# P systems–based Modelling of Cellular Signalling Pathways

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Abstract. Cellular signalling pathways are fundamental to the control and regulation of cell behaviour. Understanding the biosignalling network functions are crucial for studying different diseases and for designing effective therapeutic approaches to them. In this paper we present P systems as a feasible computational modelling tool for cellular signalling pathways that takes into consideration the inherent randomness occurring in biological phenomena and the discrete character of the components of the system. We illustrate these cellular models simulating the EGFR signalling cascade and the FAS-induced apoptosis using a deterministic strategy for evolution of P systems.

# 1 Introduction

The complexity of biomolecular cell systems is currently the focus of intensive experimental research, nevertheless the enormous amount of data about the function, activity, and interactions of such systems makes necessary the development of models able to provide a better understanding of the dynamics and properties of the systems.

A model is an abstraction of the real-world onto a mathematical/computational domain that highlights some key features while ignoring others that are assumed to be not relevant. A good model should have four properties: relevance, computability, understandability and extensibility. A model must be relevant capturing the essential properties of the phenomenon investigated; and computable so it can allow the simulation of its dynamic behaviour, as well as the qualitative and quantitative reasoning about its properties. An understandable model will correspond well to the informal concepts and ideas of molecular biology. Finally, a good model should be extensible to higher levels of organisations, like tissues, organs, organism, etc, in which molecular systems play a key role.

P systems are an unconventional model of computation inspired by the structure and the functioning of living cells which takes into consideration the discrete character of the quantity of components of the system by using rewriting rules on multisets of objects, that represent chemical substances, and strings, that represent the organisation of genes on the genome. The inherently randomness in biological phenomena is captured by using stochastic strategies . We believe that P systems satisfy the above properties required to a good model.

Cellular signalling pathways are fundamental to the control and regulation of cell behaviour. Understanding the biosignalling network functions are crucial for studying different diseases and for designing effective therapeutic approaches to them. The characterization of properties about whole–cell functions requires mathematical/computational models that quantitatively describe the relationship between different cellular components.

Ordinary differential equations (ODEs) have been successfully used to model kinetics of conventional *macroscopic* chemical reactions. That is, the approach followed by ODEs is referred as macroscopic chemistry since they model the average evolution of the concentration of chemical substances across the whole system. In this approach each chemical concentration with time is described, implicitely assuming that the fluctuation around the average value of concentration is small relative to the concentration. This assumption of homogeneity may be reasonable in some circumstances but not in many cases due to internal structure and low numbers and non–uniform distributions of certain key molecules in the cell. While differential equations models may produce useful results under certain conditions, they provide a rather incomplete view of what is actually happening in the cell [1].

Due to the complexity of cellular signalling pathways, large number of linked ODEs are often necessary for a reaction kinetics model and the many interdependent differential equations can be very sensitive to their initial conditions and constants. Time delays and spatial effects (that play a important role on pathway behaviour) are difficult to include in a ODE model [8] in which are also very difficult to change and extend, because changes of network topology may require substantial changes in most of the basic equations [2].

Recently, different agent-based approaches are being used to model a wide variety of biological systems ([9], [10], [20]) and biological processes, including biochemical pathways [8].

The *microscopic* approach considers the molecular dynamics for each single molecule involved in the system taking into account their positions, momenta of atoms, etc. This approach is computationally intractable because of the number of atoms involved, the time scale and the uncertainty of initial conditions.

Our approach is referred as *mesoscopic* chemistry [19]. Like in the microscopic approach one considers individual molecules like proteins, DNA and mRNA, but ignores many molecules such as water and non-regulated parts of the cellular machinery. Besides the position and momenta of the molecules are not modelled, instead one deals with the statistics of which reactions occur and how often. This approach is more tractable than microscopic chemistry but it provides a finer and better understanding than the macroscopic chemistry.

This paper is organised as follows. In the next section we present a deterministic strategy for the evolution of P systems. In Section 3 and 4 a study of EGFR signalling cascade and of FAS-induced apoptotic signalling pathway are given. Finally, conclusions are presented in the last section.

# 2 P Systems to simulate biosignalling cascades

In this paper we work with variant of P systems being tuples

$$\Pi = (O, L, \mu, M_1, M_2, \dots, M_n, R_1, \dots, R_n) ,$$

where:

- O is a finite alphabet of symbols representing objects (proteins and complexes of proteins);
- -L is a finite alphabet of symbols representing labels for the compartments;
- $-\mu$  is a membrane structure containing  $n \ge 1$  membranes labelled with elements from L;
- $-M_i = (w_i, l_i), 1 \le i \le n$ , are pairs which represent the initial configuration of membrane *i* with  $l_i \in L$  and  $w_i \in O^*$ ;
- $-R_i, 1 \leq i \leq n$ , are finite sets of rules associated with the membrane *i* which are of the form  $u[v]_{l_i} \rightarrow u'[v']_{l_i}$ , where  $u, v, u', v' \in O^*$  are finite multisets of objects and  $l_i$  is the label of membrane *i*.

Next, we discuss in more detail the rules that we will use in this paper.

(a) Transformation, complex formation and dissociation rules:

$$\left[\begin{array}{c} [a]_{l} \rightarrow [b]_{l} \\ [a, b]_{l} \rightarrow [c]_{l} \\ [a]_{l} \rightarrow [b, c]_{l} \end{array}\right\} \quad \text{where } a, b, c \in O, \text{ and } l \in L$$

These rules are used to specify chemical reactions taking place inside a membrane labelled by  $l \in L$ .

(b) Diffusing in and out:

$$\left[ \begin{array}{c} a \end{array} \right]_{l} \to a \left[ \begin{array}{c} \end{array} \right]_{l} \\ a \left[ \begin{array}{c} \end{array} \right]_{l} \to \left[ \begin{array}{c} a \end{array} \right]_{l} \end{array} \right\} \quad \text{where } a \in O, \text{ and } l \in L$$

We use these types of rules when chemical substances move or diffuse freely from one compartment to another.

(c) Binding and debinding rules:

$$\begin{array}{c} a \ [ \ b \ ]_l \to [ \ c \ ]_l \\ \hline \\ [ \ a \ ]_l \to b \ [ \ c \ ]_l \end{array} \right\} \quad \text{where } a, b, c \in O, \text{ and } l \in L$$

Using rules of the first type we can specify reactions consisting in the binding of a ligand swimming in one compartment to a receptor placed on the membrane surface of another compartment. The reverse reaction, debinding of substance from a receptor, can be described as well using the second rule. (d) Recruitment and releasing rules:

$$\left. \begin{array}{l} a \ [ \ b \ ]_l \to c \ [ \ ]_l \\ c \ [ \ ]_l \to a \ [ \ b \ ]_l \end{array} \right\} \quad \text{where } a, b, c \in O, \text{ and } l \in L$$

With these rules we represent the interaction between two chemicals in different compartments whereby one of them is recruited from its compartment by a chemical on the other compartment, and then the new complex remains in the latter compartment. In a releasing rules a complex, c, located in one compartment can dissociate into a and b, remaining a in the same compartment as c, and b being released into the other compartment.

# 3 P Systems using Deterministic Waiting Times Algorithm

In biological systems with large number of molecules deterministic approaches are valid because the interactions between them follows the  $\sqrt{n}$  law of physics, which says that randomness or fluctuation level in a system are inversely proportional to the square root of the number of particles.

Next, we present a *exact* deterministic strategy providing a semantic to the P systems defined above, that we will refer to as *deterministic waiting times algorithm*. It is based on the fact that in vivo chemical reactions take place in parallel in an asynchronous manner, i.e. different chemical reactions proceed at different reaction rates and the same reaction may also have different reaction rates at different times depending on the concentrations of reactants in the region. In the deterministic waiting time, is calculated and the rule (reaction) with the least waiting time is applied, changing the concentration in respective compartments. Each time when there is a change in the concentration of a molecule in any compartment, then the waiting time for reactions "using" that molecule needs to be recalculated for the compartment.

Exact deterministic method means that we do not approximate infinitesimal intervals of time by  $\Delta t$  as it is the case in ODEs, but we will associate a waiting time, computed in a deterministic way, to each reaction and will use them to determine the order in which the reactions take place.

P systems assume rates that determine the speed of reactions. In this respect, we associate to each rule a stochastic constant which represents the average number of application of the rule per time unit. This stochastic constant will be used to compute the probability of applying a rule in a given configuration. This is necessary to characterise the *reality* of the phenomenon to be modelled. The necessity of taking into account these quantitative aspects has been made clear in a few recent studies regarding the use of P systems to model biological systems.

In our models reversible complex formation reactions are frequent. In what follows we discuss how to compute mesoscopic rate constants from the macroscopic ones used in differential equations.

Our rules model reactions of the form:

$$A + B_{k} \rightleftharpoons^{k_a} C$$

This reversible reaction converges to an equilibrium, in which the number of chemical species A, B and C remains constant. The equilibrium constant,  $K_{eq}$ , expresses the quantities of reactants A and B compared to complexes C once the equilibrium is reached; that is:

$$K_{eq} = \frac{[C]}{[A] \cdot [B]} \tag{1}$$

 $K_{eq}$  can also be computed using the association  $k_a$  and dissociation  $k_d$  rate constants:

$$K_{eq} = \frac{k_a}{k_d} \tag{2}$$

The association constant  $k_a$  determines the speed of the association reaction. It measures the number of chemicals A and B that form complexes C per mol and second. For the case of regulatory proteins the association rate constant  $k_a$ can be determined experimentally.  $K_{eq}$  can also be determined experimentally using (1) and therefore  $k_d$  can be computed using (2).

Alternatively, what it can be determined experimentally is Gibbs free energy  $\Delta G$  a notion from thermodynamics which measures the effort necessary for decomplexation. Gibbs free energy is related to the equilibrium constant  $K_{eq}$  as follows:

$$K_{eq} = \exp(\frac{-\Delta G}{R \cdot T}) \tag{3}$$

where  $R = 1.9872 \, cal \, mol^{-1} \, Kelvin^{-1}$  is the universal gas constant and T is the absolute temperature at which the experiments are performed.

Therefore from (2) and (3) the dissociation constant can be determined.

The rate constants  $k_a$  and  $k_d$  we have dealt with up to now are macroscopic, they do not depend on the actual number of molecules, but on concentration. Gillespie's algorithm and thus our approach uses mesoscopic rate constants referring to actual number of molecules and they are determined from their macroscopic counterparts as follows:

$$c_a = \frac{k_a}{A \cdot V} \quad c_d = k_d$$

where  $A = 6.023 \cdot 10^{23}$  is Avogadro's number and V is the cell volume. Note that we assume the cell volume to be constant while ignoring cell growth.

Given a P system, in this strategy each rule r (representing a chemical reaction) in each membrane m has associated a velocity,  $v_r$ , by multiplying the

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stochastic kinetic constant  $c_r$  by the multiplicities of the reactants according to the mass action law. Then we compute the waiting time for the first execution of the rule r as  $\tau_r = \frac{1}{v_r}$  and return the triple  $(\tau_r, r, m)$ .

Below we give a detailed description of the *deterministic waiting times algorithm*:

#### • Initialisation

- $\star$  set time of the simulation t = 0;
- \* for every rule r associated with a membrane m in  $\mu$  compute the triple  $(\tau_r, r, m)$  by using the procedure described before; construct a list containing all such triples;
- \* sort the list of triple  $(\tau_r, r, m)$  according to  $\tau_r$  (in an ascendent order);

#### • Iteration

- $\star$  extract the first triple,  $(\tau_r, r, m)$  from the list;
- $\star$  set time of the simulation  $t = t + \tau_r$ ;
- \* update the waiting time for the rest of the triples in the list by subtracting  $\tau_r$ ;
- $\star$  apply the rule r only once updating the multiplicities of objects in the membranes affected by the application of the rule;
- \* for each membrane m' affected by the application of the rule remove the corresponding all the triples  $(\tau'_{r'}, r', m')$  from the list;
- $\star$  for each membrane m' affected by the application of the rule r recalculate the waiting times;
- ★ comparing the new waiting times with the existing ones, add the smallest triple among the two in the list and sort this list according to each waiting time;
- $\star$  iterate the process.

# • Termination

 $\star$  Terminate simulation when time of the simulation t reaches or exceeds a preset maximal time of simulation.

Note that in this algorithm every rule in each membrane has a waiting time computed in a deterministic way that is used to determine the order in which the rules are executed. Also highlight that in this method the time step varies across the evolution of the system and it is computed in each step depending on the current state of the system.

This strategy have been implemented using Scilab, a scientific software package for numerical computations providing a powerful open computing environment for engineering and scientific applications [23].

# 4 Modelling EGFR Signalling

In this section we study the EGFR Signalling Cascade where the deterministic waiting times algorithm is suitable for describing its evolution.

The epidermal growth factor receptor (EGFR) belongs to the tyrosine kinase family of receptors. Binding of the epidermal growth factor (EGF) to the extracellular domain of EGFR induces receptor dimerisation and autophosphorylation of intracellular domains. Then a multitude of proteins are recruited starting a complex signalling cascade and the receptor follows a process of internalisation ubiquitination and degradation in endosomals.

In our model we consider two marginal pathways and two principal pathways starting from the phosphorylated receptor.

In the first marginal pathway phospholipase C- $\gamma$  (PLC $_{\gamma}$ ) binds to the phospholyrated receptor, then it is phosphorylated (PLC $_{\gamma}^{*}$ ) and released into the cytoplasm where it can be translocated to the cell membrane or desphosphorylated. In the second marginal pathway the protein PI3K binds to the phospholyrated receptor, then it is phosphorylated (PI3K<sup>\*</sup>) and released into the cytoplasm where it regulates several proteins that we do not include in our model.

Both principal pathways lead to activation of Ras-GTP. The first pathway does not depend on the concentration of the Src homology and collagen domain protein (Shc). This pathway consist of a cycle where the proteins growth factor receptor-binding protein 2 (Grb2) and Son of Sevenless homolog protein (SOS) bind to the phosphorylated receptor. Later the complex Grb2-SOS is released in the cytoplasm where it dissociates into Grb2 and SOS.

In the other main pathway Shc plays a key role, it binds to the receptor and it is phosphorylated. Then either Shc<sup>\*</sup> is released in the cytoplasm or the proteins Grb2 and SOS binds to the receptor yielding a four protein complex (EGFR-EGF2\*-Shc\*-Grb2-SOS). Subsequently this complex dissociates into the complexes Shc\*-Grb2-SOS, Shc\*-Grb2 and Grb2-SOS which in turn can also dissociate to produce the proteins Shc<sup>\*</sup>, Grb2 and SOS.

Finally, Ras-GTP is activated by these two pathways and in turn it stimulates the Mitogen Activated Protein (MAP) kinase cascade by phosphorylating the proteins Raf, MEK and ERK. Subsequently phosphorylated ERK regulates several cellular proteins and nuclear transcription factors that we do not include in our model.

There exist *cross-talks* between different parts and cycles of the signalling cascade which suggest a strong robustness of the system.

In Figure 1 it is shown a detailed graphical representation of the signalling cascade.

We have developed a model of the signalling cascade described on the previous page using the following P system:

$$\mathbf{\Pi}_{EGF} = (O, \{e, s, c\}, \mu, (w_1, e), (w_2, s), (w_3, c), \mathcal{R}_e, \mathcal{R}_s, \mathcal{R}_c)$$

Our model consists of more that 60 proteins and complexes of proteins and 160 chemical reactions. We will not give all the details of the model. A complete description of  $\Pi_{EGF}$  with some supplementary information is available from the web page www.gcn.us.es/egfr.pdf. In what follows we give an outline of our model.



Fig. 1. EGFR Signalling Cascade

• Alphabet: In the alphabet *O* we represent all the proteins and complexes of proteins that take part in the signalling cascade simulated. Some of the objects from the alphabet and the chemical compounds that they represent are listed below.

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Object	Protein or Complex
EGF	Epidermal Growth Factor
EGFR	EGF Receptor
$EGFR-EGF_2$	Dimerazated Receptor
$EGFR-EGF_2^*-Shc$	$EGFR-EGF_2^*$ and $Shc$ complex
:	
MEK	Mitogenic external regulated kinase
ERK	External regulated Kinase

• Membrane Structure: In the EGFR Signalling Cascade there are three relevant regions, namely the *environment*, the *cell surface* and the *cytoplasm*. We represent them in the membrane structure as the membranes labelled with: e for the environment, s for the cell surface and c for the cytoplasm. The skin of the structure is the environment, the cell surface is the son of the environment and the father of the cytoplasm.

• Initial Multisets: In the initial multisets we represent the initial number of molecules (nM) of the chemical substances in the environment, the cell surface and the cytoplasm. These estimations has been obtained from [11, 18].

$$\begin{split} & w_1 = \{ EGF^{200} \} \\ & w_2 = \{ EGFR^{250}, Ras\text{-}GDP^{200} \} \\ & w_3 = \{ Shc^{250}, PLC_{\gamma}^{150}, PI3K^{50}, SOS^{40}, Grb2^{80}, TP_1^{100}, TP_2^{450}, TP_3^{450}, TP_4^{125}, \\ & Raf^{80}, MEK^{400}, ERK^{400}, P_1^{80}, P_2^{80}, P_3^{300} \} \end{split}$$

• **Rules:** Through the rules we model the 160 chemical reactions which form the signalling cascade.

As it can be seen in the initial multisets specified before, in the system of the EGFR Signalling Cascade the number of molecules is quite large, as a consequence of the  $\sqrt{n}$  law important fluctuations and stochastic behaviour are not expected in the evolution of the system. Because of this we have chosen the deterministic waiting times algorithm as the strategy for the evolution of the P system  $\Pi_{EGF}$ .

Next, we show two examples of rules of the system.

The set of rules associated with the environment,  $\mathcal{R}_e$ , consists only of one rule r which models the binding of the signal, EGF, to the receptor EGFR.

 $EGF[EGFR]_s \rightarrow [EGF-EGFR]_s, \quad k = 0.003 \ nM^{-1}s^{-1}$ 

The meaning of the previous rule is the following: the object EGF in the membrane containing the membrane with label s (the environment), and the object EGFR inside the membrane with label s (the cell surface) are replaced with the object EGFR-EGF in the membrane with label s; this object represents the complex receptor-signal on the cell surface. We associate the kinetic constant k, which measures the affinity between the signal and the receptor.

The deterministic waiting times algorithm is used in the evolution of the system and the waiting time associated to this rule will be computed using the next formula:

$$\tau_r = \frac{1}{0.003 \cdot |EGF| \cdot |EGFR|}$$

One example from the set of rules  $\mathcal{R}_s$  associated to the cell surface is the dimerisation of the receptor, that is the formation of a complex consisting of two receptors:

$$[EGFR, EGFR]_s \rightarrow [EGFR_2]_s, \quad k = 0.011 \ nM^{-1}s^{-1}$$

When this rule r' is executed two objects EGFR representing receptors are replaced with one object  $EGFR_2$ , representing a complex formed with two receptors, in the membrane with label s, the cell surface. The kinetic constant k is used to computed the waiting time:

$$\tau_{r'} = \frac{1}{0.011 \cdot |EGFR|^2}$$

#### 4.1 Results and Discusions

Using the software mentioned in the previous section and developed in Scilab we run some experiments; in what follows we present some of the results obtained.

In Figure 2 it is depicted the evolution of the number of autophosphorylated receptors and, in Figure 3 the number of doubly phosphorylated MEK (Mitogen External Kinase), one of the target proteins of the signalling cascade that regulates some nuclear transcription factors involved in the cell division.

Note that the activation of the receptor is very fast reaching its maximum within the first 5 seconds and then it decays fast to very low levels; on the other hand the number of doubly phosphorylated MEK is more sustained around 3 nM. These results agree well with empirical observations, see [11, 18].

In tumours it has been reported an overexpression of signals EGF in the environment and of receptors, EGFR, on the cell surface of cancerous cells. Here we investigate the effect of different EGF concentrations and number of receptors on the signalling cascade.

First, we study the effect on the evolution of the number of autophosphorylated receptors and doubly phosphorylated MEK of a range of signals, EGF, from 100 nM to 2000 nM.

In Figure 4, it can be seen that the receptor autophosphorylation is clearly concentration dependent showing different peaks for different number of signals in the environment. According to the variance in the receptor activation it is intuitive to expect different cell responses to different EGF concentrations. Here we will see that this is not the case.



Fig. 2. Autophosphorylated EGFR evolution



Fig. 3. Doubly Phosphorylated MEK evolution

Observe, in Figure 5, that the number of doubly phosphorylated MEK does not depend on the number of signals in the environment. This shows the surprising robustness of the signalling cascade with regard to the number of signals from outside due to EGF concentration. The signal is either attenuated or amplified to get the same concentration of one of the most relevant kinases in the signalling cascade, MEK. Note that after 100 seconds, when the response gets sustained, the lines representing the response to different external EGF concentrations are identical.

Now we analyse the effect on the dynamics of the signalling cascade of different numbers of receptors on the cell surface.



Fig. 4. Receptor Autophosphorylation for different environmental EGF concentrations



Fig. 5. MEK phosphorylation for different environmental EGF concentrations

In Figure 6, it is shown the evolution of the number of doubly phosphorylated MEK when there is 100 nM and 1000 nM of receptors on the cell surface. Note that now the response is considerably different; the number of activated MEK is greater when there is an overexpression of receptors on the cell surface. As a consequence of this high number of activated MEK the cells will undergo an uncontrolled process of proliferation.

The key role played by the overexpression of EGFR on the uncontrolled growth of tumours has been reported before, as a consequence of this, EGFR



Fig. 6. MEK phosphorylation for different number of receptors

is one of the main biological targets for the development of novel anticancer therapies.

Finally, stress that for this system we have used a deterministic approach obtaining results that map well experimental data. This is not always the case, in the next section we analyse a system where a stochastic approach is necessary to describe properly its behaviour.

# 5 Modelling FAS-apoptosis

The term *apoptosis* (also known as *programmed cell death*) was coined by Kerr et al. [7] as a means of distinguishing a morphologically distinctive form of cell death which was associated with normal physiology. In contrast to necrosis (a form of cell death that occurs when cells are damaged by injury), apoptosis is carried out in an ordered process without releasing intracellular materials from the dying cells.

Apoptosis is a cellular response to a *cellular insult* that starts a cascade of events which lead to the destruction of the cell. This mechanism is an innate response of the cell that helps the unwanted, injured, or improperly developed cells to commit suicide. Apoptosis protects the rest of the organism from a potentially harmful agent and dysregulation of apoptosis can contribute to development of autoimmune diseases and cancers.

Apoptosis is mediated by a family of proteases called caspases divided into two subgroups. The first group consists of caspase 8, caspase 9, and caspase 10, and they function as initiators of the cell death process. The second group contains caspase 3, caspase 6, and caspase 7, and they work as effectors. The other effector molecule in apoptosis is Apaf-1, which, together with cytochrome c, stimulates the processing of pro-caspase 9 to the mature enzyme.

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The other regulators of apoptosis are the Bcl2 family members, divided into three subgroups based on their structure. Members of the first subgroup, represented by Bcl2 and Bcl-xL, have an anti-apoptotic function. The second subgroup, represented by Bax and Bak, and the third subgroup, represented by Bid and Bad, are pro-apoptotic molecules.

Apoptotic death can be triggered by a wide variety of stimuli. Among the more studied death stimuli are DNA damage which in many cells leads to apoptotic death via a pathway dependent on p53, and the signalling pathways for FAS-induced apoptosis that was shown to be one of the most relevant processes for understanding and combating cancer, AIDS and neurodegenerative diseases such as Parkinson's disease, Alzheimer, etc.

Two pathways activated by FAS have been identified [17], and are referred to as type I (*death receptor pathway*) and type II (*mitochondrial pathway*), where caspases play a crucial role for both the initiation and execution apoptosis. The pathways diverge after activation of initiator caspases and converge at the end by activating executor caspases. In the type I pathway, initiator caspases activate executor caspases directly. In the type II pathway, a more complicated cascade is activated involving the disruption of mitochondrial membrane potential.



Fig. 7. FAS signalling pathways

Despite many molecular components of these apoptotic pathways heve been identified, we need understand how they work together into a consistent network. A way to understand complex biological processes, in general, and the complex

signalling behaviour of these pathways, in particular, is by modelling them in a computational framework and simulating them in electronic computers.

In [5] the two pathways activated by FAS starting with the stimulation of FASL (FAS ligand) until the activation of the effector caspase 3, have been modeled using ordinary differential equations in which biochemical reactions where used to describe molecular interactions.

In this section we present a P system using deterministic waiting times algorithm for modelling FAS induced apoptosis, implementing all the rules described in [5] for both pathways.

 $\mathbf{\Pi}_{FAS} = (O, \{e, s, c, m\}, \mu, (w_1, e), (w_2, s), (w_3, c), (w_4, m), \mathcal{R}_e, \mathcal{R}_s, \mathcal{R}_c, \mathcal{R}_m)$ 

Our model consists of 53 proteins and complexes of proteins and 99 chemical reactions. We will not give all the details of the model. A complete description of  $\Pi_{FAS}$  with some supplementary information is in [4]. In what follows we give an outline of our model.

• Alphabet: In the alphabet *O* we represent all the proteins and complexes of proteins that take part in the signalling cascade simulated. Some of the objects from the alphabet and the chemical compounds that they represent are listed below.

Object	Protein or Complex
FAS	Fas protein, member of the Tumor Necrosis Factor family
FASL	Fas Ligand
FADD	Fas–associating protein with death domain
:	
Apaf	Apoptotic protease activating factor
Smac	Second mitochondria–derived activator of caspase
XIAP	X–linked inhibitor of apoptosis protein

• Membrane Structure: In the FAS signalling pathways there are three relevant regions, namely the *environment*, the *cell surface*, the *cytoplasm* and the *mitochondria*. We represent them in the membrane structure as the membranes labelled with: e for the environment, s for the cell surface, c for the cytoplasm, and m for the *mitochondria*. The skin of the structure is the environment, the cell surface is the son of the environment, the father of the cytoplasm, and the grandfather of the mitochondria.

• Initial Multisets: In the initial multisets we represent the initial number of molecules of the chemical substances in the environment, the cell surface, the cytoplasm, the mitochondria. These estimations has been obtained from [5].

$$\begin{split} & w_1 = \{FASL^{12500}\} \\ & w_2 = \{FAS^{6023}\} \\ & w_3 = \{FADD^{10040}, CASP8^{20074}, FLIP^{48786}, CASP3^{120460}, Bid^{15057}, \\ & Bax^{50189}, XIAP^{18069}, Apaf^{60230}, CASP9^{12046}\} \\ & w_4 = \{Smac^{60230}, Cyto.c^{60230}, Bcl2^{45172}\} \end{split}$$

• **Rules:** Through the rules we model the 99 chemical reactions which form the signalling pathways. The rules can be found in [4] and they are described in our model as in the case of the system  $\Pi_{EGFR}$  (with different rules in the alternative cases of type II pathway in next subsection).

The set of rules associated with the environment,  $\mathcal{R}_e$ , consists only of one rule  $r_1$  which models the binding of the FAS ligand to the receptor *FAS*.

$$FASL \ [FAS]_s \to [FASC]_s , \quad k_1 = 9.09E - 05 \ nM^{-1}s^{-1}$$

The meaning of the previous rule is the following: the object FASL in the membrane containing the membrane with label s (the environment), and the object FAS inside the membrane with label s (the cell surface) are replaced with the object FASC in the membrane with label s; this object represents the complex receptor-signal on the cell surface. We associate the kinetic constant  $k_1$ , which measures the affinity between the signal and the receptor.

The deterministic waiting times algorithm is used in the evolution of the system and the waiting time associated to this rule will be computed using the next formula:

$$\tau_{r_1} = \frac{1}{9.09E - 05 \cdot |EGF| \cdot |EGFR|}$$

#### 5.1 Results and Discusions

We implemented in Java a preliminary *simulator* for the P system. It accepts as input an SBML (Systems Biology Markup Language) file containing the rules to be simulated and initial concentrations for the molecules in the system.

We compared our results with both the experimental data and with the ODEs simulation data reported in the paper [5].

One of the major proteins in the pathway, caspase 3 was compared to the experimental data. In the ODEs simulation, caspase 3 was activated at 4 hours, and it was considered close to the experimental results where it was obtained that it activated at 6 hours (see the Figure 8).

The same pathway is modeled in the membrane computing framework using the same reactions and initial conditions. The caspase 3 activation dynamics is studied when Bcl2 is at baseline value. Caspase 3 is activated in our simulator after about 7 hours which is a very good approximation of the experimental data and also the simulated pathway in [5].

There are cells (as thymocytes and fibroblasts) which are not sensitive to Bcl2 overexpression as described in [17]. In these cells caspase 8 directly activates caspase 3.

Scaffidi et al. has suggested in [17] that the type of pathway is chosen based on the concentration of caspase 8 generated in active form following FASL binding. If the caspase 8 concentration is high, then the caspase 3 is activated directly, on the other hand, if the concentration of caspase 8 is low, the type II pathway is chosen so that the system is amplifying the death signal through the mitochondria to be able to induce the cell death.

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Fig. 8. Comparison between experimental data (top left), previous ODE simulation data (top right) and the P system simulation data (down).

To check this hypothesis, the active caspase 8 formation is increased by having the initial concentration of caspase 8 set to a value 20 times greater than its baseline value while everything else was kept the same in the system. We performed the same simulation with the increase in caspase 8 initial concentration, this resulted in faster caspase 3 activation also in our simulation and is agree well with the results obtained in [17].

The Bcl2 concentration is also increased 100 times to test the sensitivity of caspase 3 activation to Bcl2. The Figure 9 shows that the caspase 3 activation is not sensitive to the increase in Bcl2 concentration.

Bcl2 is known to block the mitochondrial pathway; however, it is not clear the mechanism through which Bcl2 can block the pathway of type II. Next, we analyze the caspase 3 activation kinetics in this pathway by considering different mechanisms to block the mitochondrial pathway suggested in [3], [12] and [21]: Bcl2 might bind with (a) Bax, (b) Bid, (c) tBid, or (d) bind to both Bax and tBid.



Fig. 9. Left the P system simulation, right the ODE simulation for the change in caspase 8 initial concentration.

We design four different P systems having the rules:

 $\begin{array}{l} -r_1, \ldots, r_{95}, r_{96}, r_{97} \text{ for the case (a).} \\ -r_1, \ldots, r_{95}, r_{96}', r_{97}' \text{ for the case (b).} \\ -r_1, \ldots, r_{95}, r_{96}'', r_{97}'' \text{ for the case (c).} \\ -r_1, \ldots, r_{97}, r_{98}, r_{99} \text{ for the case (d).} \end{array}$ 

All the other rules remain the same for all the cases (see [4] for details).

The dynamics of caspase 3 activation is studied by varying the Bcl2 concentration 10 times or 100 times the baseline value. It was concluded that Bcl2 binding to both Bax and tBid is the most efficient mechanism for the pathway in comparison with the results obtained for the cases (a), (b) or (c). The same conclusions were obtained also after using our simulator for all the previous changes in the pathway.

The Figure 10 shows only the case (d) as a comparison between the ODE simulator and cellular simulator.



Fig. 10. Left the P system simulation, right the ODE simulation for the change in caspase 3 sensitivity to changes in initial concentration for Bcl2 when Bcl2 is able to bind to both Bax and tBid.

### 6 Conclusions

In this paper we have presented P systems as a new computational modelling tool for the dynamic behaviour of integrated signalling systems through a mesoscopic chemistry approach.

P systems are also general specification of the biological phenomena that can be evolved using different strategies/algorithms. A *deterministic waiting times algorithm* has been introduced, and it is based on the fact that in vivo chemical reactions take place in parallel in an asynchronous manner.

That strategy has been illustrated with the simulation of two relevant biological phenomena: the EGFR Signalling Cascade and the signalling pathways for FAS-induced apoptosis. These studies can be a guide to combining models and experiments to understand complex biological processes as integrated systems.

Our results show good correlation with the experimental data reported in the literature and with simulators based on ODEs. So, it justify the reliability of P systems as computational modelling tools to produce postdiction, and perhaps they will be able to produce plausible predictions.

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# References

- Bhalla, U.S., Iyengar, R., Emergent properties of networks of biological signaling pathways. Science, 283 (1999), 381–387.
- Blossey, R., Cardelli, L., Phillips, A. A compositional approach to the stochastic dynamics of gene networks. *Transactions on Computational Systems Biology*, IV, Lecture Notes in Computer Science, **3939** (2006), 99–122.
- Cheng, E.H., Wei, M.C., Weiler, S., Flavell, R.A., Mak, T.W., Lindsten, T., Korsmeyer, S.J. BCL-2, BCL-XL sequester BH3 domain-only molecules preventing BAX- and BAK-mediated mitochondrial apoptosis. *Molecular Cell*, 8 (2001), 705– 711.
- Cheruku, S., A. Păun, F.J. Romero, M.J. Pérez–Jiménez, O.H. Ibarra. Simulating FAS–induced apoptosis by using P systems. Communication accepted at the *Bio–Inspired Computing: Theory and Applications*, Wuhan, China, September, 18–22, 2006.
- Hua, F., Cornejo, M., Cardone, M., Stokes, C., Lauffenburger, D. Effects of Bcl-2 Levels on FAS Signaling-Induced Caspase-3 Activation: Molecular Genetic Tests of Computational Model Predictions. *The Journal of Immunology*, **175**, 2 (2005), 985–995 and correction **175**, 9 (2005), 6235–6237.
- Ibarra, O.H., Păun, A. Counting time in computing with cells. Proceedings of DNA Based Computing, DNA11, London, Ontario, 25–36, 2005.
- Kerr, J.F., Wyllie, A.H., Currie, A.R. Apoptosis: a basic biological phenomenon with wide-ranging implications in tissue kinetics. *British Journal Cancer*, 26 (1972), 239.

- Pogson, M., Smallwood, R., Qwarnstrom, E., Holcombe, Formal agent-based of intracellular chemical interactions. *BioSystems*, 85, 1 (2006), 37–45.
- 9. Holcombe, M., Gheorghe, M., Talbot, N. A hybrid machine model of rice blast fungus, Magnaphorte Grisea. *BioSystems*, **68**, 2–3 (2003), 223–228.
- Jackson, D., Holcombe, M., Ratnieks, F. Trail geometry gives polarity to ant foraiging networks. *Nature* 432 (2004), 907–909.
- Moehren G., Markevich, N., Demin, O., Kiyatkin, A., Goryanin, I., Hoek, J.B., Kholodenko, B.N. Temperature Dependence of the Epidermal Growth Factor Receptor Signaling Network Can Be Accounted for by a Kinetic Model, *Biochemistry* 41 (2002), 306–320.
- Oltavi, Z.N., Milliman, C.L., Korsmeyer, S.J. Bcl-2 heterodimerizes in vivo with a conserved homolog, Bax, that accelerates programmed cell death. *Cell*, 74, 4 (1993), 609–619.
- Gh. Păun, Computing with membranes. Journal of Computer and System Sciences, 61, 1 (2000), 108–143, and Turku Center for Computer Science-TUCS Report Nr. 208, 1998.
- 14. Gh. Păun, Membrane Computing. An Introduction. Springer-Verlag, Berlin, 2002.
- Gh. Păun, G. Rozenberg, A guide to membrane computing. *Theoretical Computer Science*, 287 (2002), 73–100.
- Pérez-Jiménez, M.J., Romero-Campero, F.J. A Study of the Robustness of the EGFR Signalling Cascade using Continuous Membrane Systems. *Lecture Notes in Computer Science*, **3561** (2005), 268 – 278.
- Scaffidi, C., Fulda. S., Srinivasan, A., Friesen, C., Li, F., Tomaselli, K.J., Debatin, K.M., Krammer, P.H., Peter, M.E. Two CD95 (APO-1/Fas) signaling pathways. *The Embo Journal*, **17** (1998), 1675–1687.
- Schoeberl, B., Eichler–Jonsson, C., Gilles, E.D., Muller, G. Computational Modeling of the Dynamics of the MAP Kinase Cascade Activated by Surface and Internalized EGF Receptors, *Nature Biotechnology*, **20**, 4 (2002), 370–375.
- Van Kampen, N.G. Stochastics processes in Physics and Chemistry, Elsevier Science B.V., Amsterdam, The Netherlands, 1992.
- Walker, D.C., Southgate, J., Hill, G., Holcombe, M., Hose, D.R., Wood S.M., MacNeil, S., Smallwood, R.H. The epitheliome: modelling the social behaviour of cells. *BioSystems*, **76**, 1–3 (2004), 89–100.
- Wang, K., Yin, X.M., Chao, D.T., Milliman, C.L., Korsmeyer, S.J. BID: a novel BH3 domain-only death agonist. *Genes & Development*, 10 (1996). 2859–2869.
- 22. ISI web page: http://esi-topics.com/erf/october2003.html
- 23. SciLab Web Site http://scilabsoft.inria.fr/