycle time dt) and the quotient is multiplied by the derivative gain (Kd). The spindle speed command sent to the spindle drive is calculated as the sum of the nominal spindle speed value (estimated by the operator for the particular temperature set-point), the proportional term and the integral term; and the derivative term is subtracted from the sum (subtracted because of its sign which is determined as previously explained in this paragraph).

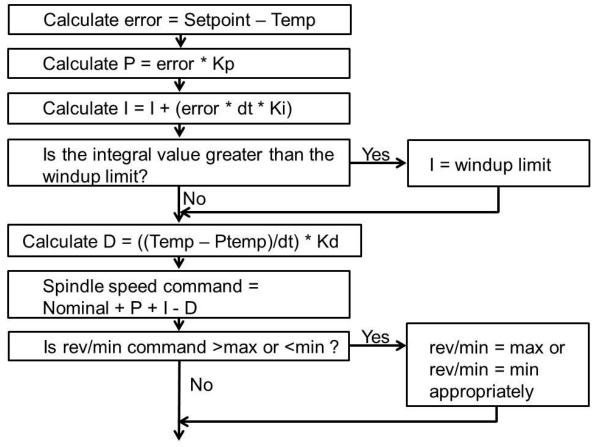


Figure 5.13. PID flow diagram

Should the error term be large and the system require a large amount of time to reach the set-point, the integral term could wind-up to a large value which would require a large amount of time to unwind after the system overshoots the set-point. This would magnify the amount which the system overshoots the set-point and the amount of time which is required to return the system to the set-point. A wind-up limit is therefore employed after the calculation of the integral term. If the integral term exceeds the wind-up limit (in either direction), the integral term is set equal to the wind-up limit which it exceeded. The nominal spindle speed value could be made unnecessary if the wind-up limit is set sufficiently large although this would degrade the system performance regarding set-points for which the system requires a relatively large amount time to realise. It is also important to avoid setting the wind-up limit too low. The main purpose of the integral term is to eliminate steady state error. Setting the limit too low could cause the system to be unable to eliminate any steadystate error. For this study, each unit of the integral term corresponds to 1 rev/min in the spindle speed command. The wind-up limit which worked well was 150 rev/min (in either direction depending on the sign of the error term). This meant that the nominal value set by the operator for the particular temperature set-point needed to be within 150 rev/min of the actual spindle speed required to maintain the set-point temperature. See Appendix E, page E-1 to page E-4 for the PLC code.

5.3.3. Ziegler Nichols Tuning Method^[3]

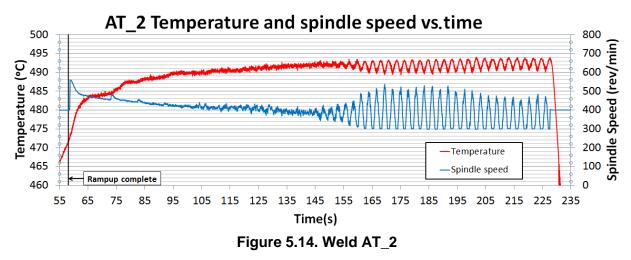
Refer to **Appendix E** for the set of algorithm tuning weld graphs. In order to determine appropriate Kp, Ki and Kd gains for the control system, the Ziegler Nichols tuning method^[3] was utilised. The procedure is conducted in the following manner^[3]:

- 1. Set Kp, Ki and Kd gains to zero.
- 2. Begin a weld with a specific temperature set-point (492°C was used).
- 3. Slowly increase Kp until the ultimate gain value (Ku) reached, where the system output (temperature) oscillates with constant amplitude.
- 4. Measure the oscillation period (Tu).
- 5. Calculate PID controller gains according to Equation 5.2 to Equation 5.4.

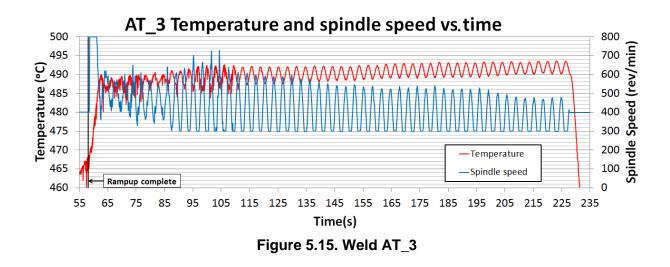
Kp = 0.6Ku	Equation 5.2 ^[3]
Ki = (2Kp) / Tu	Equation 5.3 ^[3]
Kd = (Kp x Tu) / 8	Equation 5.4 ^[3]

Step 3 increases the proportional gain until the system becomes undamped. Damping of a PID controlled system originates from two components of the system: the physical damping of the process being controlled and the damping added by the derivative term of the controller. The Ziegler Nichols tuning method ^[3] identifies sufficient system characteristics necessary to calculate appropriate controller gains. The inverse of the output oscillation period is equal to the natural frequency of the system and the critical gain is the maximum controller gain which can be set before the actuator (spindle in this case) would drive the system into an unstable condition. Increasing the proportional gain (with Ki and Kd gains equal to zero) effectively adds driving force to the system which overcomes the physical damping of the process (because zero derivative gain infers that the controller does not add any damping to the system is effectively cancelled by the driving force generated by the proportional component of the controller. This critical value for the proportional gain is therefore representative of the physical damping in the system.

The live view of temperature was monitored on the machine's human machine interface (HMI) for step 3. After step 1, step 2 and step 3, the weld data was plotted, which is shown in Figure 5.14.



Close to constant oscillation was observed near the end of "Weld AT_2". "Weld AT_3" was begun with the proportional gain set as it was at the end of "Weld AT_2". This second tuning weld was conducted so that the researcher could obtain the critical gain more accurately. The graph for "Weld AT_3" is shown in Figure 5.15.



The ultimate gain (Ku) was found to be 63.5 and from the graph, the period of the oscillation (Tu) was found to be 3.2059 s. The PID gains were calculated according to the Ziegler Nichols equations:

Кр	= 0.6Ku	= 0.6 x 63.5	= 38.1	Equation 5.5 ^[3]
Ki	= (2Kp) / Tu	= (2 x 38.1) / 3.2059	= 23.769	Equation 5.6 ^[3]

Kd = $(Kp \times Tu) / 8$ = $(38.1 \times 3.2059) / 8$ = 15.268 Equation 5.7^[3]

5.4. Algorithm Performance Testing

The parameters determined by the Ziegler Nichols tuning ^[3] where implemented in the control algorithm. "Weld AT_4" was done to test the performance of the control system given step input changes which include a rise to 491°C, after stabilisation, another step change to 541°C is introduced. This tests the heating to a set-point response of the system. The set-point then steps back down to 491°C in order to test the cooling to a set-point response of the system. The system. The integral wind-up limit was initially set high in order to allow the integral to behave approximately as it would have if there were no wind-up limit employed (set to 800 rev/min).

In Figure 5.16, it can be seen that for increasing temperature, the temperature control algorithm utilised maximum allowed spindle speed for both the low and high temperature set-points although the system required more time to achieve the higher set-point than the lower set-point. This is related to the rate of transfer of heat energy into and from the weld zone. Energy input rate depends on a number of process conditions. Three important factors include material plasticised condition (hard/soft affecting spindle torque), the spindle speed and the rate of heat conduction from the weld zone into the surrounding material. Regarding the low temperature set-point, the material is relatively cool, corresponding to high spindle torque required to maintain spindle speed. Increasing the spindle speed to the maximum limit at this temperature corresponds to a high energy input rate, allowing the weld zone temperature to approach the set-point at a high rate of change of temperature. On the contrary regarding the high temperature set-point, when the material is at a higher temperature, the material is more plasticised (softer) which corresponds to lower spindle torque. Energy input rate therefore decreases as temperature increases for a constant spindle speed (in this case 800 rev/min). The weld zone temperature therefore approaches the set-point at a lower rate of change of temperature for higher temperature set-points (as the spindle speed is limited to 800 rev/min). In addition to

this, as temperature in the weld zone increases, the rate of conduction of heat from the weld zone into the surrounding material increases according to the heat transfer equation (see Equation 5.8 ^[19]). This effect reduces the rate of change of temperature when the system approaches high weld zone temperatures.

$$\dot{Q} = k \times A \times \frac{\Delta T}{L}$$
 Equation 5.8^[19]

where

- \dot{Q} is the heat energy flow rate (W or J/s).
- k is the thermal conductivity of the material (W/m.°C or J/m.°C.s).
- A is the area (m^2) of the material through which the heat conducts.
- ΔT is the temperature difference (°C) over distance *L*.
- L is the distance (m) along the path of heat conduction over which the temperature drop ΔT is realised.

$$\alpha = \frac{k}{\rho c_{p}}$$
 Equation 5.9^[19]

where

- α is the thermal diffusivity (m²/s) of the material.
- k is the thermal conductivity of the material (W/m.°C or J/m.°C.s).
- ρ is the density (kg/m³) of the material.
- c_p is the specific heat (J/kg.°C) of the material.

Equation 5.9 can be substituted into Equation 5.8 and then by integrating both sides of the equation with respect to time, the commonly known heat law (see Equation 5.10) can be derived. This shows that Equation 5.8 conforms to the heat law in Equation 5.10.

 $Q = m \times c_p \times \Delta T$

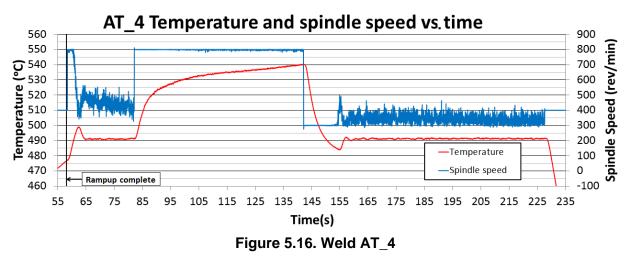
Equation 5.10

where

- Q is the amount of heat energy (J) required to change the material's temperature by ΔT .
- m is the mass (kg) of the material.
- c_p is the specific heat (J/kg.°C) of the material.
- ΔT is the temperature change of the material (°C).

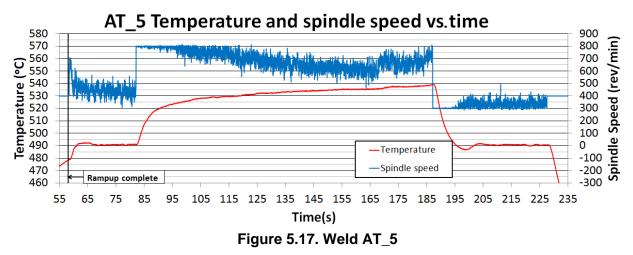
Considering Equation 5.8, the material's thermal conductivity (k) is approximately constant for the welding temperature range ^[19], the area (A) of the material through which heat is conducted from the weld zone is approximately constant, the length (*L*) between the weld zone and the surrounding material is constant, although the temperature gradient between the material in the weld zone and the surrounding material increases. This constitutes an increase in the rate of heat conducted away from the weld zone.

The longer time delay for the system to reach the high temperature set-point is thus explained by the decreasing energy input rate into the weld zone material and increasing heat energy output rate from the weld zone material as the weld zone temperature increases.



"Weld AT_4" yielded good response although the overshoot was relatively excessive (7.96°C) for the low temperature set-point. The high temperature set-point was achieved by the system at approximately the same time at which the set-point was programmed to revert to the low value. The steady state control was therefore not tested at the high temperature set-point in this weld.

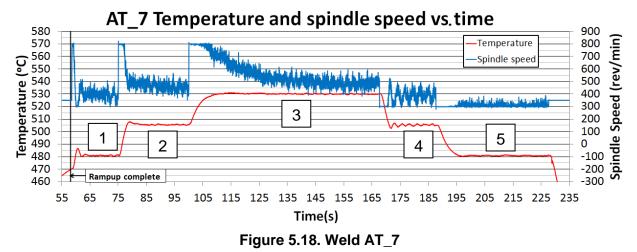
The high temperature set-point was maintained for a longer duration in "Weld AT_5" (see Figure 5.17) to allow the system more time to achieve the temperature set-point. In addition to this, the wind-up limit for the integral was decreased to 100 rev/min in an effort to reduce the overshoot. This decrease in the wind-up limit worked well for decreasing the overshoot for the low temperature set-point although it caused the spindle speed to reduce from the maximum (800 rev/min) prematurely for the high temperature set-point (weld temperature was approximately 16°C below the set-point when the spindle speed began to reduce).



From "Weld AT_4", it can be seen that when the system is at 491°C and the spindle is driven to the maximum speed of 800 rev/min, the weld zone temperature requires approximately 60 seconds to achieve the set-point of 540°C. No controller would be able to improve on the duration without an increased spindle speed limit.

From "Weld AT_4" it can be seen that a high set-point of 530°C would be achievable by the system in a more appropriate amount of time. From AT_4 the amount of time required for the system to achieve 530°C from 491°C would be approximately 17 seconds. This is reasonable considering that 530°C is the maximum temperature which the system is required to achieve.

An intermediate set-point was introduced for "Weld AT_6" onward. The set-points for heating and cooling are 481° C, 506° C and 530° C. "Weld AT_6" and "Weld AT_7" are essentially the same except that "Weld AT_7" has a reduced duration for maintaining the high temperature set-point in order to allow time for stabilisation after cooling to the final temperature set-point (see **Appendix E** for "Weld AT_6"). "Weld AT_7" is shown in Figure 5.18.



"Weld AT_7" shows that despite the fact that the system was tuned at 492°C (and assuming non-linearity of FSW temperature dynamics), the control system performance at all temperatures was acceptable and implementation of alternative control methods was not necessary.

The steady state error is defined for this system (with unitary feedback signal) as the difference between the output (measured temperature) and the set-point (operator defined) during steady state condition. The steady state error is approximately zero in all regions. This confirms that the nominal spindle speed value set by the operator was sufficiently accurate (within the integral wind-up limit of 150 rev/min) and the integral component of the controller effectively eliminated any error. There is an inherent steady state oscillation about the temperature set-point. The amplitudes of the steady state oscillation of temperature about the set-point in the five constant temperature regions (labelled in Figure 5.18) are as follows:

- Region 1 (481°C) : ≤ 1.13°C
- Region 2 (506°C) : ≤ 1.08°C
- Region 3 (530°C) : ≤ 0.89°C
- Region 4 (505°C) : ≤ 1.43°C
- Region 5 (481°C) : ≤ 0.70°C

Comparing region 2 and region 4, it is clear that the system does not behave linearly for heating versus cooling. The statistical data for the steady state temperature was determined using Microsoft Excel's data analysis tool. Table 5.3 shows the results. See **Appendix F** for the set of recorded data.

Region 2				
Mean		t-	Standard	Uncertainty
(°C)	n	critical	deviation	(95%)
505.5401	901	1.96	0.2802	0.0183

Region 4				
Mean (°C)	n	t- critical	Standard deviation	Uncertainty (95%)
505.4541	601	1.96	0.5540	0.0443

Table 5.3. AT_7 region 2 and region 4 statistics

The standard deviation of the temperature data in region 4 is greater than the standard deviation in region 2. The only difference in the process conditions is the position on the plate and the noticeably lower spindle speed required (in region 4) to maintain steady state condition at the set-point temperature. A plausible reason for the difference is that the temperature of the material surrounding the weld zone is higher in region 4 than in region 2 (because region 4 is nearer to the end of the weld and the previous region consisted of a higher temperature set-point) which causes a change in the dynamic characteristics of the process temperature. If the temperature of the material surrounding the weld zone is higher and the temperature of the weld zone is higher and the temperature of the weld zone is higher and the temperature of the weld zone is higher and the temperature of the weld zone is higher and the temperature of the weld zone is the same in both regions, region 4 has a smaller thermal gradient conducting heat away from the weld zone into the surrounding material. The steady state oscillation about the set-point was considered acceptable in both regions.

The researcher investigated the cause of the high frequency spindle speed oscillation observed in "Weld AT_4"; "Weld AT_5"; "Weld AT_6" and "Weld AT_7". The proportional, integral and derivative terms were logged during the "Weld AT_7". From

the highlighted consecutive derivative values (separated by 20 milliseconds) in the extract shown in Table 5.4, it is clearly seen that the derivative term is the cause of the high frequency oscillation in the spindle speed. See **Appendix G** for additional control data.

Weld AT_7 control data					
time	Error	Proportional	Integral	Derivative	
145	-0.209297829	-7.974247282	-77.51202686	-744.7299345	
145.02	-0.195362155	-7.443298098	-77.61429075	43.96846569	
145.04	0.054693154	2.083809173	-77.64164141	22.82852918	
145.06	0.084432622	3.216882896	-77.62047917	27.74369669	
145.08	0.03042704	1.159270224	-77.60618563	29.46189609	
145.1	0.055476033	2.11363687	-77.60854255	-651.005971	
145.12	-0.005938994	-0.226275684	-77.60114914	165.1760844	
145.14	-0.117756535	-4.48652399	-77.64014694	290.1891286	
145.16	-0.235592413	-8.976070924	-77.71049024	536.2552022	
145.18	-0.495768065	-18.88876326	-77.90437087	-390.0417655	
145.2	-0.440249792	-16.77351709	-78.11738189	718.0757328	
145.22	-0.235462059	-8.971104435	-78.26161222	-383.5979499	
145.24	-0.136298411	-5.192969446	-78.36122699	-570.9418116	
145.26	-0.050518967	-1.924772639	-78.41474566	-62.57417464	
145.28	-0.027406962	-1.04420524	-78.40451387	160.3911832	
145.3	-0.014260929	-0.543341395	-78.42947947	-508.3646151	
145.32	- 0.081256285	-3.095864444	-78.4646832	29.46391926	

 Table 5.4. AT_7 control data

Research on filtering the derivative term was conducted. In chapter 10, Section 10.5 of "Feedback Systems" ^[9], derivative filtering is addressed. The reason for employing this filter is because the derivative term in the PID controller has high gain for high rates of change of temperature ^[9]. If the temperature feedback signal contains noise, the derivative term performs as if the system is experiencing high rate of change of temperature (which is not the case). If two consecutive samples of the feedback signal happen to occur on a trough then a peak of the noise, the derivative term attempts to damp the high positive rate of change of the feedback (induced by noise and not temperature change of the system) with a high derivative term output. Conversely, if the two consecutive samples happen to fall on a peak, then a trough,

the derivative term changes sign (and magnitude) because according to the two samples, the rate of change of temperature is high in a negative direction. This explains the high magnitude alternating derivative terms highlighted in Table 5.4. The majority of the noise generated on the thermocouple signals by the electric spindle was filtered out successfully, although it was not eliminated completely. The small amount of noise remaining on the thermocouple signals is amplified by the derivative term such that it creates a considerable change to the spindle speed.

Implementing the derivative filter replaces the normal derivative term (Equation 5.11) with Equation 5.12.

$$D_1 = Kd \times dT/dt$$
 Equation 5.11

Where	D_1	is the normal derivative term.
	Kd	is the derivative gain.

dT/dt is the rate of change of temperature.

$$D_2 = Kd \times \frac{\frac{dT}{dt}}{1 + \frac{(dT) \times (\frac{Kd}{Kp})}{N}}$$
Equation 5.12^[9]

Where	D_2	is the filtered derivative term.	
	K_p	is the proportional gain.	
	Ν	is the filter factor (selected $2 \le N \ge 20$).	

The filter works on the principle that if $\frac{dT}{dt}$ is small, the denominator approximates unity and the derivative term generated is equivalent to the normal derivative in Equation 5.11. If $\frac{dT}{dt}$ tends toward infinitely large, the derivative term approximates Equation 5.13.

$$D = \frac{Kd}{(\frac{Kd}{Kp})/N} = Kp \times N$$

The response of the filtered derivative versus rate of change of temperature was plotted. The approximate maximum rate of change of temperature which occurs in the system was determined from "Weld AT_7" (see Figure 5.19) to obtain a suitable range for plotting the derivative filter response.

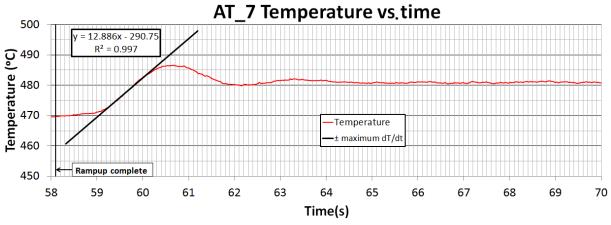
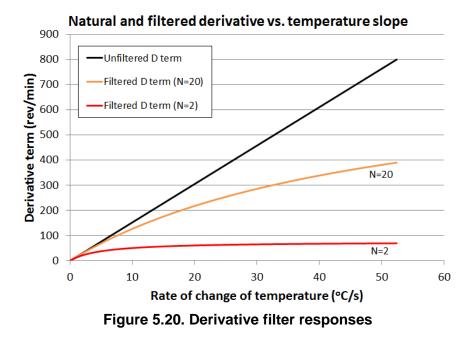
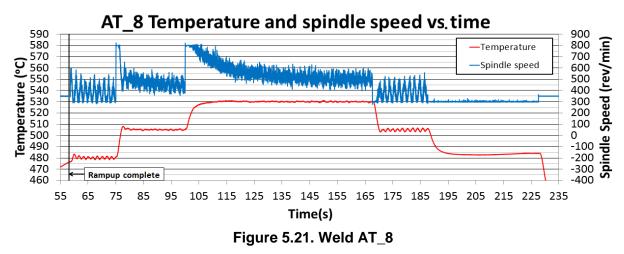


Figure 5.19. AT_7 maximum rate of temperature change

The maximum rate of change of temperature is approximately 12.9° C/s (from Figure 5.19). Rate of change of temperature considerably above this value should generate an attenuated derivative term. Using the Kp and Kd terms calculated in Section 5.3.3, the unfiltered derivative and filtered derivative responses (for N = 2 and N = 20) versus rate of change of temperature are plotted in Figure 5.20.



From Figure 5.20 it can be seen that implementing the filter with N = 2 generates the most attenuation for high rate of change of temperature although rate of change of temperature from approximately 3°C/s to 12.9°C/s generated considerably attenuated derivative terms compared to the unfiltered derivative term. Attenuating the derivative term considerably in the operating range of the process could cause the system to respond undesirably because the derivative gain calculated from the tuning of the controller would no longer generate the required derivative term regarding magnitude necessary for damping the system. Implementing the filter with N = 20 generates a derivative term similar to the unfiltered derivative up to 12.9°C/s. "Weld AT_8" (shown in Figure 5.21) tested the filter with N = 20.



Comparison of "Weld AT_7" and "Weld AT_8" shows that the filter has not improved the high frequency oscillation of the spindle speed. Since the objective of the control system is to control the temperature to match the set-point (which has been achieved by this system), the excessive actuator (the spindle in the context of this study) oscillation could be considered unimportant. On the contrary, the excessive actuator oscillation could be important when considering factors such as energy consumption and actuator wear. Investigation of these factors was not within the scope of this study.

The researcher modified the filter in Equation 5.12^[9] in order to increase the attenuation of the derivative term generated from high rate of change of temperature whilst approximately maintaining unchanged damping for the operating range of the process. The modified filtered derivative is shown in Equation 5.14.

$\left.\frac{Kd}{Kp}\right)\Big/_{N}$	Equation 5.14
) ₃	is the modified filtered derivative term.
Кp	is the proportional gain.
(d	is the derivative gain.
V	is the filter factor (N is unlimited).
) ₃ Xp Xd

JT

Adding the power r to the $\frac{dT}{dt}$ term in the denominator causes the denominator to increase faster than the numerator (provided r > 1) as the rate of change of temperature increases, causing the derivative term to decrease. D_3 approximates the normal derivative (in Equation 5.11) when $\frac{dT}{dt}$ is small which is the same value as D_2 for small $\frac{dT}{dt}$. However, if $\frac{dT}{dt}$ tends toward infinitely large, the derivative term approximates zero as shown in Equation 5.15.

$$\lim_{\substack{dT\\dt\to\infty}} D_3 = \lim_{\substack{dT\\dt\to\infty}} \left(\frac{Kd \times \frac{dT}{dt}}{\left(1 + \frac{(dT)}{dt}\right)^r \times (\frac{Kd}{Kp})} \right) = \lim_{\substack{dT\\dt\to\infty}} \left(\frac{N \times Kp}{(\frac{dT}{dt})^{r-1}} \right) = 0 \quad (r > 1)$$

Equation 5.15

Increasing the r term creates a sharper cut-off on the response curve although it decreases the magnitude of the derivative response curve for all rates of change of temperature. It is then required that the N term be increased so that the derivative term is not attenuated considerably in the operating range of the system (zero to 12.9° C/s in this case). Implementation of this filter should be done with caution because setting the N term too low and the r term too high for the system characteristics, the derivative term could provide insufficient damping in the operating range of the system. This could cause the system to become unstable.

The derivative responses (for two settings of *r* and *N*) versus rate of change of temperature $\left(\frac{dT}{dt}\right)$ are shown in green in Figure 5.22. The filters from Figure 5.20 are retained in the figure for comparison.

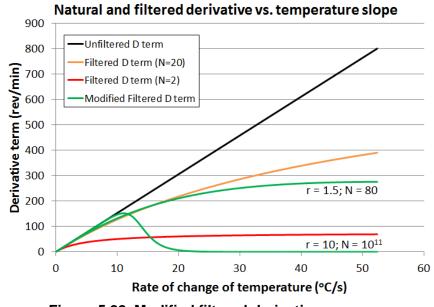


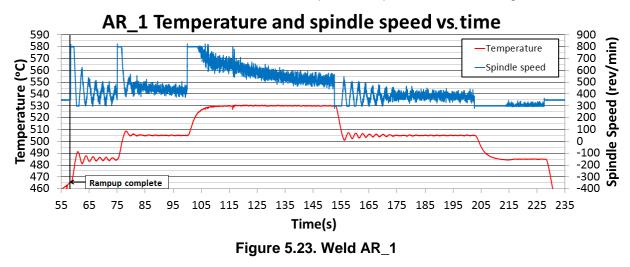
Figure 5.22. Modified filtered derivative response

The filter was tested in "Weld AT_9"; "Weld AT_11"; "Weld AT_12"; "Weld AR_1" and "Weld AR_2" (see **Appendix E**) with the following parameters:

Weld number	r	N
AT_9	1.5	80
AT_12	2	30
AT_11	2.5	300
AR_1	2.5	300
AR_2	10	10 ¹¹

Table 5.5. Filter parameters

The two welds showing the least spindle oscillation was "Weld AT_11" and "Weld AR_1". The spindle speed oscillation amplitude in the 530°C region improved from approximately 100 rev/min in "Weld AT_7" (see Figure 5.18) to approximately 75 rev/min in "Weld AT_11" and approximately 60 rev/min in "Weld AR_1" (see Figure 5.23).



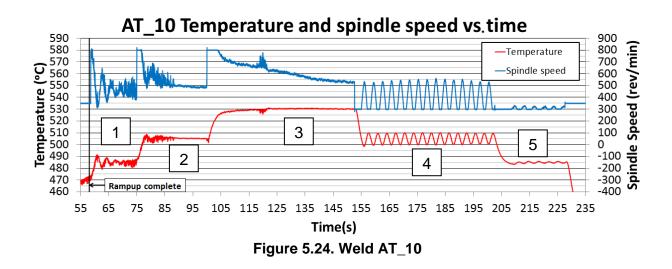
The Ziegler Nichols tuning method ^[3] contains a number of gain calculation sets for different controller options. Two of which are classic PID (implemented in the majority of the welds in this study as per the gain settings in Section 5.3.3) and PI (tested in "Weld AT_10"). A reason for which PI control would be implemented instead of PID control is that in some cases, the process does not require the derivative component because the uncompensated system naturally contains sufficient damping to limit overshoot of the set-point (provided the PI gains are not set too aggressively).

In comparison to the calculations for PID control, the gains for PI control are calculated less aggressively from the ultimate gain and oscillation period found in step 3 and step 4 of the Ziegler Nichols tuning method ^[3] (see Section 5.3.3). The main reason for this is because the controller does not add damping to the system as PID control does with the derivative term. The Kp and Ki gains therefore need to be set low enough in order to avoid excessive output oscillation and the system becoming unstable. The gains are calculated in Equation 5.16 and Equation 5.17.

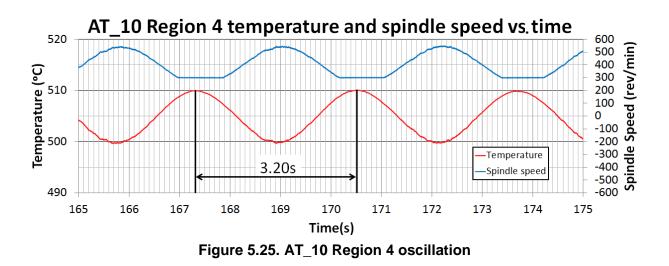
Kp	= 0.45 * Ku	= 0.45 * 63.5	= 28.58	Equation 5.16 ^[3]
Ki	= (1.2 * Kp) / Tu	= (1.2 * 28.58) / 3.2059	= 10.70	Equation 5.17 ^[3]

The PI controller was tested in "Weld AT_10" (see Figure 5.24). From "Weld AT_10", the spindle speed graph during steady state condition in region 3 confirms that the

derivative term is the cause of the excessive spindle speed oscillation during steady state condition in the previous welds such as "Weld AT_7". The PI control system performed acceptably in all regions except region 4.



Closer inspection of "Weld AT_10" region 4 (see Figure 5.25) shows that the oscillation period matches the oscillation period of the tuning "Weld AT_3" (see Figure 5.15). The system oscillates at its natural frequency. This oscillation of temperature is an indication of an undamped system.



5.5. Process Model (MATLAB)

5.5.1. System Transfer Function Identification

The System Identification (SID) Toolbox in Matlab (called with the ">>ident" command in the Matlab workspace) was used to generate a process model fit based on the data imported into Matlab from a file containing experimental input and output data.

In order to obtain weld data representing the dynamics of the temperature of the FSW process, exclusive of the controller, the temperature control is disengaged. This is therefore the open loop temperature response of the system given a specific spindle speed input. The experimental data was taken from "Weld 3.2" (see Figure 5.26). The open loop system was given a step command of 100 rev/min at approximately 127 seconds. Controller design considers system response to a step increase command on the input of the system. Only the step increase command data and the temperature response data is used for identification of the system model (or process transfer function). The data extract from the weld log ("Weld 3.2") which was imported into Matlab was taken from 90 seconds to 170 seconds into the weld.

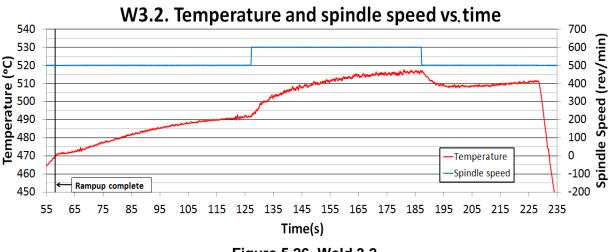
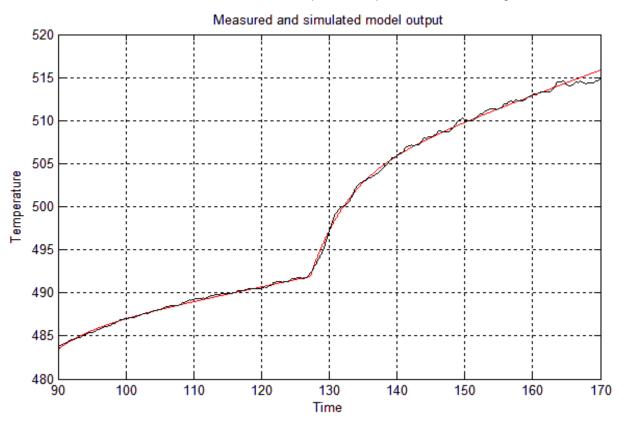


Figure 5.26. Weld 3.2

The Import data option under the "File" menu in Matlab was used to import the experimental data of weld "w3.2" from a Microsoft Excel Spreadsheet. See **Appendix H** for the temperature and spindle speed versus time graphs for weld set "w3.x". The spreadsheet contained a spindle speed command column, a temperature output column and a time column. Vectors were created for the spindle input command (named: "rpmCommand") and the temperature response (output named: "temperature"). The SID tool's data import function imports the vectors for input and output data from the matlab workspace. The SID toolbox user interface and import data dialog box can be seen on **page I-1 in Appendix I**.

Second and third order linear parametric models were generated. A second order linear parametric model estimation of the system was found to be acceptable. The model fit to the experimental data was 97.27 percent. In Figure 5.27, the red graph series (smoother of the two graphs) is the model fit to the experimental data (irregular, black graph).



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Figure 5.27. Second order model fit

The model was then dragged to the LTI viewer in the SID toolbox user interface (see **Appendix I, page I-2**) from which the transfer function of the model is exported to the Matlab workspace. The transfer function generated by the SID toolbox is a discrete transfer function (it was generated based upon discrete experimental data with 0.02 seconds sampling time). The Automatic Control Systems (ACSYS) toolbox was used to conduct the frequency design of the PID controller (see Section 5.5.2) for comparison with the PID controller found by the Ziegler Nichols tuning method ^[3] (see Section 5.3.3). The ACSYS toolbox requires a continuous transfer function in the input dialog box. The discrete transfer function model found from the SID toolbox was converted to an equivalent continuous transfer function using the ">>d2c()" Matlab command as shown in Figure 5.28.

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					Shortcuts 🛽 How to Add 🗶] What's New
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 A → ▼ ♪ → Name ▲ CarSim Controls and Statetool TFSymbolic VirtualLab Acsys.m acsys2.asv actxlicense.m hs_err_pid2328.log hs_err_pid4696.log hs_err_pid7176.log hs_err_pid7176.log hs_err_pid7176.log hs_err_pid7176.log hs_err_pid7248.log hs_err_pid7524.log TFcal.m TFsym.asv 	New to MATLAB? Watch this <u>Video</u> , see <u>Demos</u> , or read <u>Getting Started</u> . >> ident Opening System Identification Tool done. >> oe221 Transfer function from input "u1" to output "y1": 0.0004406 z - 0.0004405 z^2 - 1.996 z + 0.9963 Sampling time: 0.02 >> tf221=d2c(oe221) Transfer function from input "u1" to output "y1": 0.02207 s + 0.0002932 					

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Figure 5.28. Transfer function conversion

Verification that the continuous transfer function (labelled: "FSW Process" in Figure 5.29) is a good model of the physical FSW process, the model was simulated in Matlab Simulink with closed-loop PID control implemented. The gains found from the Ziegler Nichols tuning ^[3] of the physical system were implemented in the Simulink PID controller model. The Simulink control system model was given a step command from 481°C to 506°C at 75 seconds (into the simulation). This replicates the step command at 75 seconds in "Weld AT_7".

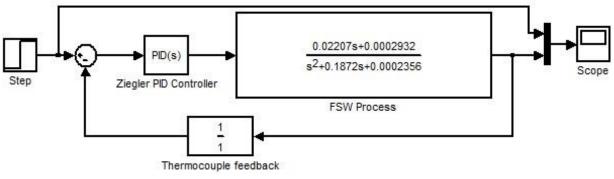


Figure 5.29. Simulink control system model

Referring to Figure 5.30 and Figure 5.31, the rise time of the control system (for a step command input) is denoted " t_r " and the settling time of the control system is denoted " t_s ". The percentage overshoot of the control system (for a step command input) is defined as the percentage of the step command magnitude by which the system response overshoots the set-point.

The temperature response of the model was compared to the physical temperature response of "Weld AT_7" and "Weld AR_1" (see **Appendix E, page E-19**) in the region of 70 seconds to 90 seconds. The simulation result is shown in Figure 5.30 and the corresponding extract from "Weld AT_7" is shown in Figure 5.31. The comparison of the results is shown in Table 5.6.

Weld/Simulation	Rise time (s)	Settling time (s)	% overshoot
Simulation	1.47	7.41	15.6
Weld AT_7	1.96	4.88	8.2
Weld AR_1	1.46	6.17	19.2

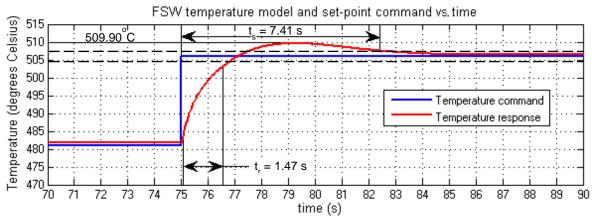


Figure 5.30. Simulink simulation of FSW control step command

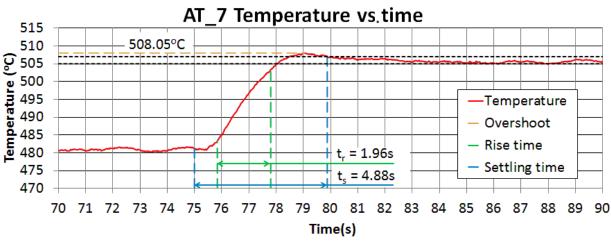


Figure 5.31. Weld AT_7 temperature response extract

The rise time of "Weld AT_7" is 0.49 seconds longer than the rise time of the simulation. The overshoot of the weld is 7.4 percent less than the overshoot of the simulation. These two observations indicate that the weld temperature control system exhibits more damping than the simulated model.

The damping ratio was calculated for each instance in Table 5.7. The model transfer function was of second order. "Automatic Control Systems" ^[20] provides an equation for calculating the overshoot for a second order system from the system damping ratio ζ (see Equation 5.18). Overshoot was obtained from the experimental results, so the equation can be manipulated to calculate the damping ratios (see Table 5.7).

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$$-\pi\zeta/\sqrt{1-\zeta^2}$$

 $\% \ overshoot = 100e$

Equation 5.18^[20]

From Equation 5.18, the damping ratio is made the subject of the formula as shown in Equation 5.19.

$$\zeta = \sqrt{\frac{\left[\ln\left(\frac{\% \ overshoot}{100}\right)\right]^2}{\left[\ln\left(\frac{\% \ overshoot}{100}\right)\right]^2 + \pi^2}}$$

Equation 5.19

Weld/Simulation	Damping ratio
Simulation	0.509
Weld AT_7	0.623
Weld AR_1	0.465

 Table 5.7. Damping ratios

To put the values from Table 5.7 into perspective; from control theory, a control system is classified as negatively damped if $\zeta < 0^{[20]}$, resulting in an unstable system; undamped if $\zeta = 0^{[20]}$, resulting in a system with constant oscillation; underdamped if $0 < \zeta < 1^{[20]}$ which results in a system which is stable and percent overshoot ranges from high to low as ζ moves from zero towards unity; critically damped if $\zeta = 1^{[20]}$ in which case the system approaches the set-point as fast as possible without any overshoot and overdamped if $\zeta > 1^{[20]}$, where the system exhibits no overshoot of the set-point although increasing ζ increases the rise time of the system ^[20]. Most control systems fall into the underdamped category for fastest response as well as acceptable overshoot.

The damping of the simulation model was found to be between the damping values of "Weld AT_7" and "Weld AR_1". The model can therefore be considered a reasonable representation of the system. Considering that a damping ratio of 0.7 is considered desirable for an acceptable trade-off between overshoot and rise time ^[20] and the

range which $\zeta = 0.7$ falls into $(0 < \zeta < 1)$, the damping ratios of the welds and simulation are reasonably close to each other.

5.5.2. Bode Diagram Frequency Design

Matlab's Automatic Control Systems toolbox (ACSYS) was used to design a PID controller for the FSW model via bode diagram frequency design. The model transfer function was entered into the G(s) process field in the ACSYS toolbox. Pages J-1 and J-2 of Appendix J show the process of entering the transfer function into ACSYS and opening the bode frequency diagram controller design tool. The openloop bode diagram of the system (i.e. controller gain equal to unity) opens when the bode frequency controller design tool is selected. The bode diagram showing the open-loop system bandwidth (taken from the -3 dB point on the magnitude graph) is 0.00185 rad/s as shown on page J-3 of Appendix J. The controller was then introduced with the design tool by adding the controller gain, poles and zeros to the frequency plot as illustrated by this section. Increasing the controller gain moves the bode diagram upward in order to increase the bandwidth of the system. The design then included PI control design (adds a pole at zero (in the s domain) which is considered an integrator and a zero to the plot) and then PD control design (adds a further zero to the plot). The zero of the PI design component was placed on the bode diagram and then moved left or right in order to manipulate the shape of the bode diagram and improve the stability margin. The zero of the PD design component was moved left or right in the bode diagram in order to improve the time response (closed-loop step response which is opened simultaneously with the bode diagram) of the system. The transfer function for a PID controller in the s domain takes the form of Equation 5.20^[20].

$$C(s) = Kp + \frac{Ki}{s} + Kd.s = \frac{Kd.s^2 + Kp.s + Ki}{s}$$
 Equation 5.20^[20]

where

C(s) is the controller transfer function.

- *Kp* is the proportional gain of the controller.
- *Ki* is the integral gain of the controller.
- *Kd* is the derivative gain of the controller.

In order to conduct the three controller design components (determine loop gain, PI design and PD design) separately, the controller transfer function needed to be modified in such a way that it becomes a product of the three appropriate components of the form of Equation 5.21^[20].

$$C(s) = (1 + K_{D1}s) \left(K_{P2} + \frac{K_{I2}}{s} \right) = \frac{K_{P2} \left(\frac{K_{I2}}{K_{P2}} + s \right) (1 + K_{D1}s)}{s}$$
$$= K_{I2} \frac{\left(1 + \frac{K_{P2}}{K_{I2}} s \right)}{s} (1 + K_{D1}s)$$
Equation 5.21^[20]

where

$$K_{I2}$$
corresponds to the controller loop gain. $\frac{\left(1+\frac{K_{P2}}{K_{I2}}s\right)}{s}$ corresponds to the PI control component zero $\left(1+\frac{K_{P2}}{K_{I2}}s\right)$ and integrator $\left(\frac{1}{s}\right)$. $(1+K_{D1}s)$ corresponds to the PD control component zero.

The relationships between the terms in Equation 5.20 and Equation 5.21 are described by Equation 5.22, Equation 5.23 and Equation 5.24.

$Kp = K_{P2} + K_{D1}K_{I2}$	Equation 5.22 ^[20]
$Ki = K_{I2}$	Equation 5.23 ^[20]
$Kd = K_{P2}K_{D1}$	Equation 5.24 [20]

The closed-loop unit step response with real time update is place next to the bode diagram as shown in Figure 5.32 and on **page J-4 in Appendix J**. As changes are made to the bode diagram, the step response automatically updates.

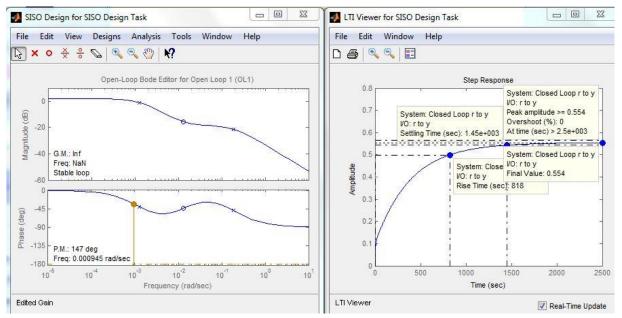
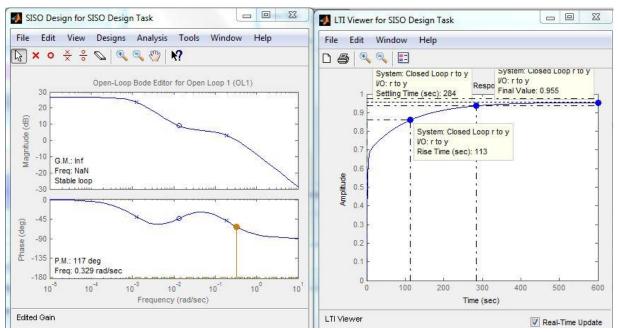


Figure 5.32. Open-loop bode and closed-loop step response

The unit step response in Figure 5.32 shows that the closed loop system without a controller (controller gain equal to unity) does not contain sufficient gain in order to drive the output to the set-point of unity (final value is 0.554). The bode diagram is moved upward in the controller design tool window using the computer mouse in order to increase the controller gain until the system step response is able to reach 95 percent of the set-point (see Figure 5.33 and **page J-5 of Appendix J**). After the integral term of the controller is added, the system will have no steady-state error (the system will reach 100 percent of the set-point).

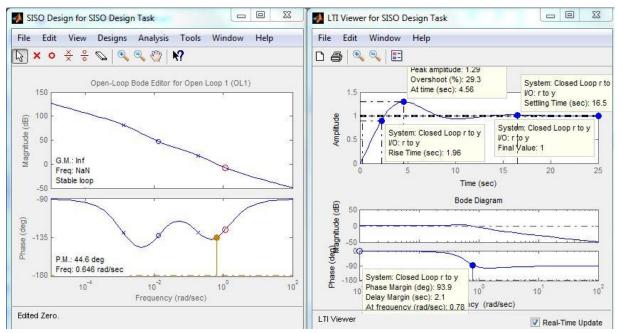


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Figure 5.33. Moved bode diagram and corresponding system step response

Changing to the compensator (controller) editor (see **page J-6 of Appendix J**), shows that moving the bode diagram upward has increased the controller gain from unity to 17.116. After the system had sufficient gain to be within reach of the set-point, the PI design component was added to the controller.

The PI control design component consists of adding the pole at s equal to zero (in the s domain) and adding a real zero which is moved in order to achieve the required phase margin on the closed-loop bode diagram of the system. The ACSYS controller design toolbox allows you to place and move poles and zeros in the open-loop bode diagram only. In order to design for a phase margin requirement on the closed-loop bode diagram, the closed-loop bode diagram is opened simultaneously with the open-loop bode diagram with live update enabled. After adding the integrator and the zero, the zero (red circle/the circle right of 1 rad/s in Figure 5.34 and **page J-7 of Appendix J**) was moved on the open-loop bode diagram in order to achieve a phase margin (stability margin) on the closed-loop bode diagram of greater than 90° which is considered a good design margin in control theory.



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Figure 5.34. Bode diagrams and step response after PI control design

Changing to the compensator (controller) editor (see **page J-8 of Appendix J**), shows that after placement of the zero, it's location in the s domain was s = -1.1377. After implementation of the PI component of the design, the PD component of the design was added.

The PD component of the controller design process increases the damping ratio of the system. Typically, the zero from the PI design and the zero from the PD design are placed close to each other on the bode diagram. The closed-loop step response (time domain) of the system was opened simultaneously with the bode diagram and live update enabled. This allows the researcher to visualise the effects which moving the zero have on the time response of the system. The zero of the PD component of the design was placed on the bode diagram near the zero placed during the PI component of the design. Moving the zero to the left improved the system overshoot although it degraded the settling time of the closed-loop step response. The purpose of this control system is to maintain the FSW temperature at the operator set-point. The beginning of the FSW process consists of the plunge and the ramp up stage during which the welding conditions are established. This region of the weld may

contain unacceptable mechanical properties and is therefore typically executed on a run-on tab which is later removed by a machining process. It was therefore decided that the temperature settling time is more important for this controller design than the temperature overshoot. It can be programmed that the overshoot and the temperature settling (at the operator set-point) will occur on the run-on tab before the weld progresses onto the weldment. At the same time overshoot should not be excessive. It was decided that less than 15 percent overshoot, which corresponds to a settling time of 9.28 seconds, was acceptable. The zero placement is shown on the bode diagram in Figure 5.35.

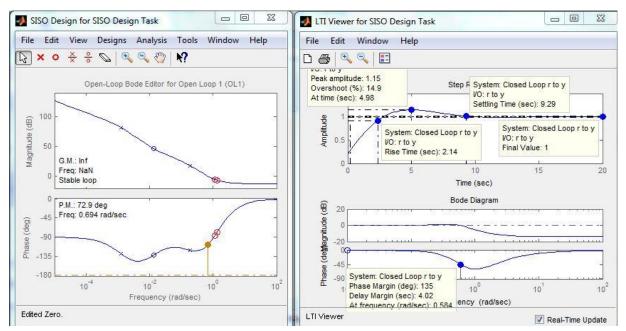


Figure 5.35. Final placement of Pl and PD design zeros

The location of the PD control design zero in the s domain is s = -1.3346 as seen in the compensator editor in Figure 5.36. Although controller loop gain, PI and PD design are conducted separately, they are done in cascade and all three components are included in the final controller design shown in the compensator editor of Figure 5.36 after PD design was completed.

The closed-loop bode diagram of the compensated system is shown in Figure 5.36. The bandwidth of the compensated system (taken from the -3 dB point on the

magnitude graph ^[21]) is 0.797 rad/s, which is a significant improvement over the uncompensated system (bandwidth of 0.00185 rad/s). The phase margin (stability margin) is 135°. It is therefore accurate to state that the compensated system is stable.

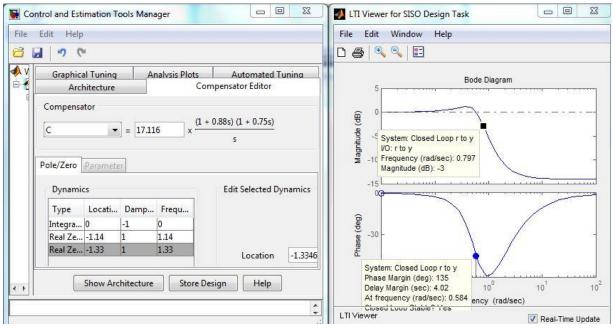


Figure 5.36. Final controller by frequency design

The coefficients of the s terms in the numerator of the compensator equation (Figure 5.36) are rounded off and are more accurately calculated as follows:

Let the compensator equation C(s) = $17.116 \frac{(1+As)(1+Bs)}{s}$

For the zero at $s = -1.1377$:	0 = (1 + A(-1.1377))
	A = 0.87897
For the zero at $s = -1.3346$:	0 = (1 + B(-1.3346))
	B = 0.74929

The compensator equation is defined as Equation 5.25.

$$C(s) = 17.116 \frac{(1+0.87897s)(1+0.74929s)}{s}$$
 Equation 5.25

The K_{P2} , K_{I2} and K_{D1} values are found by setting Equation 5.21 and Equation 5.25 equal to each other as shown in Equation 5.26.

$$C(s) = K_{I2} \frac{\left(1 + \frac{K_{P2}}{K_{I2}}s\right)}{s} (1 + K_{D1}s)$$
$$= 17.116 \frac{(1 + 0.87897s)(1 + 0.74929s)}{s}$$

Equation 5.26

From inspection of Equation 5.26:

- $\frac{K_{P2}}{K_{I2}} = 0.87897$
- $K_{I2} = 17.116$
- $K_{D1} = 0.74929$.

Therefore $K_{P2} = 0.87897 \times 17.116 = 15.04445$

The terms of the controller equation are converted into Kp, Ki and Kd gains using Equation 5.22, Equation 5.23 and Equation 5.24:

$$Kp = K_{P2} + K_{D1}K_{I2} = 15.04445 + (0.74929 \times 17.116)$$
 $= 27.8693$ $Ki = K_{I2}$ $= 17.116$ $Kd = K_{P2}K_{D1} = 15.04445 \times 0.74929$ $= 11.2727$

These *Kp*, *Ki* and *Kd* gains are reasonably similar, yet more conservative than the gains found from the Ziegler Nichols tuning method ^[3] (see Section 5.3.3) which were Kp = 38.1, Ki = 23.769 and Kd = 15.268.

The gains found from the Ziegler Nichols tuning method ^[3] were entered into ACSYS (see **page J-11 of Appendix J**) and the closed-loop bode diagram was generated

(see **page J-12 of Appendix J**). A comparison between the closed-loop bode diagrams for the Ziegler Nichols tuned ^[3] system and the bode frequency designed system (see Figure 5.36) showed that the Ziegler Nichols tuned ^[3] system had a slightly larger stability margin (141° versus 135°). The comparison also showed that the Ziegler Nichols tuned ^[3] system has a wider bandwidth (0.939 rad/s versus 0.797 rad/s).

In order to compare the performance of the Ziegler Nichols ^[3] derived PID gains and the bode frequency design derived PID gains, a Matlab Simulink simulation was conducted (see Figure 5.37, Figure 5.38 and **page J-13 to page J-16 of Appendix J**). For the comparison, the Simulink process control diagram was duplicated (FSW transfer function, feedback and PID controller), the step input was fed to the two systems and the PID gains from the two design methods were entered into the two separate PID controllers respectively. The two process outputs and the step input command were connected to a scope in order to visualise the signals.

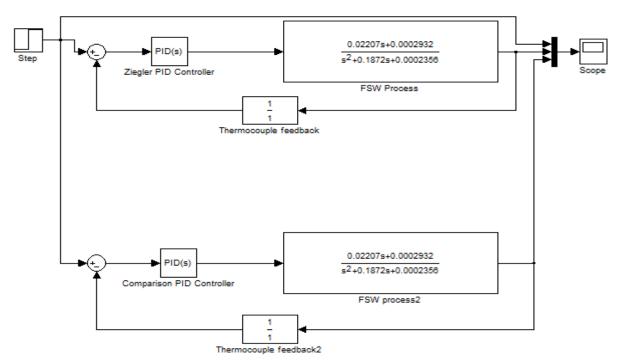


Figure 5.37. Simulink model of bode frequency design versus Ziegler Nichols design

The Simulink scope output shown in Figure 5.38 shows the step input command (blue graph) and the control system temperature outputs (Ziegler Nichols ^[3] design: red graph/graph with the least magnitude at 45 seconds; bode frequency design: green graph) versus time.

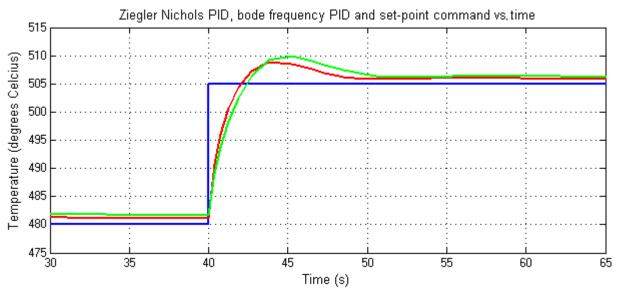


Figure 5.38. Ziegler Nichols PID design output versus bode frequency PID design

From the simulation in Figure 5.38, the Ziegler Nichols ^[3] PID design performance was marginally superior to the bode frequency PID design with a slightly faster rise time, less overshoot and a faster settling time.

Both tuning methods have their advantages and disadvantages. The disadvantages of tuning the system using the Ziegler Nichols method ^[3] could be that the tuning may contain errors from selection of the ultimate gain and measuring of the oscillation period. The disadvantages of designing a controller based on a system model (and bode diagram frequency design) is that there could be errors introduced in the generation of the system model and errors introduced in the design of the controller is not completely a precise science but also a bit of an art concerning the designer because almost every system is different and will not be designed in precisely the same way.

The advantages of the Ziegler Nichols tuning method ^[3] is that it is reasonably simple to conduct without a large amount of scientific calculations and typically produces good results. The gains obtained from this method provide a good starting point which can be modified in order to improve certain aspects of the system which are specific to that system. For example, the system may oscillate more than desired by the operator and increasing the derivative gain by a small amount could improve the situation. The operator should take caution by refraining from altering the gains excessively because the three gains each have their independent effects on the dynamics of the system although it is the same system and hence the gains affect each other's optimal positions. Altering the gains excessively could lead to an unstable system. The advantage of designing a controller based on a system model (and bode diagram frequency design) is that the controller is designed based on the dynamics of that particular system which are defined by scientific equations. If an accurate model of the system is developed, an accurate controller can be designed for it which may perform better than the controller derived from the Ziegler Nichols tuning method ^[3]. In addition to this, a model can be simulated using Matlab Simulink which allows the designer to experiment with the controller without the risk of damaging the system should he/she choose a setup which creates an unstable situation.

5.5.3. Simulink PID Tuning

The PID block in Matlab Simulink has a tuning function. By double clicking on the PID function block, the PID function block parameter window opens and there is a button labelled: "Tune" which opens the tuning facility (see **Appendix K**). The Simulink tuner automatically tunes the PID controller although the amount of power available to the system is unknown and the designer therefore chooses the response time by moving the "Response time" slider. Since the spindle speed was set to the 800 rev/min limit in "Weld AT_7" which represents the maximum power input to the system (for the temperatures at which the comparison is made), the response time was selected such that the rise time was similar to the rise time seen in "Weld AT_7".

The response time was set to 2.23 seconds which corresponds to a rise time of approximately 1.8 seconds (see **page K-2 of Appendix K**). Clicking the "Apply" button sets the corresponding P, I and D gains in the controller parameter window. The performance of the controller (the green graph/graph with the greatest magnitude at 85 seconds in Figure 5.39) was similar to that of the Ziegler Nichols ^[3] PID controller design (the red graph in Figure 5.39).

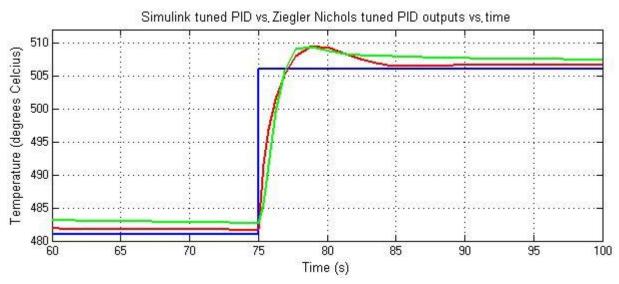


Figure 5.39. Simulink tuned PID performance versus Ziegler Nichols PID performance

A negative derivative term was generated by the Simulink PID tuner. Since the absolute values of the controller gains were similar to the gains found from the Ziegler Nichols ^[3] PID design, the simulation was executed with a positive derivative gain which has the same absolute value. The performance changed according to Figure 5.40.

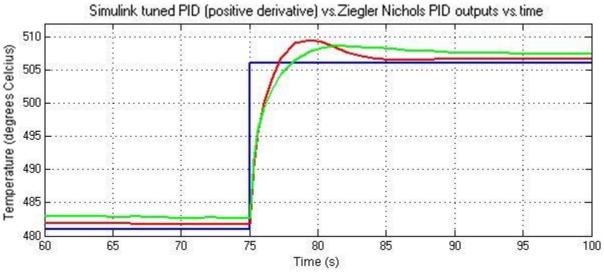


Figure 5.40. Simulink tuned PID (positive D) performance versus Ziegler Nichols PID performance

From Figure 5.39 and Figure 5.40, the performance of the PID controllers are similar although the Ziegler Nichols tuned ^[3] PID controller design consistently shows a faster settling time.

5.6. Thermal Disturbance Welds

The temperature control system utilising the PID gains found from the Ziegler Nichols tuning method ^[3] was used for the welds conducted in this section.

Welds were executed with a constant weld zone temperature of 505°C. Introducing thermal disturbances to the plate undergoing welding tests the disturbance rejection capability of the control system.

In addition to testing the disturbance rejection, weld strength consistency along the weld length was investigated. The investigation identifies any influences on weld quality which control of weld zone temperature introduces in the presence of thermal disturbances. Welds were conducted in the presence of heat sink and heat source type disturbances (detailed in Section 5.6.1 and Section 5.6.2). The area of contact

between the disturbances and the plate was approximately 3570 mm² (119 mm x 30 mm) on either side of the weld (total area of 7140 mm²). This was approximately the maximum contact area which the physical weld setup would allow between the clamps. The thermal disturbance was introduced between the two middle clamps which corresponded to the mid-point of the contact area being approximately 42 mm after the mid-point of the weld (or approximately 334 mm after the start position of the weld). Thermal paste was applied between the disturbance mechanism and the weld plate in order to eliminate any slight air gap and maximise the thermal conductivity of the junction.

The weld matrix including heat sink and heat source disturbance welds is shown in Table 5.8. The repetitions of "Weld 4.1" and "Weld 4.2" are for statistical purposes regarding the tensile results in Section 5.7.

Weld Matrix								
	Heat sink;	Heat source;						
	temperature control on	temperature control on						
	(505°C)	(505°C)						
Iteration 1	4.1.1	4.3.1						
Iteration 2	4.1.2	n/a						
Iteration 3	4.1.3	n/a						
	Heat sink;	Heat source;						
	temperature control off	temperature control off						
	(constant spindle speed	(constant spindle speed						
	of 492 rev/min)	of 492 rev/min)						
Iteration 1	4.2.1	4.4.1						
Iteration 2	4.2.2	n/a						
Iteration 3	4.2.3	n/a						

Table 5.8. Disturbance weld matrix	
------------------------------------	--

Measurements of room temperature; plate temperature on the weld path (at the disturbance position) before the disturbance was added; plate temperature on the weld path (at the disturbance position) after the disturbance was added; plate temperature at the start position of the weld (after the disturbance was added) and the plate temperature on the weld path immediately prior to the arrival of the welding tool at the disturbance were taken for each weld. The table containing all these measurements can be seen in Table 5.9 (heat sink disturbance welds) and Table 5.10 (heat source disturbance welds). "Weld 4.2.1.ni" corresponds to "Weld 3" in Figure 5.45 in which no disturbance was introduced and the temperature control algorithm was disengaged (for the purpose of comparison).

5.6.1. Heat Sink Disturbance

Weld	Room	Plate	Plate	Plate	Plate
	temperature	temperature	temperature	temperature	temperature
	(°C)	before the	after the	after the	prior to tool
		disturbance was	disturbance was	disturbance was	arrival at the
		added	added	added (start	disturbance
		(disturbance	(disturbance	position)	position
		position)	position)	(°C)	(°C)
		(°C)	(°C)		
4.1.1	23	21	-28	20	-30
4.1.2	23	20	-30	18	-32
4.1.3	23	20	-30	20	-31
4.2.1	22	23	-22	22	-20
4.2.2	24	21	-29	19	-31
4.2.3	23	21	-29	20	-31
4.2.1.ni	23	21	n/a	n/a	n/a

 Table 5.9. Heat sink weld plate temperatures

Two dry ice containers were manufactured from AA 6082-T6 for the high thermal conductivity of aluminium. Dry ice was placed in the containers as shown in Figure

5.41. Ideally, there must be high thermal conductivity between the heat sink material (dry ice) and the weld plate. The thermal conductivity of air is low and the dry ice pellets contain air gaps between them. Methanol was used to fill these gaps to improve the thermal conductivity between the dry ice itself and the aluminium container. Methanol has a freezing point of -97.7°C ^[19] and at atmospheric pressure (below the triple point pressure (518 kPa) of carbon dioxide ^[19]), carbon dioxide transforms from its solid state (dry ice) directly to its gaseous form at -78.4°C ^[19]. The temperature of dry ice is considered to be approximately -78.5°C ^[22]. The temperature of the dry ice is therefore unable to freeze the methanol. The methanol therefore continually flows between the dry ice pellets and the container in order to improved thermal conductivity.



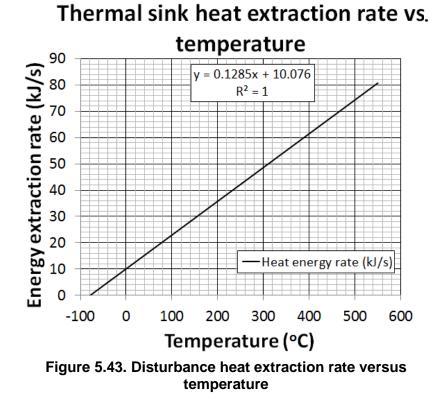
Figure 5.41. Dry ice and methanol heat sink

Figure 5.42 shows the positioning of a dry ice container relative to the weld.

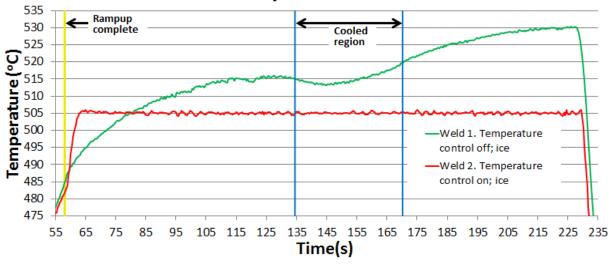


Figure 5.42. Dry ice container placement

Since the temperature of the plate (undergoing welding) near the disturbance position varies as the weld tool approaches and then travels away from the area, the heat energy extraction rate will vary accordingly. The graph of heat extraction rate versus plate temperature (average temperature below the disturbance area) is shown in Figure 5.43. The graph was generated according to Equation 5.8 ^[19] for a range of plate temperatures from dry ice temperature to maximum weld zone temperature and the plate temperature will lie within this range. In addition to this, the graph in Figure 5.43 was generated using the following information: the thickness of the bottom of the container is ten millimeters or 0.01 m; the thermal conductivity of the container (k) is 180 W/m.°C ^[23]; the container contact area is 0.00714 m²; assuming that the methanol and dry ice mixture was able to maintain the temperature of the bottom of the container pocket at -78.4°C; assuming that the junction of the disturbance to the weld plate is of equivalent or higher thermal conductivity than the aluminium.



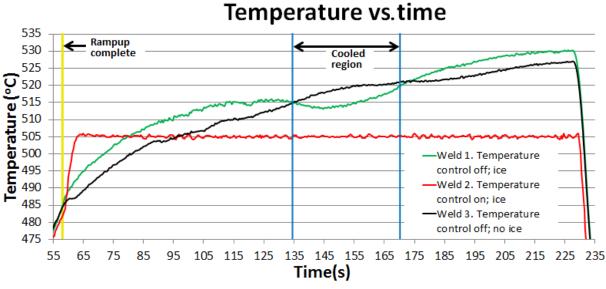
In the following two figures, "Weld 4.2.3"; "Weld 4.1.3" and weld "4.2.1.ni" are labelled: "Weld 1"; "Weld 2" and "Weld 3" respectively for clarity in this discussion. "Weld 1" and "Weld 2" in Figure 5.44 compare weld zone temperature with respect to time. "Weld 1" was conducted with constant spindle speed (temperature control disengaged) set to approximately 492 rev/min. "Weld 2" was conducted with the temperature control engaged (spindle speed varies in order to maintain weld zone temperature) and the temperature set-point was set to 505°C. Both welds had the dry ice disturbance present between the middle clamps. It is clear from the graph of "Weld 2" in Figure 5.44 that the temperature control algorithm exhibits good disturbance rejection characteristics because the constant temperature region deviates from the set-point of 505°C by no more than 1.1°C including the cooled region (disturbance position) indicated on the graph.



Temperature vs.time

Figure 5.44. Temperature control engaged/disengaged heat sink welds

"Weld 3" (in Figure 5.45) was conducted with no dry ice disturbance and no temperature control (constant spindle speed of 492 rev/min), for comparison with "Weld 1" and "Weld 2". Comparing the graphs of "Weld 1" and "Weld 3", the effect of the dry ice disturbance is clear. The temperature difference between the two temperature graphs varies and the maximum temperature difference in the cooled region is approximately 5.6°C.





The spindle speeds of the three welds are shown in Figure 5.46. The spindle speed of "Weld 1" and "Weld 3" was constant at approximately 492 rev/min. The temperature control algorithm varied the spindle speed of "Weld 2" in order to maintain the weld zone temperature at the set-point of 505°C. It is clear from the spindle speed graph of "Weld 2" that the controller increased the spindle speed as the weld tool approached and traversed into the cooled region in order to compensate for the dry ice disturbance.

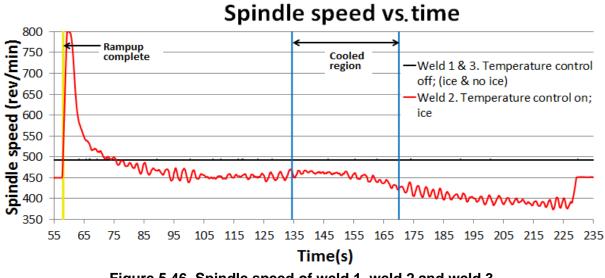


Figure 5.46. Spindle speed of weld 1, weld 2 and weld 3

Weld	Room	Plate	Plate	Plate	Plate	Plate
	temperature	temperature	temperature	temperature	temperature	temperature
	(°C)	before the	after the	after the	prior to tool	post weld
		disturbance	disturbance	disturbance	arrival at the	completion
		was added	was added	was added	disturbance	at the
		(disturbance	(disturbance	(start	position	disturbance
		position)	position)	position)	(°C)	position
		(°C)	(°C)	(°C)		(°C)
4.3.1	21	20	121	25	110	105
4.4.1	21	24	126	28	121	106
	7	Table 5.10. He	at source weld	d plate temper	atures	<u> </u>

A heat energy source disturbance was introduced to the weld plate. This disturbance causes the temperature controller to decrease the spindle speed (hence decreasing frictional heat energy input) to compensate for the disturbance.

The heat energy source was introduced by heating two steel blocks to approximately 400°C in a furnace and placing them on either side of the weld path with thermal paste between them and the weld plate. The blocks covered approximately the same area as the heat sink disturbance containers. The bottom face of the blocks were surface ground in order to maximise the contact area with the weld plate and eliminate any rust which would contaminate the thermal junction. The block positioning is shown in Figure 5.47.



Figure 5.47. Heated block disturbance close view

The heat source disturbance welds were tensile tested although the welds were not repeated for statistical purposes. The heat source disturbance welds were conducted primarily to verify that the temperature control system successfully compensates for this type of disturbance. The statistical analysis was deemed unnecessary following the statistical analysis (see Section 5.7) conducted for the welds completed and

discussed in Section 5.6.1. The positioning of the blocks relative to the weld setup is shown in Figure 5.48.

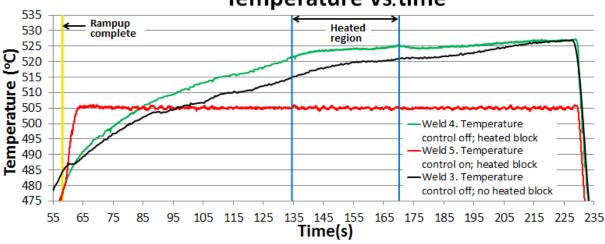


Figure 5.48. Heated steel block disturbance position relative to the weld setup

In the following two figures, "Weld 4.2.1.ni"; "Weld 4.4.1" and "Weld 4.3.1" are labelled: "Weld 3"; "Weld 4" and "Weld 5" respectively for clarity in this discussion.

The temperature versus time relationship of "Weld 4" in Figure 5.49 shows that with the temperature control disengaged and the heat source disturbance introduced, the temperature of the weld increases in the vicinity of the disturbance.

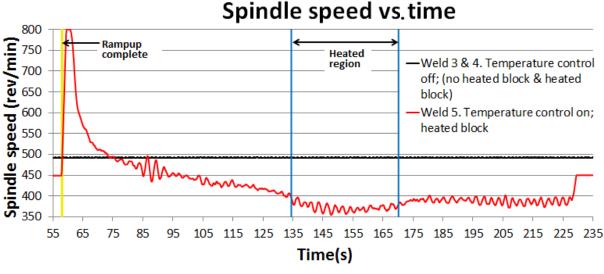
From the temperature versus time relationship of "Weld 5" in Figure 5.49, it is clear that the control system was successful in maintaining the weld zone temperature setpoint of 505°C despite the presence of the disturbance.



Temperature vs.time

Figure 5.49. Temperature control engaged/disengaged heat source welds

The spindle speeds of the three welds are shown in Figure 5.50. The spindle speed of "Weld 3" and "Weld 4" was constant at approximately 492 rev/min. The temperature control algorithm varied the spindle speed of "Weld 5" in order to maintain the weld zone temperature at the set-point of 505°C. It is clear from the spindle speed graph of "Weld 5" that the controller decreased the spindle speed when the weld tool approached and entered the heated region in order to compensate for the heated block disturbance.





5.7. Tensile Testing and Analysis

Weld strength consistency was investigated by means of tensile testing. This testing was done on the welds discussed in Section 5.6. The width of the plates on which welding was conducted was no less than 100 mm. The tensile samples were taken transversely through the welds. The tensile samples were machined to the ASTM E 8M standard for a tensile subsize specimen. Two examples of the as welded and machined tensile specimens are shown in Figure 5.51.



Figure 5.51. Tensile samples

Four positions along the weld length were tensile tested. The distance of these positions from the start point of the weld include 50 mm (near the start of the weld); 334.11 mm (mid-point of the disturbance area); 388.61 mm (end of the disturbance area) and 546 mm (near the end of the weld). The four tensile sample cut-out positions are labelled in Figure 5.52.

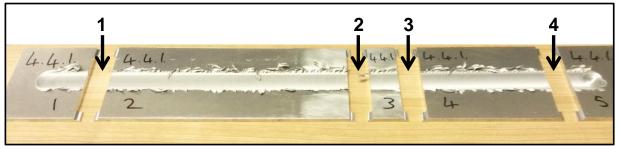


Figure 5.52. Tensile sample positions

All welds failed in the heat affected zone due to over aging of AA 6082-T6 (material strength is reduced by over aging) in this region. The welds do not fail in the parent material (over aging is approximately negligible); the weld nugget or the thermomechanically affected zone (TMAZ). Failure does not occur in the weld nugget or TMAZ because dynamic recrystallisation is experienced in these areas and smaller grain sizes are generated in these regions ^[8]. The parent material, TMAZ and weld nugget are therefore stronger than the heat affected zone (next to the weld) provided that voids do not exist in the weld nugget or TMAZ.

5.7.1. Comparison of Weld Strength at each Tensile Sample Position

The tensile test results and the statistical data for the heat sink disturbance welds are shown in Table 5.11 (Weld set 4.1: temperature controlled welds with set-point set to 505°C) and Table 5.12 (Weld set 4.2: constant spindle speed welds with spindle speed set to 492 rev/min).

	Yield strength (MPa)				Ultimat	e tensile	strength	n (MPa)
Weld repetition	sample	sample	sample	sample	sample	sample	sample	sample
number	position	position	position	position	position	position	position	position
number	1	2	3	4	1	2	3	4
4.1.1	147.54	152.48	147.27	141.69	235.00	236.42	231.27	227.80
4.1.2	146.27	144.21	144.61	142.53	231.28	230.93	229.57	226.60
4.1.3	146.27	143.51	145.73	139.08	229.81	230.21	229.98	228.72
mean	146.69	146.73	145.87	141.10	232.03	232.52	230.27	227.71
standard deviation	0.735	4.986	1.335	1.800	2.675	3.397	0.887	1.063
n	3	3	3	3	3	3	3	3
t critical	4.303	4.303	4.303	4.303	4.303	4.303	4.303	4.303
uncertainty (95%)	1.825	12.387	3.315	4.471	6.646	8.438	2.204	2.641

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Table 5.11. Tensile results of temperature controlled, heat sink disturbance welds (4.1)

	Yield strength (MPa)				Ultimat	e tensile	strength	n (MPa)
Weld repetition	sample	sample	sample	sample	sample	sample	sample	sample
number	position	position	position	position	position	position	position	position
number	1	2	3	4	1	2	3	4
4.2.1	144.65	150.97	147.07	146.17	231.83	234.11	234.27	228.71
4.2.2	141.21	149.31	150.36	148.12	228.55	233.80	235.30	232.22
4.2.3	141.80	150.54	150.57	149.08	230.01	234.81	235.28	231.58
mean	142.55	150.27	149.33	147.79	230.13	234.24	234.95	230.84
standard deviation	1.840	0.860	1.958	1.483	1.643	0.517	0.589	1.869
n	3	3	3	3	3	3	3	3
t critical	4.303	4.303	4.303	4.303	4.303	4.303	4.303	4.303
uncertainty (95%)	4.572	2.138	4.864	3.683	4.082	1.285	1.463	4.644

Table 5.12. Tensile results of constant spindle speed, heat sink disturbance welds (4.2)

Three parent samples were tensile tested in order to calculate the parent strength with statistical uncertainty. The ultimate tensile strength (UTS) of AA6082-T6 parent plate was 328.86±1.18 MPa (95 percent confidence). The weakest mean UTS from the weld tensile data was 227.71±2.64 MPa (95 percent confidence) which is approximately 69.24 percent of the parent UTS. The strongest mean UTS from the weld tensile data is 234.95±1.46 MPa (95 percent confidence) which is approximately 71.44 percent of the parent UTS. The minimum and maximum tensile strengths are both greater than 66 percent of the strength of the parent plate which is considered a good weld for heat treatable aluminium alloys ^[7].

The data presented in Table 5.11 and Table 5.12 was used to generate graphs comparing the weld strength consistency of a weld conducted with constant weld zone temperature (and therefore varying spindle speed) versus a typical FSW weld which is conducted with constant spindle speed (and therefore varying weld zone temperature). Both welds have the heat sink disturbance introduced. The comparison of weld strength at the four tensile sample positions between weld sets 4.1 and 4.2 is shown in Figure 5.53 (yield strength comparison) and Figure 5.54 (ultimate strength comparison).

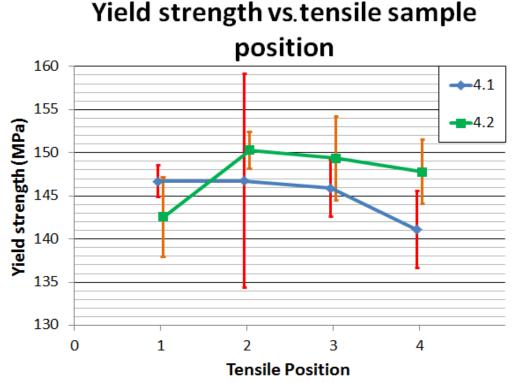


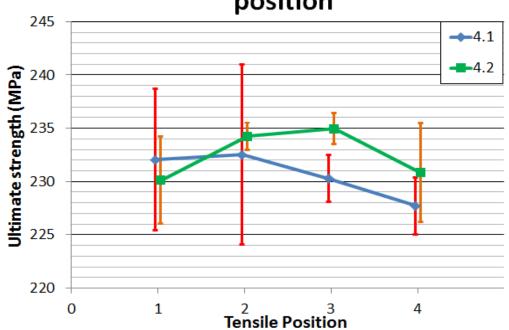
Figure 5.53. Tensile yield strength comparison between weld sets 4.1 and 4.2

The error bars of the yield strengths for position 2 and position 3 overlap substantially. This suggests that the difference between weld set 4.1 and weld set 4.2 at these positions can be attributed to experimental error. The yield strengths at position 1 and position 4 also have overlapping error bars although the amount by which they overlap is less than for position 2 or position 3. Statistical t-tests were conducted using Microsoft Excel's data analysis tool. Each t-test compared the weld yield strength of the two weld sets (4.1 and 4.2) at each of the four tensile sample positions. The t-tests determine whether or not the difference in weld strength can be attributed to experimental error or not, with 95 percent confidence. The results of the t-tests are shown in Table 5.13.

t-test results	Yield strength	Yield strength	Yield strength	Yield strength	
	position 1	position 2	position 3	position 4	
p value	0.022443	0.292119	0.064690	0.007659	

Table 5.13. Yield strength t-test results

The results from the t-tests suggest that the difference between weld set 4.1 and weld set 4.2 at position 1 cannot be attributed to experimental error (p=0.022<0.05 or 2.2 percent probability that the difference can be attributed to experimental error). The test result for position 2 suggests that the difference between weld set 4.1 and weld set 4.2 can be attributed to experimental error with relatively large probability (p=0.292>0.05). The t-test result for position 3 suggests that the difference between weld set 4.1 and weld set 4.1 and weld set 4.1 and weld set 4.2 can be attributed to experimental error (p=0.065>0.05) although the p value is marginally larger than 0.05 which means that it could be argued that the difference may or may not be attributed to experimental error. The t-test for position 4 suggests strongly that the strength difference between weld set 4.1 and weld set 4.2 cannot be attributed to experimental error (p=0.008<0.05).



Ultimate strength vs.tensile sample position

Figure 5.54. Ultimate tensile strength comparison between weld sets 4.1 and 4.2

T-tests were conducted for the ultimate tensile strengths at each tensile sample position. The results are shown in Table 5.14.

	Ultimate	Ultimate	Ultimate	Ultimate
t-test results	strength	strength	strength	strength
	position 1	position 2	position 3	position 4
p value	0.35369	0.434816	0.001603	0.065289

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Table 5.14. Ultimate strength t-test results

The t-tests conducted for the ultimate strength results suggest strongly that the ultimate strength difference between weld set 4.1 and weld set 4.2 at position 1 and position 2 are attributed to experimental error (p=0.354>0.05 and p=0.435>0.05). The t-test for position 3 suggests strongly that the ultimate strength difference between weld set 4.1 and weld set 4.2 cannot be attributed to experimental error. The t-test for position 4 suggests that the strength difference between weld set 4.1 and weld set 4.2 cannot be attributed to experimental error. The t-test for position 4 suggests that the strength difference between weld set 4.1 and weld set 4.2 can be attributed to experimental error although it is not a strong suggestion because the p value is marginally larger than 0.05 (p=0.065>0.05). The t-tests generated using the Microsoft Excel data analysis tool are shown in **Appendix L**.

In conclusion of the presented statistical t-tests and referring to Table 5.13 and Table 5.14, the yield strength at position 1 can be considered different for weld set 4.1 and weld set 4.2, although the ultimate strength can be considered the same. Regarding position 2, both the yield strength and the ultimate strength can be considered the same between weld set 4.1 and weld set 4.2. Regarding position 3, the yield strength can be argued to be different and the ultimate strength can be considered different between weld set 4.1 and weld set 4.2. Regarding position 4, the yield strength can be considered to be different and the ultimate strength can be argued to be different and the ultimate strength can be argued to be different and the ultimate strength can be argued to be different and the ultimate strength can be argued to be different between weld set 4.1 and weld set 4.2. Regarding position 4, the yield strength can be considered different and the ultimate strength can be argued to be different and the ultimate strength can be argued to be different and the ultimate strength can be argued to be different and the ultimate strength can be argued to be different between weld set 4.1 and weld set 4.2.

5.7.2. Investigation of Weld Strength Consistency

For the purpose of this study, the standard deviation of the weld strength along the weld length is considered an indication of weld strength consistency. The difference in weld strength consistency between weld set 4.1 and weld set 4.2 is calculated from the data taken from Table 5.11 and Table 5.12 and shown in Table 5.15 and Table 5.16.

	Yield strength (Mpa)									
		sample	sample	sample	sample					
Weld	Weld	position	position	position	position	standard				
number	repetition	1	2	3	4	deviation				
	4.1.1	147.54	152.48	147.27	141.69	4.407				
4.1	4.1.2	146.27	144.21	144.61	142.53	1.535				
	4.1.3	146.27	143.51	145.73	139.08	3.271				
	4.2.1	144.65	150.97	147.07	146.17	2.697				
4.2	4.2.2	141.21	149.31	150.36	148.12	4.130				
	4.2.3	141.80	150.54	150.57	149.08	4.186				

Table 5.15. Yield tensile strength standard deviations

A statistical t-test was conducted to investigate the weld yield strength consistency (represented by the standard deviation) difference between weld set 4.1 and weld set 4.2. The two sets of data on which the test was conducted are highlighted green and blue in Table 5.15. The mean standard deviation for weld set 4.1 is 3.071 MPa and the mean standard deviation for weld set 4.2 is 3.671 MPa. The standard deviation of weld set 4.1 is smaller than the standard deviation of weld set 4.2 which proposes that the strength is more consistent in weld set 4.1 although the p value of the t-test was 0.569. This strongly suggests that this difference between the standard deviations of strength in weld set 4.1 and the standard deviations of strength in weld set 4.2 and the standard deviations of strength in weld set 4.1 and the standard deviations of strength in weld set 4.2 and the standard deviations of strength in weld set 4.2 and the standard deviations of strength in weld set 4.2 and the standard deviations of strength in weld set 4.2 and the standard deviations of strength in weld set 4.2 and the standard deviations of strength in weld set 4.2 and the standard deviations of strength in weld set 4.2 and the standard deviations of strength in weld set 4.2 can be attributed to experimental error. The t-test generated by the Microsoft Excel data analysis tool can be seen in **Appendix L, page L-3**.

	Ultimate tensile strength (MPa)					
		sample	sample	sample	sample	
Weld	Weld	position	position	position	position	standard
number	repetition	1	2	3	4	deviation
4.1	4.1.1	235.00	236.42	231.27	227.80	3.880
	4.1.2	231.28	230.93	229.57	226.60	2.129
	4.1.3	229.81	230.21	229.98	228.72	0.661
4.2	4.2.1	231.83	234.11	234.27	228.71	2.598
	4.2.2	228.55	233.80	235.30	232.22	2.899
	4.2.3	230.01	234.81	235.28	231.58	2.543

 Table 5.16. Ultimate tensile strength standard deviations

A statistical t-test was conducted to investigate the weld ultimate strength consistency (represented by the standard deviation) difference between weld set 4.1 and weld set 4.2. The two sets of data on which the test was conducted are highlighted green and blue in Table 5.16. The mean standard deviation for weld set 4.1 is 2.223 MPa and the mean standard deviation for weld set 4.2 is 2.680 MPa. The standard deviation of weld set 4.1 is smaller than the standard deviation of weld set 4.2 which proposes that the strength is more consistent in weld set 4.1 although the p value of the t-test was 0.651. This strongly suggests that this difference between the standard deviations of strength in weld set 4.1 and the standard deviations of strength in weld set 4.2 can be attributed to experimental error. The t-test generated by the Microsoft Excel data analysis tool can be seen in **Appendix L, page L-3**.

5.8. Summary

Initially, the process window was established on the MTS FSW platform. This process discovered the correct tool tilt angle, the correct forge force and the safe maximum and minimum limits for spindle speed such that the tool does not seize/fracture nor over plunge. This process window is unique to the particular weld setup in this study.

In the preliminary stage of the study, the weld zone temperature response to spindle speed changes was investigated and the process found to be non-linear. This stage of the study provided the researcher with a better understanding of the process temperature response to changes in spindle speed and a set of data from which to generate a mathematical model of the process.

The PID temperature control algorithm layout, design and implementation were explained in detail. The tuning theory (Ziegler Nichols tuning method ^[3]) by which the algorithm was tuned and the method carried out by the researcher was explained in detail. After implementation of the control algorithm, the procedure for testing the response of the control system by implementing step command changes in the temperature set-point was explained. The results from the tuning welds and performance testing welds were discussed. Various derivative filter designs were developed and tested in order to deduce the oscillation of the spindle speed during temperature control.

A mathematical model (transfer function) was developed using Matlab's system identification tool. The result was a second order transfer function. The PID gains found from the Ziegler Nichols tuning method ^[3] were used in the PID controller connected to the process model in Matlab Simulink. The simulation response was found to be relatively similar to the response of the actual system.

Two Matlab controller design tools were utilised to generate PID controllers based on the process model (transfer function) generated. The performance of each of these controllers was simulated in comparison to simulation of the Ziegler Nichols ^[3] PID controller design mentioned in the previous paragraph. The two controller design tools utilised include Matlab's Automatic Control Systems toolbox (ACSYS) and Matlab Simulink PID tuner. The ACSYS toolbox was used to perform bode diagram frequency design of a PID controller. The purpose of the development of these controllers was for comparison with the controller designed using the Ziegler Nichols tuning method ^[3]).

Utilising the PID controller found from the Ziegler Nichols tuning method ^[3], the disturbance rejection capability of the control system was tested. Heat sink and heat source type disturbances were introduced and the control system successfully compensated for them by maintaining constant weld zone temperature to within 1.1°C of the set-point temperature (505°C).

In order to investigate weld strength consistency of a constant temperature weld versus a typical FSW conducted with constant spindle speed (in the presence of a heat sink disturbance), tensile tests were conducted. The welds from which the tensile samples were machined, consisted of a constant temperature weld with repetitions (weld set 4.1; temperature: 505°C) and a constant spindle speed weld with repetitions (weld set 4.2; spindle speed: 492 rev/min). Four tensile samples were machined from each weld. Each weld set consisted of three repetitions in order to produce a sufficient number of tensile samples for statistical purposes. Differences in weld strength between weld set 4.1 and weld set 4.2 at various positions which could not be attributed to experimental error were found statistically. Some differences in weld strength between weld set 4.1 and weld set 4.2 at various positions which could be attributed to experimental error were also found statistically.

An investigation of weld strength standard deviation along the weld length as a representation of weld strength consistency was carried out.

Chapter 6

Conclusions and Future Research

As proven by this study, weld zone temperature of FSW can be controlled using PID control provided that the performance reported in this document is acceptable to the specific production process for which it is used. Typically there is no reason to change weld temperature during a weld and the production process setup usually contains a run-on tab or a limited region at the beginning of the weld where reduced weld quality can be tolerated. All FSW welds need to ramp up weld zone temperature from room temperature to the required weld temperature in the beginning stage. Once up to temperature, a well-tuned PID controller is able to maintain the weld zone temperature with deviation from the set-point of less than 1.1°C as proven by this study. If any undesirable overshoot were to occur whilst the system achieves welding temperature, it could be programmed to take place in the ramp up region on the run-on tab.

The results show that FSW temperature response to spindle speed changes can be relatively accurately modelled using Matlab's system identification tool. The results also show that the Matlab ACSYS controller design tool as well as Matlab Simulink can be used to design PID controllers which closely match the controller design obtained from the practical Ziegler Nichols tuning method ^[3].

This study identified that in some control cases; the derivative term of the PID controller may cause undesirable oscillation of the system actuator due to the derivative term's high gain for high frequency signals (generally caused by noise on the sensor feedback signal). The study showed that filter design and implementation on the feedback signal and/or implementation of a filter type derivative equation

(executed during calculation of the derivative term) can reduce the oscillation of the system actuator.

The PID controller implemented in this study (designed using the Ziegler Nichols tuning method ^[3]) improved the system bandwidth from 0.00185 rad/s (of the uncompensated system) to 0.939 rad/s (of the PID compensated system). The PID control system exhibits good thermal disturbance rejection as evidenced by the heat energy sink and heat energy source disturbance welds conducted in this study (see Section 5.6). The control system was able to maintain the weld temperature to within 1.1°C of the set-point despite the presence of the disturbances.

Tensile testing showed no significant improvement of weld quality by maintaining constant weld temperature. It is important to note that this statement pertains to welds conducted with weld zone temperature in the range of temperature reported in this study. Minimum UTS to maximum UTS recorded in this study ranged from 227.71±2.641 MPa (95 percent confidence), which is approximately 69.24 percent of the parent UTS, to 234.95±1.463 MPa (95 percent confidence) which is approximately 71.44 percent of the parent UTS. This range is 7.24±4.104 MPa (95 percent confidence) which is small relative to the weld strength (less than 5%) which could be considered insignificant.

Weld zone temperature which is too low will cause defects to develop in the weld which would reduce weld strength considerably. A weld of this nature was not executed in this study. The temperature control system ensures that the weld is conducted with sufficient weld zone temperature in order to avoid defect production (provided the temperature set-point is correct for the specific weld setup). In the process window of FSW weld zone temperature, above a certain critical temperature, according to results found in literature titled: "Effects of Tool-Workpiece Interference Temperature on Weld Quality and Quality Improvements Through Temperature Control in Friction Stir Welding" ^[8], weld quality is approximately constant although

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weld zone temperature below a critical value resulted in the production of defects and therefore reduced weld quality.

6.1. Future Research

Future research could include executing low temperature welds (minimum spindle speed) which introduce a heat energy sink which creates a larger temperature gradient between itself and the weld plate (such as liquid nitrogen placed in the containers instead of dry ice and methanol) which would cause a lower weld temperature at the disturbance. This could possibly reduce the weld zone temperature (with the temperature control disengaged) to a value below the critical temperature where voids begin to form in the weld (hence dramatically reducing weld quality). This would further test the control algorithm although it would introduce risks such as tool seizure and/or fracture. From common knowledge and literature titled: "Effects of Tool-Workpiece Interference Temperature on Weld Quality and Quality Improvements Through Temperature Control in Friction Stir Welding"^[8], it is known that below a certain temperature, voids will begin to form, dramatically reducing weld quality. From this study it was found that the critical temperature below which weld quality is dramatically reduced lies below the temperature obtained when conducting a weld at the lower safe limit of spindle speed determined for the particular weld setup in this study. A wide range of weld temperature therefore exists in which the resultant weld strength is approximately constant.

Alternative control algorithms could be developed such as fuzzy logic and genetic algorithms. The performance of these control methods could be compared to the results obtained in this study. The thermal disturbances could be modelled in order to be able to introduce them into the control system simulation. The disturbance rejection of the simulated model can then be compared to the disturbance rejection of the actual control system.

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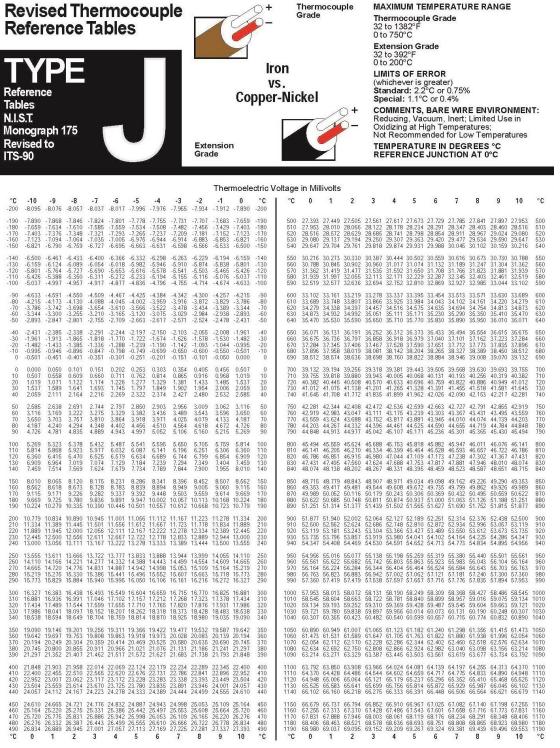
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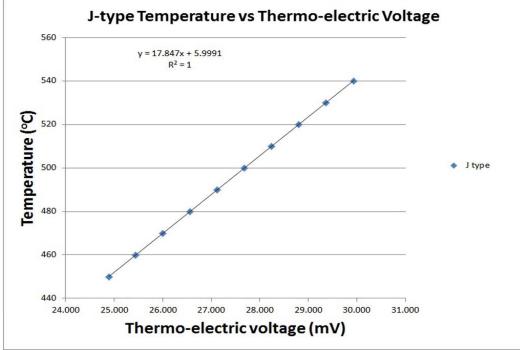
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sample T no. °C	1	2	3	4	5	6	7	8	9	10	11	average (mV)	standard deviation (mV)
450	24.61	24.665	24.721	24.776	24.832	24.887	24.943	24.998	25.053	25.109	25.164	24.887	0.18
460	25.164	25.22	25.275	25.331	25.386	25.442	25.497	25.553	25.608	25.664	25.72	25.442	0.18
470	25.72	25.775	25.831	25.886	25.942	25.998	26.053	26.109	26.165	26.22	26.276	25.998	0.18
480	26.276	26.332	26.387	26.443	26.499	26.555	26.61	26.666	26.722	26.778	26.834	26.555	0.18
490	2 <mark>6.8</mark> 34	26.889	26.945	27.001	27.057	<mark>27.11</mark> 3	27.169	27.225	27.281	27.337	<mark>27.39</mark> 3	27.113	0.18
500	27.393	27.449	27.505	27.561	27.617	27.673	27.729	27.785	27.841	27. <mark>8</mark> 97	<mark>27.95</mark> 3	27.673	0.1
510	27.953	28.01	28.066	28.122	28.178	28.234	28.291	28.347	28.403	28.46	28.516	28.235	0.1
520	28.516	28.572	28.629	28.685	28.741	28.798	28.854	28.911	28.967	29.024	29.08	28.798	0.1
530	29.08	29.137	29.194	29.25	29.307	29.363	29.42	29.477	29.534	29.59	29.647	29.364	0.1
540	29.647	29.704	29.761	29.818	29.874	29.931	29.988	30.045	30.102	30.159	30.216	29.931	0.1

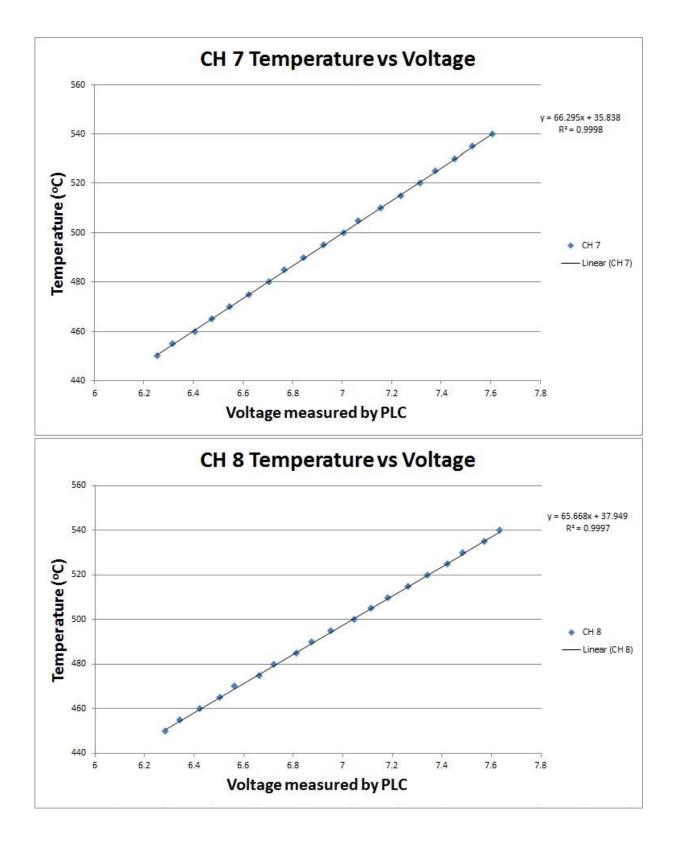
Relevant extract from the J-type thermocouple table:



Thermocouple calibration data obtained experimentally where Temperature was measured with a digital thermometer and the voltage output from the telemetry system was measured by the PLC via its analog input cards:

Temp (°C)	CH 7	CH 8
(thermometer)	(voltage)	(voltage)
· · · · · · · · · · · · · · · · · · ·	((0-7
450	6.25	6.28
450	6.26	6.29
455	6.31	6.34
455	6.32	6.35
460	6.41	6.42
460	6.4	6.43
465	6.47	6.5
465	6.48	6.51
470	6.54	6.56
470	6.55	6.57
475	6.63	6.66
<mark>4</mark> 75	6.62	6.67
480	6.7	6.72
480	6.71	6.73
485	6.76	6.81
485	6.77	6.82
490	6.85	6.87
490	6.84	6.88
495	6.92	6.96
495	6.93	6.95
500	7	7.04
500	7.01	7.06
505	7.07	7.11
505	7.06	7.12
510	7.15	7.19
510	7.16	7.18
515	7.23	7.27
515	[2] [2] [2] [2] [2] [2] [2] [2] [2] [2] [2]	7.26
520	7.31	7.35
520	7.32	7.34
525	7.38	7.43
525	7.37	7.42
530	7.45	7.48
530	7.46	7.49
535	7.52	7.57
535	7.53	7.58
540	7.61	7.64
540	7.6	7.63

Temp (°C)	CH 7 voltage average	CH 8 voltage average
450	6.255	6,285
450	6.315	6.345
455	6.405	6.425
400	6.475	6.505
470	6.545	6.565
475	6.625	6.665
480	6.705	6.725
485	6.765	6.815
490	6.845	6.875
495	6.925	6.955
500	7.005	7.05
505	7.065	7.115
510	7.155	7.185
515	7.235	7.265
520	7.315	7.345
525	7.375	7.425
530	7.455	7.485
535	7.525	7.575
540	7.605	7.635



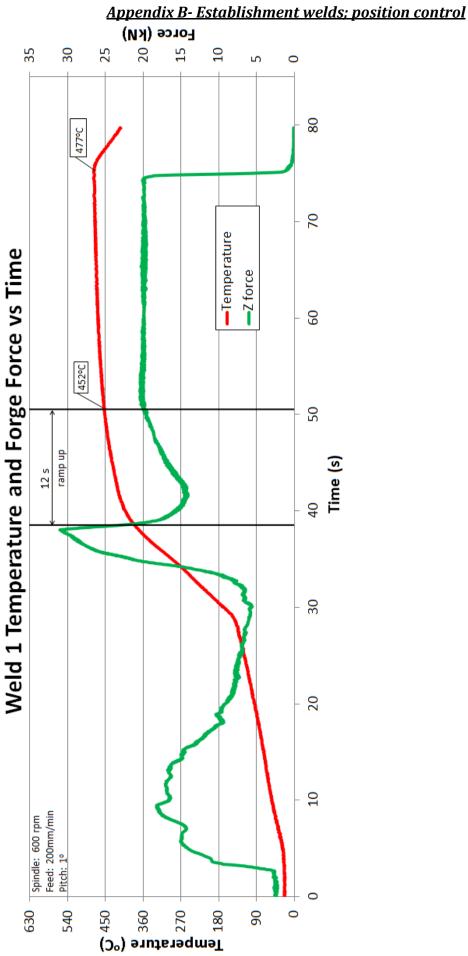
A	0 8	ш О	5	- н	۲	M	0 N	٩	R	T	V W	X	Z AA	AB AC
sa statistical error														
55 Temo (°C) (thermometer)	450	455	460	465	470	475	480	485	490	495	200	505	510	515
57 thermocouple voltage mV	24.887	25.164	25.442	25.720	25.998	26.276	26.555	26.834	27.113	27.393	27.673	27.954	28.235	28.516
58 CH 7 calibration reading (voltage)	6.25 6.26	6.31 6.32	6.41 6.40	6.47 6.48	6.54 6.55	6.63 6.62	6.70 6.71		6.85 6.84					
59 apparent gain	251.134	250.751	251.947	251.557	251.560	252.319	252.309	251.920	252.645	252.619	252.954	252.918	253.236	253.540
61 std dev	0.00707	0.00707	0.00707	0.00707	0.00707	0.00707	0.00707	0.00707	0.00707	0.00707	0.00707	0.00707	0.00707	0.00707
62 t critical	12.710	12.710	12.710	12.710	12.710	12.710	12.710	12.710	12.710	12.710	12.710	12.710	12.710	12.710
63 n	2.000	2.000	2.000	2.000	2.000	2.000	2.000	2.000	2.000	2.000	2.000	2.000	2.000	2.000
64 uncertainty (95%)	0.0635	0.0636	0.0635	0.0636	0.0635	0.0635	0.0635	0.0635	0.0635	0.0635	0.0635	0.0636	0.0635	0.0635
65 mean	6.255	6.315	6.405	6.475	6.545	6.625	6.705	6.765	6.845	6.925	7.005	7.065	7.155	7.235
67 max thermocouple voltage (mV)	29.931													
68 CH 7 (voltage max)	7.610													
69 thermocouple error (%)	0.0075													
70 maximum thermocouple voltage error (mV)	0.2245													
71 CH7 gain	252.6651													
72 maximum thermocouple voltage error after telemetry gain (V)	0.0567													
73 CH7 maximum uncertainty (V) (confidence:95%)	0.0636													
74 Combined error (V) (confidence: 95%)	0.085													
75 Combined error (%) (confidence: 95%) 76	1.119													
77 Temp (°C) (thermometer)	450	455	460	465	470	475	480	485	490	495	500	505	510	515
78 [thermocouple voltage mV	24.887	25.164	25.442	25.720	25.998	26.276	26.555	26.834	27.113	27.393	27.673	27.954	28.235	28.516
79 CH 8 calibration reading (voltage)	6.28 6.29	6.34 6.35	6.42 6.43	6.50 6.51	6.56 6.57	6.66 6.67	6.72 6.73	6.81 6.82	6.87 6.88	6.96 6.95	5 7.04 7.06	5 7.11 7.12	7.19 7.18	7.27 7.26
80 apparent gain	252.340	251.943	252.340	252.724	252.330	253.461	253.062	253.783	253.383	254.079	254.400	254.348	254.653	254.943
82 std dev	0.00707	0.00707	0.00707	0.00707	0.00707	0.00707	0.00707	0.00707	0.00707	0.00707	0.01414	0.00707	0.00707	0.00707
83 t critical	12.710	12.710	12.710	12.710	12.710	12.710	12.710	12.710	12.710	12.710	12.710	12.710	12.710	12.710
84 n	2.000	2.000	2.000	2.000	2.000	2.000	2.000	2.000	2.000	2.000	2.000	2.000	2.000	2.000
85 uncertainty (95%)	0.064	0.064	0.064	0.064	0.064	0.064	0.064	0.064	0.064	0.064	0.127	0.064	0.064	0.064
86 mean	6.285	6.345	6.425	6.505	6.565	6.665	6.725	6.815	6.875	6.955	7.050	7.115	7.185	7.265
88 max thermocouple voltage (mV)	29.931													
89 CH 8 (voltage max)	7.640													
90 thermocouple error (%)	0.0075													
91 maximum thermocouple voltage error (mV)	0.2245													
92 CH8 gain	253.8860													
93 maximum thermocouple voltage error after telemetry gain (V)	0.0570													
94 CH8 maximum uncertainty (V) (confidence:95%)	0.1271													
95 Complied error (V) (complence: 35%)	0.139													
96 Combined error (%) (connaence: 35%)	1.823													

AM				1	1 7.60																				1 7.63							10									
AL			540	29.931	7.61	254.248	70700.0	12.710	2.000	0.0636	7.605												540	29.931	7.64	255.251		0.00707	12.710	2.000	0.064	7.635									
AK			_		7.53		Ì																		7.58		ľ	•													
A			535	29.647	7.52	253.647	20200.0	12.710	2.000	0.0636	7.525												535	29.647	7.57	255.334		0.00707	12.710	2.000	0.064	7.575									
AI					7.46		t																		7.49		ľ	•				•									
AH			530	29.364	7.45	253.716	0.00707	12.710	2.000	0 DERE	7.455												530	29.364	7.48	254.738		0.00707	12.710	2.000	0.064	7.485									
AG					7.37																				7.42		-					•									
AF			525	29.081	7.38	253.776	10700	12.710	2.000	0.0635	7.375												525	29.081	7.43	255.496		0.00707	12.710	2.000	0.064	7.425									
AE					7.32																				7.34		•					•									
AD			520	28.798	7.31	253.838	10700	12.710	2.000	0.0636	7.315												520	28.798	7.35			0.00707	12.710	2.000	0.064	7.345									
AC		\vdash	_		7.24																				7.26		-					•									
7	5	5	26	57	58	65 0	8 6	62	63	7	65	99	67	89	69	70	71	72	73	74	75	76	1	78	79	8	81	82	8	8	50	86	87	88	68	8	91	92	6	94	y

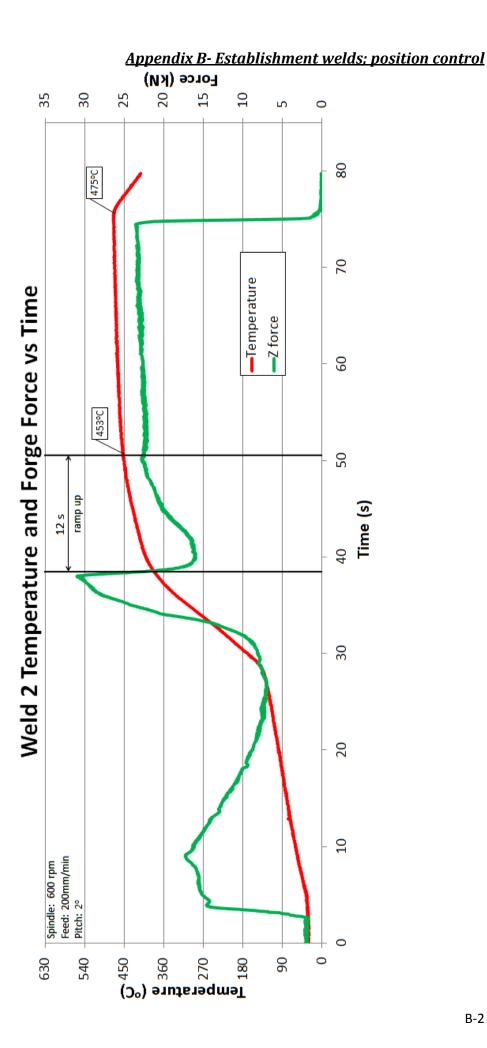
•	0	c	u	3	-	
					-	
se statistical error						
55						
56 Temp (°C) (thermometer)	450	455	460	465	470	475
57 Ithermocouple voltage mV	24.8870909090909	25.164454545454545	25.44181818182	25.719772727272	25.99772727273	26.27622727273
58 CH 7 calibration reading (voltage)	6.25 6.2		6.32 6.41	6.4 6.47		6.55 6.63 6.62
59 apparent gain	=B58/(B57/1000)	=D58/(D57/1000)	=F58/(F57/1000)	=H58/(H57/1000)	=J58/(J57/1000)	=L58/(L57/1000)
60						
61 std dev	=STDEV(B58:C58)	=STDEV(D58:E58)	=STDEV(F58:G58)	=STDEV(H58:158)	=STDEV(J58:K58)	=STDEV(L58:M58)
62 t critical	12.71	12.71	12.71	12.71	12.71	12.71
63 П	2	2	2	2	2	2
64 incertainty (95%)	=B62+B61/SORT/B63)	=D62+D61/SORT(D63)	=F63*F61/SORT/F63)	=H63+H61/SORT/H63	=162+161/SORT/163)	= 62* 61 /SORT/I 63)
	-AVEDAGE/B58-C581	-AVEDAGE/D58-F581	AVEDAGE(F58-G58)	-AVFDAGF/H58-1581	-AVEDAGE/ISB·KSB/	-AVEDAGE/158-M581
55 Filterin						
are thermocounde welface (m/)	-MAYIC7-C7					
de of recordence man (control of the control of the	0.0075					
an instantonetic and representation (m/l)						
	/00.600=					
	=AVERAGE(B59.AMD9)					
72 maximum thermocouple voltage error after telemetry gain (V)	=B70*B71/1000					
73 CH7 maximum uncertainty (V) (confidence:95%)	=MAX(B64:AM64)					
74 Combined error (V) (confidence: 95%)	=SQRT(B72^2+B73^2)					
75 Combined error (%) (confidence: 95%)	=(B74/B68)*100					
76						
77 Temp (°C) (thermometer)	450	455	460	465	470	475
78 thermocouple voltage mV	24.8870909090909	25.164454545454545	25.4418181818182	25.7197727272727	25.99772727273	26.27622727273
79 CH 8 calibration reading (voltage)		6.29 6.34	6.35 6.42	6.43 6.5	6.51 6.56	6.57 6.66 6.67
80 apparent gain	=B79/(B78/1000)	=D79/(D78/1000)	=F79/(F78/1000)	=H79/(H78/1000)	=179/(J78/1000)	=L79/(L78/1000)
81	1			1		1
82 std dev	=STDEV(B79:C79)	=STDEV(D79:E79)	=STDEV(F79:G79)	=STDEV(H79:179)	=STDEV(J79:K79)	=STDEV(L79:M79)
83 [t critical	12.71	12.71	12.71	12.71	12.71	12.71
84 D	2	2	2	2	2	2
8s uncertainty (95%)	=B83+B82/SQRT(B84)	=D83*D82/SQRT(D84)	=F83+F82/SQRT(F84)	=H83*H82/SQRT(H84)	=J83*J82/SQRT(J84)	=L83+L82/SQRT(L84)
86 mean	=AVERAGE(B79:C79)	=AVERAGE(D79:E79)	=AVERAGE(F79:G79)	=AVERAGE(H79:179)	=AVERAGE(J79:K79)	=AVERAGE(L79:M79)
87						
88 max thermocouple voltage (mV)	=MAX(78:78)					
89 CH 8 (voltage max)	=MAX(79:79)					
90 thermocouple error (%)	0.0075					
91 maximum thermocouple voltage error (mV)	=B90*B88					
92 ICH8 gain	=AVERAGE(B80:AM80)					
93 maximum thermocouple voltage error after telemetry gain (V)	=B91+B92/1000					
94 CH8 maximum uncertainty (V) (confidence:95%)	=MAX(B85:AM85)					
95 Combined error (V) (confidence: 95%)	=SQRT(B93^2+B94^2)					
se Combined error (%) (confidence: 95%)	=(B95/B89)*100					

AG			7.37								7.42					
AC AL	525	29.08072727273	7.32 7.38	=AF58/(AF57/1000)	=STDEV(AF58:AG58)	12.71	2	-afe2-afe1/sgrTafe3) -avenage[af58-ag58]	525	29.080727272733	7.34 7.43	=AF79/(AF78/1000)	=STDEV(AF79:AG79)	12.11	= =AF83*AF82/SORT(AF84)	AVERAGE(AFP9-AG79)
5	520	28.7979090909091		=AD58/(AD57/1000)	=STDEV(AD58:AE58)	12.71	2	=AD61/SQRT(AD63) =AVEAGE(AD58:AE58)	520	28.7979090909091		=AD79/(AD78/1000)	=STDEV(AD79:AE79)	17.11	=ADR3*ADR2/SORT(ADR4)	=AVERAGE(AD79-AE79)
			7.24								7.26					
	515	28.51622727273	7.16 7.23	=AB58/(AB57/1000)	=STDEV(AB58:AC58)	12.71	2	=AB62 *AB61/SORT(AB63) =AVERAGE(AB58 AG58)	515	28.5162272727273	7.18 7.27	=AB79/(AB78/1000)	=STDEV(AB79:AC79)	12.11	=AB83*AB82/SORT(AB84)	AVERAGE(AR7) ACT9)
	510	28.23454545454555	Γ	=Z58/(Z57/1000)	=STDEV(Z58:AA58)	12.71	2	=22 ² 261/SQRT[263] =AVERAGE[28/A458]	510	345454545455		=Z79/(Z78/1000)	=STDEV(Z79:AA79)	17.71	=783+782/SORT(784)	AVERAGE(J79 JA79)
	505	27.9537727272727		=X58/(X57/1000)	=STDEV(X58:Y58)	12.71	2	=X62*X61/SQRT(X63) =AVERAGE(X58Y58)	505	27.9537727272727		=X79/(X78/1000)	=STDEV(X79:Y79)	12./1	=X83*X82/SORT(X84)	=AVERAGE(X)3:Y19)
	200	27.673		=V58/(V57/1000)	=STDEV(V58:W58)	12.71	2	=V62*V61/SQRTV63) =AVERAGE(V58:W58)	200	27.673		=V79/(V78/1000)	=STDEV(V79:W79)	2	=V83*V82/SORTIV84)	aveace(v?)
•	495	27.3930454545455		=T58/(T57/1000)	=STDEV(T58:U58)	12.71	2	=T62+T61/SQRT(T63) -AVERAGE(T58:U58)	495	27.3930454545455		=T79/(T78/1000)	=STDEV(T79:U79)	12./1	=TR3+TR2/SORT(TR4)	AVERAGE [T9.U79]
r	490	27.1130909090909	6.77 6.85	=R58/(R57/1000)	=STDEV(R58:S58)	12.71	2	=RG2-RE1/SORT(R63) =AVEPAGE(R58-558)	490	27.113090909090909	6.82 6.87	=R79/(R78/1000)	=STDEV(R79:S79)	12.11	=RR3+RR2/SORT(R84)	AVERAGE(R79579)
	485	26.833909090901		=P58/(P57/1000)	=STDEV(P58:058)	12.71	2	=P62*P6J/SQRT(P63) *AVERAGE(P58:038)	485	26.8339090909091		=P79/(P78/1000)	=STDEV(P79:Q79)	1/71	=PR3+PR2/SORT(PR4)	AVERAGE(P79.079)
-	480	26.554727272723	6.7	=N58/(N57/1000)	=STDEV(N58:058)	12.71	2	=N27-N61/SORT(N63) #AVERAGE(N58:O58)	480	26.5547272727273		=N79/(N78/1000)	=STDEV(N79:079)	12./1	=NR3+NR2/SORT(NR4)	=AVERAGE(N79.079)
5			6.62	5 5				64 65 66 66 66 66 70 71 71 71 73 73			6.67					888 877 888 888 889 90 91 92 93 93

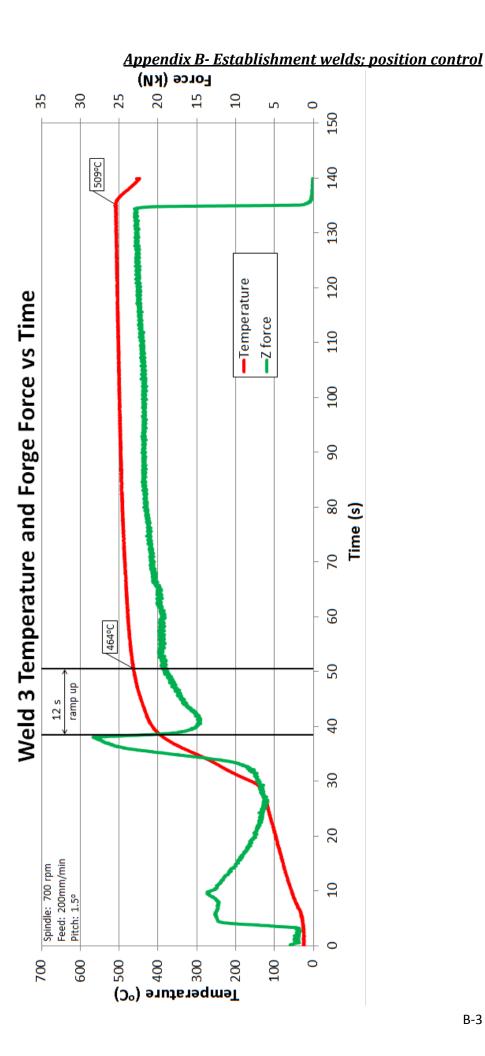
54 53 53 53 54 54 55 53 535 255454555 53 25 74 76 56 23 74 23 255355555 25 25 75 76 56 73 745 23 745 23 75 76 56 73 745 745 745 76 76 76 56 73 745 745 745 76 76 76 56 73 745 745 745 74 76 76 57 23 23 23 23 23 23 76 74 74 74 74 74 76 76 75 74 74 74 74 76 76 75 74 74 74 74 76 76 76 74 74 74 74 76	AG.	АН	A	A	AK	AL	AM
530 535 535 536 500 737 7.45 25.6474554555 25.6474554565 29.31365656565 737 7.45 25.6474554561 25.6474554561 25.6474554561 457DEV(AH55A156) -4.510EV(AH55A156) -4.510EV(AH55A156) -5.510EV(AH55A156) -5.510EV(AH55A156) 12.71 2.71 2.71 2.71 2.71 2.71 2.71 2.71 2.71 2.71 2.71 2.71 2.71 2.71 2.71 2.71 2.71 2.71 2.71 2.71 2.71 2.71 2.71 2.71 2.71 2.71 2.71 2.71 2.71 2.71 2.71 2.72 2.74 2.71 2.71 2.71 2.71 2.71 2.71 2.71 2.71 2.71 2.71 2.71 2.71 2.71 2.72 2.8555555555555555555555555555555555555	et						
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29 29 29 29 29 29 20<	10	530		535		540	
7.37 7.45 7.36 7.31 7.45	2	29.3635454545455		29.6474545454545		29.931363636363636	
=AH58/(AH57/1000) =AL58/(A157/1000) =AL58/(A157/1000) -\$TDEV(AH58A158) -\$TDEV(A158A58) \$TDEV(A158A68) 1271 2 2 1271 2 2 -#VERAGE(AH56A159) -#AL57/1000) -#L57/1000) -at62*AH6150RT(AH63) -#CVERAGE(AH56A159) -#CVERAGE(AH56A159) -at62*AH6150RT(AH63) -#AVERAGE(AH56A159) -#AVERAGE(AH56A159) -at62*AH6150RT(AH63) -#AVERAGE(AH56A159) -#AVERAGE(AH56A159) -at62*AH6150RT(AH63) -#AVERAGE(AH56A159) -#AVERAGE(AH56A159) -at473/(AT78/1000) -#AVERAGE(AH79A179) -#AVERAGE(AL79-AM79) -at473/(AT78/1000) -at77/1000) -at79/(AT78/1000) -at473/(AT78/1000) -at79/(AT78/1000) -at79/(AT78/1000) -at171 -at77 -at79/(AT78/1000) -at18*H192*A179) -at83*A1825/06T1(A1494) -at171 -at83*A1825/06T1(A1494) -at18*H18*H192*A179) -at83*A1825/06T1(A1494) -at18*H18*H192*A179) -at83*A1825/06T1(A1494) -at18*H18*H192*A179) -at83*A1825/06T1(A1944) -at18*H192*A179) -at8		7.45	.46	7.52	7.53	7.61	7.6
"eTDEV(AHSE ALS6) "eTDEV(ALSE ANS6) "eTDEV(ALSE ANS6) 1271 2 1271 2 2 2 2 2 3 2 2 2 4VERAGE(AHSE ALS6) 24/E4245455 2 2 4VERAGE(AHSEALS6) 2 2 2 2 -4462*4451/SGRT(AH55) -4462*4451/SGRT(AH55) -4462*4451/SGRT(AH55) 4VERAGE(AHSEALS6) 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2		=AH58/(AH57/1000)		=AJ58/(AJ57/1000)		=AL58/(AL57/1000)	
"45TDEVIAH58A158) "45TDEVIAH58A158) "45TDEVIAH58A158) 12.71 2 2 2 2 2 *AVERAGE(AH58A158) *AUE2*A161/SQRT[AL63) *AUE2*A161/SQRT[AL63) *AVERAGE(AH58A158) *AUE2*A161/SQRT[AL63) *AUE2*A161/SQRT[AL63) *AVERAGE(AH58A158) *AUE2*A161/SQRT[AH63) *AUE2*A161/SQRT[AL63) *AVERAGE(AH58A158) *AVERAGE(AL58AM58) *AUE3*A153 *AVERAGE(AH58A158) *AUE3*A159) *AUE3*A159 \$S00 \$S00 \$S0 \$S0 \$S00 \$S0 \$S0 \$S0	_						
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2 2 2 =AH62*AH6J/GQRT(AH65) =AL62*A461/SQRT(AH65) =AL62*A461/SQRT(AH65) =AL62*A461/SQRT(AH65) =AH62*AH61/SQRT(AH65) =AL62*A461/SQRT(AH65) =AL62*A461/SQRT(AH65) =AL62*A461/SQRT(AH65) =AH62*AH61/SQRT(AH65) =AL62*A461/SQRT(AH65) =AL62*A461/SQRT(AH65) =AL62*A461/SQRT(AH65) =S00 530 535 29.61/S45454545 20.91/S6666666 S00 535 29.647/S454545455 7.82 20.91/S6666666 S10 7.40 7.40 7.40 7.64 20 535 29.647/S4545455 29.91/S6666666 20.91/S6666666 21 7.40 7.40 7.40 7.40 7.40 21 7.41 7.40 7.41 7.40 7.41 21 7.41 7.000 1.71 2 2 21 21 1.71 1.71 2 2 21 21 1.71 1.71 2 2 21 21 21 2 2 2	01	12.71		12.71		12.71	
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530 535 540 530 535 540 7.22 29.38554545455 540 7.32 7.49 7.57 29.385545454555 7.49 7.51 27.73 7.49 7.57 =AH79/(AH78/1000) =AH79/(AH78/1000) =AH79/(AH78/1000) =AH79/(AH78/1000) 25.71 20.6474545454545455 27.71 27.71 27.71 2.71 27.71 2.71 27.71 2.71 27.71 2.71 27.71 2.71 27.71 2.73 27.71 2.744567(A179-A179) =AH82/SORT(AH94) =A185-A482/SORT(A484) =A185-A482/SORT(AH94) =A185-A482/SORT(A484)							
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530 535 742 29 59355456565 742 743 75 54 -ar179/(Ar178/1000) 7.43 7.55 7.56 -ar179/(Ar178/1000) -ar179/(Ar178/1000) 7.56 7.56 -ar179/(Ar178/1000) -ar179/(Ar178/1000) 7.56 7.56 -ar179/(Ar178/1000) -ar179/(Ar178/1000) 7.56 7.56 -ar178/Ar179 -ar179/(Ar178/1000) 7.51 7.51 -ar178/Ar179 -ar179/(Ar178/1000) 2.71 2.71 12.71 2 2 2.71 2.71 2 2 2 2.71 2.71 2 2 2 2.73 3.4153*AL82/SQRT(AL84) -ar185*Art82/SQRT(Ar184) -ar185*AL82/SQRT(Ar184) -ar183*AL82/SQRT(Ar184) -ar185*Art82/SQRT(Ar194) -ar187*AL82/SQRT(Ar194) -ar183*AL82/SQRT(Ar184) -ar185*Art82/SQRT(Ar194) -ar185*AL82/SQRT(Ar194) -ar183*AL82/SQRT(Ar194)							
29:6654545555 26:64745454545 29:1565656565 7.42 7.49 7.49 7.64 8.479(A175)(A17		530		535		540	
7.42 7.48 7.49 7.57 7.54 7.64 - M-TP9/(M-T8/1000) - M-T9/(M-T8/1000) - M-T9/(M-T8/1000) - M-T9/(M-T8/1000) - SEDEV(AH79-AI79) - SEDEV(AL79-AK79) - SEDEV(AL79-AK79) - SEDEV(AL79-AK79) 12.71 1.2.71 1.2.71 1.2.71 1.2.71 2 2 2 2 2 - eH85-eH83-eH82-SQRT(AH84) - aL83-AL82/SQRT(AL84) - aL83-AL82/SQRT(AL84) - aAH83-eH82-AH73-A179) - aL83-AL82/SQRT(AL84) - aL83-AL82/SQRT(AL84) - aVERAGE(AH79-A179) - aL83-AL82/SQRT(AL84) - aL83-AL82/SQRT(AL84)		29.3635454545455		29.647454545454545		29.931363636363636	
-4179/(4178/1000) -4179/(4178/1000) -51DEV(4H79-A179) -51DEV(4J79-AK79) 12.71 12.71 -2 -4H83-4H82/90RT(AH84) -4488-7492) -4N88-74179-4179) -4VERAGE(AJ79-A779) -4VERAGE(AH79-A179) -4VERAGE(AJ79-A779)		7.48	.49	7.57	7.58	7.64	7.63
-stdev(AH79-A179) -stdev(AJ79-AK79) 12.71 12.7 		=AH79/(AH78/1000)		=AJ79/(AJ78/1000)		=AL79/(AL78/1000)	
=STDEV(AH79:A179) =STDEV(A179:AK79) 12.71 2.21 2.2483:4482/SQRT(A484) = 4885:4482/SQRT(A484) =AVERAGE(AH79:A179) =AVERAGE(A179:AK79) =AVERAGE(AH79:A179)							
12.71 12.71 = 4H83-4H82/90RT(AH84) = 4885-M82/90RT(AH84) = 4885-M82/90RT(AH84) = 4885-M82/90RT(AH84) = 40 FRAGE(AL79-A/79) = 40 FRAG		=STDEV(AH79:AI79)		=STDEV(AJ79:AK79)		=STDEV(AL79:AM79)	
2 -4H3*4H82/5QRT(AH84) 2 -4H3*4H82/5QRT(AH84) -4H3*4H82/5QRT(AH84) -4H3*4H84) -4H84*4H84		12 71		12 71		12 71	
-aH83-aH82/SQRT(AH84) -al83-sU82/SQRT(AJ84) -aVERAGE(AH79-A179) -aVERAGE(AT79-aK79)		2		2		2	
AVERAGE(AH79A179) - AVERAGE(AJ79A79) - AVERAGE(AJ79A79)				(ValV)1003/ calV+201V-		108 IV/LdOs/ c8 IV+28 IV-	
AVEKAGL(AH')9-AVEKAGL(AU'9)						-שרפס שרפל/סמעו (שרפא)	
				=AVERAGE(AU/9:AK/9)		=AVERAGE(AL/9:AM/9)	

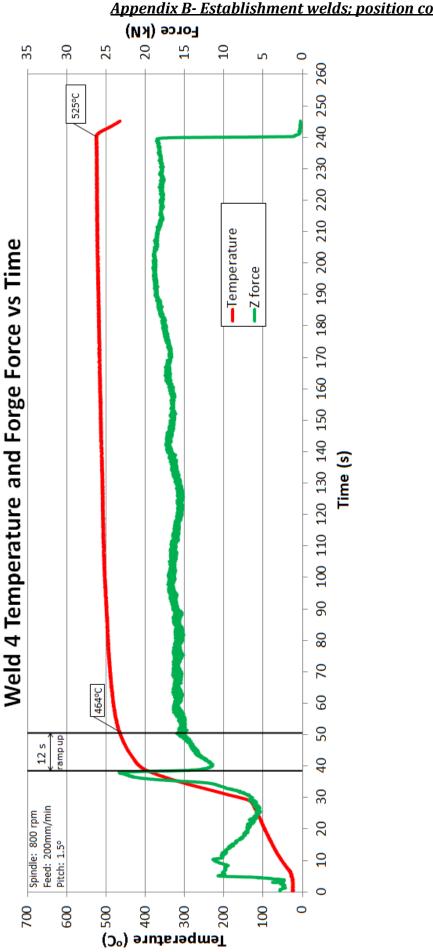


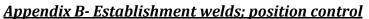


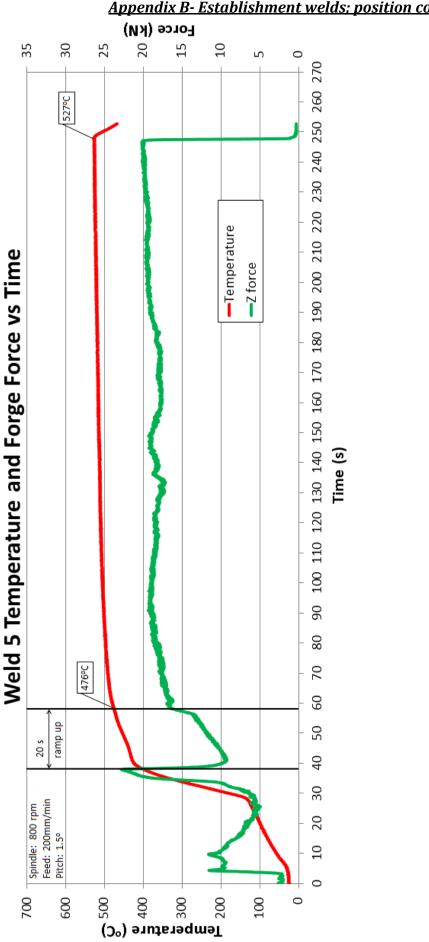


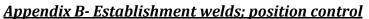


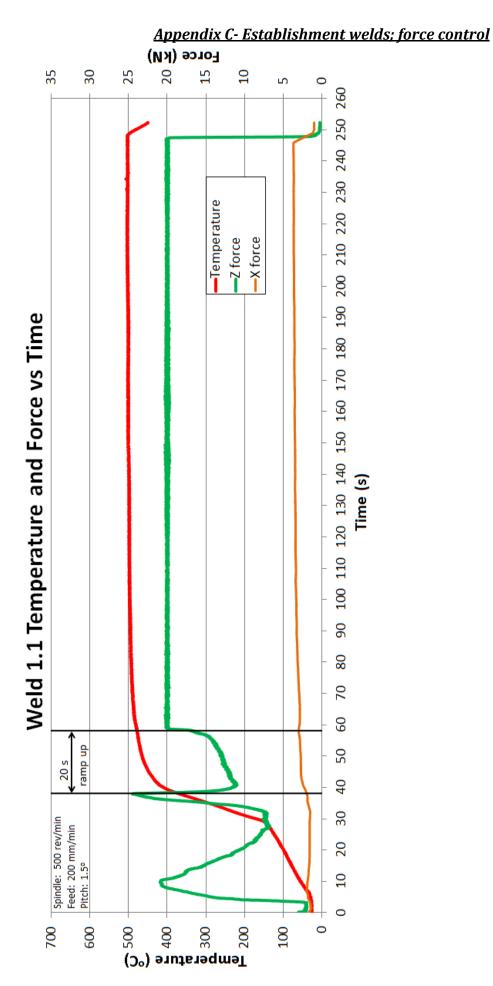




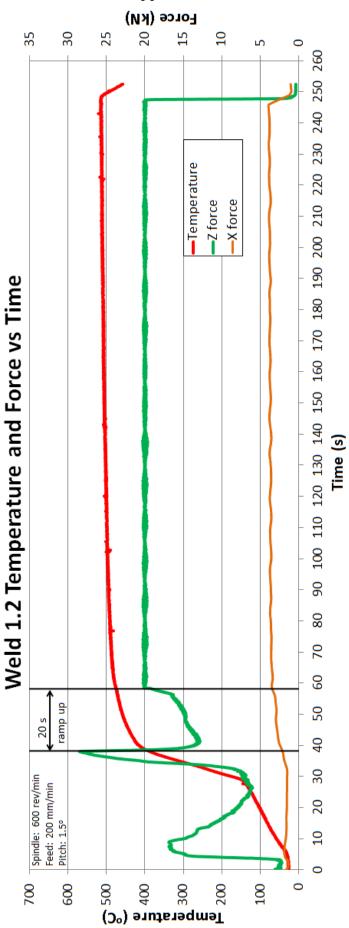


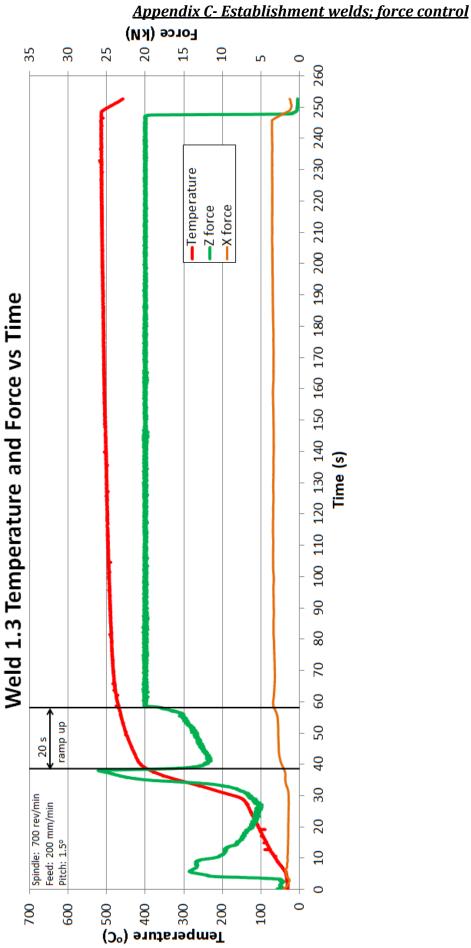


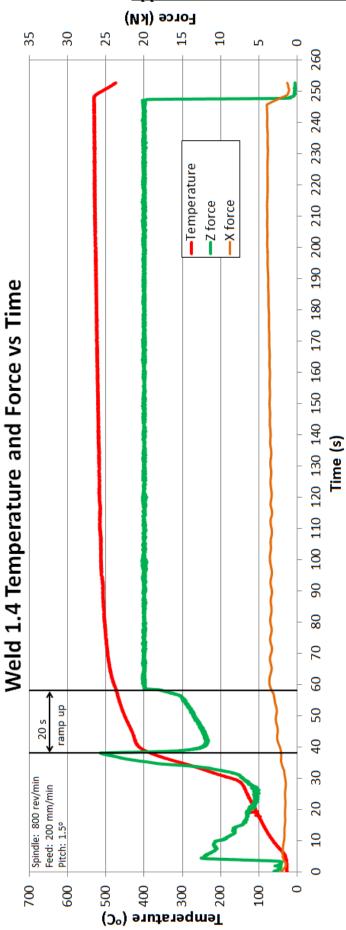


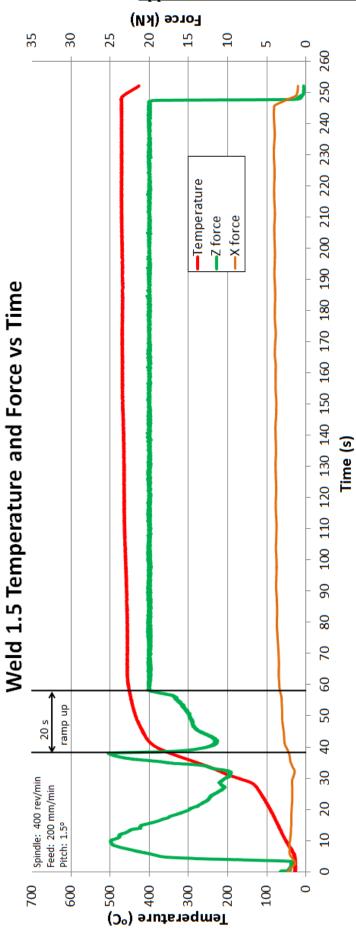


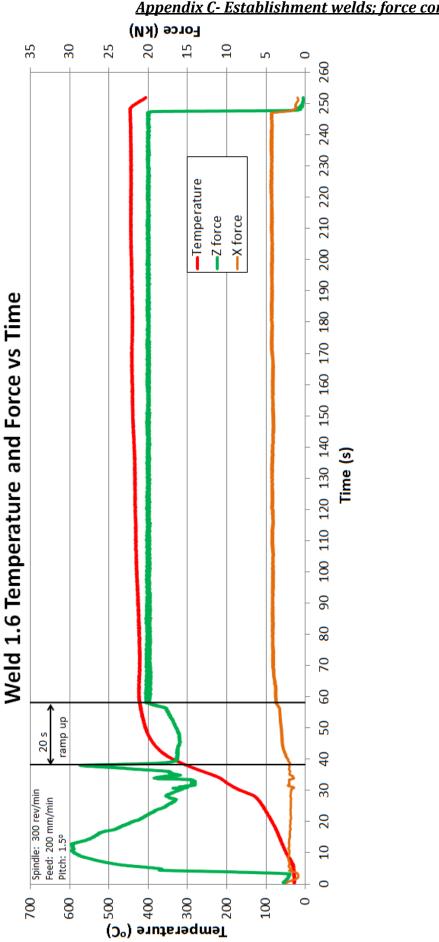
C-1

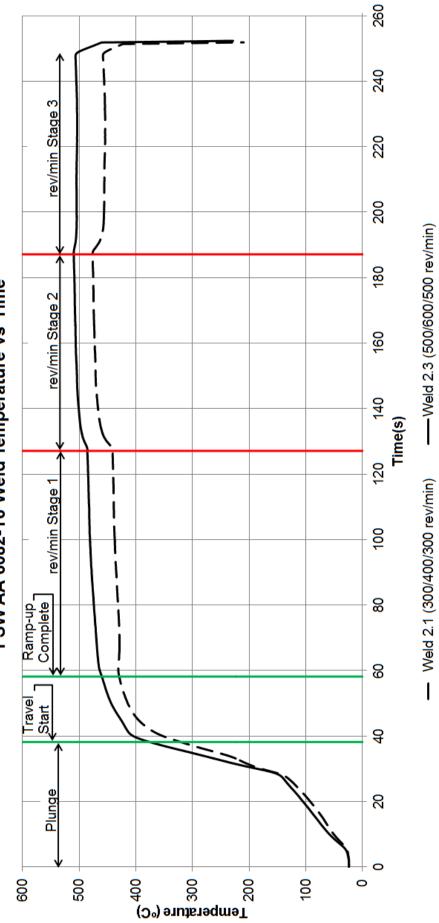




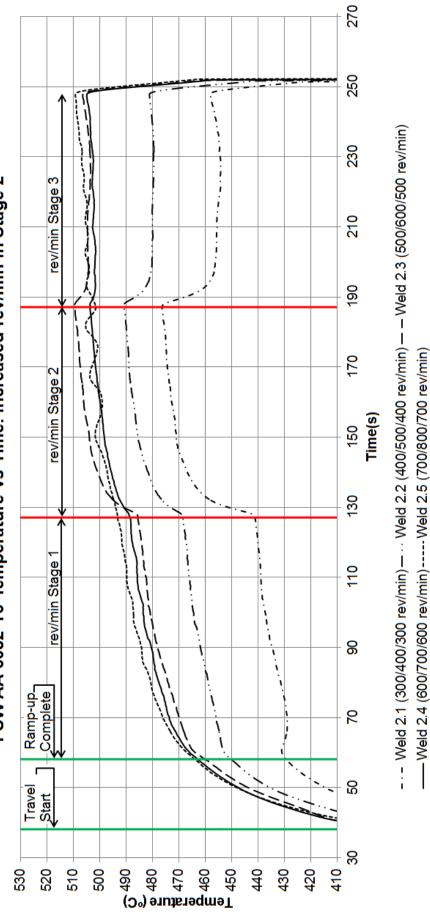


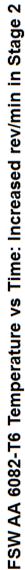


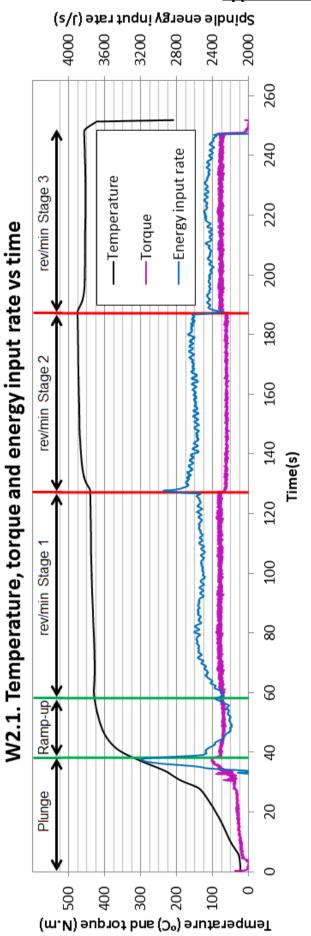




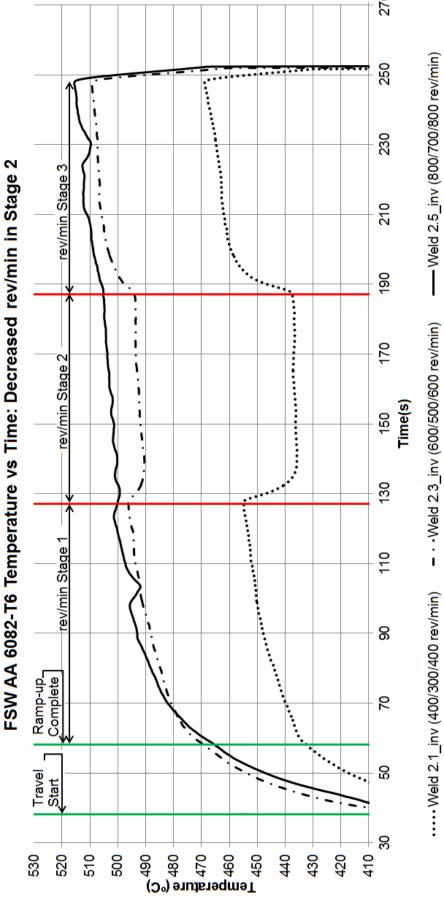


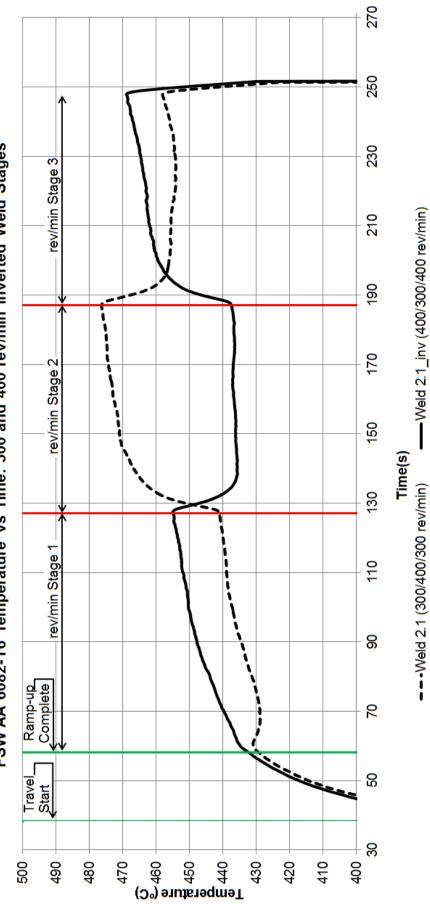




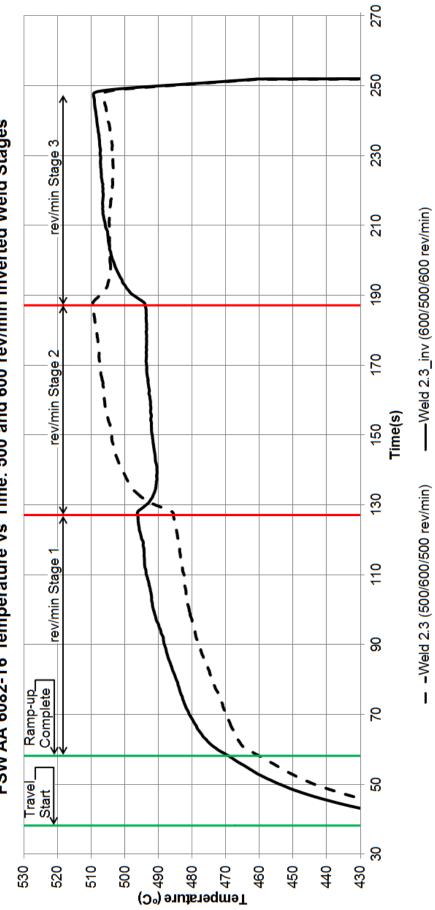




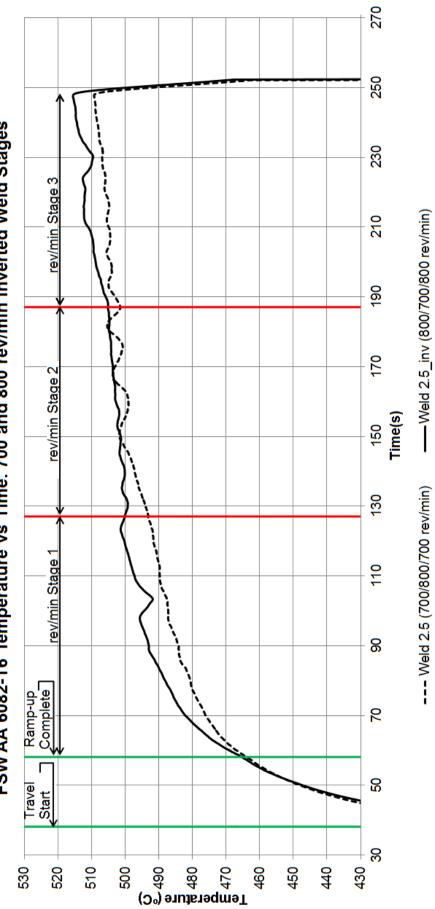




FSW AA 6082-T6 Temperature vs Time: 300 and 400 rev/min Inverted Weld Stages

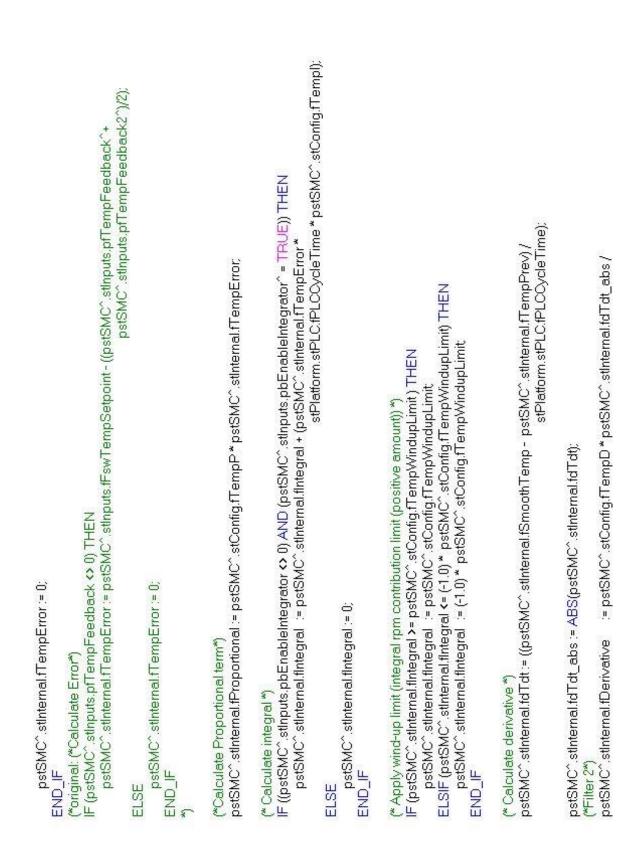


FSW AA 6082-T6 Temperature vs Time: 500 and 600 rev/min Inverted Weld Stages

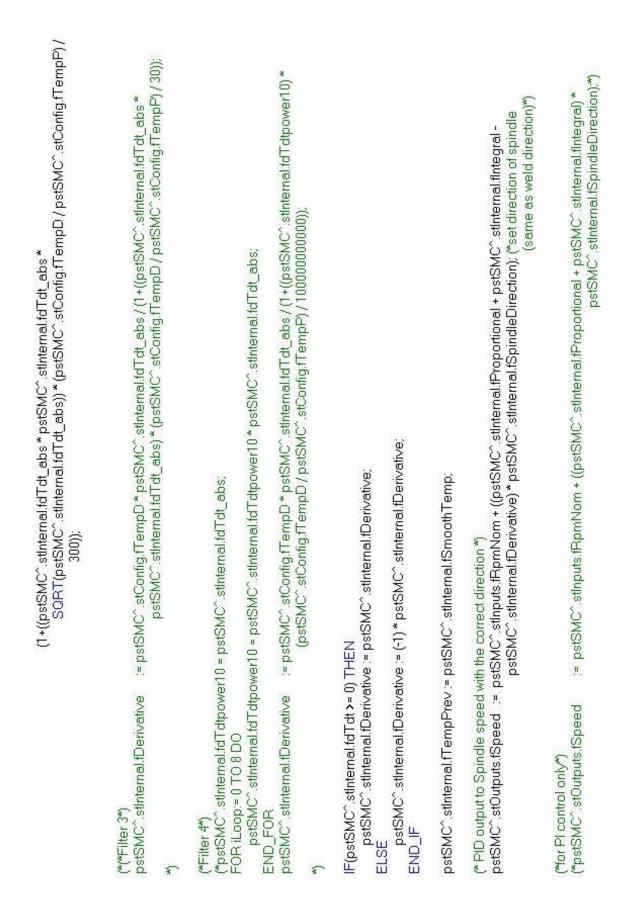


FSW AA 6082-T6 Temperature vs Time: 700 and 800 rev/min Inverted Weld Stages

Control: puts.bDriveEnable = TRUE; puts.bDriveNotHalt = TRUE; puts.bDriveOn = TRUE; puts.eControlMode = eSDCM_VelocityControl;	IF (pstSMC^ stInputs.fRpmNom >=0) THEN pstSMC^ stInternal.fSpindleDirection := 1.0; ELSE pstSMC^ stInternal.fSpindleDirection := -1.0; END_IF	*Calculate moving average of temperature*) FOR iLoop:= 0 TO 99 DO IF (iLoop<99) THEN pstSMC^ stInternal.arrTemperature_history[iLoop] := pstSMC^ stInternal.arrTemperature_history[iLoop + 1]: pstSMC^ stInternal.arrTemperature_history[iLoop] := ((pstSMC^ stInputs.pfTempFeedback^+) pstSMC^ stInternal.arrTemperature_history[iLoop] := ((pstSMC^ stInputs.pfTempFeedback^+)		SmoothTemp := 0;	FOR nLoop:= 0 TO 99 DO pstSMC^.stInternal.fSmoothTemp := pstSMC^.stInternal.fSmoothTemp + pstSMC^.stInternal.arrTemperature_history[nLoop]; END_FOR	pstSMC^.stInternal.fSmoothTemp := pstSMC^.stInternal.fSmoothTemp / 100;	<pre>(*Calculate Error*) IF (pstSMC^.stInputs.pfTempFeedback <> 0) THEN pstSMC^ stInternal.fTempError := pstSMC^ stInputs.fFswTempSetpoint - pstSMC^ stInternal.fSmoothTemp; ELSE</pre>
eSDCM_TemperatureControl: pstSMC^.stOutputs.bDriveEnable pstSMC^.stOutputs.bDriveNotHalt pstSMC^.stOutputs.bDriveOn pstSMC^.stOutputs.eControlMode	IF (pstSMC [^] , stInputs.fRpmNom >=0) THEN pstSMC [^] .stInternal.fSpindleDirection ELSE pstSMC [^] .stInternal.fSpindleDirection END_IF	(*Calculate moving avera FOR iLoop:= 0 TO 99 DO IF (ILoop<99) THEN pstSMC [*] .stInternal.a ELSE pstSMC [*] .stInternal.a	END_IFOR	pstSMC [*] .stInternal.fSmoothTemp := 0;	FOR nLoop:= 0 TO 99 DC pstSMC^.stInternal.f6 END_FOR	pstSMC [*] .stInternal.fSmoo	(*Calculate Error*) IF (pstSMC^.stInputs.pfTe pstSMC^.stInternal.f1 ELSE



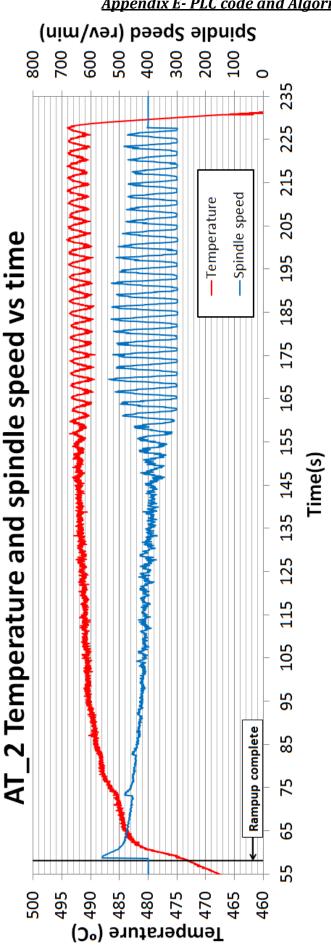
<u> Appendix E- PLC code and Algorithm tuning welds</u>

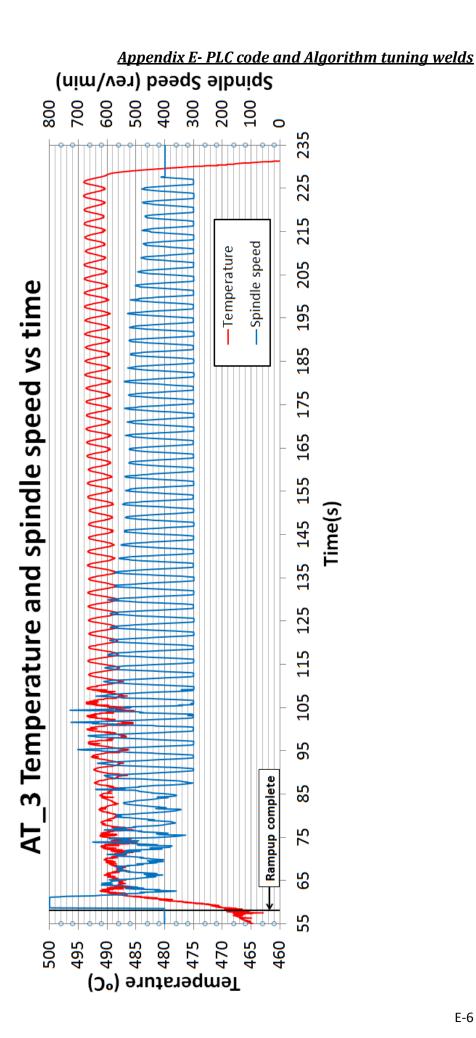


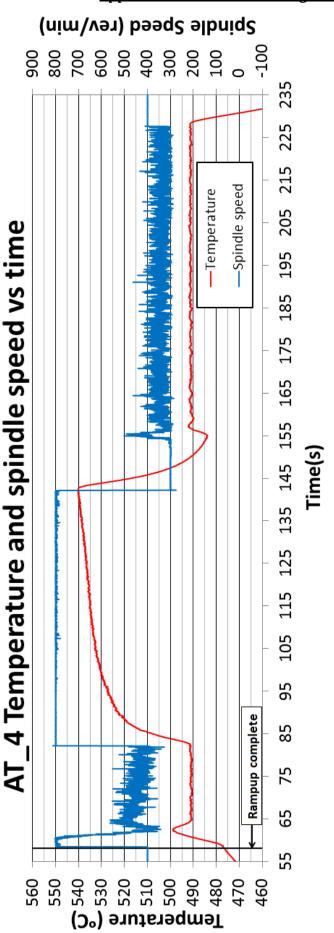
Appendix E- PLC code and Algorithm tuning welds

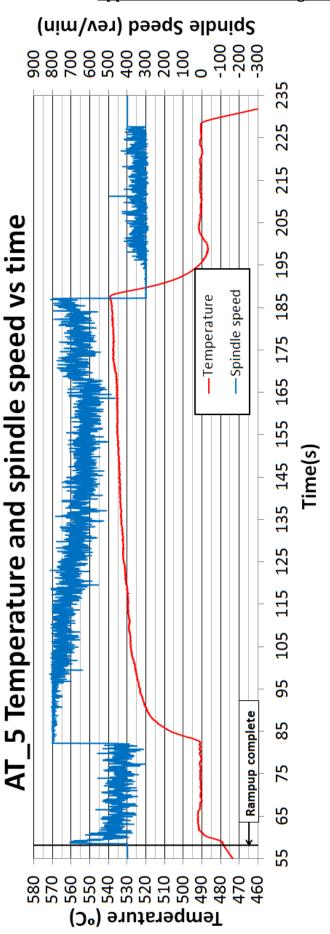
ELSIF (pstSMC^{*}, stOutputs fSpeed > pstSMC^{*}, stInputs fRpmMax) THEN ELSIF (pstSMC^{*}, stOutputs fSpeed < pstSMC^{*}, stInputs fRpmMax) THEN IF (pstSMC^ stOutputs.fSpeed < pstSMC^ stInputs.fRpmMin) THEN IF (pstSMC^ stOutputs.fSpeed > pstSMC^ stInputs.fRpmMin) THEN pstSMC^{*}.stOutputs.fSpeed := pstSMC^{*}.stInputs.fRpmMin; pstSMC^{*}.stOutputs.fSpeed := pstSMC^{*}.stInputs.fRpmMax pstSMC^{*}.stOutputs.fSpeed := pstSMC^{*}.stInputs.fRpmMin; pstSMC^{*}, stOutputs fSpeed := pstSMC^{*}, stInputs fRpmMax IF (pstSMC[°], stInternal.fSpindleDirection > 0)THEN pstSMC^{*}.stOutputs.fPosition := 0.0; END_IF END_IF ELSE

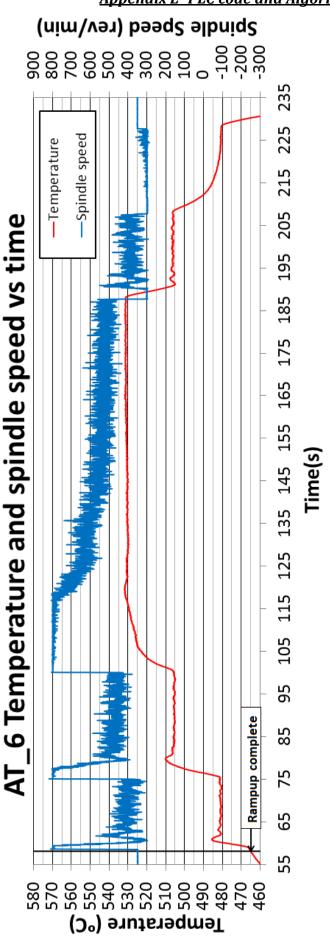
pstSMC^ stInternal.fCoolerTimer := stPlatform.stPLC.fPLCOycleTime; pstSMC^{*}.stOutputs.fTorque := 0.0;



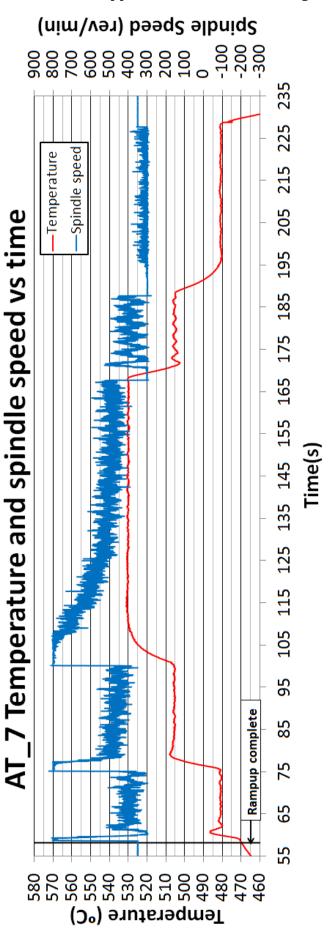


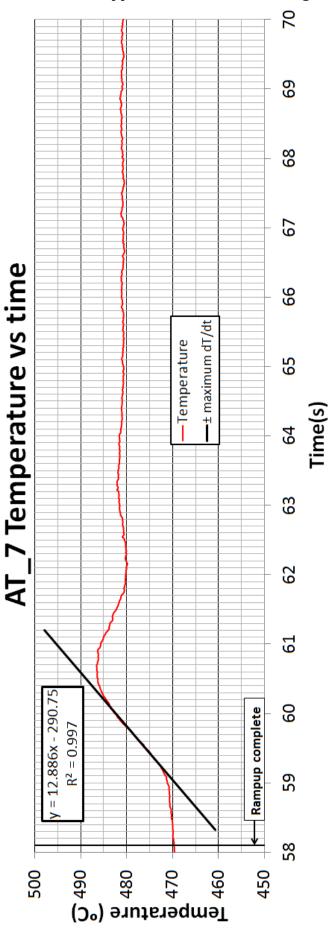




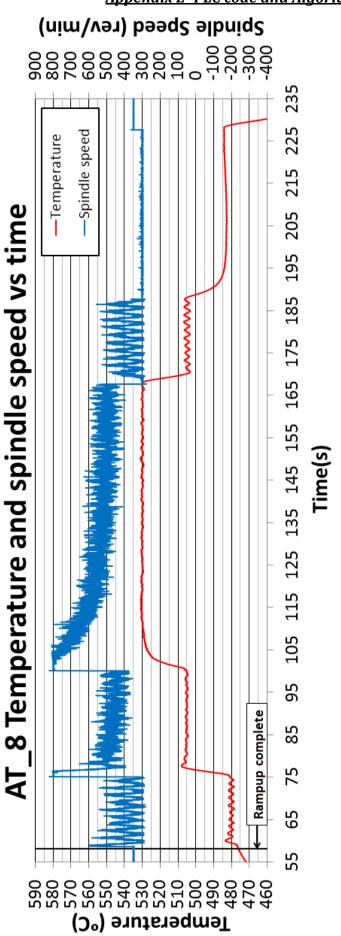


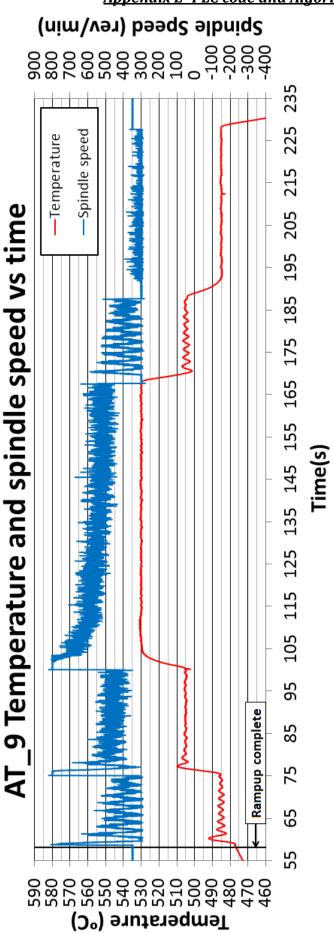
<u>Appendix E- PLC code and Algorithm tuning welds</u>

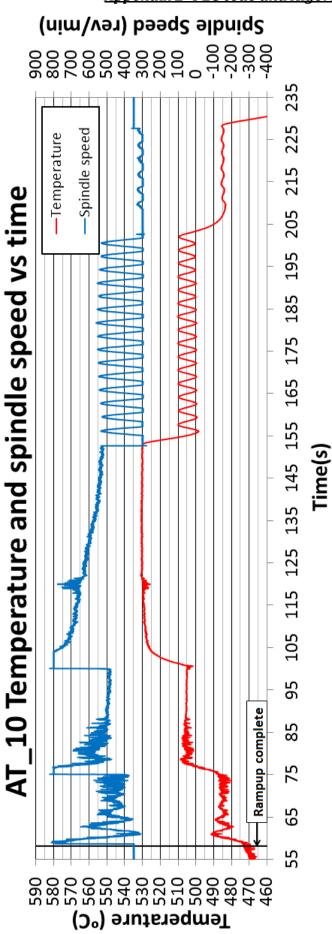


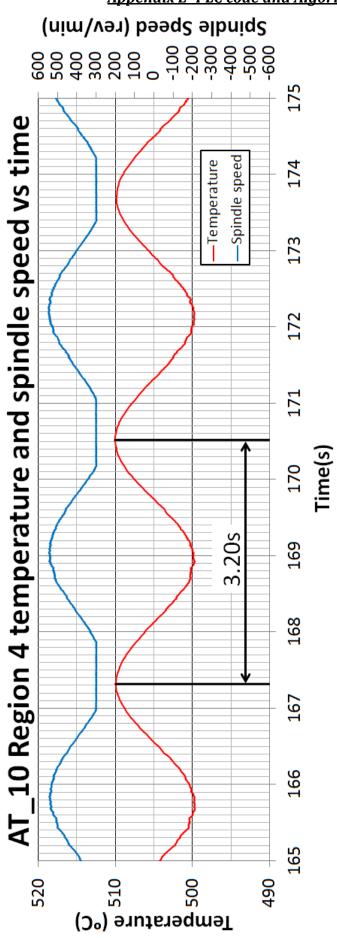


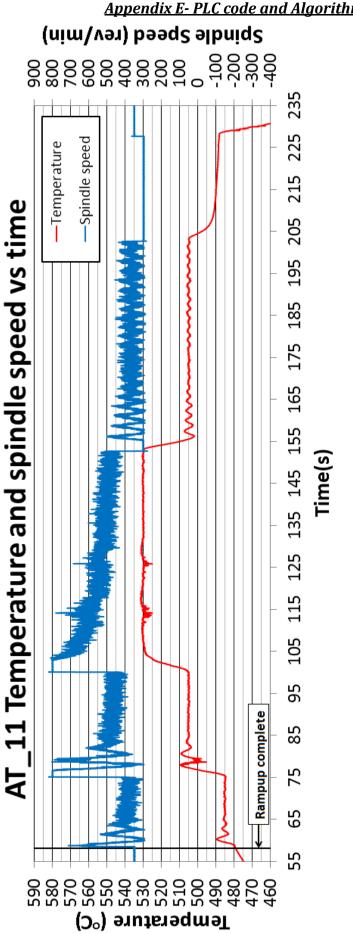
Appendix E- PLC code and Algorithm tuning welds



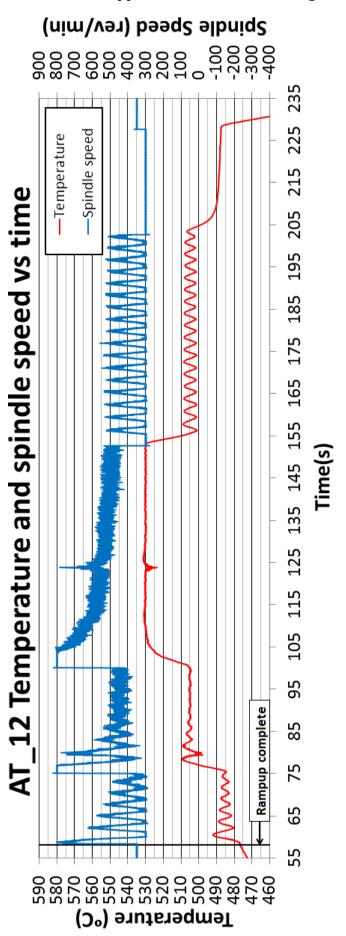


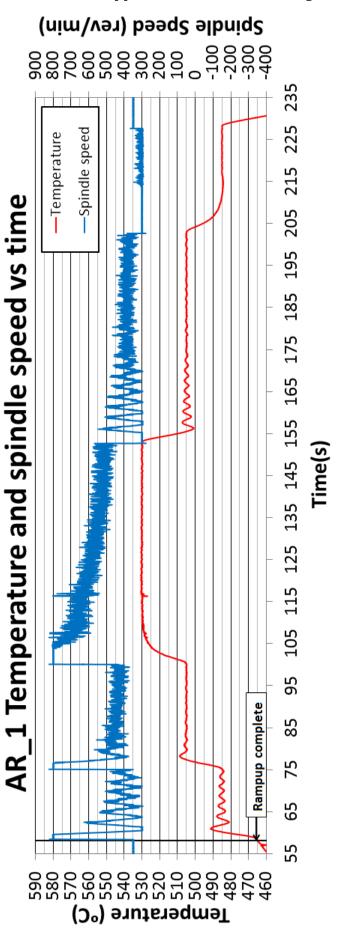


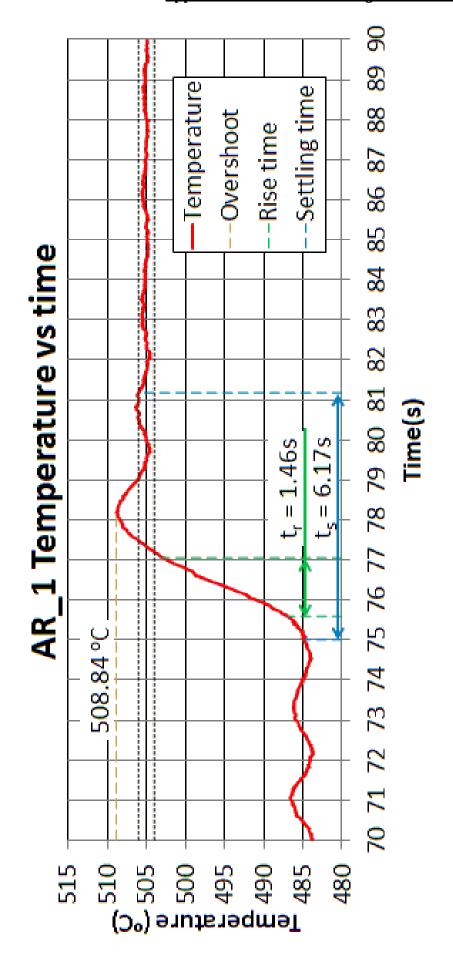




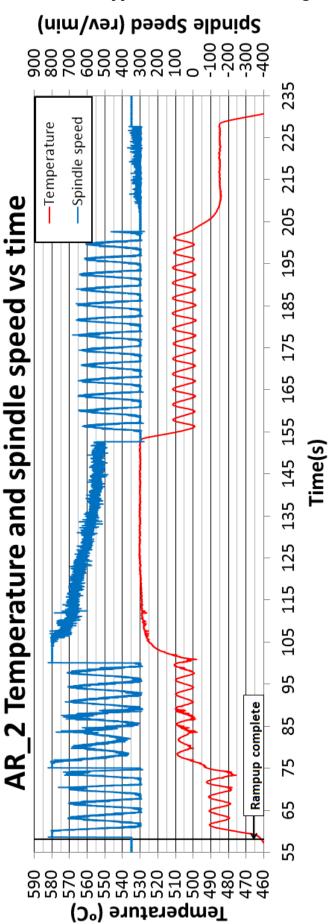
Appendix E- PLC code and Algorithm tuning welds











AT 7	' steady s	tate r	egions
Region	/	Region	
2	Region 2	4	Region 4
time	temperature (°C)	time	temperature (°C)
(s) 82	(C) 506.4276	(s) 175	(C) 505.2010
82.02	506.4370	175.02	505.3032
02.02	500.4570	175.02	505.5052
82.04	506.2319	175.04	505.2334
82.06	506.2922	175.06	505.2229
82.08	506.1275	175.08	505.1837
82.1	506.2932	175.1	505.2465
82.12	506.2361	175.12	505.3329
82.14	506.1663	175.14	505.4301
82.16	506.2219	175.16	505.5032
82.18	506.2329	175.18	505.4712
82.2	506.2314	175.2	505.5257
82.22	506.1856	175.22	505.5754
82.24	506.1929	175.24	505.6701
82.26	506.0652	175.26	505.7098
82.28	506.0945	175.28	505.6221
82.3	506.1558	175.3	505.6781
82.32	506.1102	175.32	505.8021
82.34	506.1986	175.34	505.5572
82.36	506.0921	175.36	505.6992
82.38	506.0209	175.38	505.6872
82.4	506.0856	175.4	505.9018
82.42	506.1528	175.42	505.9619
82.44	506.0825	175.44	505.9640
82.46	505.9920	175.46	505.9605
82.48	505.9980	175.48	505.9849
82.5	505.9562	175.5	506.0990
82.52	505.9063	175.52	505.9943
82.54	505.8178	175.54	506.1356
82.56	505.7907	175.56	506.1799
82.58	505.8235	175.58	506.3083
82.6	505.8792	175.6	506.3756
82.62	505.8384	175.62	506.2402
82.64	505.8940	175.64	506.2416
82.66	505.8164	175.66	506.3371
82.68	505.7475	175.68	506.3434

Region 2				
Mean (°C)	n	t- critical	Standard deviation	Uncertainty (95%)
505.5401	901	1.96	0.2802	0.0183

Region 4				
Mean (°C)	n	t- critical	Standard deviation	Uncertainty (95%)
505.4541	601	1.96	0.5540	0.0443

*Note: data sampling period is 20 ms although the PLC program (including the temperature control algorithm code) is executed every millisecond

82.7	505.7297	175.7	506.3901
82.72	505.6256	175.72	506.4330
82.74	505.6166	175.74	506.3421
82.76	505.5431	175.76	506.3217
82.78	505.6464	175.78	506.3784
82.8	505.6783	175.8	506.3527
82.82	505.6746	175.82	506.3452
82.84	505.7170	175.84	506.2554
82.86	505.6886	175.86	506.1596
82.88	505.6908	175.88	506.1369
82.9	505.6114	175.9	506.1438
82.92	505.7011	175.92	506.1251
82.94	505.6056	175.94	506.0302
82.96	505.4452	175.96	505.9876
82.98	505.5348	175.98	505.9377
83	505.4462	176	506.0070
83.02	505.4932	176.02	505.9258
83.04	505.7212	176.04	505.8791
83.06	505.7446	176.06	505.7398
83.08	505.7681	176.08	505.7926
83.1	505.8811	176.1	505.7663
83.12	505.9248	176.12	505.7461
83.14	505.9785	176.14	505.7283
83.16	505.8027	176.16	505.7343
83.18	505.7637	176.18	505.6902
83.2	505.7410	176.2	505.6608
83.22	505.7962	176.22	505.4998
83.24	505.9669	176.24	505.4174
83.26	505.8956	176.26	505.4109
83.28	505.7298	176.28	505.2624
83.3	505.7822	176.3	505.1792
83.32	505.7715	176.32	505.1039
83.34	505.7451	176.34	505.2878
83.36	505.7539	176.36	505.2702
83.38	505.7426	176.38	505.1331
83.4	505.7223	176.4	505.0037
83.42	505.6635	176.42	505.0802
83.44	505.7246	176.44	505.2138
83.46	505.5428	176.46	505.0453
83.48	505.6355	176.48	505.0808
83.5	505.5715	176.5	505.0436
83.52	505.4879	176.52	505.0183
83.54	505.4161	176.54	505.0830

83.56	505.5096	176.56	504.9205
83.58	505.6250	176.58	504.7950
83.6	505.7408	176.6	504.8107
83.62	505.8048	176.62	504.7838
83.64	505.5313	176.64	504.5655
83.66	505.5111	176.66	504.4793
83.68	505.4583	176.68	504.6601
83.7	505.3917	176.7	504.5045
83.72	505.4489	176.72	504.4554
83.74	505.5110	176.74	504.5236
83.76	505.4505	176.76	504.5073
83.78	505.5990	176.78	504.4674
83.8	505.6369	176.8	504.3194
83.82	505.5546	176.82	504.3448
83.84	505.5591	176.84	504.2129
83.86	505.6025	176.86	504.3568
83.88	505.6332	176.88	504.3878
83.9	505.6326	176.9	504.5345
83.92	505.4234	176.92	504.5003
83.94	505.4068	176.94	504.5393
83.96	505.4913	176.96	504.6085
83.98	505.4525	176.98	504.6186
84	505.4826	177	504.5515
84.02	505.5999	177.02	504.5165
84.04	505.6276	177.04	504.5314
84.06	505.6732	177.06	504.5821
84.08	505.6076	177.08	504.6411
84.1	505.7481	177.1	504.6500
84.12	505.7277	177.12	504.7165
84.14	505.6862	177.14	504.8363
84.16	505.7603	177.16	504.7386
84.18	505.8647	177.18	504.7712
84.2	505.6187	177.2	504.8450
84.22	505.6237	177.22	504.9184
84.24	505.6106	177.24	504.9986
84.26	505.6906	177.26	504.9115
84.28	505.7352	177.28	504.9915
84.3	505.5414	177.3	505.0813
84.32	505.4872	177.32	505.0927
84.34	505.6447	177.34	505.2184
84.36	505.7279	177.36	505.3386
84.38	505.7341	177.38	505.3190
84.4	505.5120	177.4	505.3685

84.44505.4062177.44505.561184.46505.3336177.45505.731484.48505.3892177.48505.670784.5505.3725177.5505.641584.52505.5792177.54505.692484.54505.5792177.54505.598484.55505.515177.62505.540084.64505.515177.62505.846084.62505.515177.62505.846084.63505.5240177.62505.846084.64505.5174177.62505.842084.65505.5240177.62505.634584.66505.7224177.62505.634584.74505.5138177.78505.634384.75505.6174177.78505.724884.74505.6174177.78505.733884.75505.6174177.78505.763584.76505.6174177.78505.763584.78505.4145177.8505.904984.84505.1632177.84506.036784.85505.1632177.94506.036184.94505.2355177.95506.046884.95505.1825177.96506.042884.94505.2353177.96506.042884.95505.1825177.96506.042684.94505.2367177.98505.932385.04505.1825178.04506.102185.04505.1825178.04506.102285.04505.18				<u> </u>
84.46505.3336177.46505.731484.48505.3892177.58505.671084.52505.3725177.52505.641584.52505.5792177.54505.692484.54505.5792177.54505.598484.55505.5513177.62505.540184.64505.5515177.62505.846084.65505.5540177.62505.846084.64505.5154177.62505.846084.65505.5242177.64505.642384.66505.5242177.64505.634584.68505.5342177.72505.634584.72505.5138177.72505.724884.74505.6174177.74505.783884.75505.6174177.78505.733884.76505.6174177.78505.763584.78505.5138177.79505.617484.84505.4145177.84505.904984.84505.1632177.94506.036784.85505.1632177.94506.0198184.94505.2305177.94506.0198184.95505.1632177.94506.0192184.96505.2325177.94506.026184.98505.1632177.94506.0192184.94505.2325177.94506.026184.95505.1825177.94506.026184.96505.3237178.06506.026185.06505.3237178.06506.126985.04	84.42		177.42	505.3860
84.48505.3892177.48505.670784.5505.3725177.5505.641584.52505.5792177.54505.692484.54505.5792177.54505.598484.52505.5513177.65505.540084.64505.5513177.62505.840084.62505.5540177.62505.840084.63505.7224177.64505.617384.64505.5138177.74505.623184.64505.5138177.74505.623384.64505.5138177.74505.623384.74505.6174177.74505.724884.74505.6174177.74505.847884.74505.6466177.76505.847884.74505.6466177.76505.847884.78505.4145177.84505.904984.84505.3760177.84505.904984.84505.2467177.84506.036784.85505.2590177.94506.098184.92505.2590177.94506.046884.93505.1670177.94505.842585.04505.3235177.94506.098184.94505.3235177.94506.072385.04505.3235177.94506.072385.04505.1721178.04506.107585.05505.1721178.04506.108785.04505.2962178.04506.108785.05505.4747178.18506.108785.04505	84.44			
84.52505.3725177.52505.641584.52505.4863177.52505.671084.54505.5792177.54505.692484.55505.5513177.65505.54084.64505.5515177.62505.840084.62505.5540177.64505.840084.64505.5724177.64505.845784.65505.7224177.64505.643284.64505.5138177.74505.643384.74505.5138177.74505.623384.75505.6466177.76505.847884.76505.6466177.76505.847884.78505.5138177.78505.724884.74505.6174177.78505.731884.75505.6466177.76505.847884.78505.4145177.8505.731884.82505.4145177.84505.904984.84505.3760177.84506.036784.84505.2467177.84506.036184.94505.3235177.94506.046884.94505.2590177.94506.046884.94505.3235177.94506.046884.94505.3235177.94506.046884.95505.1721178.04506.103285.04505.2962178.04506.103285.04505.2962178.04506.103785.04505.3237178.04506.103685.04505.4747178.18506.103285.04505	84.46	505.3336		505.7314
84.52505.4863177.52505.671084.54505.5792177.54505.692484.56505.5513177.68505.54084.62505.5515177.62505.846084.64505.5540177.64505.716084.62505.5242177.64505.845784.63505.7224177.64505.634584.74505.4326177.7505.623384.75505.6174177.74505.724884.74505.6174177.74505.847884.75505.6466177.75505.847884.76505.6466177.76505.847884.78505.4145177.8505.738384.78505.4145177.84505.934484.84505.3760177.84505.984484.85505.1632177.84505.984484.86505.2590177.94506.098184.98505.2438177.94506.098184.94505.3235177.94506.098184.95505.1632177.94506.098184.96505.2590177.94506.098184.97505.1670177.98505.932385.08505.1670177.98505.932385.04505.2962178.04506.1072385.04505.2962178.04506.126985.05505.1721178.08506.126985.04505.4726178.14506.139785.04505.4726178.14506.139785.14505	84.48	505.3892	177.48	505.6707
84.54505.5792177.54505.692484.56505.5513177.65505.598484.62505.5515177.62505.81384.62505.5540177.64505.840084.64505.512177.64505.845084.64505.7224177.64505.634584.65505.7224177.64505.634584.76505.5432177.75505.623384.72505.138177.72505.642384.74505.6174177.74505.847884.75505.6466177.76505.847884.76505.6466177.76505.847884.78505.1632177.84505.904984.84505.1632177.84505.904984.84505.2467177.84506.036784.85505.1632177.94506.098184.94505.2590177.92506.056984.94505.2590177.92506.004884.95505.1670177.98505.932385.04505.2962178.04506.102184.98505.1670177.98505.932385.04505.2962178.04506.092185.05505.1721178.08506.126985.04505.2962178.14506.108085.05505.1721178.08506.126985.04505.4726178.14506.108085.05505.1721178.08506.126985.04505.529178.14506.108085.14505.5	84.5	505.3725	177.5	505.6415
84.56505.5513177.56505.598484.58505.5021177.68505.581384.62505.5540177.62505.846084.64505.6017177.64505.716084.64505.7224177.66505.845784.68505.5842177.68505.634584.73505.4326177.7505.662384.74505.6174177.74505.724884.75505.6466177.76505.847884.76505.6466177.76505.847884.78505.5830177.78505.731884.82505.4145177.80505.731384.82505.4145177.80505.904984.84505.3760177.84506.036784.84505.2467177.84506.109884.92505.2590177.92506.058984.93505.1632177.94506.109184.94505.2590177.92506.004884.95505.1825177.94506.109184.96505.2167177.80505.923385.02505.1721178.02505.923385.03505.1825178506.080685.04505.2962178.04506.109185.05505.1721178.08506.126985.04505.2962178.04506.126985.05505.1721178.08506.126985.04505.4726178.14506.108085.12505.4726178.14506.108085.14505.5	84.52	505.4863	177.52	505.6710
84.58505.5021177.58505.544084.62505.5515177.62505.843084.62505.5540177.62505.846084.64505.6017177.64505.716084.65505.7224177.66505.845784.68505.5842177.7505.662384.72505.5138177.7505.62384.73505.6174177.74505.724884.74505.6174177.76505.847884.75505.6466177.76505.847884.78505.4145177.8505.733584.82505.1632177.84505.904984.84505.3760177.84505.984484.84505.1632177.96505.064684.84505.3760177.84506.036784.85505.1632177.90506.098184.92505.2590177.92506.056984.94505.2325177.96506.004884.98505.1670177.84505.932385.02505.1721178.02506.072385.04505.2962178.14506.108785.05505.3237178.06506.080685.08505.4547178.18506.108285.104505.4726178.14506.192885.104505.4726178.14506.192885.124505.36677178.18506.108285.125505.2083178.22506.026185.124505.2083178.22506.026185.245<	84.54	505.5792	177.54	505.6924
84.6505.5515177.6505.581384.62505.5540177.62505.846084.64505.6017177.64505.716084.65505.7224177.68505.634584.76505.5842177.7505.62384.72505.5138177.72505.724884.74505.6174177.74505.783884.75505.6466177.76505.847884.76505.5830177.78505.731884.82505.5830177.84505.763584.82505.4461177.82505.904984.84505.7603177.84506.036784.84505.1632177.98505.984484.84505.2467177.88506.109884.94505.2438177.94506.109184.95505.1632177.94506.004884.94505.2590177.94506.004884.95505.1235177.96506.004884.98505.1670177.98505.932385.02505.1721178.02506.072385.04505.2962178.04506.167585.05505.1237178.08506.126985.10505.4726178.18506.192885.12505.7141178.12506.090785.14505.529178.14506.192885.15505.4726178.16506.192785.14505.529178.14506.192885.14505.3667178.16506.192785.14505.36	84.56	505.5513	177.56	505.5984
84.62505.5540177.62505.846084.64505.6017177.64505.716084.66505.7224177.68505.845784.68505.5842177.7505.634584.7505.4326177.7505.662384.72505.5138177.72505.724884.74505.6174177.74505.788884.75505.6466177.76505.847884.78505.5830177.78505.737184.8505.4145177.82505.904984.84505.3760177.84505.934984.84505.1632177.84505.984184.84505.2467177.88506.036784.85505.2590177.92506.098184.92505.2590177.92506.056984.93505.1670177.98505.932384.94505.1670177.98505.932385.05505.1825178505.032385.04505.2962178.04506.072385.05505.3237178.06506.080685.08505.4527178.18506.126985.10505.4726178.14506.192885.11505.4726178.14506.192885.12505.4726178.14506.192885.14505.529178.14506.192885.15505.3667178.16506.192885.16505.3677178.18506.108285.12505.3866178.22506.026185.22505.2083	84.58	505.5021	177.58	505.5440
84.64505.6017177.64505.716084.66505.7224177.66505.845784.68505.5842177.78505.634584.7505.4326177.7505.662384.72505.5138177.72505.724884.74505.6174177.74505.758884.75505.6466177.76505.847884.76505.6466177.78505.847884.78505.5830177.84505.763584.82505.4145177.8505.904984.84505.1632177.84506.036784.84505.1632177.84506.036784.84505.2407177.88506.109884.94505.2438177.94506.098184.94505.2438177.94506.004884.94505.1670177.88505.932384.95505.1825178505.932385.04505.2962178.04506.072385.04505.2323178.04506.102985.05505.1825178.04506.126985.06505.3237178.06506.080685.08505.4547178.08506.126985.10505.4726178.14506.192885.12505.7141178.12506.090785.14505.5529178.14506.192885.15505.3667178.16506.139785.14505.5529178.14506.192885.15505.3866178.2506.026185.24505.233	84.6	505.5515	177.6	505.5813
84.66505.7224177.66505.845784.68505.5842177.68505.634584.7505.4326177.7505.662384.72505.5138177.72505.724884.74505.6174177.74505.788884.75505.6466177.76505.847884.76505.6466177.78505.877184.8505.5830177.8505.763584.82505.4145177.8505.904984.84505.3760177.84506.036784.85505.1632177.86505.984484.86505.2467177.88506.109884.92505.2590177.92506.056984.94505.3235177.94506.109184.95505.1670177.98505.942584.96505.1721178.02506.072384.98505.1721178.04506.102685.04505.2962178.04506.126985.05505.1721178.08506.126985.06505.3237178.08506.126985.07178.14506.080685.08505.4776178.18506.132785.10505.4796178.14506.139785.12505.3267178.14506.132785.14505.3677178.18506.132785.15505.3667178.18506.132785.16505.3263178.22506.026185.22505.2083178.24506.026185.24505.2353178.2	84.62	505.5540	177.62	505.8460
84.68505.5842177.68505.634584.7505.4326177.7505.662384.72505.5138177.72505.724884.74505.6174177.74505.78884.76505.6466177.76505.847884.78505.5830177.78505.763584.82505.4145177.8505.904984.84505.3760177.84506.036784.85505.1632177.86505.984484.84505.3760177.88506.109884.94505.2467177.88506.098184.95505.2590177.92506.056984.94505.2335177.94506.109184.95505.1670177.98505.042384.96505.1670177.98505.923385.02505.1721178.02506.072385.04505.2962178.04506.105785.05505.13237178.06506.080685.06505.3237178.08506.126985.01505.4726178.14506.080785.12505.7141178.12506.090785.14505.529178.14506.192885.15505.3667178.18506.108285.16505.3677178.18506.108285.16505.3667178.18506.108285.18505.3667178.18506.108285.22505.3866178.2506.026185.24505.2353178.24505.9257	84.64	505.6017	177.64	505.7160
84.7505.4326177.7505.662384.72505.5138177.72505.724884.74505.6174177.74505.758884.76505.6466177.76505.847884.78505.5830177.78505.763584.82505.4145177.8505.763584.82505.4811177.82505.904984.84505.3600177.84506.036784.85505.1632177.86505.984484.86505.1632177.86505.984484.88505.2467177.88506.109884.94505.2590177.92506.056984.95505.2590177.92506.056984.94505.2438177.94506.109184.95505.1825177.96506.004884.98505.1670177.88505.932385.02505.1721178.02506.072385.04505.2962178.04506.167585.05505.4726178.18506.080685.08505.4726178.18506.080785.14505.5299178.14506.192885.15505.4796178.18506.108285.16505.4796178.18506.108285.18505.3667178.18506.108285.14505.3667178.18506.108285.15505.3866178.2506.026185.22505.3866178.2506.026185.24505.2353178.24505.9257	84.66	505.7224	177.66	505.8457
84.72505.5138177.72505.724884.74505.6174177.74505.758884.76505.6466177.76505.847884.78505.5830177.78505.877184.8505.4145177.8505.763584.82505.4811177.82505.904984.84505.3760177.84506.036784.85505.1632177.86505.984484.86505.2467177.88506.098184.91505.2467177.92506.098184.92505.2438177.94506.109184.94505.2438177.94506.004884.95505.1670177.98505.842585.02505.1825177.96506.004884.98505.1670177.98505.932385.02505.1721178.02506.072385.04505.2962178.14506.105985.05505.4547178.08506.126985.10505.4726178.14506.080685.12505.7141178.12506.090785.14505.529178.14506.192885.15505.4796178.18506.108285.16505.3677178.18506.108285.12505.3866178.2506.026185.22505.2083178.24506.026185.24505.2353178.24505.9257	84.68	505.5842	177.68	505.6345
84.74505.6174177.74505.758884.76505.6466177.76505.847884.78505.5830177.78505.877184.8505.4145177.8505.763584.82505.4811177.82505.904984.84505.3760177.84506.036784.85505.1632177.86505.984484.86505.2467177.88506.098184.92505.2467177.92506.098184.93505.2438177.94506.109184.94505.2438177.94506.048884.95505.1670177.98505.932384.96505.1670177.98505.932385.02505.1721178.02506.072385.04505.2962178.04506.167585.06505.3237178.08506.126985.12505.4726178.14506.080685.12505.7141178.12506.090785.14505.529178.14506.192885.15505.4776178.18506.192885.16505.4796178.16506.192785.18505.3677178.18506.108285.22505.2083178.22506.026185.24505.2083178.24506.026185.24505.2353178.24505.9257	84.7	505.4326	177.7	505.6623
84.76505.6466177.76505.847884.78505.5830177.78505.877184.8505.4145177.8505.763584.82505.4811177.82505.904984.84505.3760177.84506.036784.86505.1632177.86505.984484.87505.2467177.88506.109884.9505.2467177.92506.098184.92505.2590177.92506.056984.94505.2438177.94506.109184.95505.1670177.98505.042384.96505.3235177.96506.004884.98505.1670177.98505.932385.02505.1721178.02506.072385.04505.2962178.04506.167585.05505.4726178.16506.080685.12505.7141178.12506.090785.14505.529178.14506.192885.15505.4796178.18506.108285.16505.4796178.18506.108285.18505.3677178.18506.108285.22505.2083178.22506.026185.24505.2353178.24506.0261	84.72	505.5138	177.72	505.7248
84.78505.5830177.78505.877184.8505.4145177.8505.763584.82505.4811177.82505.904984.84505.3760177.84506.036784.86505.1632177.86505.984484.88505.2467177.88506.098184.9505.3425177.9506.098184.92505.2590177.92506.098184.94505.2438177.94506.109184.95505.1670177.98505.048884.98505.1670177.98505.932385.02505.1721178.02506.072385.04505.2962178.04506.167585.05505.3237178.06506.080685.08505.4547178.08506.126985.14505.529178.14506.080985.15505.4726178.14506.192885.16505.4796178.16506.139785.18505.3866178.2506.085285.22505.2083178.22506.026185.24505.2083178.24506.026185.24505.2083178.24505.9257	84.74	505.6174	177.74	505.7588
84.8505.4145177.8505.763584.82505.4811177.82505.904984.84505.3760177.84506.036784.86505.1632177.86505.984484.88505.2467177.88506.109884.9505.3425177.9506.098184.92505.2590177.92506.098184.94505.2438177.94506.109184.95505.1670177.98505.042884.96505.1670177.98505.932384.98505.1670177.98505.932385.02505.1721178.02506.072385.04505.2962178.04506.167585.05505.3237178.08506.126985.10505.4726178.18506.080685.12505.7141178.12506.090785.14505.5529178.14506.192885.15505.3677178.18506.139785.18505.3677178.18506.108285.22505.2083178.22506.026185.24505.2083178.24505.9257	84.76	505.6466	177.76	505.8478
84.82505.4811177.82505.904984.84505.3760177.84506.036784.86505.1632177.86505.984484.88505.2467177.88506.109884.9505.3425177.9506.098184.92505.2590177.92506.056984.94505.2438177.94506.109184.95505.3235177.96506.004884.96505.3235177.96506.004884.98505.1670177.98505.932385.02505.1721178.02506.072385.04505.2962178.04506.167585.06505.3237178.06506.080685.08505.4547178.08506.126985.11505.4726178.14506.090785.12505.4796178.14506.192885.16505.4796178.16506.139785.18505.3677178.18506.108285.22505.2083178.22506.026185.24505.2353178.24505.9257	84.78	505.5830	177.78	505.8771
84.84505.3760177.84506.036784.86505.1632177.86505.984484.88505.2467177.88506.109884.9505.3425177.9506.098184.92505.2590177.92506.098184.94505.2438177.94506.109184.95505.3235177.96506.004884.96505.3235177.96506.004884.98505.1670177.98505.842585505.1825178505.932385.02505.1721178.02506.072385.04505.2962178.04506.167585.05505.3237178.06506.080685.08505.4726178.18506.080785.14505.5529178.14506.090785.14505.5529178.14506.192885.16505.4796178.16506.139785.18505.3677178.18506.085285.22505.2083178.22506.026185.24505.2353178.24505.9257	84.8	505.4145	177.8	505.7635
84.86505.1632177.86505.984484.88505.2467177.88506.109884.9505.3425177.9506.098184.92505.2590177.92506.056984.94505.2438177.94506.109184.96505.3235177.96506.004884.98505.1670177.98505.932385.02505.1721178.02506.072385.04505.2962178.04506.167585.06505.3237178.08506.126985.12505.7141178.08506.126985.14505.5529178.14506.090785.14505.5529178.14506.192885.16505.4796178.16506.139785.18505.3677178.18506.108285.22505.2083178.22506.026185.24505.2083178.24506.026185.24505.2353178.24505.9257	84.82	505.4811	177.82	505.9049
84.88505.2467177.88506.109884.91505.3425177.92506.098184.92505.2590177.92506.098184.94505.2438177.94506.109184.96505.3235177.96506.004884.98505.1670177.98505.842585505.1825178505.932385.02505.1721178.02506.072385.04505.2962178.04506.167585.05505.3237178.06506.080685.08505.4726178.18506.080985.12505.7141178.12506.090785.14505.5529178.14506.192885.15505.4796178.16506.139785.18505.3677178.18506.108285.22505.2083178.22506.026185.24505.2083178.24506.0261	84.84	505.3760	177.84	506.0367
84.9505.3425177.9506.098184.92505.2590177.92506.056984.94505.2438177.94506.109184.96505.3235177.96506.004884.98505.1670177.98505.842585505.1825178505.932385.02505.1721178.02506.072385.04505.2962178.04506.167585.06505.3237178.06506.080685.10505.4726178.1506.080985.12505.7141178.12506.090785.14505.5299178.14506.192885.16505.4796178.16506.139785.18505.3677178.18506.108285.22505.2083178.22506.026185.24505.2083178.24506.026185.24505.2353178.24505.9257	84.86	505.1632	177.86	505.9844
84.92505.2590177.92506.056984.94505.2438177.94506.109184.96505.3235177.96506.004884.98505.1670177.98505.842585505.1825178505.932385.02505.1721178.02506.072385.04505.2962178.04506.167585.05505.4726178.08506.080685.08505.4726178.18506.080985.12505.7141178.12506.090785.14505.5299178.14506.192885.15505.4796178.16506.139785.18505.3677178.18506.108285.22505.2083178.22506.026185.24505.2083178.24506.0261	84.88	505.2467	177.88	506.1098
84.94505.2438177.94506.109184.96505.3235177.96506.004884.98505.1670177.98505.842585505.1825178505.932385.02505.1721178.02506.072385.04505.2962178.04506.167585.06505.3237178.06506.080685.08505.4547178.08506.126985.11505.7141178.12506.090785.12505.7141178.12506.090785.14505.529178.14506.192885.16505.4796178.16506.139785.18505.3677178.18506.108285.22505.2083178.22506.026185.24505.2353178.24505.9257	84.9	505.3425	177.9	506.0981
84.96505.3235177.96506.004884.98505.1670177.98505.842585505.1825178505.932385.02505.1721178.02506.072385.04505.2962178.04506.167585.06505.3237178.06506.080685.08505.4547178.08506.126985.1505.4726178.1506.080985.12505.7141178.12506.090785.14505.529178.14506.192885.15505.3677178.18506.139785.18505.3677178.18506.085285.22505.2083178.22506.026185.24505.2353178.24505.9257	84.92	505.2590	177.92	506.0569
84.98505.1670177.98505.842585505.1825178505.932385.02505.1721178.02506.072385.04505.2962178.04506.167585.06505.3237178.06506.080685.08505.4547178.08506.126985.1505.7141178.12506.090785.14505.529178.14506.192885.15505.4796178.16506.139785.16505.3677178.18506.108285.22505.2083178.22506.026185.24505.2353178.24505.9257	84.94	505.2438	177.94	506.1091
85505.1825178505.932385.02505.1721178.02506.072385.04505.2962178.04506.167585.06505.3237178.06506.080685.08505.4547178.08506.126985.1505.4726178.1506.080985.12505.7141178.12506.090785.14505.5529178.14506.192885.15505.4796178.16506.139785.18505.3677178.18506.085285.22505.2083178.22506.026185.24505.2353178.24505.9257	84.96	505.3235	177.96	506.0048
85.02505.1721178.02506.072385.04505.2962178.04506.167585.06505.3237178.06506.080685.08505.4547178.08506.126985.1505.4726178.1506.080985.12505.7141178.12506.090785.14505.529178.14506.192885.16505.4796178.16506.139785.18505.3677178.18506.085285.22505.2083178.22506.026185.24505.2353178.24505.9257	84.98	505.1670	177.98	505.8425
85.04505.2962178.04506.167585.06505.3237178.06506.080685.08505.4547178.08506.126985.1505.4726178.1506.080985.12505.7141178.12506.090785.14505.5529178.14506.192885.16505.4796178.16506.139785.18505.3677178.18506.085285.22505.2083178.22506.026185.24505.2353178.24505.9257	85	505.1825	178	505.9323
85.06505.3237178.06506.080685.08505.4547178.08506.126985.1505.4726178.1506.080985.12505.7141178.12506.090785.14505.5529178.14506.192885.16505.4796178.16506.139785.18505.3677178.18506.085285.22505.2083178.22506.026185.24505.2353178.24505.9257	85.02	505.1721	178.02	506.0723
85.08505.4547178.08506.126985.1505.4726178.1506.080985.12505.7141178.12506.090785.14505.5529178.14506.192885.16505.4796178.16506.139785.18505.3677178.18506.085285.2505.2083178.22506.026185.24505.2353178.24505.9257	85.04	505.2962	178.04	506.1675
85.1505.4726178.1506.080985.12505.7141178.12506.090785.14505.5529178.14506.192885.16505.4796178.16506.139785.18505.3677178.18506.085285.2505.3866178.2506.085285.24505.2353178.24505.9257	85.06	505.3237	178.06	506.0806
85.12505.7141178.12506.090785.14505.5529178.14506.192885.16505.4796178.16506.139785.18505.3677178.18506.108285.2505.3866178.2506.085285.22505.2083178.22506.026185.24505.2353178.24505.9257	85.08	505.4547	178.08	506.1269
85.14505.5529178.14506.192885.16505.4796178.16506.139785.18505.3677178.18506.108285.2505.3866178.2506.085285.22505.2083178.22506.026185.24505.2353178.24505.9257	85.1	505.4726	178.1	506.0809
85.16505.4796178.16506.139785.18505.3677178.18506.108285.2505.3866178.2506.085285.22505.2083178.22506.026185.24505.2353178.24505.9257	85.12	505.7141	178.12	506.0907
85.18505.3677178.18506.108285.2505.3866178.2506.085285.22505.2083178.22506.026185.24505.2353178.24505.9257	85.14	505.5529		506.1928
85.2505.3866178.2506.085285.22505.2083178.22506.026185.24505.2353178.24505.9257	85.16	505.4796	178.16	506.1397
85.22505.2083178.22506.026185.24505.2353178.24505.9257	85.18	505.3677	178.18	506.1082
85.24 505.2353 178.24 505.9257	85.2	505.3866	178.2	506.0852
	85.22	505.2083	178.22	506.0261
	85.24	505.2353	178.24	505.9257
85.26 505.3211 178.26 505.9336	85.26	505.3211	178.26	505.9336

85.28	505.4141	178.28	505.9516
85.3	505.3633	178.3	506.2919
85.32	505.4287	178.32	506.2376
85.34	505.5702	178.34	506.2557
85.36	505.7534	178.36	506.2427
85.38	505.5661	178.38	506.3063
85.4	505.4255	178.4	506.1519
85.42	505.4752	178.42	506.0983
85.44	505.4387	178.44	506.1402
85.46	505.4390	178.46	506.1040
85.48	505.5765	178.48	505.8192
85.5	505.3091	178.5	506.0310
85.52	505.1033	178.52	506.0646
85.54	505.1355	178.54	506.0387
85.56	505.1864	178.56	505.9824
85.58	505.1334	178.58	505.9618
85.6	505.3142	178.6	505.8924
85.62	505.2514	178.62	505.9431
85.64	505.2977	178.64	505.9174
85.66	505.2601	178.66	505.8585
85.68	505.3296	178.68	505.8610
85.7	505.3454	178.7	505.8046
85.72	505.2129	178.72	505.6899
85.74	505.0318	178.74	505.8088
85.76	505.0149	178.76	505.7209
85.78	505.1422	178.78	505.5909
85.8	504.9819	178.8	505.6676
85.82	505.1378	178.82	505.5691
85.84	505.1934	178.84	505.4219
85.86	505.2023	178.86	505.3214
85.88	505.2223	178.88	505.2367
85.9	505.2175	178.9	505.1169
85.92	505.3226	178.92	505.0646
85.94	505.2904	178.94	505.0396
85.96	505.1988	178.96	504.9403
85.98	505.2524	178.98	504.9270
86	505.2573	179	504.9853
86.02	505.1837	179.02	504.9593
86.04	505.1180	179.04	505.0309
86.06	505.1179	179.06	505.1288
86.08	505.0388	179.08	505.1075
86.1	505.1786	179.1	505.0607
86.12	505.0711	179.12	505.1402

86.14	505.0888	179.14	505.0644
86.16	504.9519	179.16	505.0269
86.18	505.0373	179.18	505.0756
86.2	505.1116	179.2	505.0030
86.22	505.2252	179.22	504.7715
86.24	505.3534	179.24	504.7085
86.26	505.2538	179.26	504.4897
86.28	505.1315	179.28	504.5373
86.3	505.1434	179.3	504.6154
86.32	505.2915	179.32	504.6095
86.34	505.4223	179.34	504.6905
86.36	505.4460	179.36	504.6415
86.38	505.4731	179.38	504.5122
86.4	505.5273	179.4	504.4366
86.42	505.5952	179.42	504.3981
86.44	505.6208	179.44	504.3362
86.46	505.6521	179.46	504.3815
86.48	505.6702	179.48	504.3371
86.5	505.6903	179.5	504.4404
86.52	505.7518	179.52	504.5753
86.54	505.7203	179.54	504.5708
86.56	505.8988	179.56	504.6102
86.58	505.8260	179.58	504.5189
86.6	505.7026	179.6	504.4794
86.62	505.6694	179.62	504.4331
86.64	505.6948	179.64	504.6190
86.66	505.6958	179.66	504.6067
86.68	505.7463	179.68	504.6373
86.7	505.8070	179.7	504.4872
86.72	505.8520	179.72	504.4036
86.74	505.8384	179.74	504.3321
86.76	505.9706	179.76	504.2932
86.78	505.8468	179.78	504.3221
86.8	505.7535	179.8	504.2755
86.82	505.7289	179.82	504.2269
86.84	505.7184	179.84	504.3410
86.86	505.5687	179.86	504.4478
86.88	505.6860	179.88	504.3708
86.9	505.6040	179.9	504.3650
86.92	505.5486	179.92	504.4801
86.94	505.6060	179.94	504.4699
86.96	505.4428	179.96	504.4543
86.98	505.4767	179.98	504.5984

87	505.5858	180	504.6487
87.02	505.5255	180.02	504.5886
87.04	505.5614	180.04	504.7249
87.06	505.5087	180.06	504.8053
87.08	505.6061	180.08	504.9738
87.1	505.5793	180.1	505.0309
87.12	505.6976	180.12	504.9899
87.14	505.6098	180.14	505.0868
87.16	505.7692	180.16	505.0346
87.18	505.7677	180.18	504.8929
87.2	505.8080	180.2	504.8945
87.22	505.8572	180.22	505.0582
87.24	505.7922	180.24	505.0069
87.26	505.7893	180.26	505.1369
87.28	505.7385	180.28	505.1472
87.3	505.6260	180.3	505.2388
87.32	505.5303	180.32	505.1489
87.34	505.6183	180.34	505.1082
87.36	505.6634	180.36	505.0947
87.38	505.6104	180.38	505.1766
87.4	505.6315	180.4	505.1595
87.42	505.5954	180.42	505.3561
87.44	505.6839	180.44	505.4894
87.46	505.5544	180.46	505.4524
87.48	505.5105	180.48	505.4139
87.5	505.3965	180.5	505.4646
87.52	505.4811	180.52	505.5780
87.54	505.5175	180.54	505.5748
87.56	505.3433	180.56	505.7221
87.58	505.2698	180.58	505.6430
87.6	505.2847	180.6	505.5116
87.62	505.2704	180.62	505.6217
87.64	505.3397	180.64	505.6632
87.66	505.3231	180.66	505.7310
87.68	505.4064	180.68	505.9004
87.7	505.3552	180.7	505.7956
87.72	505.2661	180.72	505.9903
87.74	505.3271	180.74	505.9559
87.76	505.3801	180.76	506.0650
87.78	505.2947	180.78	505.9798
87.8	505.2103	180.8	506.0988
87.82	505.2013	180.82	506.2224
87.84	505.1194	180.84	506.2711

87.86	505.0223	180.86	506.3467
87.88	505.0342	180.88	506.4268
87.9	505.0739	180.9	506.2978
87.92	505.1113	180.92	506.1431
87.94	505.0441	180.94	506.2307
87.96	504.9707	180.96	506.1201
87.98	504.9455	180.98	506.1914
88	505.0406	181	506.1172
88.02	505.0913	181.02	505.9760
88.04	505.1206	181.04	505.9420
88.06	505.1648	181.06	506.1215
88.08	505.0924	181.08	506.3252
88.1	505.0708	181.1	506.1981
88.12	505.1643	181.12	506.1607
88.14	505.1018	181.14	506.1852
88.16	505.1901	181.16	506.0975
88.18	505.1427	181.18	506.0205
88.2	505.1581	181.2	505.9384
88.22	505.0813	181.22	505.9960
88.24	505.1297	181.24	506.0129
88.26	505.2291	181.26	506.1286
88.28	505.1781	181.28	506.0148
88.3	505.2096	181.3	505.8329
88.32	505.2141	181.32	505.8162
88.34	505.2188	181.34	505.8445
88.36	505.2985	181.36	505.7768
88.38	505.3315	181.38	505.9215
88.4	505.2536	181.4	505.9162
88.42	505.2438	181.42	506.0260
88.44	505.3189	181.44	505.9307
88.46	505.4141	181.46	505.7676
88.48	505.3971	181.48	505.7912
88.5	505.6275	181.5	505.7975
88.52	505.4977	181.52	505.8465
88.54	505.5096	181.54	505.7921
88.56	505.5646	181.56	505.6962
88.58	505.6749	181.58	505.4908
88.6	505.6828	181.6	505.4508
88.62	505.6911	181.62	505.4387
88.64	505.6612	181.64	505.3122
88.66	505.5979	181.66	505.4329
88.68	505.6754	181.68	505.4171
88.7	505.5211	181.7	505.3835

88.72	505.5980	181.72	505.2943
88.74	505.7850	181.74	505.1895
88.76	505.6522	181.76	505.0835
88.78	505.7059	181.78	505.0769
88.8	505.7332	181.8	504.9840
88.82	505.6928	181.82	504.9376
88.84	505.7554	181.84	504.9571
88.86	505.8923	181.86	505.0805
88.88	505.8759	181.88	505.1917
88.9	505.9229	181.9	504.9875
88.92	505.9248	181.92	505.0719
88.94	506.0492	181.94	504.9772
88.96	506.0705	181.96	504.8713
88.98	506.1597	181.98	504.7947
89	506.2739	182	504.7829
89.02	506.3318	182.02	504.7925
89.04	506.1872	182.04	504.7074
89.06	506.1189	182.06	504.7391
89.08	506.2268	182.08	504.8920
89.1	506.2044	182.1	504.9000
89.12	506.2512	182.12	504.8102
89.14	506.1561	182.14	504.8141
89.16	506.1202	182.16	504.6619
89.18	506.1756	182.18	504.6401
89.2	506.1511	182.2	504.8155
89.22	505.9796	182.22	504.7932
89.24	505.9428	182.24	504.7479
89.26	506.0132	182.26	504.6093
89.28	505.9270	182.28	504.5416
89.3	506.0224	182.3	504.5307
89.32	506.0367	182.32	504.4821
89.34	506.1279	182.34	504.5736
89.36	506.0834	182.36	504.5961
89.38	506.1668	182.38	504.7280
89.4	506.2000	182.4	504.7264
89.42	506.1655	182.42	504.5804
89.44	505.9869	182.44	504.6060
89.46	506.0507	182.46	504.6817
89.48	506.0195	182.48	504.7624
89.5	506.0529	182.5	504.8449
89.52	506.1307	182.52	504.7881
89.54	506.0071	182.54	504.8854
89.56	506.0607	182.56	504.9473

89.58	505.9491	182.58	504.7956
89.6	506.0100	182.6	504.9253
89.62	505.9929	182.62	505.0227
89.64	505.8919	182.64	505.2636
89.66	505.7343	182.66	505.3455
89.68	505.7171	182.68	505.2803
89.7	505.7355	182.7	505.2871
89.72	505.8016	182.72	505.1307
89.74	505.9028	182.74	505.1207
89.76	505.8791	182.76	505.0429
89.78	505.7736	182.78	504.9710
89.8	505.7095	182.8	504.9844
89.82	505.6738	182.82	504.9913
89.84	505.6682	182.84	504.9763
89.86	505.6197	182.86	505.0663
89.88	505.6242	182.88	504.9706
89.9	505.5413	182.9	505.0246
89.92	505.5571	182.92	504.9440
89.94	505.4406	182.94	505.2510
89.96	505.4802	182.96	505.4070
89.98	505.7146	182.98	505.4034
90	505.6850	183	505.4679
90.02	505.5592	183.02	505.4262
90.04	505.5687	183.04	505.5839
90.06	505.4911	183.06	505.6005
90.08	505.4118	183.08	505.7155
90.1	505.4732	183.1	505.6108
90.12	505.5189	183.12	505.6096
90.14	505.6170	183.14	505.7344
90.16	505.8246	183.16	505.7436
90.18	505.8716	183.18	505.8831
90.2	505.7961	183.2	505.9765
90.22	505.7201	183.22	506.0271
90.24	505.6919	183.24	506.0272
90.26	505.8151	183.26	506.0985
90.28	505.8216	183.28	506.1161
90.3	505.7906	183.3	506.1458
90.32	505.7941	183.32	506.2164
90.34	505.6603	183.34	506.1943
90.36	505.5865	183.36	506.2448
90.38	505.4176	183.38	506.0839
90.4	505.5175	183.4	506.0062
90.42	505.5917	183.42	505.9362

90.44	505.5486	183.44	505.8508
90.46	505.4080	183.46	505.8514
90.48	505.3962	183.48	505.8196
90.5	505.3657	183.5	505.8731
90.52	505.4949	183.52	505.7876
90.54	505.4973	183.54	505.7015
90.56	505.3828	183.56	505.7641
90.58	505.6078	183.58	505.7033
90.6	505.4799	183.6	505.7161
90.62	505.3811	183.62	505.8249
90.64	505.3202	183.64	505.7963
90.66	505.3373	183.66	505.8447
90.68	505.2800	183.68	505.8228
90.7	505.4103	183.7	505.8528
90.72	505.3725	183.72	505.7855
90.74	505.3229	183.74	505.7563
90.76	505.3584	183.76	505.7106
90.78	505.4834	183.78	505.6208
90.8	505.4687	183.8	505.7148
90.82	505.4218	183.82	505.7042
90.84	505.3374	183.84	505.7771
90.86	505.4378	183.86	505.7084
90.88	505.4711	183.88	505.7048
90.9	505.5439	183.9	505.8013
90.92	505.6342	183.92	505.8196
90.94	505.4965	183.94	505.7637
90.96	505.4440	183.96	505.7677
90.98	505.5621	183.98	505.7828
91	505.7184	184	505.6948
91.02	505.6723	184.02	505.7237
91.04	505.6290	184.04	505.6311
91.06	505.5749	184.06	505.6680
91.08	505.6687	184.08	505.6029
91.1	505.6928	184.1	505.5971
91.12	505.6249	184.12	505.5901
91.14	505.6952	184.14	505.5502
91.16	505.6054	184.16	505.6139
91.18	505.6431	184.18	505.6237
91.2	505.6031	184.2	505.6151
91.22	505.6379	184.22	505.6942
91.24	505.5584	184.24	505.7404
91.26	505.4337	184.26	505.8236
91.28	505.5558	184.28	505.7165

91.3	505.6035	184.3	505.7857
91.32	505.6542	184.32	505.7530
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91.38	505.3377	184.38	505.4807
91.4	505.2919	184.4	505.4843
91.42	505.3229	184.42	505.6173
91.44	505.3485	184.44	505.6312
91.46	505.4958	184.46	505.8109
91.48	505.3276	184.48	505.7310
91.5	505.3572	184.5	505.6393
91.52	505.4020	184.52	505.5864
91.54	505.2298	184.54	505.5407
91.56	505.3239	184.56	505.5401
91.58	505.3453	184.58	505.3859
91.6	505.5034	184.6	505.3241
91.62	505.4898	184.62	505.2589
91.64	505.4916	184.64	505.3285
91.66	505.3936	184.66	505.2900
91.68	505.3418	184.68	505.2762
91.7	505.3567	184.7	505.3402
91.72	505.2026	184.72	505.3580
91.74	505.1424	184.74	505.3478
91.76	505.0705	184.76	505.3671
91.78	505.2602	184.78	505.2766
91.8	505.1685	184.8	505.2940
91.82	505.1771	184.82	505.2357
91.84	505.1271	184.84	505.3491
91.86	505.0512	184.86	505.2524
91.88	505.1502	184.88	505.2303
91.9	505.2694	184.9	505.2172
91.92	505.2887	184.92	505.1949
91.94	505.3043	184.94	505.1549
91.96	505.4704	184.96	505.0862
91.98	505.3651	184.98	505.0732
92	505.3380	185	505.0332
92.02	505.3299	185.02	505.1308
92.04	505.4250	185.04	505.1800
92.06	505.2883	185.06	505.2572
92.08	505.2382	185.08	505.1465
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92.12	505.4147	185.12	505.1442
92.14	505.4456	185.14	505.2300

92.16	505.4486	185.16	505.0798
92.18	505.4809	185.18	505.0994
92.2	505.3937	185.2	505.0297
92.22	505.4590	185.22	504.9878
92.24	505.2326	185.24	505.0215
92.26	505.1851	185.26	505.0020
92.28	505.1951	185.28	504.9228
92.3	505.2810	185.3	504.9626
92.32	505.2964	185.32	505.0032
92.34	505.2918	185.34	504.9177
92.36	505.0994	185.36	504.8932
92.38	505.0587	185.38	505.0071
92.4	504.9983	185.4	504.9594
92.42	504.9230	185.42	504.8533
92.44	504.9290	185.44	504.9170
92.46	504.9588	185.46	504.8330
92.48	505.0161	185.48	504.9642
92.5	505.0378	185.5	505.0565
92.52	505.0422	185.52	505.2729
92.54	505.0380	185.54	505.3632
92.56	505.2340	185.56	505.3619
92.58	505.1501	185.58	505.4438
92.6	505.0900	185.6	505.5956
92.62	505.0103	185.62	505.6570
92.64	505.0625	185.64	505.6489
92.66	505.1682	185.66	505.5863
92.68	505.0777	185.68	505.5884
92.7	505.1767	185.7	505.5889
92.72	505.2153	185.72	505.7372
92.74	505.4119	185.74	505.7138
92.76	505.4513	185.76	505.7629
92.78	505.5465	185.78	505.6325
92.8	505.6269	185.8	505.6690
92.82	505.6045	185.82	505.6712
92.84	505.5005	185.84	505.7942
92.86	505.3918	185.86	505.7257
92.88	505.5202	185.88	505.7541
92.9	505.4105	185.9	505.7634
92.92	505.3731	185.92	505.8832
92.94	505.3299	185.94	505.9021
92.96	505.2627	185.96	506.0140
92.98	505.2408	185.98	505.8557
93	505.1428	186	505.9977

93.02	505.2208	186.02	506.0382
93.04	505.2506	186.04	506.0021
93.06	505.2971	186.06	506.1257
93.08	505.2631	186.08	506.0152
93.1	505.3054	186.1	505.9965
93.12	505.3298	186.12	506.0857
93.14	505.4218	186.14	505.9959
93.16	505.4615	186.16	505.9792
93.18	505.3410	186.18	506.1324
93.2	505.4123	186.2	506.1275
93.22	505.3038	186.22	506.1467
93.24	505.3427	186.24	506.1772
93.26	505.3452	186.26	506.1117
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93.34	505.4683	186.34	506.0622
93.36	505.3732	186.36	506.1246
93.38	505.4586	186.38	506.0050
93.4	505.4028	186.4	506.0595
93.42	505.4664	186.42	506.1007
93.44	505.3883	186.44	506.2129
93.46	505.4185	186.46	506.3976
93.48	505.4085	186.48	506.4007
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93.52	505.3895	186.52	506.3214
93.54	505.4574	186.54	506.3374
93.56	505.4909	186.56	506.2842
93.58	505.4543	186.58	506.2536
93.6	505.4147	186.6	506.2094
93.62	505.3122	186.62	506.1171
93.64	505.3985	186.64	506.1819
93.66	505.3816	186.66	506.0574
93.68	505.5048	186.68	505.9872
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93.72	505.4428	186.72	505.9099
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93.78	505.3212	186.78	505.8902
93.8	505.4347	186.8	505.8718
93.82	505.4787	186.82	505.8193
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93.94	505.5591	186.94	505.2702
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94.04	505.7922		
94.06	505.5673		
94.08	505.4481		
94.1	505.4997		
94.12	505.5263		
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94.66	505.2069		
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<u> Appendix F- Weld AT 7 data</u>

<u> Appendix F- Weld AT 7 data</u>

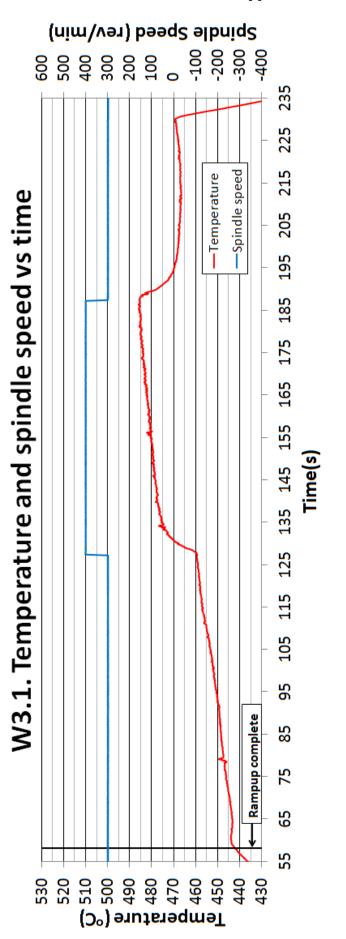
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100	505.5222	

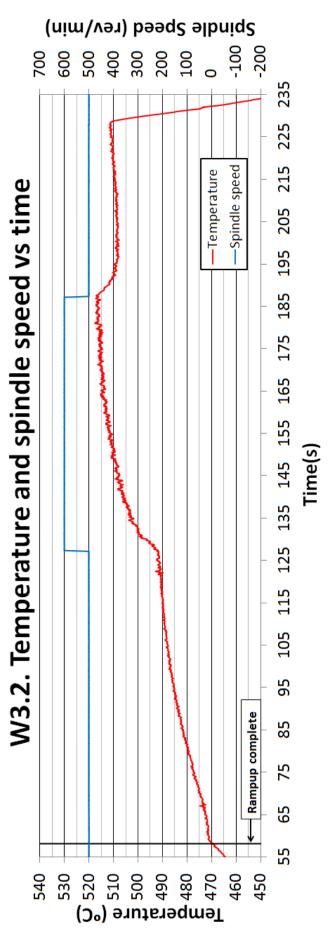
Weld AT_7 control data									
time	Error	Proportional	Integral	Derivative					
145	-0.209297829	-7.974247282	-77.51202686	-744.7299345					
145.02	-0.195362155	-7.443298098	-77.61429075	43.96846569					
145.04	0.054693154	2.083809173	-77.64164141	22.82852918					
145.06	0.084432622	3.216882896	-77.62047917	27.74369669					
145.08	0.03042704	1.159270224	-77.60618563	29.46189609					
145.1	0.055476033	2.11363687	-77.60854255	-651.005971					
145.12	-0.005938994	-0.226275684	-77.60114914	165.1760844					
145.14	-0.117756535	-4.48652399	-77.64014694	290.1891286					
145.16	-0.235592413	-8.976070924	-77.71049024	536.2552022					
145.18	-0.495768065	-18.88876326	-77.90437087	-390.0417655					
145.2	-0.440249792	-16.77351709	-78.11738189	718.0757328					
145.22	-0.235462059	-8.971104435	-78.26161222	-383.5979499					
145.24	-0.136298411	-5.192969446	-78.36122699	-570.9418116					
145.26	-0.050518967	-1.924772639	-78.41474566	-62.57417464					
145.28	-0.027406962	-1.04420524	-78.40451387	160.3911832					
145.3	-0.014260929	-0.543341395	-78.42947947	-508.3646151					
145.32	-0.081256285	-3.095864444	-78.4646832	29.46391926					
145.34	-0.10159715	-3.870851417	-78.53325747	-317.0417726					
145.36	-0.215097308	-8.195207447	-78.61696692	574.7840468					
145.38	-0.229833482	-8.756655651	-78.72330866	-196.0744483					
145.4	-0.385109003	-14.67265302	-78.87298006	57.36724361					
145.42	-0.32137258	-12.24429529	-79.03499978	448.1142828					
145.44	-0.33283831	-12.68113961	-79.18943429	-152.5486202					
145.46	-0.229425807	-8.741123257	-79.3365239	-116.7859997					
145.48	-0.309942189	-11.80879741	-79.47107941	9.259494926					
145.5	-0.179979717	-6.8572272	-79.60350093	-277.333119					
145.52	-0.205311887	-7.822382876	-79.68855924	277.4157128					
145.54	-0.181954959	-6.93248394	-79.78330322	-13.02595106					
145.56	-0.278495229	-10.61066823	-79.89012999	-32.88907374					
145.58	-0.308459928	-11.75232327	-80.02561289	-44.96454301					
145.6	-0.243525324	-9.278314849	-80.14664813	-291.8143417					
145.62	-0.180513394	-6.877560306	-80.25391156	-700.6799952					
145.64	-0.132409688	-5.044809117	-80.32779747	623.0813203					
145.66	-0.011832391	-0.4508141	-80.3860564	-252.9306891					
145.68	-0.026624136	-1.014379568	-80.40611959	-163.0332609					
145.7	0.041588478	1.584521009	-80.38447481	-151.2300936					
145.72	0.042645179	1.624781314	-80.37271855	-338.0954863					
145.74	0.044462575	1.694024122	-80.35983204	-172.3468942					
145.76	0.056411091	2.149262581	-80.34109604	-397.9681861					
145.78	0.079758661	3.038804979	-80.31049	-46.51107528					

			<u>аррениі</u>	<u>IX G- Weld AT</u> / (
145.8	0.125282985	4.773281715	-80.25760203	-251.1008652
145.82	0.087490181	3.333375906	-80.19360801	709.0521933
145.84	0.211638557	8.063429037	-80.11790728	102.7578924
145.86	0.278415159	10.60761755	-80.01330618	-84.65330304
145.88	0.157752293	6.010362358	-79.89642755	51.96576369
145.9	0.077651097	2.958506805	-79.85990782	50.0215473
145.92	0.146532306	5.58288086	-79.83204896	-694.6924523
145.94	0.16781523	6.393760267	-79.76859868	-577.9243481
145.96	0.090027925	3.430063947	-79.70929461	-688.3669374
145.98	0.053395075	2.034352345	-79.70083822	-164.4405882
146	0.085096043	3.242159252	-79.67285395	930.4936173
146.02	-0.083921137	-3.197395337	-79.66851174	851.4191484
146.04	-0.081126904	-3.090935051	-79.70610822	-72.43874341
146.06	0.033533401	1.277622591	-79.71540053	6.362761026
146.08	-0.106790471	-4.068716943	-79.73453012	-53.96888621
146.1	-0.122919277	-4.683224447	-79.77140217	780.2984872
146.12	-0.175363583	-6.681352528	-79.81626753	953.3307014
146.14	-0.18465081	-7.035195861	-79.88749036	932.254277
146.16	-0.041380661	-1.576603186	-79.95510123	-13.85497117
146.18	-0.123006792	-4.686558783	-79.97169492	-73.96912145
146.2	-0.317744797	-12.10607678	-80.06160224	971.5294168
146.22	-0.197648366	-7.530402735	-80.18029854	-98.77041059
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146.26	-0.279814907	-10.66094796	-80.41889257	-37.80840832
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146.3	-0.024452636	-0.931645434	-80.57151988	-288.8447719
146.32	-0.006014549	-0.229154322	-80.59579719	-340.1730711
146.34	-0.196603791	-7.49060442	-80.64484918	-18.41519738
146.36	-0.222208759	-8.466153728	-80.72975227	716.6195388
146.38	-0.052388841	-1.996014833	-80.80094624	-93.86518018
146.4	-0.005210137	-0.198506207	-80.81303344	-67.02707286
146.42	-0.001956056	-0.074525735	-80.822266	-456.6882256
146.44	-0.068306063	-2.602460998	-80.85533799	193.9778442
146.46	0.000112291	0.004278279	-80.9052371	2.510288682
146.48	-0.038073425	-1.450597478	-80.89190983	223.532149
146.5	-6.64194E-05	-0.00253058	-80.88436167	-34.84854512
146.52	-0.028849442	-1.09916375	-80.89291681	45.46738497
146.54	-0.006659331	-0.253720523	-80.92212944	-538.2369686
146.56	0.107727452	4.104415921	-80.90327896	15.50531859
146.58	0.027591095	1.051220712	-80.88322466	105.7098623
146.6	-0.010444388	-0.397931183	-80.87341452	343.7370856
146.62	-0.031466789	-1.198884676	-80.87540918	-77.57198094
146.64	0.048405482	1.844248866	-80.86903334	-266.2065381

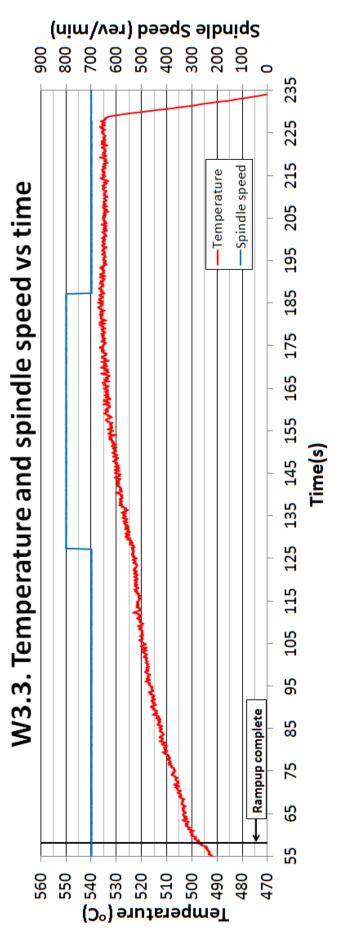
146.68 146.7 146.72	-0.048279059 -0.102875276 -0.008133495 -0.074856123	-1.839432161 -3.919548008	-80.87623164 -80.90362215	-62.33895573 -62.36934023
146.7 146.72	-0.008133495		-80.90362215	-62.36934023
146.72		0 200006163		
	0 07/056122	-0.309886162	-80.91203772	27.86690911
146 74	-0.074830123	-2.852018273	-80.95080347	31.31466998
140.74	-0.221733746	-8.448055713	-81.02484093	-82.65500364
146.76	0.042928512	1.635576321	-81.03740587	-19.15315961
146.78	-0.020436054	-0.778613664	-81.01958442	445.3526726
146.8	-0.149175992	-5.683605308	-81.06329562	-20.13018478
146.82	-0.095712985	-3.646664735	-81.10428522	-5.381264236
146.84	-0.245871768	-9.367714364	-81.19493721	1013.541252
146.86	-0.286156089	-10.90254698	-81.32560512	153.445003
146.88	-0.373066247	-14.21382402	-81.48259195	-22.15432962
146.9	-0.547382421	-20.85527023	-81.67384934	461.9675745
146.92	-0.592436888	-22.57184543	-81.9380889	11.12170539
146.94	-0.535569076	-20.40518181	-82.2102473	-38.61685792
146.96	-0.51590496	-19.65597899	-82.45204903	70.79728222
146.98	-0.421820658	-16.07136707	-82.65822549	-256.346258
147	-0.415711178	-15.83859587	-82.86618455	-296.9715257
147.02	-0.405905014	-15.46498102	-83.08284238	103.3340606
147.04	-0.558975569	-21.29696917	-83.29902789	47.04920697
147.06	-0.492180238	-18.75206706	-83.52957117	-3.973665453
147.08	-0.257440028	-9.80846507	-83.71410754	-397.5099123
147.1	-0.343606433	-13.0914051	-83.85507958	-92.5559533
147.12	-0.342388523	-13.04500274	-84.01989193	-311.7865398
147.14	-0.25429273	-9.688553024	-84.16379229	-53.96979774
147.16	-0.094425517	-3.597612208	-84.23273815	-247.7834127
147.18	-0.143844324	-5.48046875	-84.30565147	-456.4522174
147.2	-0.195325523	-7.441902441	-84.36908796	-65.09010316
147.22	-0.238135823	-9.072974859	-84.48042736	-366.9052835
147.24	-0.373787199	-14.24129228	-84.65729523	-329.6913554
147.26	-0.352326227	-13.42362926	-84.84832689	-26.9281884
147.28	-0.178042489	-6.78341882	-84.97188193	-481.3459295
147.3	-0.227525974	-8.66873962	-85.05048358	-78.50395909
147.32	-0.256322585	-9.765890477	-85.17484389	-340.918057
147.34	-0.290665911	-11.0743712	-85.28907232	-5.660234989
147.36	-0.38715614	-14.75064894	-85.46951015	-56.16407177
147.38	-0.313890861	-11.95924181	-85.64251482	-24.02897315
147.4	-0.401752994	-15.30678907	-85.82670753	84.92968029
147.42	-0.327072912	-12.46147794	-85.99939109	-94.98502987
147.44	-0.390559955	-14.88033429	-86.15601056	380.5123736
147.46	-0.467593276	-17.81530381	-86.37201213	-68.37059107
147.48	-0.526456089	-20.057977	-86.61422312	122.2487982
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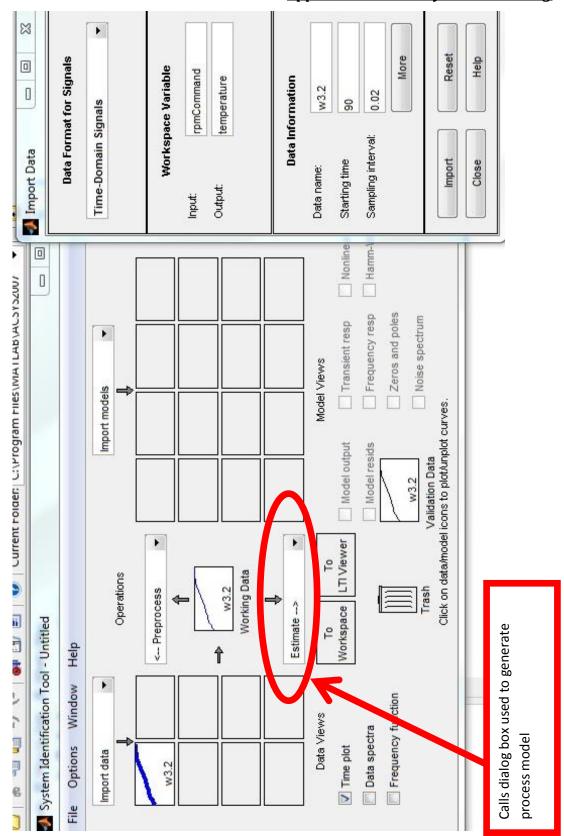
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147.56	-0.089182534	-3.397854564	-87.08392843	66.08131344
147.58	-0.046879259	-1.78609977	-87.12421003	133.7372245
147.6	0.023570511	0.898036463	-87.12316096	55.2143542
147.62	0.076023586	2.896498618	-87.11650996	-189.9243968
147.64	-0.001326548	-0.05054147	-87.08062331	56.81694946
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147.68	0.106074255	4.041429112	-86.99775141	60.59130539
147.7	-0.041510045	-1.581532712	-87.00149975	-377.709243
147.72	-0.052077727	-1.984161401	-87.0446439	-393.0882965
147.74	0.069671396	2.654480189	-87.03898093	-236.2319811
147.76	0.18761249	7.14803585	-86.98128328	-44.46918117
147.78	0.14932102	5.689130857	-86.89883759	1.462570454
147.8	-0.013334089	-0.508028808	-86.88659078	-385.1280575
147.82	0.064885938	2.472154251	-86.88192416	47.92932817
147.84	-0.041118347	-1.566609007	-86.90053156	-8.130873702
147.86	-0.110524578	-4.210986416	-86.94490685	-119.8742138
147.88	-0.054346086	-2.070585863	-86.96113686	103.650414
147.9	-0.004962396	-0.189067272	-86.95505057	353.7512809
147.92	-0.104351824	-3.975804485	-86.97754254	-21.59111553
147.94	0.115624944	4.405310381	-86.98570578	-225.7089597
147.96	0.188229772	7.171554295	-86.90577025	8.111875297
147.98	0.08660872	3.29979223	-86.83491628	-19.69596134
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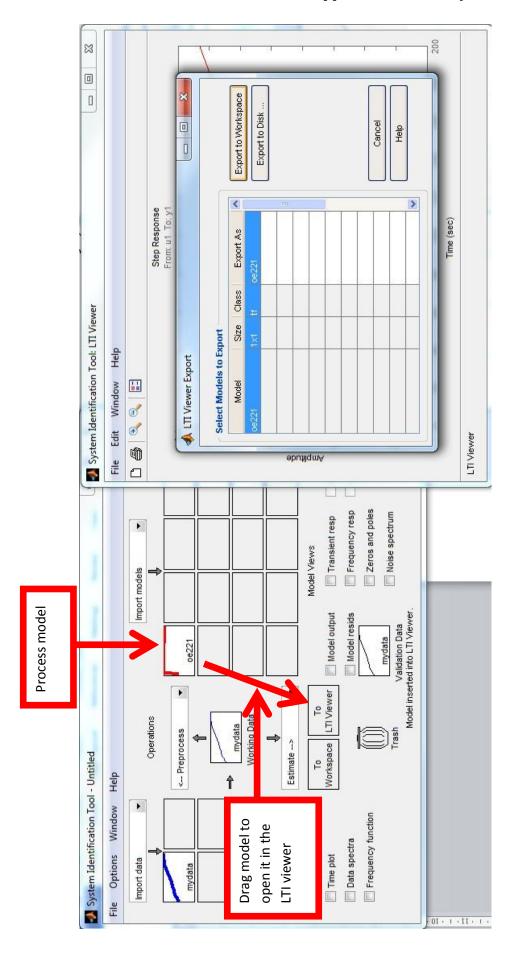


H-2

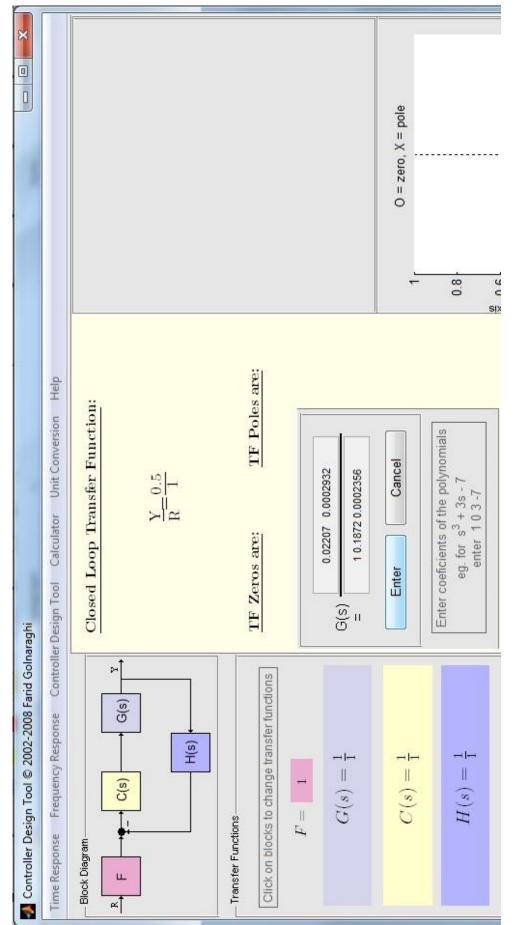




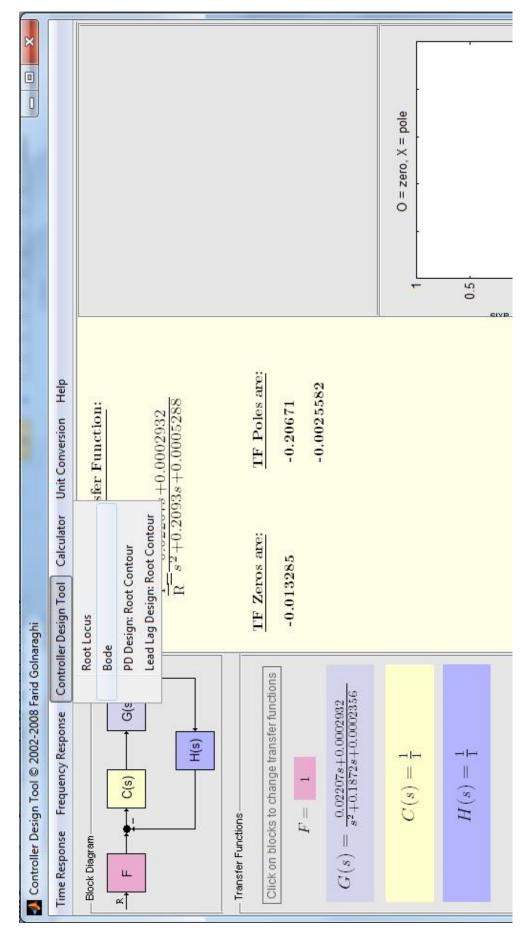
Appendix I- Matlab System Modelling

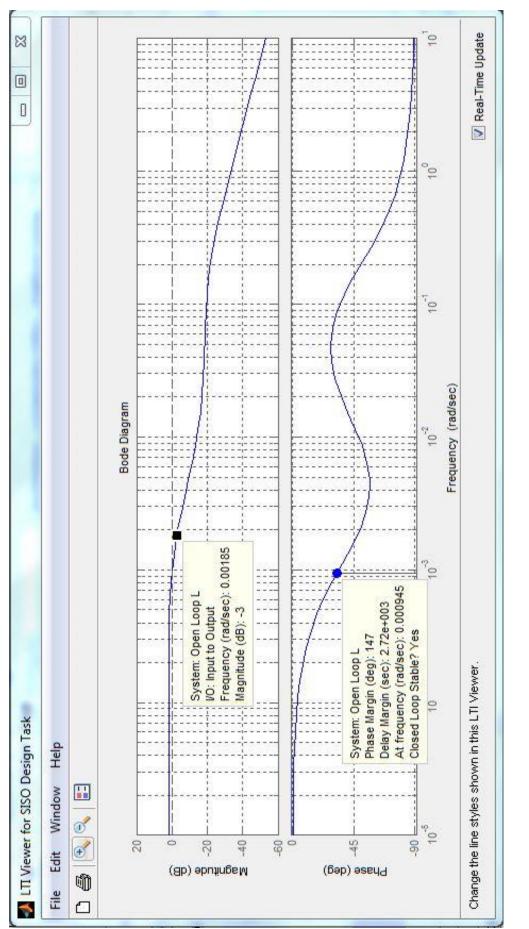


Appendix I- Matlab System Modelling



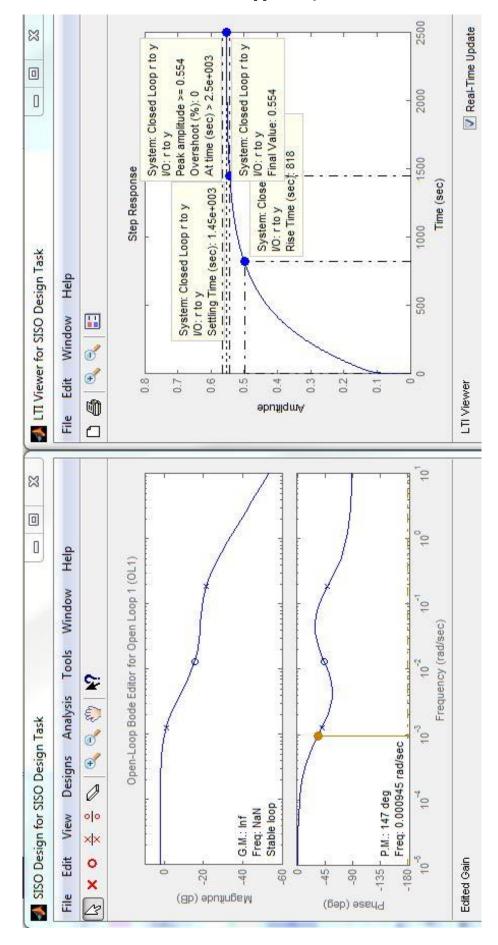
Appendix J- Matlab ACSYS PID bode design

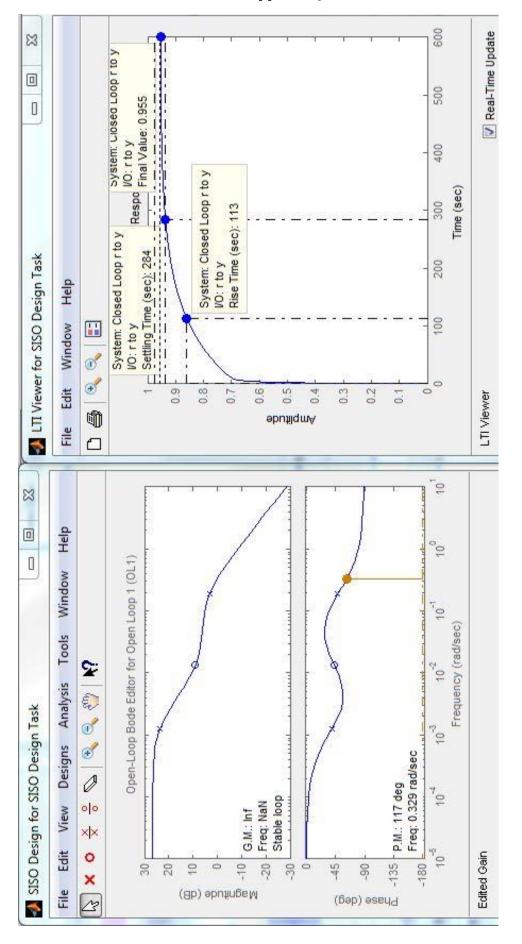


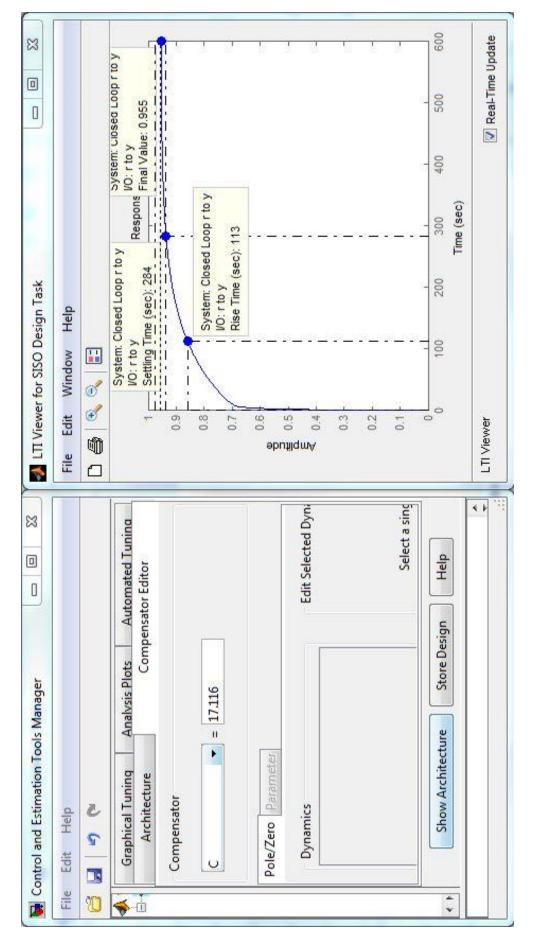


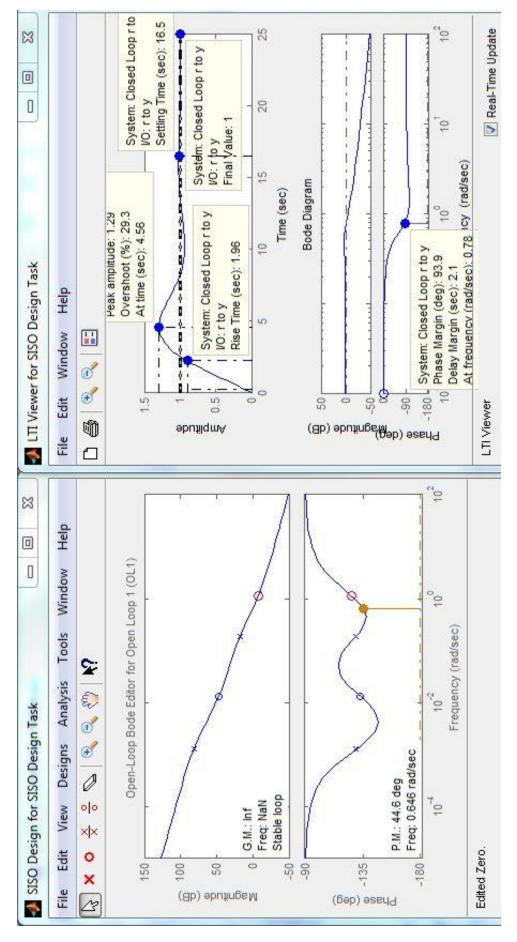
Appendix J- Matlab ACSYS PID bode design

<u> Appendix J- Matlab ACSYS PID bode design</u>



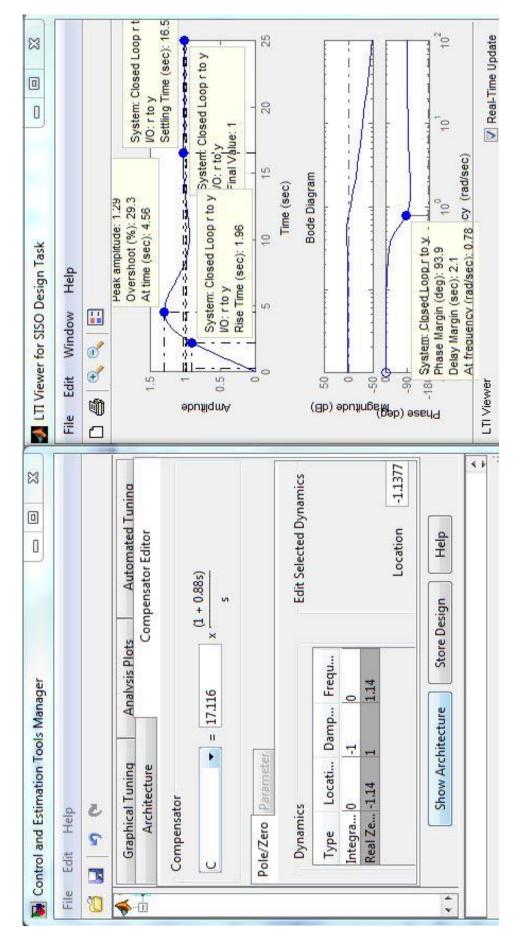


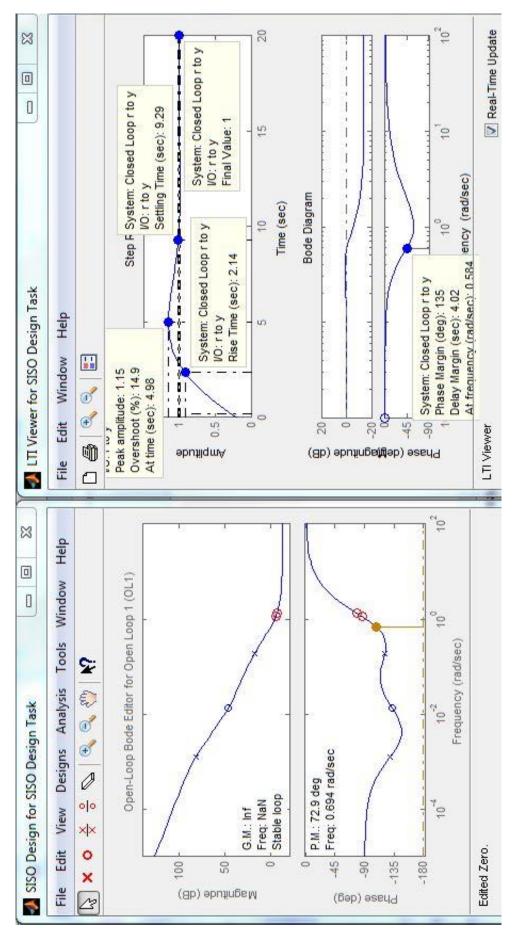




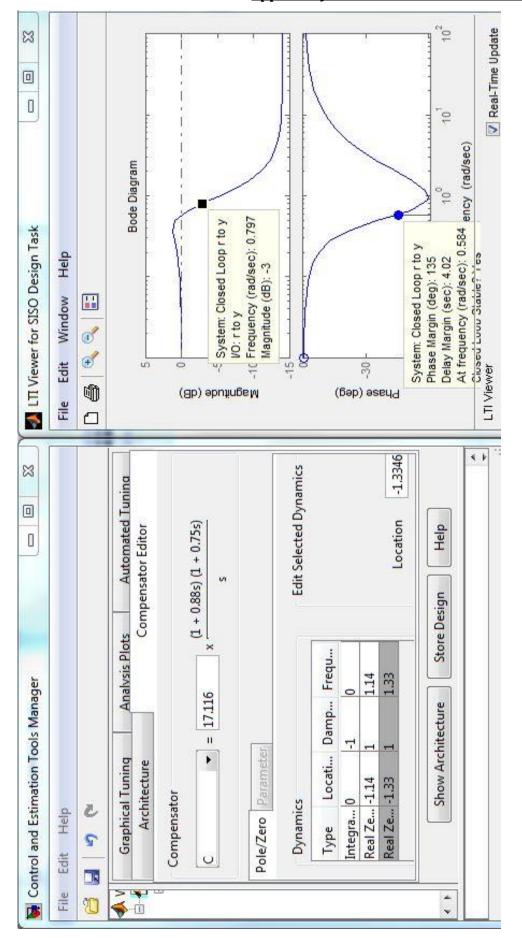
<u> Appendix J- Matlab ACSYS PID bode design</u>

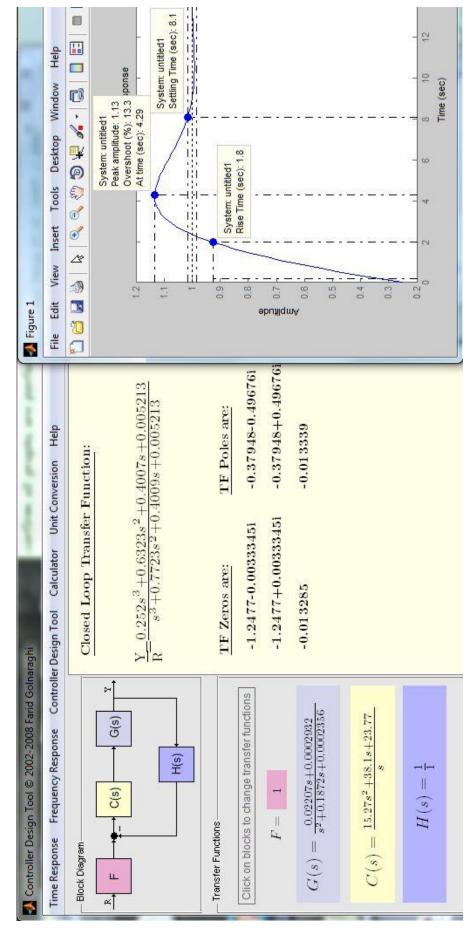
<u> Appendix J- Matlab ACSYS PID bode design</u>

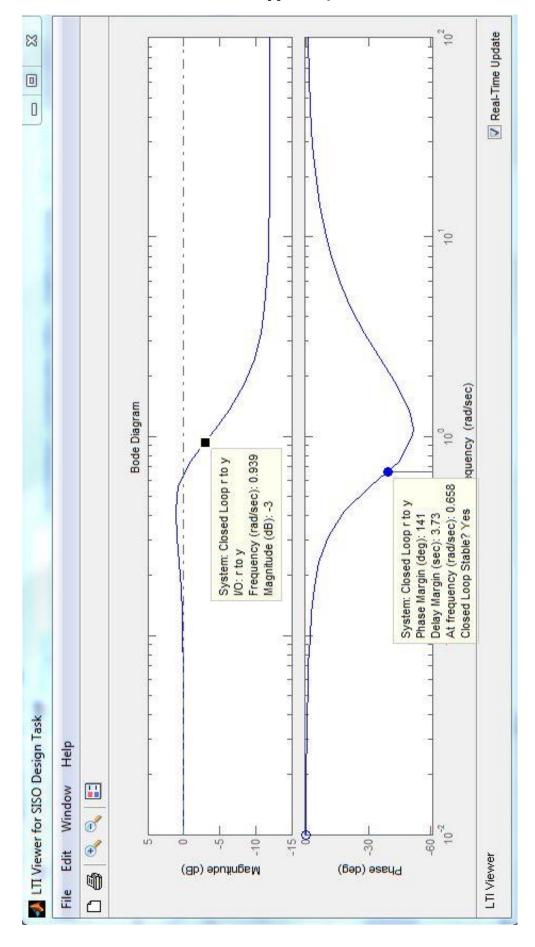




Appendix J- Matlab ACSYS PID bode design



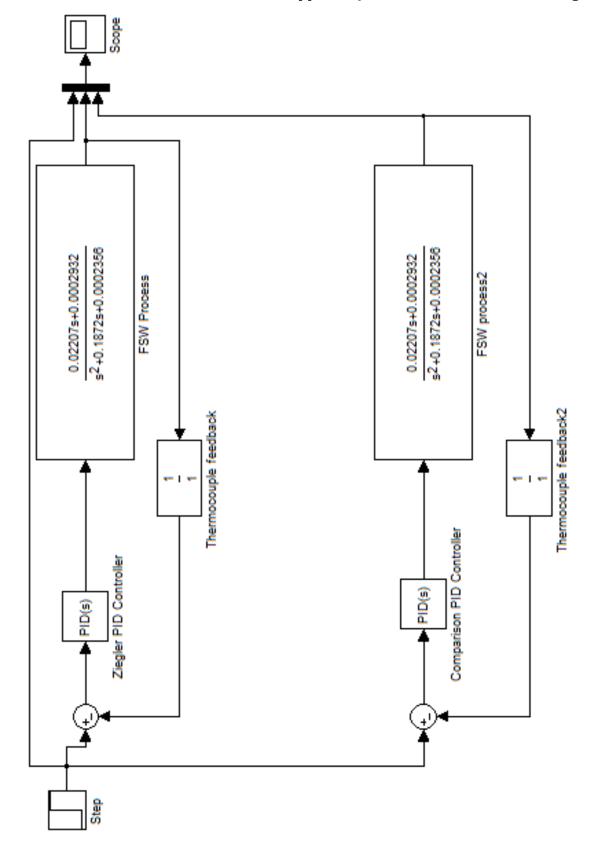


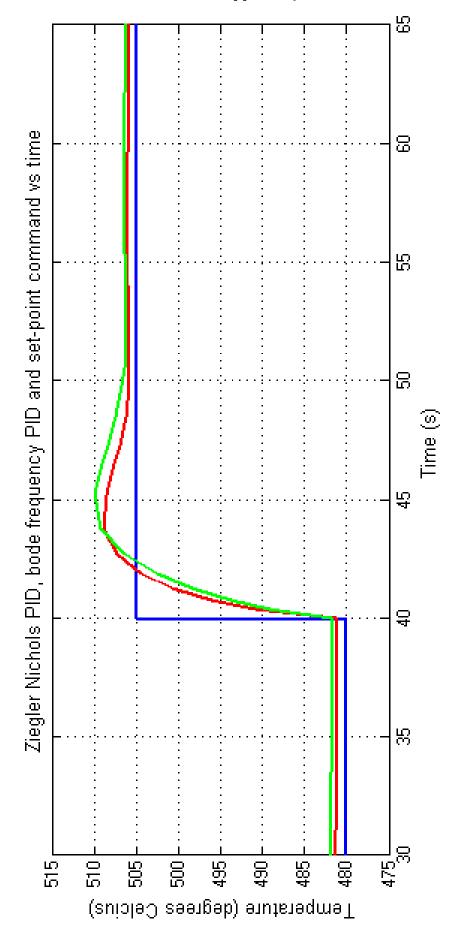


Step			
Dutput a step			
Parameters			
Step time:			
40			
Initial value:			
480			
Final value:			
505			
Sample time	:		
0			
Interpret	vector parame	ters as 1-D	
🗸 Enable ze	ro-crossing de	tection	
	ок	Cancel	Help

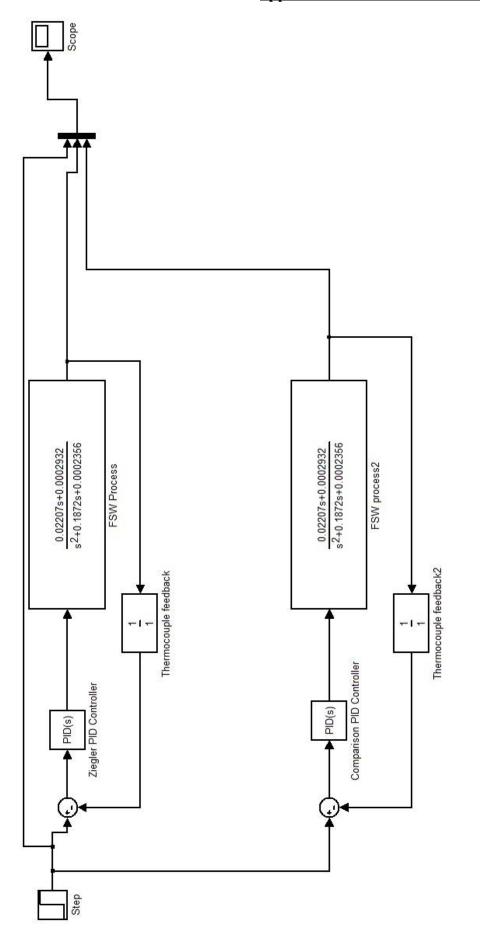
🙀 Function Block Parameters: Zregler PID Controller	Function Block Par	🙀 Function Block Parameters: Comparison PID Controller	X
PID Controller	PID Controller		•
This block implements continuous- and discrete-time PID control algorithms and includes advanced features si anti-windup, external reset, and signal tracking. You can tune the PID gains automatically using the 'Tune' bi (requires Simulink Control Design).	This block implements continuous- anti-windup, external reset, and si (requires Simulink Control Design)	This block implements continuous- and discrete-time PID control algorithms and includes advanced features such anti-windup, external reset, and signal tracking. You can tune the PID gains automatically using the "Tune' buttu (requires Simulink Control Design).	anced features such ng the 'Tune' buttı
Controller: PD	Controller: PID		
Time-domain:	Time-domain:		
Continuous-time	 Continuous-time 	Ð	ш
 Discrete-time 	Discrete-time		
Main PID Advanced Data Types State Attributes	Main PID Advanced	nced Data Types State Attributes	
Controller settings	Controller settings		
Controller form: Parallel	Controller form:	Parallel	
Proportional (P): 38.1	Proportional (P):	27.8693	
Integral (I): 23.769	Integral (I):	17.116	
Derivative (D): 15.268 Filter coefficient (N): 2	Derivative (D):	11.2727 Filter coefficient (N): 2	
Tune			Tune
Initial conditions	Initial conditions		
Source: internal	Source: internal	la	k
E	•	E	-
OK Cancel Help Apply	0	OK Cancel He	Help Apply

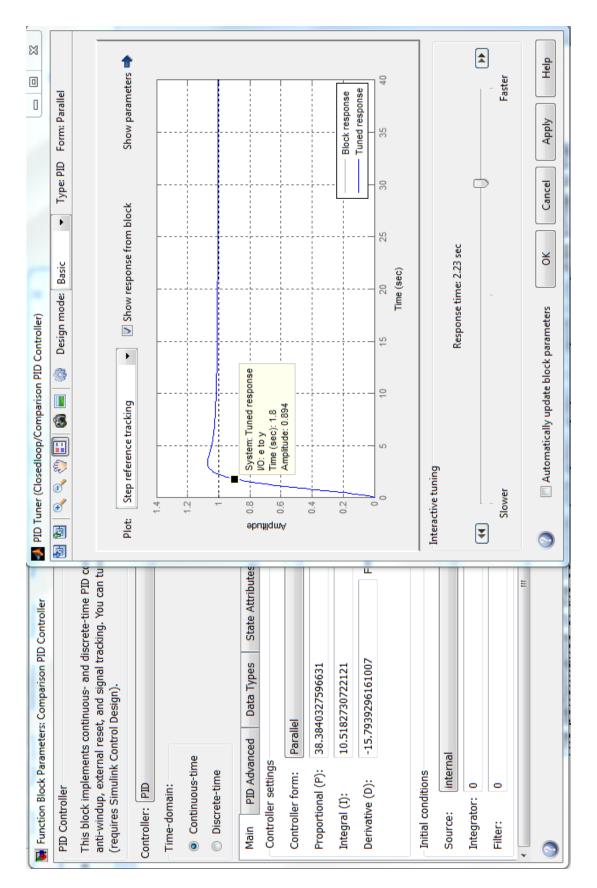
Appendix J- Matlab ACSYS PID bode design





Appendix J- Matlab ACSYS PID bode design



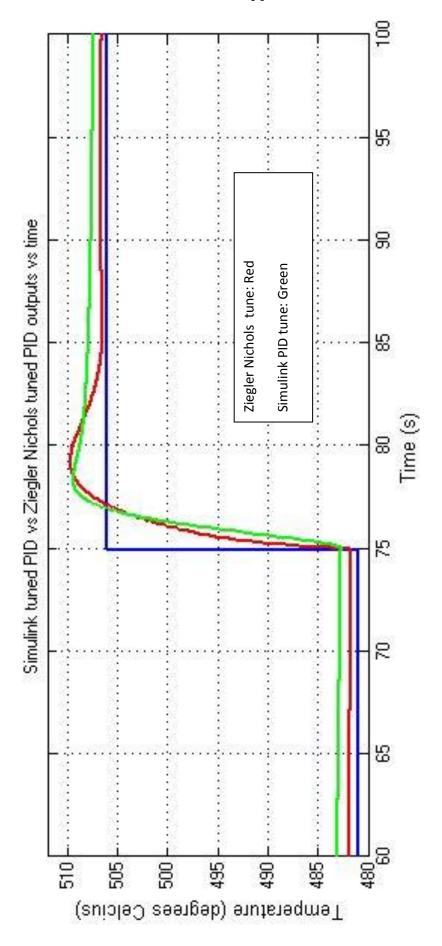


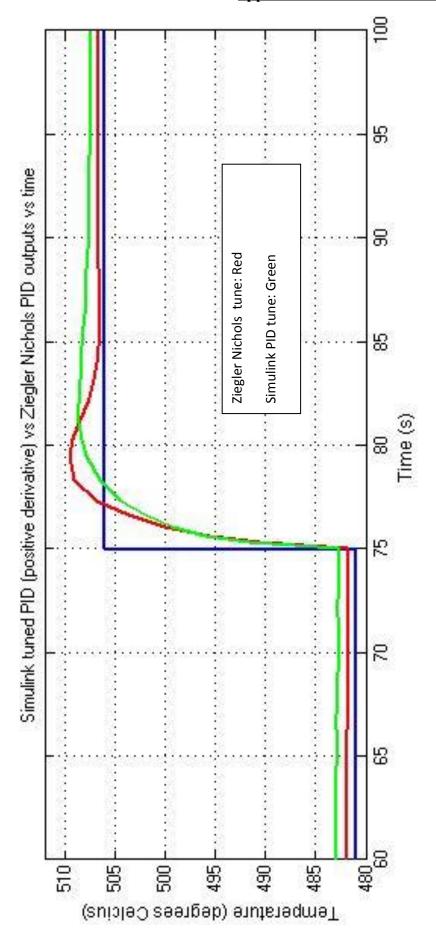
×						ш													
blier		This block implements continuous- and discrete-time PID control algorithms and includes advanced features such as anti-windup, external reset, and signal tracking. You can tune the PID gains automatically using the 'Tune' button (requires Simulink Control Design).					State Attributes					Filter coefficient (N): 2.43030288804969	Tune					Ĕ	OK Cancel Help Apply
Function Block Parameters: Comparison PID Controller		This block implements continuous- and discrete-t- anti-windup, external reset, and signal tracking.) (requires Simulink Control Design).			-time	ē	PID Advanced Data Types State	ings	n: Parallel	<pre>): 38.3840327596631</pre>	10.5182730722121	-15.7939296161007		IS	internal				
Function Block	PID Controller	This block imple anti-windup, ex (requires Simul	Controller: PID	Time-domain:	 Continuous-time 	Oiscrete-time	Main PID A	-Controller settings	Controller form:	Proportional (P):	Integral (I):	Derivative (D):		Initial conditions	Source: in	Integrator: 0	Filter: 0		0
X	•	thms and includes advanced features such as gains automatically using the 'Tune' button				ш						2	Tune					-	Cancel Help Apply
🙀 Function Block Parameters: Ziegler PID Controller		This block implements continuous- and discrete-time PID control algorithms and includes advanced features such as anti-windup, external reset, and signal tracking. You can tune the PID gains automatically using the 'Tune' button (requires Simulink Control Design).	Controller:	Time-domain:	 Continuous-time 	Discrete-time	PID Advanced Data Types State Attributes	Controller settings	Controller form: Parallel	Proportional (P): 38.1	23.769	Derivative (D): 15.268 Filter coefficient (N): 2		Initial conditions	Source: internal	Integrator: 0	0	10 1	OK

Appendix K- Matlab Simulink PID tune

Function Block Parameters: Ziegler PID Controller	Function Block Parameters: Comparison PID Controller
PID Controller	PID Controller
This block implements continuous- and discrete-time PID control algorithms and includes advanced features such as anti-windup, external reset, and signal tracking. You can tune the PID gains automatically using the 'Tune' button (requires Simulink Control Design).	This block implements continuous- and discrete-time PID control algorithms and includes advanced features such as anti-windup, external reset, and signal tracking. You can tune the PID gains automatically using the "Tune' button (requires Simulink Control Design).
Controller: PD	Controller: [PID
Time-domain:	Time-domain:
 Continuous-time 	Continuous-time
◎ Discrete-time	◎ Discrete-time
Main PID Advanced Data Types State Attributes	Main PID Advanced Data Types State Attributes
- Controller settings	Controller settings
Controller form: Parallel	Controller form: Parallel
Proportional (P): 38.1	Proportional (P): 38.3840327596631
Integral (I): 23.769	Integral (I): 10.5182730722121
Derivative (D): 15.268 Filter coefficient (N): 2	Derivative (D): 15.7939296161007 Filter coefficient (N): 2.43030288804969
Tune	Tune
Initial conditions	Initial conditions
Source: Internal	Source: Internal
Integrator: 0	Integrator: 0
Filter: 0	Filter: 0
E	E
OK Cancel Help Apply	OK Cancel Help Apply

K-4





K-6

t tests (comparing 4.1	and 4.2	2)			
yield 1			yield 2		
t-Test: Two-Sample Assuming E	qual Varia	inces	t-Test: Two-Sample Assuming Ed	qual Varia	inces
	Variable 1	Variable 2		Variable 1	Variable 2
Mean	146.69	142.553	Mean	146.733	150.274
Variance	0.53975	3.38641	Variance	24.8612	0.740383
Observations	3	3	Observations	3	3
Pooled Variance	1.96308		Pooled Variance	12.8008	
Hypothesized Mean Difference	0		Hypothesized Mean Difference	0	
df	4		df	4	
t Stat	3.6157		t Stat	-1.21225	
P(T<=t) one-tail	0.01122		P(T<=t) one-tail	0.14606	
t Critical one-tail	2.13185		t Critical one-tail	2.13185	
P(T<=t) two-tail	0.02244		P(T<=t) two-tail	0.29212	
t Critical two-tail	2.77645		t Critical two-tail	2.77645	
yield 3			yield 4		
t-Test: Two-Sample Assuming E	qual Varia	inces	t-Test: Two-Sample Assuming Ed	qual Varia	inces
	Variable 1	Variable 2		Variable 1	Variable 2
Mean	145.871	149.331	Mean	141.1	147.7887
Variance	1.78094	3.83269	Variance	3.23882	2.19835
Observations	3	3	Observations	3	3
Pooled Variance	2.80682		Pooled Variance	2.71859	
Hypothesized Mean Difference	0		Hypothesized Mean Difference	0	
df	4		df	4	
t Stat	-2.52963		t Stat	-4.96861	
P(T<=t) one-tail	0.03235		P(T<=t) one-tail	0.00383	
t Critical one-tail	2.13185		t Critical one-tail	2.13185	
P(T<=t) two-tail	0.06469		P(T<=t) two-tail	0.00766	
t Critical two-tail	2.77645		t Critical two-tail	2.77645	

ultimate 1			ultimate 2		
t-Test: Two-Sample Assuming Ec	qual Varia	nces	t-Test: Two-Sample Assuming Ed	qual Varia	ances
	Variable 1	/ariable 2		Variable 1	Variable 2
Mean	232.03	230.13	Mean	232.52	234.24
Variance	7.1559	2.7004	Variance	11.5371	0.2677
Observations	3	3	Observations	3	3
Pooled Variance	4.92815		Pooled Variance	5.9024	
Hypothesized Mean Difference	0		Hypothesized Mean Difference	0	
df	4		df	4	
t Stat	1.04823		t Stat	-0.86708	
P(T<=t) one-tail	0.17684		P(T<=t) one-tail	0.21741	
t Critical one-tail	2.13185		t Critical one-tail	2.13185	
P(T<=t) two-tail	0.35369		P(T<=t) two-tail	0.43482	
t Critical two-tail	2.77645		t Critical two-tail	2.77645	
ultimate 3			ultimate 4		
t-Test: Two-Sample Assuming Ec	qual Varia	nces	t-Test: Two-Sample Assuming Ed	qual Varia	ances
	Variable 1	/ariable 2		Variable 1	Variable 2
Mean	230.273	234.95	Mean	227.707	230.8367
Variance	0.78703	0.3469	Variance	1.13013	3.494433
Observations	3	3	Observations	3	3
Pooled Variance	0.56697		Pooled Variance	2.31228	
Hypothesized Mean Difference	0		Hypothesized Mean Difference	0	
df	4		df	4	
t Stat	-7.60682		t Stat	-2.52098	
P(T<=t) one-tail	0.0008		P(T<=t) one-tail	0.03264	
t Critical one-tail	2.13185		t Critical one-tail	2.13185	
P(T<=t) two-tail	0.0016		P(T<=t) two-tail	0.06529	
t Critical two-tail	2.77645		t Critical two-tail	2,77645	

	standard deviations of 4.1 yield	standard deviations of 4.2 yield
Mean	3.070942735	3.670922025
Variance	2.091544868	0.71287331
Observations	3	3
Pooled Variance	1.402209089	
Hypothesized Mean Difference	0	
df	4	
t Stat	-0.620548172	
P(T<=t) one-tail	0.284252603	
t Critical one-tail	2.131846786	
P(T<=t) two-tail	0.568505207	
t Critical two-tail	2.776445105	

t-Test: Two-Sample Assuming Equal Variances

t-Test: Two-Sample Assuming Equal Variances

	standard	standard
	<i>deviations of</i> 4.1 ultimate	deviations of 4.2 ultimate
Mean	2.22301058	2.679940826
Variance	2.59746511	0.036621591
Observations	3	3
Pooled Variance	1.31704335	
Hypothesized Mean Difference	0	
df	4	
t Stat	-0.487635709	
P(T<=t) one-tail	0.32566394	
t Critical one-tail	2.131846786	
P(T<=t) two-tail	0.65132788	
t Critical two-tail	2.776445105	