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Transmission properties of hollow-core photonic bandgap fibers in relation to molecular spectroscopy

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The transmission properties of five types of hollow-core photonic bandgap fibers (HC-PBFs) are characterized in the telecom wavelength range around $1.5\ \mu\text{m}$. The variations in optical transmission are measured as a function of laser frequency over a 2 GHz scan range as well as a function of time over several hours. The influence of these variations on spectroscopy of molecules in a HC-PBF is simulated. © 2010 Optical Society of America

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1. Introduction

Gas-filled hollow-core photonic bandgap fibers (HC-PBFs) can be used for efficient interaction between light and molecules or atoms over long optical path lengths. The tight confinement of light within the HC-PBFs allows for nonlinear interactions at power levels much lower than required in free space [1–3]. Long gas-filled HC-PBFs in connection with tunable or broadband light sources have been proposed as sensitive gas sensors [4–9]. The concentration of the gas of interest is derived from the measured area of an isolated absorption line. High sensitivity in a compact setup is possible with a long coiled HC-PBF. However, as the length of the HC-PBF is increased, the response time of the sensor increases as well. For gas entering the HC-PBF by diffusion from the fiber ends, the response time scales with the square of the fiber length [10]. Faster response is possible if small radial holes are laser drilled into the core along the fiber [11] or if the fiber is sectioned with small air gaps between each section [12]. Gas-filled HC-PBFs can also be used as temperature sen-

sors when the fibers are filled with low-pressure gas. The linewidths of isolated absorption lines are mainly due to the Doppler broadening and, hence, depend on the gas temperature [13,14].

These sensor applications require a well-defined spectroscopic baseline in order to accurately derive the integrated area or the linewidth of an isolated absorption line. The baseline is obtained from the optical transmission of the HC-PBF in the absence of an absorbing gas. Ideally, the baseline should be flat over a frequency range corresponding to a few times the linewidth of the relevant absorption line. Alternatively, if the application allows the fiber to be repeatedly filled and vented, it will be sufficient for the baseline to remain unchanged during the filling time. This will allow the actual baseline to be measured either before or after filling the fiber with gas. The limitation in the accuracy and sensitivity of gas sensors and temperature sensors based on gas-filled HC-PBFs due to variations in the spectroscopic baseline with frequency and time is investigated in this paper.

The optical transmissions of five types of HC-PBFs in the telecom wavelength range around $1.5\ \mu\text{m}$ are measured as a function of time and as a function of laser frequency over a scan range of about 2 GHz.

Polarization properties of the HC-PBFs are characterized. Simulated absorption profiles are added to these transmission data, which constitute our baselines, and the accuracy at which the integrated areas and linewidths can be recovered by least-squares fitting is determined. Similar measurements and analyses of a standard single-mode optical fiber are made for comparison.

2. Experimental Configuration

The experimental setup is shown in Fig. 1. A laser spectrometer developed for accurate measurements of the $^{13}\text{C}_2\text{H}_2$ $P(16)$ transition at 1542.3837 nm is used as the light source. The spectrometer is based on two Koheras E15 fiber lasers with a nominal output of 25 mW: a master laser and a slave laser. The master laser is locked to the acetylene $P(16)$ transition using wavelength modulated saturation spectroscopy in a setup similar to the setup of Balling *et al.* [15]. The Allan deviation describing the stability of the master laser is below 5 kHz for averaging times between 50 ms and several hours. The slave laser is offset locked to the master laser using a setup based on the ideas of Schünemann *et al.* [16]. The offset frequency is set by a Rohde & Schwartz SML01 signal generator, which is controlled by a personal computer (PC). The frequency of the slave laser is stepped with the signal generator across a 2 GHz frequency range with a dead time of about 50 ms per frequency step. At each step, the frequency is changed by 20 MHz and the actual differences between the master and the slave laser frequencies, as well as the power transmitted through the HC-PBF under test, are measured for about 50 ms. The difference between the master and the slave laser frequencies deviates less than 10 kHz from the set frequency. Inaccuracies in laser frequencies can be neglected in the following analyses.

The output of the slave laser passes through a fiber-coupled acousto-optic modulator (AOM) and is subsequently collimated in free space. The beam

passes an uncoated wedge acting as a beam splitter. The transmitted part goes to a photodetector (New Focus 2033), which is used to stabilize the optical power via feedback to the RF power driving the AOM. The beam reflected from the beam splitter is carefully mode matched to the HC-PBF under the assumption that core eccentricities are negligible. Two mirrors are used to adjust the beam path, and the HC-PBF is mounted on a three-dimensional translational stage. An aspheric lens with a focal length of 8 mm is placed in front of the HC-PBF for focusing into the fiber. For each fiber, an additional lens is placed in the beam path to improve the coupling efficiency. Various focal lengths and positions for the additional lens are tested while optimizing the position of the 8 mm lens in order to maximize the coupling efficiency. This additional lens is left out of the setup for those fibers where it does not improve the coupling efficiency.

The HC-PBF under test is coiled with a diameter of about 7 cm and carefully fixed to an aluminum plate. The ends of the fiber are open and exposed to the air in the laboratory. The output of the fiber is collimated and the optical power, which is typically between 50 and 100 μW , is detected by using an aspheric lens with a focal length of 4.5 mm and another New Focus 2033 photoreceiver. The voltage from the photoreceiver is measured with a HP 3457A voltmeter. The focusing lens, the HC-PBF, and the photo receiver are placed inside a foam enclosure to minimize turbulence, temperature fluctuations, and stray light. The temperature of the aluminum plate is monitored with a Pt-100 temperature sensor.

The windows in front of the photodiodes have been removed for both New Focus 2033 detectors in order to reduce interference effects. The relative out-of-loop power stability in the absence of the HC-PBF, but with every thing else in place (including lenses), has an Allan deviation below 10^{-5} for averaging times between 25 and 2000 s. The relative variations in the detected optical power over the 2 GHz frequency scan are below 0.03%.

Before each set of measurements, both ends of the HC-PBF are cleaved and the coupling into the fiber is optimized. Each set of measurements is started during the afternoon, and a PC controls the scanning of the laser frequency and collects data from the HP 3457A voltmeter, the temperature sensor, and the laser offset frequency from a HP 5381A counter. Each 2 GHz scan takes about 15 s. The measurement continues overnight and the data collected between 10 p.m. and 6:30 a.m., when the laboratory environment is most stable, are used.

Four sets of measurements are completed for each type of HC-PBF. The tested HC-PBF types are listed in Table 1 together with their specified and measured properties. All five HC-PBFs were manufactured by NKT Photonics and cut to a length of 3.0 m. The first three HC-PBFs are HC19-1550-01, HC1550-02, and HC1550-PM-01 [17]. HC-PBF 4 is similar to HC-PBF 3, but with an outer diameter

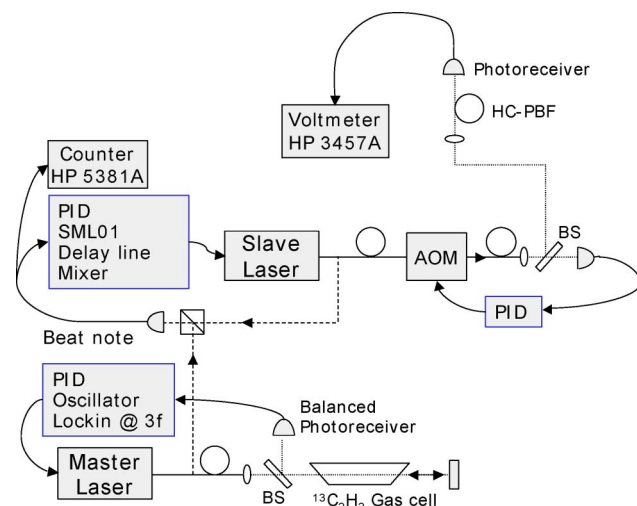


Fig. 1. (Color online) Experimental setup. PID, feedback controller; BS, beam splitter; AOM, acousto-optic modulator.

scaled down by approximately 2%, so that 1550 nm is located 30 nm closer to the long wavelength edge of the fiber's low loss region. HC-PBF 5 is similar to HC-PBF 2, but with a cladding air-filling fraction of 84%. The cladding pitch and core size were scaled accordingly to maintain the bandgap at 1550 nm.

The same measurements are performed for a 1 m long standard SMF-28 fiber with FC/APC connectors, which is used as a reference. The coupling efficiencies listed in Table 1 are determined as the measured transmission corrected for the bulk loss specified in Table 1. The bulk loss was determined at NKT Photonics using the cutback method. The coupling efficiency uncertainties are calculated as the standard deviation over the measurements from each realignment of the coupling into a given fiber.

3. Polarization Properties

Two of the five HC-PBFs in this study are manufactured as polarization-maintaining fibers. The polarization properties of these fibers are determined by measuring the four Stokes parameters of the HC-PBF output for different orientations of the linearly polarized input field. The Stokes parameters are given by

$$\begin{aligned} S_0 &= P_H + P_V, & S_1 &= P_H - P_V, \\ S_2 &= P_{+45} - P_{-45}, & S_3 &= P_{\sigma^+} - P_{\sigma^-}, \end{aligned}$$

where P_H , P_V , P_{+45} , P_{-45} , P_{σ^+} , and P_{σ^-} denote the power of the horizontally polarized light, the vertically polarized light, the light polarized +45 degrees to the horizontal plane, the light polarized -45 degrees to the horizontal plane, the right-hand circularly polarized light and the left-hand circularly polarized light, respectively. The degree of polarization is defined as [18]

$$V = \frac{\sqrt{S_1^2 + S_2^2 + S_3^2}}{S_0}.$$

The Stokes parameters are measured using the following procedure: a quarter-wave plate and a half-

wave plate are calibrated so that they each rotate a linearly polarized beam in such a way that an equal amount of the beam is transmitted through and reflected from a polarizer placed after the wave plate. A polarizer is placed at the output end of the fiber and the power of the transmitted and reflected beams are measured in the three cases: without any wave plate at the output end, with the calibrated quarter-wave plate placed between the fiber output end and the polarizer, and, third, with the calibrated quarter-wave plate replaced by the calibrated half-wave plate. These measurements are repeated for various orientations of the input beam polarization. The maximum and minimum degree of polarization for each of the two polarization-maintaining fibers and for fiber HC-PBF 5 are listed in Table 1. We find that HC-PBF 5 behaves as a polarization-maintaining fiber even though it was not intentionally manufactured as such. The minimum degree of polarization in Table 1 is well below 100%, which shows that the HC-PBF can transform perfectly polarized light into partially polarized light. This is possible if the HC-PBF output is a superposition of multiple free-space spatial modes having different polarizations.

The fibers HC-PBF 1 and HC-PBF 2 did not maintain a stable output polarization during the time needed to characterize the polarization properties.

4. Analysis of Transmission Data

The transmission of the fiber, i.e. the ratio between the output power of the fiber and the input power, is measured as the laser frequency is scanned across the 2 GHz range. The transmission measurements are subsequently normalized to the mean transmission for each scan. The variation in transmission listed in Table 1 is the difference between the maximum transmission and the minimum transmission for a single scan. This variation over the 2 GHz scan ranges from 0.30% to 3.59% for the HC-PBFs and 0.02% to 0.10% for the SMF-28. Figure 2(a) shows the normalized transmission with the smallest variation for each fiber, while Fig. 2(b) shows the normalized transmission with the largest variation. Figure 2 shows that the HC-PBFs have nonflat

Table 1. Specified Parameters (Rows 1–5) and Measured Parameters (Rows 6–9) for Each of the Tested Fibers^a

	HC-PBF 1	HC-PBF 2	HC-PBF 3	HC-PBF 4	HC-PBF 5	SMF-28
Polarization maintaining	N	N	Y	Y	N ^b	N
Specified loss (dB/km)	13	20	16	19	~100 ^c	0.7
Air-filling fraction of cladding (%)	91	91	91	91	84	—
Core size ^d	19 cell	7 cell	7 cell	7 cell	7 cell	—
Core diameter (μm)	20	11	13	13	8	8
Coupling efficiency (%)	86 ± 2	67 ± 1	73 ± 7	65 ± 8	74 ± 1	78 ± 7
Min variation (%)	0.30	0.52	0.63	0.72	0.42	0.02
Max variation (%)	1.13	1.89	2.49	3.59	0.60	0.10
Max/min degree of polarization (%)	—	—	99/82	100/84	98/83	—

^aFurther details of the parameters are given in the text.

^bThe 3 m of fiber used in these experiments behaved as a polarization-maintaining fiber, though it was not manufactured as such.

^cEstimated by NKT Photonics.

^dIn units of cladding cells.

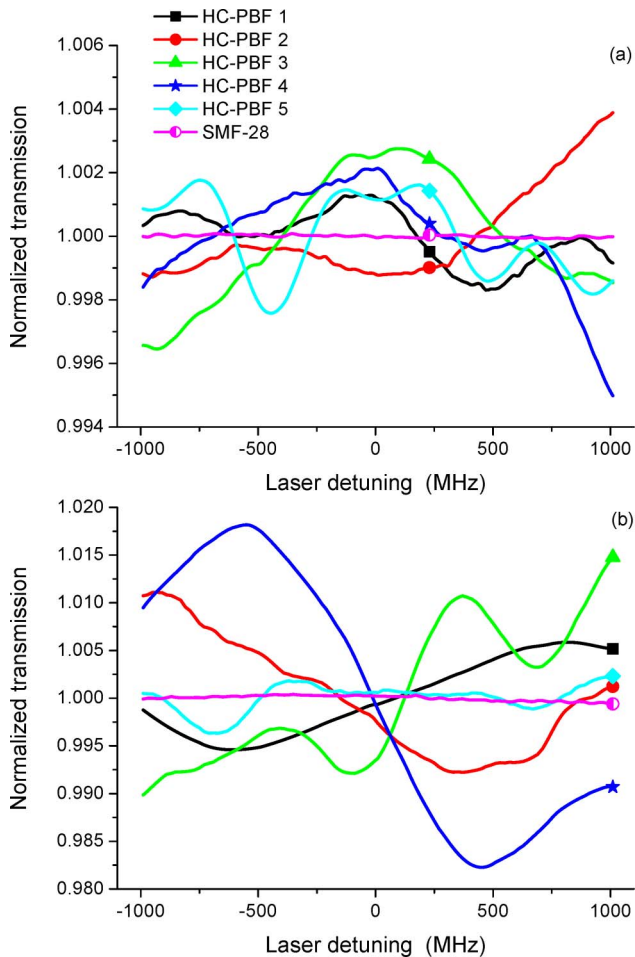


Fig. 2. (Color online) Normalized transmission through the fibers as the laser frequency is scanned over 2 GHz (a) for the measurements with the smallest variation for each fiber type and (b) for the measurements with the largest variation. Note that the scalings of the vertical axes are not identical.

transmission spectra and that the spectra change over time. This change is not only due to different in-coupling conditions, but it has also been observed to occur over time within each set of measurements. A comparison between the coupling efficiencies and the transmission variations listed in Table 1 shows that the HC-PBFs with the largest variation in transmission are the ones with the lowest coupling efficiencies. Lower coupling efficiency could imply a higher degree of coupling to surface modes or higher-order core modes. HC-PBF 1 has the largest core size and would, therefore, be expected to support a larger number of higher-order modes, which, in turn, could lead to a higher variation in transmission. However, a larger core is also expected to reduce the number of surface modes [19]. Interference between coupled core modes and surface modes is known to give significant baseline variations in the output from HC-PBFs [12].

Averaging over time can reduce the variance of the transmission and, thus, increase the sensitivity of a sensor based on a gas-filled HC-PBF. The Allan var-

iance method was introduced to analyze the stability over time for frequency standards [20,21], but the method has also been used to characterize gas sensors based on laser spectroscopy [22,23]. The Allan variance of the transmission at a certain laser frequency is the average of the squared differences between successive values of the transmission measured with a specified averaging time. For a set of successive transmission measurements comprising N data points ($T_i, i = 1, \dots, N$) at a certain laser frequency, the Allan variance corresponding to the averaging time τ is given by

$$\langle \sigma_A^2(s) \rangle_\tau = \frac{1}{2(m-1)} \sum_{k=1}^{m-1} [A_{k+1}(s) - A_k(s)]^2,$$

where

$$A_k(s) = \frac{1}{s} \sum_{i=1+s(k-1)}^{sk} T_i, \quad k = 1, \dots, m.$$

m is the largest integer less than or equal to N/s , and s is the number of data points sampled during the time τ . The Allan deviation, which is the square root of the Allan variance, is for a given set of measurements calculated for each laser frequency using all data from 10 p.m. to 6:30 a.m. The normalized transmission Allan deviation is calculated as the average over the Allan deviations for each laser frequency in the 2 GHz scan range. A normalized transmission Allan deviation is obtained from each set of measurements, and we obtain four normalized transmission Allan deviation graphs for each type of fiber. Figure 3 shows the normalized transmission Allan deviations with the smallest minimum value for each type of fiber. The optimum averaging time for the five HC-PBFs is between 100 and 200 s, while the optimum averaging time for the SMF-28 is above 2000 s. The minimum normalized transmission Allan deviation for the HC-PBFs lies between 2×10^{-5} and 6×10^{-5} . The various normalized transmission Allan

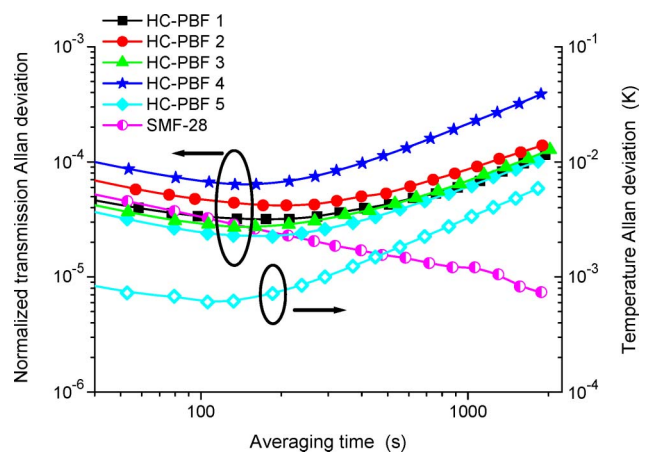


Fig. 3. (Color online) Normalized transmission Allan deviation with the smallest minimum for each fiber. The open diamond symbols represent the temperature Allan deviation corresponding to the plotted HC-PBF 5 transmission data.

deviations obtained for each fiber show some variations, but they all follow the same general trend for a given type of fiber. The Allan deviation for the temperature measurements corresponding to the normalized transmission Allan deviation is plotted for HC-PBF 5 in Fig. 3. This temperature Allan deviation has a shape similar to the normalized transmission Allan deviations for the hollow-core fibers. In particular, they all have a minimum between 100 and 200 s. This indicates that the temporal variations in the hollow-core fiber transmissions are coupled to temperature variations, which was also observed in [12]. The interference between different modes in a fiber depends on the temperature [24]. This could explain why the transmission Allan deviation for the SMF-28 differs from the hollow-core fibers. Since the SMF-28 supports only the fundamental mode, there are no higher-order modes or surface modes to exhibit temperature-dependent interference.

5. Simulated Absorption Spectra

The measured transmission spectra at 10 p.m., 12 a.m., 2 a.m., 4 a.m., and 6 a.m. from each set of measurements are multiplied by the mathematical expression for the optical transmission near an isolated Doppler broadened molecular absorption line given by

$$T(\Delta) = \exp\left(-\frac{\alpha}{\sqrt{\pi}\delta\nu_D} e^{-\Delta^2/\delta\nu_D^2}\right),$$

where Δ is the laser detuning, α is the area of the absorption line, which is set to $0.5 \cdot \pi^{1/2} \delta\nu_D$, and $\delta\nu_D$ is the $1/e$ Doppler width, which is set to 260 MHz for a typical light molecule at room temperature with absorption lines in the wavelength range around 1550 nm.

For each modeled spectrum, the linewidth and the area of the absorption line are retrieved using a least-squares fitting routine. The relative differences between the model area ($0.5 \cdot \pi^{1/2} \delta\nu_D$) and the retrieved areas are plotted in Fig. 4(a). The numbers listed below the measurement data in Fig. 4 are the standard deviation calculated over the 20 data points for the corresponding fiber.

In a modified analysis, the modeled spectra are normalized with the fiber transmission measured 30 min later. This corresponds to the situation where the fiber is evacuated in 30 min and a subsequent measurement of the transmission is used as the baseline. The 30 min are chosen as a typical time needed for filling or venting a 3 m long HC-PBF [10]. Figure 4(b) shows the relative differences between the model area and the retrieved areas in this case. The relative differences are clearly reduced by this normalization.

The relative errors in the retrieved linewidths follow, in general, the same trend as the relative error in the retrieved areas. The largest standard deviation for the relative linewidth errors is obtained

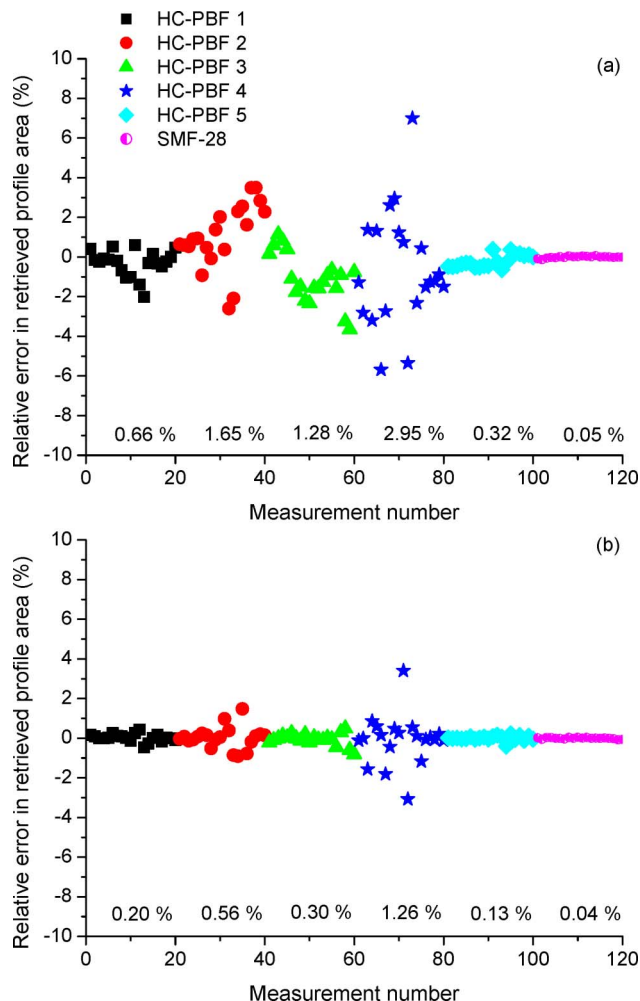


Fig. 4. (Color online) (a) Relative errors in the retrieved absorption line area for each of the tested fibers when modeled with a Gaussian profile. The numbers listed below the measurement data are the standard deviations calculated over the 20 data points for the corresponding fiber. (b) Similar to (a), but with each modeled spectrum normalized to the measured fiber transmission 30 min later.

for HC-PBF 4 (1.6%), whereas HC-PBF 5 gives the smallest standard deviation for the relative linewidth errors (0.28%). These standard deviations can be reduced by about a factor of 2 if the modeled spectra are normalized to the transmission measured 30 min later. The relative errors in the retrieved linewidths will induce a 2 times larger relative error in the temperature reading of a thermometer based on molecular spectroscopy in a HC-PBF since the linewidth scales with the square root of the temperature. For the best fiber at room temperature, these data correspond to a typical uncertainty of 2 K in a configuration without cycling of the gas pressure.

If the Gaussian line shape is replaced with a Lorentzian line shape of the same FWHM linewidth, which is representative for the collisional broadening regime, the standard deviation of the relative errors in area and linewidth increases with a factor of about 2.

6. Conclusions

The transmission properties of five different HC-PBFs have been characterized as a function of laser frequency over a scan range of 2 GHz and as a function of time over several hours. The influence of the variations in transmission on the potential accuracy of sensors based on gas-filled HC-PBFs has been determined. For short measurement times, where the baseline does not change (i.e., a few minutes or shorter), the baseline variations contribute to the overall gas sensor uncertainty by 0.3% to 3.0%, depending on the actual HC-PBF. This can be improved by a factor of 2 to 4 if the gas pressure is cycled and the baseline is measured with the empty fiber. The typical uncertainty for a thermometer based on molecular spectroscopy in a HC-PBF is found to be about 2 K at room temperature.

The temporal variation of the HC-PBF transmission is found to be correlated to the variation in temperature. The temperature Allan deviation for 30 min of averaging time is about 5 mK. Reduction in temperature variation by active stabilization is expected to improve the temporal variation of the transmission. Alternatively, mechanical vibration of the HC-PBF, as well as rapid variations in HC-PBF temperature, can be used to average out the transmission variations [12].

The fiber HC-PBF 5, which is expected to have the largest suppression of higher-order modes, has the smallest variations in optical transmission over the 2 GHz scan range, as well as over time.

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