# The Multi-Detector Powder Neutron Diffractometer at Risø National Laboratory 

Als-Nielsen, Jens Aage; Andersen, Niels Hessel; Broholm, C.; Clausen, K.N.; Lebech, Bente

Publication date:
1988

Document Version
Publisher's PDF, also known as Version of record

Link back to DTU Orbit

Citation (APA):
Als-Nielsen, J. A., Andersen, N. H., Broholm, C., Clausen, K. N., \& Lebech, B. (1988). The Multi-Detector Powder Neutron Diffractometer at Risø National Laboratory. (Risø-M; No. 2720).

## DTU Library

Technical Information Center of Denmark

## General rights

Copyright and moral rights for the publications made accessible in the public portal are retained by the authors and/or other copyright owners and it is a condition of accessing publications that users recognise and abide by the legal requirements associated with these rights.

- Users may download and print one copy of any publication from the public portal for the purpose of private study or research
- You may not further distribute the material or use it for any profit-making activity or commercial gain
- You may freely distribute the URL identifying the publication in the public portal


# The Multi-Detector <br> Powder Neutron Diffractometer at Risø National Laboratory 

J. Als-Nielsen, N. H. Andersen, C. Broholm, K.N. Clausen and B. Lebech


#### Abstract

The report describes a new multi-detector powder neutron diffractometer installed at the DR3 reactor at Risø. The report gives details of the design criteria and operating instructions in order to ease operation of the instrument by actual and potential users. The individual components (collimators, monochromator, detectors) are described in detail. An example of a study of the oxygen uptake of $\mathrm{YBa}_{2} \mathrm{Cu}_{3} \mathrm{O}_{7 \text {-x }}$ is given.


## Risø National Laboratory, DK-4000 Roskilde, Denmark June 1988

ISBN 87-550-1434-8
ISSN 0418-6435
Grafisk Service, Riso

## Contents

Page

1. Introduction ..... 5
1.1. Principles of Powder Diffraction ..... 5
1.2. Design Criteria ..... 7
2. Monochromator ..... 9
2.1. Lattice Spacing ..... 9
2.2. Higher Order Contamination ..... 9
2.3. Mosaicity ..... 10
2.4. Sagital Focussing ..... 10
3. Collimators ..... 10
4. Detectors and Electronics ..... 12
5. Powder Spectrum Resolution ..... 12
6. Software ..... 14
6.1. Single Detector Mode ..... 14
6.2. Multi Detector Mode ..... 15
7. Lining-up the Multi-Detector Diffractometer ..... 16
7.1. Monochromator ..... 17
7.2. Monochromator-Sample Collimator ..... 17
7.3. Sample Table Alignment ..... 17
7.4. Sample Scattering Angle ..... 18
7.5. Detector-Bank Collimator Alignment ..... 18
7.6. Monochromator Scattering Angle ..... 18
8. Example of a Structure Study ..... 18
8.1. Phase Equilibrium and Kinetics of the Uptake of Oxygen of $\mathrm{YBa}_{2} \mathrm{Cu}_{3} \mathrm{O}_{7 \text {-x }}$ ..... 19
Acknowledgements ..... 21
9. Appendices
A1. Summary Sheet for the Ris $\phi$ Powder Diffractometer ..... 23
A2. Electronic Set-Up ..... 25
A3. Powder Line-Broadening due to Vertical Divergence ..... 27
A4. Example of Computer Aided Line-Up Sequence ..... 31

## 1. Introduction

### 1.1. Principles of Powder Diffraction

The principles of diffraction of X-rays from a crystalline powder has been known for more than 75 years. The dif fraction pattern yields detailed information about the atomic struciure of crystalline material. The same principles apply for neutron beams as demonstrated in the pioneering experiments about 40 years ago. However, neutron diffraction has some special features: Light atoms or isotopes thereof diffract as well as heavier atoms and it is often possible to locate the position in the unit cell of e.g. hydrogen (deuterium) or oxygen atoms from a neutron powder diffraction pattern. Because of the magnetic moment of the neutron one can determine magnetic structures from neutron powder patterns. Neutron beams are very penetrating and the sample can therefore be placed in furnaces, magnets and/or suitable sample containers.

The method of powder diffraction is a mature field and the reader should not expect to learn about some new fundamental principles from this report; the basic techniques are described in standard textbooks on diffraction and crystal structure analysis (e.g. G.E. Bacon, "Neutron Diffraction" (Clarendon Press, Oxford) 1975). Here it suffices to
recapitulate that one obtains two kinds of information from a diffraction pattern:
(i) From the location of the peaks in the spectrum one gets the dimensions of the unit cell, which in turn may be used to identify the chemical compound(s) in the sample and possibly contaminating phases.
(ii) From the peak intensities one can derive the cooroinates of the atoms within the unit cell as well as the thermal vibration amplitudes and site occupancies.

In this report we describe a new neutron powder diffractometer, which has been installed at the DR3 reactor at Ris 6 , in order to ease the operation of this instrument by actual and potential users. Let us start by recapitulating the salient features of neutron powder diffraction. A monochromatic neutron beam is extracted from the Maxwellian spectrum emerging from the reactor by Bragg reflection from a single crystal, c.f. Fig. 1. The wave vector $k$ of the monochromatic beam is related to the Bragg angle $\theta_{M}$ and the reciprocal lattice vector of the monochromator ${ }^{1} M$

$$
\begin{equation*}
2 k \sin \theta_{M}=q_{M} \tag{1}
\end{equation*}
$$

The monockromatic beam is Bragg reflected from crystalline grains in the powder sample into Debye-Scherrer cones. The scattering angle of a particular cone, $2 \theta_{\mathrm{S}}=2 \theta_{\text {hk }} \ell$ is related to the reciprocal lattice vector thke by

$$
\begin{equation*}
2 k \sin 0_{\text {hke }}=\theta_{\text {the }} \tag{2}
\end{equation*}
$$



Fig. 1. Layout of the multi-detector powder diffractometer at DR3, Risø. Twenty detectors D1...D20 witn Soller collimators C1...C20 spans $100^{\circ}$ of scattering angle so a $5^{\circ}$ scan of the detector bank furnishes the complete powder pattern. CO defines the collimation of the incident beam.

The reciprocal lattice vector thkl has integer coordinates ( $h, k, \ell$ ), the socalled Miller indices. The unit cell in reciprocal space is spanned by $(h, k, l)=(1,0,0)$, $(0,1,0)$ and $(0,0,1)$ and these basis vectors are denoted $a^{*} \cdot b^{*}$ and $c^{*}$, respectively. They are related to the real space unit cell basis vectors $a, b$, and $c$ by

$$
\begin{aligned}
& a^{*} / 2_{u}=b \times c / V, \\
& b^{*} / 2_{u}=c \times a / V, c^{*} / 2 u=a \times b / V,
\end{aligned}
$$

with

$$
V \equiv(a \times b) \cdot c
$$

The amplitude of the ( $h, k, f$ ) Bragg scattered wave is proportional to the structure factor $\mathrm{F}_{\mathrm{hk}}$ ?

$$
\begin{equation*}
r_{h k f}=\sum, r_{1} \exp \left(i_{h k e} r_{j}\right) \tag{4}
\end{equation*}
$$



Fig. 2. Unit cell of $\mathrm{YBa} \mathrm{Ba}_{2} \mathrm{Cu}_{3} \mathrm{O}_{7-x}$. Site $0(5)$ is not occupied for $x=0$ (see section 8.1).

In Eq. (3) $r_{j}$ denotes the position of the $j$ 'th atom in the unit cell. An example of a unit cell is given in Fig. 2. The $j^{\prime}$ th atom (or for neutron scattering rather the $j^{\prime}$ th nucleus) has a scattering length $b_{j}$, an average site occupancy $c_{j}$ and a mean squared thermal vibration amplitude $\left\langle u_{j}{ }^{2}\right\rangle$. The quantity $f_{j}$ in Eq. (3) is defined as

$$
\begin{equation*}
f_{j}=c_{j} b_{j} \exp \left(-i_{h k \ell}^{2}<u_{j}^{2}>\right) \tag{4}
\end{equation*}
$$

The intensity $I_{h k e}$ integrated over scattering angle is proportional to the square of the structure factor

$$
\begin{equation*}
I_{h k \ell^{\alpha}} j_{b k f} l_{i}\left(1 l_{h k f}\right)\left|F_{h k f}\right|^{2} \tag{5}
\end{equation*}
$$

Here jhk $\ell$ is the multiplicity of the ( $h, k, \ell$ ) reflection and $L\left(\theta_{h k} \rho\right)$, the Lorentz factor, is a smooth and well known function of the scattering angle $\theta_{\text {hhl }}$.

### 1.2. Design Criteria

A powder spectrum obtained with the new diffractometer is shown in Fig. 3 . It contains about 50 separated powder peaks at positions corresponding to a range of thke moduli from $1.5 \AA^{-1}$ to $8 \AA^{-1}$. The line spacing decreases with increasing angle simply because the density of moduli $t_{h k} \ell$ increases with increasing Miller indices. The variation of peak intensities reflects the variation of the structure factor, c.f. Eqs. (3) and ( 5 ), with ( $h, k, \ell$ ). The observable dynamic range of intensities is about 100:1. This range is determined by the background level which in turn is given by the sum of a general stray neutron background level and the diffuse scattering from the sample and sample container. The latter contribution is the dominant part in Fig. 3.

The quantities one wants to obtain from a powder diffraction measurement are the atomic positions $r_{j}$ in the unit cell as well as the site occupancy $c_{j}$ and the root mean square (r.m.s.) thermal amplitude $<u_{j}{ }^{2}>1 / 2$. Usually this is obtained by modelling the unit cell with a certain number of adjustable parameters, calculating the structure factor by Eqs. (3) and (4) and comparing to the measured intensities using Eq. (5). The number of measured reflections thus determines the maximum number of adjustable parameters in the model unit cell.

We shall now discuss the means to obtain the maximal number of reflections within a reasonably short time. First of all we note in conjunction with Eq.(2) that only grains with the correct orientation contribute to an ( $h, k, t$ ) reflection. The correct orientation means that the reciprocal lattice vector of the reflecting grain is at an angle of $\mathrm{n} / 2-\theta_{\text {hk }} \boldsymbol{\ell}$ with respect to the incoming beam direction. Second, only a relatively small part of the Debye-Scherrer cone is subtended by the detector. Therefore the intensity, even at a scattering angle where the Bragg law of Eq. (2) is fulfilled, is rather low - certainly less than $0.1 \%$ of the incident beam intensity, so a counting time of say at least ten seconds is needed to obtain sufficient accuracy. Furthermore, the Bragg peaks are progressively more closely spaced as one moves to higher and higher ( $\mathrm{h}, \mathrm{k}, \ell$ ) indices, i.e. to larger scattering angle. So in order to separate the Bragg peaks the resolution must be narrow at large scattering angles. As will be explained in section 5 , the high angle resolution is proportional to the inverse of $\tan \left(\theta_{M}\right)$. It is therefore advantageous to operate at a rather large value of $\theta_{\mathbf{M}}$.

The required resolution implies also that the incident as well as the scattered beams must be well collimated, a condition which can only be obtained at the expense of intensity. So how can one compensate for the inherent low intensity? First of all one does not need a high angular resolution perpendicular to the


Fig. 3. Powder diffraction pattern from $\mathrm{YBa}_{2} \mathrm{Cu}_{3} \mathrm{O}_{7-x}$ obtained with a $\mathrm{Ge}(311)$ monochromator at $20_{M}=85.6^{\circ}(\lambda=2.32 \AA)$. The counting time for the full pattern was about one hour. Top: Observed (...) and profile refined (-) patterns. Bottom: Difference between the observed and calculated patterns.
scattering plane, neither of the incident beam nor of the Bragg scattered beam. Accordingly we use (i) a rather high monochromator crystal subtending the full height of the reactor beam and bent to partially focus the beam in the vertical plane onto the sample, and (ii) a rather high detector to subtend as much as practically possible of the DebyeScherrer cone. Second, the transmission of the collimators defining the direction of the incident and scattered beams should be high.

The necessesary angular resolution to separate Bragg peaks at wave vector transfers around $9 \AA^{-1}$ is around $10^{\prime}$ or 3 milliradians using a wave vector around $4 \AA^{-1}$. This could be obtained by 1 mm wide slits 30 cm apart, but the sample width is usually much wider than 1 mm , so in order to take advantage of the available sample size (width) we use a multi-slit collimator, a so-called Soller collimator. It consists of a set of channels separated by thin, but strongly neutron absorbing walls. The wall thickness
relative to the channel width determines the loss in transmission. Third, by using a bank of N detectors each having Soller collimator pointing towards the sample one reduces the data aquisition time by $1 / \mathrm{N}$ compared to a single detector system. In the present case we use a detector bank of twenty detectors spanning an angular range of about $100^{\circ}$. The full diffraction pattern shown in Fig. 3 is then obtained by 100 angular settings of the detector bank yielding 2000 data points.

Having now described the basic features of the powder diffractometer we shall in the following sections discuss the individual components in more detail. A summary of the components of the diffractometer are given in appendix A1.

## 2.Monochromator

### 2.1. Lattice Spacing

As discussed in the previous section one should use a large Bragg angle at the monochromator. With the present monochromator shielding and space in the DR3 reactor the maximal value of $2 \theta_{\mathrm{M}}$ is $90^{\circ}$. The thermal Maxwellian spectrum peaks around 40 meV and the corresponding value of $k$ is around $4 \AA^{-1}$. From Eq. (1) with $\theta_{M}=45^{\circ}$ we then find $t_{M}$ should be approximately $6 \AA^{-1}$ which corresponds to a lattice spacing of around $1 \AA$.

### 2.2. Higher Order Contamination

The monchromatic beam should not be contaminated by higher order reflections relative to the dynamic range of approximately 100:1. The higher harmonic wave vectors $2 k, 3 k$ etc. correspond to energies of 4,9 etc. times the primary energy. The reactor spectrum implies that only second harmonic contamination may present a problem. It may be overcome by using a monochromator reflection where the second order reflection is forbidden. The concept of forbidden reflections may be unaerstood from Eqs. (3) and (4). Assume that the monochromator only have one kind of atoms, all with the same thermal vibration amplitude. The structure factor in Eq. (3) is then simply a summation over phase factors. The reader may easily verify that in an f.c.c. unit cell only reflections with all indices either even or odd are non vanishing.

The diamond structure can be considered as two interpenetrating f.c.c. lattices displaced $1 / 4$ of a cube diagonal. In addition to the f.c.c. selection rule the diamond lattice therefore implies that ( $1+\exp (i n / 2(h+k+l)$ ) must be non vanishing. In particular, if ( $h, k, \ell$ ) are all odd, the sum is odd. Therefore, the reflection is allowed, but the second order ( $2 \mathrm{~h}, 2 \mathrm{k}, 2 \ell$ ) has an even sum so the second order reflection is forbidden. Semiconductors such as Si and Ge have the diamond structure and they can be
grown as large crystals. We have chosen to use a Ge monochromator crystal which can be oriented to reflect from the ( $h, \ell, \ell$ ) planes. For $\ell=1$ and odd $h=1,3,5,7$ ett. one obtains reflections where second order is forbidden. The $t_{511}$ reciprocal lattice vector has a length of $5.7709 \AA^{-1}$ which is a convenient magnitude.

### 2.3. Mosaicity

Semiconductor crystals have however one drawback as monochromator crystals: they are too perfect. The monochromator crystal should have a mosaic spread at least of the same order of magnitude as the collimation between monochromator and sample, i.e. 10 , in order to utilize as broad a wavelength band as possible of the reactor spectrum without significantly deteriorating the powder spectrum resolution. It is possible to obtain such a mosaic spread artificially in a Ge crystal by applying a uniaxial pressure at elevated temperatures. Our monochromator Ge crystal was prepared in such a way by the Crystal Laboratory at Institute Laue Langevin, Grenoble, France and obtained a mosaicity of about $10^{\circ}$ FWHM (Full Width at Half Maximum).

### 2.4. Sagital Focussing

In addition to having an appropriate lattice spacing, mosaicity and forbidden second order, the monochromator crystal should also focus spatially in the vertical plane so that the 10 cm high reactor
beam is focussed to a height of a few centimeters at the sample position, i.e. the top part of the crystal should reflect the reactor beam downwards and the bottom part should reflect it upwards. A monolithic Ge crystal cannot be bend to provide this socalled sagital focussing, it is too brittle. Consequently we cut our pressed Ge monolithic crystal into smaller pieces: $12 \times 12 \mathrm{~mm}(3,1,1)$ faces that are 8 mm thick. Out of these pieces we selected 21 crystals with similar mosaicity and mounted them in the monochromator holder in a $3 \times 7$ array so that each of them could be tuned to the appropriate orientation in a test beam. Once correctly oriented they were fixed by embedding in epoxy so the final monochromator assembly has a fixed radius of curvature for the sagital focussing. However, the final radius of curvature is not very critical because the neutron source in the reactor is quite extended and hence the focussing effect is considerably blurred in practice. Therefore all the ( $h, 1,1$ ) reflections with $h=1,3,5$ and 7 have approximately sagital focussing.

## 3. Collimators

The direction of the incident and scattered beam is determined by multislit collimators, socalled Soller collimators. The angular divergence is $10^{\prime}$ obtained by a slit width of 1.0 mm and a !ength of 320 mm . The height of each slit
is 100 mm . The slit walls should be thin in order to obtain a high transmission of the Soller collimator, but at the same time highly neutron absorbing so that cross-talk between slits can be neglected. We manufactured walls of a 0.012 mm thin plastic foil coated on both sides with approximately 0.03 mm paint in which the strongly neutron absorbing material $\mathrm{Gd}_{2} \mathrm{O}_{3}$ was dissolved in an amount of 250 $\mathrm{g} / \mathrm{l}$. The transmission through such a wall at a glancing angle of $2 \times 10^{\prime}$ is around $10^{-8}$ at $1 \AA$, so cross-talk between channels is eliminated. The channel width is provided by spacers at the top and bottom of the channel. A special tool was developed to mount the stack of coated plastic foils and spacers in a stainless steel frame so that all foils are straight and accurately parallel to the outer edge of the steel frame.

As indicated in Fig. 1 each of the twenty detectors has a collimator in front. However, we have a separate mounting of the detectors and collimators into a collimator bank and a detector bank for the following reasons. The detectors need a substantial amount of shielding around to reduce the stray neutron background to an acceptable level. As shielding material we use an epoxy with a neutron absorbing boron compound so that fast neutrons are being moderated and then absorbed. Test of this detector shielding material indicates that a shielding thickness of about 20 cm is required on all sides around the detector. This means
that the shielding around the detector bank is a bulky entity weighing around 400 kg and it would therefore not be trivial to move the detector bank around with a precision of a fraction of the coliimation width, say by a precision of 1'. However, the detector response is quite flat across the detector window, so if just the collimator bank is moved precisely one can relax on the precision of the movement of the detector bank. There is a further advantage of separate collimator and detector banks. In a fixed beam, e.g. the incident beam properly attenuated or on a powder diffracted beam one can scan the entire collimator bank in front of a fixed detector and thereby experimentally find possible errors in the equidistant mounting of the collimators. The collimators were mounted on a counter weight balanced turntable with a nominel angular separation of $5.289^{\circ}$. The collimator bank scan over an angular range of $20 \times 5.289^{\prime \prime}=105.8^{\prime \prime}$ with fixed detector gave a maximal error of $0.025^{\circ}$ and a standard deviation of $0.015^{\prime \prime}$. These numbers are so small compared to the collimation width of $10^{\circ}$ or $0.167^{\circ}$ that the collimators for all practical purposes can be considered as rigidly equidistant. In setting up a powder pattern scan the angle between neighboring collimators is divided into a number of steps, so in the last point of the scan collimator $n$ is precisely one step from the starting angle of collimator $\mathrm{n}+1$.

## 4. Detectors and Electronics

The twenty detectors are $\mathrm{He}^{3}$ filled gas proportional counters manufactured by LND, Inc., New York, USA. The He3 pressure of 5 atm . together with a thickness of 2 cm gives an efficiency of $63 \%$ at a wavelength of $1.3 \AA$. The sensitive area is 2 cm wide by 10 cm high. The detectors all have the same gas filling and they are in fact quite similar in efficiency. Right on top of the detectur bank and within the shielding is mounted a pre-amplifier bank, the advantage of the proximity being an improved signal to noise ratin due to the minimal capacitance. Output signals from the twenty preamplifiers are led to a bank of main amplifiers ard single channel analysers outside the shielding. Each main amplifier can oe tuned by a potentiometer to provide a pulse height of 4 V and a pulse width of approximately $3 \mu \mathrm{~s}$. All Single Channel Analysers are set to provide a standard TTL pulse for an input pulse between 0.75 V and 4.5 V . The SCA output on 20 lines are then fed into a decoder providing an interface to the computer. The detector electronics is described in some detail in appendix A2.

## 5. Powder Spectrum Resolution

The width of a powder line, c.f. Fig. 3, is partly determined by the collimators


Fig. 4. Top: The resolution width (FWHM) in a powder spectrum is at small angles mainly determined by collimation ( $W_{2 \theta}$ ), but at large angles mainly by monochromaticity ( $W_{k}$ ). Bottom: Comparison of measured resolution widths from a standard $\mathrm{Al}_{2} \mathrm{O}_{3}$ powder with Eqs. (6) and (7).
determining the direction of the incident and scattered ray, and partly by the wavelength spread of the monochromatic beam. In Fig. 4a is depicted two extreme cases : At very small angles the width , W , is determined by collimation only ( $W=W_{20}$ ), whereas in the opposite extreme case of large scattering angles the width is determined solely by the realtive wave vector spread $8 \mathrm{k} / \mathrm{k}$ ( $W=W_{k}$ ). If the entrance and exit collimators have identical widths 0 , then

$$
\begin{equation*}
W_{20}=k \sqrt{20} \tag{6}
\end{equation*}
$$

whereas the width $W_{k}$ follows by differentiating the relation shke $=$ $2 k \sin \left(\theta_{h k}\right)$

$$
\begin{equation*}
W_{k}=L_{h k \ell}(\delta k / k) \tag{7}
\end{equation*}
$$

The relative wave vector or wavelength spread $8 \mathbf{k} / \mathbf{k}$ is

$$
\begin{equation*}
\delta \mathrm{W} / \mathrm{k}=80_{\mathrm{M}} / \tan \left(0_{\mathrm{M}}\right) \tag{8}
\end{equation*}
$$

In Fig. $4 \mathrm{~b} \mathbf{W}_{20}$ and $\mathrm{W}_{\mathrm{k}}$ are compared to experimental widths from an $\mathrm{Al}_{2} \mathrm{O}_{3}$ standard powder sample using either the (311) or the (511) reflections of the Ge monochromator crystal set at $2 \theta_{\mathrm{M}}=$ $85.6^{\circ}$. In plotting $W_{k}$ we have used $8 \mathrm{k} / \mathrm{k}$ $=0.35 \%$ corresponding to $8 \theta_{\mathrm{M}}=11^{\circ}$,


Fig. 5. At low angles the combination of straight Soller collimators and curved Debye-Scherrer cones implies a line shape with a tail on the low angle side. The full curve is calculated as described in appendix $A 3$.
which is quite a reasonable value given the $10^{\circ}$ collimation between monochromator and sample and the effective mosaicity of the monochromator crystal. Note that the slope of $W_{k}$ versus $\tau_{h k \ell}$ is inversely proportional to $\tan \left(\theta_{M}\right)$ showing the advantage of using a high take-off angle from the monochromator to obtain good resolution at large wave vector transfers.

The discussion above of resolution at very large and very small angles assumed that the vertical resolution can be neglected in the sense that the part of the Debye-Scherrer cone contributing to the scattering can be approximated by a vertical line. However, at very small and at large scattering angies, the DebyeScherrer cone is indeed very concave, and that may affect the observed line shape. At small angles this will lead to a tail on the low angle side of a powder peak and at large angles to a tail on the high angle side. An example is given in Fig. 5 showing a powder peak at $2 \theta_{\mathrm{S}}=11^{\circ}$. The full detector height was 10 cm which together with a sample to detector distance of 60 cm leads to an azimuthal angular range on the Debye-Scherrer cone of as much as $-25^{\prime \prime}$ to $+25^{\prime \prime}$. A quantitative evaluation of the line shape is given in appendix A3 and shown as the full curve in Fig. 5.

## 6.Software

The powder diffractometer is controlled by a PDP11-23 computer under the multi-user TSX-11 operating system, and is equipped with a hard disc, two floppy discs, a standard video display (VDU) and a graphics screen. The control programme is an extended version of the TASCOM programme used in general for Riso neutron- and x-ray spectrometers. The extension handles the twenty separate detectors used for the powder diffractometer. However, the programme can still operate on any single one of these detectors, which is a useful option for line-up purposes and special investigations of selected powder peaks. It is therefore useful to divide this section into single detector mode and multidetector mode.

### 6.1. Single Detector Mode

Very briefly, the main purpose in this mode is for a selected detector in the detector bank to carry out the following sequence of instructions :
(i) to set the detector at a given scattering angle,
(ii) to measure for a certain time or for a preset accumulated number of counts in the monitor channel,
(iii) to print the result in a user determined format on the screen and printer
iv) to move to the next point in a user defined angular scan and repeat (i)(iii),
(v) by completion of the scan to provide a $x$-y plot in user-defined assignments of $(x, y)$, to find peak position and width if the data can be interpreted in terms of a peak, to store the data of the scan in a datafile on disc and to up-date the file number by one.

We will assume that the reader is familiar with the general operation of TASCOM or refer to the TASCOM manual. Here we shall only recall the special features of single detector mode on the powder spectrometer by explaining the function of a few variables.

CHAN CHANnel number or detector number in the range $1-20$, c.f. Fig. 1. The accumulated intensity in this detector is as usual denoted I.

TTC Two Theta of Channel CHAN in degrees.

PLTY provides labelling of axes etc. in the plot. Must be set to "SNGD" in SiNGle Detector Mode.

Q The wave vector transfer seen by detector number CHAN.
$\mathrm{CQ} \quad$ ls +1 for scattering to the left, -1 for scattering to the right, when following the neutrons from the source.

CO56 Coupled movement of detector bank (motor 5,100 steps/ degree) and collimator bank (mo:or 6, 2000 steps/degree). Its value is 1 for coupied movement (with approximately the same speed of the two banks) and 0 for independent movement of motor 5 and 6.

### 6.2. Multi Detector Mode

In this mode the computer has to handle the intensities from all twenty detectors. The input comes from the twentydetector decoder described in section 4. The amount of data is large and is therefore stored on disc in compact, socalled "unformatted" files. Such a datafile of type <filename.MLT> contains a user defined file text and date, the angular offset of each of the twenty detectors (in practice the offsets are all 0 , c.f. section 3 ) and the relative efficiency of each detector (in practise all unity). Then follows the first angular setting and the corresponding twenty intensities. the second angular setting and the corresponding twenty intensities and so on. A program outside TASCOM called MANMLT translates an MLT file to an ASCII file. Typical file sizes for 100 angular settings are 17 blocks for the MLT file and 110 blocks for the ASCII file. In addition to provide ASCII format the MANMLT program also sorts the data in sequence of increasing angles, which is a useful feature when an ASCI file is the database for plotting routines,
structure refinement, etc. On-line monitoring of the powder spectrum as it is being accumulated, is provided on the graphics screen. There are a number of options concerning scaling of the plots as explained below.

By completion of the scan, the screen picture is dumped on the printer and with TASCOM commands it is also possible at this stage to plot for example one or more sections of the full spectrum without translating the file into ASCII format. Special commands and variables in the Multi Detector Mode include:

PLTY must be set to "MLTD" in theMul.Ti Detector mode.

LOOK $=1$ if on-line graphics is to appear on the screen during data accumulation. The command PLOT (see below) is disabled.
$=0$ to disable on-line graphics. The command PLOT (see below) is enabled.

PLOT plots the accumulated data (in MLT format), according to the scaling criteria set by LIMX and LIMY, provided LOOK $=0$.

LIMX $=1$, user assigned values of XMIN and XMAX
$=2$, automatic value of XMAX, XMIN $=0$.
$=0$, automatic values of XMIN and XMAX..

LIMY $=1$, user assigned values to YMIN and YMAX.
$=2$, automatic value of YMAX. YMIN $=0$.
$=0$, automatic value of YMIN and YMAX.

VT24 $=1$ for a graphics scan (ex. VT240 or VT340).
$=0$ for any other terminal (disabling graphics plots).
mechanical alterations to the spectrometer, or a new monochromator reflertion has been chosen, or there are other reasons to disbelieve the present zero angles, a new determination of these should be carried out. This process as well as ensuring that the monochromator is reflecting a monochromatic beam optimally onto the sample, is called lining up the spectrometer.

## 7. Lining-Up <br> the Multi-Detector Diffractometer

Any angle determination is a relative measurement. The reference angle or zero angle of each angle measurement must therefore be known to sufficient accuracy. Any time there have been

Each element of the spectrometer must be lined up without requiring knowledge of the yet unknown parameters of the remaining elements. This makes the natural direction of the line-up procedure follow the neutron beam through the spectrometer. Each step in this process are described in the following.

| Ge <br> reflection | $\tau \mathrm{M}$ | fast rotation <br> negative time/s | count rate/keps <br> $\mathrm{M} 1=8560$ |
| :---: | :---: | :---: | :---: |
| $(133)$ | 4.84104 | 0 | 7.5 |
| $(111)$ | 1.92363 | 23 | 20.0 |
| $(533)$ | 7.28276 | 37 | 8.6 |
| $(422)$ | 5.44086 | 43 | 20.0 |
| $(733)$ | 8.95402 | 47 | 4.5 |
| $(311)$ | 3.68348 | 53 | 17.0 |
| $(822)$ | 9.42384 | 59 | 5.0 |
| $(511)$ | 5.77090 | 63 | 16.0 |
| $(711)$ | 7.93134 | 67 | 7.0 |
| $(400)$ | 4.44244 | 78 | 20.0 |

Table 1. Characteristics of reflections from the Ge monochromator. Column 3 is the time taken by the manually operated rotation device to rotate between the various reflections. This time may be used in connection with column 4 to find the desired monochromator reflection. The count rates in column 4 are from a fisston monitor at TAS3.

To ensure a rapid and well defined lineup of the spectrometer the computer which controls the spectrometer may guide the user through this process. A reproduction of the computer output during such a line-up procedure is given in appendix $\mathbf{A} 4$.

### 7.1. Monochromator

The monochromator must be rotated so the desired reciprocal lattice vector halves the angle that the monochromator scattering angle is set to. It must also be assured that the reciprocal lattice vector lies in the horizontal scattering plane of the spectrometer. The standard Ge monochromator is as noted earlier oriented in the ( $h, \ell, \ell$ ) plane. As a help to identifying the desired reflection Fig. 6 shows the reciprocal lattice vectors with an appreciable assuciated reflectivity in this plane. The monochromator is


Fig. 6. Reflections with appreciable intensity from the Ge monochromator mounted in the ( $h, \ell, \ell$ ) plane. The arrow indicates the sequence in which the reflections appear when rotating in the pristive direction on the monochromator rolation device.
rotated by a manually operated motor drive unit with no absolute encoder. The time taken to rotate between two reflections can, however, be used to identify them (see Table 1). Once the desired reflection has been identified the countrate on a monitor placed immediately at the exit from the monochromator drum is optimized by rotating and tilting the monochromator with the manually operated motor drive.

### 7.2. Monochromator-Sample Collimator

The next step is to align the mono-chromator-sample collimator (CO in Fig. 1) parallel to the direction of the beam from the monochromator. For this purpose the monitor is placed immediately after the collimator, which is mounted on a rotation device which is then rotated until maximum intensity is transmitted through the collimator CO. At this step a monochromatic collimated incident neutron beam has been prepared.

### 7.3. Sample Table Alignment

The centre of the sample table must now be centred in the incident deam. This is done by moving a strong incoherent scatterer (a perspex rod) placed on the sample table through the incident beam while monitoring the total countrate of all twenty detectors. The position at which the intensity is maximal corresponds to the sample being centred in the incident beam. After completing
this step wc have centred the sample table in the collimated monochromatic incident beam.

### 7.4. Sample ©cattering Angle

The zero ang's of the sample scattering angle is now determined by scanning one detector through the attenuated incident beam. This zero angle may also be measured by scanning through the powder peaks corresponding to scattering to right and left from a powder sample. The zero angle is then the bisecting direction in between these two directions.

### 7.5. Detector-Hank Collimator Alignment

The alignment of the detector-bank with respect to the collimators ( $\mathrm{C}, \mathrm{C} 2, \ldots$ in Fig. 1) is established by scanning a detector through the incident beam after this has passed through the corresponding collimator. The detectors are placed behind their rcspective collimators when this intensity is optimized.

### 7.6. Motochromator Scattering Angle

Finally the scattering angle at the monochromator, and thereby the neutron wave vector $k$ (see Eq. 1), is determined by measuring the scattering angle of a powder peak of an aluminum
oxide standard sample. From Bragg's law the following equation holds

$$
\frac{t_{s}}{s_{M}}=\frac{\sin 0_{s}}{\sin \theta_{M}}
$$

where $\tau_{\mathrm{s}}, \theta_{\mathrm{S}}$ are the reciprocal lattice vector and half scattering angle at the sample, and $\mathrm{I}_{\mathbf{M}}, \boldsymbol{\theta}_{\mathbf{M}}$ are the corresponding values for the monochromator. So by measuring $\boldsymbol{\theta}_{\mathrm{s}}$ for the known values of $\mathrm{t}_{\mathrm{s}}$ and $\mathrm{t}_{\mathrm{m}}$ we find the scattering angle at the monochromator

$$
20_{M}=2 \operatorname{Arcsin}\left(\frac{L^{\prime}}{L_{S}} \sin v_{s}\right)
$$

## 8. Example of a Structure Study

Shortly after the discovery of the ceramic superconductors at the end of 1986 it was realized that the occurrence of high temperature superconductivity is closely related to the properties of the copperoxygen bonds. Structural studies are therefore very important in the search for the basic principles of high-T ${ }_{c}$ superconductivity as well as a number of materials properties related to applications.

Since the ceramic high-T $\mathrm{T}_{\mathrm{c}}$ superconductors are available sofar mainly as powder samples, and important struc tural features are related to minor crystalline distorsions of almost tetrago
nal structures, there is a need for a high resolution spectrometer. Many aspects related to synthesis and studies of kinetics in the structural transformations call for short measuring times. The multi-detector high-resolution powder neutron diffractometer was designed and constructed to meet these requirements. As an example some studies of the structural properties connected to the oxygen stoichiometry in $\mathrm{YBa}_{2} \mathrm{Cu}_{2} \mathrm{O}_{7-x}$, will be mentioned. A neutron wave length of $\mathrm{A}=2.32 \AA$ obtained with a Ge(311) monochromator at $\mathrm{H}_{\mathrm{M}}=85.6^{\prime \prime}$ was used for the measurements.

### 8.1. I'hase Rquilibrium and Kinetics of the Oxygen Uptake of $\mathrm{YHa}_{2} \mathrm{Cu}_{3} \mathrm{O}_{7-x}$

For $x<0.5, \mathrm{YBa}_{2} \mathrm{Cu}_{3} \mathrm{O}_{7} \mathrm{x}$ has an orthorhombic structure as shown in Fig. 2. The temperature variation of the lattice parameters are shown in Fig. 7. At room temperature almost full oxygen uccupancy in the crystalline lattice is found on the sites $0(1), 0(2), 0(3)$, and $0(4)$ in Fig. 2, whereas site $0(5)$ is essentially empty. On heating, deviations from stoichiometry occur and result in a partial occupancy on the $0(1)$-site. Simultaneously the $0(5)$-site becomes increasingly populated. At temperatures above $660^{\prime \prime} C$, sites $0(1)$ and $0(5)$ are equally populated and the crystal structure transform from orthorhombic to tetragonal. If non-stoichiometric $\mathrm{YBa}_{2} \mathrm{Cu}_{3} \mathrm{O}_{7-\mathrm{x}}$ is quenched from high temperatures or cooled in vacuum, the
non-stoichiometry remain, and the superconducting properties are significantly deteriorated. For $x$ approaching 1 superconductivity disappears and antiferromagnetic order is observed. It is therefore important to study the conditions for phase equilibrium and the kinetics of oxygen uptake in this system.

Three sequences in studies related to these properties of $\mathrm{YBa}_{2} \mathrm{Cu}_{3} \mathrm{O}_{7 \text {-x }}$ should be mentioned. First, when heated in $100 \%$ oxygen the orthorhombic lattice expands as shown in Fig. At temperatures above $600^{\circ} \mathrm{C}$ the a - and b-axes sterts to approach each other and a phase transition to the tetragonal structure is observed at $670^{\circ} \mathrm{C}$. As mentioned the


Fig. 7. Temperature variation of the lattice parameters in $\mathrm{YBa}_{2} \mathrm{Cu}_{3} \mathrm{O}_{7-\mathrm{x}}$. Open symbols refer to heating in 100\% 02: V Jorbensen ef al., o our data. © our results. cooling under vacuum from above $700^{\circ} \mathrm{C}$.
phase transition is driven by the depletion of oxygen from site $0(1)$ and disordering by occupancy on site $0(5)$ (Fig. 2). These properties may be determined from structural refinements on the full powder spectrum shown in Fig. 3. However, it is worth mentioning that the depletion of oxygen from the basal plane sites $0(1)$ and $0(5)$ may be studied qualitatively from the intensity of the (001)-peak found at $2 \theta=11.3^{\circ}$ in the powder diffraction pattern. In a $100 \%$ oxygen atmosphere Jorgensen et al. (Phys. Rev. B36, 3608 (1987)) have determined an equilibrium oxygen con centration corresponding to $x=0.58$ at $818^{\prime \prime} \mathrm{C}$. Structural refinements on our data have not yet been completed. Although, there are some differences in the lattice constants obtained in our study and that of Jorgensen et al. (see Fig. 7), we expect a qualitatively similar behaviour.

The lattice expands on heating despite the loss of oxygen. Actually, the loss of oxygen contributes as a driving mechan ism in the expansion of the lattice. This is also seen from the experimental results shown in Fig. 7, where the sample has been evacuated in the tetragonal phase above $700^{\circ} \mathrm{C}$ with a significant ex pansion of the $c$-axis as a result. A semiquantitative evaluation of the stoichio metry, based on the (002)-peak intensity, indicates an equilibrium stoichiometry in vacuum at these temperatures corresponding to $\mathrm{YBa}_{2} \mathrm{Cu}_{3} \mathrm{O}_{6}$. Subsequent cooling under vacuum maintain the
tetragonal phase and the oxygen deficiency. At room temperature the oxygen deficient tetragonal phase has proven to be stable in air for more than a week.

A third experiment has been performed in order to study the kinetics of the oxygen uptake towards equilibrium. The sample being cooled under vauum from $700^{\circ} \mathrm{C}$ to room temperature, and thereby maintained in the oxygen deficit tetragonal phase, was heated semi-dynamical with an increase of $25^{\prime \prime} \mathrm{C}$ every two hours, and the transformation towards the orthorhombic equilibrium phase was


Fig. 8. Tetragonal (200), - and orthorhombic $(020)_{0}$ - and $(200)_{0}$-Bragg. peaks used to study the transformation between tetragonal and orthorhombic phase


Fig. 9. Temperature variation of the Bragg-peak intensities of: $\bar{\nabla}$ - the tetragonal (200) ${ }_{t}$-peak, 0 - the sum of orthorhombic ( 020$)_{0}$ - and $(200)_{0}$-peaks.
studied. From a study of the tetragonal (200)-peak, which splits into close-lying (200)- and (020)-peaks in the orthorhombic phase shown in Fig. 8, it is observed that only these two phases are present during the transformation. This indicates that the transformation occurs via a diffusion process through the orthorhombic phase developing from the surface of the grains of the ceramic sample. The temperature variation in the tetragonal (200)-peak invensity and the sum of orthorhombic (200)- and (020)-peak intensities are shown in Fig. 9. The results show that the annealing process leading to oxygen equilibrium in $\mathrm{YBa}_{2} \mathrm{Cu}_{3} \mathrm{O}_{7 \times x}$ may be performed at temperatures as low as $200^{\circ} \mathrm{C}$, which is significantly lower than usually recom
mended e.g. during synthesis. An isothermal annealing process performed at $165^{\circ} \mathrm{C}$ showed that $75 \%$ of the sample was transformed from the tetragonal to the orthorhombic phase within fifty hours. Further studies of these properties are in progress.

## Acknowledgements

The powder diffractometer was constructed by J. Linderholm and the crystal orientation device by K. Theodor. The assembling and installation of the mechanical parts were done by L. G. Jensen and 'T. Kjæer. 'The production of mechanical parts at the Risw Central Workshop and the electonics at Electronics Depaitment within a very short time are much appreciated. The Ge monochromator crystal was pressed at the Institute Laue Langevin, Grenoble, France by Drs. A. Freund and B. Hamelin at ILL and Mr. T. Lorentzen from Riso. The data analysis of the kinetics of $\mathrm{YBa}_{2} \mathrm{Cu}_{3} \mathrm{O}_{7-x}$ was done by Mr. H. Friis Poulsen. We have benefitted from enlightening discussions with Dr. M. Lehmann from Institute Laue Langevin.

## Appendix A.1. Summary Sheet for the Risø Powder Diffractometer

## A.l.1. Monochromator

Ge: Diamond structure, $\mathrm{a}=5.6574 \AA$

Mounting: $3 \times 7$ Pressed Ge crystals of dimensions: $12 \times 12 \times 8 \mathrm{~mm}^{3}$ with (311) perpendicular to the surface mounted on a Gd shielded vertically curved Al holder.

Relative structure factors $(F): \quad 1$ for $h+k+\ell=4 n(h, k, \ell)$ all even
0.7071 for ( $h, k, \ell$ ) all odd

0 all other combinations of ( $h, k, \ell$ )

Mosaicity: $\mathbf{1 0}^{\prime}$ (FWHM)

For $90^{\prime \prime}$ take off angle at the monochromator:

| mono- <br> chromator <br> reflection | wave- <br> length <br> $A$ | wave <br> vector <br> $A^{-1}$ | energy <br> meV | Q-range $A^{-1}$ <br> for $5^{\circ}-110^{\prime \prime}$ in <br> $2 \theta$ |
| :---: | :---: | :---: | :---: | :---: |
| $(111)$ | 4.6192 | 1.3602 | 3.83 | $0.12-2.23$ |
| $(311)$ | 2.4123 | 2.6046 | 14.06 | $0.23-4.27$ |
| $(511)$ | 1.5397 | 4.0807 | 34.50 | $0.36-6.69$ |
| $(711)$ | 1.1203 | 5.6083 | 65.17 | $0.40-9.19$ |
| $(911)$ | 0.8782 | 7.1546 | 106.07 | $0.62-11.72$ |

## A.1.2. Collimators

The collimator-bank before detector bank consists of twenty Soller collimators with collimation $10^{\prime}$ and separation $5.289^{\circ}$.

Collimator sheets: Gd coated mylar-fnil

Transmission through a single foil:

| angle | transm. (1 $\AA)$ | transm. (2 $\AA)$ |
| :---: | :---: | :---: |
| $90^{\circ}$ | 0.92 | 0.85 |
| $10^{\prime}$ | $7 \cdot 10^{-13}$ | $5 \cdot 10^{-25}$ |
| $20^{\prime}$ | $9 \cdot 10^{-7}$ | $7 \cdot 10^{-13}$ |

# Collimation: Reactor - Monochromator $\mathbf{1 5}^{\prime}, 30^{\prime}$ or $60^{\prime}$ <br> Monochromator - Sample 10' <br> Sample - Dectector $\quad 10^{\prime}$ 

## A.1.3. Detector-bank

20 single ${ }^{3} \mathrm{He}$ detectors: I ND, Inc. type 2624
${ }^{3} \mathrm{He}$ pressure 5 atm
Effective volume $20 \times 20 \times 100 \mathrm{~mm}^{3}$
High Voltage 1300 V
Gas amplification $\approx 15$
Separation between Detectors $\quad 5.289^{\circ}$

## Appendix A.2. Electronic Set-Up

## A2.1. 'fAS3-Set-Up

Beam: Thermal

Special features:

|  | motor | No. of steps/degree |
| :---: | :---: | :---: |
| Detector bank | M5 | 100 |
| Collimator bank | M6 | 2000 |

NB: The following cables should be checked:

1) In the CAMAC CRATE there should always be a cable from the upper INH ALL in the HYTEC module to the back of the MATRIX encoder in the NIM bin.
2) On the top of the MOTOR DRIVE cupboard cable 240 should be connected to the left most unit and cables 333 and 142 to the adjacent motor unit.

## A.2.2. Detector electronics

1 Single High-Voltage supply.
20 Pre-amplifiers mounted directly on top of the Detectors.
10 Double amplifier/SCA (Single Channel Analyser) units. DCoffset and gain can be adjusted individually for all 20 amplifiers.

1 Power module with potentiometers for setting of a common lower and upper limit for all twenty SCA.

Adjustment of amplifier/SCA P1849:


Fig. 10. Double A mp/SCA module
Adjust gain so that the maximum peakheight for the signals is 4 V .

Adjust offset so that background is $\mathbf{0} \mathbf{V}$.

Connect oscilloscope to terminals GND (ground) and AMPOUT.
Oscilloscope settings:
Vertical 1V/division DC
Timebase $1 \mu$ sidivision
Trigg Coupl DC
Trig mode TRIG


Adjustment of common discriminator levels for the SCA's P1850:

Fig. 11. Power module
Adjust the lower limit so that it exceeds the electronic noise level.
Typical setting 0.7-1.0 V.
Adjust the upper limit so that it exceeds the 'neutron'pulse height.
Typical setting 4.5-5.0 V .

Connect oscilloscope to terminals GND (ground) and LOW.OUT or UPP.OUT, respectively.

Oscilloscope settings:
Vertical 1V/division DC
Timebase Irrelevant
Trig Coupl DC
Trig mode AUTO

## Appendix A.3. Powder Line-Broadening due to Vertical Divergence

## A.3.1. Problem

A crystalline powder scatters a horizontal monochromatic beam into a Debye-Scherrer cone of opening angle $2 \theta$ (see Fig. 12). For the special case of $2 \theta=90^{\circ}$ the cone is degenerated into a vertical flat disc. In that special case the horizontal component of the scattered ray is independent of the azimuthal angle $t$ around the DebyeScherrer cone. But for $2 \theta<90^{\circ}$ this horizontal component is less than $2 \theta$, whereas for $2 \theta>90^{\circ}$ the horizontal component is larger than 2A. In a powder diffractometer with vertical Soller slits before the detector, the powder line will be broadened to the low angle side for $2 \theta<90^{\circ}$ and similarly to the high angle side for $2 \theta>90^{\circ}$. It is the purpose of this appendix to calculate the corresponding powder line-shape.

## A. 3.2. Quantitative Evaluation

The incident, horizontal wave vector $\mathbf{k}_{\mathbf{i}}=\mathbf{O R}$ is Bragg scattered through angle $2 \theta$ in the horizontal plane to wave vector $\mathbf{k}_{\boldsymbol{f}}=\mathbf{O Q}$, the wave vector transfer t being a reciprocal lattice vector of a particular grain in the powder (see Fig. 12). Since the problem is entirely geometric we can choose our units of reciprocal space so that $\left|\mathbf{k}_{\boldsymbol{i}}\right|=\left|\mathbf{k}_{\mathrm{i}}\right|=1$. In general the scattered wave vector $\mathbf{k}_{\boldsymbol{f}}$ is not horizontal but is somewhere on the Debye-Scherrer cone, say along OP' with azimuthal angle $t$. The projection of $O P$ on the horizontal plane is $O P^{\prime}$. The Cartesian coordinates of OP, OP' and OQ are

$$
\left.\begin{array}{l}
\text { OP }=(\sin 2 \theta \operatorname{cost}, \cos 2 \theta, \sin 2 \theta \sin t) \\
\text { OQ }=(\sin 2 \theta, \quad \cos 2 \theta, \quad 0 \quad) \\
\text { OP } P^{\prime}=(\sin 2 \theta \cos t, \cos 2 \theta,
\end{array} \quad 0 \quad\right)
$$

The vertical angle $v$ of the scattered ray $O P$ is given by

$$
\begin{equation*}
\sin v=\sin 2 \theta \sin t \tag{Al}
\end{equation*}
$$



Fig. 12. Scattering geometry used to calculate the diffraction lineprofile from a DebyeScherrer cone for a high detector.
and the length of $O P^{\prime}$ is simply cosv.

The angular difference in the horizontal plane between $\mathrm{OP}^{\prime}$ and $\mathbf{O Q}$ is denoted $\delta$, and we want to determine $\delta$ for given values of $v$ and $2 \theta$. This is easily done by evaluating the scalar product of OP' and OQ:

$$
O P^{\prime} \cdot O Q=\cos v \cdot 1 \cdot \cos \delta
$$

or

$$
\begin{equation*}
\operatorname{cosv} \cos \delta=\left|1-(1-\operatorname{cost}) \sin ^{2} 20\right| \tag{A2}
\end{equation*}
$$

Let us, for brevity denote $\sin 2 H$ by a:

$$
\begin{equation*}
a \equiv \sin 20 \tag{A3}
\end{equation*}
$$

The angles $v$ and $t$ are small, and by series expansion one obtains from Eq. (A1) the approximate relation

$$
\begin{equation*}
v(t)=a\left(11-t^{2} / 6\left(t-a^{2}\right)\right) \tag{Ala}
\end{equation*}
$$

Equation (A2) is evaluated in a similar manner resulting in

$$
\begin{equation*}
\delta(t)=\left(t^{2} / 2\right) a\left(1-a^{2}\right)^{-1 / 2} \tag{A2a}
\end{equation*}
$$

when utilizing the result of Eq. (A1a).

The detector can only accept vertical angles less than a certain limit $\mathrm{v}_{1}$ set by the detector height Z and the distance R to the sample:

$$
\begin{equation*}
|V| \leq v_{1} \quad \text { with } \tan v_{1}=Z /(2 R) \tag{A4a}
\end{equation*}
$$

The corresponding maximal azimuthal angle $t_{1}$ is derived from Eq. (A1)

$$
\begin{equation*}
\operatorname{sint}_{1}=a^{-1} \cdot \sin v_{1} \tag{A4b}
\end{equation*}
$$

and the corresponding maximal angle $\delta, \delta_{1}$, from Eqs. (A1) and (A2) is given by

$$
\begin{equation*}
\left.\operatorname{cosv}_{1} \cos \delta_{1}=11-(1-\operatorname{cost},) a^{2}\right] \tag{A4c}
\end{equation*}
$$

The scattered intensity is evenly distributed around the DebyeScherrer cone assuming no texture in the grain orientation in the sample. The distribution in terms of the variable $\delta, f(\delta)$, is then given by

$$
\begin{equation*}
f(\delta) \cdot d \delta=t_{1}^{-1} \cdot d t \tag{A5}
\end{equation*}
$$

or

$$
\begin{equation*}
f(\delta)=(t, d \delta / d t)^{-1} \tag{A6}
\end{equation*}
$$

Inserting the derivative, $\mathrm{d} 8 / \mathrm{dt}$, from Eq. (A2a) in terms of the variable $\delta$ and its extremal value $8_{1}$ one finds

$$
f(\delta)= \begin{cases}\left(2 \sqrt{8 \delta_{1}},-1\right. & \text { for } 0<\delta<\delta_{1}  \tag{A7}\\ 0 & \text { for all uther } \delta\end{cases}
$$

Finally we shall consider the folding of $f(8)$ with the resolution function which we assume to be Gaussian, $G(8)$, with a certain standard deviation o. The general expression for the observed lineshape at a spectrometer misset $8_{0}$ from the ideal Bragg angle of $2 \theta$ is

$$
\begin{equation*}
I\left(\delta_{0}\right)=\int_{\delta=-\infty}^{\infty} G\left(\delta-\delta_{0}\right) f(\delta) d \delta \tag{A8}
\end{equation*}
$$

It is convenient to measure $\delta, \delta_{0}$ and $\delta_{1}$ in units of the standard deviation $\sigma$ so in terms of the dimensionless variables

$$
\begin{equation*}
x \equiv \delta / 0, x_{0} \equiv \delta_{0} / 0 \text { and } x_{1} \equiv \delta_{1} / 0 \tag{A9}
\end{equation*}
$$

we get

$$
\begin{equation*}
I\left(x_{0}\right)=\int_{0}^{x_{1}} \frac{1}{2 \sqrt{x x_{1}}} \frac{1}{\sqrt{2 n}} e^{-i x-x_{0}^{1} / 2} d x \tag{A10}
\end{equation*}
$$

An example is given in Fig. 13. Here the Bragg scattering angle $2 \theta_{B}=10^{\circ}$, and an appreciable amount of the Debye-Scherrer cone intensity $\left(-28^{\circ}<t<28^{\circ}\right)$ is picked up by the 10 cm high detector at a distance of $\mathbf{6 0 ~ c m}$ from the sample. The corresponding maximal horizontal deviation $\delta_{1}$ is $1.2^{\circ}$ and the powder line has in accordance a low-angle tail extending out to $\delta_{1}$. Note that the problem is symmetric around $2 \theta=90^{\circ}$; in other words a similar line shape, but mirrored so low angles become high angles, would occur at $\mathbf{2 H}=\mathbf{1 7 0 ^ { \circ }}$. In practice though, the resolution which we at $10^{\circ}$ take to be $\sqrt{ } 2$ times the angular width of each Soller collimator, is wider at $\mathbf{2 H} \div 170^{\circ}$ due to the wavelength spread of the incident beam.


Fig. 13. Calculated diffraction line-profile for a 10 cm high detector at $2 \theta_{\mathrm{B}}$ $=10^{\circ}$. Distance detector. sample 60 cm , collimation 10'(single Soller FWHM).

## Appendix A.4. Example of Computer Aided Line-Up Sequence

Below is an example of lining-up the spectrometer using the LU1LU5 commands of the TASCOM system for the multidetector spectrometer. All input typoed by the user has been underlined.

```
#
```




```
F: -5xix culintion tomem
```



```
\because5x> *-x 3is:
|!格0
```





```
#%%
```




```
\begin{tabular}{|c|c|c|c|}
\hline \[
\begin{gathered}
\vdots \\
: \because:-: .
\end{gathered}
\] & \(\because\) &  : &  \\
\hline [1]: & 1.5itic & 0 & 1.5 \\
\hline : \(1: 1\) & [.:\%4 & \(2]\) & 30.9 \\
\hline \(=\) & T.EO7 & 37 & 1.4 \\
\hline 5 & 9.4.4t & - \(]\) & 2is. \\
\hline : &  & 47 & 4.5 \\
\hline :19 & 3.6859 & 5 & 17.9 \\
\hline 59: & - 4230 & 5 & 5.0 \\
\hline \% & ?.7nem & \({ }^{4}\) & 16.0 \\
\hline !:? & 1,07ij & 67 & 7.0 \\
\hline (bi) & 4.上;4 & 3 & 20.0 \\
\hline
\end{tabular}
```





## rou ate now in lue.ras






```
: an ax Exin
```







$\begin{array}{lll}1 & 9.53854 & 0.57744 \\ 5 & 30.67 \% & 197.605\end{array}$



:






$\because 5$ Mer




```
3N: Cjirsom;
    * = 0.00%%%

```

30

```




```

| ： | ＝ | E | 6 | － | 5 | ： | F | － |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ： | －1．1． | －30． | 2 mm ． | －102． | C．Bes |  | 2w－ | 5tat |
| － | Wat． | －5． | 50. | － | 4 min | 28＊＊ | 2004 | 5＊島 |
| 3 | －ed． | －85． | 20. | 4nat． | an | 3 | \％03． | 5iten |
| 1 | －reat | －絈． | 2100 | cama | －20t | E．tw | 2 Ta | 54．0．00 |
| $\underline{1}$ | cela | －17． | 2nest | amen | C．123 | A．de | 7TM0 | 5100 |
| ＋ | －35 | －89． | 3040 | －ntut． | －403 | 4．tin | 2－10 | 3400 |
| ： | －tis | －173． | 200. | － | Q．rs | ame | ates | Su－年 |
| 즐 | －i゙¢ | －5． | 2404． | －10． | 4 4 \％ | 3 Hen | 4010．0 | 3n＋0 |
| － | －mis | － | Tom． | amiol | 4－mit |  | ：75Ps | 94．0\％ |
| ： | Tal | － 5. | Hes． | －1．0． | E．ENE | ：13\％ | 2006． 0 | －1．th |
| ： | － | －8． | 3 m | － |  | 500\％ | －${ }^{\text {a }}$ | 4．07 |
| ： | －Efs？ | －3\％． | 3uent | Tand |  |  | 33\％ | 9404 |
| $:$ | Fioi | 4. | － | － | 0.801 | Hat | 57\％ | 8．0．0 |
| $\because$ | －7．0． | 0. | Jemp | andm | andy | 214．0 | － 90.4 | H．${ }^{\text {a }}$ |
| ！ | －30．0． | $\underline{1}$. | 2mot. |  | turs | 46．0．0 | ：20．7 | 24.8 |
| ： | －rel． | t． | Sevor | crues． | 40ns | 12．w | －37．4 | Sex |
| ： 7 | －Tal． | 70． | 3－4． |  | －．ind | 4T＊ | 57x | 9\％${ }^{\text {at }}$ |
| ：－ | －36．3． | H． | 300． |  | －cist | 1000 | 3 mb | 39\％或 |
| 5 | ？ | 11. | 300． | ． | ante | 5．en | 2513＋ | 946 |
| $\therefore$ | －30］． | th． | 240． | 180． | E．10， | 780 | 24．7． | Smicos |
| －1 | －20． | 158. | 200． | － |  | 2．0n | ate | Sx．${ }^{\text {ch }}$ |
| $\because$ | Tilus | 17. | 2 m |  | 45w | 3n＋ | 7ned | 94．0 |
| 7 | － | 17． | Hen |  | 4854 | R．dit | 可嵒 | 901－ |
| 8 | －90］． | if． | zue． |  | C．10n | 囫相 | 200） | 38．09 |
| － | －3bil | 23. | 3 ln |  | ＊．89\％ | 3．0．tim | 工雨 | Sit |
| $\therefore$ | －5\％4． | Si． | 206． | nemb | － 1884 | Q80＊ | F＝0it | 94ind |

```











等






ジット





```

$\therefore$ :5:

```
c5w

\begin{tabular}{|c|c|c|}
\hline －10ek & & \\
\hline I & S¢7．74 & 25．0．0 \\
\hline ： & ［567．97 & 4．4750 \\
\hline
\end{tabular}






For
－





\begin{tabular}{|c|c|}
\hline Exaflectio & TH04 \\
\hline （111） & ［．920］ \\
\hline （113） & 3．4030 \\
\hline （60） & 4.4809 \\
\hline 1851 & s．ema \\
\hline （119） & 5．7800 \\
\hline ［15， & 7．25\％\％ \\
\hline （11） & 1.93131 \\
\hline （37） & 4.80 \\
\hline 12．） & 5．420．4 \\
\hline 138， & ［1．i56］3 \\
\hline
\end{tabular}






20－mave日 16：30）

\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|c|c|c|c|}
\hline \multirow[t]{2}{*}{\begin{tabular}{l}
「風要： \\
587 ：
\end{tabular}} & 1504 & \multirow[t]{2}{*}{} & \multirow[t]{2}{*}{85} & \multicolumn{2}{|l|}{－ 15.2178} & ＊ & \multicolumn{2}{|l|}{2.700 m} & \multirow[t]{2}{*}{15} & \multicolumn{2}{|c|}{2．324} & \multirow[t]{2}{*}{Own ：} & \multirow[t]{2}{*}{10．0ent} \\
\hline & N00 & & & & & & & & & & & & \\
\hline \(J\) & 明 & \(\cdots\) & & 6 & \(\omega\) & 0 & t & F & & b & ITC & & \\
\hline 1 & －3x） & & 1. & IS3． & 3203． & 2.451 & P． & 753．0 & & 501．0 & 67．06\％ & & \\
\hline － & －4803． & & 1. & 691． & 2000． & 2．7907 & 14．000 & 744．0 & & 30．1．0 & 07.040 & & \\
\hline 3 & －Ti4］． & & 1. & tese． &  & 2．fir & 14．60 & 7\％ & & 1081．0 & 67．850 & & \\
\hline 4 & － 86. & & 1. & 508． & STEM． & 2．517 & 11．080 & 7n．e & & 3001.0 & 67．140 & & \\
\hline ？ & －－59．3． & & 1. & 185. & 31\％． & 2．574 & 11.000 & 13 Br 4 & & 12 l 1.8 & 67．140 & & \\
\hline 6 & －20． & & 1. & ［14， & 3 me ． & 3．040 & 30．009 & 712．0 & & 1006．0 & 67．220 & & \\
\hline ＇ & －50． & & 1. & 1047. & T30． & 3，0025 & S．0en & 7414．0 & & 1031．0 & 47．24＊ & & \\
\hline 3 & －tw & & \(f\). & 5471. & \(3 \times 120\). & 3．0041 & －100 & 740）． 0 & & 109\％．0 & 17．309 & & \\
\hline ＊ & －\({ }^{\text {ces }}\) ． & & J， & 197． & 3780 & 1．0i51 & 13.00 & 753.0 & & 1001．0 & 47．3070 & & \\
\hline （i） & －5\％4． & & 1. & 678． & HFTh． & 3．0973 & 17．00 & 750．0 & & 50tt． 6 & 17．370 & & \\
\hline \(: 1\) & －053． & & 1. & 146. & 3 N & 3．004 & 214．00 & 754.0 & & cioth of & 47．47\％ & & \\
\hline t： & －70）． & & 1. & 14．7． & 7274． & 2，0109 & 30.60 & 785.0 & & ICol．0 & 67．460 & & \\
\hline 12 & －54． & & 1. & \(19 \% 1\). & 3153. & 2．012 & 47．00 & 730.4 & & Smet． 6 & 67．509\％ & & \\
\hline 11 & －5\％N． & & 1. & 198. & 7 TNO & 3．013\％ & 10，09 & 7atil & & S01．9 & 67.509 & & \\
\hline 15 & －503． & & 6. & 197. & STM． & J．01F & 41．06 & 310． & & 10\％100 & 67.580 & & \\
\hline \(!6\) & －PAJ． & & 1. & \(20 p 3\). & 20．0． & 3.0147 & W2．0．0 & 7\％6．0 & & H00t．0 & 17．860 & & \\
\hline \(\because\) & －6is）． & & 1. & zut． & 4 H & 3.918 & ग7．00 & 7814.0 & & 1095．0 & 67.040 & & \\
\hline 13 & －9\％3． & & 1. & 7215， & 4／80． & 3.019 & 13．09 & 74\％．6 & & sivid & 47．70\％ & & \\
\hline ！ & －763． & & 1. & 2015. & 40tw． & J．624 & 10．00 & 782.9 & & 10018 & 67．7400 & & \\
\hline \(\therefore\) & －503． & & 6. & 2019. & 比为． & 1.000 & 121.00 & 747.0 & & 1001.0 & 17．749 & & \\
\hline 3 & ＋5］． & & 1. & 2023. & ¢040． & 3.054 & 83．000 & \＄427．0 & & sels． 6 & 67．080 & & \\
\hline 4 & FG\％ & & 1. & 2727. & 0 Nos． & 3.077 & R．009 & 7597. & & 1904， 0 & 67．840 & & \\
\hline 7 & －54． & & 1. & 2031. & Hint． & 3.6871 & 27．009 & 7411.6 & & 1061.0 & 67．4010 & & \\
\hline 3 & －2505． & & 1. & 745， & \(40 \% 0\). & 3.063 & 16.000 & 742.6 & & 1001，0 & 67.9487 & & \\
\hline \％ & －6．0． & & 1. & 2517， & 0970. & 3.090 & 15，090 & 74．0 & & 1001.0 & 67．780 & & \\
\hline \(\therefore\) & －63\％． & & 1. & 2043. & 400． & 3.634 & 0．004 & 70．0 & & 10 LL .0 & 40．03\％ & & \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|}
\hline  & 16：\％10 &  \\
\hline
\end{tabular}

Ef3:1 W ©


    1 16i.119 17.93
    743.52 171.8费



\section*{}


\section*{Bibliographic DataSheet}
Kise National I_aboratory Kisw-M-2720

Title and autbor(s)
The Multi-DeLector Powder Neutron Diffirachmeter
at Risp Nationallistboratory
J. Als Nieisen, N.H. Andersen, C. Brohulni, K.N. Clausen and
B. I.ebech

Date
Sune ti, 1988
1kepartment or group
Ihysics Department
(iroups own registration numberts)

\section*{PrujecUcontract no.}

\section*{Hage:}

37

\section*{Tables}

4
Illustrations
13
Helerences

\section*{Isiln}
67.550 .14148

\section*{Abstruct (Max. 2000 char.)}

Thr repurt describes a new multi-detector piwder neutron diffractometer inatalied at the DR3 roucher at hise. The report gives delails of the design criletia and aperating insuructions in order Io easc operation of the instrument by actual and potential users. the individual components (collimntars, monachromator, detecturs) are deacribed in delail. An example of a studyof the uxygen uplake of \(\mathrm{YHa}_{2} \mathrm{Cu}_{3} \mathrm{O}_{7 \times}\) is given.

Descriplars-INIS/EDA
ACCURACY;COLIIMATORS; DESIGN: MONOCHROMATOR;
NEIUTON DIFFRACTOMETEHS; POWIDERS, SPECIFICATIONS
Available on request from:


Tulephone 023712 12, ext. 2262. Teiefax 02360609```

