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Closed loop simulation for a magnetic gradiometry mission

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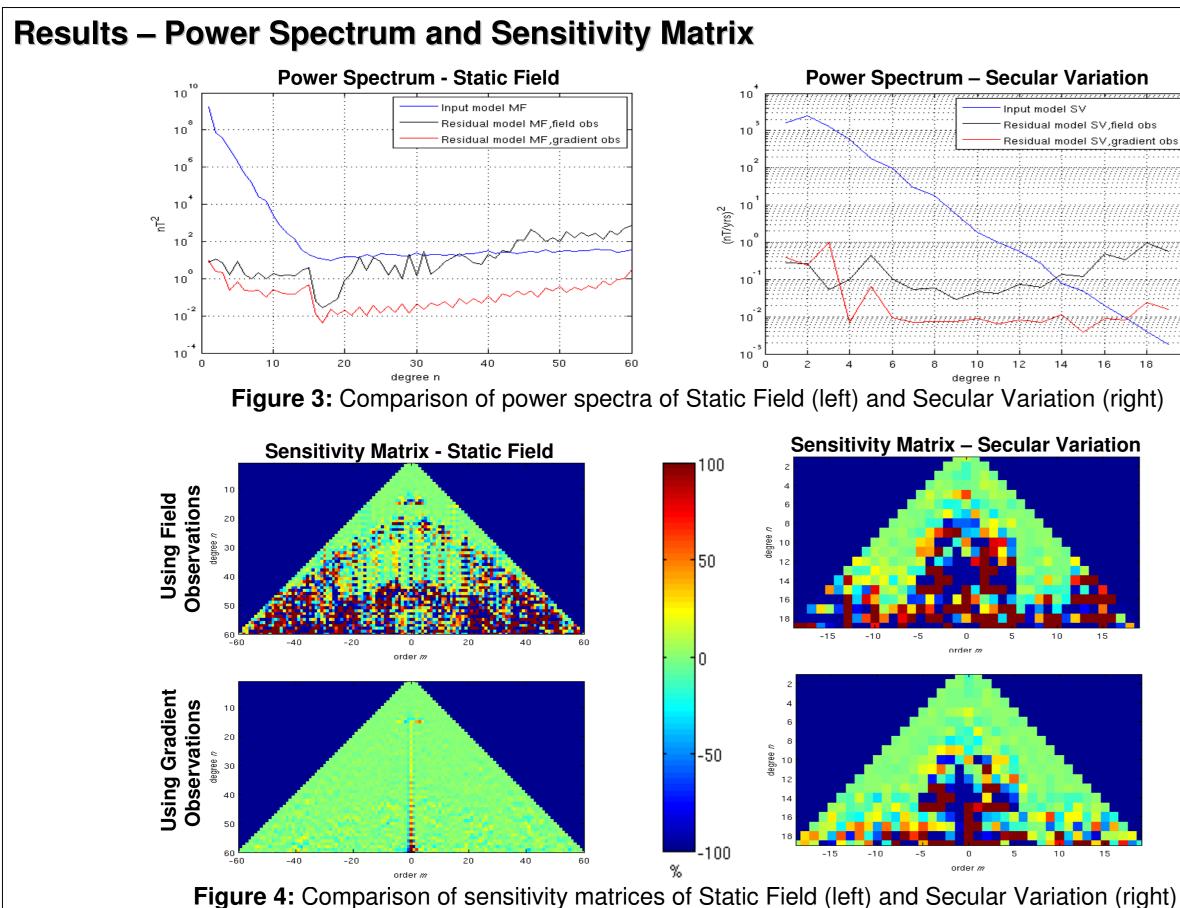
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Introduction Magnetic Gradient Tensor Visualization In the near future the Swarm satellite mission will for the first time measure the East-West Crustal field resulting from Magnetic Field model MF6 for degree values 15<n< 60 gradient of the magnetic field, which contains valuable information on the North-South oriented • The information contained in the field components is reproduced by the gradients features of crustal magnetization Going beyond Swarm, we performed a simulation of a full • Each tensor element enhances certain features of the crustal field magnetic gradiometry mission, emphasizing on the benefits of measuring the full gradient • The gradient tensor provides additional information tensor in addition to the three field components. Using simulated orbits from a low Earthorbiting satellite, synthetic data of the magnetic field vector and of the nine elements of the Crustal Field at h=300km magnetic gradient tensor are calculated using a given (input) magnetic field model for the various field contributions (in the core, lithosphere, magnetosphere, and ionosphere). From these synthetic data we estimate field models using either the magnetic vector field measurements only or full gradient observations, and compare our model retrieval with the original (input) model. This study shows qualitatively the scientific benefit of measurements of the gradient tensor in space. Magnetic Gradiometry • Measurement of the first derivative of each magnetic field component (**B**_r, **B**_θ, **B**_θ) along each spacial direction ($\mathbf{r}, \boldsymbol{\theta}, \boldsymbol{\phi}$) • In the 3D space that defines the gradient tensor, consisting of $3 \times 3 = 9$ spatial derivatives and forming a second rank tensor • Approximation when looking for small scale features • The magnetic field **B** is always a solenoid field: 8 elements instead of 9 to be identified in order to fully determine the gradient tensor • $[\nabla B]_{rr}$: outlines steep boundaries $\nabla \cdot \mathbf{B} = 0 \Leftrightarrow tr(\nabla \mathbf{B}) = 0$ • $[\nabla B]_{AB} \& [\nabla B]_{RB}$: outline East-West structures • In case we are in a source free environment: 5 instead of 8 elements to be identified in • $[\nabla B]_{m}$ & $[\nabla B]_{r}$: outline North-South structures order to fully determine the gradient tensor • $[\nabla B]_{\theta_0}$: outlines body corners **Results – Field residuals on ground Power Spectrum - Static Field** Power Spectrum – Secular Variatior Input model MF Input model Si -Residual model MF,field obs Residual model SV,field obs Residual model MF, gradient of esidual model SV.gradient 0 2 4 6 8 10 12 14 16 18 40 Figure 3: Comparison of power spectra of Static Field (left) and Secular Variation (right)

$$7\mathbf{B} = \begin{pmatrix} \frac{\partial B_r}{\partial r} & \frac{1}{r} \frac{\partial B_r}{\partial \theta} - \frac{1}{r} B_{\theta} & \frac{1}{r\sin\theta} \frac{\partial B_r}{\partial \phi} - \frac{1}{r} B_{\phi} \\ \frac{\partial B_{\theta}}{\partial r} & \frac{1}{r} \frac{\partial B_{\theta}}{\partial \theta} + \frac{1}{r} B_r & \frac{1}{r\sin\theta} \frac{\partial B_{\theta}}{\partial \phi} - \frac{\cot\theta}{r} B_{\phi} \\ \frac{\partial B_{\phi}}{\partial r} & \frac{1}{r} \frac{\partial B_{\phi}}{\partial \theta} & \frac{1}{r\sin\theta} \frac{\partial B_{\phi}}{\partial \phi} + \frac{1}{r} B_r + \frac{\cot\theta}{r} B_{\theta} \end{pmatrix} \approx \begin{pmatrix} \frac{\partial B_r}{\partial r} & \frac{1}{r} \frac{\partial B_r}{\partial \theta} & \frac{1}{r\sin\theta} \frac{\partial B_r}{\partial \phi} \\ \frac{\partial B_{\theta}}{\partial r} & \frac{1}{r} \frac{\partial B_{\phi}}{\partial \theta} & \frac{1}{r\sin\theta} \frac{\partial B_{\phi}}{\partial \phi} + \frac{1}{r} B_r + \frac{\cot\theta}{r} B_{\theta} \end{pmatrix}$$

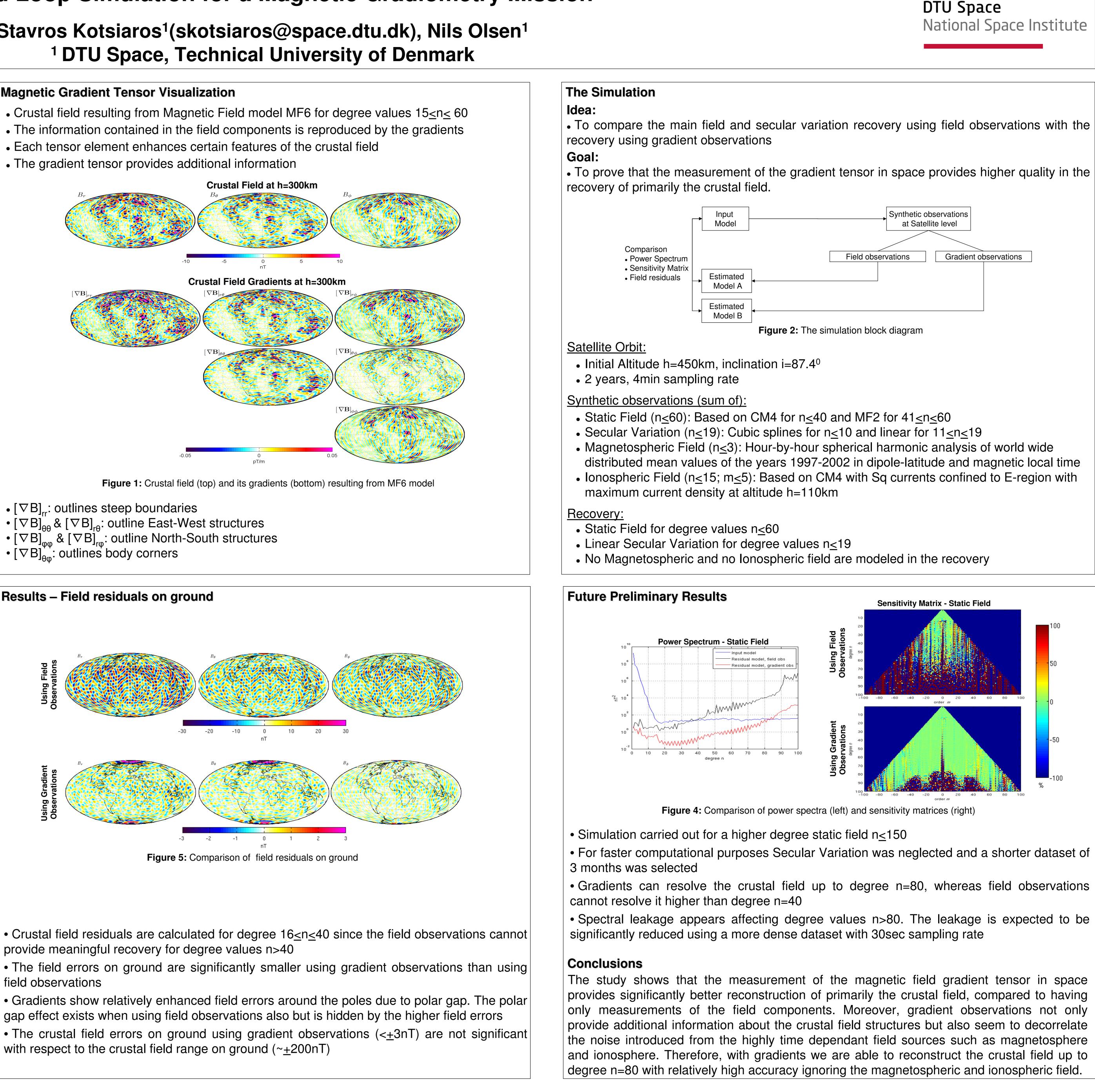
$$(\mathbf{\nabla}\mathbf{B}) = (\mathbf{\nabla}\mathbf{B})^T$$



• Gradients reconstruct the crustal field with 100 times higher accuracy and the Secular Variation with 10 times higher accuracy than field observations • Gradients can resolve the crustal field higher than degree 60 and the Secular variation up to degree 17, whereas field observations cannot go higher than degree 40 and 12 respectively • Gradients suppress the effect of spectral leakage from magnetospheric and ionospheric field which is shown as enhanced diagonal error structures when using field observations • Gradients recover Secular Variation with higher accuracy compared to field observations especially for tesseral coefficients

Closed Loop Simulation for a Magnetic Gradiometry Mission

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provide meaningful recovery for degree values n>40 field observations

with respect to the crustal field range on ground ($\sim \pm 200$ nT)