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If you believe that this document breaches copyright please contact us providing details, and we will remove access to the work immediately and investigate your claim. ON THE ELECTRODYNAMICS OF PARTIAL DISCHARGES IN VOIDS IN SOLID DIELECTRICS

A. Pedersen

INTRODUCTION

Partial discharges in voids in a solid dielectric are often discussed in terms of a simple equivalent capacitive circuit known as the *abc*-model. The void is represented by a capacitance and discharges are simulated as discharges of this capacitance, see Whitehead [1]. An equivalent circuit is a system which can generate as faithfully as possible the signals which are manifest at the terminals of the actual system, and in this respect the *abc*-model has been quite successful. It is, however, important to realize that the processes within an equivalent circuit need not in any way be identical to the processes which are involved in the real system. This is evident for the *abc*-model since this model describes a phenomenon, which is inherently a field problem, in terms of lumped circuit parameters.

To envisage a void as a capacitor requires a very loose interpretation of the concept of capacitance. This concept is intimately related to conducting electrodes between which a space-charge free electrostatic field can be established. This means that the field must be Laplacian. Strict proportionality will consequently exist between the charge Q on the electrode and the applied voltage U, i.e.

 $Q = CU , \qquad (1)$

where C is the capacitance. A meaningful application of equation (1) to the field within a void is hardly possible since the field is a Poisson-field when space-charges are present, and this implies that Q will not be proportional to U.

The transients which are manifest at the electrodes of a system during partialdischarge activity are related to the charges which, in view of Faraday's icepail experiment, are induced on the electrodes. The primary sources for these induced-charges are the charges which, as a result of the partial-discharge activity, are distributed within the voids.

The induced-charge can be expressed as the difference between the charge on the electrode when discharges have occurred and the charge which would have been on the electrode had the system remained discharge free, Repp et al. [2]. The direct implementation of this approach can be rather cumbersome as it requires the solution of Poisson's equation. A more straightforward approach is possible through an application of the principle of super- position. This can be done in two different ways depending on whether the analysis is based on the *D*-field, Pedersen [3], Crichton et al. [4], or on the *P*-field, Pedersen [5]. The former, the Maxwellian description, is more convenient for practical applications, whereas the latter, the quasi-molecular description, is suitable for fundamental studies of the physics of the phenomenon.

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THE CONCEPT OF INDUCED CHARGES

Maxwellian Description

The charge Q_1 on the i'th electrode in a space-charge free system consisting of N electrodes is given by

$$Q_{i} = \sum_{j=1}^{N} C_{ij} (U_{i} - U_{j})$$
(2)

with

$$\sum_{i=1}^{N} Q_i = 0. \tag{3}$$

 $U_{\rm i}$ and $U_{\rm j}$ are the potentials of the i'th and the j'th electrodes, and $C_{\rm i\,j}$ is the partial capacitance between these electrodes. If space-charges are present in the space between the electrodes an additional charge $q_{\rm i}$, the induced charge, will appear on the i'th electrode, i.e.

$$Q_{i} = q_{i} + \sum_{j=1}^{N} C_{ij} (U_{i} - U_{j}).$$
 (4)

The induced-charge depends in a unique way on the locations and magnitudes of the space-charges. They are independent of the electrode potentials if the permittivities do not depend on the electric field. An infinitesimal charge dQ located somewhere between the electrodes will induce a charge dq_i on the i'th electrode and dq_i will, in view of the principle of superposition, be proportional to dQ, i.e.

$$dq_i = -\lambda_i dQ . \tag{5}$$

The parameter λ_i is a dimensionless positive scalar function which depends on the location of dQ only. The entire induced-charge on the i'th electrode from a distribution of space charges can thus be expressed in the form

$$q_{i} = -\iint \lambda_{i} \rho d\Omega - \iint \lambda_{i} \sigma dS , \qquad (6)$$

in which ρ is the volume-charge density in the volume element $d\Omega$ and σ is the surface-charge density on the surface element dS of an interface between two dielectrics. The volume integral is extended over all space and the surface integral over all dielectric interfaces. In a study of partial discharges in voids in solid dielectrics the space-charges will be located within the voids and on the walls of these voids.

The response function λ_1 can, as shown by Maxwell [6], be found by applying Green's reciprocal theorem to the system in the following way. The total charge on the i'th electrode will be q_1 if all electrodes are at zero potential, see equation (4), and space-charges are deposited in the space between the electrodes. We compare this with the situation when $\rho = 0$ and $\sigma = 0$ everywhere, the potential of the i'th electrode is U_1 and all other electrodes are at zero potential. Applying Green's reciprocal theorem, Clemmow [7], to these two situations yields

$$U_{i}q_{i} + \iiint V_{i}\rho d\Omega + \iint V_{i}\sigma dS = 0 .$$
⁽⁷⁾

$$q_{\mathbf{i}} = - \iint (V_{\mathbf{i}}/U_{\mathbf{i}})\rho d\Omega - \iint (V_{\mathbf{i}}/U_{\mathbf{i}})\sigma dS .$$
(8)

 V_i denotes the scalar potentials at d Ω and dS when the i'th electrode is at the potential U_{i} , all other electrodes are at zero potential and the system is space-chare free. Comparing (6) and (8) shows that

$$\lambda_{i} = V_{i}/U_{i} \quad . \tag{9}$$

Since V_i is the solution to Laplace's equation

$$\operatorname{div}(\epsilon \operatorname{grad} V_{i}) = 0 \tag{10}$$

 λ_i can be determined from

$$\operatorname{div}(\epsilon \operatorname{grad} \lambda_i) = 0 \tag{11}$$

in which ϵ denotes the permittivity. The boundary conditions are $\lambda_1 = 1$ at the surface of the i'th electrode and $\lambda_1 = 0$ at the surfaces of all the other electrodes. In addition, the following condition must be fulfilled at all dielectric interfaces such as the walls of the voids, viz.

$$\epsilon_{+}(\partial\lambda_{i}/\partial n)_{+} = \epsilon_{-}(\partial\lambda_{i}/\partial n)_{-}$$
(12)

where λ_i is differentiated in the direction normal to the interface and the signs + and - refer to the two sides of the interface. Since equation (11) is Laplace's equation any standard method for the calculation of space- charge free electrostatic fields can be used to evaluate λ_i .

Quasi-Molecular Description

The polarization P in the dielectrics is a significant property when discussing the induced charge in a system which contains polarizable materials. The importance of the polarization is, however, not evident from the analysis given above since the effect of the polarization is automatically included in the λ function. This is an advantage when the analysis is applied to practical systems whereas it may be less suitable in studies of the physics of the phenomenon.

The effect of the polarization P can be taken into account by adopting a quasimolecular description [5]. This means that the entire space between the electrodes is viewed as vacuum in which the dielectric is represented by a distribution of dipoles with a dipole moment density equal to P. The induced-charge on an electrode is then considered to consist of two parts. One which is linked with the space-charge distribution created by partial discharge activities, and another part which is related to the dipoles, that is to the polarization P.

The induced charge related to a dipole can be found by visualizing a dipole as two charges Q and -Q separated by an infinitesimal distance dr. The dipole moment thus becomes

$$d\vec{\mu} = Qd\vec{r} . \tag{13}$$

Let φ denote the λ -function for vacuum, then

$$\varphi_{i}(\vec{r} + d\vec{r}) = \varphi(\vec{r}) + d\vec{r} \cdot \operatorname{grad} \varphi_{i} , \qquad (14)$$

where \vec{r} is the radius-vector indicating the position of the dipole. The induced-charge on the i'th electrode thus becomes

$$dq_i = -d\mu \cdot \operatorname{grad} \varphi_i . \tag{15}$$

The response function for vacuum $\varphi_{\underline{i}}$ is given by Laplace's equation for vacuum, i.e.

$$\operatorname{div}\operatorname{grad}\varphi_{\mathbf{i}}=0\tag{16}$$

or

$$\nabla^2 \varphi_{\mathbf{i}} = 0 \quad . \tag{17}$$

The boundary conditions are $\varphi_i = 1$ at the surface of the i'th electrode and $\varphi_i = 0$ at all other electrodes. No condition is imposed on φ_i at the dielectric interfaces. Any available method of electrostatic field calculation in vacuum can thus be applied to obtain φ_i from the equations

$$\nabla^2 V_{\rm vi} = 0 \tag{18}$$

and

$$\varphi_{\mathbf{i}} = V_{\mathbf{v}\mathbf{i}}/U_{\mathbf{i}} \quad . \tag{19}$$

 V_{vi} is the scalar potential in a point of the space-charge free electrostatic field *in vacuum* where the potential of the i'th electrode is U_i and all other electrodes are at zero potential.

The polarization P in a point of the solid dielectric will depend on the applied voltages and on the space-charges formed by partial discharges, i.e.

$$\vec{P} = \vec{P}_a + \vec{P}_s , \qquad (20)$$

where $P_{\rm g}$ is linked with the applied voltages and $P_{\rm g}$ is related solely to the inter-electrode space-charges. The resulting induced-charge on the i'th electrode as a result of partial discharge activities will thus be given by

$$q_{i} = - \iiint [\varphi_{i}\rho + P_{s} \cdot \operatorname{grad} \varphi_{i}] d\Omega - \iint \varphi_{i}\sigma dS .$$
(21)

The volume integral is extended over the entire space between the electrodes and the surface integral over all dielectric interfaces, that is the walls of the voids.

CURRENT PULSES IN THE LEADS

During the periods of time in which partial discharges are developing transient currents can flow in the leads to the electrodes and voltage transients can be observed. In addition a transfer of charge may occur from an electrode to the space between the electrodes. This is likely to appear if a void is located at an interface between an electrode and the solid dielectric.

Let I_{i} denote the total current flowing in the lead towards the i'th electrode and let I_{ti} be the current which represents the transfer of charge from the i'th electrode towards the inter-electrode space. These currents are, in view of the principle of the conservation of charges, related to the total net charge Q_{i} on the i'th electrode in the following way

$$I_{i} = I_{ti} + dQ_{i}/dt$$
 (22)

or

$$I_{i} = I_{ti} + \frac{dq_{i}}{dt} + \sum_{j=1}^{N} c_{ij} \left[\frac{dU_{i}}{dt} - \frac{dU_{i}}{dt} \right].$$
(23)

Differentiating equation (6) with respect to the time t yields

$$\frac{dq_1}{dt} = -\iiint \lambda_1 \frac{\partial \rho}{\partial t} d\Omega - \iint \lambda_1 \frac{\partial \sigma}{\partial t} dS$$
(24)

which by means of the continuity equations

div
$$\vec{J} + \frac{\partial \rho}{\partial t} = 0$$
 and Div $\vec{J} + \frac{\partial \sigma}{\partial t} = 0$ (25)

can be written in the form

.

$$\frac{dq_i}{dt} = \iiint \lambda_i \, \operatorname{div} \, \vec{J} \, \mathrm{d\Omega} + \iint \lambda_i \, \operatorname{Div} \, \vec{J} \, \mathrm{dS} \, . \tag{26}$$

 \vec{J} is the current density in a point within a void during discharge activities. Div \vec{J} is the interface divergence defined in the following way, Fischer [8],

Div
$$\vec{J} = \vec{n} \cdot (\vec{J}_{+} - \vec{J}_{-})$$
 (27)

where the signs + and - refer to the two sides of the interface, and \vec{n} is a unit vector normal to the interface and directed away from the positive side. It is in this analysis assumed that the effect of the surface conductivity of the interfaces, i.e. the walls of voids, can be neglected. Introducing the identities

$$div(\lambda_{1}\vec{J}) = \lambda_{1}div \vec{J} + \vec{J} \cdot grad\lambda_{1}$$
(28)

and

$$\lambda_{i} \text{Div} \vec{J} = \text{Div}(\lambda_{i} \vec{J})$$
(29)

then leads to

$$\frac{dq_i}{dt} = \iiint div(\lambda_i J) d\Omega + \iint Div(\lambda_i J) dS - \iiint J \cdot grad\lambda_i d\Omega .$$
(30)

Applying the extended divergence theorem of Gauss, Joos [9], to the vector field $\lambda_1 J$ reveals that

$$I_{ti} + \iiint \operatorname{div}(\lambda_{i}\vec{J})\mathrm{d}\Omega + \iint \operatorname{Div}(\lambda_{i}\vec{J})\mathrm{d}S = 0 .$$
(31)

This means that

$$\frac{dq_i}{dt} = -I_{ti} - \iiint \tilde{J} \cdot \operatorname{grad}_{\lambda_i d\Omega} .$$
(32)

Inserting this in equation (23) shows that the total current flowing in the lead towards i'th electrode is given by

$$I_{i} = -\iiint \vec{J} \cdot \operatorname{grad}_{i} d\Omega + \sum_{j=1}^{N} C_{ij} \left[\frac{dU_{i}}{dt} - \frac{dU_{j}}{dt} \right] .$$
(33)

Since the λ_1 -function is determined by Laplace's equation, see equation (11), the gradient of λ_1 can be found from

$$\operatorname{grad}_{\lambda_{i}} = -\vec{E}_{i}/U_{i} , \qquad (34)$$

in which \vec{E}_i is the field strength in the space-charge free electrostatic field between the electrodes of the system if the potential of the i'th electrode is U_i and all other electrodes are at zero potential. It should be emphasized that U_i and E_i are entirely fictitious quantities since U_i can be given any arbitrarily chosen value in the computational procedure, i.e. U_i is not synonymous with the potential of the i'th electrode during discharge activities. For this reason E_i and U_i should not be inserted in the expression for the current.

Should it be desirable to include the polarization in the analysis a similar procedure can be applied to equation (21). This leads to the following expression for the total current in the lead to the i'th electrode.

$$I_{i} = - \iiint \left\{ \left[\vec{J} + \frac{\partial \vec{P}_{g}}{\partial t} \right] \cdot \operatorname{grad}_{\varphi_{i}} \right\} d\Omega + \sum_{j=1}^{N} C_{ij} \left[\frac{dU_{j}}{dt} - \frac{dU_{j}}{dt} \right] .$$
(35)

The gradient of φ_i can be calculated from

+

$$\operatorname{grad} \varphi_{\mathbf{i}} = - \dot{E}_{\mathbf{v}\mathbf{i}} / U_{\mathbf{i}}$$
, (36)

where $E_{\rm vi}$ is the field strength in the electrostatic field associated with $U_{\rm i}$ when the entire space between the electrodes is vacuum and all other electrodes are at zero potential.

The current density J is related to the motion of electrons and ions within the voids during discharge activities, viz.

$$\vec{J} = \sum_{k=0}^{m} \rho_k \vec{u}_k$$
(37)

where ρ is the charge density and \vec{u} the drift velocity, k=0 refers to electrons and m is the number of possible species of positive and negative ions which are participating in the discharge activity.

A direct application of equations (21) and (35) to practical systems would be rather complicated because of the explicit occurrence of the polarization in these equations. A closer analysis, see Pedersen [5], shows that the polarization does play an important role, and that this effect becomes more dominant the more oblate the void is with respect to the direction of the

applied electric field.

Formulae similar to those derived above, but for systems in which polarizable materials are absent, have been given by many authors, see for example von Engel and Steenbeck [10], Ramo [11], Shockley [12]. These formulae are sometimes referred to as the Ramo-Shockley theorem. It should be remembered, however, that a quantitative treatment based on Faraday's concept of induced charges dates back at least to Maxwell [6].

Although the analysis given above is discussed with special reference to partial discharges in voids, the sets of formulae are of general validity for similar systems in which currents in the external leads depend on charges in motion in the space between the electrodes.

APPLICATION TO PARTIAL DISCHARGES

A discharge in a void results in a deployment of charges on the surface S of the void. The surface-charge density σ will attain such values that the electric field within the void will reduce until the discharge is quenched. Since the detection of partial discharges often refers to signals which are manifest at the terminal electrode we can leave out the subscripts in the following discussion. The resulting induced-charge q on this terminal electrode is, in view of equation (6), given by

$$q = -\iint_{S} \lambda \sigma dS . \tag{38}$$

The dimensions of the void are normally small relative to the distance to the electrode, and the nett charge contained within the void will remain zero. This means that the charges which are deposited on the wall S of the void can be considered, to a first approximation, as an electric dipole configuration with the dipole moment

$$\vec{\mu} = \iint_{S} \vec{r} \sigma dS \tag{39}$$

where \vec{r} is a radius vector which locates the position of the surface element dS. The induced-charge which arises from this dipole is given by, see equation (15),

 $q = -\vec{\mu} \cdot \operatorname{grad} \lambda \quad (40)$

In general the gradient of λ can be determined only in such cases where the location and the geometrical form of the void are known. This difficulty can to some extent be circumvented by replacing λ with the value which the λ - function would attain if we assume that the entire insulating system is completely free from any voids. Let λ_0 denote this idealized function. The gradients of λ and λ_0 are connected by

$$\operatorname{grad}\lambda = h \operatorname{grad}\lambda_0$$
 (41)

If the application is restricted to simple geometries, such as spheroids, we can consider the parameter h to be a scalar. Based on the mathematical analogies between the λ -function and the electrostatic field it is easily seen that

$$1 < h < \epsilon_r$$
 (42)

where ϵ_r is the relative permittivity of the ambient dielectric. The lower limit applies to voids which are very prolate with respect to the direction of the applied electric field. The upper limit is approached for a very oblate void. Introducing λ_0 leads to the following expression for the induced charge

 $q = -\dot{h\mu} \cdot \operatorname{grad}_{\lambda_0} . \tag{43}$

An assessment of the dipole moment requires a knowledge of the shape and location of the void. The nature of the gas within the void must also be known. A quantitative analysis related to ellipsoidal voids has been given by Crichton et al. [4].

All the required data will not be available in connection with partial discharge testing of commercial high voltage equipment. The dipole moment and the parameter h will, however, remain constant if we consider discharges in a number of voids of fixed volume and form containing the same gas, but placed at different locations within the insulating system. The induced-charge will in such cases vary with the location of the void in the same way as the gradient of λ_0 or, in view of the analogy with the electrostatic field, as indicated by the variation of the electric field strength for the idealized void-free system.

TRANSIENTS RELATED TO INDUCED-CHARGES

Although the observable transients are inherently related to the inducedcharges, the properties which primarily are measured are transients in the applied-voltage and current-pulses in the lead to the terminal electrode. The relationship between these properties and the induced-charge can be found in the following manner. Just prior to the first discharge the potential of the electrode is U and the associated charge on the electrode is Q. We compare this with the situation immediately after the discharge is quenched. The potential has now dropped to $U - \Delta U$ and the charge on the electrode has become $Q + \Delta Q$, where ΔQ is the charge transferred to the electrode from the external source. Green's reciprocal theorem then yields

$$(U - \Delta U)Q = U(Q + \Delta Q) + \iint V \sigma dS, \qquad (44)$$

where V is the scalar potential at the surface element dS for the dischargefree situation. Since $V = \lambda U$ in consequence of equations (11) and (12), and Q = CU, where C is the capacitance of the system, we obtain

$$-\iint\limits_{S} \lambda \sigma dS = C\Delta U + \Delta Q \tag{45}$$

or

$$q = C \Delta U + \Delta Q . \tag{46}$$

If the impedance of the circuit is large for the current which is associated with the discharge, then $C\Delta U$ can be much larger then ΔQ . The induced-charge is then given by approximately

 $q = C \Delta U$. (47)

It should be emphasized that the capacitance of the system is not affected by

DISCHARGE PHENOMENA IN VOIDS FILLED WITH FIBROUS MATERIALS

P.H.F. Morshuis, F.H. Kreuger

ABSTRACT

Untill now paper 3-phase belt type cables were succesfully used for voltages upto 20 kV in great parts of the world. Replacement of paper by extruded insulation has been unsuccesfull and service voltages no higher than 5 kV can be applied because of the large discharges and uncontrolled field in the interstices at the core and the belt. Belt-type cables remained paper-insulated for that reason.

A breakthrough has been obtained when a non-woven fibrous tape was applied to the cores to improve the longitudinal water tightness. As these tapes are very poor dielectrics, with low breakdown stress, it was expected that the breakdown tests would be impaired. At the contrary, the life expectancy was raised from less than 10 years to more than 30 years at 10 kV. Further study revealed that this dielectric improvement was caused by a considerable reduction of the discharges in the interstices of the cable; reductions of several hundred times were measured.

INTRODUCTION

To obtain a waterstop in the longitudinal direction of a 3-phase belted cable, a thin non-woven tape was applied to the core insulation and to the interstices between the belt insulation and the core insulation (Figure 1), Kreuger, Morshuis et al. [1]. The discharge diagram of this cable and a non-taped cable are shown in Figure 2. The research on the discharge mechanism of voids filled with a nonwoven, fibrous tape was initiated by the discharge limiting effect of the tape in the cable and by the fact that the cable life was significantly increased.

To study the discharge mechanism of these taped cables a model was built that represented the interstices in the cable.

EXPERIMENTAL METHOD

The testcircuit for measuring partial discharges consists of a 50 Hz high voltage source that can deliver a programmable number of half or whole 50 Hz periods. This set-up makes it possible to study subsequent discharges or Lichtenberg figures during specific time intervals. A balanced discharge detection system is used (Figure 3) combined with a storage facility. Lichtenberg figures can be

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not prohibit a sound qualitative assessment of the insulation to be made on the basis of such measurements.

CONCLUSION

A correct interpretation of partial-discharge transients can be attained only through the concept of induced-charge. The application of this concept has enabled a partial-discharge theory to be developed through which the influence of relevant void parameters can be assessed in a correct way. In contrast, the widely adopted *abc*-capacitance model does not allow this insight to be achieved. In addition, the *abc*-model is based on an erroneous application of the concept of capacitance, and, although this simple approach can be a useful tool when discussing measuring techniques, it may lead to quite incorrect conclusions.

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