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Staging superstructures in high- T_c Sr/O codoped La_{2-x}Sr_xCuO_{4+y}

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We present high-energy x-ray diffraction studies on the structural phases of an optimal high- T_c superconductor $\text{La}_{2-x}\text{Sr}_x\text{CuO}_{4+y}$ tailored by co-hole-doping. This is specifically done by varying the content of two very different chemical species, Sr and O, respectively, in order to study the influence of each. A superstructure known as staging is observed in all samples, with the staging number n increasing for higher Sr dopings x. We find that the staging phases emerge abruptly with temperature, and can be described as a second-order phase transition with transition temperatures slightly depending on the Sr doping. The Sr appears to correlate the interstitial oxygen in a way that stabilizes the reproducibility of the staging phase both in terms of staging period and volume fraction in a specific sample. The structural details as investigated in this paper appear to have no direct bearing on the electronic phase separation previously observed in the same samples. This provides evidence that the electronic phase separation is determined by the overall hole concentration rather than specific Sr/O content and concomitant structural details.

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I. INTRODUCTION

The rich phase diagram of the superconducting cuprates continues to motivate new investigations for the mechanism behind high- T_c superconductivity in these materials [1–8]. In samples where hole doping is performed by chemical substitution of La for Sr to give La_{2-x}Sr_xCuO₄, it is well known that the details of the superconducting and magnetic phases strongly depend on x. Evidence for electronic phase separation, which can possibly be explained by the formation of percolative hole networks [9,10], has been given in samples which are instead hole doped with oxygen to give $La_2CuO_{4+\nu}$. The details depend on y, but one electronic phase is a bulk superconductor with discrete T_c in the range 30–45 K, while the other is an antiferromagnetic phase which is commensurate for y < 0.055 and modulated with $\delta \sim 0.10$ –0.13 for higher dopings [10–13]. A range of superstructures measurable by diffraction techniques form as a consequence of oxygen intercalation. In highly oxygenated La₂CuO_{4+v}, the details and spatial distribution of the superstructures as well as T_c [14,15] and the strength of the modulated antiferromagnetic signal [16] depend strongly on the cooling rate. It would thus be practical to study other systems which are electronically similar when at low-temperature equilibrium, but which can be reached at natural cooling rates. This is a major motivation for this study.

In setting the stage for the work in this paper, we recap important findings in the isostructural compound La_2NiO_{4+y} , where the intercalated oxygen density tends to modulate along the c axis in a superstructure known as staging [17]. The superstructure is characterized by a number n referring to

the periodicity of the intercalated oxygen layers in terms of NiO_6 spacings. A similar superstructure has been observed in La_2CuO_{4+y} [18,19], and in both compounds the staging number is expected to decrease with increased oxygen concentration along with smaller shifts associated with increased quenching temperature [16,18,20]. An illustration of this superstructure is shown in Figs. 1(a)–1(c).

In order to study the role of the mobile versus localized dopants, we have prepared single crystals of $\text{La}_{2-x}\text{Sr}_x\text{CuO}_{4+y}$, hole doped to a level of $0.125 \leqslant n_h \leqslant 0.16$ by a combination of Sr chemical substitution and intercalation of O [21]. We have previously investigated the superconducting and magnetic properties and found that a unique superconducting phase and a unique stripelike magnetic phase is present in all Sr/O codoped samples with remarkably coinciding transition temperatures $T_c \approx T_N \approx 40$ K regardless of x [21,22]. See Supplemental Material [23] for an estimate of the oxygen contents.

In this work, we investigate the structural impacts of this co-hole-doping by combining Sr substitution for La and intercalation of oxygen. We find that each of the investigated samples exhibit staging, or hints of staging.

II. METHODS

The samples studied in this work are the same single crystals with Sr doping x = 0.00, 0.04, 0.065, and 0.09 as first studied in Ref. [21]. The x = 0.00 crystal was grown in a crucible, while the others were grown by the traveling solvent floating zone method in an optical furnace. The crystals were electrochemically oxidized through electrolysis in a NaOH solution bath [18].

X-ray scattering data presented in this work were performed at the high-energy x-ray (100 keV) triple-axis diffractometer BW5 [24] at the now decommissioned DORIS III storage ring

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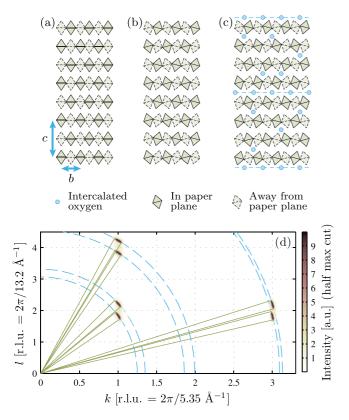


FIG. 1. Illustration of relevant structures, with only CuO_6 octahedra and interstitial oxygen shown. (a) Tetragonal F4/mmm and (b) orthorhombic Bmab structures of $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$ seen along the a axis. (c) Example of a staged structure caused by layers of favorable positions for interstitial oxygen due to tilt flip domain borders. Figure inspired by [13,17,18]. (d) Map of investigations of the [0KL] plane for the x=0.04 sample at $T=10\,\text{K}$, close to Bmab allowed positions (012), (014), and (032). The intensity of each pair of peaks has been scaled for visibility. Blue dashed arcs are centered in origo, showing how the resolution function is widest transverse to q. Green lines mark out the FWHM of the long axis for each peak.

at DESY, Germany. The beam size for this instrument at the sample position was between 1×1 and 2×2 mm², while the used samples had typical dimensions of 1 to 5 mm. In all experiments, the crystals were cooled with <2 K/min unless specifically stated otherwise. The slow cooling rate should allow reproducible ordering of the intercalated oxygen [16].

Throughout this work, the Miller indices refer to the orthorhombic Bmab notation (a < b < c, a and b in the range 5.3–5.4 Å and c in the range 13.0–13.2 Å for our samples), also in the tetragonal state above the transition temperature where the unit cell is described in the space group F4/mmm (where the more conventional setting is I4/mmm).

III. RESULTS

We have mapped areas of the [0KL] plane close to *Bmab* allowed positions in a Sr/O codoped crystal with x = 0.04 by sample rotation scans, as shown in Fig. 1(d). Superstructure peaks are observed with positions corresponding to a modulated structure along the c axis in a similar manner as the staging in $\text{La}_2\text{NiO}_{4+y}$. The observed superstructure peaks are

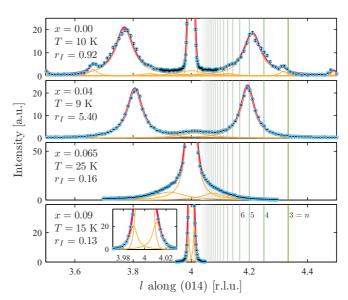


FIG. 2. Low-temperature data for the four samples. The plots for the x=0.00, 0.065, and 0.09 samples are cut off from the maximum intensities of 101.4, 196.5, and 196.9, respectively, to show the staging peaks. The inset plot in the bottom panel shows a zoom for clarity. Black lines indicate error bars, and are in general smaller than the data symbols. Red thick curves show full fits of the spectra, composed of the sum of individual peaks (thin orange curves) and a flat background. Vertical green lines indicate integer n staging. The relative intensity r_I is calculated from the integrated intensities as given in Eq. (2).

broadened transverse to the scattering vector, along the dashed arcs, with FWHM between 1.4° and 3.4° , and specifically $2.25(5)^{\circ}$ for the staging peak pairs close to (014). For comparison, the transverse spread of the close-by fundamental Bragg reflection (004) is FWHM = 0.3° , which means the transverse broadening is intrinsic to the superstructures. Along the scattering vector of the superstructure peak, the FWHM is between 0.25 and 0.34 Å $^{-1}$, which is much more than the FWHM = 0.009 Å $^{-1}$ of close-by (004). This means that the distribution of unit-cell lengths in the staged volume of the sample is broader than for the unstaged volume. This is also reflected in the noninteger values and distribution width of the staging period values discussed below.

In order to identify and characterize the superstructures as function of Sr content, further measurements were done by scans along l through the Bmab allowed reflection (014) in the four samples. Figure 2 shows examples of these scans at low temperatures for each of the samples. In all samples, a peak at the Bmab allowed position (014) is observed. In order to analyze the data further, we relate the reciprocal distance from the (014) position Δl to the staging number n by

$$n = \frac{1}{\Delta l}. (1)$$

For the x = 0.00 sample, several individual staging peaks were observed on both sides of the central Bmab position. The largest peaks correspond to a staging number n between 4 and 5, while smaller peaks were observed with n just above 3 and between 7 and 8 on either side of this. For the x = 0.04 sample, clear staging peaks with n just above 5 were observed

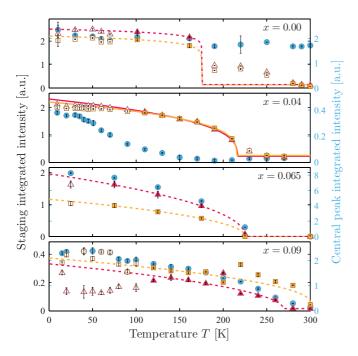


FIG. 3. Temperature dependence of integrated intensities of staging peaks (red triangles for low l and yellow squares for high l) and central peaks (blue circles). Lines for the staging data are power-law fits to the filled markers only. Empty markers are excluded from the fits due to order-parameter saturation (low temperatures) and critical scattering (close to transition temperatures).

on either side of the anomalously small central Bmab peak. For the x=0.065 sample, the high shoulders of the Bmab peak could be fitted with staging peaks with n between 13 and 14. Although no staging is visible to the naked eye in the data for the x=0.09 sample, we found that the best fit of the data was to a large central Bmab peak with small shoulders reminiscent of staging with a very high n.

The relation between the staged and nonstaged phases, calculated as the relative integrated intensity r_I between the average of the two largest staging peaks I_{staging} and the central Bmab peak I_{Bmab} ,

$$r_I = \frac{I_{\text{staging}}}{I_{Bmab}},\tag{2}$$

is also shown in Fig. 2. The relative integrated intensity is used as a measure of the amount of the sample which is staged. 1

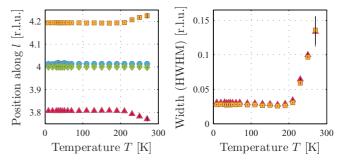


FIG. 4. Overview of peak positions (left) and staging peak widths (right) for the x=0.04 sample. Blue circles show the position of the central *Bmab* peak while green diamonds show the midpoint of the staging peaks, which are in turn positioned at the yellow squares and red triangles. There is a clear difference between the blue circles and the green diamonds, indicating different c-axis lengths for the *Bmab* and the staged structures. Note that the *Bmab* peak position was held fixed in the fit to the T=60 K value above this temperature. The widths show a clear increase around the phase transition, as expected for a second-order phase transition.

Scans similar to those in Fig. 2 were taken at various temperatures and the data were fitted to the best Lorentzian and/or Gaussian peak shapes in order to obtain individual integrated intensities, positions, and widths for each peak. The integrated intensities for the central Bmab peak and the staging peaks (for the x=0.00 sample only the most intense pair of staging peaks) are shown in Fig. 3. Each data set shows phase transitions with varying transition temperatures and decay rates for the Bmab and staging peaks, respectively. Note, however, that the staging peaks are comparable in intensity and widths by pairs, and that for all samples the staging transition appears quite abruptly. The x=0.00 Bmab peak data did not show a phase transition below room temperature, which is in accordance with earlier investigations [25].

The staging transition is most clearly interpreted in the x = 0.04 sample, wherefore we have chosen to analyze these data in more detail and generalize the observations to the other samples where applicable. For each temperature, the scan was fit to three Lorentzians (with positions and widths plotted in Fig. 4). A small difference observed between the position of the observed Bmab peaks and the center between the positions of the staging peaks indicated a phase separation between the staged and nonstaged parts of the samples with slightly different c-axis lengths. Furthermore, since the staging transition temperature is higher than the Bmab transition temperature at least in the x = 0.04 sample, staging cannot be a superstructure of *Bmab* within the same sample volume. This confirms earlier results on oxygen-only doped compounds [16,18,26]. As the relative intensity of the (014) and staging peaks seen in Fig. 3 does not depend monotonically on Sr content, we also believe that the specific amount of staged/nonstaged volume in each sample does not depend (monotonically) on Sr content. Finally, the width of the staging peaks is seen to diverge close to the transition in the right part of Fig. 4, as expected from a second-order phase transition.

The staging temperature data in Fig. 3 were fit with a power law as shown for the x = 0.04 sample with a solid line. We use a method commonly used for perovskites [27] to

¹We assume that the excess oxygen is close to homogeneously distributed throughout the sample, but that the excess oxygen in some volume of the sample is ordering in staging patterns. The rest of the oxygen remains disordered and structurally affects only the *Bmab* lattice parameters in the remainder of the sample volume. With these assumptions, the ratio of the staging peak to *Bmab* intensity should give us an indication of the degree of staging order. Another way of assessing the staging order strength would be to normalize the staging intensity versus weak fundamental peaks for each individual sample, but unfortunately time only permitted us to collect data at fundamental peaks which were very strong and therefore subject to extinction effects (varying between samples due to varying sizes/shapes) and thus not fitted for normalization purposes.

exclude low-temperature data points due to saturation of the signal, and data points just above the transition due to critical scattering. The power-law fit yields $T_{\rm staging} = 215.8(7)~{\rm K}$, which is a significantly smaller transition temperature than in the nickelates [17]. The obtained critical exponents 2β for the staging peaks are 0.312(14) and 0.36(2), respectively, which fall between two-dimensional (2D) and three-dimensional (3D) Ising models, leaning closer to the 2D model [28]. This leads us to speculate that similar 2D directional kinetics could be behind the formation of the staging superstructures.

In order to analyze staging in the more difficult data sets for some of the other samples, it was necessary to use a gradient analysis method² to fix the transition temperature before fitting with a power law, the results of which are shown as dashed lines in Fig. 3. We observe an indication of slightly increasing transition temperature with x and comparable critical exponents, with exception of the improbably low exponent we found for the x=0.00 sample, possibly caused by our exclusion of data points due to a second, overlapping, phase transition at higher temperature stemming from a staging phase with higher n.

The Bmab transition is clearly much more gradual (extending more than 100 K) than the fast staging transition for the x = 0.04 sample. This also seems to apply for the other samples, although the conclusion is less clear because of the fewer data points around the transition (x = 0.065, 0.09) or lack of data above room temperature (x = 0.00, 0.09). This indicates a different mechanism behind the growth of the *Bmab* volumes than the staging volumes. A similar gradual transition as seen in the Bmab volume of our samples has also been observed in similar systems on peak positions which were forbidden according to the average or majority structure of the sample [17,29]. In the chemically similar compound La_{2-x}Ba_xCuO₄ octahedral tilt fluctuations can average to look like low-temperature orthorhombic (LTO) structure [30] which may be related to our case. For our range of Sr doping values, both staging and Bmab transition temperatures are below the Bmab transition temperature of the corresponding oxygen-stoichiometric compound [31] (an overview is shown in the Supplemental Material [23]).

Finally, an investigation of the effect of cooling rate was performed on the x=0.00 and 0.04 samples, as shown in Fig. 5. The same scans as previously described and shown in Fig. 2 were performed after fast (>2 K/min) and slow (<2 K/min) cooling rates. We see clear stage 2, 3, and 4 peaks after the first fast cool, but also some diffuse signal close to the central *Bmab* peak, while the second slow cool only manages to produce stage 5 on top of the diffuse signal. In the sample with Sr, however, the cooling rate has no effect on the scattering pattern, which is dominated by stage 5.

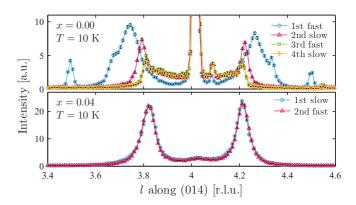


FIG. 5. Cooling history dependency of the measured signals for the x = 0.00 (top) and x = 0.04 (bottom) samples. The top scattering pattern is changed remarkably from the one shown in the top plot of Fig. 2 because of the initial fast cool.

IV. DISCUSSION

The staging numbers found for the oxygen-only doped sample fit well with previously found values for similar samples [18], while the staging observed in the three Sr-doped samples have increasing staging numbers following increasing Sr doping. The peak shoulders observed for the x = 0.09sample are analyzed as staging, with staging numbers of up to 90, which seem very high. However, analyzing the widths of the fitted staging peaks for the samples gives an indication of the correlation lengths, which do indeed allow for such long-range interactions. Typical widths of low-temperature staging peaks along l for the x = 0.09 sample are HWHM = 0.0022 Å^{-1} , corresponding to typical correlation lengths in the order of $\pi/\text{HWHM} = 1400\,\text{Å}$ (assuming experimental resolution is negligible), or about 110 unit cells along c. This is indeed a larger correlation length than the n/2 = 44.5 unit cells needed for inferring a staging number of 90 for the sample.

The *Bmab* (014) peak observed for the x = 0.04 sample was heavily suppressed, which could either be due to a Sr dopinginduced minimum in the scattering intensity for the reflection or, more likely, be an indication of the staged phase, which does not exhibit the central Bmab peak, being a very large part of the sample, hence showing only the staging peaks with high intensity [18]. The Bmab peak decreased gradually with temperature similarly to what has been observed previously for optimally Sr-doped La_{1.85}Sr_{0.15}CuO₄ [32]. The nature of the HTT-LTO transition was described by the same author as largely being displacive and continuous, whereas another author has suggested that substantial CuO₆ octahedral tilt (and concomitant charge) disorder is present in optimal and underdoped La_{2-x}Sr_xCuO₄ [33,34]. Further studies, possibly including other codoped samples with low x and a larger *Bmab* volume fraction, are needed in order to rule out either explanation here.

An estimate of the relative volume fractions of the staged/nonstaged structural phase was given by the ratio of integrated intensities r_I [Eq. (2)] shown in Fig. 2. For each sample, this ratio has a completely different value than the ratio of the superconducting and magnetic volume fractions, which are (in order of low to high x) 0.56, 0.79, 4.26, and 1.13 (these values are calculated in the Supplemental Material

²We define the transition temperature as the temperature where the slope of the data curve is at a maximum, following Ref. [45]. In order to do this analysis, the integrated intensity data have been interpolated linearly and smoothed with a low-pass Butterworth filter, allowing us to find the gradient in a meaningful way. This method gave results in agreement with the results found directly through fitting in the data sets where this was possible, and is detailed further in the Supplemental Material [23].

[23]). Thus, it is clear that the two types of phase separation, structural and electronic, are not directly correlated.

From the transition temperature of the staging peaks observed in Fig. 3, it is seen that a higher Sr doping results in a harder binding of the staged phase, observed as a tendency for increasing transition temperature. This indicates that the Sr could be correlating the staging oxygen, keeping them in a more stable position than what would be the case at La-only sites. Assuming a second-order phase transition approach to the transitions for the staging signals, as was argued for the x = 0.04 sample, with the widths seen in Fig. 4, the critical exponents for the Sr-doped samples were all in the range between the 2D and 3D Ising models. At the same time, Sr defects seem to promote faster diffusion of the intercalated oxygen than in oxygen-only doped samples. Thus, Sr/O codoping allows equilibrium to be reached and the same staging pattern evolved even at fast cooling rates, in contrast to oxygen-only doped samples. We therefore suggest that future studies of oxygenated samples consider codoping to avoid temperature hysteresis.

Possibly our most important observation in the codoped samples is that the characteristics of the staging patterns, which represent structural modulations along the c axis, do not influence the electronic low-temperature state which is phase separated between an optimal bulk superconductor with high $T_c \approx 40 \text{ K}$ [21] and low pinning [35] and a long-range ordered stripelike modulated antiferromagnet with $T_N \approx T_c \approx 40$ K [22]. The coexistence of similar electronic phases has been explained in other cuprates as being intertwined in a spatially self-organized pattern with order parameters modulated along the c axis [36,37]. These systems ($La_{2-x}Ba_xCuO_4$, $La_{2-x-y}Nd_ySr_xCuO_4$, $YBa_2Cu_3O_{6+x}$), however, all seem frustrated such that either bulk 3D superconductivity [38,39] or static antiferromagnetic order [40] is suppressed. In some cases, evidence for 2D superconducting correlations has been observed for temperatures close to our T_c [41,42]. We infer that intercalation of oxygen apparently lifts both the frustration of the Josephson coupling (since T_c is optimal in all samples) as well as stabilizes the magnetic order in a long-range modulated antiferromagnetic pattern with period \sim 8.

The influence is, however, not simple. In a naive picture the staged volume would be oxygen rich (as the superconducting volume with $n_h \sim 0.16$) and the *Bmab* areas hole poor (as the magnetic volume with $n_h \sim 0.125$). We, however, show in this work that the relative volume fractions of the staged/nonstaged phase do not follow the same trend as the relative volume fractions of the magnetic/superconducting domains.

V. CONCLUSION

In conclusion, we have shown that our codoped $La_{2-x}Sr_xCuO_{4+y}$ samples exhibit staging, or hints of staging, with dependence on their Sr content. We found that the Sr doping promotes faster oxygen diffusion and stabilizes the staged phase, removing temperature hysteresis while at the same time resulting in a tendency for higher transition temperatures for higher doping. We also see that the staging number n increases fast with x. However, the significantly varying characteristics of the staging superstructure which we have discussed in this work, compared with the differently varying characteristics of the electronic phase separation in the same samples, indicate that the interstitial oxygen taking part in the staging superstructure does not (directly) influence the lowtemperature electronic phase separation. Hence, further studies of the intercalated oxygen and the possible connection to electronic phase separation in similar samples are still needed.

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