# Using Graph-based Modelling to explore changes in students' affective states during exploratory learning tasks

Beate Grawemeyer Birkbeck Knowledge Lab Birkbeck, University of London London, UK beate@dcs.bbk.ac.uk

Wayne Holmes Institute of Educational Technology The Open University Milton Keynes, UK wayne.holmes@open.ac.uk

Alex Wollenschlaeger Birkbeck Knowledge Lab Birkbeck, University of London London, UK awolle01@dcs.bbk.ac.uk

Manolis Mavrikis UCL Knowledge Lab UCL Institute of Education University College London London, UK m.mavrikis@ucl.ac.uk Sergio Gutierrez-Santos Birkbeck Knowledge Lab Birkbeck, University of London London, UK sergut@dcs.bbk.ac.uk Alexandra Poulovassilis

Birkbeck Knowledge Lab Birkbeck, University of London London, UK ap@dcs.bbk.ac.uk

## ABSTRACT

This paper describes how graph-based modelling can be used to explore interactions associated with a change in students' affective state when they are working with an exploratory learning environment (ELE). We report on a user study with an ELE that is able to detect students' affective states from their interactions and speech. The data collected during the user study was modelled, visualized and queried as a graph. We were interested in exploring if there was a difference between low- and high-performing students in the kinds of interactions that occurred during a change in their affective state. Our findings provide new insights into how students are interacting with the ELE and the effects of the system's interventions on students' affective states.

#### **Keywords**

Graph Modelling, Interaction Data, Exploratory Learning Environment, Affect

# 1. INTRODUCTION

Much research recently has focussed on *Exploratory Learn*ing Environments (ELEs) which encourage students' openended interaction with a knowledge domain, combined with intelligent components that aim to provide pedagogical support to ensure students' productive interaction [15]. Such components can provide different types of feedback to students, ranging from unsolicited prompts and nudges, to lowinterruption feedback that students can choose to view if they wish. The aim of this feedback is to balance students' freedom to explore alternative task solution approaches while at the same time providing sufficient support to ensure that the intended learning goals are being achieved [15]. The data gathered from students' interactions with ELEs provides a rich source of information for understanding how students are using the ELE and how its intelligent support may be enhanced to support them better. The overarching aim of our research is to identify when students need support when working with ELEs and what kind of support should be provided by the system. In the present paper, our focus is on identifying key events that contribute towards a change in a student's *affective state*.

It is well understood that affect interacts with and influences the learning process [19, 9, 1]. While positive affective states (such as surprise, satisfaction or curiosity) contribute towards learning, negative states (such as frustration or boredom) can undermine learning. Also, D'Mello et al. elaborate on how confusion, which superficially might be considered a negative affective state, is likely to promote learning under appropriate conditions [9]. It is therefore important to deepen our understanding of the role of affective states for learning, and to be able to move students out of states that inhibit learning. We focus on a subset of the affective states identified by Pekrun [21]: flow/enjoyment, surprise, frustration, and boredom. We also add confusion, which has been identified elsewhere as an important affective state during learning [9, 23].

In this paper we are concerned with identifying interaction events that are associated with a change in students' affective state as they interact with an affect-aware ELE called *Fractions Lab* that aims to develop their knowledge of fractions. Student-system interaction data from learning environments has an inherent temporal dimension, with successive events being related through the "next event" relationship. It is therefore natural to model this data in graph form, with event occurrences being represented as nodes in the graph, and the "next event" connections between them as edges, and this is indeed the data modelling approach that we adopt in this paper.

In Section 2 we review related work in affect-aware intelligent support and in graph-based modelling of learningrelated data. Section 3 briefly describes the Fractions Lab ELE and its affect-aware intelligent support, to the level of detail needed for this paper. Section 4 describes a user study using Fractions Lab, the data collection, graph-based modelling, querying and analysis. Sections 5 and 6 present and discuss the results. Section 7 gives our concluding remarks and directions of further work.

## 2. RELATED WORK

Only a limited amount of research has been undertaken to investigate how a student's affect or motivation can be taken into account to provide learning material or motivational feedback. One early example is del Soldato & du Boulay [7] who use a student's motivation to decide whether to provide the next task or to provide hints. Another example is Santos et al. [26] who show that affect as well as motivation and self-efficacy impact the effectiveness of motivational feedback and recommendations. Additionally, Woolf et al. [31] developed an affective pedagogical agent which is able to mirror a student's affective state, or acknowledge a student's affective state if it is negative. Another example is Conati & MacLaren [5], who developed a pedagogical agent to provide support according to the affective state of the student and their personal goal. Also, Shen et al. [28] recommend learning material to the student based on their affective state. D'Mello et al. [8] developed a system that is able to respond to students via a conversation that takes into account the affective state of the student. Grawemeyer et al. [13] use a student's affective state to select the type and the presentation of feedback within the Fractions Lab ELE with the aim of providing an enhanced learning experience. Grawemeyer et al. [14] report on findings that indicate that affect can be viewed as a proxy of how easy or difficult it is for students to carry out a particular reasoning step needed to perform a learning task; their results indicate that low-performing students have more difficulties in performing tasks when the tools provided to them do not fully match the reasoning step that is needed whereas high-performing students are more at ease with a range of different reasoning tools.

In this paper we add to the current literature by investigating key events that have an effect on students' affective state. We adopt a graph-based approach to modelling, querying and visualizing student-system interactions data arising from the use of ELEs, extending preliminary work in this area reported in [24]. Other work has also modelled learning-related data as graphs, e.g. [16] for providing support to moderators in e-discussion environments; [22, 27] for supporting learning of argumentation; [3] for supporting students' "navigation" through learning objects; [6] for recognising students' activity planning in ELEs; and [30] for gaining understanding of learners' interactions in professional networks. Previous work closest to ours is that on interaction networks and hint generation [29, 10, 11], in which the graphs used consist of nodes representing states within a problem-solving space and edges representing students' actions in transitioning between states. In these environments, students are required to select and apply rules, and the interaction network aims to represent information relating to students' problem-solving in moving from state to state. Our approach differs from this in that we use graphs to model fine-grained event-based interaction data arising from an ELE. In our graphs, nodes represent occurrences of key indicators that are detected, inferred or generated by the

ELE (i.e. nodes represent events, not problem states); and the edges between such nodes represent the "next event" relationship. Also, we do not use the graph-modelled data to automatically generate feedback for the student, but rather to investigate the effects of the system's interventions in order to better understand how students interact with the ELE, with the aim of improving its support for students.

# 3. THE FRACTIONS LAB ELE

Fractions Lab is an ELE that forms part of the iTalk2Learn learning platform targeted at children aged 8-12 years old who are learning about fractions. Figure 1 illustrates the

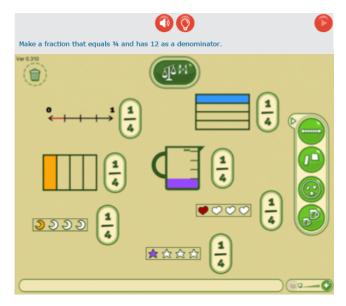


Figure 1: Exploratory learning environment - Fractions Lab.

Fractions Lab user interface. The learning task is displayed at the top of the screen. Students undertake the task by first choosing a fraction representation from the right-most vertical menu, which they then manipulate (in the work area at the centre of the interface) in order to construct their task solution. The different fraction representations are: a number line, rectangles, sets, and liquids. The large button at the top of the work area provides access to a variety of tools (to compare, add and subtract fractions). As students are interacting with the learning environment they are asked to talk aloud about their reasoning process. This speech, together with their interactions with the ELE, are used to detect students' affective states using a combination of Bayesian and rule-based reasoning [13]. The detection of the affective state is based on keywords and prosodic features that were identified through Wizard-of-Oz studies [18, 20], where students' speech was recorded and used to determine keywords and speech pause histograms that can provide insights into the student's affective state. Additionally, students' interaction data is used to add evidence to the detected affective state, such as whether students viewed and followed the most recent feedback.

The affective states detected by Fractions Lab can be ranked according to their effect on learning on the basis of previous studies (see Section 1). For example, being in flow is a positive affective state as it indicates that the student is engaging with the learning task well. Confusion is mostly associated with realising misconceptions, which also contributes towards learning, while frustration and boredom are likely to have a negative effect on learning.

Adaptive support is provided based on the student's detected affective state and performance. Table 1 (from [13]) shows the different types of feedback provided by the system. The system's adaptive support selects the feedback type and the feedback message based on a Bayesian network that aims to improve the student's affective state (where as discussed in Section 1 — flow and surprise are viewed as positive affective states, confusion as a neutral state, and boredom and frustration as negative states). A second Bayesian network determines whether the feedback message is presented to the student in low-interruption or highinterruption mode: low interruption is through the lightbulb at the top of the screen being lit up, and the student may or may not elect to click on the light-bulb to view the feedback message; high interruption is through a pop-up window that shows the message. The automatic affect detection shows good performance for detecting being in flow (precision: 86.2%, recall: 84.2%), but lower performance for the other affective states: confusion (precision: 67.9%, recall: 86.8%), frustration (precision: 28.6%, recall: 80.0%), boredom (precision: 80.0%, recall: 10.8%). We refer readers to [13] for full details.

Table 1: Feedback Types and Examples

Feedback Type	Example			
AFFECT	Well done. You're working really			
BOOSTS	hard!			
AFFIRMATION	The way that you worked that out			
prompts	was excellent. Now go to the next			
	task.			
NEXT STEP	Use the comparison box to compare			
feedback	your fractions.			
OTHER PROB-	What do you need to do now, to			
LEM SOLVING	complete the fraction?			
feedback				
REFLECTIVE	What do you notice about the two			
prompts	fractions?			
TALK ALOUD	Please explain what you are doing.			
prompts				
TASK SE-	Are you sure that you have answered			
QUENCE	the task fully? Please read the task			
prompts	again.			

## 4. USER STUDY

We conducted a user study in which iTalk2learn was used by students in a classroom setting, over several sessions, for the purpose of gathering student-system interaction data.

## 4.1 Participants

41 students took part in the study, all primary school students aged between 8 and 10 years old, recruited from two schools in the UK (one in the north of England, one in the south). These students were part of a larger evaluation of iTalk2Learn that also included other conditions, which are not relevant for the research reported in this paper. For more information of these please see [25]. Parental consent for their involvement in the study was obtained for all students.

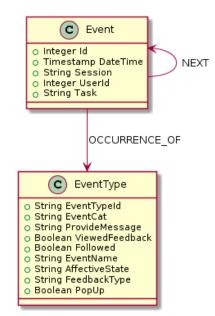
## 4.2 Procedure

At the start of each session, students were given a short introduction to iTalk2Learn and Fractions Lab. Students then completed an online questionnaire that assessed their knowledge of fractions (the pre-test). This was followed by 40 minutes during which the students engaged with iTalk2learn, including the Fractions Lab ELE with the affect-aware support. After the 40 minutes, the students completed a second online questionnaire that again assessed their knowledge of fractions (a post-test similar to the pre-test).

#### 4.3 Data collection and modelling

In addition to the pre- and post-test questionnaire, the learning platform logged every student-system interaction, such as fractions being created or changed by students, buttons clicked within Fractions Lab, feedback being provided by the system, feedback being viewed by students, and the system's detection of students' affective states. All these events were saved in the iTalk2Learn database, along with a timestamp.

This data was then remodelled into a graph form, according to the graph data model shown in Figure 2. We see that the data model comprises two node types: Event nodes and EventType nodes. Event nodes capture occurrences of key



#### Figure 2: Graph data model for student-system interaction data.

interactions and have properties including:

- Id: a unique identifier for each event
- DateTime: the timestamp of the event

- Session: identifier for each session
- UserId: identifier for each student
- Task: identifier for each task

EventType nodes provide additional metadata about each event. The type of event determines which of the metadata fields are populated. The fields include:

- EventTypeId: a unique identifier for each event type
- EventCat: the category into which an event type falls: one of {system, intervention, fraction, affect}
- ProvideMessage: a feedback message available for the user to view.
- ViewedFeedback: indicates whether or not the previous feedback was viewed.
- Followed: indicates whether or not the previous feedback was followed.
- EventName: a description of the event type
- AffectiveState: the detected affective state of the user: one of {flow, surprise, confusion, frustration, boredom}
- FeedbackType: the feedback type, as listed in Table 1.
- PopUp: if feedback was presented within a high interruptive pop-up window or in a low-interruptive mode.

The data model includes two edge types: NEXT and OC-CURRENCE\_OF. Edges labelled NEXT link together successive Event nodes, allowing us to build up a sequence of consecutive events that describe the full history of studentsystem interactions as a student works on a task during a session. The OCCURRENCE\_OF relationship links each Event node to an EventType node.

In order to construct this graph representation, the data logged by iTalk2Learn was exported as text, which was then parsed and pre-processed using Python and the Pandas and py2neo libraries, and subsequently loaded into Neo4j Community Edition graph database. To visualize the resulting data graph we developed a custom visualization tool in JavaScript using the Node.js library. This tool was built on top of the linkurious.js library [17], which provides a customizable rendering engine for displaying graph data in a browser, and supports multiple graph layout algorithms.

An example sequence of events visualized using our tool is shown in Figure 3. Nodes are placed using the Fruchterman-Rheingold algorithm [12] provided by the linkurious.js library. Fruchterman-Rheingold is a force-directed algorithm which uses principles from physics for laying out the nodes of the graph. In our tool, the algorithm is used purely for aesthetic reasons. That said, without an effective layout algorithm, it would not be possible to make sense of the visualization as the nodes would be positioned randomly and may lie on top of one another, obscuring the ability to see sequences of Event nodes. In addition to allowing the viewing of large-scale changes in affective state, our visualization tool also allows 'zooming into' a section of the graph. An example of this is shown in Figure 4, where we see part of an event sequence for a student working on a task. Combined with mouse-over tool-tips, the tool allows researchers to interactively explore the student-system interactions data.

#### 4.4 Data analysis

Having viewed and interacted with visualizations such as these, we were interested to explore further the kinds of events that contribute towards changes in students' affective state as they work with Fractions Lab. To do this, we used Neo4j's graph query language, Cypher, to extract the metadata relating to pairs of consecutive events that exhibit a change in a student's affective state.

The Cypher query used is as follows:

```
MATCH (start_event: Event)-[:OCCURRENCE_OF]->(start_type: EventType),
        (end_event: Event)-[:OCCURRENCE_OF]->(end_type: EventType),
        p = (start_event)-[:NEXT]->(end_event)
WHERE start_type.affective_state in
        ["flow", "boredom", "confusion", "frustration"]
        AND end_type.affective_state in
        ["flow", "boredom", "confusion", "frustration"]
        AND start_type.affective_state = end_type.affective_state
        RETURN *
```

This query searches the graph for adjacent Event nodes connected by a NEXT relationship, and the EventType nodes they are connected to via OCCURRENCE\_OF relationships, such that the affective states associated with the EventType nodes are not equal. By adjusting the sets of affective states, the query can be modified to include specific transitions as needed. Note that we do not include 'surprise' in the sets of 'from' and 'to' affective states (nor in our analysis below) because it is currently not reliably detected by iTalk2Learn's affect-detection algorithms.

### 5. RESULTS

As part of our data analysis, we were interested to explore differences in students' affective states and interactions compared with their post-test score performance. Students' performance, based on the post-test score, was on average 3.83 (SD=1.46; min=0; max=6). A median split of students' post-test scores resulted in a higher- and a lowerperforming group (high: 27 students; low: 14 students). In the low-performing group, students increased their knowledge of fractions between the pre- and post-test from M=1.43 (SD=1.09) to M=2.50 (SD=1.02). In the high-performing group, students increased their knowledge between the preand post-test from M=3.04 (SD=1.63) to M=4.52 (SD=1.16). Students' performance in the pre-test was significantly different between the high- and low-performing students t(39) =-3.320 p=.000). There was also a significant difference in the post-test between the low- and high-performing students (t(39) = -5.51, p = .002).

In order to investigate which interactions moved students into a different affective state we used association rule learning (c.f. [2, 4]) over the data returned by the above Cypher query.



Figure 3: Part of an event sequence indicating the interactions between a student and the system as the student worked on a task in Fractions Lab. Positive affective states are displayed in green, neutral in orange and negative in red. This view allows researchers to quickly spot changes in affective state that can be analysed further.

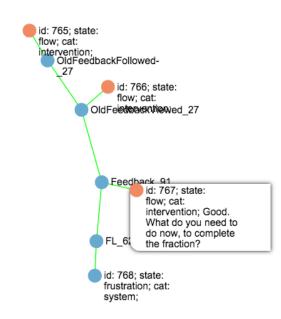


Figure 4: Zoomed-in view of an event sequence, showing Event nodes (blue, forming the "backbone") and EventType nodes (orange, branching off) in more detail. The NEXT and OCCURRENCE\_OF relationships are shown in green. The figure also shows tool-tips that provide information on the metadata associated with nodes.

#### 5.1 Association Rule Learning

The data included in the association rule learning included four variables relating to the pairs of consecutive events exhibiting an affect change. Variable 1 was the affective state (AffectiveState) associated with the first event. Variable 2 was the type of feedback (FeedbackType, see Table 1) provided by the system in the first event; if the first event was not a system intervention then this variable was blank. Variable 3 was the affective state associated with the second event. Variable 4 was the description of the second event (EventName); if the second event was not associated with a user interaction then this variable was blank.

In our association rule mining, only rules that included the affective state of the first event on the left-hand side (LHS) of the rule and the affective state of the second event on the right-hand side (RHS) of the rule were considered. Figure 5 and Figure 6 show the top 5 rules inferred for each student group (ranked by 'lift'). The 'support' indicates the frequency of the item-set appearing in the data (a number in the range 0-1). The 'confidence' indicates how often the rule has been found true i.e. the proportion of occurences of the LHS of the rule that also contain the RHS (a number in the range 0-1). The 'lift' indicates the performance of the rule at predicting the case (a number above 1) — the higher the lift, the higher the predictive performance of the rule.

The top two rules for low-performing students show that acknowledging receipt of feedback (by pressing the 'Done' button in the pop-up window providing a high-interruption message) and receiving reflective prompts when being in *flow* is likely to result in *frustration*. This might imply that the cog-

LHS		RHS	support	conf.	lift
{*doneButtonPressed*, before_flow}	$\Rightarrow$	{after_frustration	} 0.014	0.667	4.142
{before_flow, REFLECTION}	$\Rightarrow$	{after_frustration	} 0.069	0.556	3.452
{before_flow, Numerator}	$\Rightarrow$	{after_frustration	} 0.010	0.500	3.106
{before_flow, CloseFeedbackPopup}	$\Rightarrow$	{after_confusion}	0.010	1.000	2.679
{before_flow, TASK_NOT_FINISHED}	$\Rightarrow$	{after_confusion}	0.014	1.000	2.679

Figure 5: Top 5 rules for low-performing group.

nitive demands on low-performing students on receiving this feedback were too high for them, possibly due to a lack of knowledge about fractions. The third rule shows that when students were in *flow* and changed the numerator of their fraction they were likely to move into *frustration*. Again this might imply that cognitive demands were too high for them to understand how the fraction representation changed based on their interaction with the numerator. The fourth rule shows that viewing high-interruption feedback (and in particular closing the pop-up window that contains the feedback) can lead from being in *flow* to being in *confusion*. This might be due to the feedback message causing students to realise a misconception. The fifth rule shows that providing the Task Not Finished message can lead from being in flow to confusion, possibly because students might not have been aware that they had not finished the task.

LHS		RHS	support conf. lift
{*closeFeedbackPopup*, before_flow, PROBLEM_SOLVING}	}⇒	{after_frustration}	0.008 0.800 5.732
{before_flow, Denominator, PROBLEM_SOLVING}	$\Rightarrow$	{after_frustration}	0.015 0.571 4.094
{before_flow, Denominator}	$\Rightarrow$	{after_frustration}	0.021 0.478 3.426
{*lightBulbPressedOn*, before_flow}	$\Rightarrow$	{after_confusion}	0.008 1.000 2.710
{AFFECT_BOOSTS, before_frustration}	$\Rightarrow$	{after_confusion}	0.012 1.000 2.710

#### Figure 6: Top 5 rules for high-performing group.

The first two rules for high-performing students indicate that open-ended problem solving support is likely to move them from *flow* to *frustration*, in particular when subsequently changing the denominator of their fraction. This might imply that the cognitive load was too high to reason about the learning task upon receiving support for openended problem solving. The third rule highlights that a change of the denominator when being in *flow* can move students to *frustration*. Similarly to rule 3 for the lowpeforming students, this might imply that cognitive demands were too high for students to understand how the fraction representation changed based on their interaction with the denominator. The fourth rule indicates that when students press on a glowing light-bulb (and hence receive the lowinterruption feedback) they may move from flow to confusion, possibly because they have become aware of a misconception. The fifth rule shows that affect boosts can move students from *frustration* into the more positive affective state of *confusion*; this might imply that encouraging students to continue with their learning task can reduce cognitive load.

#### 6. DISCUSSION

As described earlier, we were interested in identifying key interaction events that are associated with a change in students' affective states as they interact with the Fractions Lab ELE. Students were divided into a low- and high-performing group based on a median split of their knowledge of fractions gathered from the post-test questionnaire. The analysis has shown that in both groups students moved from a positive affective state (*flow*) to a negative one (*frustration*) via the provision of certain forms of feedback and via their interaction with either the numerator or the denominator of their current fraction. In the low-performing group, receiving reflective prompts and working on the numerator were the main contributors to this affect change, while in the high-performing group it was support for open-ended problem solving and working on the denominator of their fraction. It is interesting to see that both reflective prompts and open-ended problem solving support encourage students to think about their reasoning steps, either what they have done so far (reflective prompts) or what they need to do in order to solve the task (open-ended problem solving support).

Students in the low-performing group may move from flow to confusion when viewing high-interruption feedback and when seeing the Task Not Finished message. Students in the high-performing group may move from flow to confusion when viewing low-interruption feedback. (We note that, by the design of Fractions Lab's affect-aware support — see discussion in [13] — low-performing students are more likely to receive high-interruption feedback, and high-performing students low-interruption feedback.) In both cases, students may be being prompted to reflect on their solution approach which may in turn be leading them to realise a misconception.

Finally, the analysis shows that the system's affect boosts are able to move high-performing students from *frustration* into the more positive affective state of *confusion*. A similar, but lower-ranked, rule was found to move low-performing students from *confusion* into *flow* (with support 0.017, confidence 1.0 and lift 2.179).

# 7. CONCLUSION

This paper has investigated key events that occur when students' affective state changes as they interact with an exploratory learning environment called Factions Lab, targeted at learning about fractions. Modelling the studentsystem interactions data that was collected by the learning environment during a classroom-based User Study in a graph form allowed us to visualize and interact with this data, and ultimately to formulate queries for extracting the necessary data to perform our analyses. Specifically, association rule mining was used to identify events that are associated with a change in students' affective state.

Students were divided into a low- and a high-performing group. We found that students are likely to move from *flow* to *frustration* when provided with reflective prompts in the low-performing group and open-ended problem solving support in the high-performing group. This might imply that these types of support are imposing too high a cognitive demand on students and require modification. Additionally, interaction with the numerator or denominator of their fraction is likely to move low or high performing students, respectively, from *flow* to *frustration*. Viewing highinterruption or low-interruption feedback may move low or high performing students, respectively, from *flow* to *confusion*. Finally, our analysis points to the positive effect of Affect Boosts, for both categories of student.

These findings extend earlier findings reported in [13] with a

finer-grained analysis of students' affective state changes as they interact with Fractions Lab. The study in [13] found that students are mostly in positive affective states when working with Fractions Lab, and that affect-aware support is more likely to reduce students' boredom compared to non-affect aware support. Here, we have identified specific student-system interactions that may lead students from being in flow to being in confusion or frustration, thereby identifying areas where further work may be needed in the design of Fraction Lab's affect-aware support. We have also reaffirmed the design goal of the system's provision of Affect Boosts.

Situations where the system's affect-aware feedback may need to be modified include: (i) Reviewing the content of both the high- and the low-interruption messages, to see if the incidences of confusion can be reduced. (ii) Considering extending the provision of reflective prompts and open-ended support with additional affect boost messages and low-interruption hints that students might also select to view, in order to mitigate against frustration. (iii) Considering providing more scaffolds when students are manipulating their fractions, for example additional low-interruption feedback.

These insights into the relationship between feedback, affect, the interactions with the ELE, and performance would not have been easy to make without the approach described here. Exploratory learning environments such as Fractions Lab can generate very large volumes of student-system interactions data, making their interpretation a challenging task for researchers. We have seen here how modelling such data as a graph can open up new data visualization, querying and analysis opportunities, leading to new insights into how students are interacting with the ELE and the effects of the system's interventions, with the ultimate goal of designing improved support for students.

Future work includes further scrutiny of the graph-modelled data derived from this and follow-on User Studies with Fractions Lab, identification of additional research questions relating to the effectiveness of the system's affect-aware support, and development of additional queries, analyses and visualizations to tackle these research questions. Particularly of interest is to look more closely at the *sequence* of interaction events leading up to changes in students' affective states (as opposed to just individual events). We are also interested to explore how our visualizations can help to identify patterns of interactions that are associated with misconceptions and with learning. Also important is the development of a fully-functional GUI through which researchers, designers or even teachers with little computing expertise can explore the data from their different perspectives.

#### 8. **REFERENCES**

- R. S. J. d. Baker, S. K. D'Mello, M. T. Rodrigo, and A. C. Graesser. Better to be frustrated than bored: The incidence, persistence, and impact of learners' cognitive-affective states during interactions with three different computer-based learning environments. *Int. J. Hum.-Comput. Stud.*, 68, 2010.
- [2] D. L. Bazaldua, R. S. J. de Baker, and M. O. S. Pedro. Comparing expert and metric-based

assessments of association rule interestingness. In Proceedings of EDM, 2014.

- [3] N. Belacel, G. Durand, and F. LaPlante. A binary integer programming model for global optimization of learning path discovery. *G-EDM*, 2014.
- [4] D. Ben-Naim, M. Bain, and N. Marcus. A user-driven and data-driven approach for supporting teachers in reflection and adaptation of adaptive tutorials. In *Proceedings of EDM*, 2009.
- [5] C. Conati and H. MacLaren. Empirically building and evaluating a probabilistic model of user affect. User Modeling and User-Adapted Interaction, 2009.
- [6] R. Dekel and K. Gal. On-line plan recognition in exploratory learning environments. *G-EDM*, 2014.
- [7] T. del Soldato and B. du Boulay. Implementation of motivational tactics in tutoring systems. *Journal of Artificial Intelligence in Education*, 6(4), 1996.
- [8] S. D'Mello and A. Graesser. Autotutor and affective autotutor: Learning by talking with cognitively and emotionally intelligent computers that talk back. *ACM TiiS*, 2013.
- [9] S. K. D'Mello, B. Lehman, R. Pekrun, and A. C. Graesser. Confusion can be beneficial for learning. *Learning & Instruction*, 29(1):153–170, 2014.
- [10] M. Eagle and T. Barnes. Exploring differences in problem solving with data-driven approach maps. *EDM*, 2014.
- [11] M. Eagle, D. Hicks, B. Peddycord III, and T. Barnes. Exploring networks of problem-solving interactions. *LAK*, pages 21–30, 2015.
- [12] E. Fruchterman, T.M.J.and Reingold. Graph drawing by force-directed placement. Software: Practice and Experience.
- [13] B. Grawemeyer, M. Mavrikis, W. Holmes, S. Gutiérrez-Santos, M. Wiedmann, and N. Rummel. Affective learning: Improving engagement and enhancing learning with affect-aware feedback. User Modeling and User-Adapted Interaction - Special Issue on Impact of Learner Modeling, 2017.
- [14] B. Grawemeyer, M. Mavrikis, C. Mazziotti, A. Hansen, A. van Leeuwen, and N. Rummel. Exploring students' affective states during learning with external representations. In 18th International Conference on Artificial Intelligence in Education (AIED 2017), 2017.
- [15] S. Gutierrez-Santos, M. Mavrikis, and G. D. Magoulas. A Separation of Concerns for Engineering Intelligent Support for Exploratory Learning Environments. J. Research and Practice in Inf. Tech., 44:347–360, 2013.
- [16] A. Harrer, R. Hever, and S. Ziebarth. Empowering researchers to detect interaction patterns in e-collaboration. Frontiers in Artificial Intelligence and Applications, 158:503, 2007.
- [17] S. Heymann. https://github.com/linkurious/linkurious.js.
- [18] R. Janning, C. Schatten, and L. Schmidt-Thieme. Perceived task-difficulty recognition from log-file information for the use in adaptive intelligent tutoring systems. *International Journal of Artificial Intelligence in Education*, pages 855–876, 2016.
- [19] B. Kort, R. Reilly, and R. Picard. An affective model

of the interplay between emotions and learning. In *IEEE International Conference on Advanced Learning Technologies*, number 43-46, 2001.

- [20] M. Mavrikis, B. Grawemeyer, A. Hansen, , and S. Gutiérrez-Santos. Exploring the potential of speech recognition to support problem solving and reflection wizards go to school in the elementary maths classroom. In *EC-TEL 2014*, pages 263–276, 2014.
- [21] R. Pekrun. The control-value theory of achievement emotions: Assumptions, corollaries, and implications for educational research and practice. J. Edu. Psych. Rev., pages 315–341, 2006.
- [22] N. Pinkwart and et al. Graph grammars: An ITS technology for diagram representations. *FLAIRS*, pages 433–438, 2008.
- [23] K. Porayska-Pomsta, M. Mavrikis, and H. Pain. Diagnosing and acting on student affect: the tutor's perspective. User Modeling and User-Adapted Interaction, 18(1):125–173, 2008.
- [24] A. Poulovassilis, S. Gutierrez-Santos, and M. Mavrikis. Graph-based modelling of students' interaction data from exploratory learning environments. In *Proceedings of G-EDM, at EDM*, 2015.
- [25] N. Rummel, M. Mavrikis, M. Wiedmann, K. Loibl, C. Mazziotti, W. Holmes, and H. A. Combining exploratory learning with structured practice to foster conceptual and procedural fractions knowledge. In *Proceedings of ISLS*, 2016.
- [26] O. Santos, M. Saneiro, S. Salmeron-Majadas, and B. J.G. A methodological approach to elicit affective educational recommendataions. In *IEEE ICALT*, 2014.
- [27] O. Scheuer and B. McLaren. CASE: A configurable argumentation support engine. *IEEE Trans. Learn. Tech.*, 6(2):144–157, 2013.
- [28] L. Shen, M. Wang, and R. Shen. Affective e-learning: Using "emotional" data to improve learning in pervasive learning environment. *Educational Technology & Society*, 12(2):176–189, 2009.
- [29] V. Sheshadri, C. Lynch, and T. Barnes. InVis: An EDM tool for graphical rendering and analysis of student interaction data. *G-EDM*, 2014.
- [30] D. Suthers. From contingencies to network-level phenomena: Multilevel analysis of activity and actors in heterogeneous networked learning environments. *LAK*, 2015.
- [31] B. Woolf, W. Burleson, I. Arroyo, T. Dragon, D. Cooper, and R. Picard. Affect-aware tutors: recognising and responding to student affect. *Int. J. Learning Technology*, 4(3-4):129–164, 2009.