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*In silico* assessment of mouth-throat effects on regional deposition in the upper tracheobronchial airways.

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**Abstract**

Regional deposition of inhaled medicines is a valuable metric of effectiveness in drug delivery applications to the lung. *In silico* methods are now emerging as a valuable tool for the detailed description of localized deposition in the respiratory airways. In this context, there is a need to minimize the computational cost of high-fidelity numerical approaches. Motivated by this need, the present study is designed to assess the role of the extrathoracic airways in determining regional deposition in the upper bronchial airways. Three mouth-throat geometries, with significantly different geometric and filtering characteristics, are merged onto the same tracheobronchial tree that extends to generation 8, and Large Eddy Simulations are carried out at steady inhalation flowrates of 30 and 60 *L/min*. At both flowrates, large flow field differences in the extrathoracic airways across the three geometries largely die out below the main bifurcation. Importantly, localized deposition frac-

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tions are found to remain practically identical for particles with aerodynamic diameters of up to  $d_p = 4\mu m$  and  $d_p = 2.5\mu m$  at 30 and 60  $L/min$ , respectively. For larger particles, differences in the localized deposition fractions are shown to be mainly due to variations in the mouth-throat filtering rather than upstream flow effects or differences in the local flow field. Deposition efficiencies in the individual airway segments exhibit strong correlations across the three geometries, for all particle sizes. The results suggest that accurate predictions of regional deposition in the tracheobronchial airways can therefore be obtained if the particle size distribution that escapes filtering in the mouth-throat (ex-cast dose) of a particular patient is known or can be estimated. These findings open the prospect for significant reductions in the computational expense, especially in the context of *in silico* population studies, where the aerosol size distribution and precomputed flow field from standardized mouth-throat models could be used with large numbers of tracheobronchial trees available in chest-CT databases.

*Keywords:*

particle deposition, upper tracheobronchial airways, Large Eddy Simulations, regional deposition, Computational Fluid Dynamics, ex-cast aerosol size distribution

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## 1. Introduction

2 Drug delivery via the pulmonary route is widely used for the treatment  
3 of pulmonary infections and respiratory diseases such as asthma, Chronic  
4 Obstructive Pulmonary Disease (COPD) and cystic fibrosis. More recently,  
5 the inhaled route has also emerged as a promising method for the systemic

6 administration of drugs, due to the favorable absorption characteristics of  
7 the lungs (Smyth and Hickey, 2011).

8 The amount of drug that deposits in different regions of the respiratory  
9 tract is an important factor that affects the efficacy of inhaled drug delivery.  
10 Knowledge of the regional deposition within the lungs can assist with drug  
11 dosing decisions, and is valuable in assessing the effectiveness of drug tar-  
12 geting strategies and in optimizing patient maneuvering during inhalation.  
13 However, determining regional deposition accurately is not an easy task.

14 *In vivo*, deposition patterns can be determined using nuclear imaging  
15 techniques, such as 2D gamma scintigraphy, single photon emission com-  
16 puted tomography (SPECT), or positron emission tomography (PET), by  
17 the addition of a radiolabel to the aerosol formulation (Conway, 2012). These  
18 methods have the advantage of describing the real state, but remain limited  
19 by a number of challenges, such as insufficient spatial resolution and concerns  
20 from patient exposure to radiation.

21 *In vitro*, regional deposition in the tracheobronchial (TB) tree can be de-  
22 termined by using replicas of human airways derived from Computed Tomog-  
23 raphy (CT) scans, and because higher doses of radioactivity can be applied,  
24 they often provide better spatial resolution relative to *in vivo* methods. How-  
25 ever, they are time-consuming and cannot easily be performed on a routine  
26 basis. As a result, the current industry standard is the use of pharmacopeial  
27 induction ports mounted on cascade impactors, which provides estimates of  
28 total lung deposition (Olson et al., 2013). However, when the bioavailability  
29 of the drug is less than 100%, the deposited lung dose is overpredicted due to  
30 mucociliary clearance of the dose fraction deposited in the TB region (Olsson

31 [and Backman, 2014](#)). In this case, the efficacy of drug delivery depends, in  
32 part, on the site of deposition within the airways. Therefore, quantifying  
33 regional deposition is important in assessing and optimizing the systemic  
34 delivery of drugs with limited lung bioavailability, as well as in topical treat-  
35 ments requiring the targeting of specific lung sites.

36 *In silico* models can complement *in vivo/in vitro* tests and provide de-  
37 tailed information on regional deposition patterns. They can be used to  
38 perform repeated numerical experiments aiming to isolate the effect of a par-  
39 ticular variable, something that is difficult to achieve *in vitro* or *in vivo*. A  
40 concise critical review of Computational Fluid Dynamics (CFD) techniques  
41 for *in silico* studies of the upper airways is given in [Koullapis et al. \(2017\)](#).

42 Due to the geometrical complexity and high Reynolds numbers, espe-  
43 cially at flowrates that are relevant to drug delivery via Dry Powder In-  
44 halers (DPIs), airflow in the upper airways usually transitions to turbulence  
45 ([Tawhai and Lin, 2011](#)). Three different methods can be applied to solve  
46 the turbulent flow: direct numerical simulations (DNS), Reynolds averaged  
47 Navier-Stokes (RANS) and large eddy simulations (LES). DNS resolves the  
48 turbulent fluctuations at all scales, providing the most accurate picture of  
49 the flow ([Nicolaou and Zaki, 2013](#)), but still remains exceedingly costly to  
50 perform on current computers. Presently, most CFD studies solve only for  
51 the averaged (or mean) flow using the RANS equations. A large reduction  
52 in computational cost is achieved in comparison to DNS, however accurate  
53 prediction of the laminar-turbulent-laminar flow transition that occurs in the  
54 TB airways is challenging for RANS ([Kleinstreuer and Zhang, 2010](#)). A more  
55 robust choice is the method of Large Eddy Simulations (LES), where only

56 the smallest scales of motion are discarded and accounted for via a model.  
57 The computational expense of LES is considerably higher than that of RANS,  
58 but it retains significantly more elements of the underlying turbulence physics  
59 (Radhakrishnan and Kassinos, 2009; Koullapis et al., 2016).

60 With increasing gains in computing power, LES has become affordable for  
61 research purposes, but its application remains challenging for both popula-  
62 tion studies, where a large sample would need to be simulated, and for routine  
63 clinical use on a patient-specific basis. Therefore, there is a need to reduce  
64 the computational times required to predict regional deposition. Moreover,  
65 whereas CT-reconstruction of the imaged TB airways is straightforward and  
66 semi-automated in specialized imaging softwares (Miyawaki et al., 2016b),  
67 reconstruction of the extrathoracic airways is more challenging due to the  
68 complexity of the structures in this region. Therefore, *in silico* assessments  
69 of regional deposition in the TB region can be accelerated further if recon-  
70 struction of a patient's MT geometry is not required. In addition to this, a  
71 large amount of chest CT-scans, which typically exclude the extrathoracic  
72 airways (Miyawaki et al., 2017), are available and could potentially be used  
73 for population studies of lung deposition.

74 The pronounced effect of geometric variation on deposition in the ex-  
75 trathoracic airways is well documented in the literature (Grgic et al., 2004a;  
76 Heenan et al., 2004; Burnell et al., 2007; Nicolaou and Zaki, 2013). Grgic  
77 et al. (2004a) performed measurements in several realistic MT geometries at  
78 flowrates of 30 and 90  $L/min$  for particle diameters of 3-6.5 $\mu m$ . They found  
79 that both total and regional deposition exhibit large inter-subject differences,  
80 as well as intra-subject variability to a lesser extent. Deposition was found

81 to occur primarily via impaction, and the mouth area was identified as the  
82 largest obstacle for inhaled aerosols. An empirical Reynolds number correc-  
83 tion,  $Re^{0.37}$ , was applied to the Stokes number (Grgic et al., 2004b), which  
84 reduced scatter in the reported deposition efficiencies, and provided better  
85 collapse of their data onto a single curve.

86 In a later study, Nicolaou and Zaki (2013) examined the flow in a subset  
87 of four MT geometries used by Grgic et al. (2004a). Adopting an immersed  
88 boundary method to simplify the task of grid generation for the realistic  
89 airway geometries (Nicolaou et al., 2015), the authors performed DNS of the  
90 flow and related the predicted flow to the variations in deposition observed  
91 in the *in vitro* measurements. It was found that geometric variation, even  
92 within the same subject, has a large impact on both the mean velocity profiles  
93 and the turbulence intensities. Their analysis revealed that the empirical  
94 correlation  $StkRe^{0.37}$  arises due to the fact that deposition in the airways  
95 occurs via both impaction and turbulent diffusion. More recently, the authors  
96 proposed the use of an instantaneous Stokes number, based on the local  
97 properties of the flow field, for a more accurate representation of particle  
98 transport and deposition in the airways (Nicolaou and Zaki, 2016).

99 In an effort to identify key geometric parameters governing MT depo-  
100 sition, Burnell et al. (2007) investigated retention of drug aerosols inhaled  
101 from four delivery devices in 12 physical MT models *in vitro*. They found  
102 that deposition in the 12 models was dependent on the inhalation delivery  
103 system and that the most influential factor in MT deposition was the total  
104 volume. The airway geometries were ranked based on their retention effi-  
105 ciency and three models that represent high, median and low oropharyngeal

106 filtration were identified. They suggested that these three models may rea-  
107 sonably cover the range of MT dimensions in the adult population and could  
108 therefore be used to indicate the expected range of MT deposition.

109 Besides the effect of geometric variability, previous studies have shown  
110 the importance of taking into account the laryngeal jet in order to accu-  
111 rately predict the airflow and aerosol deposition in the central airways. [Lin  
112 et al. \(2007\)](#) published the first DNS study in a subject-specific model of  
113 the upper airways with and without the MT region. They highlighted the  
114 role of the laryngeal jet in the production of turbulence downstream of the  
115 glottis constriction and concluded that subject-specific evaluations should  
116 include the extrathoracic airways. In a similar study, [Xi et al. \(2008\)](#) ex-  
117 amined airflow and particle deposition in the upper TB airways in models  
118 with and without an approximate larynx using RANS. Significant differences  
119 were revealed between the two TB models in terms of flow patterns, aerosol  
120 dynamics, and wall deposition values.

121 In an LES study, [Choi et al. \(2009\)](#) investigated further the effect of  
122 truncation of the extrathoracic airways on the airflow in the trachea and  
123 downstream regions, in an effort to reduce imaging and computational costs.  
124 It was observed that the larger the truncation, the more inaccurate the flow  
125 fields. However, when the geometry was truncated at the midpharynx and a  
126 uniform velocity boundary condition was imposed, the predicted maximum  
127 mean velocity and rms fluctuations in the trachea and the distal bronchial  
128 airways were in fair agreement with the complete geometry. Working towards  
129 the same goal, [Miyawaki et al. \(2017\)](#) proposed an idealised laryngeal model  
130 that can be attached to the imaged central airways starting from the trachea.



131 It was found that by imposing isotropic turbulent conditions proximal to  
132 the glottis, the laryngeal model approximation could reproduce a realistic  
133 level of turbulence compared to the full geometry containing the patient's  
134 mouth-throat. In addition, it was concluded that if particle deposition in the  
135 central airways is of interest, inclusion of the extrathoracic region may not  
136 be necessary.

137 In the current study, an *in silico* assessment of MT effects on deposition  
138 in the central airways is carried out. Three extrathoracic airway geometries,  
139 with different geometric and deposition characteristics, are merged onto the  
140 same TB tree that extends to generation 8. LES simulations are performed  
141 at steady inhalation flowrates of 30 and 60  $L/min$ , which are relevant to drug  
142 delivery applications. The objective of this investigation is to quantify the  
143 effect of geometric (and thus flow field) variations in the extrathoracic airways  
144 on regional aerosol deposition in the first few generations of the human TB  
145 tree. The critical question we address is whether standardized MT models  
146 can be used to predict regional deposition in the bronchial airways with  
147 acceptable accuracy. A positive answer to this question would result in three  
148 important advantages:

- 149 1. Imaging and reconstructing the patient's extrathoracic airways would  
150 not be required. This would accelerate *in silico* assessments, and would  
151 be beneficial for the patient as it reduces exposure to radiation.
- 152 2. Precomputed flow fields in these standard MT models could be adopted  
153 for predictions of deposition in the bronchial tree, which would result  
154 in significant computational savings.
- 155 3. It could provide a rational approach to using the large number of chest

156 CT-scans lacking MT data for *in silico* population studies.

157 The paper is organized as follows: Section 2 presents the airway geome-  
158 tries employed in this study, the numerical method adopted for the solution  
159 of the flow equations, and the particle-tracking scheme. Validation cases are  
160 also reported. In Section 3, results are presented for the airflow and particle  
161 deposition across the airway geometries at two flow rates,  $Q = 30, 60 L/min$ .  
162 Finally, in Section 4 we summarize the main findings of the current study  
163 and discuss limitations and future extensions.

## 164 2. Methods

### 165 2.1. Airway geometries

166 Three extrathoracic geometries, extending from a circular inlet at the  
167 mouth to the upper trachea, were merged onto the same model of the in-  
168 trathoracic airways. The three MT models are shown in fig. 1.

169 [Figure 1 about here.]

170 The first geometry, R1, was developed by Lovelace Respiratory Research  
171 Institute. Details on the dimensions of the model are provided in [Cheng et al.](#)  
172 (1997). The anterior oral cavity was molded from an *in vivo* dental impres-  
173 sion of a living Caucasian male at approximately 50% of full opening, and  
174 the remaining model was cast postmortem. The two other MT geometries,  
175 S1a and S2, were used in the *in vitro* deposition measurements of [Grgic et al.](#)  
176 (2004a) and in the DNS study of [Nicolaou and Zaki](#) (2013). These models  
177 were obtained using magnetic resonance imaging (MRI), as explained in de-  
178 tail by [McRobbie et al.](#) (2003). The main dimensions of the three MT models

179 are listed in Table 1. The equivalent mean diameter was calculated assuming  
 180 a circular cross-sectional area,

$$D_{mean} = 2\sqrt{\frac{V}{\pi L}}, \quad (1)$$

181 where  $V$  is the volume of the geometry and  $L$  is the sagittal length. The de-  
 182 gree of area constriction at the glottis, which affects the characteristics of the  
 183 laryngeal jet (Choi et al., 2009), is also reported in Table 1 ( $A_{glottis}/A_{trachea}$ ).

184 [Table 1 about here.]

185 The considerable variations in the geometric characteristics of the three  
 186 MT models result in notable differences in the airflow fields, which are dis-  
 187 cussed in the following section. In addition, their respective filtering efficien-  
 188 cies also show large deviations. This is reflected in figures 13(b) and 19(b),  
 189 where the CFD-predicted deposition fractions for the three MT models are  
 190 shown as a function of particle size at inhalation flowrates of 30 L/min and 60  
 191 L/min, respectively. Model R1 has the lowest deposition and S1a the highest.  
 192 In all three cases, deposition increases with particle size. For the purpose of  
 193 the present study, differences in the extrathoracic airways are desirable since  
 194 we are seeking to quantify their effect on the regional deposition in the upper  
 195 TB region. Thus, the three models (R1, S1a and S2) were chosen to provide  
 196 a large degree of variability in the geometric characteristics, the flow field,  
 197 and the filtering properties.

198 The TB geometry is shown in fig. 2. The model was obtained from a high-  
 199 resolution CT of the lungs of an adult male free of pathological alterations,

200 excised at autopsy and fixed in nearly end-inspiratory volume (Schmidt et al.,  
201 2004). Geometrical details can be found in Lizal et al. (2015). Segments 23-  
202 32 are outlets used for connecting the relatively small terminal branches into  
203 one larger outlet. The TB airway geometry together with the R1 MT model  
204 were used by Lizal et al. (2015) to measure regional aerosol deposition *in*  
205 *vitro* via PET. In section 2.3, we use these *in vitro* results for validation of  
206 our *in silico* predictions.

207 [Figure 2 about here.]

208 Finally, fig. 3 shows the three merged geometries used in our study. The  
209 MT geometries S1a and S2 were merged with the TB tree so that the location  
210 of the glottis constriction remained at the same height level as in geometry  
211 R1. In order to ensure a smooth geometric transition from the MT to the  
212 TB region, cubic spline interpolation was applied at multiple points along  
213 the circumferences of the MT outlet and the TB model inlet. The curves  
214 were then used to generate smooth surfaces that join the two domains. The  
215 merging procedure was carried out in Ansys ICEM CFD meshing software.  
216 Zoom-in locations in fig. 3(b) and (c) illustrate front and side views of the  
217 merging regions, in the upper and lower panels respectively.

218 [Figure 3 about here.]

## 219 2.2. Simulation Details

### 220 2.2.1. Continuous phase

221 Large Eddy Simulations (LES) are performed using the dynamic version  
222 of the Smagorinsky-Lilly subgrid scale model (Lilly, 1992) in order to exam-  
223 ine the unsteady flow in the realistic airway geometries. Previous studies

224 have shown that this model performs well in transitional flows in the hu-  
 225 man airways (Radhakrishnan and Kassinos, 2009; Koullapis et al., 2016).  
 226 The airflow is described by the filtered set of incompressible Navier-Stokes  
 227 equations,

$$\frac{\partial \bar{u}_j}{\partial x_j} = 0 \quad (2)$$

$$\frac{\partial \bar{u}_i}{\partial t} + \bar{u}_j \frac{\partial \bar{u}_i}{\partial x_j} = -\frac{1}{\rho} \frac{\partial \bar{p}}{\partial x_i} + \frac{\partial}{\partial x_j} \left[ (\nu + \nu_{sgs}) \frac{\partial \bar{u}_i}{\partial x_j} \right]. \quad (3)$$

228 Here,  $\bar{u}_i$ ,  $\bar{p}$ ,  $\rho = 1.2 \text{ kg/m}^3$ ,  $\nu = 1.7 \times 10^{-5} \text{ m}^2/\text{s}$  and  $\nu_{sgs}$  are the velocity com-  
 229 ponent in the i-direction, the pressure, the density and kinematic viscosity of  
 230 air, and the subgrid-scale (SGS) turbulent eddy viscosity, respectively. The  
 231 overbar denotes resolved quantities.

232 The effect of the MT geometry on deposition in the central airways is  
 233 examined for steady inhalation flowrates of 30 and 60  $L/min$ . Table 2 sum-  
 234 marizes the bulk velocity and Reynolds number at the mouth inlet and the  
 235 trachea, which are given by,

$$U_b = \frac{Q}{A}, \quad Re = \frac{U_b D}{\nu},$$

236 where the inlet and trachea diameters are used for the mouth inlet and the  
 237 trachea, respectively.

238 [Table 2 about here.]

239 For the lower flowrate of 30  $L/min$ , the Reynolds number at the inlet of  
 240 models R1 and S2 is in the laminar regime and thus a parabolic velocity  
 241 profile is imposed. For all other cases, the Reynolds number at the inlets is

242 in the transitional to turbulent regime. In order to generate appropriate inlet  
243 velocity conditions, a mapped inlet (or recycling) boundary condition is used  
244 (Tabor et al., 2004). To apply this boundary condition, the pipe at the inlet  
245 is extended by a length equal to ten times its diameter. The pipe section  
246 is initially fed with an instantaneous turbulent velocity field generated in a  
247 separate pipe flow LES. During the simulation, the velocity field from the  
248 mid-plane of the pipe domain is mapped to the inlet boundary. Scaling of the  
249 velocities is applied to enforce the specified bulk flow rate. In this manner,  
250 turbulent flow is sustained in the extended pipe section, and a turbulent  
251 velocity profile enters the mouth inlet.

252 The volumetric flowrates at the 10 terminal outlets are prescribed based  
253 on the values measured *in vitro* (Lizal et al., 2015). These outlet conditions  
254 result in high asymmetry in the ventilation of the two lungs: the left lung  
255 receives 29% of the inhaled air whereas the right lung receives 71%. A no-slip  
256 velocity condition is imposed on the airway walls and atmospheric pressure  
257 is set at the inlet boundary.

258 The governing equations (eqn. 2 and 3) are discretized using a finite  
259 volume method and solved using OpenFOAM, an open-source CFD code.  
260 The scheme is second-order accurate in both space and time. To ensure  
261 numerical stability the time steps used are 5 and  $2.5 \times 10^{-6}$  s for the cases  
262 of 30 and 60 *L/min*, respectively. The mesh densities used in the three cases  
263 are determined based on a preliminary mesh sensitivity study carried out in  
264 the S1a MT model. The final generated meshes consist of approximately 50  
265 million computational cells. Further details on the mesh convergence study  
266 are provided in Section 2.3.

267 *2.2.2. Particle phase*

268 Spherical, rigid and non-rotating particles are introduced at the mouth in-  
 269 let. Using a Lagrangian approach, the motion of each particle is individually  
 270 computed by solving Newton's equations to determine the particle velocity,  
 271  $\vec{u}_p$ , and position,  $\vec{x}_p$ ,

$$m_p \frac{d\vec{u}_p}{dt} = \vec{F}_D + \vec{F}_G + \vec{F}_B, \quad \frac{d\vec{x}_p}{dt} = \vec{u}_p. \quad (4)$$

Here  $m_p$  is the particle mass, and  $\vec{F}_D$ ,  $\vec{F}_G = m_p \vec{g}$ , and  $\vec{F}_B$  are the drag, gravity, and Brownian forces, respectively. The gravitational acceleration vector,  $\vec{g}$ , points in the downward vertical direction.

The drag force acting on the spherical particles is given by,

$$\vec{F}_D = \frac{m_p}{\tau_p} (\vec{u} - \vec{u}_p), \quad (5)$$

where  $\vec{u}$  is the filtered fluid velocity interpolated at the position of the particle and  $\tau_p$  is the particle response time, defined as:

$$\tau_p = \frac{\rho_p d_p^2 C_c}{18 \mu_f C_D \frac{Re_p}{24}}, \quad (6)$$

with  $\rho_p = 914 \text{ kg/m}^3$  being the particle density,  $d_p$  the particle diameter,  $\mu_f = 2.04 \times 10^{-5} \text{ kg/ms}$  the dynamic fluid viscosity and  $Re_p = d_p |\vec{u} - \vec{u}_p| / \nu_f$  the particle Reynolds number.  $C_c$  is the Cunningham correction factor, which accounts for slip at the particle surface due to non-continuum effects. It is defined as  $C_c = 1 + \frac{2\lambda}{d_p} [1.257 + 0.4 \exp(-0.55 d_p / \lambda)]$ , where  $\lambda = 0.070 \mu\text{m}$  is the mean free path of air. The drag coefficient,  $C_D$ , is based on the correlation

proposed by [Schiller and Naumann \(1935\)](#):

$$C_D = \begin{cases} \frac{24}{Re_p}(1 + 0.15Re_p^{0.687}) & \text{if } Re_p \leq 1000 \\ 0.44 & \text{if } Re_p > 1000. \end{cases} \quad (7)$$

The Brownian force is important for submicron particles and causes diffusion due to collisions with the air molecules ([Finlay, 2001](#)). The expression for the amplitude of its  $i$ th component is based on the correlation proposed by [Li and Ahmadi \(1992\)](#),

$$F_{B,i} = \zeta_i \sqrt{\frac{1}{\tilde{D}} \frac{2k_B^2 T^2}{\Delta t}}, \quad (8)$$

272 where  $\zeta_i$  is a zero mean variant from a Gaussian probability density function,  
 273  $T=310K$  is the absolute temperature,  $\tilde{D} = (k_B T C_c) / (3\pi\mu_f d_p)$  is the Brown-  
 274 ian diffusion coefficient,  $k_B = 1.3806488 \times 10^{-23} \text{ m}^2 \text{ kg} / \text{s}^2 \text{ K}$  is the Boltzmann  
 275 constant and  $\Delta t$  is the time step used for integration of the particle equations.

276 At each time step, the flow equations are solved first in order to obtain  
 277 the filtered fluid velocity field needed for the calculation of the drag force.  
 278 Then, eqn. 4 is integrated with an implicit Euler scheme. The particle-  
 279 tracking algorithm developed by [Macpherson et al. \(2009\)](#) is adopted. At  
 280 every time step 10 particles for each size are released from random positions  
 281 at the mouth inlet. Particles are released over a time period equal to a flow-  
 282 through in the trachea, and the total number of injected particles is 100,000  
 283 for each particle size. The initial velocity of the particles is set to match the  
 284 air velocity at the inlet. A particle is considered deposited if the distance  
 285 from its centre to the airway wall is equal or less than the particle radius.  
 286 One-way coupling is considered, assuming dilute particle suspensions.



287 *2.3. Validation*

288 *2.3.1. Airflow*

289 In order to determine the required mesh density for our simulations, a set  
290 of preliminary LES in MT model S1a were performed on different mesh sizes,  
291 and the results were compared to DNS data (Nicolaou and Zaki, 2013). Ge-  
292 ometry S1a was selected among the three MT models as the most challenging  
293 case due to the higher inlet Reynolds number, which results in turbulent inlet  
294 conditions even at the lower flowrate of 30 *L/min*. Since the flow relaminar-  
295 izes in the downstream regions, the mesh convergence study was limited to  
296 the MT region. Turbulent velocity conditions were imposed at the inlet using  
297 the mapped inlet boundary condition. At the outlet, a convective outflow  
298 condition was applied, in accordance to the DNS simulations of Nicolaou and  
299 Zaki (2013).

300 Four meshes with increasing densities were generated, designated as Meshes  
301 1 to 4. The near-wall region was resolved with prismatic elements, while the  
302 core of the domain was meshed with tetrahedral elements. Cross-sectional  
303 views of the four meshes near the inlet of S1a are shown in fig. 4. Table 3  
304 reports grid characteristics, such as the initial cell height ( $\Delta r_{min}$ ), the num-  
305 ber of prism layers near the walls, the average expansion ratio of the prism  
306 layers ( $\lambda$ ), the total number of computational cells, the average cell volume  
307 ( $V_{cell,avg.}$ ) and the average and maximum  $y^+$  values. In upper airway appli-  
308 cations, turbulence is usually most active in the shear layers formed between  
309 high and low speed regions, such as the laryngeal jet (Tawhai and Lin, 2011).  
310 Thus, use of a strict  $y^+ = 1$  condition for the near wall mesh is not essential.  
311 Based on this observation, the average cell volume of the generated meshes

312 was approximately halved in every grid refinement. To further assess the  
313 mesh resolution near the walls, the number of prism layers was doubled and  
314 the spacing of the first computing node was reduced to one third in Mesh 4  
315 compared to Mesh 3.

316 [Table 3 about here.]

317 [Figure 4 about here.]

318 Fig. 5 displays the contours of mean velocity magnitude in the central  
319 sagittal plane and at various cross-sections of MT S1a. Results obtained  
320 with the four different meshes are shown alongside the DNS data obtained  
321 using an immersed boundary method (Nicolaou et al., 2015). Fig. 6 shows 2D  
322 profiles of the mean velocity magnitude at the lines of intersection between  
323 cross-sections A1-A2 to E1-E2 and the central sagittal plane. The mean  
324 velocity contours and 2D profiles indicate small differences among the four  
325 meshes. The LES and DNS results are in good agreement overall, which  
326 suggests adequate resolution for this flow configuration. Some differences are  
327 found in the low-speed regions at cross-section C1-C2, which are likely due  
328 to numerical or subgrid turbulence modelling aspects.

329 [Figure 5 about here.]

330 [Figure 6 about here.]

331 Based on the findings presented above, meshes with densities similar to  
332 Mesh 2 were generated for the three MT-TB models, and LES simulations  
333 were carried out at inlet flowrates of 30 and 60  $L/min$ .

334 *2.3.2. Particle deposition*

335 For validation purposes, deposition in geometry R1 was compared to the  
336 *in vitro* measurements by Lizal et al. (2015). Fig. 7 displays the deposition  
337 fractions at the individual geometry segments numbered in fig. 2, for particles  
338 of size  $4.3\mu\text{m}$  at flowrates of 15 and 60  $L/\text{min}$ . The error bars attached to the  
339 *in vitro* results at  $Q = 60 L/\text{min}$  correspond to the estimated experimental  
340 uncertainties as reported by the authors (Lizal et al., 2015). Numerical and  
341 experimental results are shown to be in reasonable agreement. Possible rea-  
342 sons for the observed discrepancies include experimental uncertainties at the  
343 inlet related to the velocity profile and the particle distribution. The *in vitro*  
344 inlet conditions might deviate from the velocity profiles and uniform particle  
345 distribution assumed in the CFD simulations due to the effect of the devices  
346 located upstream of the mouth in the experimental apparatus (Lizal et al.,  
347 2015). Similar levels of deviation between numerical and *in vitro* deposition  
348 results were reported by Koullapis et al. (2017), who applied six different  
349 LES and RANS solvers with different particle-tracking schemes to geometry  
350 R1.

351 In order to assess the degree of uncertainties as compared with other  
352 existing measurement data, we have plotted our CFD-predicted deposition  
353 efficiencies in the distal branches along with *in vitro* results from Lizal et al.  
354 (2015), Zhou and Cheng (2005) and Chan and Lippmann (1980). Fig. 8  
355 displays deposition efficiencies versus the Stokes number (Stk), which is cal-  
356 culated using the diameter and bulk velocity of the parent airway in a par-  
357 ticular bifurcation. As can be seen in the deposition plot, our results fall  
358 within the scatter of the experimental data.

359 [Figure 7 about here.]

360 [Figure 8 about here.]

### 361 **3. Results and Discussion**

362 We begin by examining the flow and aerosol deposition across the three  
363 geometries at the lower inhalation flow rate,  $Q = 30L/min$ . The mean and  
364 turbulent flow characteristics in the extra- and intra-thoracic airways are  
365 presented first, followed by the results for regional deposition. The validity  
366 of the findings is then assessed at a higher inhalation flow rate,  $Q = 60L/min$ ,  
367 in order to provide a conclusive picture of MT effects on the flow and regional  
368 deposition in the TB airways.

#### 369 *3.1. Lower inhalation rate, $Q = 30 L/min$*

##### 370 *3.1.1. Airflow*

371 Figures 9 and 10 show contours of the mean velocity magnitude and  
372 turbulent kinetic energy,  $k = \frac{1}{2} \overline{u'_i u'_i}$  ( $u'_i$  are the fluctuating velocities), in the  
373 MT region and the trachea across the three geometries. Fig. 9(a) also displays  
374 isosurfaces of the mean velocity that outline the laryngeal jet. The mean  
375 velocity and turbulent kinetic energy are normalized by the bulk velocity in  
376 the trachea. Large qualitative differences in the flow characteristics can be  
377 observed in the oral cavities, pharyngeal and laryngeal regions of the three  
378 models. In the oral cavities of R1 and S2, lower velocities are observed, due to  
379 the larger cross-sectional areas compared to S1a. Moreover, the recirculation  
380 regions at the top and bottom walls of the oral passage are larger in these two  
381 geometries. Differences can also be identified in the turbulent kinetic energy

382 levels. The airflow entering the mouth of model S1a is in the transitional  
383 regime. As a result, higher values of  $k$  are recorded near the inlet of S1a  
384 compared to the other two geometries, where the inflow is laminar. Low  
385 velocities and levels of turbulent kinetic energy persist in the pharynx and  
386 larynx of R1. In S1a, the flow accelerates in the narrow larynx, and high  
387 turbulent kinetic energy levels appear at the height of the epiglottis, which  
388 are attributed to the formation of the separated shear layer. In S2, the flow  
389 accelerates at the entrance of the pharynx as a result of the large reduction  
390 in cross-sectional area, and the maximum kinetic energy is observed in this  
391 region. In all three geometries, recirculation zones are found near the anterior  
392 wall at the height (R1, S2) and downstream (S1a) of the epiglottis, due  
393 to the airway curvature. These flow characteristics are consistent with the  
394 observations of [Nicolaou and Zaki \(2013\)](#), where a more detailed description  
395 of the airflow in geometries S1a and S2 is provided.

396 An important flow feature in the extrathoracic airways, which determines  
397 the mean and fluctuating behaviors of the flow downstream, is the laryngeal  
398 jet ([Choi et al., 2009](#)). The characteristics of the laryngeal jet are notably  
399 different in the three cases and are largely affected by the degree of constrict-  
400 tion at the glottis (see Table 1). Geometry R1 has a mild glottal constriction  
401 ( $< 30\%$  reduction in area at the glottis), resulting in a low-speed jet that is  
402 too weak to induce significant mixing with the ambient air, as indicated by  
403 the low turbulent kinetic energy levels in the trachea (fig. 10(b)). On the  
404 other hand, the higher degree of glottal constriction in S1a and S2 results  
405 in much stronger turbulent fluctuations that are convected down to the tra-  
406 chea. In S1a, the narrower glottal passage, in conjunction with the forward

407 inclination of the trachea, shifts the jet core towards the anterior wall of  
408 the upper trachea (velocity isosurfaces and stations A-C for S1a in fig. 9(a)  
409 and (b)) and leads to the formation of a large recirculation region near the  
410 rear wall. In S2, the laryngeal jet expands over a shorter length and a less  
411 pronounced recirculation zone develops due to the vertical orientation of the  
412 trachea below the glottis.

413 As we move to the mid-height of the trachea (station C), the flow has  
414 time to develop and differences in the mean velocity fields start to diminish  
415 notably, although variations are still evident in the turbulent kinetic energy  
416 levels. Further downstream (station D), differences in the mean flow and  
417 turbulence characteristics across geometries are further reduced and only  
418 small discrepancies remain, due to the effects of the upstream flow.

419 [Figure 9 about here.]

420 [Figure 10 about here.]

421 Contours of the normalized mean velocity magnitude in the main bronchi,  
422 and in the smaller airways of generations 3 and 4, are shown in fig. 11. A  
423 notable feature of the flowfield is the pronounced asymmetry at the main  
424 bifurcation, marked by a much larger recirculation zone near the outer wall  
425 of the left main bronchus (fig. 11(a)). The asymmetry in the flow reflects  
426 that of the airways; the left main bronchus branches off the carina at an  
427 angle of  $60^\circ$ , significantly larger than the  $48^\circ$  branching angle of the right  
428 bronchus. The recirculation regions are qualitatively similar across the three  
429 geometries, and only minor differences are observed at the main bifurcation  
430 and in the left main bronchus (fig. 11(a)). Slightly larger variations exist in

431 the right main bronchus, which can be attributed to the higher ventilation of  
432 the right lung. Further down the TB tree, we continue to observe a similar  
433 trend. Variations in the flow are more prominent in the right lung, mainly  
434 in the recirculation regions, as shown in fig. 11(c). Overall however, despite  
435 significant differences in the extrathoracic flow dynamics, the mean velocity  
436 in the TB tree remains qualitatively similar across the three geometries.

437 The corresponding results for the turbulent field in the TB tree are shown  
438 in fig. 12. Higher levels of turbulent kinetic energy are observed in the central  
439 bifurcation and the right main bronchus of models S1a and S2 (fig. 12(a))  
440 compared to geometry R1. These differences can be attributed to the stronger  
441 turbulent intensities arising in the upstream regions of S1a and S2 that are  
442 then convected into the TB tree. Minor differences in turbulent kinetic energy  
443 levels, between S1a and S2 on one hand and R1 on the other, persist in the  
444 distal regions of the left and right lungs, as shown in figs. 12(b) and 12(c),  
445 respectively. It should be noted that turbulent kinetic energy levels in the  
446 bronchial airways are approximately an order of magnitude smaller than  
447 the values recorded in the extrathoracic regions, and thus the transport of  
448 particles is not expected to be affected significantly by these low intensity  
449 turbulent fluctuations.

450 In summary, the effect of geometric variation on the mean and turbulent  
451 flow characteristics in the extrathoracic region was found to be significant  
452 across the three geometries. This is to be expected, since the three models  
453 were chosen so as to provide a large degree of variability. The differences  
454 in the flow fields, however, settled down to relatively minor discrepancies  
455 in the bronchial tree. In the next section, we examine the regional particle

456 deposition, in order to determine the impact of upstream flow effects and  
 457 differences in the local flow field on TB deposition.

458 [Figure 11 about here.]

459 [Figure 12 about here.]

### 460 3.1.2. Particle deposition

461 Fig. 13 shows the deposition fractions as a function of particle size at  
 462 30 L/min in (a) the overall geometry, (b) the mouth-throat region, and (c)  
 463 the tracheobronchial tree. In addition, Fig. 13(c) displays particle sizes in  
 464 terms of the Stokes number based on the mean diameter and bulk velocity  
 465 in the trachea,

$$Stk_{trachea} = \frac{\rho_p d_p^2 U_{trachea}}{18\mu_f D_{trachea}}, \quad (9)$$

466 where  $U_{trachea}$  is given in Table 2 and  $D_{trachea} = 1.63 \text{ cm}$ .

467 Deposition results in the overall geometry follow a similar trend to MT  
 468 deposition, with model S1a having the highest values and R1 the lowest.  
 469 However, differences in the overall deposition across the three geometries  
 470 are significantly smaller than those noted for MT deposition. This is due  
 471 to reverse filtering effects occurring in the TB and MT regions that tend to  
 472 partially compensate for each other. While in the MT region the highest and  
 473 lowest deposition fractions correspond to models S1a and R1, respectively,  
 474 in the TB region these trends are reversed, as shown in fig. 13(c). It is also  
 475 worth noting that in the TB region, deposition appears to be appreciable at  
 476 seemingly very small Stokes numbers ( $Stk < 5 \times 10^{-2}$ ). This is attributed to



477 the fact that the reported Stokes numbers are calculated based on the mean  
478 diameter and bulk velocity in the trachea and thus do not reflect the local  
479 properties of the geometry and the flowfield (Nicolaou and Zaki, 2016). In  
480 geometry S1a, deposition of the  $10\mu m$  particles in the TB region is lower  
481 than for the smaller particles of 6 and  $8\mu m$ , due to the significant filtering  
482 that occurs upstream in the extrathoracic airways. It is important to note  
483 that for particles smaller than  $4\mu m$  ( $Stk_{trachea} < 5.94 \times 10^{-3}$ ), TB deposition  
484 is unaffected by the MT model. Even for  $6\mu m$  particles ( $Stk_{trachea} = 1.34 \times$   
485  $10^{-2}$ ), the maximum variation in TB deposition is less than 4% and, reduces  
486 below 3% if differences in deposition in the trachea (segment 2) are excluded.  
487 Therefore, these results suggest that for particle sizes typically used in drug  
488 delivery applications, i.e. 1-5 microns, localized deposition in the central  
489 airways is largely unaffected by the MT geometry.

490 Deposition within the TB tree can be examined in further detail by de-  
491 termining the deposition fractions in individual airway segments, as shown  
492 in fig. 14 for various particle sizes at  $30 L/min$ . Beyond the trachea, and for  
493 particles smaller than  $6\mu m$ , similar deposition fractions are observed across  
494 the three geometries, even at the localized level. Essentially, for particles  
495 smaller than  $4\mu m$ , differences are negligible in the vast majority of segments  
496 within the TB region. For larger particles with diameters above  $8\mu m$ , vari-  
497 ability in TB regional deposition across the three geometries becomes more  
498 significant. This variation arises due to the large differences in the MT fil-  
499 tering, which are as high as 70% for  $10\mu m$  particles between geometries S1a  
500 and R1 (fig. 13(b)).

501 The conclusions made herein are based on results at  $30 L/min$ . However,

502 many inhaler devices, such as DPIs, typically operate at higher inhalation  
503 flowrates (Wong et al., 2012). Therefore, in the following section, we assess  
504 the validity of these findings at a higher flowrate of  $60 L/min$ .

505 [Figure 13 about here.]

506 [Figure 14 about here.]

### 507 3.2. Higher inhalation rate, $Q = 60 L/min$

#### 508 3.2.1. Airflow

509 Figures 15 and 16 show contours of the normalized mean velocity magni-  
510 tude and turbulent kinetic energy in the MT region and the trachea across  
511 the three geometries at a flowrate of  $60 L/min$ . Fig. 15(a) also displays iso-  
512 surfaces of normalized mean velocity that outline the laryngeal jet. The mean  
513 flow features remain similar to those noted for the lower flowrate. Neverthe-  
514 less, small reductions in the magnitudes of the normalized mean velocities  
515 are evident at this higher flowrate. These lower velocities result from the in-  
516 creased turbulent mixing that occurs as the flowrate, and hence the Reynolds  
517 number, doubles. Turbulent kinetic energy levels in the MT and the trachea  
518 also exhibit strong resemblance to those observed at the lower flowrate, with  
519 the local maxima appearing at the same locations. As in the lower flowrate  
520 case, the effect of geometric variation is clearly evident in the MT region.  
521 However, at the exit to the trachea (D1-D2), the flow is qualitatively similar  
522 across all three geometries despite the higher flowrate and increased turbu-  
523 lence levels.

524 [Figure 15 about here.]

525 [Figure 16 about here.]

526 As we move deeper into the TB tree, first into the main bronchi and then  
527 into bronchial generations 3 and 4, the mean velocity fields are again found  
528 to remain similar across the three cases, as shown in fig. 17. The same holds  
529 for the turbulent kinetic energy levels in the TB region, shown in fig. 18. In  
530 conclusion, despite significant differences in the extrathoracic flow features,  
531 the mean and turbulent fields in the TB tree remain qualitatively similar  
532 across the three geometries even at a flowrate of  $60 L/min$ .

533 [Figure 17 about here.]

534 [Figure 18 about here.]

### 535 3.2.2. Particle deposition

536 Fig. 19 shows the deposition fractions versus particle size at  $60 L/min$  in  
537 (a) the overall geometry, (b) the mouth-throat region, and (c) the tracheo-  
538 bronchial tree. In fig. 19(c), the Stokes number based on tracheal parameters  
539 is also displayed. At this flowrate, greater differences are observed in the over-  
540 all deposition of the smaller particles among the three models (fig. 19(a)).  
541 MT deposition is again significantly different across the three geometries,  
542 and notably at this flowrate, a larger variation is observed for the interme-  
543 diate particle sizes. In S1a, the largest particles are almost entirely filtered  
544 out in the MT (fig. 19(b)). For particles larger than  $2.5\mu m$ , deposition in  
545 the TB region is inversely related to the MT filtering: model R1 has the  
546 highest TB deposition, and S1a the lowest. For particles smaller than  $2.5\mu m$   
547 ( $Stk_{trachea} < 4.64 \times 10^{-3}$ ), TB deposition is unaffected by the MT, whereas

548 for  $4\mu m$  particles ( $Stk_{trachea} = 1.19 \times 10^{-2}$ ) the maximum variation in TB  
549 deposition is 7.5%.

550 [Figure 19 about here.]

551 Fig. 20 shows the deposition fractions in the individual airway segments  
552 for various particle sizes. For particles smaller than  $2.5\mu m$  and downstream  
553 of the first bifurcation (segment 3), segmental deposition fractions are in  
554 good agreement across the three geometries. At  $d_p = 4\mu m$ , slight differences  
555 in localized deposition are observed. For larger particle sizes, the differences  
556 become non-negligible in most of the segments.

557 In order to assess whether the observed differences in localized deposition  
558 in the TB tree are partly due to local flowfield variations or entirely due to  
559 the differential filtering that occurs in the MT region, we examine the seg-  
560 mental deposition efficiencies, defined as the ratio of the number of particles  
561 depositing in a particular segment to the number of particles entering that  
562 segment. Fig. 21 shows the segmental deposition efficiencies for various parti-  
563 cle sizes in the three models. The results show that localized filtering in  
564 the TB tree is practically unchanged among the three models for all parti-  
565 cle sizes. Pairwise deposition efficiency scatter plots for the various particle  
566 sizes are shown in fig. 22. In order to quantify the degree of similarity across  
567 the three geometries, pairwise correlation coefficients,  $r$ , are also reported in  
568 fig. 22. A good collapse of the deposition efficiency values on the  $y = x$  line  
569 is evident, and the correlation coefficients, which in all but one case ( $1\mu m$ ,  
570 R1 vs S2,  $r = 0.9816$ ) are above 0.99, confirm a strong linear correlation.  
571 These results indicate that the minor differences observed in the local TB

572 flow field are largely inconsequential as far as deposition is concerned, and  
573 that the variation in regional deposition fractions results from the differences  
574 in MT filtering.

### 575 3.2.3. Interpretation of results

576 The findings in this section provide useful insight on the suitability of  
577 standardized MT models for accurate predictions of regional deposition in the  
578 upper TB region. For particles with  $Stk_{trachea} < 5.94 \times 10^{-2}$  ( $d_p < 4\mu m$ ) at  
579  $Q = 30 L/min$  and  $Stk_{trachea} < 4.64 \times 10^{-2}$  ( $d_p < 2.5\mu m$ ) at  $Q = 60 L/min$ ,  
580 localized deposition fractions in the TB tree remain practically unchanged in-  
581 dependent of the MT geometry employed. By adopting the precomputed flow  
582 field from a standard MT model, simulations could therefore be restricted to  
583 the tracheobronchial tree resulting in significant computational savings. For  
584 larger particles however, TB deposition, as expressed in terms of deposition  
585 fractions, depends on the MT filtering. Therefore, in order to obtain accu-  
586 rate localized deposition estimates, a standardized MT model with similar  
587 filtering as the patient's MT should be selected. The question then becomes  
588 how to identify the standard model with similar filtering properties; the an-  
589 swer depends on the underlying objective. For example, one scenario is that  
590 of population studies aimed at identifying functional/structural parameters  
591 of the intrathoracic airways that determine regional TB deposition for var-  
592 ious classes of patients. In this context, one could envisage using a small  
593 number of standardized MT geometries, selected so as to be representative  
594 of the expected variability in target patient populations. The aerosol size  
595 distribution that escapes MT filtering (ex-cast dose) and the precomputed  
596 flow field in these particular MT models could then be adopted, which would

597 significantly minimize the time and cost required to compute regional de-  
598 position in the central airways. This would be of significant advantage in  
599 the context of population studies where large numbers of simulations have  
600 to be carried out in order to have an adequate statistical sample. A different  
601 scenario is that of patient-specific simulations. Here, the primary motivation  
602 is to spare the patient the need to image the extrathoracic airways and to  
603 minimize diagnosis time. In this context, further work is needed to identify  
604 key parameters that could be used to match the patient to a specific MT  
605 model. For example, [Burnell et al. \(2007\)](#) conducted an *in vitro* study across  
606 a number of MT geometries, in order to determine the key geometric char-  
607 acteristics governing mouth-throat deposition. Of 51 dimensional variables  
608 investigated, the single most influential factor was found to be the total vol-  
609 ume of the extrathoracic airways. While not conclusive, such studies point  
610 to the possibility that a combination of structural and/or functional param-  
611 eters (such as the patient's inhalation profile) could eventually be shown to  
612 provide a reliable means of classifying the patient's extrathoracic airways.  
613 Clearly, further work is needed in this direction in the form of combined *in*  
614 *vitro* and *in silico* studies, a goal that we are currently pursuing.

615 [Figure 20 about here.]

616 [Figure 21 about here.]

617 [Figure 22 about here.]

#### 618 4. Conclusions

619 The objective of the current study was to quantify the effect of geometric  
620 variation in the mouth and throat on regional deposition in the first gen-

621 erations of a realistic TB tree. Three extrathoracic airways with different  
622 geometric and deposition characteristics were merged onto the same TB ge-  
623 ometry, and the airflow and particle transport were simulated using LES  
624 under steady inhalation conditions at 30 and 60  $L/min$ . The large flowfield  
625 differences observed in the extrathoracic airways and the trachea were found  
626 to largely vanish by the first bifurcation, and the mean flow features and  
627 turbulent kinetic energy levels in the TB region remained similar, regardless  
628 of the inhalation flowrate and the degree of glottal constriction. Localized  
629 deposition in the TB tree was practically unaffected by the MT filtering  
630 for particles smaller than  $4\mu m$  ( $Stk_{trachea} = 5.94 \times 10^{-3}$ ) at 30  $L/min$ , and  
631  $2.5\mu m$  ( $Stk_{trachea} = 4.64 \times 10^{-3}$ ) at 60  $L/min$ . The variability in the depo-  
632 sition fractions at larger particle sizes was shown to be due to variation in  
633 the MT filtering across geometries, rather than differences in the local flow  
634 field. These findings suggest that accurate predictions of regional deposition  
635 in the TB airways can therefore be obtained using standardized MT models  
636 with similar filtering characteristics as the patient's extrathoracic airways.  
637 This approach would circumvent the need to image and reconstruct the ex-  
638 trathoracic airways, reducing patient exposure to radiation and accelerating  
639 *in silico* studies. Furthermore, by adopting the ex-cast dose and precomputed  
640 flow field from standardized MT models, significant computational savings  
641 can be achieved as simulations can be restricted to the TB region, without  
642 the need to include the extrathoracic airways.

643 In the work presented herein, we have merged three MT geometries with  
644 significantly different airflow characteristics as well as filtering efficiencies to  
645 a single TB tree. One would need to repeat this study with more geometries

646 before attempting to generalize observations, nevertheless the prospect is  
647 promising. If the current results are found to be repeatable with different  
648 combinations of airway geometries, large-scale *in silico* studies of regional  
649 deposition in a large sample of TB tree geometries could be performed using  
650 a small set of representative ex-cast particle distributions that cover the  
651 desired cross-sections of patient populations. The large number of chest CT-  
652 scans that are available on medical databases, which typically exclude the  
653 extrathoracic airways, could therefore be utilized in population studies aimed  
654 at identifying the key factors that influence regional deposition patterns.

655 We note that in the present study we have adopted steady inspiratory flow  
656 rates, whereas patient-specific or inhaler-dependent inhalation waveforms are  
657 transient. Transient flow simulations would be required in order to assess  
658 whether the present findings are also valid under these inhalation conditions.  
659 [Tian et al. \(2011\)](#) numerically investigated the effect of transient vs. steady-  
660 state conditions and found that transient inhalation influences the deposition  
661 of particles in the MT and upper TB airways through the third generation,  
662 where the Womersley number is greater than 1. On the other hand, transient  
663 conditions were shown to have little influence on deposition in the TB regions  
664 located distally to the fourth generation, and a steady-state approximation  
665 accurately captured deposition. Deposition in the upper airways during the  
666 exhalation phase is considered to be minor compared to deposition upon in-  
667 halation ([Finlay, 2001](#)). For this reason, the majority of *in vitro* and *in silico*  
668 deposition studies in the upper airways consider only the inhalation phase  
669 ([Grgic et al., 2004a](#); [Lizal et al., 2015](#); [Lambert et al., 2011](#)). In addition to  
670 the flowrate profile, the velocity profiles at the mouth inlet were assumed to



671 be parabolic or turbulent in the present study. In actual drug delivery appli-  
672 cations through an inhaler, however, the inlet velocity profile could deviate  
673 from these conditions due to airflow structures convected from the device.  
674 The effect of inlet velocity profile on aerosol deposition in the upper airways  
675 was examined by Koullapis et al. (2016). Although the authors found that  
676 imposed conditions at the mouth inlet did indeed affect aerosol filtering in  
677 the oral cavity, differences in the flow field dissipated by the time the flow  
678 reached the mid-trachea. Therefore, while one might anticipate a weak effect  
679 of inlet conditions on localized deposition fractions in the TB tree, we expect  
680 the deposition efficiencies to remain fairly insensitive, and the conclusions of  
681 the present study to hold for different inlet conditions as well.

682 In our study the walls of the airway models were assumed rigid. In  
683 reality, however, lungs deform and thus, airway diameter and length vary  
684 during breathing. In a recent study, Miyawaki et al. (2016a) examined the  
685 effect of rigid vs deforming airways on particle transport and deposition in  
686 a subject-specific airway model of the central airways. A difference of 22%  
687 on average, depending on the generation number, was observed between the  
688 rigid and deforming models. Furthermore, the cumulative average deposition  
689 fraction in the rigid model was consistently smaller and the relative difference  
690 between the two models reached 13% in generation 4. In our study, since  
691 the same TB geometry is used in the three cases considered, the degree of  
692 uncertainty in deposition results due to airway deformation is expected to  
693 be similar in all cases.

694 Finally, we also note that for certain DPIs, flow rates as high as  $90 L/min$   
695 are relevant (Islam and Cleary, 2012). Extrapolating from the conclusions

696 of the present work, at this high inhalation rate, one would expect smaller  
697 particle sizes to be affected by the differences in the MT filtering. Neverthe-  
698 less, the expectation is that the deposition efficiencies would remain largely  
699 unaffected. Therefore, one of the main outcomes of this work would remain  
700 valid: ex-cast particle distributions (adjusted for flowrate and patient class)  
701 could be used to compute regional deposition in the proximal TB tree for *in*  
702 *silico* population studies or routine clinical use on a patient-specific basis.

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### 712 **References**

- 713 Burnell, P. K. P., Asking, L., Borgstrom, L., Nichols, S. C., Olsson, B.,  
714 Prime, D., Shrubbs, I., 2007. Studies of the human oropharyngeal airspaces  
715 using magnetic resonance imaging IV - the oropharyngeal retention effect  
716 for four inhalation delivery systems. *Journal of Aerosol Medicine* 20 (3),  
717 269–281.
- 718 Chan, T., Lippmann, M., 1980. Experimental measurements and empirical

- 719 modelling of the regional deposition of inhaled particles in humans. Amer-  
720 ican Industrial Hygiene Association Journal 41 (6), 399–409.
- 721 Cheng, K. H., Cheng, Y. S., Yeh, H. C., 1997. Measurements of airway  
722 dimensions and calculation of mass transfer characteristics of the human  
723 oral passage. Biomechanical Engineering 119, 476–482.
- 724 Choi, J., Tawhai, M., Hoffman, E., Lin, C.-L., 2009. On intra- and intersub-  
725 ject variabilities of airflow in the human lungs. Phys. Fluids 21 (101901).
- 726 Conway, J., 2012. Lung imaging - two dimensional gamma scintigraphy,  
727 SPECT, CT and PET. Advanced Drug Delivery Reviews 64 (4), 357–368.
- 728 Finlay, W. H., 2001. The Mechanics of Inhaled Pharmaceutical Aerosols.  
729 Academic Press, New York.
- 730 Grgic, B., Finlay, W. H., Burnell, P. K. P., Heenan, A. F., 2004a. In vitro  
731 intersubject and intrasubject deposition measurements in realistic mouth–  
732 throat geometries. Journal of Aerosol Science 35 (8), 1025–1040.
- 733 Grgic, B., Finlay, W. H., Heenan, A. F., 2004b. Regional aerosol deposition  
734 and ow measurements in an idealized mouth and throat. Journal of Aerosol  
735 Science 35, 21–32.
- 736 Heenan, A., Finlay, W., Grgic, B., Pollard, A., Burnell, P., 2004. An investi-  
737 gation of the relationship between the flow field and regional deposition in  
738 realistic extra-thoracic airways. Journal of Aerosol Science 35, 1013–1023.
- 739 Islam, N., Cleary, M. J., 2012. Developing an efficient and reliable dry pow-

- 740 der inhaler for pulmonary drug delivery - a review for multidisciplinary  
741 researchers. *Medical Engineering and Physics* 34 (Islama), 409–427.
- 742 Kleinstreuer, C., Zhang, Z., 2010. Airflow and particle transport in the hu-  
743 man respiratory system. *Annual Review of Fluid Mechanics* 42, 301–334.
- 744 Koullapis, P., Kassinos, S. C., Muela, J., Perez-Segarra, C., Rigola, J.,  
745 Lehmkuhl, O., Cui, Y., Sommerfeld, M., Elcner, J., Jicha, M., Saveljic,  
746 I., Filipovic, N., Lizal, F., Nicolaou, L., 2017. Regional aerosol deposition  
747 in the human airways: The siminhale benchmark case and a critical  
748 assessment of in silico methods. *European Journal of Pharmaceutical*  
749 *Sciences*.
- 750 URL [http://www.sciencedirect.com/science/article/pii/  
751 S0928098717304992](http://www.sciencedirect.com/science/article/pii/S0928098717304992)
- 752 Koullapis, P. G., Kassinos, S., Bivolarova, M. P., Melikov, A. K., 2016. Par-  
753 ticle deposition in a realistic geometry of the human conducting airways:  
754 Effects of inlet velocity profile, inhalation flowrate and electrostatic charge.  
755 *Journal of Biomechanics* 49, 2201–2212.
- 756 Lambert, A., O’Shaughnessy, P., Tawhai, M., Hoffman, E., Lin, C.-L., 2011.  
757 Regional deposition of particles in an imaged-based airway model: Large  
758 eddy simulation and left-right lung ventilation asymmetry. *Aerosol Science*  
759 *and Technology* 45, 11–25.
- 760 Li, A., Ahmadi, G., 1992. Dispersion and deposition of spherical particles  
761 from point sources in a turbulent channel flow. *Aerosol Science and Tech-*  
762 *nology* 16, 209–226.

- 763 Lilly, D. K., 1992. A proposed modification of the Germano subgrid-scale  
764 closure method. *Physics of Fluids A* 4 (3), 633–635.
- 765 Lin, C.-L., Tawhai, M., McLennan, G., Hoffman, E., 2007. Characteristics of  
766 the turbulent laryngeal jet and its effect on airflow in the human intra-  
767 thoracic airways. *Respiratory Physiology and Neurobiology* 157, 295–309.
- 768 Lizal, F., Belka, M., Adam, J., Jedelsky, J., Jicha, M., 2015. A method for  
769 in vitro regional aerosol deposition measurement in a model of the human  
770 tracheobronchial tree by the positron emission tomography. *Proceedings*  
771 *IMEchanical E Part H, Engineering in Medicine* 229 (10), 750–757.
- 772 Macpherson, G. B., Nordin, N., Weller, G., 2009. Particle tracking in un-  
773 structured, arbitrary polyhedral meshes for use in CFD and molecular  
774 dynamics. *Communications in Numerical Methods in Engineering* 25 (3),  
775 263–273.
- 776 McRobbie, D., Pritchard, S., Quest, R., 2003. Studies of the human oropharyngeal  
777 airspaces using magnetic resonance imaging. I. Validation of a  
778 three-dimensional MRI method for producing ex vivo virtual and physical  
779 casts of the oropharyngeal airways during inspiration. *Journal of Aerosol*  
780 *Medicinejournal of Aerosol Medicine* 16, 401–415.
- 781 Miyawaki, S., Hoffman, E. A., Lin, C.-L., 10 2016a. Effect of static vs. dy-  
782 namic imaging on particle transport in CT-based numerical models of hu-  
783 man central airways. *Journal of Aerosol Science* 100, 129–139.
- 784 URL <http://www.ncbi.nlm.nih.gov/pmc/articles/PMC5224794/>

- 785 Miyawaki, S., Hoffman, E. A., Lin, C.-L., 2017. Numerical simulations of  
786 aerosol delivery to the human lung with an idealized laryngeal model,  
787 image-based airway model, and automatic meshing algorithm. *Computers  
788 & Fluids* 148, 1–9.  
789 URL [http://www.sciencedirect.com/science/article/pii/  
790 S0045793017300531](http://www.sciencedirect.com/science/article/pii/S0045793017300531)
- 791 Miyawaki, S., Tawhai, M. H., Hoffman, E. A., Wenzel, S. E., Lin, C.-L.,  
792 2016b. Automatic construction of subject-specific human airway geome-  
793 try including trifurcations based on a CT-segmented airway skeleton and  
794 surface. *Biomechanics and Modeling in Mechanobiology*, 1–14.
- 795 Nicolaou, L., Jung, S. Y., Zaki, T. A., 2015. A robust direct-forcing immersed  
796 boundary method with enhanced stability for moving body problems in  
797 curvilinear coordinates. *Computers and Fluids* 119, 101–114.
- 798 Nicolaou, L., Zaki, T. A., 2013. Direct numerical simulations of flow in real-  
799 istic mouth–throat geometries. *Journal of Aerosol Science* 57, 71–87.
- 800 Nicolaou, L., Zaki, T. A., 2016. Characterization of aerosol Stokes number in  
801 90° bends and idealized extrathoracic airways. *Journal of Aerosol Science*  
802 102, 105–127.
- 803 Olson, D. E., Borgstrom, L., H., L., Svensson, M., 2013. Validation of a  
804 general in vitro approach for prediction of total lung deposition in healthy  
805 adults for pharmaceutical inhalation products. *Journal of Aerosol Medicine  
806 and Pulmonary Drug Delivery* 26 (0), 1–115.

- 807 Olsson, B., Backman, P., 2014. Mouth-throat models for realistic in vitro  
808 testing - a proposal for debate. *Respiratory Drug Delivery* 1, 287–294.
- 809 Radhakrishnan, H., Kassinos, S., 2009. CFD modeling of turbulent flow and  
810 particle deposition in human lungs. 31st Annual International Conference  
811 of the IEEE EMBS, Mineapolis, Minnesota, USA, 2867–2870.
- 812 Schiller, L., Naumann, Z., 1935. Ver. Deutsch Ing.
- 813 Schmidt, A., Zidowitz, S., Kriete, A., 2004. A digital reference model of the  
814 human bronchial tree. *Comput Med Imaging Graph* 28, 203–211.
- 815 Smyth, H. D. C., Hickey, A. J., 2011. *Controlled Pulmonary Drug Delivery,*  
816 *Advances in Delivery Science and Technology Series.* Springer, New York.
- 817 Tabor, G. R., Baba-Ahmadi, M. H., de Villiers, E., Weller, H. G., 2004. Con-  
818 struction of inlet conditions for LES of turbulent channel flow. European  
819 Congress on Computational Methods in Applied Sciences and Engineering  
820 (ECCOMAS).
- 821 Tawhai, M., Lin, C.-L., 2011. Airway gas flow. *Comprehensive Physiology* 1,  
822 1135–1157.
- 823 Tian, G., Longest, P. W., Su, G., Walenga, R. L., Hindle, M., 2011. De-  
824 velopment of a stochastic individual path (SIP) model for predicting the  
825 tracheobronchial deposition of pharmaceutical aerosols: effects of transient  
826 inhalation and sampling the airways. *Journal of Aerosol Science* 42, 781–  
827 99.

- 828 Wong, W., Fletcher, D. F., Traini, D., Chan, H.-K., Young, P. M., 2012.  
829 The use of computational approaches in inhaler development. *Advanced*  
830 *Drug Delivery Reviews* 64 (4), 312 – 322.  
831 URL [http://www.sciencedirect.com/science/article/pii/](http://www.sciencedirect.com/science/article/pii/S0169409X11002730)  
832 [S0169409X11002730](http://www.sciencedirect.com/science/article/pii/S0169409X11002730)
- 833 Xi, J., Longest, P. W., Martonen, T. B., 2008. Effects of the laryngeal jet on  
834 nano- and microparticle transport and deposition in an approximate model  
835 of the upper tracheobronchial airways. *Journal of Applied Physiology* 104,  
836 1761–1777.
- 837 Zhou, Y., Cheng, Y.-S., 2005. Particle deposition in a cast of human tracheo-  
838 bronchial airways. *Aerosol Science and Technology* 39 (6), 492–500.



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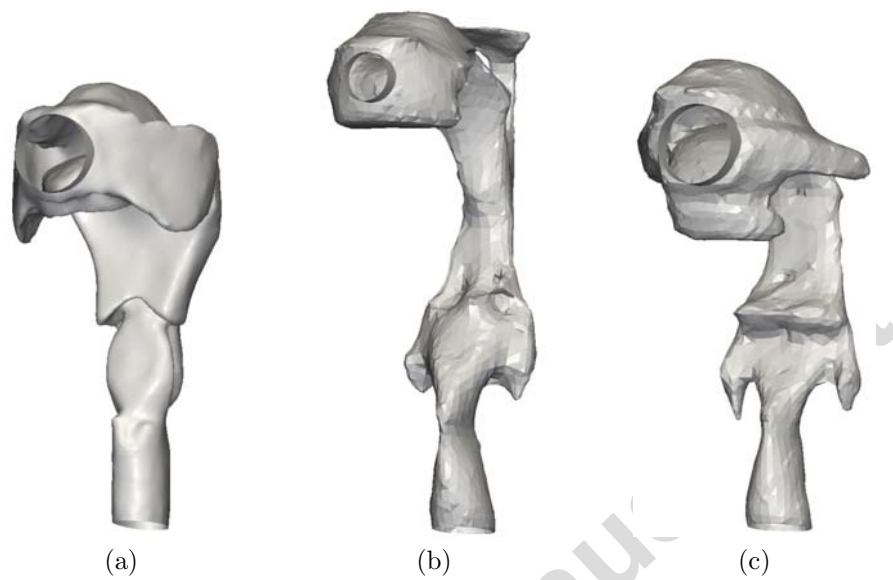


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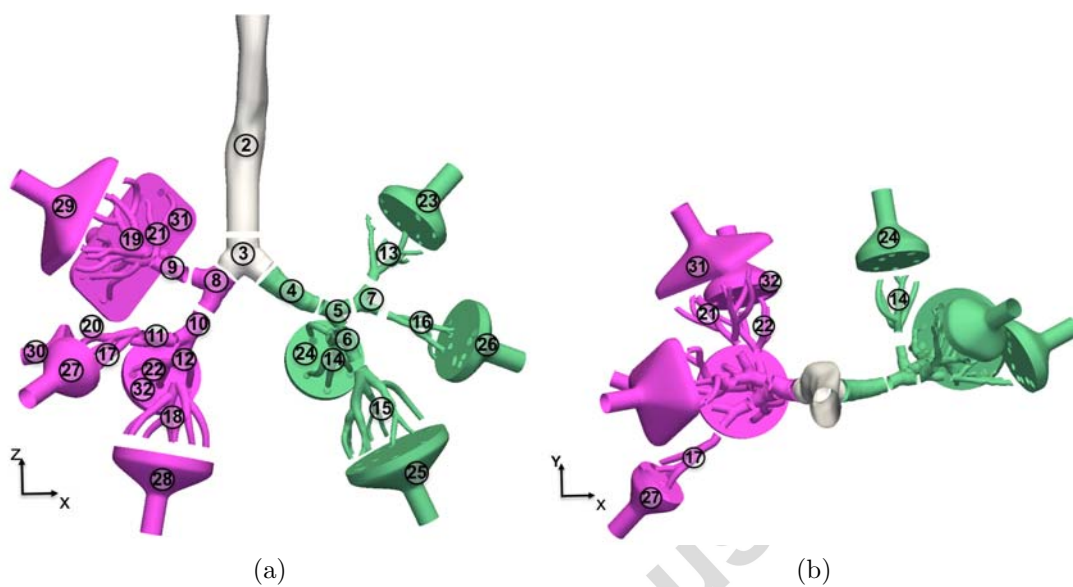


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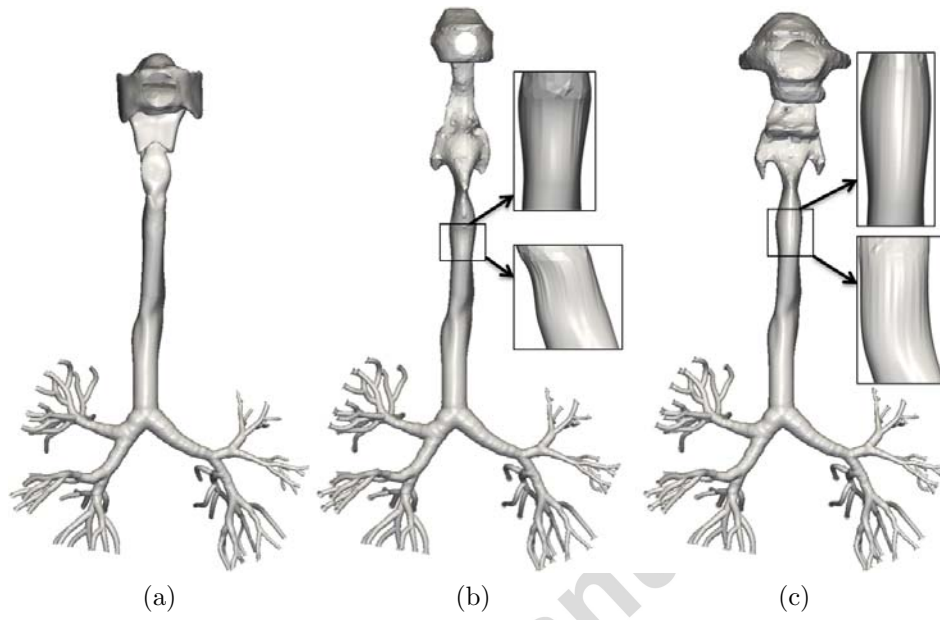


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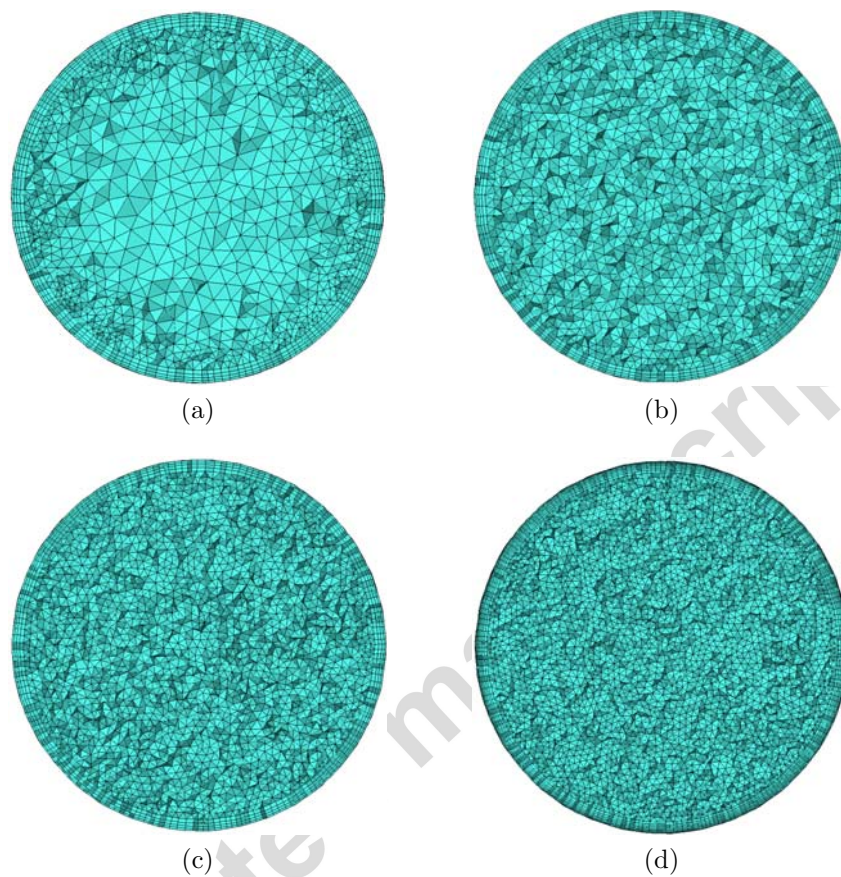


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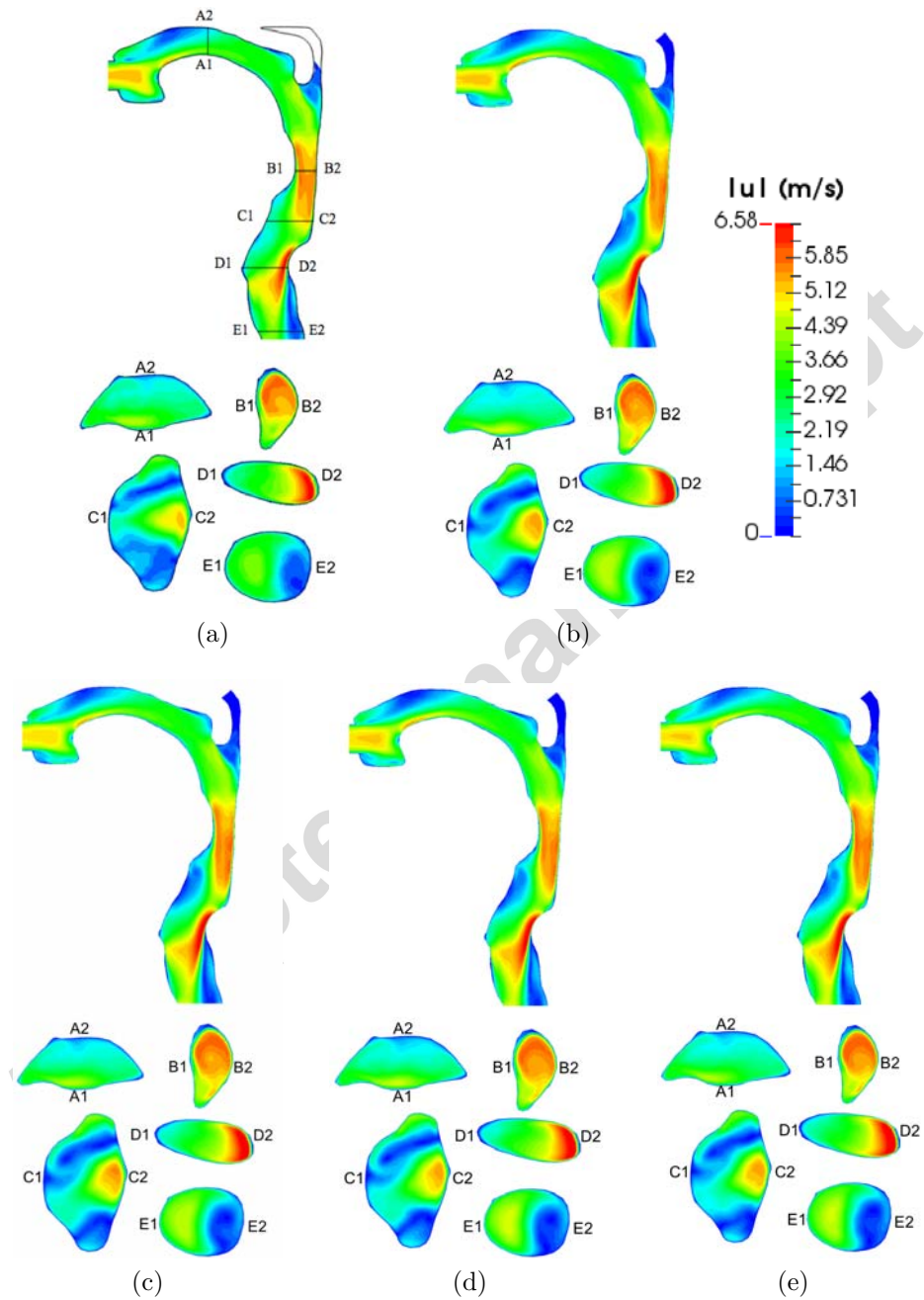


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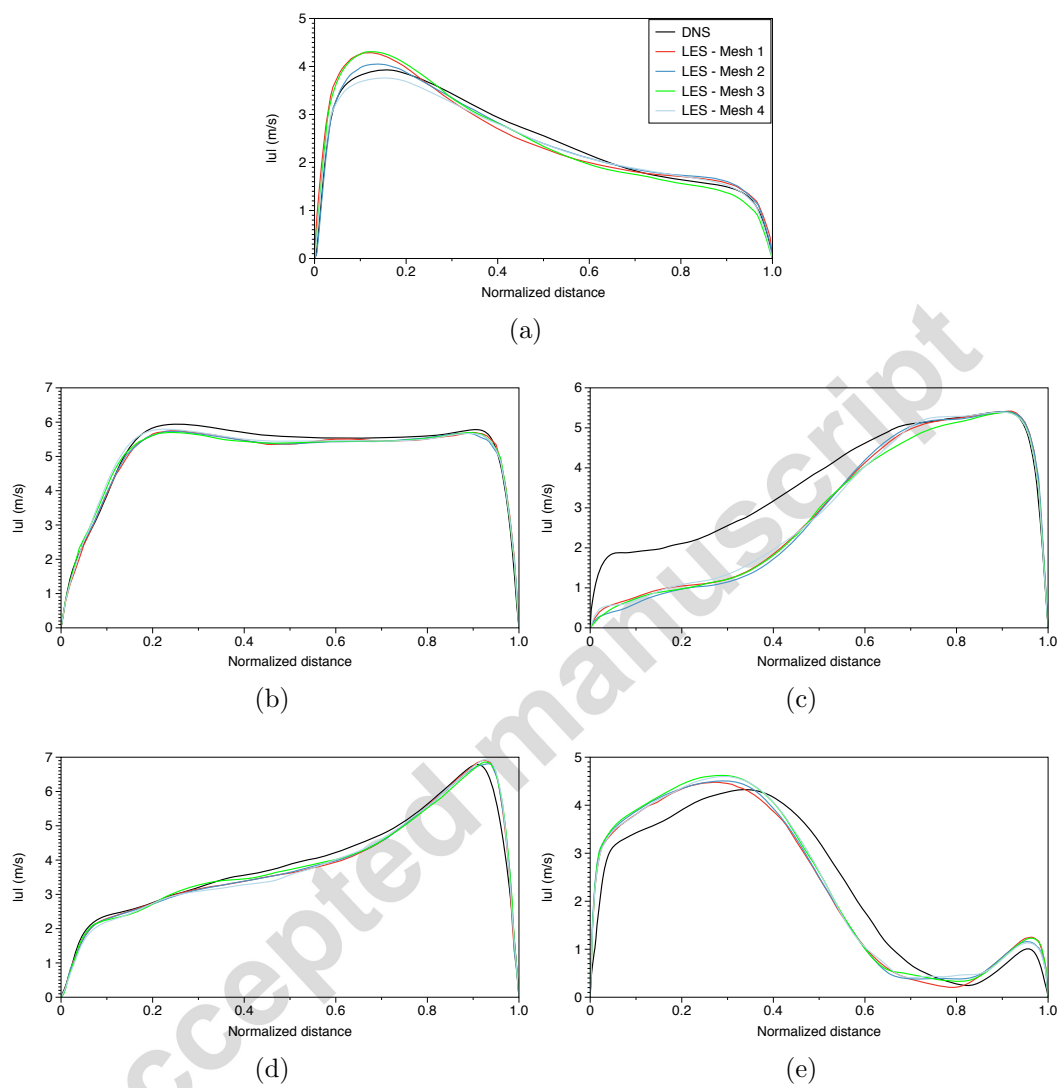


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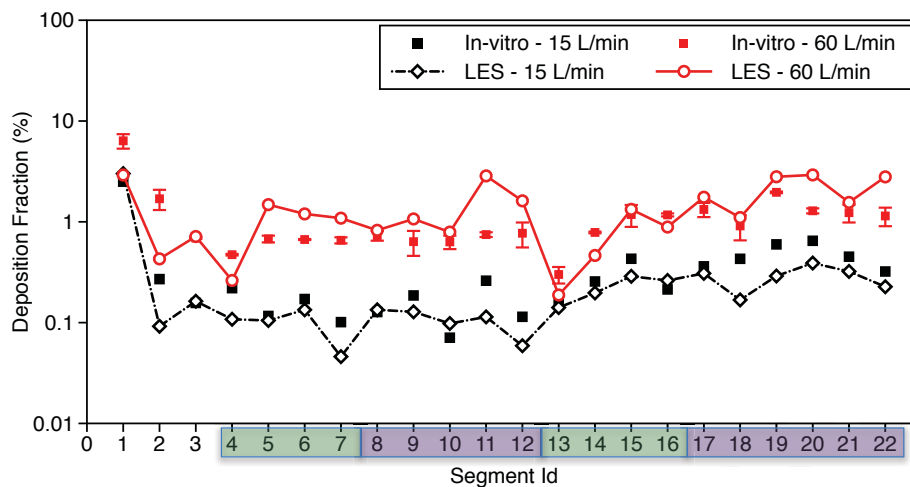


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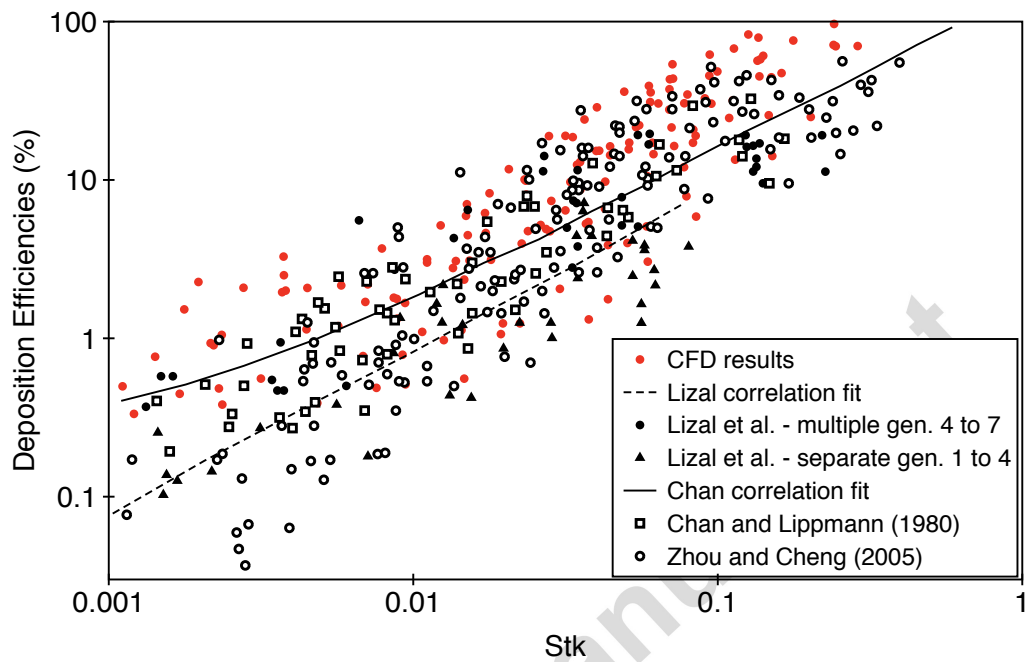
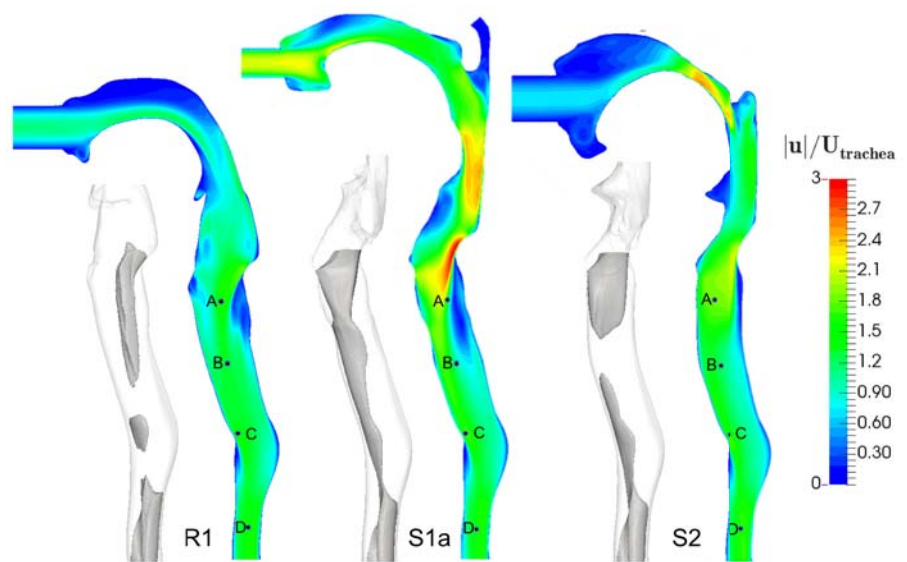
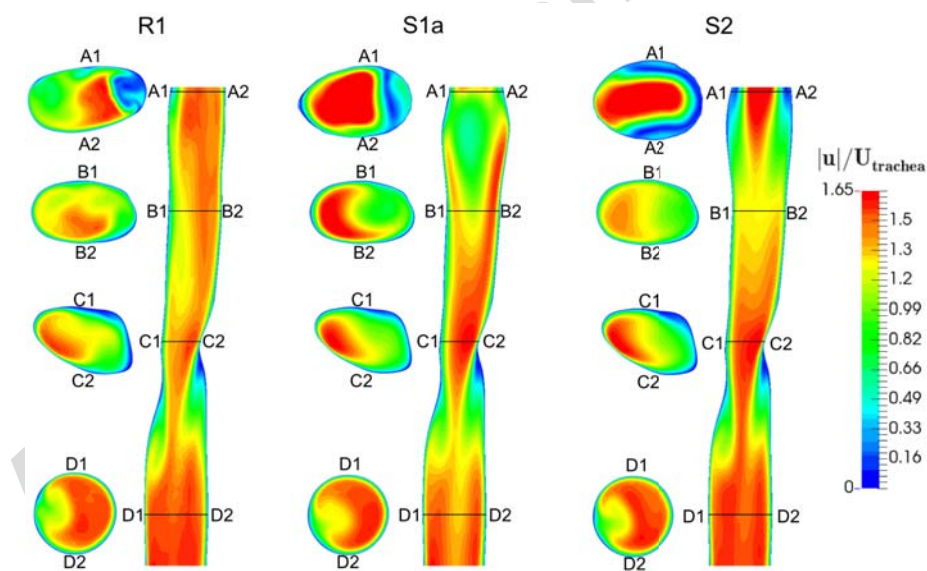


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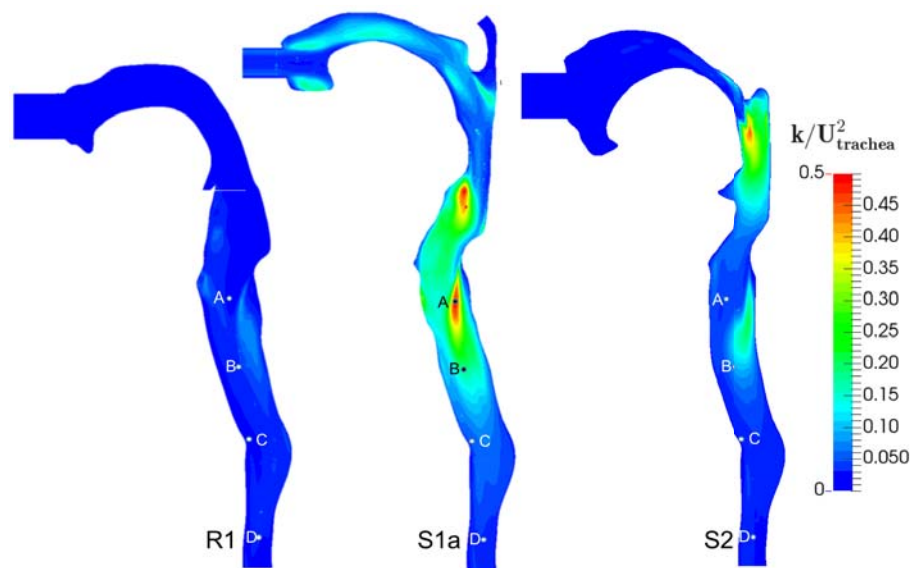


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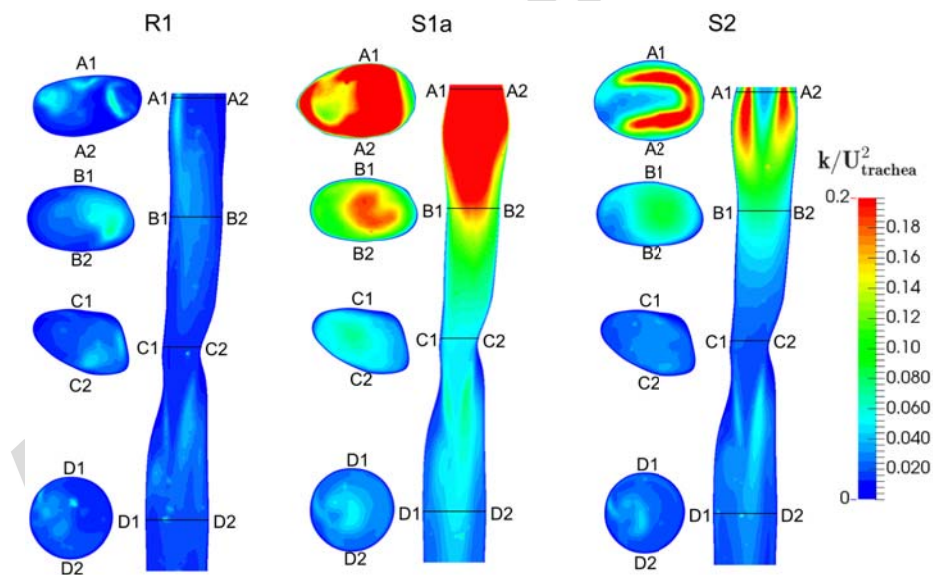


(b)

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(a)



(b)

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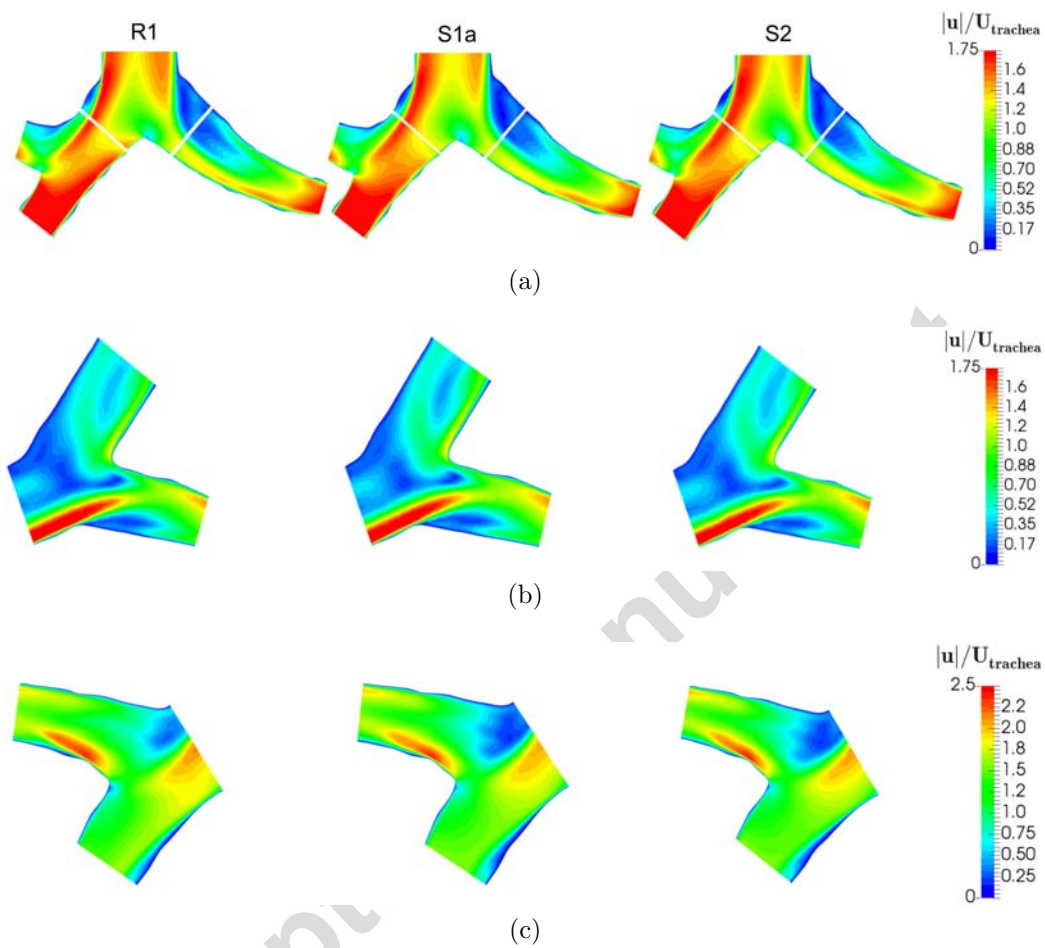


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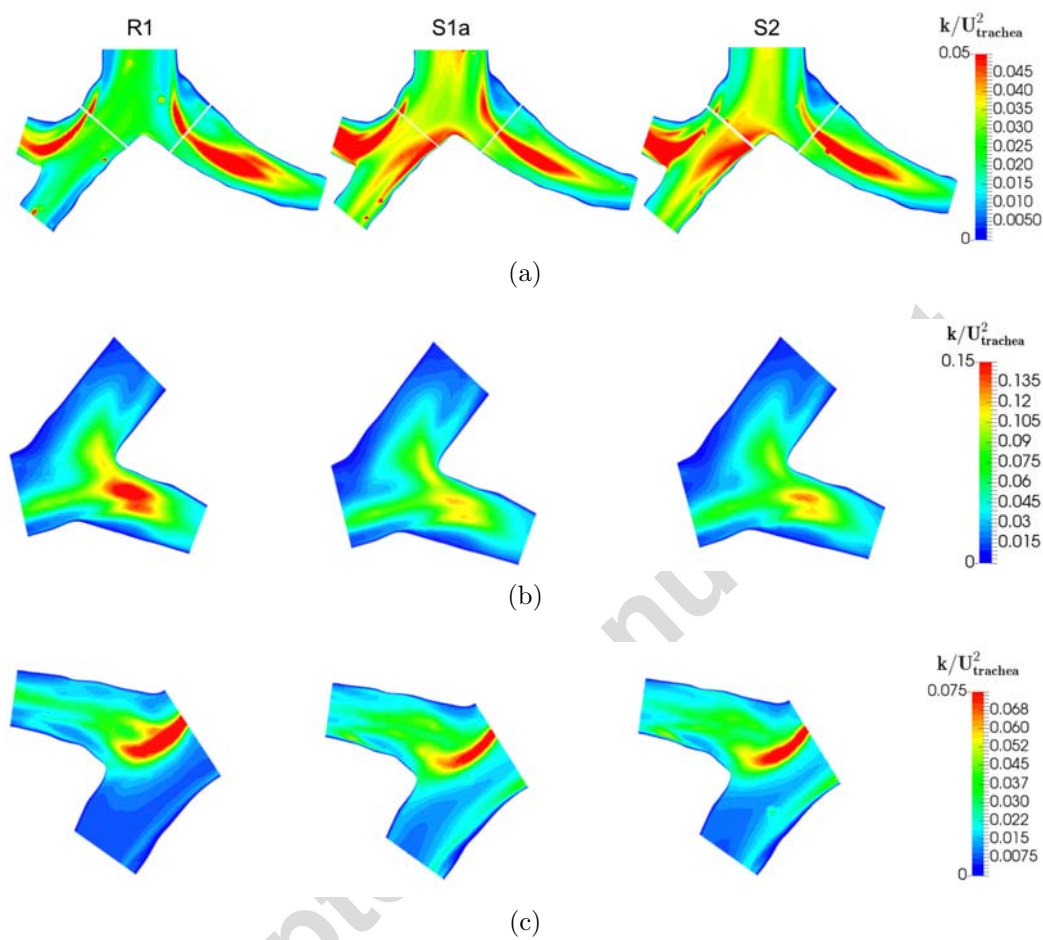


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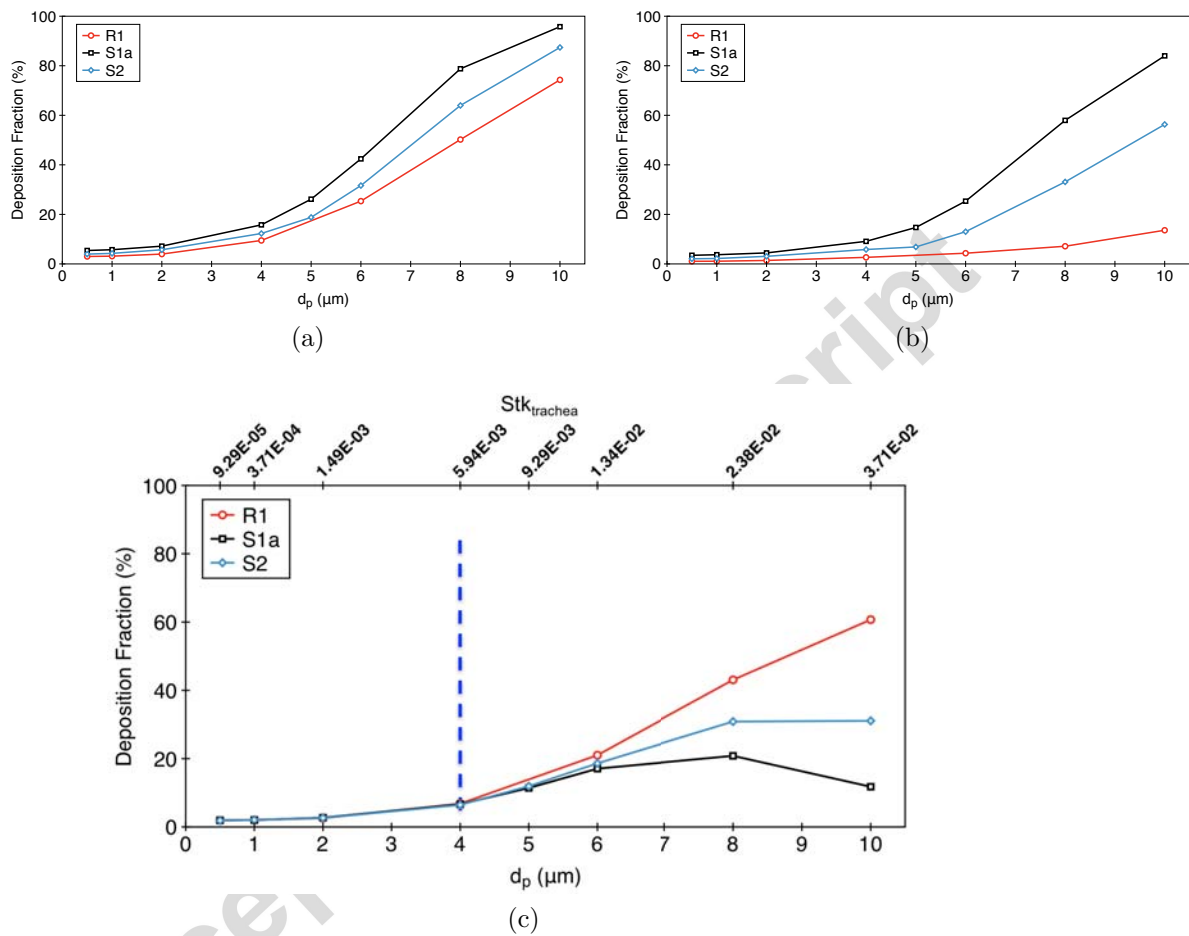


Figure 13: Deposition fractions versus particle size at  $Q = 30 \text{ L/min}$ : (a) overall; (b) mouth and throat; and (c) tracheobronchial. In (c), the Stokes numbers based on tracheal parameters are also displayed.



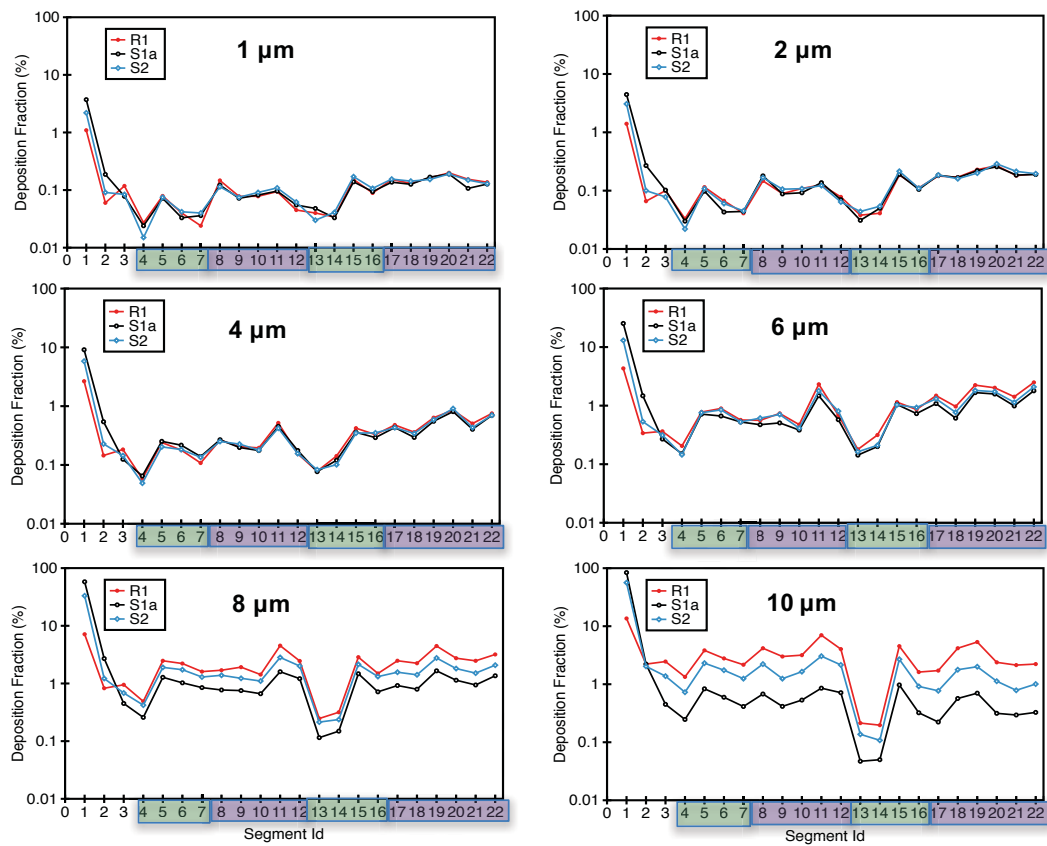


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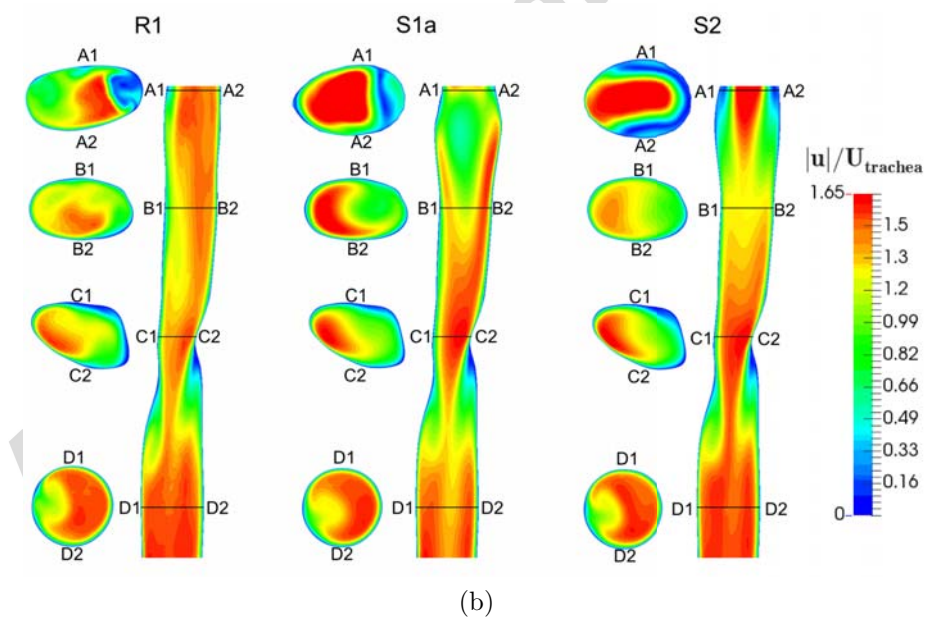
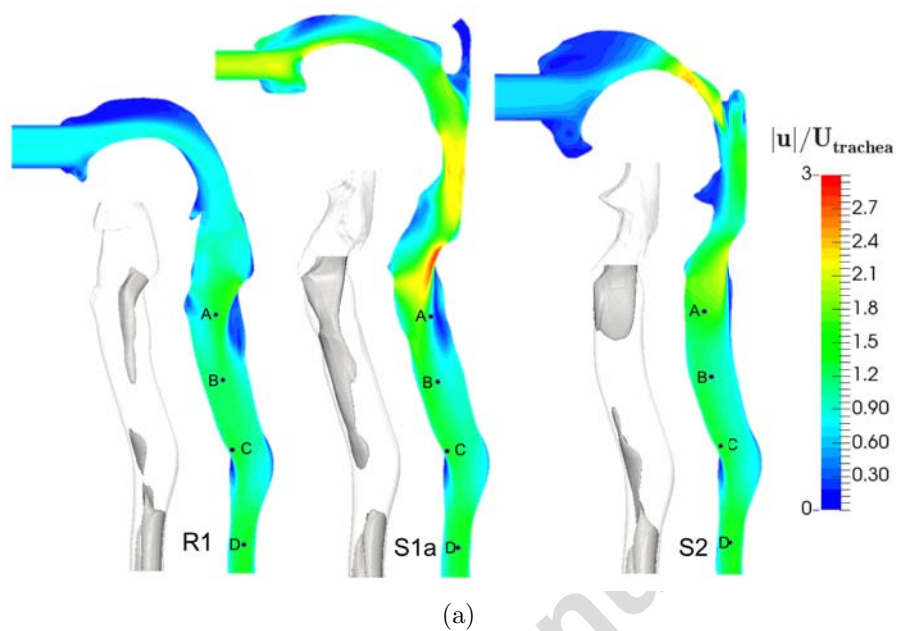
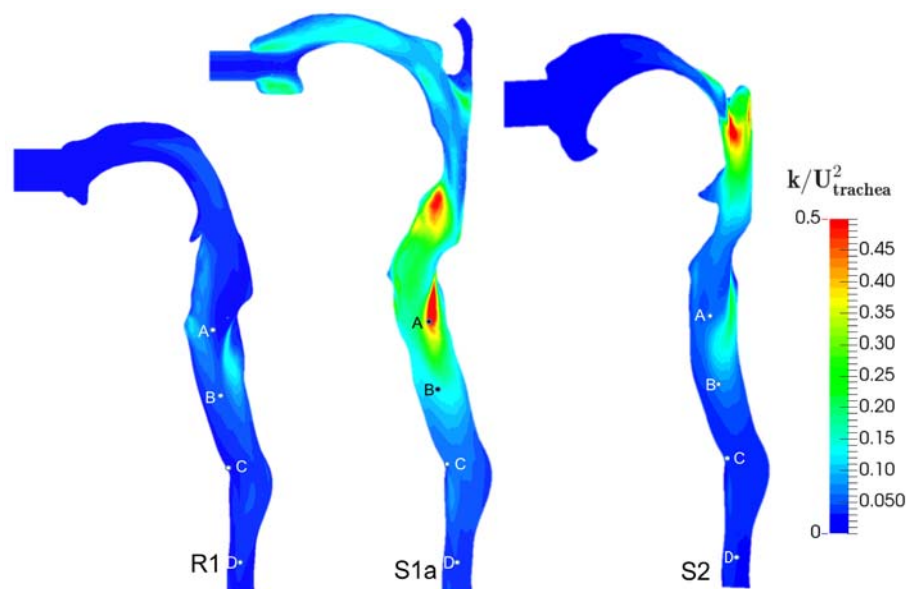
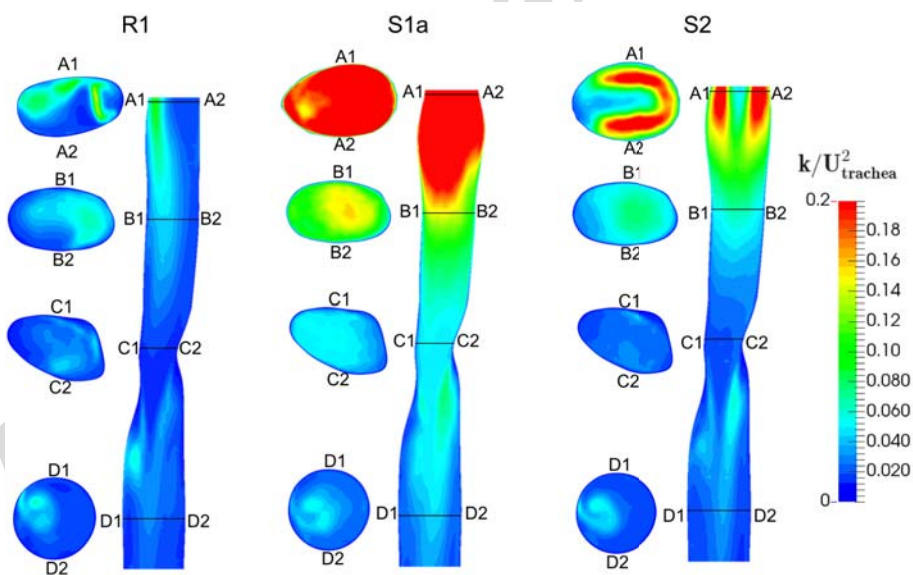


Figure 15: Contours of normalized mean velocity magnitude in (a) the mouth-throat region (side view), and (b) the trachea (top and front views) at  $Q = 60 L/min$ . In (a) isosurfaces of  $|u|/U_{trachea} = 1.35$  are shown.



(a)



(b)

Figure 16: Contours of normalized turbulent kinetic energy in (a) the mouth-throat region (side view), and (b) the trachea (top and front views) at  $Q = 60 L/min$ .

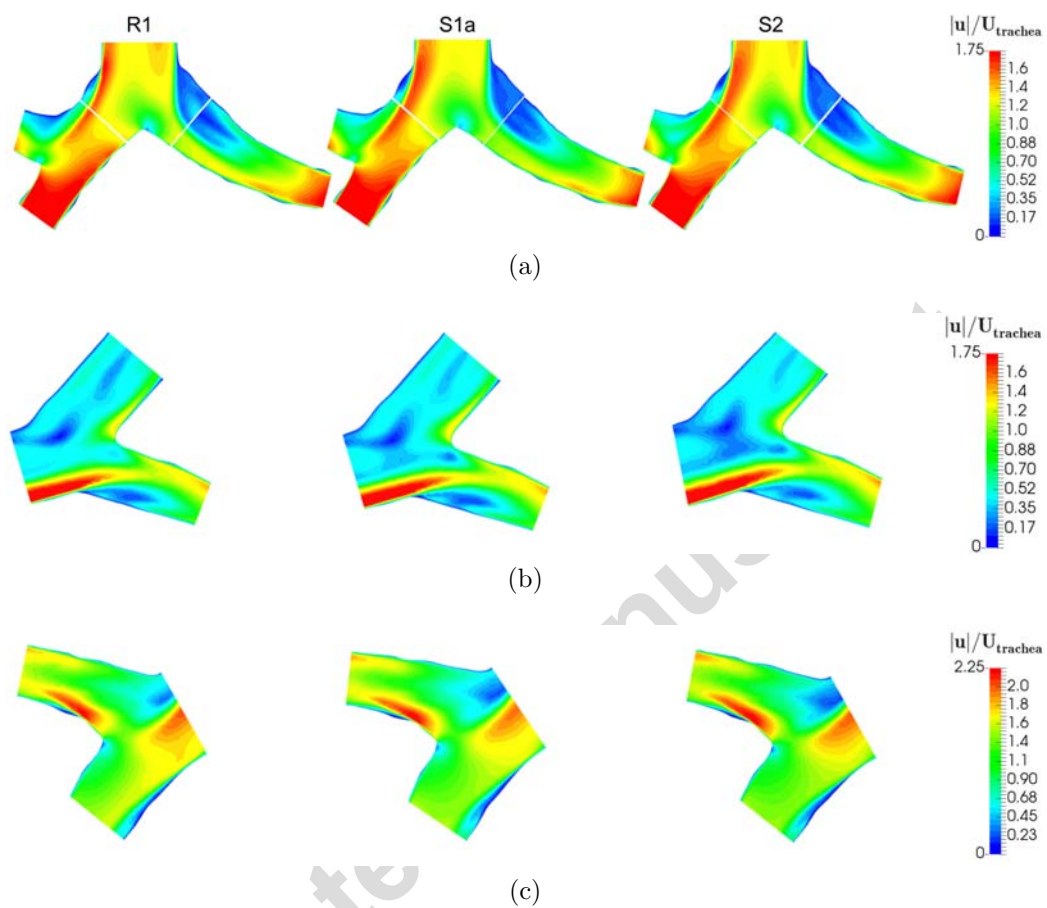


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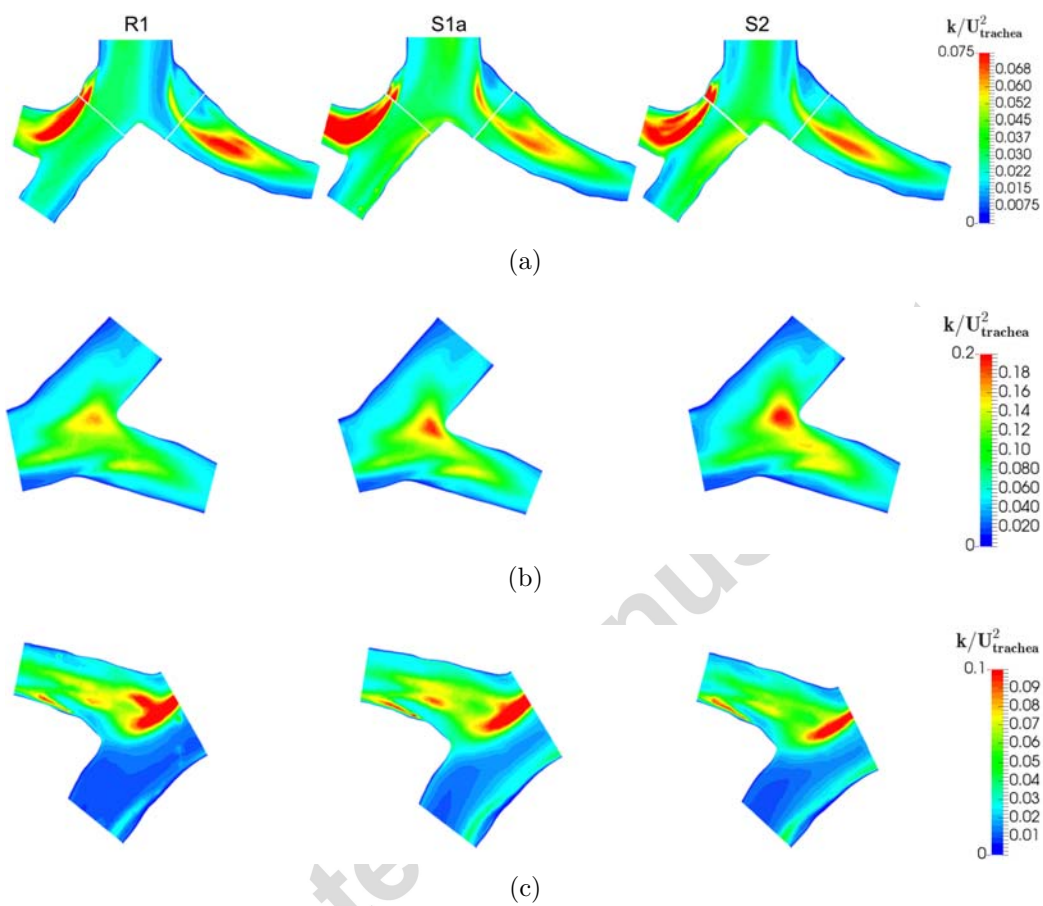


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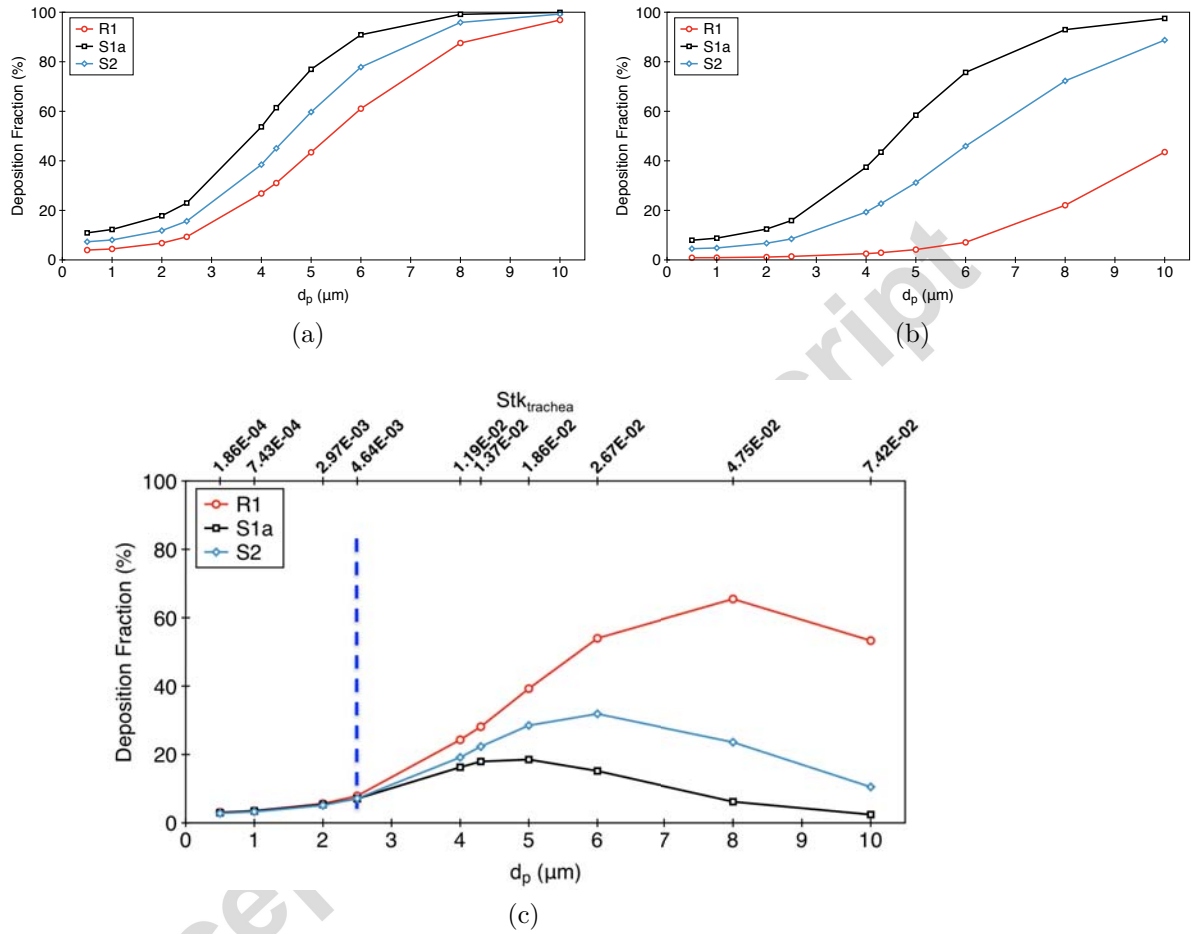


Figure 19: Deposition fractions versus particle size at  $Q = 60 L/min$ : (a) overall; (b) mouth and throat; and (c) tracheobronchial. In (c), the Stokes numbers based on tracheal parameters are also displayed.

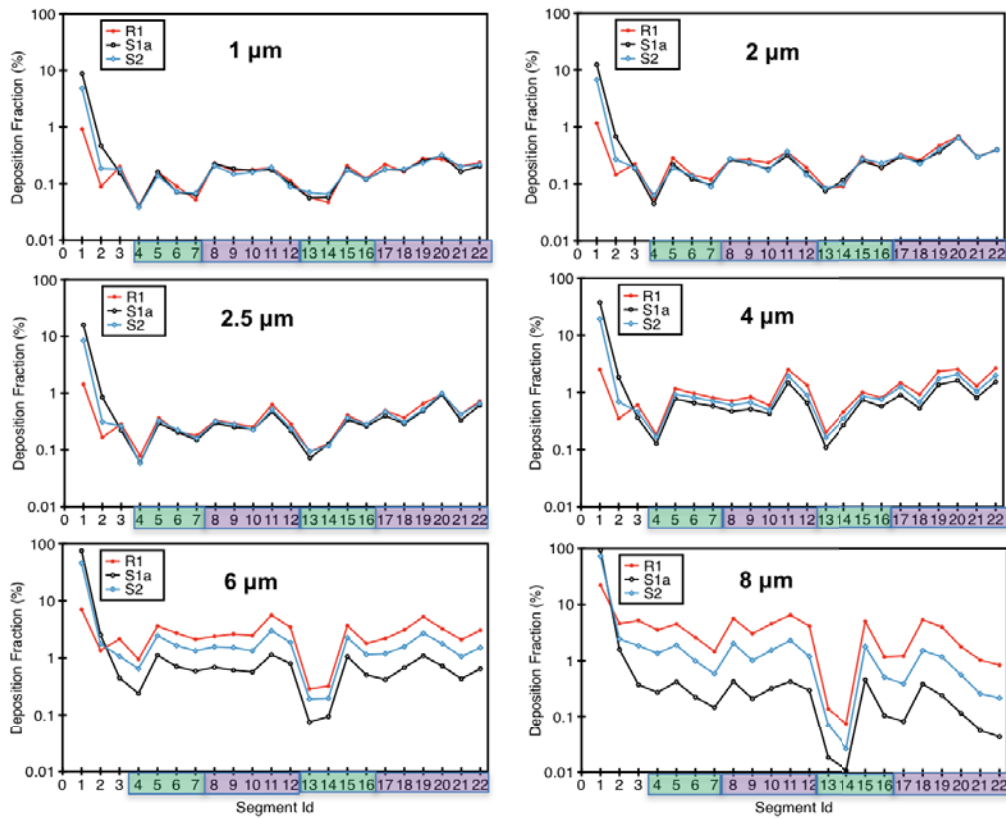


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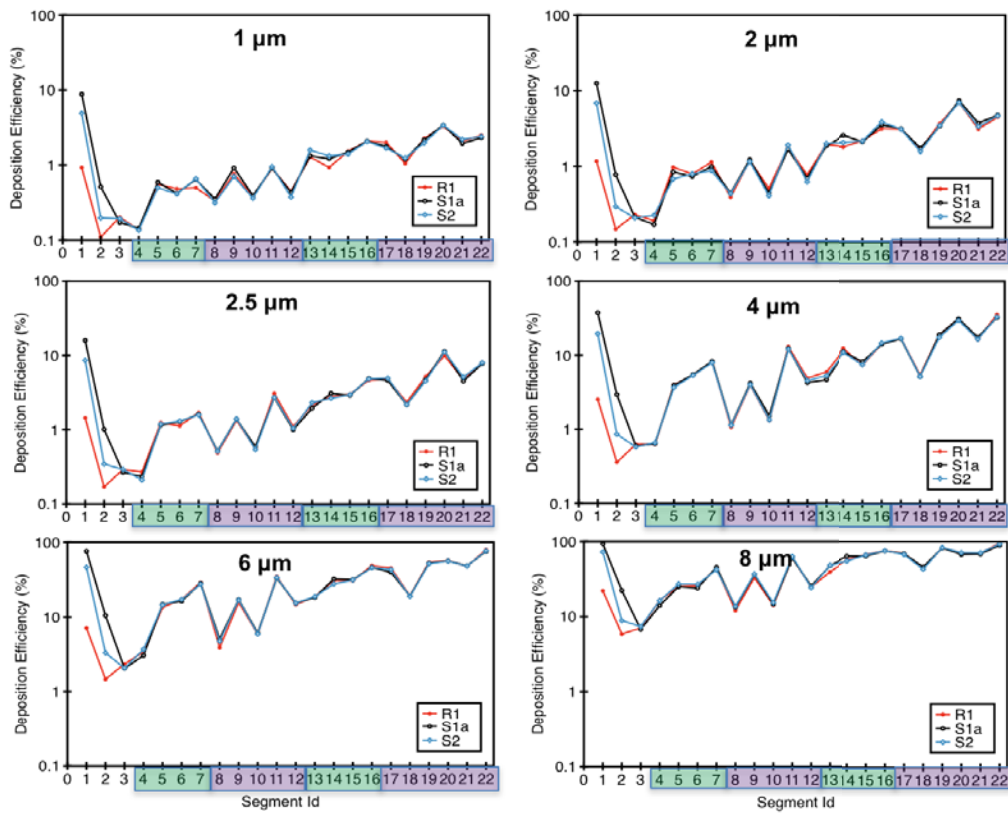


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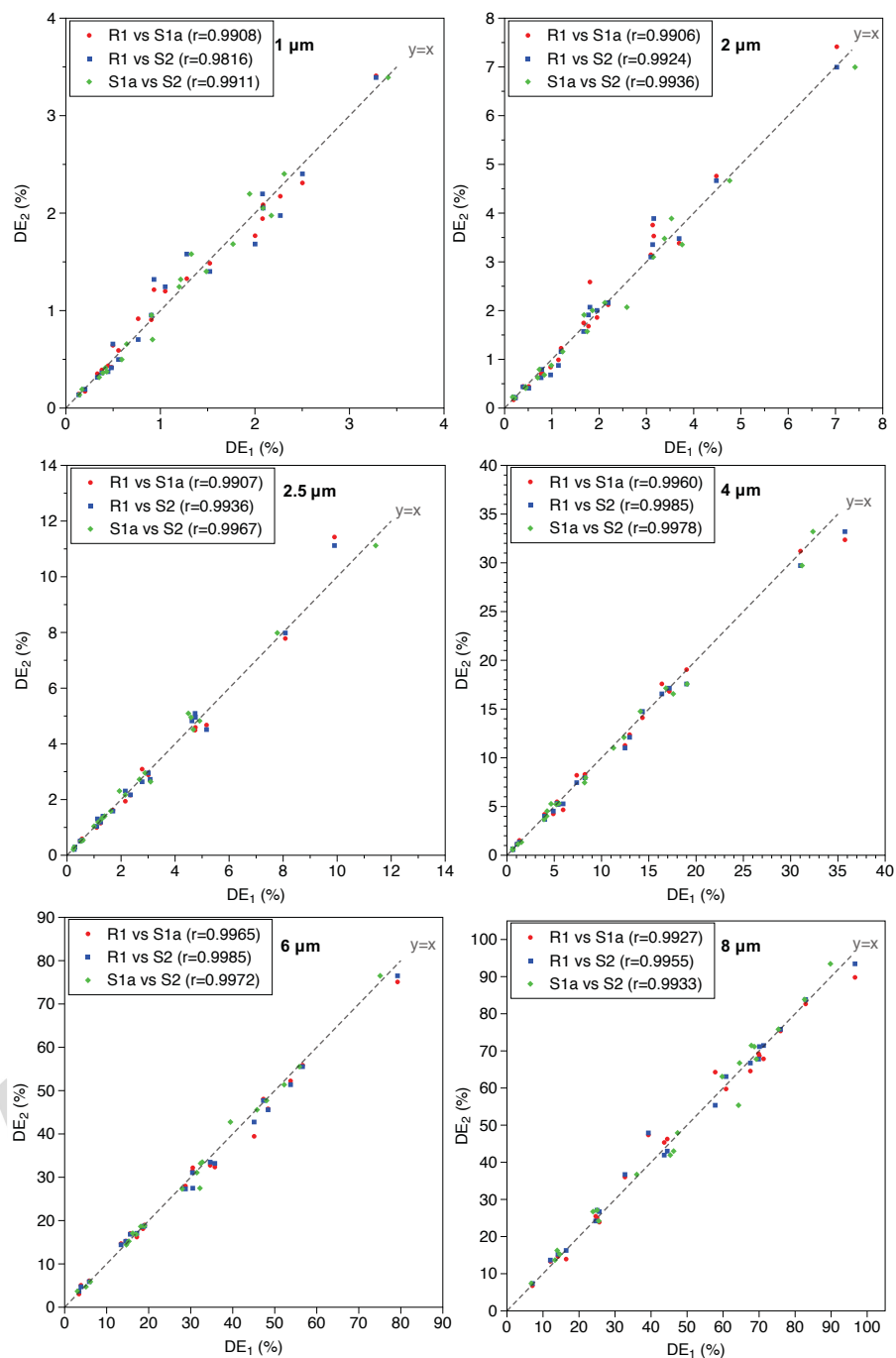


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Mouth-throat model	R1	S1a	S2
$D_{\text{inlet}}$ (cm)	2	1.3	2.3
Volume (cm <sup>3</sup> )	69.25	51.56	81.73
Length (cm)	15.86	19.1	18.6
$D_{\text{mean}}$ (cm)	2.36	1.85	2.37
$A_{\text{glottis}}/A_{\text{trachea}}$	0.716	0.456	0.492

Table 1: Dimensions of the mouth-throat geometries.

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Mouth-throat model	R1	S1a	S2
$Q(L/min)$	30 / 60	30 / 60	30 / 60
$U_{inlet}$ (m/s)	1.59 / 3.18	3.77 / 7.54	1.2 / 2.4
$U_{trachea}$ (m/s)	2.4 / 4.8	2.4 / 4.8	2.4 / 4.8
$Re_{inlet}$	1871 / 3742	2883 / 5766	1628 / 3256
$Re_{trachea}$	2300 / 5600	2300 / 5600	2300 / 5600

Table 2: Mean velocity and Reynolds number at the inlet and the trachea for the three geometries at the two flowrates examined.

Mesh	1	2	3	4
$\Delta r_{min}(mm)$	0.081	0.065	0.065	0.022
Prism layers	4	4	4	8
$\lambda$	1.22	1.22	1.22	1.22
Comp. cells ( $\times 10^6$ )	7	12	24	42
$V_{cell,avg.}(mm^3)$	0.01	0.0063	0.0032	0.0018
Max $y^+$	3.27	3.73	3.76	1.48
Avg. $y^+$	0.88	0.73	0.71	0.24

Table 3: Characteristics of Meshes 1-4 generated for the preliminary tests in the S1a mouth-throat geometry.  $\Delta r_{min}$  is the initial cell height,  $\lambda$  the average expansion ratio of the prism layers and  $V_{cell,avg.}$  the average cell volume in the domain.