brought to you by I CORE

Technical University of Denmark



Pressure-induced changes in Cr3+-doped elpasolites and LiCaAlF6: Interpretation of macroscopic data

Trueba, A.,; García Lastra, Juan Maria; Aramburu, J. A.; García-Fernández, P.; Barriuso, M. T.; Moreno,

Published in:

Physical Review B (Condensed Matter and Materials Physics)

Link to article, DOI: 10.1103/PhysRevB.81.233104

Publication date:

2010

Document Version Publisher's PDF, also known as Version of record

Link back to DTU Orbit

Citation (APA):

Trueba, A. ., García Lastra, J. M., Aramburu, J. A., García-Fernández, P., Barriuso, M. T., & Moreno, M. (2010). Pressure-induced changes in Cr3+-doped elpasolites and LiCaAlF6: Interpretation of macroscopic data. Physical Review B (Condensed Matter and Materials Physics), 81(23), 233104. DOI: 10.1103/PhysRevB.81.233104

DTU Library

Technical Information Center of Denmark

General rights

Copyright and moral rights for the publications made accessible in the public portal are retained by the authors and/or other copyright owners and it is a condition of accessing publications that users recognise and abide by the legal requirements associated with these rights.

- Users may download and print one copy of any publication from the public portal for the purpose of private study or research.
- You may not further distribute the material or use it for any profit-making activity or commercial gain
- You may freely distribute the URL identifying the publication in the public portal

Pressure-induced changes in Cr³⁺-doped elpasolites and LiCaAlF₆: Interpretation of macroscopic data

A. Trueba, ¹ J. M. García-Lastra, ² J. A. Aramburu, ¹ P. García-Fernández, ¹ M. T. Barriuso, ³ and M. Moreno ¹ Grupo de Física Computacional de Materiales, Departamento de Ciencias de la Tierra y Física de la Materia Condensada, Universidad de Cantabria, Avenida de los Castros s/n, 39005 Santander, Spain

²Center for Atomic-Scale Materials Design, Department of Physics, Technical University of Denmark, DK-2800 Kongens Lyngby, Denmark

³Grupo de Física Computacional de Materiales, Departamento de Física Moderna, Universidad de Cantabria, Avenida de los Castros s/n, 39005 Santander, Spain

(Received 3 May 2010; revised manuscript received 4 June 2010; published 24 June 2010)

In the research of pressure effects on Cr^{3+} -doped insulating lattices, it is crucial to understand the dependence of the 10Dq parameter on the sample volume, V. This problem is explored in the present work through *ab initio* calculations on Cr^{3+} -doped K_2NaScF_6 , Cs_2NaYCl_6 , and Cs_2NaYBr_6 elpasolite lattices as a function of pressure in the 0–5 GPa range. From the calculated values of the lattice parameter and the Cr^{3+} - X^- (X=F, Cl, and Br) distance, R, it is found that R varies with the cell volume, v_c , as $v_c^{(1/3\beta)}$ where β lies around 2.6. These results allow one to understand quantitatively the 10Dq dependence on $V^{-m/3}$ for $LiCaAlF_6:Cr^{3+}$ where the measured exponent m=2.3 is seemingly anomalous when compared to the values found for ruby (m=4.5) or NiO (m=5).

DOI: 10.1103/PhysRevB.81.233104 PACS number(s): 71.70.-d, 61.50.Ks, 71.15.-m, 71.55.-i

During the last decades, the interest in obtaining new tunable solid-state lasers and photoluminiscent materials has greatly promoted the study of optical properties of insulating materials doped with Cr³+ ions.¹-³ In this domain of research, particular attention has been paid to the changes in optical properties induced by an applied pressure.⁴ Indeed pressure modifies the energy of electronic transitions related to a transition-metal complex, a property widely used for measuring the actual value of pressure in diamond-anvil cells using the Cr³+ emission.⁵.⁶ Moreover, in the case of halide host lattices doped with Cr³+ ions pressure can change the nature of the first excited state responsible for the luminescence. This spin crossover transition produces a strong variation in the emission pattern going from a broad band to a sharp one.⁵-10

Among the host lattices used for incorporating Cr^{3+} impurities, a great deal of work has been carried out on those involving a trivalent cation^{10–19} such as Al_2O_3 , K_2NaScF_6 , K_2NaYCl_6 , or $LiCaAlF_6$. Indeed in these cases, the Cr^{3+} impurity enters the trivalent site thus giving rise to a center without any close charge compensation, a situation which is thus markedly different from that appearing in systems such as $KMF_3: Cr^{3+}$ or $K_2MF_4: Cr^{3+}$ (M=Mg and Zn) where different centers are simultaneously observed.^{8,9,20}

When a hydrostatic pressure, P, is applied on a halide lattice doped with Cr^{3+} it is crucial to look into the variations induced on the cubic-field splitting parameter, 10Dq. Indeed this parameter alone governs the position of the first spin allowed transition $^4A_2 \rightarrow ^4T_2$ in octahedral symmetry, and, in particular, its separation with respect to the sharp $^4A_2 \rightarrow ^2E$ transition as the later is much less sensitive to an applied pressure. 5,6,11 Experimental results obtained on pure insulator materials such as 21,22 NiO or MnO under pressure reveal that 10Dq is related to the macroscopic sample volume, V, through the law,

$$\frac{10Dq}{10Dq_0} = \left(\frac{V_0}{V}\right)^{m/3}.\tag{1}$$

Here V_0 and $10Dq_0$ refer to the values at zero pressure while the exponent m is found to be equal to 5. A similar law has been derived for ruby under pressure 11 obtaining m=4.5. Values of the exponent m around 5 have also been measured for Al_2O_3 doped with trivalent cations 23 such as Ti^{3+} , V^{3+} , or Ni^{3+} .

From a microscopic standpoint when an impurity, M^{c+} , enters an insulating lattice its valence electrons are usually *confined* in the $MX_{\rm N}^{c-{\rm Na}}$ complex formed with the N nearest X^{a-} anions. 24 Along this line, it should be noticed that according to Kohn, the localization of electrons is the fingerprint of every insulating material. 25,26 Bearing in mind these considerations, it turns out that 10Dq for an octahedral MX_6^{c-6a} complex microscopically depends on the M-X distance, R. The law describing the R dependence of 10Dq derived from theoretical calculations is found to be $^{24-28}$

$$\frac{10Dq}{10Dq_0} = \left(\frac{R_0}{R}\right)^n,\tag{2}$$

where the n exponent is usually found to lie in the 4–6 region.²⁴ The microscopic origin of this strong dependence of 10Dq on R has previously been discussed.^{24,29} The link between Eqs. (1) and (2) is easily made for NiO or MnO compounds exhibiting a NaCl crystal structure. Indeed in this simple lattice structure the cell volume, v_c , and thus the sample volume, V, are necessarily proportional to R^3 thus implying m=n.

However, recent measurements carried out on LiCaAlF₆: Cr^{3+} reveal¹⁰ that the macroscopic exponent m is not close to 5 but only equal to 2.3 a result which is thus seemingly surprising when compared to the figures measured

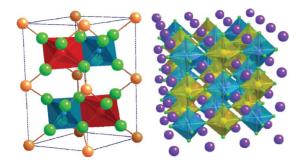


FIG. 1. (Color online) Left: unit cell of the LiCaAlF₆ structure, colquiriite-type with trigonal space group P31c, showing AlF₆ (blue) and LiF₆ (red) slightly distorted octahedra. Right: cubic elpasolite K₂NaScF₆ structure, with space group Fm3m, showing ScF₆ (blue) and NaF₆ (yellow) perfect octahedra. The ratio between the Sc³⁺-F⁻ distance and the lattice parameter, a, defines the u parameter.

for Al₂O₃: M^{3+} (M=Cr, Ti, V, and Ni), NiO, or MnO under hydrostatic pressures. 11,21–23 Nevertheless, considering the crystal structure³⁰ of LiCaAlF₆ (Fig. 1) the anomalous value of the exponent m measured for LiCaAlF₆: Cr^{3+} might simply reflect that the simple cubic power relation between R and the cell volume, v_c , no longer holds. In fact, in the colquiriite-type LiCaAlF₆ structure the CrF_6^{3-} complex (formed under $Al^{3+} \rightarrow Cr^{3+}$ substitution) is embedded in a softer region involving monovalent and divalent cations. A similar situation holds for cubic elpasolite lattices such as K₂NaScF₆ (Fig. 1) doped with Cr³⁺ where in the region outside the CrF₆³⁻ complex there are only monovalent cations. Owing to this fact if the lattice parameter, a, of cubic elpasolite host lattices such as K2NaScF6, Cs2NaYCl6, or Cs₂NaYBr₆ is varied by a hydrostatic pressure we do not know, a priori, how this change will modify the microscopic volume of the hard CrX_6^{3-} unit (X=F, Cl, and Br) contained in it.

Bearing in mind this analysis, a quantitative interpretation of the experimental dependence of 10Dq on the macroscopic volume, V, requires one to determine the actual relationship between the cell volume and R for any applied pressure. This work is aimed at building this bridge by means of ab initio calculations. As, at variance with colquiriite LiCaAlF₆, elpasolites such as K2NaScF6, Cs2NaYCl6, or Cs2NaYBr6 are cubic, 15 we have first looked into the pressure dependence of both the lattice parameter, a, and the Cr^{3+} -ligand distance, R, for this simpler type of lattice. In order to properly achieve this goal, we report here the calculated pressure dependence of a and R quantities for Cr³⁺-doped K₂NaScF₆, Cs₂NaYBr₆, and Cs2NaYCl6 lattices involving different halide anions. Data corresponding to the first two systems have been calculated for the present work while results for Cs₂NaYCl₆: Cr³⁺ have been derived from the analysis of data conveyed in a previous study.31

Seeking to obtain reliable values of a and R parameters as a function of P, we have performed both periodic and cluster calculations following a method which has previously been tested. Periodic calculations have been performed by means of plane-wave calculations using pseudopotentials under the framework of the density-functional theory. The

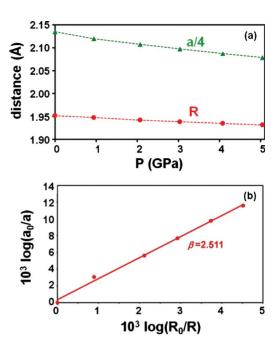


FIG. 2. (Color online) (a) Variation in the lattice parameter, a, and metal-ligand distance, R, in Cr^{3+} -doped K_2NaScF_6 upon applied pressure. (b) Relative variation in the lattice constant with respect to the metal-ligand distance in K_2NaScF_6 : Cr^{3+} .

Perdew-Burke-Ernzehoff exchange-correlation functional³² was employed in combination with the Fritz-Haber institute library's pseudopotentials, 33 a $2 \times 2 \times 2$ reciprocal-space sampling mesh and a plane-wave kinetic energy cutoff of 40 hartree. The ABINIT code³⁴ version 5.4.4 was used throughout these calculations. In particular, we have performed geometry optimizations for several values of the pressure in the range from 0 to 5 GPa, keeping the symmetry of the lattice. At each value of the external pressure, both the lattice parameter, a, and the u parameter, characteristic of the elpasolite structure [Fig. 1(b)], have been derived. In a second step, the geometry of $CrX_6M_8Na_6^{11+}$ (X=F, Cl, Br, and I; M=Cs and K) clusters has been optimized to obtain the local geometry around the Cr³⁺ impurity in the three K₂NaScF₆, Cs₂NaYCl₆, and Cs₂NaYBr₆ cubic elpasolites. In this case, the calculations were performed using the Becke-Perdew exchange-correlation functional^{35,36} and high-quality basis sets of triple-ζ plus polarization type formed of localized Slater-type functions as implemented in the 2008 and 2009 version of the ADF code.³⁷ Additional data on the method of calculation can be found in Ref. 31.

Obtained results on the pressure dependence of a and R parameters for K_2NaScF_6 : Cr^{3+} are displayed in Fig. 2(a). It should be noted first of all that the calculated values at zero pressure, a_0 and R_0 , compare well with available experimental data. For instance, the obtained a_0 =8.54 Å figure derived in the present calculations is only 0.8% higher than the experimental one. In the same vein R_0 =1.95 Å derived for K_2NaScF_6 : Cr^{3+} , it is not unreasonable when compared to the R_0 values measured for pure compounds containing CrF_6^3 units such as K_2NaCrF_6 (R_e =1.93 Å) or Rb_2KCrF_6 (R_e =1.94 Å).

It can be noted in Fig. 2(a) that the relative decrease in a

TABLE I. Calculated values of β and n exponents for the three elpasolite lattices doped with Cr^{3+} . The value of the macroscopic exponent, m, is derived through Eq. (4).

System	β	n	m
K ₂ NaScF ₆ : Cr ³⁺	2.51	4.5	1.80
Cs ₂ NaYCl ₆ : Cr ³⁺	2.44	4.5	1.84
$Cs_2NaYBr_6:Cr^{3+}$	2.89	4.8	1.66

induced by pressure is clearly higher than that experienced by the Cr^{3+} -F⁻ distance. This results confirms, albeit qualitatively, that a change in the lattice parameter due to pressure leads to smaller effects on the *hard part* of the unit cell. From the calculated a(P) and R(P) curves, the relation between a and R parameters for any value of the pressure is determined. Results are shown in Fig. 2(b) which point out that the relation between a and R is well represented by the law,

$$\frac{R_0}{R} = \left(\frac{a_0}{a}\right)^{1/\beta}.\tag{3}$$

The value of the β parameter derived from the present calculations for K_2NaGaF_6 : Cr^{3+} is found to be equal to 2.5 thus implying that R changes like $V^{1/7.5}$ instead of $V^{1/3}$. In Table I are collected the β values calculated for the three elpasolites doped with Cr^{3+} , together with the corresponding values of the exponent n reflecting the R dependence of 10Dq. A behavior quite similar to that displayed in Fig. 2 is encountered looking at the results obtained for Cr^{3+} -doped Cs_2NaYCl_6 and Cs_2NaYBr_6 lattices with values of the exponent β close to that found for K_2NaScF_6 : Cr^{3+} . It can be noticed that for the three systems, the calculated figures for the exponent n are around 5. A similar conclusion was reached in the work by Brik and Ogasawara. ²⁸

According to the present analysis, Eqs. (1)–(3) and the β values collected in Table I, there is a relation between the macroscopic exponent, m, and the microscopic exponent, n, given by

$$n = m\beta. \tag{4}$$

This simple relation and the β and n values of Table I indicate that in the case of Cr^{3+} -doped elpasolite lattices, the experimental dependence of 10Dq on the sample volume [given by Eq. (1)] should involve a *macroscopic* exponent, m, in the region 1.65–1.85 which is thus much smaller than the microscopic one.

The present study on elpasolites doped with Cr^{3+} thus sheds light on the origin of the *anomalous* m=2.3 value obtained from the experimental dependence of 10Dq on pressure for LiCaAlF₆: Cr^{3+} . As the microscopic exponent, n is essentially characteristic of the complex, then using the value n=4.5 derived for the CrF_6^{3-} unit (Table I) and Eq. (4) we get $\beta=2.0$ for LiCaAlF₆: Cr^{3+} , a value which is slightly smaller than $\beta=2.5$ calculated for K_2NaScF_6 : Cr^{3+} . This

result is certainly not unreasonable if one takes into account that the cations involved in the soft part of an elpasolite lattice are all monovalent while in the case of LiCaAlF₆ one of such cations is divalent.

The present study thus stresses that the knowledge of the actual value of the β parameter from ab initio calculations can be of great help for properly interpreting the experimental pressure dependence of optical, EPR, and Raman spectra of transition-metal impurities in insulating lattices. This knowledge is especially important when the complex formed by the impurity resides in the less compressible part of the unit cell such as it happens for Cr3+ impurities in elpasolite or LiCaAlF₆ lattices. In fact, taking as a guide the case of the microscopic exponent, n, a precise determination of its value by means of extended x-ray absorption fine structure (EX-AFS) spectroscopy would require extremely accurate measurements of the changes in R induced by an applied pressure. Bearing in mind that for K₂NaScF₆: Cr³⁺ a pressure of 5 GPa induces a reduction in R of only 2 pm [Fig. 2(a)] and that the current uncertainties on R values derived through EXAFS technique are at least of 1 pm,³⁹ a direct measurement of the microscopic exponent seems a rather difficult task to be accomplished. Probably due to this reason no direct measurements of the R dependence on pressure have been reported¹⁰ for LiCaAlF₆: Cr³⁺.

Although experimental results for $Al_2O_3:M^{3+}$ (M=Cr, Ti, V, and Ni) indicate that the β exponent is close to one this situation is likely to be no longer true²⁴ when the M^{c+} impurity replaces a host cation, H^{q+} , with smaller nominal charge (q < c). In fact, in cases such as NaCl:Rh²⁺ or $K_2MgF_4:Cr^{3+}$, the RhCl⁴⁻ and CrF_6^{3-} complexes formed with remote charge compensation are to a good extent elastically decoupled^{40,41} from the rest of the lattice. Thus, for this kind of systems β values clearly higher than the unity are also expected.

Before ending this analysis, it should be noted here that the metal-ligand distance of the CrF₆³⁻ unit can also be modified by changing the chemical pressure exerted by the lattice on the complex, for example, by changing a host lattice such as K_2NaScF_6 (a=8.47 Å) by another isomorphous one such as K_2NaAlF_6 (a=8.09 Å). The measured increase ¹⁹ in the 10Dq parameter of the CrF_6^{3-} unit on passing from $K_2NaScF_6:Cr^{3+}$ (10Dq=1.97 eV) to $K_2NaAlF_6:Cr^{3+}$ (10Dq=2.01 eV) is however only of 0.04 eV. By contrast, a reduction in the lattice parameter of K_2NaScF_6 , $\Delta a =$ −0.38 Å, by a hydrostatic pressure would lead, according to Eq. (1) and the calculated m=1.80 value, to an increase in 10Dq equal to 0.17 eV which is much higher than that found by changing the chemical pressure on the CrF_6^{3-} complex. This conclusion is thus in line with previous findings on transition metal impurities in insulating lattices showing that variations in local vibrational frequencies induced by a hydrostatic pressure can be quite different from those produced by changing the host lattice. 42,43

Further research on the present issues is now underway.

The support by the Spanish Ministerio de Ciencia y Tecnología under Project No. FIS2009-07083 is acknowledged.

- ¹R. C. Powell, *Physics of Solid-State Laser Materials* (Springer-Verlag, New York, 1998).
- ²C. E. Webb and J. D. Jones, *Handbook of Laser Technology and Applications: Laser Design and Laser Systems* (IOP, Bristol, 2004), Vol. II.
- ³T. A. Samtleben and J. Hulliger, Opt. Lasers Eng. **43**, 251 (2005).
- ⁴K. L. Bray, Top. Curr. Chem. **213**, 1 (2001).
- ⁵ A. H. Jahren, M. B. Kruger, and R. J. Jeanloz, J. Appl. Phys. **71**, 1579 (1992).
- ⁶K. Syassen, High Press. Res. **28**, 75 (2008).
- ⁷J. F. Dolan, L. A. Kappers, and R. H. Bartram, Phys. Rev. B **33**, 7339 (1986).
- ⁸ M. Mortier, Q. Wang, J. Y. Buzare, M. Rousseau, and B. Piriou, Phys. Rev. B **56**, 3022 (1997).
- ⁹P. T. C. Freire, O. Pilla, and V. Lemos, Phys. Rev. B **49**, 9232 (1994).
- ¹⁰M. N. Sanz-Ortiz, F. Rodriguez, I. Hernández, R. Valiente, and S. Kück, Phys. Rev. B 81, 045114 (2010).
- ¹¹S. Duclos, Y. K. Vohra, and A. L. Ruoff, Phys. Rev. B 41, 5372 (1990).
- ¹²J. F. Dolan, A. G. Rinzler, L. A. Kappers, and R. H. Bartram, J. Phys. Chem. Solids **53**, 905 (1992).
- ¹³H. W. H. Lee, S. A. Payne, and L. L. Chase, Phys. Rev. B 39, 8907 (1989).
- ¹⁴A. Monnier, D. Chambaz, H. Bill, H. U. Gudel, and J. Weber, J. Chem. Phys. **91**, 6650 (1989).
- ¹⁵C. Reber, H. U. Gudel, G. Meyer, T. Schleid, and C. A. Daul, Inorg. Chem. **28**, 3249 (1989).
- ¹⁶A. G. Rinzler, J. F. Dolan, L. A. Kappers, D. S. Hamilton, and R. H. Bartram, J. Phys. Chem. Solids 54, 89 (1993).
- ¹⁷O. S. Wenger and H. U. Gudel, J. Chem. Phys. **114**, 5832 (2001).
- ¹⁸P. A. Tanner, Chem. Phys. Lett. **394**, 458 (2004).
- ¹⁹I. Hernández, F. Rodriguez, and A. Tressaud, Inorg. Chem. 47, 10288 (2008).
- ²⁰H. Takeuchi, M. Arakawa, H. Aoki, T. Yosida, and K. Horai, J. Phys. Soc. Jpn. **51**, 3166 (1982).
- ²¹ H. G. Drickamer, J. Chem. Phys. **47**, 1880 (1967).
- ²² Y. Mita, Y. Sakai, D. Izaki, M. Kobayashi, S. Endo, and S. Mochizuki, Phys. Status Solidi B 223, 247 (2001).
- ²³ H. G. Drickamer and C. W. Frank, *Electronic Transitions and the*

- High Pressure Chemistry of Solids (Chapman Hall, London, 1973).
- ²⁴M. Moreno, M. T. Barriuso, J. A. Aramburu, P. García-Fernandez, and J. M. García-Lastra, J. Phys.: Condens. Matter 18, R315 (2006).
- ²⁵W. Kohn, Many Body Physics (Gordon and Breach, New York, 1968).
- ²⁶R. Resta, J. Phys.: Condens. Matter **14**, R625 (2002).
- ²⁷ V. Luaña, M. Bermejo, M. Flórez, J. M. Recio, and L. Pueyo, J. Chem. Phys. **90**, 6409 (1989).
- ²⁸M. G. Brik and K. Ogasawara, Phys. Rev. B **74**, 045105 (2006).
- ²⁹ M. Moreno, J. A. Aramburu, and M. T. Barriuso, Phys. Rev. B 56, 14423 (1997).
- ³⁰ Y. Ono, K. Nakano, K. Shimamura, T. Fukuda, and T. Kajitani, J. Cryst. Growth 229, 505 (2001).
- ³¹ J. M. García-Lastra, M. Moreno, and M. T. Barriuso, J. Chem. Phys. **128**, 144708 (2008).
- ³² J. P. Perdew, K. Burke, and M. Ernzerhof, Phys. Rev. Lett. 77, 3865 (1996).
- ³³ M. Fuchs and M. Scheffler, Comput. Phys. Commun. 119, 67 (1999).
- ³⁴ X. Gonze, G. M. Rignanese, M. Verstraete *et al.*, Z. Kristallogr. **220**, 558 (2005).
- ³⁵ A. D. Becke, Phys. Rev. A **38**, 3098 (1988).
- ³⁶J. P. Perdew, Phys. Rev. B **33**, 8822 (1986).
- ³⁷G. te Velde, F. M. Bickelhaupt, E. J. Baerends, C. F. Guerra, S. J. A. Van Gisbergen, J. G. Snijders, and T. Ziegler, J. Comput. Chem. 22, 931 (2001).
- ³⁸ V. Luaña, G. Fernández Rodrigo, E. Francisco, and L. Pueyo, J. Sol. St. Chem. **66**, 263 (1987).
- ³⁹ A. Juhin, G. Calas, D. Cabaret, L. Galoisy, and J. L. Hazemann, Phys. Rev. B **76**, 054105 (2007).
- ⁴⁰P. García-Fernández, C. Sousa, J. A. Aramburu, M. T. Barriuso, and M. Moreno, Phys. Rev. B 72, 155107 (2005).
- ⁴¹ J. M. García-Lastra, M. T. Barriuso, J. A. Aramburu, and M. Moreno, J. Phys.: Condens. Matter 22, 155502 (2010).
- ⁴²M. T. Barriuso, M. Moreno, and J. A. Aramburu, Phys. Rev. B 65, 064441 (2002).
- ⁴³ J. M. García-Lastra, T. Wesolowski, M. T. Barriuso, J. A. Aramburu, and M. Moreno, J. Phys.: Condens. Matter 18, 1519 (2006).