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## PELREF. A numerical code for computing the ablated state of a refuelling pellet

Forskningscenter Risø, Roskilde

*Publication date:*  
1981

*Document Version*  
Publisher's PDF, also known as Version of record

[Link back to DTU Orbit](#)

*Citation (APA):*  
Chang, C. T. (1981). PELREF. A numerical code for computing the ablated state of a refuelling pellet. (Risø-M; No. 2219).

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RISØ-M-2219

PELREF

A numerical code for computing the ablated state of a  
refuelling pellet

C.T. Chang

Abstract. Assuming a constant specific heat ratio and using the  
neutral shielding model, this report presents a numerical code  
for calculating the ablation rate and the state of the ablatant  
of a refuelling pellet. Results are given for plasma conditions  
corresponding to present and to future toroidal devices.

UDC 621.039.626 : 621.039.633 : 681.3.06

May 1981

Risø National Laboratory, DK 4000 Roskilde, Denmark

ISBN 87-550-0653-1

ISSN 0418-6435

Risø Repro 1981

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## 1. INTRODUCTION

A numerical code for computing the ablation rate of a refuelling pellet, clearly should exist among a few laboratories. For various purposes, as, for example, the development of a diagnostic method in evaluating the pellet local ablation rate, the calculating of the fuel transport rate, and the possible modification and extension of the existing neutral shielding model<sup>(1)</sup>, etc., it should be desirable to have such a computational code at our own disposal.

This report summarizes the result of such an effort. Section 2 first gives a brief description of the neutral shielding model relevant to the numerical analysis. This is followed by a derivation of the asymptotic solution of the ablated flow. Section 3 gives a brief description of the code and the general computational results obtained. A detailed description of a typical program is included in the appendix A. Examples of computational results are given for a present experimental and a future large toroidal device.

## 2. THE MODEL

### 2.1. Governing equations

According to the neutral-shielding model<sup>(1),(2)</sup> of a refuelling pellet, the kinetic energy of the ablated flow is described by the equation

$$\frac{dw}{dr} = \frac{2w}{(\theta-w)} \left[ A_* r^2 \frac{dg}{dr} - 2 \frac{\theta}{r} \right] \quad (1)$$

where  $w = v^2$  and  $\theta$  are the kinetic energy density and temperature normalized with respect to their values at the sonic radius,

$r_*$ . Similarly,  $r$  is the normalized radial coordinate; thus, at the sonic radius,  $r = 1$ . The pellet surface is denoted by  $\hat{r} = r_p / r_*$ .

The dimensionless input rate of the electron energy is given by

$$\frac{dq}{dr} = \frac{\rho_* \Lambda_* r_*}{m_{H_2}} \sigma \Lambda'(E) q \quad (2)$$

where  $\Lambda'(E) = \Lambda(E) / \Lambda_*$  is the normalized "total energy loss cross section". The total energy loss cross section  $\Lambda(E)$  has two terms: The inelastic collision term is represented by the stopping cross section  $2L(E)/E$ ; the elastic collision is represented by the scattering cross section,  $\sigma(E)$ . Thus

$$\Lambda(E) = 2 \frac{L(E)}{E} + \sigma(E) \quad (3)$$

where

$$L(E) [\text{eV-cm}^2] = \{2.35 \times 10^{14} + 4 \times 10^{11} E + 2 \times 10^{17} E^{-2}\}^{-1} \quad (4a)$$

$$\begin{aligned} \sigma(E) [\text{cm}^2] &= 8.8 \times 10^{13} E^{-1.71} - 1.62 \times 10^{-12} E^{-1.932} \\ &\quad \text{for } E \geq 100 \text{ eV} \quad , \\ &= 1.13 \times 10^{-14} E^{-1} \quad (4b) \\ &\quad \text{for } E < 100 \text{ eV} \quad . \end{aligned}$$

The parameter  $\Lambda_*$ , which appeared in Eq. (1), is a constant depending on physical parameters at the sonic radius and the mass ablation rate  $G$ . Thus

$$\Lambda_* = \frac{4\pi f_B Q \left(\frac{Y-1}{Y}\right) q_* r_*^2}{kT_* G} m_{H_2} \quad (5)$$

where  $f_B$  and  $Q$  are reduction factors of the incident electron energy flux due to the magnetic field effect and the inelastic collision losses occurring in the ablated cloud. For simplicity, in the original model<sup>(1)</sup>  $f_B$  and  $Q$  were taken as constants;  $f_B \approx 0.5$ ,  $Q \approx 0.6$ .

If we seek a solution of a continuously accelerated flow of the ablatant, i.e.  $\frac{dw}{dr} > 0$  everywhere and the requirement at the far downstream  $\left(\frac{dq}{dr}\right)_{r \rightarrow \infty} \rightarrow 0$ , we observe that from Eq. (1) the flow downstream at a great distance must be supersonic, i.e.  $w > \theta$ . On the other hand, since we expect the temperature of the ablatant to be low near the pellet surface, the flow must be subsonic there, i.e.  $w < \theta$ .

At the sonic radius, since  $\theta = w$  we must impose the condition to make the terms in the square bracket of Eq. (1) vanish. As a result, we obtain

$$2\pi f_B Q \left(\frac{\gamma-1}{\gamma}\right) \frac{q_* \rho_* r_*^3 \lambda_*}{k T_* G} - 1 = 0 . \quad (6)$$

Using Eq. (6) and the mass conservation equations

$$\rho v r^2 = \rho_* \sqrt{w} r_*^2 = 1 .$$

Eq. (1) can be reduced to

$$\frac{dw}{dr} = \frac{4w\theta}{(\theta-w)r} \left[ \frac{\lambda' q r}{\theta \sqrt{w}} - 1 \right] . \quad (1a)$$

For the purpose of numerical computation, it would be more appropriate to replace  $w$  by  $v = \sqrt{w}$ , the governing equations of the ablated flow can then be written as follows:

$$\frac{dv}{dr} = \frac{2v\theta}{(\theta-v^2)r} \left[ \frac{\lambda' q}{\theta v} - \frac{1}{r} \right] , \quad (7)$$

$$\frac{d\theta}{dr} = 2 \frac{\lambda' q}{v} - (\gamma - 1) v \frac{dv}{dr} , \quad (8)$$

$$\frac{dq}{dr} = \lambda_* \frac{\lambda' q}{r^2 v} , \quad (9)$$

$$\frac{dE'}{dr} = 2\lambda_* \left[ \frac{L(E)}{E_* \lambda_*} \right] \frac{1}{r^2 v} , \quad (10)$$

$$\rho v r^2 = 1 , \quad (11)$$

$$p = \rho \theta . \quad (12)$$



The Mach number of the flow is given by

$$M = (v^2/\theta)^{1/2} . \quad (13)$$

All parameters except  $E$  in the above system of equations are normalized with respect to their values at the sonic radius. The incident electron energy at the normalized sonic radius  $r = 1$  is denoted by  $E_*$ ; thus,  $E' = E/E_*$  is the normalized electron energy. Notice that  $L(E)/E_*$  has the dimension of a cross section, and  $L(E)/E_*\Lambda_*$  is dimensionless.

The above system of equations contains two parameters,  $\lambda_*$  and  $\Lambda_*$ . They are defined as

$$\lambda_* = \rho_* \Lambda_* r_* / m_{H_2} , \quad (14)$$

$$\Lambda_* = \Lambda(E_*) . \quad (15)$$

Both  $\Lambda_*$  and  $\lambda_*$  depend on  $E_*$ , the incident electron energy at the sonic radius. As indicated by Eq. (3) and Eqs. (4a) and (4b), once  $E_*$  is chosen,  $\Lambda_* \equiv \Lambda(E_*)$  is fixed; however  $\lambda_*$ , to be shown subsequently, varies within a limited range.

## 2.2. Eigenvalue of the problem

At the sonic radius of  $r = 1$ , all flow parameters and  $\Lambda'$  become unity while  $\frac{dv}{dr}$  becomes indeterminate. For a given value of  $E_*$ , this derivative

$$z_s = \left( \frac{dv}{dr} \right)_{r=1} \quad (16)$$

as will be shown, depends on the parameter  $\lambda_*$ , which therefore can be viewed as an eigenvalue of the problem.

From Eqs. (8-10), we have at  $r = 1$

$$\frac{d\theta}{dr} = 2 - (r-1)z_s , \quad (17)$$

$$\frac{dq}{dr} = \lambda_* , \quad (18)$$

$$\frac{dE}{dr} = 2 \frac{\Lambda_* L(E_*)}{E_* \Lambda_*} , \quad (19)$$

whereas  $Z_s$  can be determined from Eq. (7) by applying the L'Hôpital's rule. This gives a quadratic equation in  $Z_s$ ; its explicit solution is given by

$$Z_s = \left( \frac{3-\gamma}{1+\gamma} \right) \left\{ 1 \pm \sqrt{1 - 2 \frac{(1+\gamma)}{(3-\gamma)^2} (\lambda_* + \psi_* - 1)} \right\} , \quad (20)$$

where

$$\psi_* = \left( \frac{d\Lambda'}{dr} \right)_{r=1} \quad (21)$$

and can be written as

$$\begin{aligned} \psi_* &= \frac{E_*}{\Lambda_*} \left( \frac{d\Lambda}{dE} \right)_{E=E_*} \cdot \left( \frac{dE}{dr} \right)_{r=1} , \\ &= 2\lambda_* \frac{L(E_*)}{\Lambda_*^2} \left( \frac{d\Lambda}{dE} \right)_{E=E_*} . \end{aligned} \quad (22)$$

Introducing

$$N_* = 2 \frac{L(E_*)}{\Lambda_*^2} \left( \frac{d\Lambda}{dE} \right)_{E=E_*} \quad (23)$$

we may further write  $\psi_* = N\lambda_*$  and replace the eigenvalue,  $\lambda_*$ , by

$$K = (1 + N_*)\lambda_* . \quad (24)$$

The derivative  $Z_s = \left( \frac{dv}{dr} \right)_{r=1}$  now is related to  $K$  by

$$Z_s = \left( \frac{3-\gamma}{1+\gamma} \right) \left\{ 1 \pm \sqrt{1 + 2 \frac{(1+\gamma)}{(3-\gamma)^2} (1 - K)} \right\} . \quad (25)$$

As a first requirement for  $Z_s$  to be real, it is necessary that

$$2 \frac{(1+\gamma)}{(3-\gamma)^2} (K-1) < 1 . \quad (26)$$

However, if we expect a solution with  $\frac{dv}{dr} > 0$  in the entire flow,  $Z_s$  must be positive. Furthermore, if we require the uniqueness

of the positive root (i.e., the two real roots of  $Z_s$  are of different sign) we must impose the condition that

$$1 + 2 \frac{\gamma+1}{(3-\gamma)^2} (1-K) > 1 \quad \text{or } K < 1 .$$

Stated briefly, after a value of  $E_*$  is assigned, according to Eq. (23) we find that  $N_*$  is fixed, the proper value of  $\lambda_*$  must be chosen such that  $K$  is within the open interval (0,1).

### 2.3. Boundary conditions

In view of the low sublimation energy of solid deuterium and the expectation of the existence of a self-shielding mechanism, the boundary conditions at the pellet surface  $\hat{r} = r_p/r_*$  may be written as

$$q(\lambda_*, E_*) = 0 \quad \left. \vphantom{q(\lambda_*, E_*)} \right\} \quad (27)$$

$$\theta(\lambda_*, E_*) = 0 \quad \left. \vphantom{\theta(\lambda_*, E_*)} \right\} \text{ at } r = \hat{r} . \quad (28)$$

The boundary conditions at the far distance region downstream clearly can be taken as

$$\left. \begin{aligned} q(\lambda_*, E_*) \rightarrow \tilde{q} = q_0/q_* \\ E(\lambda_*, E_*) \rightarrow \tilde{E} = E_0/E_* \end{aligned} \right\} \text{ at } r \geq r_m , \quad (30)$$

or alternatively,

$$\frac{dq}{dr} \rightarrow 0, \quad \frac{dE}{dr} \rightarrow 0 \text{ for } r \geq r_m . \quad (31)$$

By specifying these boundary conditions and defining all the derivatives in terms of the given value  $E_*$  and a guessed eigenvalue  $\lambda_*$ , we may then proceed the integration from the sonic surface inward to see whether the inner boundary conditions are satisfied at the pellet surface. For a given  $E_*$  the process has to be repeated by guessing the value  $\lambda_*$  until Eqs. (27) and (28) are satisfied. In other words, Eqs. (27) and (28) really are used to locate the pellet surface. Similarly, we may consider

the outer boundary conditions as a means of locating the ablated cloud boundary.

#### 2.4. Flow parameters at the sonic radius

Since all the flow parameters thus far were normalized with respect to their values at the sonic radius, to obtain their actual physical values it is necessary to determine their corresponding values at the sonic radius first. Using the facts that the flow is sonic, the mass is conserved, and the state of the ablatant can be taken as an ideal gas, we have the following three algebraic equations:

$$v_* = (\gamma k T_* / m_{H_2})^{1/2} \quad (32)$$

$$\rho_* v_* r_*^2 = G / 4\pi \quad (33)$$

$$P_* = \rho_* k T_* / m_{H_2} \quad (34)$$

These equations together with the two auxiliary equations:

$$f_B Q \left( \frac{\gamma-1}{r} \right) q_* \rho_* \lambda_* r_*^3 = k T_* \frac{G}{2\pi} \quad (6)$$

and

$$\lambda_* m_{H_2} = \rho_* \lambda_* r_* \quad (14)$$

form a system of five equations for the eight unknowns;  $G$ ,  $\rho_*$ ,  $P_*$ ,  $T_*$ ,  $v_*$ ,  $r_*$ ,  $q_*$  and  $E_*$  (recalling that both  $\lambda_*$  and  $\lambda_*$  depend on  $E_*$ ). If we consider  $E_*$ ,  $r_*$ , and  $q_*$  as given, they can be solved explicitly

$$\frac{G}{4\pi} = \frac{\lambda_* m_{H_2}^{2/3} [f_B Q (\gamma-1) q_*]^{1/3} r_*^{4/3}}{(2\lambda_*^2)^{1/3}} \quad (35)$$

$$\rho_* = \frac{\lambda_* m_{H_2}}{\lambda_* r_*} \quad (36)$$

$$k T_* = \frac{m_{H_2}^{1/3}}{\gamma} \left[ \frac{f_B Q (\gamma-1) q_* r_* \lambda_*}{2} \right]^{2/3} \quad (37)$$

$$v_* = \left[ \frac{f_B Q (\gamma-1) q_* r_* \Lambda_*}{2 m_{H_2}} \right]^{1/3}, \quad (38)$$

$$\gamma p_* = \left( \frac{m_{H_2}}{\Lambda_* r_*} \right)^{1/3} \left[ \frac{f_B Q (\gamma-1) q_*}{2} \right]^{2/3} \lambda_*. \quad (39)$$

Since the factor  $f_B Q$  always appears together with  $q_*$ , we may absorb it into  $q_*$ . We recall that  $r_*$  and  $E_*$  are related to the pellet radius  $r_p$  and the unattenuated electron energy  $E_0$  (or the plasma temperature  $2kT_0$ ) by

$$r_* = r_p / \hat{f}, \quad (40)$$

$$E_* = E_0 / \tilde{E} = 2 kT_0 / \tilde{E}, \quad (41)$$

and

$$q_* = q_0 / \tilde{q} = [n_0 (4\pi m_e)^{-1/2} (2kT_0)^{3/2}] / \tilde{q}. \quad (42)$$

These expressions, Eqs. (35-39), in turn can be related to the plasma parameters  $n_0$ ,  $kT_0$  and the pellet radius,  $r_p$ . For example, we have explicitly,

$$G = 8.4125 \times 10^{-17} (\gamma-1)^{1/3} \frac{\lambda_*}{\Lambda_*^{2/3}} \frac{n_0^{1/3} (kT_0)^{1/2} \left(\frac{r_p}{\hat{f}}\right)^{4/3}}{\tilde{q}^{1/3}}, \quad (35a)$$

$$p_* = 3.3452 \times 10^{-24} \left(\frac{\lambda_*}{\Lambda_*}\right) \frac{\hat{f}}{r_p} \quad (36a)$$

and

$$kT_* = \frac{8.3592}{\gamma} \left[ (\gamma-1) n_0 \left(\frac{r_p}{\hat{f}}\right) \frac{\Lambda_*}{\tilde{q}} \right]^{2/3} (kT_0). \quad (37a)$$

(All quantities appearing above are in C.G.S. units except for  $kT_0$  and  $kT_*$  which are in eV).

On account of the dependence of  $\lambda_*$ ,  $\Lambda_*$ ,  $\tilde{q}$  and  $\hat{f}$  on  $E_*$ , these equations indicate that for a given pellet radius  $r_p$  and the ambient plasma condition of  $n_0$  and  $kT_0$ , the mass ablation rate,  $G$ , and the state of the ablatant,  $p_*$  and  $kT_*$ , are still undeter-

mined. In practice, this implies that based on the expected value of  $\tilde{E}$ , one must first guess a proper value of  $E_*$  ( $E_* = 2kT_0/\tilde{E}$ ), and calculate  $\hat{r}, \tilde{q}$  and  $\tilde{E}$  which, in turn, give a set of calculated  $r_p, q_0$ , and  $kT_0$ . The process is to be iterated until the calculated values of  $r_p, q_0$ , and  $kT_0$  agree reasonably well with their initial given values.

### 2.5. The asymptotic solutions

From the computational results, we notice that once the ablated flow passes beyond the sonic radius, both the electron energy flux  $q$  and the energy  $E'$  approach their corresponding values of the ambient plasma quickly. This indicates that asymptotic solutions of the flow parameters might exist at a sufficiently larger value of  $r$ .

To study this possibility, we introduce a new variable

$$\mu = v^2/\theta, \quad (43)$$

or  $\mu \equiv M^2$ , to replace the dependent variable  $\theta$ . The system of differential equations, Eqs. (7)-(10), now takes the following form:

$$\frac{dv}{dr} = \frac{2V}{1-\mu} \left[ \frac{\Lambda' q \mu}{v^3} - \frac{1}{r} \right], \quad (44)$$

$$\frac{d\mu}{dr} = \left[ \frac{(\gamma-1)\mu^2 + 2\mu}{v} \right] \frac{dv}{dr} - 2\Lambda' \frac{q\mu^2}{v^3}, \quad (45)$$

$$\frac{dq}{dr} = \lambda_* \frac{\Lambda' q}{r^2 v}, \quad (46)$$

$$\frac{dE'}{dr} = 2\lambda_* \left[ \frac{L(E)}{E_* \Lambda_*} \right] \frac{1}{r^2 v}. \quad (47)$$

Assuming that  $\lambda, q$ , and  $\mu$  are slowly varying functions of  $r$ , for  $r \gg r_0$ , we may put

$$1-\mu = A(r), \quad \Lambda' q \mu = B(r), \quad (48).$$

Eq. (44) may then be written as

$$\frac{dv}{dr} = 2 \frac{V}{A} \left[ \frac{B}{v^3} - \frac{1}{r} \right] \quad (49)$$

As a first approximation, neglecting  $1/r$  and considering  $A$  and  $B$  as constants, we have

$$\frac{dv}{dr} = 2 \frac{B}{A} \frac{1}{v^2} \quad \text{or } v^3 \sim r ,$$

we then may put

$$v(r) = y(r)r^{1/3}, \quad (50)$$

After substituting this into Eq. (49), we obtain

$$\frac{dy}{2 \frac{B}{A} \frac{1}{y^2} - 2 \left( \frac{1}{A+6} \right) y} = \frac{dr}{r} \quad (51)$$

Introducing  $C_1 = 2 \frac{B}{A}$ ,  $C_2 = -2 \left( \frac{1}{A} + \frac{1}{6} \right)$

then

$$\begin{aligned} \frac{C_1}{C_2} &= - \frac{B}{\left(1 + \frac{A}{6}\right)} \\ &= - 6 \frac{\Lambda' q \mu}{7 - \mu} \end{aligned} \quad (52)$$

Denoting all asymptotic values of the variables concerned by " $\sim$ ", we now impose the condition that for  $r \gg r_0$

$$\frac{C_1}{C_2} = - 6 \frac{\tilde{\Lambda}' \tilde{q} \tilde{\mu}}{7 - \tilde{\mu}} = \text{constant.} \quad (52a)$$

Eq. (51) can be written as

$$\frac{3y^2 dy}{\frac{C_1}{C_2} + y^3} = 3 C_2 \frac{dr}{r} \quad (53)$$

Carrying out the integration from  $r_0$  to  $r$ , we obtain

$$\frac{C_1/C_2 + y^3}{C_1/C_2 + y_0^3} = \left(\frac{r}{r_0}\right)^{3C_2} .$$

Solving the above equation for  $y^3$ , we find

$$y^3 = \left(\frac{r}{r_0}\right)^{3C_2} \left[ \left(\frac{C_1}{C_2}\right) + y_0^3 \right] - \frac{C_1}{C_2} . \quad (54)$$

If we require that  $y = \text{constant}$  for  $r > r_0$ , we have

$$y_0^3 = \frac{v_0^3}{r_0^3} = -\frac{C_1}{C_2} = 6 \frac{\tilde{\lambda} \tilde{q} \tilde{\mu}}{7-\tilde{\mu}} , \quad (55)$$

then

$$y = \left(-\frac{C_1}{C_2}\right)^{1/3} = \left(\frac{6 \tilde{\lambda} \tilde{q} \tilde{\mu}}{7-\tilde{\mu}}\right)^{1/3} , \quad (56)$$

or

$$\tilde{v}(r) = \left(\frac{6 \tilde{\lambda} \tilde{q} \tilde{\mu}}{7-\tilde{\mu}}\right)^{1/3} r^{1/3} . \quad (57)$$

From Eq. (45), when  $\mu \rightarrow \tilde{\mu}$ , or  $\frac{d\mu}{dr} = 0$ , we have

$$\tilde{v}^2 \frac{d\tilde{v}}{dr} = \frac{\Lambda' q}{\frac{\gamma-1}{2} + \frac{1}{\tilde{\mu}}} . \quad (58)$$

Substituting Eq. (57) into (58), after rearranging the terms, we obtain finally

$$\tilde{\mu} = 5/\gamma . \quad (59)$$

Using Eq. (57) we eliminate  $\tilde{v}$  in (58) and get

$$\tilde{v} = \left(\frac{30 \tilde{\lambda} \tilde{q}}{7\gamma-5}\right)^{1/3} r^{1/3} . \quad (60)$$

Similarly

$$\tilde{\theta} = \frac{\tilde{v}^2}{\tilde{\mu}} = \frac{\gamma}{5} \left(\frac{30 \tilde{\lambda} \tilde{q}}{7\gamma-5}\right)^{1/3} r^{2/3} , \quad (61)$$

$$\tilde{\rho} = \frac{1}{\tilde{v} r^2} = \left(\frac{30 \tilde{\lambda} \tilde{q}}{7\gamma-5}\right)^{-1/3} r^{-7/3} \quad (62)$$



### 3. COMPUTATIONAL CODE AND GENERAL RESULTS

To facilitate numerical computations, as shown in Table I, a change of notation was made. Notice that the dependent variable  $v$ ,  $\theta$ ,  $q$ ,  $E$  and their derivatives are denoted by  $Y1$ ,  $Y2$ ,  $Y3$ ,  $Y4$  and  $Z[1]$ ,  $z[2]$ ,  $z[3]$ ,  $z[4]$  in the procedure  $F(X, Y, Z)$ , they are denoted by  $YY[1,1]$ ,  $YY[1,2]$ ,  $YY[1,3]$ ,  $YY[1,4]$  and  $YY[2,1]/H$ ,  $YY[2,2]/H$ ,  $YY[2,3]/H$  and  $YY[2,4]/H$ , respectively, in the integration procedure  $DIFSUB$ .

When we proceed to integrate the system of equations, Eqs. (7)-(10), from the sonic radius inward towards the pellet surface, we expect a steep drop in the values of  $q$  and  $E$ . On the other hand, when we integrate from the sonic radius outward, we expect a slow rise in the values of  $q$  and  $E$  towards the ambient plasma condition of  $q_0$  and  $E_0$ . Based on these considerations, we adopted the  $DIFSUB$  method<sup>(3)</sup> to carry out the integration. This is because this integration procedure is essentially a predictor-corrector method and the integration steps are self-adjustable.

By using the procedure  $RISOE/DIFSUB/A$ <sup>(4)</sup>, the system of equations, Eqs. (7)-(10), was integrated numerically. The boundary condition, Eq. (31), at the far downstream region, however, was replaced by

$$M = \sqrt{5/\gamma} \quad \text{for } r \geq r_*$$

A program named  $PELREF$  (abbreviation for pellet refuelling) was then written in the Algol language. The general computational results for a range of  $E_*$  ( $1 \times 10^2 - 4 \times 10^4$  eV) are shown in Table II. In the table,  $\hat{r}$  is normalized pellet radius, i.e.  $\hat{r} = r_p/r_*$  and  $r_M$  is the normalized ablated cloud boundary where the flow Mach number is within  $10^{-3}$  of its asymptotic value.

To display the results obtained, three different types of plotting programs were also written.

The PELREF/CURVE shows the computed results in graphic form from the pellet surface outward to a radial distance of seven times the sonic radius. Some typical results are shown in Fig. 1a and Fig. 2a. A detailed description of the program is given in the appendix.

PELREF/CL shows the results of the subsonic region in further detail.

PELREF/ASYMP shows the results in the supersonic region from the sonic radius  $r = 1$  to a distance of  $r = 25$  and compares the results with the asymptotic solutions of Section 2.5. Computational results indicate that for an ablatant with specific heat ratio  $\gamma = 1.4$  in the range of  $E_*$  investigated, the flow parameters already reach their asymptotic values at a distance of ten times the sonic radius. Typical results are shown in Fig. 1b and Fig. 2b, respectively.

Table I. Corresponding notations used in the analysis and in the program.

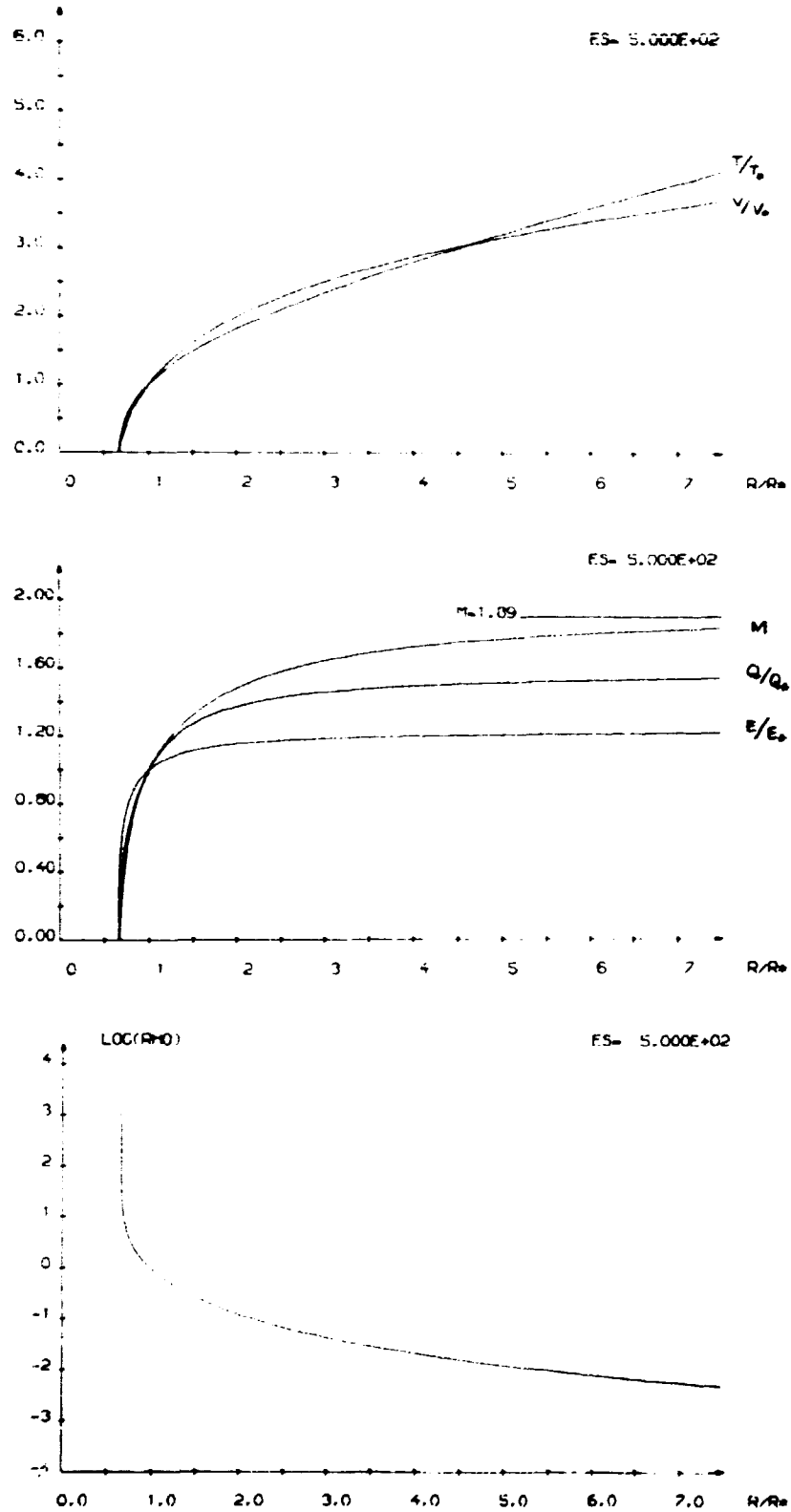
| <u>Symbols used in the analysis</u>       | <u>Symbols used in the program</u> |
|-------------------------------------------|------------------------------------|
| $L(E)$                                    | L                                  |
| $\sigma(E)$                               | S                                  |
| $\lambda(E)$                              | A                                  |
| $E_*$                                     | ES                                 |
| $\Lambda_* \equiv \Lambda(E_*)$           | AS                                 |
| $\Lambda'(E) \equiv \Lambda(E)/\Lambda_*$ | AO                                 |
| $L(E_*)$                                  | LS                                 |
| $\sigma(E_*)$                             | SS                                 |
| $(d\sigma/dE)E = E_*$                     | DS                                 |
| $\lambda_*$                               | C                                  |
| $N_*$                                     | NS                                 |
| $\gamma$                                  | G                                  |
| $r$                                       | X                                  |
| $v$                                       | Y1, YY[1,1]                        |
| $\theta$                                  | Y2, YY[1,2]                        |
| $q$                                       | Y3, YY[1,3]                        |
| $E'$                                      | Y4, YY[1,4]                        |
| $dv/dr$                                   | Z[1], YY[2,1]/H                    |
| $d\theta/dr$                              | Z[2], YY[2,2]/H                    |
| $dq/dr$                                   | Z[3], YY[2,3]/H                    |
| $dE'/dr$                                  | Z[4], YY[2,4]/H                    |

Table II. Summary of computational results ( $\gamma = 1.4$ )

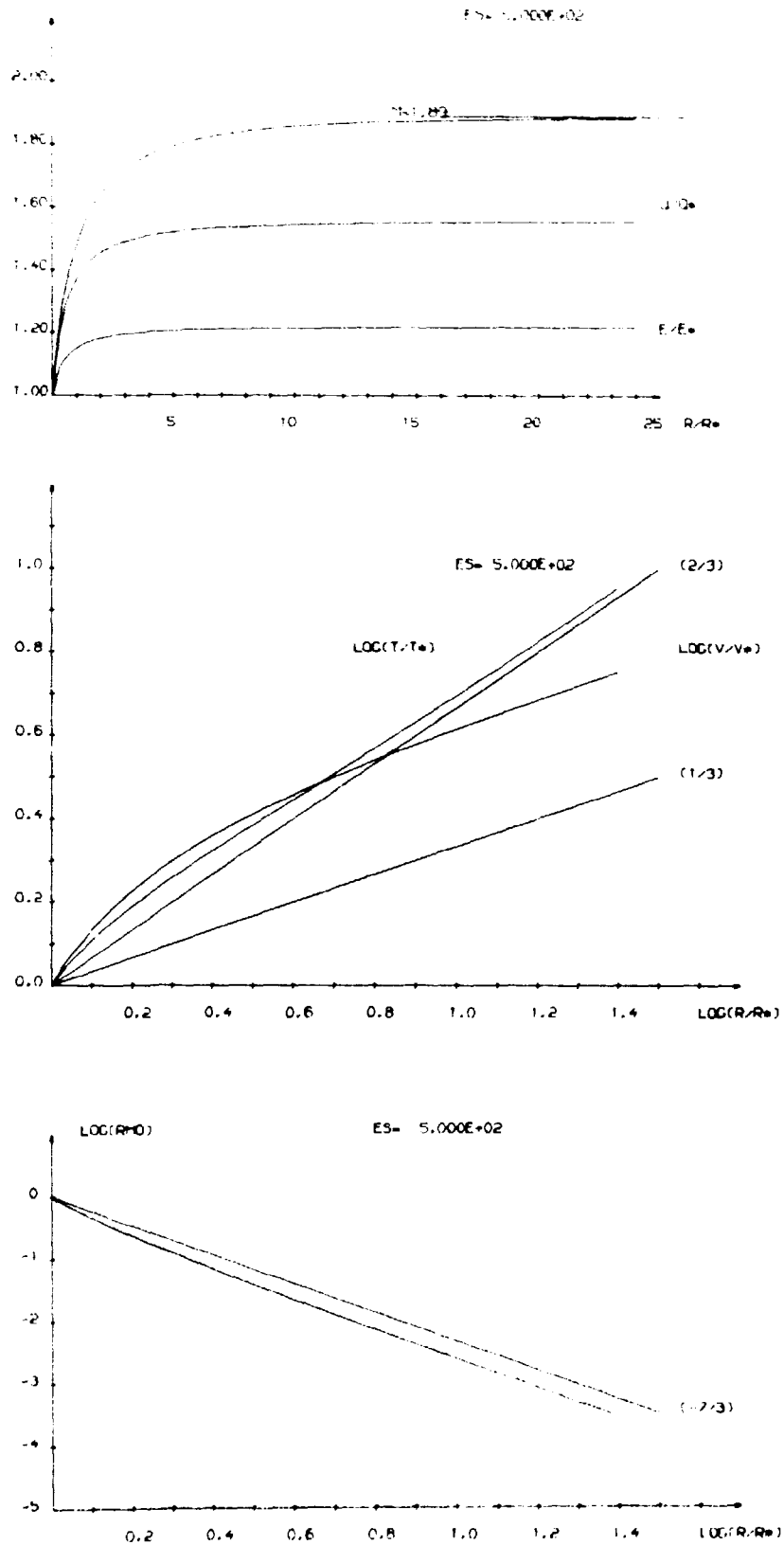
| Es<br>(eV) | AS          | NS       | C      | $\tilde{q}$ | $\tilde{E}$ | f      | $r_M$ | $KT_O$<br>(eV) |
|------------|-------------|----------|--------|-------------|-------------|--------|-------|----------------|
| 1.0 E 02   | 1.8080 E-16 | -0.37499 | 0.9203 | 1.548       | 1.181       | 0.5990 | 93    | 5.9050 E 01    |
| 3.0 E 02   | 4.3255 E-17 | -0.60708 | 0.9712 | 1.557       | 1.212       | 0.6509 | 48    | 1.8180 E 02    |
| 5.0 E 02   | 2.0633 E-17 | -0.66295 | 0.9853 | 1.557       | 1.218       | 0.6623 | 43    | 3.0450 E 02    |
| 7.5 E 02   | 1.1133 E-17 | -0.69458 | 0.9904 | 1.560       | 1.218       | 0.6697 | 38    | 4.5675 E 02    |
| 1.0 E 03   | 7.0809 E-18 | -0.70825 | 1.0016 | 1.560       | 1.218       | 0.6717 | 38    | 6.0900 E 02    |
| 2.0 E 03   | 2.2810 E-18 | -0.70755 | 0.9961 | 1.557       | 1.204       | 0.6750 | 38    | 1.2040 E 03    |
| 5.0 E 03   | 4.7948 E-19 | -0.64405 | 0.9844 | 1.561       | 1.178       | 0.6659 | 51    | 2.9450 E 03    |
| 7.0 E 03   | 2.6786 E-19 | -0.60967 | 0.9761 | 1.561       | 1.167       | 0.6604 | 61    | 4.0845 E 03    |
| 3.0 E 04   | 2.1256 E-20 | -0.44642 | 0.9361 | 1.560       | 1.119       | 0.6285 | 107   | 1.6785 E 04    |
| 4.0 E 04   | 1.2882 E-20 | -0.41598 | 0.9286 | 1.559       | 1.111       | 0.6218 | 128   | 2.2220 E 04    |

REFERENCES

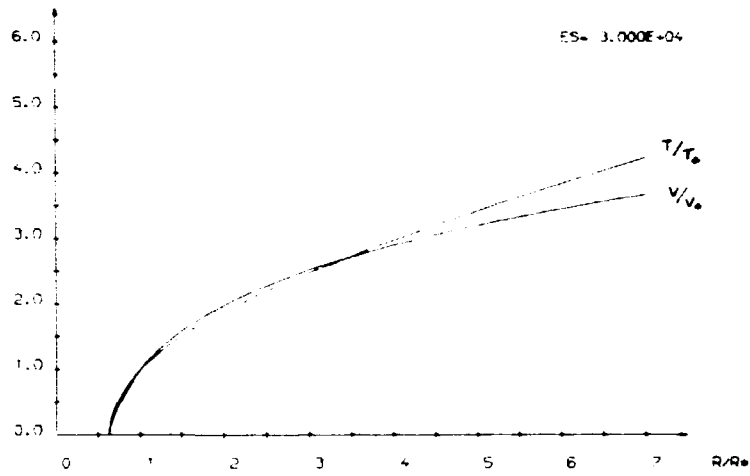
- 1) PARKS, P.B., TURNBULL, R.J. (1978). Phys. Fluids 21, 1735.
- 2) PARKS, P.B. (1977). "Model of the Ablating Solid Hydrogen Pellet in a Plasma", Dissertation, University of Illinois.
- 3) GEAR, C.W. (1971). "Numerical Initial Value Problems in Ordinary Differential Equations", Prentice-Hall pp. 158-166.
- 4) RISOE/DIFFSUB/A, Risoe Computing Machine Library.



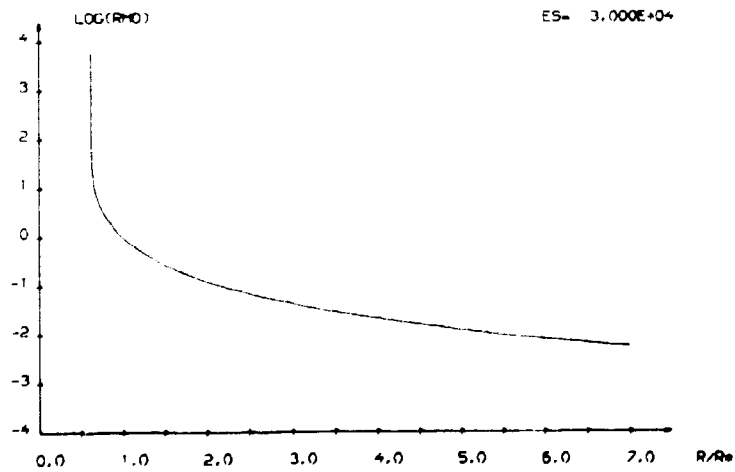
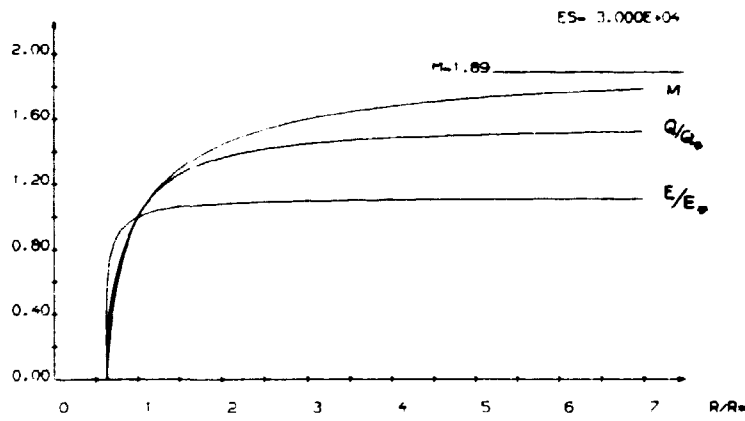
**Fig. 1a.** Dimensionless temperature,  $T/T_0$ , flow velocity,  $v/v_0$ , density,  $RHO = \rho/\rho_0$ , Mach number,  $M$ , incident electron energy flux,  $Q/Q_0$ , and incident electron energy  $E/E_0$ , versus dimensionless radius  $R/R_0$ . Incident electron energy at the sonic radius  $R_0$ ,  $ES = 500$  eV ( $kT_0 = 305$  eV). The surface of the pellet is located at  $\hat{r} = 0.6623$ .



**Fig. 1b.** Comparison of the dimensionless flow parameters  $v/v_0$ ,  $T/T_0$ , and  $\rho/\rho_0$  in the supersonic region obtained from the numerical integration with their corresponding asymptotic solutions (curves denoted by the bracket). Incident electron energy at the sonic radius  $ES = 500$  eV. The asymptotic values of  $Q/Q_0$ , and  $E/E_0$ , are 1.557 and 1.218, respectively.

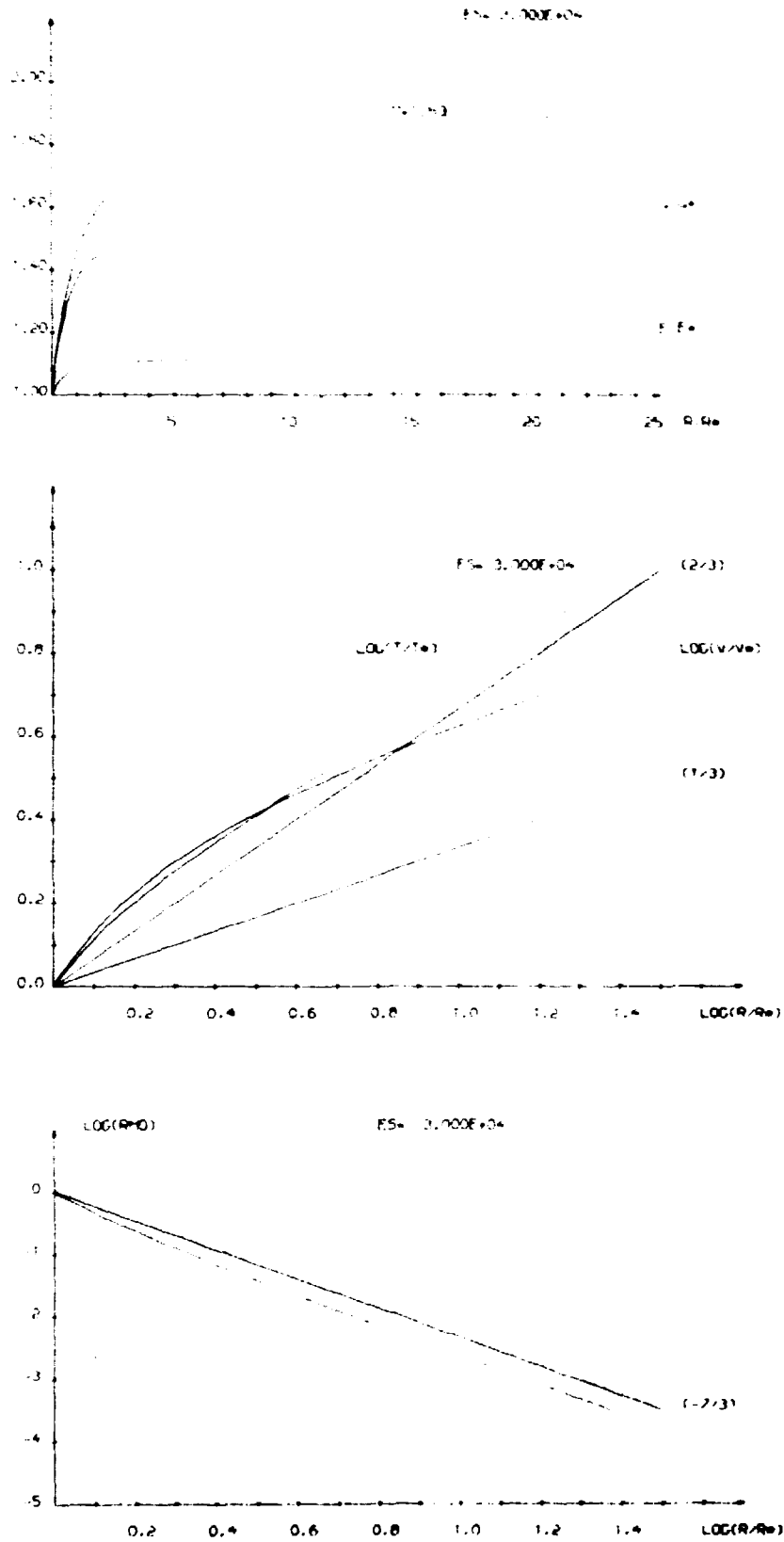


PLOT NO. 01  
EFF: 52%, PLOTTIME: 107 SECS.



**Fig. 2a.** Dimensionless flow parameters of the ablatant, incident electron energy and energy flux versus dimensionless radius,  $R/R_0$ . Incident electron energy at the sonic radius,  $ES = 3 \times 10^4$  eV ( $kT_0 = 1.68 \times 10^4$  eV). The surface of the pellet is located at  $\hat{r} = 0.6285$ .





**Fig. 2b.** Comparison of the dimensionless flow parameters  $V/V_0$ ,  $T/T_0$ , and  $\rho/\rho_0$  in the supersonic region obtained from the numerical integration with their corresponding asymptotic solutions (curves denoted by the brackets). Incident electron energy at the sonic radius  $ES = 3 \times 10^4$  eV. The asymptotic values of  $Q/Q_0$  and  $E/E_0$  are 1.560 and 1.119, respectively.

**APPENDIX**

**Detailed description of the program PELREF/CURVE and the accompanying procedure PELAB.**

PELREF/CURVE (15/J4/41)

```
130  $ SET INSTALLATION
230  $ BEGIN
330  $ COMMENT ::::::::::::::::::::::::::::::::::::::::::::::::::::
430  $       THIS PROGRAM USES THE PROCEDURE PELAB TO PLOT THE
530  $       COMPUTATED RESULTS FROM THE PELLEY SURFACE UP TO A
630  $       DISTANCE OF SEVEN TIMES THE SONIC RADIUS
730  $       ::::::::::::::::::::::::::::::::::::::::::::::::::::
830
930  $ INCLUDE "RISOE/PLUTSTART/A"
1030 $ INCLUDE "RISOE/PLUTAXES/A"
1130 $ INCLUDE "RISOE/PLUTLIL/A"
1230 FILE INP (KIND =DISK,FILETYPE=7), OUT (KIND =PRINTER)
1330 REAL ES,AG,C,K,M,XMAX,XMIN,RHMIN,RHMAX,QMAX,EMAX,PR,NP
1430 INTEGER I,I*MAX,M,B,IA,X,M,L,B,J
1530 ARRAY XS(0:200),XL(0:200),RS(0:0.0:200),RL(0:0:200)
1630 $ INCLUDE "PELAR/A"
1730
1830 WRITE(OUT, </"PROGRAM PELREF/CURVE"/>)
1930
2030 $ COMMENT ::::::::::::::::::::::::::::::::::::::::::::::::::::
2130 $       THE INPUT DATA IS GIVEN BY DATAPEL
2230 $       ::::::::::::::::::::::::::::::::::::::::::::::::::::
2330 READ(INP, <ES,K,XMAX,PR,NP>)
2430 WRITE(OUT, <"ES="E10.3, " K="F6.5, " XMAX="F6.2>, ES,K,XMAX)
2530 PELAB(ES,K,XMAX,PR,NP)
2630
2730 $ COMMENT ::::::::::::::::::::::::::::::::::::::::::::::::::::
2830 $       NOW BEGIN THE PLUTTING
2930 $       ::::::::::::::::::::::::::::::::::::::::::::::::::::
3030
3130   DELTAX:= 0.75/200; DELTAY:=0.1/50;
3230   SETORIG(0.3,0);
3330   PLUTAXES(0,0,0,7.5,7.5,2,0,5,0,2);
3430   PLUTSTRING((STRINGBUFF(=1,<"R/A">),7.0,-0.2,0.3);
3530   FOR M=7 STEP -1 UNTIL 0 DO
3630   PLUTSTRING((STRINGBUFF(=1,<"I">M),M-0.15,-0.2,0.3);
3730   FOR M=0 STEP 3.4 UNTIL 7.0 DO
3830   PLUTSTRING((STRINGBUFF(=1,<"F5.2">,M),-0.6,M,0.3);
3930   PLUTSTRING((STRINGBUFF(=1,<"ES="E10.3>,ES),0.2,0.7);
4030   PLUTSTRING((STRINGBUFF(=1,<"M=1.89">),4.5,1.89,0.3);
4130   PLOTLINE(5.2,1.89,7.5,1.89);
4230   XS(0)=1; FOR I=1,2,3,4,5,6 DO RS(I,0)=1;
4330   XL(0)=1; FOR I=1,2,3,4,5,6 DO RL(I,0)=1;
4430   FOR J=3,4,5,6 DO
4530   BEGIN 3;SETCHAR("3"); 4;SETCHAR("4"); 5;SETCHAR("6"); END;
4630   FOR I=IMAX STEP -1 UNTIL 1 DO
4730   PLOTLINE(XS(I),RS(J,1),XS(I-1),RS(J,1));
4830   FOR B=M STEP 1 UNTIL MMAX-1 DO
4930   PLOTLINE(XL(B),RL(J,B),XL(B+1),RL(J,B+1));
5030   END;
5130   DELTAX:=0.1; DELTAY:=0.1;
5230 $ ::::::::::::::::::::::::::::::::::::::::::::::::::::
5330 $ STARTPLUT;
5430   DELTAX:= 0.75/200; DELTAY:=0.1/20;
5530   SETORIG(0.3,0);
5630   PLUTAXES(0,0,0,7.5,7.6,5,0,5,0,5);
5730
5830   PLUTSTRING((STRINGBUFF(=1,<"H/A">),7.4,-0.5,0.3);
5930   FOR M=7 STEP -1 UNTIL 0 DO
6030   PLUTSTRING((STRINGBUFF(=1,<"I">M),M-0.15,-0.5,0.3);
6130   FOR M=0 STEP 1 UNTIL 4 DO
6230   PLUTSTRING((STRINGBUFF(=1,<"F4.1">,M),-0.6,M,0.3);
6330   PLUTSTRING((STRINGBUFF(=1,<"ES="E10.3>,ES),6.6,0.3);
6430   XS(0)=1; FOR I=1,2,3,4,5,6 DO RS(I,0)=1;
6530   XL(0)=1; FOR I=1,2,3,4,5,6 DO RL(I,0)=1;
6630   FOR J=1,2 DO
6730   BEGIN 2;SETCHAR("1"); 2;SETCHAR("2"); END;
6830   FOR I=IMAX STEP -1 UNTIL 1 DO
6930   PLOTLINE(XS(I),RS(J,1),XS(I-1),RS(J,1));
7030   FOR B=M STEP 1 UNTIL MMAX-1 DO
7130   PLOTLINE(XL(B),RL(J,B),XL(B+1),RL(J,B+1));
7230   END;
7330   DELTAX:=0.1; DELTAY:=0.1;
7430 $ ::::::::::::::::::::::::::::::::::::::::::::::::::::
7530 $ STARTPLUT;
7630   N:= ENTIER( LOG(ABS(RHMIN)) )-1; WRITE(OUT, <"N="I3>,N);
7730   NL:= ENTIER( LOG(ABS(RHMAX)) )+1; WRITE(OUT, <"NL="I3>,NL);
7830   DELTAX:=0.75/200; DELTAY:=0.1*(NL-N)/120;
7930   SETORIG(0.3,-N);
8030   PLUTAXES(0,0,0,7.5,7.5,0,0,4,0,2,1,0);
8130   PLUTSTRING((STRINGBUFF(=1,<"R/A">),7.0,N-0.05,0.3);
8230   FOR M=7 STEP -1 UNTIL 0 DO
8330   PLUTSTRING((STRINGBUFF(=1,<"F4.1">,M),M-0.15,N-0.65,0.3);
8430   FOR M=N STEP 1 UNTIL NL DO
8530   PLUTSTRING((STRINGBUFF(=1,<"I">M),M-0.45,M,0.3);
8630   PLUTSTRING((STRINGBUFF(=1,<"LOG(RH)>"),0.45,NL+0.4,0.3);
8730   PLUTSTRING((STRINGBUFF(=1,<"ES="E10.3>,ES),6,NL+0.4,0.3);
8830   SETCHAR("N");
8930   XS(0)=1; RS(0)=1;
9030   FOR I=IMAX STEP -1 UNTIL 1 DO
9130   PLOTLINE(XS(I),LOG(ABS(XS(I))),XS(I-1),LOG(ABS(RS(I-1)))));
9230   XL(0)=1; RL(0)=1;
9330   FOR B=N STEP 1 UNTIL MMAX-1 DO
9430   PLOTLINE(XL(B),LOG(RL(B,N)),XL(B+1),LOG(RL(B,N)));
9530
9630 $ INCLUDE "RISOE/PLUTSLUT/A"
9730 $ END OF PROGRAM.
9830
```

ORACLE: PELL474 (M/7/5/11)

```

1000 PROCEDURE PCLARE(FS,K,XMAX,PR,MP);
1010 VALUE ES,K,XMAX,PR,MP; REAL ES,K,XMAX,PR,MP;
1020
1030 JEGI. COMMENT '::::::::::::::::::::::::::::::::::::::::::::::::::::::::::::';
1040 ' THIS PROCEDURE USES THE QUAD50 METHOD TO CALCULATE '
1050 ' THE RELATION OF A REFUELLING PELLETT '
1060 ' ::::::::::::::::::::::::::::::::::::::::::::::::::::::';
1070
1080 LABEL SLUT-REP-LEFT;
1090 INTEGER N,IA,J,START;
1100 REAL X,ZS,XL,XS,SS,SSS,OHU,WACH,PI;
1110 REAL M,HC,CMJ,UMHAX,EPS,MF;
1120 ARRAY SAVE,VY(318,0:4),Y(14,0:1),YMAX,ERROR,Y,Z,INT(N:1);
1130 PROCEDURE DERIV(X,Y,PH,PI);VALUE N;INTEGER N;ARRAY X,Y(0,PH);
1140 BEGIN;
1150 PROCEDURE FCS(Y,Z); VALUE X; REAL X; ARRAY Y,Z(1);
1160 REAL X;
1170 X:=L+0.4*AD*(Y(2)-Y(1))+Y(1);
1180 Y(1):=Y(1); Y(2):=Y(2); Y(3):=Y(3); Y(4):=Y(4);
1190 IF Y(1) > 0 AND X <= PH THEN
1200 SEU(Y);
1210 L:=X;
1220 X:=L/2.34*(1+0.11*(E+2)+17/E+2);
1230 IF E > 100 THEN X:=0.04+13/E+1.71-1.62*12/L+1.032;
1240 ELSE X:=1.13*(1+E);
1250 X:=X+L/4;
1260 X:=X+X*AS;
1270 IF Y(2)=0 THEN Z(1):=ZS ELSE
1280 Z(1):=2*Y(1)+Y(2)/(Y(2)-Y(1))-2*(AD*Y(3)/(Y(2)-Y(1))-1/X);
1290 Z(2):=AD*Y(1)-0.4*(Y(2)-Y(1));
1300 Z(3):=0.4*(Y(3)/(Y(1)+0.2));
1310 Z(4):=2*(L-X)/(ES+AS)/(Y(1)+0.2);
1320
1330 END;
1340 GOTO SLUT;
1350 END;
1360
1370 PROCEDURE "ISOP/DIFSUB/A";
1380
1390 ZS:=2/3*(1-53*Y(2.975-1.07*(K)));
1400 WRITE(OUT,4*ZS,"E11.4D,24);
1410 SS:=1/2.35*(1+0.11*(ES+20)/ES+2); WRITE(OUT,4*SS,"F10.7D,24);
1420 SS:=1/ES+10.8; EN:=0.1*(ES+1)/ES+1.71-1.62*12/ES+1.032;
1430 WRITE(OUT,4*EN,"E10.3D,24);
1440 AS:=2*SS/ES;
1450 WRITE(OUT,4*AS,"E11.4D,24);
1460 JS:=1/ES+10.8; EN:=1.50*(12/ES+2.71+3.1298*12/ES+2.932;
1470 ELSE -1.13*(1+E)/ES+2;
1480 WRITE(OUT,4*JS,"E10.3D,24);
1490 WACH:=1/PH*(1+0.11*(ES+20)/ES+2)*SS*(4*11*(ES+40)/ES+2)*LS+(1-DS);
1500 C:=1/PH*(1+0.11*(ES+20)/ES+2);
1510 WRITE(OUT,4*C,"E11.4D,24);
1520
1530 COMMENT '::::::::::::::::::::::::::::::::::::::::::::::::::::::::::::';
1540 ' NOW BEGIN THE INTEGRATION '
1550 ' ::::::::::::::::::::::::::::::::::::::::::::::::::::::';
1560
1570 EP:=14*(1-53*Y(2.975-1.07*(K))); XMAX:=41; N:=10; M:=10;
1580
1590 BEGIN;
1600 JSTART:=0; IF I=2;
1610 THEN I:=I+1; THEN I:=I+1; THEN I:=I+1; THEN I:=I+1; THEN I:=I+1;
1620 Y(1):=Y(1); Y(2):=Y(2); Y(3):=Y(3); Y(4):=Y(4);
1630 Y(1):=Y(1); Y(2):=Y(2); Y(3):=Y(3); Y(4):=Y(4);
1640 WRITE(OUT,4*Y(1),4*Y(2),4*Y(3),4*Y(4),4*Y(1),4*Y(2),4*Y(3),4*Y(4),
1650 "X12.0E",X10);
1660 FOR I:=1 STEP 1 UNTIL 4 DO Y(1):=Y(1);
1670 Y(1):=Y(1);
1680 WRITE(OUT,4*Y(1),4*Y(2),4*Y(3),4*Y(4),Z(1),Z(2),Z(3),Z(4),M);
1690 IF I=4 THEN GO TO LEFT ELSE
1700 BEGIN;
1710 FOR I:=1 TO 4 WHILE X <= XMAX AND WACH <= SORT(25/7) AND
1720 SIGN(A) <= SIGN(S);
1730 BEGIN;
1740 RHM:=1; OHU:=1; EPS:=1;
1750 DIFSUB(4,X,Y,SAVE,RHM,UMHAX,EPS,MF,YMAX,ERROR,KFLAG,JSTART,
1760 PI,PH);
1770 RHM:=1/(Y(1)-1);
1780 PI:=RHM*Y(1);
1790 WACH:=Y(1)/SORT(Y(1,2));
1800 R(1):=Y(1);
1810 R(2):=Y(1); R(3):=Y(1,2); R(4):=Y(1,3);
1820 R(5):=Y(1,4); R(6):=RHM; R(7):=RHM; R(8):=RHM;
1830 OHU:=MAX(OHU,RHM); EPS:=MAX(EPS,Y(1));
1840 EN:=MAX(EN,RHM);
1850 END;
1860 WRITE(OUT,4*Y(1),4*Y(2),4*Y(3),4*Y(4),Y(1),Y(2),Y(3),Y(4),
1870 "X12.0E",X10);
1880 WRITE(OUT,4*Y(1),4*Y(2),4*Y(3),4*Y(4),R(1),R(2),R(3),R(4),R(5),R(6),R(7),R(8),
1890 "X12.0E",X10);
1900 RHM:=RHM*Y(2)/Y(1);
1910 WRITE(OUT,4*Y(1),4*Y(2),4*Y(3),4*Y(4),RHM,OHU,EN);
1920 WRITE(OUT,4*Y(1),4*Y(2),4*Y(3),4*Y(4),RHM,OHU,EN);
1930 WRITE(OUT,4*Y(1),4*Y(2),4*Y(3),4*Y(4),RHM,OHU,EN);
1940 WRITE(OUT,4*Y(1),4*Y(2),4*Y(3),4*Y(4),RHM,OHU,EN);
1950 END;
1960 H:=N; HMAX:=0; IS GO TO REP;
1970
1980 LEFT;
1990 FOR I:=1 TO 4 WHILE Y(1) <= SAVE(I,1) AND Y(1,3) > 0;
2000 BEGIN;
2010 RHM:=1; OHU:=1; EPS:=1;
2020 DIFSUB(4,X,Y,SAVE,RHM,UMHAX,EPS,MF,YMAX,ERROR,KFLAG,JSTART,
2030 PI,PH);
2040 RHM:=1/(Y(1)-1);
2050 PI:=RHM*Y(1);
2060 WACH:=Y(1)/SORT(Y(1,2));
2070 R(1):=Y(1);
2080 R(2):=Y(1); R(3):=Y(1,2); R(4):=Y(1,3);
2090 R(5):=Y(1,4); R(6):=RHM; R(7):=RHM; R(8):=RHM;
2100 OHU:=MAX(OHU,RHM); EPS:=MAX(EPS,Y(1));
2110 EN:=MAX(EN,RHM);
2120 END;
2130 WRITE(OUT,4*Y(1),4*Y(2),4*Y(3),4*Y(4),Y(1),Y(2),Y(3),Y(4),
2140 "X12.0E",X10);
2150 WRITE(OUT,4*Y(1),4*Y(2),4*Y(3),4*Y(4),R(1),R(2),R(3),R(4),R(5),R(6),R(7),R(8),
2160 "X12.0E",X10);
2170 RHM:=RHM*Y(2)/Y(1);
2180 WRITE(OUT,4*Y(1),4*Y(2),4*Y(3),4*Y(4),RHM,OHU,EN);
2190
2200
2210 WRITE(OUT,4*Y(1),4*Y(2),4*Y(3),4*Y(4),RHM,OHU,EN);
2220 WRITE(OUT,4*Y(1),4*Y(2),4*Y(3),4*Y(4),RHM,OHU,EN);
2230
2240 SLUT;
2250 WRITE(OUT,4*Y(1),4*Y(2),4*Y(3),4*Y(4),RHM,OHU,EN);
2260 WRITE(OUT,4*Y(1),4*Y(2),4*Y(3),4*Y(4),RHM,OHU,EN);
2270
2280 END PCLARE;

```

2219

Risø - M -

|                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    |                                                            |
|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------|
| <p>Title and author(s)</p> <p>PELREF</p> <p>(A numerical code for computing the ablated state of a refuelling pellet)</p> <p>C.T. Chang</p>                                                                                                                                                                                                                                                                                                                                                                                        | <p>Date</p> <p>May 1981</p>                                |
| <p>27 pages + tables + illustrations</p>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | <p>Department or group</p> <p>Physics</p>                  |
| <p>Abstract</p> <p>Assuming a constant specific heat ratio and using the neutral shielding model, this report presents a numerical code for calculating the ablation rate and the state of the ablatant of a refuelling pellet. Results are given for plasma conditions corresponding to present and to future toroidal devices.</p> <p>Available on request from Risø Library, Risø National Laboratory (Risø Bibliotek), Forsøgsanlæg Risø), DK-4000 Roskilde, Denmark<br/>Telephone: (02) 37 12 12, ext. 2262. Telex: 43116</p> | <p>Group's own registration number(s)</p> <p>Copies to</p> |