Zagreb International Review of Economics & Business, Vol. 10, No. 2, pp. 95-105, 2007 SHORT ARTICLE © 2007 Economics Faculty Zagreb All rights reserved. Printed in Croatia ISSN 1331-5609; UDC: 33+65

Project Investment Decision-Making

Domen Zavrl*

Abstract: Project evaluation is the control of the planning and implementation of project activities with regard to the objectives to be achieved. In this paper we assume the objective to be efficient outcome and profit maximization. This means that project evaluation puts normative assessments into the context of planning and management and hence into the context of intentional action and cycles of action. The model for project evaluation we propose has two money holders who must decide how to invest their money in two investment funds (financial intermediaries) that, in turn, will use the money to bid to acquire ownership in two projects. The general case when the number of money holders, the number of funds, and the number of investments are arbitrary may be handled in a similar manner to the development below, but at a cost of greater complexity. As a result no mechanism to achieve the maximum outcome is present and different methods to find optimal structure under uncertainty and different cost structures are discussed.

Keywords: project evaluation, profit maximization, uncertainty, coordination failure

JEL Classification: G31

Introduction

The model for project evaluationwepropose has two money holders who must decide how to invest their money in two investment funds that, in turn, will use the money to bid to acquire ownership in two projects. Importantly, the profitability of each project depends on the specific joint ownership structure that results from the money which each MIF receives, as the funds are assumed to have different management capabilities.

We start by assuming that N > 0 money points are owned by the population which consists of two individuals, I_1 and I_2 . Money holder I_1 , l = 1, 2, has $V_1 > 0$ money points where $V_1 + V_2 = N$. The number of money points held by each individual may

^{*} Domen Zavrl is at University of Primorska, Koper, Slovenia.

differ to allow the possibility of pre-auction trading. Each I_i must decide independently on the number of money points to invest in each of two money funds, $F_j j = 1,2$. The number of money points that I_i , chooses to allocate to F_1 is denoted by $x, x \in [0, V_1]$ with the remaining $V_1 - x$ money points being allocated to F_2 .

Similarly,we denote by $y, y \in [0, V_2]$, the money points investment of I_1 in F_2 , with $V_2 - y$ being invested in F_2 . As a consequence of investing its money points in this manner I_1 acquires the proportion $\frac{x}{x+y}$ of the profit of F_1 , and $\frac{V_1 - x}{(V_1 - x) + (V_2 - y)}$ of the profit of F_2 . Correspondingly, I_2 acquires the proportion $\frac{y}{x+y}$ of the profit of F_1 and $\frac{V_2 - y}{(V_1 - x) + (V_2 - y)}$ of the profit of F_2 . The general case when the number of money holders, the number of funds, and the number of

when the number of money holders, the number of funds, and the number of investments are arbitrary may be handled in a similar manner to the development below, but at a cost of greater complexity.

At the outset, neither F_j has any money. In order to attract money from the I_1 , each F_j reveals information useful to the I_1 . We assume that this information relates to the cost structure of the F_j . Specifically,weassume that each F_j announces that its costs will be a fixed proportion of the revenues it will earn by investing the money points that it will acquire. This assumption is equivalent to the assumption that the profit of the F_j is equal to $\sigma_j R_j (x + y)$ where σ_j is constant, $\sigma_j \in [0,1]$, j = 1, 2, and $R_j: \Re_+ \to \Re_+$ is the revenue received by F_j as a result of the bidding game in which, using money points acquired from the I_1 , F_1 and F_2 , compete to acquire share in the projects offered for financing. The σ_j can be thought of as the proportion of revenue that the F_j promise to distribute to the share holders. $R_1(x + y)$ depends on x + y since this is the number of money points available to F_1 for investment in projects. Similarly, $R_2(x + y)$ has the same dependence since the total number of money points, N, is fixed.

Thus I_1 , receives m_1 : where $\Re^2 \to \Re_+$

$$m_1(x,y) = \frac{x}{x+y} \sigma_1 R_1(x+y) + \frac{V_1 - x}{(V_1 - x) + (V_2 - y)} \sigma_2 R_2(x+y)$$

Thus I_2 , receives m_2 : where $\Re^2 \to \Re_+$

$$m_2(x,y) = \frac{y}{x+y}\sigma_1 R_1(x+y) + \frac{V_2 - y}{(V_1 - x) + (V_2 - y)}\sigma_2 R_2(x+y)$$

 I_1 chooses x to maximize m_1 and I_2 chooses y to maximize m_2 . We refer to the problem of simultaneously maximizing m_1 and m_2 as the money investment problem (MIP). In what follows, we take x and y to be continuous over their respective ranges.

The $R_j(x+y)$ are determined by the following process. With $N_1 = x + y$ and $N_2 = N - N_1$ respectively, F_1 and F_2 play a non-cooperative game in which they submit bids to acquire shares in company *i*, we = 1,2. Each F_j submits a money point bid of a_{ij} in company where $a_{ij} \ge 0$ and $\sum_i a_{ij} = N_j$. As a consequence of the bidding, each F_j receives the proportion of $p_{ij} = \frac{a_{ij}}{\sum_i a_{ij}}$ of π_i , the profit of project

i.weassume that the $\pi_i: \Re^2_+ \to \Re_+$, we = 1, 2, depend on $p_{ij}, j = 1, 2$, that is, weassume that the F_j have different skills in managing and restructuring the projects in which they have acquired share, and that the impact of their skills on the profit of a given project depends on the proportion of ownership that they achieve in the project as a result of the bidding game.

Furthermore, we assume, for tractability, that the profit functions $\pi_i(p_{i1}, p_{i2})$ can be reasonably approximated by a first-order Taylor expansion. It follows, since $p_{i1} + p_{i1} = 1$ for we = 1, 2, that:

$$\pi_{1}(p_{11}, p_{12} = \pi_{1}(0, 1) + p_{11} \left[\frac{\partial \pi_{1}(0, 1)}{\partial p_{11}} - \frac{\partial \pi_{1}(0, 1)}{\partial p_{12}} \right]$$

$$\pi_{2}(p_{21}, p_{22}) = \pi_{2}(1, 0) + p_{22} \left[\frac{\partial \pi_{2}(1, 0)}{\partial p_{22}} - \frac{\partial \pi_{2}(1, 0)}{\partial p_{21}} \right]$$

In the remainder of the paper we use the notation $k_{12} = \pi_1(0,1); k_{21} = \pi_2(1,0);$

$$\Delta_1 = \frac{\partial \pi_1(0,1)}{\partial p_{11}} - \frac{\partial \pi_1(0,1)}{\partial p_{1,2}}; \Delta_2 = \frac{\partial \pi_2(1,0)}{\partial p_{22}} - \frac{\partial \pi_2(1,0)}{\partial p_{21}}; \text{ and } r_i = \frac{\Delta_i}{k_{ij}} \text{ for } j \neq i.$$

In summary, we assume that the profit function can be written as;

$$\pi_i = k_{ij} + p_{ii}\Delta_i = k_{ij}(1 + p_{ii}r_i)$$
 for $i \neq j, i, j = 1, 2$

The parameter k_{12} represents the profit that project 1 would make if it were totally purchased by F_2 . The parameter k_{21} has a similar interpretation. The parameter Δ_1 represents the difference in the differential advantage (disadvantage) that F_1 has over F_2 , in managing project 1. The parameter Δ_2 has a similar interpretation. Thus, π_1 is modeled as the sum of the value that would occur if F_2 were to manage project 1 exclusively plus the improvement, (deterioration) when ownership is shared with F_1 . The profit π_2 has a similar interpretation. Notice that if F_1 , and F_2 , have the same differential impact on π_1 , the value of the profit function would be the same regardless of how ownership were shared. We note that since the p_{ii} depend on x + y, the π_i depend on x + y also. For subsequent use, we define $\pi_i(z) = k_{ij} + z\Delta_i$. Thus, after having submitted their bids, F_i receives the revenue $p_{1i}\pi_1(p_{11}) + p_{2i}\pi_2(p_{22})$.

The revenue accruing to F_j at the Nash equilibrium of the bidding game is what we call $R_j(N_1)$ and thus the profit available for distribution to the I_j by F_j is where $N_1 = x + y$.

We assume that both I_i share the same information set concerning the projects and skill levels, as well as the reasoning and characteristics of the F_j . Since the $R_j(N_1)$, the results of the bidding game between the F_j , are required by the I_i to solve their problem, we investigate this bidding game first.

The Money Fund Problem

We now formalize the non-cooperative bidding game played by the F_j . Given N_1 and N_2 , and given the bids of F_j , $j' \neq j$, F_j must choose its bids to maximize its profit. Since, by earlier assumption, its profit is a fixed multiple of its revenue, F_j 's bids must satisfy

$$\max_{a_{1j},a_{2j}}\sum_{i}p_{ij}\pi_{i}(p_{ii})$$

subject to $a_{ij} \ge 0$ and $\sum_{i} a_{ij} = N_{j}$ and where $p_{ij} = \frac{a_{ij}}{\sum_{j} a_{ij}}$. I refer to these programs as the money fund problem (VFP).

The Lagrangian for F_1 is:

$$L_{1} = p_{11}\pi_{1}(p_{11}) + p_{21}\pi_{2}(p_{22}) - \lambda_{1}(a_{11} + a_{21} - N_{1})$$

with first-order conditions:

$$\frac{\partial L_1}{\partial a_{11}} = 0 = \frac{(1 - p_{11})}{a_{1\bullet}} \pi_1 + p_{11} \frac{(1 - p_{11})}{a_{1\bullet}} \Delta_1 - \lambda_1 = \frac{(1 - p_{11})}{a_{1\bullet}} (\pi_1 + p_{11}\Delta_1) - \lambda_1 \quad (1)$$

$$\frac{\partial L_1}{\partial a_{21}} = 0 = \frac{(1 - p_{21})}{a_{2\bullet}} \pi_2 - p_{21} \frac{p_{22}}{a_{2\bullet}} \Delta_2 - \lambda_1 = \frac{p_{22}}{a_{2\bullet}} (\pi_2 - \Delta_2 + p_{22}\Delta_2) - \lambda_1$$
(2)

$$\frac{\partial L_1}{\partial \lambda_1} = 0 = a_{11} + a_{21} - N_1$$
where
$$a_{i\bullet} = \sum_j a_{ij}$$
(3)

Similarly, the Lagrangian for F_2 is:

$$L_{2} = p_{12}\pi_{1}(p_{11}) + p_{22}\pi_{2}(p_{22}) - \lambda_{2}(a_{12} + a_{22} - N_{2})$$

with first-order conditions:

$$\frac{\partial L_2}{\partial a_{12}} = 0 = \frac{(1 - p_{12})}{a_{1\bullet}} \pi_1 - p_{12} \frac{p_{11}}{a_{1\bullet}} \Delta_1 - \lambda_2 = \frac{p_{11}}{a_{1\bullet}} (\pi_1 - \Delta_1 + p_{11}\Delta_1) - \lambda_2$$
(4)

$$\frac{\partial L_2}{\partial a_{22}} = 0 = \frac{(1 - p_{22})}{a_{2\bullet}} \pi_2 - p_{22} \frac{(1 - p_{22})}{a_{2\bullet}} \Delta_2 - \lambda_2 = \frac{(1 - p_{22})}{a_{2\bullet}} (\pi_2 + p_{22}\Delta_2) - \lambda_2$$
(5)
$$\frac{\partial L_2}{\partial \lambda_2} = 0 = a_{12} + a_{22} - N_2$$
(6)

Before presenting the solution to the VFP, we provide the following lemma. Recall that

$$r_i = \frac{\Delta_i}{k_{ij}}$$
 and $\pi_i(z) = k_{ij} + z\Delta_i$.

Lemma 1

Let $k_{ij} > 0$ for $i \neq j$ and let $r_i \in (-1,1]$. For any $\alpha \in [0,1]$, there exists a unique set of values $z_1^*, z_2^*, \Theta^* \in [0,1]$ that simultaneously satisfy.

$$(i) 1 - z_{1} = \Theta \frac{1 + r_{1} z_{1}}{1 + 2r_{1} z_{1}}$$

$$(ii) 1 - z_{2} = (1 - \Theta) \frac{1 + r_{2} z_{2}}{1 + 2r_{2} z_{2}}$$

$$(iii) z_{1} \pi_{1}(z_{1}) + (1 - z_{2}) \pi_{2}(z_{2}) = \alpha \left[\pi_{1}(z_{1}) + \pi_{2}(z_{2})\right]$$

Theorem 1

When $k_{ij} > 0$ for $i \neq j$, and when $r_i \in (-1,1]$, there exists a Nash equilibrium of the VFP and it is unique. In particular, let z_1^* , z_2^* , and Θ^* be the solutions to the equations of lemma 1 corresponding to $\alpha = N_1/N$. Then, under the stated conditions, the

unique solution to equations (1)-(6), i.e., the Nash equilibrium of the VFP for i, j = 1,2 and $j \neq i$ is:

$$a_{ii}^{*} = K^{-1} z_{i}^{*} \pi_{i}(z_{i}^{*}), \quad a_{ij}^{*} = K^{-1} (1 - z_{i}^{*}) \pi_{i}(z_{i}^{*}), \quad \lambda_{1} = K\Theta^{*}, \quad \lambda_{2} = K(1 - \Theta^{*})$$

here $K = \frac{\pi_{1}(z_{1}^{*}) + \pi_{2}(z_{2}^{*})}{N}$

It is useful to highlight a result established in the proof of Theorem 1 signifying the proportion of each project owned by each fund.wedo this in the next corollary. In what follows, an asterisk above any function denotes that function evaluated at the solution to the VFP presented in Theorem 1.

Corollary 1

The solution to the VFP yields $p_{ii}^* = z_i^*$.

Interpreting $\pi_i^*/a_{i_{\bullet}}^*$ as the resulting value per money in project *I*, Theorem 1 establishes that these values are the same for both projects at the Nash equilibrium of the bidding game. Furthermore, this common value is equal to the economy-wide value of a money given by $(\pi_1^* + \pi_2^*)/N$. This common value of a money is also equal to the sum of the two shadow prices that is denoted by *K* in Theorem 1. An additional money to the system, yielding approximately the value *K*, would be divided between F_1 and F_2 in the amounts λ_1 and λ_2 . Thus, F_1 , would receive Θ^* percent of this additional amount, and F_2 the remainder, $1-\Theta^*$ where Θ^* incorporates, among other things, the relative skill levels of F_1 and F_2 .

At the Nash equilibrium, a total of $K^{-1}\pi_j^* = N(\pi_j^*/(\pi_1^* + \pi_2^*))$ money points are invested in project j, j = 1, 2, with F_j contributing z_j^* percent of these money points.wecan interpret this total either as the part of the outstanding number of money points acquired by company j being proportional to π_j^* , or as the profit of project jdenominated in units of economy-wide value per money. Although the money investment in projectwedepends on π_j^* , this profit cannot be known in advance since it depends on the composition of ownership resulting from the bidding game itself. Finally, the ratio $a_{ii}^*/a_{ij}^* = p_{ii}^*/p_{ij}^* = z_i^*/(1 - z_i^*)$, $j \neq i$ depends on all the parameters of the problem including the skill levels of the F_j . We next establish the revenue that receives as a consequence of the solution to the VFP. Let $\prod_{i=1}^{\infty} \pi_i^* + \pi_2^*$.

Corollary 2

At the Nash equilibrium of the VFP, the revenue to F_i is equal to $(N_i/N) \prod^*$.

W

The solution to the VPF yields each F_j the proportion N_j/N of the sum of the profits produced by projects 1 and 2 at the Nash solution. This establishes that $R_j(N_1) = (N_j/N) \prod^*$ and that profit equals $\sigma_j(N_j/N) \prod^*$. It also follows that at the Nash equilibrium, the revenue per money for each of the F_j is identical. We can now return to the problem facing the I_j , the original money holders.

The Money Investment Problem

For the money investment problem (MIP) in which I_i wishes to maximize m_1 , I_i must know $R_1(x + y)$ and $R_2(x + y)$. From Corollary 2 and the remarks following it, $R_j = p_{1j}^* \pi_1^* + p_{2j}^* \pi_2^* = (N_j/N) \prod^*$ where $\prod^* = \pi_1^* + \pi_2^*$. Having assumed that each I_i has the same information concerning the bidding game played by F_1 and F_2 conditional on the funds having $N_1 = x + y$ money points, and $N_2 = N - N_1$ money points, respectively, it follows that each I_i also knows the Nash equilibrium of the VFP as presented in Theorem 1. Consequently, the respective objective functions of the I_i can be restated as:

$$m_{1}(x,y) = \frac{x}{x+y}\sigma_{1}\frac{N_{1}}{N}\Pi^{*} + \frac{V_{1}-x}{(V_{1}-x)+(V_{2}-y)}\sigma_{2}\frac{N_{2}}{N}\Pi^{*}$$

and

$$m_{2}(x,y) = \frac{y}{x+y}\sigma_{1}\frac{N_{1}}{N}\prod^{*} + \frac{V_{2}-y}{(V_{1}-x)+(V_{2}-y)}\sigma_{2}\frac{N_{2}}{N}\prod^{*}$$

Since $N_1 = x + y$ and $N_2 = N - N_1$, the last expressions can be reduced to:

$$m_1(x,y) = \left[\sigma_1 \frac{x}{N} + \sigma_2 \frac{V_1 - x}{N}\right] \prod^* (x+y)$$

and

$$m_2(x,y) = \left[\sigma_1 \frac{y}{N} + \sigma_2 \frac{V_2 - y}{N}\right] \prod^* (x+y)$$

Thus, in the money investment problem (MIP), investor I_1 seeks where

$$x^* = \underset{x \in [0, V_1]}{\operatorname{arg max}} m_1(x, y) \text{ subject to } y \in [0, V_2]$$

and investor I_2 , seeks where

$$y^* = \underset{y \in [0, V_2]}{\operatorname{arg\,max}} m_2(x, y) \text{ subject to } x \in [0, V_1]$$

We next define an efficient allocation of money points. Let $N_1^* = \arg \max_{N_1 \in [0, N]} \prod^* (N_1)$. Note that N_1^* is an apportionment of money points to the VPFs that achieves the maximum total profit.

Definition 1

An allocation of money points $(x, y), x \in [0, V_1], y \in [0, V_2]$, is an efficient allocation if $x + y = N_1^*$.

The case when $\sigma_1 = \sigma_2 = \sigma$. We continue by investigating the case in which the F_j pay out the same proportion of their revenues to the I_i ; that is the case when $\sigma_1 = \sigma_2 = \sigma$. In this situation, $m_1 = \sigma(V_1/N) \prod^* (x+y)$. Since increasing $\prod^* (x+y)$ benefits both I_i it is in their joint interest to achieve the largest possible by their respective money investments. It follows that it is in the interest of the I_i to choose their investments to be efficient. It also follows that there exists an infinity of equilibria to the VIP of the form (x^*, y^*) where $x^* = N_1^* - y^*$ for $x^* \in [0, V_2]$ and for $y^* \in [0, V_2]$. We summarize the previous remarks in the following theorem.

Theorem 2

When $\sigma_1 = \sigma_2 = \sigma$ there exists an infinity of equilibria to the MIP consisting of the set of efficient allocations.

But despite the fact that the I_i find it in their interest to have $x^* + y^* = N_1^*$, the non-cooperative nature of the Nash game offers no mechanism to cause the target N_1^* to be met. Since the target represents the division of the total number of money points in the system between the F_j that maximizes economy-wide profit, there is consequently no mechanism to achieve this efficient outcome. Thus, the failure to achieve efficiency is the result of the absence of coordination between the money holders.

Notice that this coordination failure is present even in the case in which the money point holders have identical and full information, and have as their goal the wish to allocate their money points in a manner consistent with the maximization of economy-wide profit.wenow show that the introduction of uncertainty exacerbates the situation since it creates a situation in which the goal of the money holders is no longer one of maximizing total economy-wide profit; in fact, we show that the goal differs for the different money point holders. When uncertainty is present, we must consider the investors' attitudes toward risk. To this end, we let $u_1: \mathfrak{R}_+ \to \mathfrak{R}_+$ with $u_1(m_1) = 1 - \exp(-\gamma_1 m_1), \gamma_1 > 0$ be the utility function of I_1 . We assume that all information is known to the money point holders as before, with one exception: Δ_1 is known imperfectly. We assume that both money point holders perceive $\widetilde{\Delta}_1$ as a random variable, distributed normally with mean Δ_1 (as before) and variance σ^2 . We denote this density as $\phi(\Delta_1, \sigma^2)$. It follows that $\widetilde{\Pi}^*$ is random since $\widetilde{\Pi}^* = k_{12} + k_{21} + p_{11}\Delta_1 + p_{22}\Delta_2$. The expectation of any function of $\widetilde{\Delta}_1$ with respect to ϕ is denoted by E_{ϕ} . Thus $E_{\phi}\widetilde{\Pi}^* = \Pi^*$ with Π^* as before. Let $N_1^*(\phi) = \max_{N_1} E_{\phi}\Pi^* = \max_{N_1} \Pi^*(N_1)$. We define Assumption A to be made up of the following statements:

 I_i has utility function $u_i(m_i) = 1 - \exp(-\gamma_i m_i), \gamma_i > 0;$ I_i is a von Neumann-Morgenstern expected utility of wealth maximizer; $\sigma_1 = \sigma_2 = \sigma;$ $\tilde{\Delta}_1$ is distributed as $\phi(\Delta_1, \sigma^2)$; All other information is known with certainty; Both I_i have the same information; and The funds F_j are risk-neutral.

In what follows, we let N_{11} be the target of I_1 and N_{12} be the target of I_2 .

Theorem 3

In the presence of uncertainty about the difference in the differential impact of the funds' skills on the profit of company 1, and if F_1 , is expected, but uncertain, to be more skilled than F_2 in managing company 1, then risk-averse money holders allocate fewer money points to F_2 compared to the certainty case, and more money points to resulting in an inefficient allocation of money points among the funds. In particular, let Assumption A hold. Let $\gamma_1 V_1 \neq \gamma_2 V_2$, $\Delta_1 > 0$ and $N_1^*(\phi) \in (0, N)$. Then there exists a constant c such that for $\sigma^2 \in (0, c)$, $N_{11} \neq N_{12}$, $N_{11} < N_1^*(\phi)$ and $N_{12} < N_1^*(\phi)$.

We see from Theorem 3 that the immediate impact or the introduction of uncertainty regarding the relative skills of the funds on the profit of company 1 causes a shifting of money points away from F_1 . As a consequence, even if $N_1^*(\phi)$ were close to N, F_2 would receive more money points as the uncertainty increases. Earlier we showed that when $\sigma_1 = \sigma_2$ and when all information was known with certainty, each I_1 strove to achieve the target N_1^* , which, if achieved, would maximize the money holders' respective wealths as well as implement the efficient outcome. That is, the money holders were aiming at the right target; a coordination

failure, however, prevented them from achieving it. This suggested that had a coordination mechanism existed, the efficient allocation would have been implemented. Now, with the introduction of uncertainty into the model, we see that the target at which the I_i aim is not the optimal value $N_1^*(\phi)$ and the I_i may have different targets, both unequal to $N_1^*(\phi)$. Coordination would not resolve this inefficiency. Though we introduced uncertainty only in regard to Δ_1 , any broader introduction of uncertainty would have further exacerbated the problem. It is not surprising that the introduction of uncertainty results in a sub-optimal solution. However, wenext show that even with certainty and with complete information, when the payouts of the funds to the differ, inefficiency also results.

The case when $\sigma_1 \neq \sigma_2$. We have assumed so far that the F_j have identical cost structures. Generally, however, since the F_j are not identical, they could have different cost structures, leading them to select different percentages of their revenues to pay out, that is, $\sigma_1 \neq \sigma_2$. When $\sigma_1 \neq \sigma_2$, it is no longer true that the I_i will both benefit by seeking to maximize Π^* since the share of Π^* that I_i receives depends, in this case, on the investments x^* and y^* . Importantly, for the case $\sigma_1 \neq \sigma_2$, the optimal choices of x^* and y^* by I_1 , and I_2 , respectively, need not always produce a division of the money points consistent with the maximization of economy-wide profit. We show these results to be true in Theorem 4, where we present the solution to the VIP when $\sigma_1 \neq \sigma_2$. To make this point as starkly as possible, we let .

Theorem 4

Even with certainty and even if the money holders start with the same number of money points, when the payouts of the funds differ, the unique Nash equilibrium of the VIP leads to a common inefficient target. In particular, let $\sigma_1 \neq \sigma_2$, $V_1 = V_2 = V$ and let

$$G(N_1) = \Pi^*(N_1) + \frac{N}{2} \left(\frac{N_1}{N} + \frac{\sigma_2}{\sigma_1 - \sigma_2} \right) \frac{d\Pi^*(N_1)}{dN_1} \text{ for } N_1 \in (0, N).$$

Then the unique Nash equilibrium of the VIP is:

$$x^* = y^* = \frac{N_1^{\circ}}{2},$$

where either $N_1^{\circ} \in (0, N)$ and satisfies $G(N_1^{\circ}) = 0$ or $N_1^{\circ} = 0$ or N. If $\Delta_j \neq 0$ for at least one value of j and $N_1^{\circ} \in (0, N)$, then $N_1^{\circ} \neq N_1^{*}$.

When payouts are different, each I_1 will invest $N_1^{\circ}/2$ in F_1 , yielding a total of N_1° money points to F_1 . Since $N_1^{\circ} \neq N_1^{*}$, N_1° will not be the efficient allocation of money points to F_1 , and thus will not maximize total economy-wide profit. Additionally, whereas a coordination failure between the I_1 is responsible for inefficient outcomes when $\sigma_1 = \sigma_2$, even permitting coordination when $\sigma_1 \neq \sigma_2$ would not result in an efficient outcome. That is, when $\sigma_1 \neq \sigma_2$, the goal of the money holders is not the goal of maximizing total economy-wide profit, as it was for the case when $\sigma_1 = \sigma_2$.

SELECTED READINGS

- Alchian, A., Demsetz, H., (1972), Production, Information Costs, and Economic Organization. American Economic Review 62, 777-805.
- Bekaert G. and C. R. Harvey (2000), 'Foreign Speculators and Emerging Equity Markets, Journal of Finance, 55, 565-614.
- Boardman, A.E. and A.R. Vining (1989). "Ownership and Performance in Competitive Environments: A Comparison of Private, Mixed and Competitive Enterprises", Journal of Law and Economics, Vol. 32, April pp. 1-33.
- Carlin, W., J. van Reenen and T. Wolfe (1995): Enterprise Restructuring and Dynamism in Transition Economies, Economics of Transition 3, p. 427-458.
- Carlin, Wendy, John Van Reenen and Toby Wolfe (1995), 'Enterprise Restructuring in Early Transition: The Case Study Evidence from Central and Eastern Europe,' Economics of Transition, 3, 4, 427-58.
- Djankov, S. (1999a): Ownership Structure and Enterprise Restructuring in Six Newly Independent States, Comparative Economic Studies 41, p. 75-95.
- Djankov, S. (1999b): The restructuring of insider-dominated banks: A Comparative Analysis, Economics of Transition 7, p. 467-480.
- Freeman, R.E. and W.M. Evan (1990): Corporate Governance: A Stakeholder Interpretation, Journal of Behavioural Economics 19, p. 337-359.
- Friedman A.L. and S. Miles (2002): Developing Stakeholder Theory, Journal of Management Studies 39, p. 1-21.
- Frooman, J. (1999): Stakeholder Influence Strategies, Academy of Management Review 24, p. 191-202.
- Jones, T.M. and A.C. Wicks (1999): Convergent Stakeholder Theory, Academy of Management Review 24, p. 206-221.
- La Porta, R., Lopez-de-Silanes, F., Shleifer, A., Vishny, R., 1997. Legal Determinants of External Finance. Journal of Finance 52, 1131-1150.
- Mitchell, R.K., B.R. Agle and D.J. Wood (1997): Toward a Theory of Stakeholder Identification and Salience: Defining the Principle of Who and What really counts, Academy of Management Review 22, p. 853-886.