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# Cryptanalysis of a certificateless signcryption scheme in the standard model

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## A B S T R A C T

Certificateless signcryption is a useful primitive which simultaneously provides the functionalities of certificateless encryption and certificateless signature. Recently, Liu et al. [15] proposed a new certificateless signcryption scheme, and claimed that their scheme is provably secure without random oracles in a strengthened security model, where the malicious-but-passive KGC attack is considered. Unfortunately, by giving concrete attacks, we indicate that Liu et al. certificateless signcryption scheme is not secure in this strengthened security model.

### Keywords:

Certificateless signcryption  
Malicious-but-passive KGC attack  
Semantic security  
Existential unforgeability

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## 1. Introduction

To simplify the certificate management in traditional public key infrastructure (PKI), Shamir introduced the concept of identity-based cryptography, where an entity's public key is determined as his identity such as email address, and the corresponding private key is generated by a trusted third party named private key generator (PKG). The identity is a natural link to a user, hence it can eliminate the need for certificates as used in traditional PKI. However, identity-based cryptography inevitably suffers from the key escrow problem, i.e., all the users' private keys are known to the PKG who thus can perform cryptographic operations (such as decryption and signing) on behalf of these users.

In order to resolve the above key escrow problem for identity-based cryptography, Al-Riyami and Paterson [1] introduced the concept of certificateless public key cryptography (CL-PKC). In CL-PKC, a third party named key generation center (KGC) is also involved. However, in contrast to the PKG in identity-based cryptography, the KGC does not generate the full private key for the user. Instead, the KGC only supplies the user with a partial private key which is computed from the user's identity. The user then chooses a secret value and combines the partial private key to generate the full private key. CL-PKC can successfully resolve the key escrow problem while avoiding the use of certificates.

Since its advent, CL-PKC has attracted great interest, and many certificateless cryptosystems have been proposed, including many certificateless encryption schemes and certificateless signature schemes, e.g. [10,3,14,12,8,16,9,17,11,13]. As an extension of the signcryption [18] in the certificateless scenario, Barbosa and Farshim [4] introduced the concept of

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certificateless signcryption, which simultaneously provides the functionalities of certificateless encryption and certificateless signature. In [4], Barbosa and Farshim proposed a concrete certificateless signcryption scheme, and proved its security in the random oracle model [5]. As indicated in [6,7], a proof in the random oracle model can only serve as a heuristic argument and cannot ensure the security in the real implementation. In addition, the security model defined in [4] does not consider the malicious-but-passive KGC attack [2], which allows the KGC to embed extra trapdoors in the system parameters. As noted by Liu et al. [15], Barbosa and Farshim's certificateless signcryption scheme will be insecure under the malicious-but-passive KGC attack. To address the above problems, Liu et al. [15] proposed a new certificateless signcryption scheme, and claimed that their scheme is provably secure without random oracles, even under the malicious-but-passive KGC attack. However, in this paper, by giving concrete attacks, we indicate that Liu et al. certificateless signcryption scheme is not secure against the malicious-but-passive KGC attack.

## 2. Preliminaries

### 2.1. Bilinear pairing

Let  $\mathbb{G}$  and  $\mathbb{G}_T$  be two (multiplicative) cyclic groups with prime order  $p$ . A bilinear pairing is a map  $e : \mathbb{G} \times \mathbb{G} \rightarrow \mathbb{G}_T$  with the following properties:

- **Bilinearity:**  $\forall g_1, g_2 \in \mathbb{G}, \forall a, b \in \mathbb{Z}_p^*$ , we have  $e(g_1^a, g_2^b) = e(g_1, g_2)^{ab}$ ;
- **Non-degeneracy:** There exist  $g_1, g_2 \in \mathbb{G}$  such that  $e(g_1, g_2) \neq 1_{\mathbb{G}_T}$ , where  $1_{\mathbb{G}_T}$  denotes the identity element of group  $\mathbb{G}_T$ ;
- **Computability:** There exists an efficient algorithm to compute  $e(g_1, g_2)$  for  $\forall g_1, g_2 \in \mathbb{G}$ .

### 2.2. Formal model of certificateless signcryption

In this subsection, we shall review the definition and security notions specified in [15], only with slight notational differences.

#### 2.2.1. Definition of certificateless signcryption

A certificateless signcryption scheme consists of the following six algorithms:

- Setup( $\kappa$ ):** On input a security parameter  $\kappa$ , this setup algorithm generates a master key  $msk$  and the system parameters  $params$ . After this algorithm is performed, the KGC publishes  $params$  and keeps  $msk$  secret.
- Partial-Private-Key-Extract( $params, msk, u$ ):** On input  $params, msk$  and an identity  $u$ , this algorithm outputs the partial private key  $d_u$  for identity  $u$ . Note that the KGC executes this algorithm to generate  $d_u$  and sends it to the corresponding owner  $u$  via a secure channel.
- User-Key-Generate( $params, u$ ):** On input  $params$  and an identity  $u$ , this algorithm returns a secret value  $x_u$  and a corresponding public key  $pk_u$  for identity  $u$ . Note that the entity  $u$  executes this algorithm to generate his public key, and then distributes the public key  $pk_u$  without being certificated.
- Private-Key-Extract( $params, d_u, x_u$ ):** On input  $params$ , and entity's partial private key  $d_u$  and secret value  $x_u$ , this algorithm generates the entity's full private key  $sk_u$ . Note that this algorithm is executed by the entity itself.
- Signcrypt( $params, M, sk_S, u_S, pk_S, u_R, pk_R$ ):** On input  $params$ , a message  $M$ , a sender's private key  $sk_S$ , identity  $u_S$  and public key  $pk_S$ , and a receiver's identity  $u_R$  and public key  $pk_R$ , this algorithm outputs a ciphertext  $\sigma$  or an error symbol  $\perp$ .
- Unsigncrypt( $\sigma, sk_R, u_S, pk_S$ ):** On input a ciphertext  $\sigma$ , the receiver's private key  $sk_R$ , and the sender's identity  $u_S$  and public key  $pk_S$ , this algorithm outputs the plaintext  $M$  or an error symbol  $\perp$ .

#### 2.2.2. Security models

Based on Barbosa and Farshim's model [4], Liu et al. [15] presented a strengthened model considering the malicious-but-passive KGC attack.

**Confidentiality.** The confidentiality security for a certificateless signcryption scheme is defined via the following two games against Type I and Type II adversaries:

**Game I.** In this game, a Type I adversary models an "outsider" adversary, who can replace the public key of arbitrary identities but cannot corrupt the master secret key. Concretely, this game is played between a challenger  $\mathcal{C}$  and a Type I adversary  $\mathcal{A}_I$  as below:

- **Initialization.** Challenger  $\mathcal{C}$  runs algorithm Setup to generate the master secret key  $msk$  and the system parameters  $params$ .  $\mathcal{C}$  gives  $params$  to  $\mathcal{A}_I$  and keeps  $msk$  secret.

- **Phase 1.** In this phase,  $\mathcal{A}_I$  adaptively performs a polynomially bounded number of queries as below:
  - *Request public key.* When  $\mathcal{A}_I$  supplies an identity  $u$  and requests the public key for  $u$ , challenger  $\mathcal{C}$  responds with the corresponding public key  $pk_u$ .
  - *Extract partial private key.* When  $\mathcal{A}_I$  supplies an identity  $u$  and requests  $u$ 's partial private key,  $\mathcal{C}$  responds with the partial private key  $d_u$  for this identity.
  - *Replace public key.* When  $\mathcal{A}_I$  supplies an identity  $u$  and a new valid public key value  $pk'_u$ , challenger  $\mathcal{C}$  replaces the current public key with  $pk'_u$ .
  - *Extract private key.* When  $\mathcal{A}_I$  requests the private key of an identity  $u$  whose public key was not replaced, challenger  $\mathcal{C}$  responds with the private key  $sk_u$  for this identity.
  - *Signcrypt.* When  $\mathcal{A}_I$  submits a sender with identity  $u_S$ , a receiver with identity  $u_R$  and a message  $M$ , challenger  $\mathcal{C}$  first runs  $\text{Signcrypt}(params, M, sk_S, u_S, pk_S, u_R, pk_R)$ , and then returns the resulting ciphertext to  $\mathcal{A}_I$ . Here  $sk_S$  denotes the sender's private key. Note that it is possible for the challenger to be unaware of the sender's secret value when the associated public key has been replaced by adversary  $\mathcal{A}_I$ . In this case, we require  $\mathcal{A}_I$  to provide the sender's secret value.
  - *Unsigncrypt.* When  $\mathcal{A}_I$  submits a ciphertext  $\sigma$ , a sender with identity  $u_S$  and a receiver with identity  $u_R$ , challenger  $\mathcal{C}$  returns the result of  $\text{Unsigncrypt}(\sigma, sk_R, u_S, pk_S)$ . Note that it is possible for the challenger to be unaware of the receiver's secret value when the associated public key has been replaced by adversary  $\mathcal{A}_I$ . In this case, we require  $\mathcal{A}_I$  to provide the receiver's secret value.
- **Challenge.** Once  $\mathcal{A}_I$  decides that phase 1 is over, it outputs two distinct identities  $\{u_{S^*}, u_{R^*}\}$  and two equal-length messages  $\{M_0, M_1\}$ . Challenger  $\mathcal{C}$  first chooses a bit  $\gamma$  randomly, and then computes  $\sigma^* = \text{Signcrypt}(params, M_\gamma, sk_{S^*}, u_{S^*}, pk_{S^*}, u_{R^*}, pk_{R^*})$ . Finally,  $\mathcal{C}$  gives  $\sigma^*$  to  $\mathcal{A}_I$ .
- **Phase 2.** Adversary  $\mathcal{A}_I$  continues to issue queries as in phase 1, and  $\mathcal{C}$  responds in the same way as in phase 1.
- **Response.** Finally, adversary  $\mathcal{A}_I$  returns a bit  $\gamma^*$ . We say that  $\mathcal{A}_I$  wins the above game if  $\gamma^* = \gamma$  and the following conditions are simultaneously satisfied:
  - (1)  $\mathcal{A}_I$  cannot extract the private key for  $u_{R^*}$ .
  - (2)  $\mathcal{A}_I$  cannot extract the private key for any identity if the corresponding public key has been replaced.
  - (3)  $\mathcal{A}_I$  cannot extract the partial private key for  $u_{R^*}$  if  $\mathcal{A}_I$  has replaced the public key  $pk_{R^*}$  before the challenge phase.
  - (4) In phase 2,  $\mathcal{A}_I$  cannot make an unsigncrypt query on the challenge ciphertext  $\sigma^*$  under  $u_{S^*}$  and  $u_{R^*}$  unless the sender's public key  $pk_{S^*}$  or the receiver's public key  $pk_{R^*}$ , that were used to signcrypt  $M_\gamma$ , has been replaced after the challenge phase.

We define  $\mathcal{A}_I$ 's advantage as  $\text{Adv}_{\mathcal{A}_I}^{\text{IND-CLSC-CCA}^2} = |2\Pr[\gamma^* = \gamma] - 1|$ .

**Game II.** In this game, a Type II adversary models an "insider" adversary, who can corrupt the master secret key but cannot replace any public key. Concretely, this game is played between a challenger  $\mathcal{C}$  and a Type II adversary  $\mathcal{A}_{II}$  as below:

- **Initialization.** Adversary  $\mathcal{A}_{II}$  runs algorithm *Setup* to generate the master secret key  $msk$  and the system parameters  $params$ .  $\mathcal{A}_{II}$  then gives  $params$  and  $msk$  to  $\mathcal{C}$ . We should keep in mind that  $\mathcal{A}_{II}$  generates  $params$  and  $msk$  by itself.
- **Phase 1.** In this phase,  $\mathcal{A}_{II}$  adaptively issues a polynomially bounded number of queries as in game I. The only constraint is that  $\mathcal{A}_{II}$  cannot replace any public key. Obviously,  $\mathcal{A}_{II}$  can compute the partial private key of any identity by itself with the master secret key.
- **Challenge.** Once  $\mathcal{A}_{II}$  decides that phase 1 is over, it outputs two distinct identities  $\{u_{S^*}, u_{R^*}\}$  and two equal-length messages  $\{M_0, M_1\}$ . Challenger  $\mathcal{C}$  first chooses a bit  $\gamma$  randomly, and then computes  $\sigma^* = \text{Signcrypt}(params, M_\gamma, sk_{S^*}, u_{S^*}, pk_{S^*}, u_{R^*}, pk_{R^*})$ . Finally,  $\mathcal{C}$  returns  $\sigma^*$  to  $\mathcal{A}_{II}$ .
- **Phase 2.** Adversary  $\mathcal{A}_{II}$  continues to issue queries as in phase 1, and  $\mathcal{C}$  responds in the same way as in phase 1.
- **Response.** Finally, adversary  $\mathcal{A}_{II}$  returns a bit  $\gamma^*$ . We say that  $\mathcal{A}_{II}$  wins the above game if  $\gamma^* = \gamma$  and the following conditions are simultaneously satisfied:
  - (1)  $\mathcal{A}_{II}$  cannot extract the private key for the challenge identity  $u_{R^*}$ .
  - (2) In phase 2,  $\mathcal{A}_{II}$  cannot make an unsigncrypt query on the challenge ciphertext  $\sigma^*$  under  $u_{S^*}, u_{R^*}$  and public key  $pk_{R^*}$  that were used to signcrypt  $M_\gamma$ .

We define  $\mathcal{A}_{II}$ 's advantage as  $\text{Adv}_{\mathcal{A}_{II}}^{\text{IND-CLSC-CCA}^2} = |2\Pr[\gamma^* = \gamma] - 1|$ .

A certificateless signcrypt scheme is said to be semantically secure against adaptive chosen ciphertext attacks, if there exists neither polynomial time Type I adversary nor polynomial time Type II adversary who has a non-negligible advantage in game I and game II, respectively.

**Unforgeability.** The authenticity security (existential unforgeability against chosen message attacks (EUF-CMA)) for a certificateless signcrypt scheme is captured by the following two games against Type I and Type II adversaries, respectively.

**Game III.** This game is played between a challenger  $\mathcal{C}$  and a Type I adversary  $\mathcal{A}_I$  for a certificateless signcrypt scheme as follows:

- **Initialization.** Challenger  $\mathcal{C}$  runs algorithm *Setup* to generate the master secret key  $msk$  and the system parameters  $params$ . Then  $\mathcal{C}$  gives  $params$  to  $\mathcal{A}_I$  and keeps the master secret key  $msk$  to itself.

- **Queries.** In this phase,  $\mathcal{A}_I$  adaptively issues a polynomial bounded number of queries as in game I.
- **Output.** Finally,  $\mathcal{A}_I$  outputs a new triple  $(\sigma^*, u_{S^*}, u_{R^*})$ , which is not produced by the signcryption query. Adversary  $\mathcal{A}_I$  wins game III if the result of  $\text{Unsigncrypt}(\sigma^*, sk_{R^*}, u_{S^*}, pk_{S^*})$  is not the symbol  $\perp$  and the queries are subject to the following constraints:
  - (1)  $\mathcal{A}_I$  cannot extract the private key for  $u_{S^*}$ .
  - (2)  $\mathcal{A}_I$  cannot extract the private key for any identity if the corresponding public key has been replaced.
  - (3)  $\mathcal{A}_I$  cannot extract the partial private key for  $u_{S^*}$ .

We define  $\mathcal{A}_I$ 's success probability in game III to be  $\text{Succ}_{\mathcal{A}_I}^{\text{EUF-CLSC-CMA}} = \Pr[\mathcal{A}_I \text{ wins}]$ .

**Game IV.** This game is played between a challenger  $\mathcal{C}$  and a Type II adversary  $\mathcal{A}_{II}$  for a certificateless signcryption scheme as follows:

- **Initialization.** Adversary  $\mathcal{A}_{II}$  runs algorithm *Setup* to generate the master secret key  $msk$  and the system parameters  $params$ . Then  $\mathcal{A}_{II}$  gives  $params$  to  $\mathcal{C}$ . Note that  $\mathcal{A}_{II}$  generates  $msk$  and  $params$  itself.
- **Queries.** In this phase,  $\mathcal{A}_{II}$  adaptively issues a polynomial bounded number of queries as in game II.
- **Output.** Finally,  $\mathcal{A}_{II}$  outputs a new triple  $(\sigma^*, u_{S^*}, u_{R^*})$ , which is not produced by the signcryption query. Adversary  $\mathcal{A}_{II}$  wins game IV if the result of  $\text{Unsigncrypt}(\sigma^*, sk_{R^*}, u_{S^*}, pk_{S^*})$  is not the error symbol  $\perp$  and  $\mathcal{A}_{II}$  did not extract the private key for  $u_{S^*}$ .

We define  $\mathcal{A}_{II}$ 's success probability in game IV to be  $\text{Succ}_{\mathcal{A}_{II}}^{\text{EUF-CLSC-CMA}} = \Pr[\mathcal{A}_{II} \text{ wins}]$ .

A certificateless signcryption scheme is said to be existentially unforgeable under adaptive chosen message attacks, if there exists neither polynomial time Type I adversary nor polynomial time Type II adversary who has a non-negligible success probability in game III and game IV, respectively.

### 3. Review of Liu et al.'s certificateless signcryption scheme

In this section, we review Liu et al.'s identity-based signcryption scheme [15], which is specified by the following algorithms:

**Setup:** Let  $(\mathbb{G}, \mathbb{G}_T)$  be bilinear groups such that  $|\mathbb{G}| = |\mathbb{G}_T| = p$  for some prime  $p$ , and let  $g$  be a generator of  $\mathbb{G}$ . Given a pairing  $e : \mathbb{G} \times \mathbb{G} \rightarrow \mathbb{G}_T$  and a collision resistant hash function  $H : \{0, 1\}^m \rightarrow \{0, 1\}^m$ , the KGC randomly chooses  $\alpha \in \mathbb{Z}_p$  and computes  $g_1 = g^\alpha$ . In addition, the KGC randomly picks  $g_2, u', v' \in \mathbb{G}$  and two random vectors  $\vec{U} = (u_i)_n, \vec{V} = (v_j)_m$  from group  $\mathbb{G}$  with lengths  $n$  and  $m$ , respectively. The system parameters are  $params = (\mathbb{G}, \mathbb{G}_T, e, g, g_1, g_2, u', v', \vec{U}, \vec{V}, H)$  and the master secret key is  $msk = g_2^\alpha$ .

**Partial-Private-Key-Extract:** Let  $u[i]$  denote the  $i$ th bit of an identity  $u \in \{0, 1\}^n$  and  $\mathcal{U} = \{i | u[i] = 1, i = 1, \dots, n\}$ . The KGC with master secret key  $msk = g_2^\alpha$  randomly picks  $r \in \mathbb{Z}_p$  and computes

$$d_u = (d_{u,1}, d_{u,2}) = \left( g_2^\alpha \left( u' \prod_{i \in \mathcal{U}} u_i \right)^r, g^r \right).$$

An entity with identity  $u$  is given  $d_u$  as his partial private key. Therefore, the partial private keys for the sender  $u_S$  and the receiver  $u_R$  are respectively

$$d_S = (d_{S,1}, d_{S,2}) = \left( g_2^\alpha \left( u' \prod_{i \in \mathcal{U}_S} u_i \right)^{r_S}, g^{r_S} \right),$$

$$d_R = (d_{R,1}, d_{R,2}) = \left( g_2^\alpha \left( u' \prod_{i \in \mathcal{U}_R} u_i \right)^{r_R}, g^{r_R} \right).$$

**User-Key-Generate:** An entity with identity  $u$  randomly chooses a secret value  $x_u \in \mathbb{Z}_p$  and sets his public key to be  $pk_u = e(g_1, g_2)^{x_u}$ .

**Private-Key-Extract:** An entity with identity  $u$  randomly picks  $r' \in \mathbb{Z}_p$ , and computes his private key as

$$sk_u = (sk_{u,1}, sk_{u,2}) = \left( d_{u,1}^{x_u} \left( u' \prod_{i \in \mathcal{U}} u_i \right)^{r'}, d_{u,2}^{x_u} g^{r'} \right) = g_2^{2x_u} \left( u' \prod_{i \in \mathcal{U}} u_i \right)^t, g^t,$$

where  $t = rx_u + r'$ .

**Signcrypt:** To send a plaintext  $M \in \mathbb{G}_T$  to the receiver with identity  $u_R$  and public key  $pk_R$ , the sender with identity  $u_S$  uses his private key  $sk_S = (sk_{S,1}, sk_{S,2})$  to perform the following steps:

1. Randomly pick  $r'' \in \mathbb{Z}_p$ .

2. Compute  $\sigma_1 = M \cdot pk_R^{r''} = M \cdot e(g_1, g_2)^{x_R \cdot r''}$ .
3. Compute  $\sigma_2 = g^{r''}$ .
4. Compute  $\sigma_3 = \left( u' \prod_{i \in \mathcal{U}_R} u_i \right)^{r''}$ .
5. Set  $\sigma_4 = sk_{S,2}$ .
6. Compute  $\bar{M} = H(\sigma_1, \sigma_2, \sigma_3, \sigma_4, u_R, pk_R) \in \{0, 1\}^m$ , where  $\bar{M}[j]$  denotes the  $j$ th bit of  $\bar{M}$  and  $\mathcal{M} = \{j | \bar{M}[j] = 1, j = 1, 2, \dots, m\}$ .
7. Compute  $\sigma_5 = sk_{S,1} \cdot \left( v' \prod_{j \in \mathcal{M}} v_j \right)^{r''}$ .
8. Output the ciphertext  $\sigma = (\sigma_1, \sigma_2, \sigma_3, \sigma_4, \sigma_5)$ .

Unsigncrypt: Upon receiving a ciphertext  $\sigma = (\sigma_1, \sigma_2, \sigma_3, \sigma_4, \sigma_5)$ , the receiver decrypts the ciphertext as follows:

1. Compute  $\bar{M} = H(\sigma_1, \sigma_2, \sigma_3, \sigma_4, u_R, pk_R) \in \{0, 1\}^m$ , where  $\bar{M}[j]$  denotes the  $j$ th bit of  $\bar{M}$  and  $\mathcal{M} = \{j | \bar{M}[j] = 1, j = 1, 2, \dots, m\}$ .
2. Check whether the following equality holds:

$$e(\sigma_5, g) = pk_S \cdot e\left(u' \prod_{i \in \mathcal{U}_S} u_i, \sigma_4\right) e\left(v' \prod_{j \in \mathcal{M}} v_j, \sigma_2\right). \quad (1)$$

If no, output  $\perp$ ; otherwise, output  $M \leftarrow \sigma_1 \cdot \frac{e(\sigma_3, sk_{R,2})}{e(\sigma_2, sk_{R,1})}$ .

#### 4. Cryptanalysis of Liu et al.'s scheme

Liu et al. [15] claimed that their scheme is both semantically secure against adaptive chosen-ciphertext attacks and existentially unforgeable against adaptive chosen message attacks. However, in this section, we shall disprove their claims by giving two concrete attacks.

##### 4.1. Attack against semantic security

Liu et al. [15] claimed their scheme is semantically secure even in the strengthened model considering the malicious-but-passive KGC attack. Unfortunately, this is not true, since there exists a polynomial time Type II adversary  $\mathcal{A}_{II}$  who can always win game II as below:

1. In the initialization phase, adversary  $\mathcal{A}_{II}$  generates the master secret key  $msk$  and the system parameters  $params$  for challenger  $\mathcal{C}$ . In particular, adversary  $\mathcal{A}_{II}$  defines the parameters  $u', \vec{U} = (u_i)_n, v'$  and  $\vec{V} = (v_j)_m$  as below:

$$u' = g^{x'}, \quad u_1 = g^{x_1}, \dots, \quad u_n = g^{x_n}, \quad v' = g^{y'}, \quad v_1 = g^{y_1}, \dots, \quad v_m = g^{y_m},$$

where  $x', x_1, \dots, x_n, y', y_1, \dots, y_n \in_R \mathbb{Z}_p$  are chosen by adversary  $\mathcal{A}_{II}$ .

2. In phase 1, adversary  $\mathcal{A}_{II}$  needs not issue any query.
3. In the challenge phase,  $\mathcal{A}_{II}$  outputs two distinct identities  $\{u_{S'}, u_{R'}\}$  and two plaintexts  $\{M_0, M_1\} \in \mathbb{G}_T^2$ . Then,  $\mathcal{A}_{II}$  is given a challenge ciphertext  $\sigma^* = \text{Signcrypt}(params, M_\gamma, sk_{S'}, u_{S'}, pk_{S'}, u_{R'}, pk_{R'})$ , where  $\gamma$  is the random bit chosen by the challenger. Recall that  $\mathcal{A}_{II}$ 's goal is to correctly guess the value  $\gamma$ . Note that according to algorithm Signcrypt, the ciphertext  $\sigma^* = (\sigma_1^*, \sigma_2^*, \sigma_3^*, \sigma_4^*, \sigma_5^*)$  is of the following forms:

$$\sigma_1^* = M_\gamma \cdot e(g_1, g_2)^{x_{R'} \cdot r''}, \quad \sigma_2^* = g^{r''}, \quad \sigma_3^* = \left( u' \prod_{i \in \mathcal{U}_{R'}} u_i \right)^{r''},$$

$$\sigma_4^* = sk_{S',2}, \quad \sigma_5^* = sk_{S',1} \cdot \left( v' \prod_{j \in \mathcal{M}_\gamma} v_j \right)^{r''},$$

where  $\mathcal{U}_{R'} = \{i | u_{R'}[i] = 1, i = 1, \dots, n\}$ ,  $\mathcal{M}_\gamma = \{j | \bar{M}_\gamma[j] = 1, \dots, m\}$ , and  $\bar{M}_\gamma = H(\sigma_1^*, \sigma_2^*, \sigma_3^*, \sigma_4^*, u_{R'}, pk_{R'})$ .

4. In phase 2, adversary  $\mathcal{A}_{II}$  first randomly picks  $\hat{r} \in_R \mathbb{Z}_p$  and defines another ciphertext  $\sigma' = (\sigma'_1, \sigma'_2, \sigma'_3, \sigma'_4, \sigma'_5)$  with

$$\sigma'_1 = \sigma_1^* \cdot e(g_1, g_2)^{x_{R'} \cdot \hat{r}}, \quad \sigma'_2 = \sigma_2^* \cdot g^{\hat{r}}, \quad \sigma'_3 = \sigma_3^* \cdot \left( u' \prod_{i \in \mathcal{U}_{R'}} u_i \right)^{\hat{r}}, \quad \sigma'_4 = \sigma_4^*,$$

$$\sigma'_5 = \frac{\sigma_5^*}{(\sigma_2^*)^{y' + \sum_{j \in \mathcal{M}_\gamma} y_j}} \cdot (\sigma_2^*)^{y' + \sum_{j \in \mathcal{M}'_\gamma} y_j} \cdot \left( v' \prod_{j \in \mathcal{M}'_\gamma} v_j \right)^{\hat{r}},$$

where  $\mathcal{M}'_\gamma = \{j | \bar{M}'_\gamma[j] = 1, \dots, m\}$ ,  $\bar{M}'_\gamma = H(\sigma'_1, \sigma'_2, \sigma'_3, \sigma'_4, u_{R'}, pk_{R'})$ . Observe that  $\sigma' = (\sigma'_1, \sigma'_2, \sigma'_3, \sigma'_4, \sigma'_5)$  is indeed a valid ciphertext under the same message  $M_\gamma$ , the same sender with identity  $u_{S'}$  and public key  $pk_{S'} = e(g_1, g_2)^{x_{S'}}$ , and the same receiver with identity  $u_{R'}$  and public key  $pk_{R'} = e(g_1, g_2)^{x_{R'}}$ , since

$$\sigma'_1 = \sigma_1^* \cdot e(g_1, g_2)^{x_{R^*}^{\hat{r}}} = M_\gamma \cdot e(g_1, g_2)^{x_{R^*} \cdot (r'' + \hat{r})},$$

$$\sigma'_2 = \sigma_2^* \cdot g^{\hat{r}} = g^{r'' + \hat{r}},$$

$$\sigma'_3 = \sigma_3^* \cdot \left( u' \prod_{i \in \mathcal{U}_{R^*}} u_i \right)^{\hat{r}} = \left( u' \prod_{i \in \mathcal{U}_{R^*}} u_i \right)^{r'' + \hat{r}},$$

$$\sigma'_4 = \sigma_4^* = sk_{S^*, 2},$$

$$\begin{aligned} \sigma'_5 &= \frac{\sigma_5^*}{(\sigma_2^*)^{y' + \sum_{j \in \mathcal{M}'_\gamma} y_j}} \cdot (\sigma_2^*)^{y' + \sum_{j \in \mathcal{M}'_\gamma} y_j} \cdot \left( v' \prod_{j \in \mathcal{M}'_\gamma} v_j \right)^{\hat{r}} = \frac{sk_{S^*, 1} \cdot (v' \prod_{j \in \mathcal{M}'_\gamma} v_j)^{r''}}{(g^{r''})^{y' + \sum_{j \in \mathcal{M}'_\gamma} y_j}} \cdot (g^{r''})^{y' + \sum_{j \in \mathcal{M}'_\gamma} y_j} \cdot \left( v' \prod_{j \in \mathcal{M}'_\gamma} v_j \right)^{\hat{r}} \\ &= \frac{sk_{S^*, 1} \cdot (v' \prod_{j \in \mathcal{M}'_\gamma} v_j)^{r''}}{(g^{y' + \sum_{j \in \mathcal{M}'_\gamma} y_j})^{r''}} \cdot (g^{y' + \sum_{j \in \mathcal{M}'_\gamma} y_j})^{r''} \cdot \left( v' \prod_{j \in \mathcal{M}'_\gamma} v_j \right)^{\hat{r}} = \frac{sk_{S^*, 1} \cdot (v' \prod_{j \in \mathcal{M}'_\gamma} v_j)^{r''}}{(g^{y' \prod_{j \in \mathcal{M}'_\gamma} g^{y_j}})^{r''}} \cdot \left( g^{y' \prod_{j \in \mathcal{M}'_\gamma} g^{y_j}} \right)^{r''} \cdot \left( v' \prod_{j \in \mathcal{M}'_\gamma} v_j \right)^{\hat{r}} \\ &= \frac{sk_{S^*, 1} \cdot (v' \prod_{j \in \mathcal{M}'_\gamma} v_j)^{r''}}{(v' \prod_{j \in \mathcal{M}'_\gamma} v_j)^{r''}} \cdot \left( v' \prod_{j \in \mathcal{M}'_\gamma} v_j \right)^{r''} \cdot \left( v' \prod_{j \in \mathcal{M}'_\gamma} v_j \right)^{\hat{r}} = sk_{S^*, 1} \cdot \left( v' \prod_{j \in \mathcal{M}'_\gamma} v_j \right)^{r'' + \hat{r}}. \end{aligned}$$

Next, adversary  $\mathcal{A}_{II}$  issues an unsignryption query by submitting the ciphertext  $\sigma'$ , the sender with identity  $u_{S^*}$  and the receiver with identity  $u_{R^*}$ . Recall that according to the restrictions specified in game II, it is legal for  $\mathcal{A}_{II}$  to issue this query since  $\sigma' \neq \sigma^*$ . So, the challenger has to return the underlying message  $M_\gamma$  to  $\mathcal{A}_{II}$ . With  $M_\gamma$ , adversary  $\mathcal{A}_{II}$  can certainly know the value  $\gamma$ , and thus wins game II.

Therefore, Liu et al.'s scheme is not semantically secure against chosen-ciphertext attacks.

#### 4.2. Attack against existential unforgeability

In this subsection, we shall indicate that Liu et al.'s scheme is not existentially unforgeable against chosen message attacks. At a high level, the insecurity of Liu et al.'s scheme lies in the fact that, given a ciphertext generated by a sender, a Type II adversary can derive the sender's full private key, and hence can arbitrarily forge signcryption on behalf of this sender. Concretely, there exists a polynomial time Type II adversary  $\mathcal{A}_{II}$  who can always win game IV as below:

1. In the initialization phase, adversary  $\mathcal{A}_{II}$  generates the master secret key  $msk$  and the system parameters  $params$  for challenger  $\mathcal{C}$ . In particular, adversary  $\mathcal{A}_{II}$  defines the parameters  $v'$  and  $\vec{V} = (v_j)_m$  as below:

$$v' = g^{y'}, \quad v_1 = g^{y_1}, \dots, v_m = g^{y_m},$$

where  $y', y_1, \dots, y_m \in_R \mathbb{Z}_p$  are chosen by adversary  $\mathcal{A}_{II}$ .

2. In the queries phase, adversary  $\mathcal{A}_{II}$  issues a signcryption query by submitting a sender with identity  $u_{S^*}$ , a receiver with identity  $u_{R^*}$  and a message  $M$ . Then adversary  $\mathcal{A}_{II}$  is given a ciphertext  $\sigma = \text{Signcrypt}(params, M, sk_{S^*}, u_{S^*}, pk_{S^*}, u_{R^*}, pk_{R^*})$ . Note that according to algorithm  $\text{Signcrypt}$ , the ciphertext  $\sigma = (\sigma_1, \sigma_2, \sigma_3, \sigma_4, \sigma_5)$  is of the following forms:

$$\sigma_1 = M \cdot e(g_1, g_2)^{x_{R^*} r''}, \quad \sigma_2 = g^{r''}, \quad \sigma_3 = \left( u' \prod_{i \in \mathcal{U}_{R^*}} u_i \right)^{r''},$$

$$\sigma_4 = sk_{S^*, 2}, \quad \sigma_5 = sk_{S^*, 1} \cdot \left( v' \prod_{j \in \mathcal{M}} v_j \right)^{r''},$$

where  $\mathcal{U}_{R^*} = \{i | u_{R^*}[i] = 1, i = 1, \dots, n\}$ ,  $\mathcal{M}_{\vec{v}} = \{j | \vec{M}[j] = 1, \dots, m\}$ , and  $\vec{M} = H(\sigma_1, \sigma_2, \sigma_3, \sigma_4, u_{R^*}, pk_{R^*})$ .

From  $\sigma_2 = g^{r''}$  and  $\sigma_5 = sk_{S^*, 1} \cdot (v' \prod_{j \in \mathcal{M}} v_j)^{r''}$ , adversary  $\mathcal{A}_{II}$  can derive the sender's private key component  $sk_{S^*, 1}$  by computing  $\frac{\sigma_5}{\sigma_2^{y' + \sum_{j \in \mathcal{M}} y_j}}$ , since

$$\frac{\sigma_5}{\sigma_2^{y' + \sum_{j \in \mathcal{M}} y_j}} = \frac{sk_{S^*, 1} \cdot (v' \prod_{j \in \mathcal{M}} v_j)^{r''}}{(g^{r''})^{y' + \sum_{j \in \mathcal{M}} y_j}} = \frac{sk_{S^*, 1} \cdot \left( v' \prod_{j \in \mathcal{M}} v_j \right)^{r''}}{(g^{y' + \sum_{j \in \mathcal{M}} y_j})^{r''}} = \frac{sk_{S^*, 1} \cdot (v' \prod_{j \in \mathcal{M}} v_j)^{r''}}{(g^{y' \prod_{j \in \mathcal{M}} g^{y_j}})^{r''}} = \frac{sk_{S^*, 1} \cdot (v' \prod_{j \in \mathcal{M}} v_j)^{r''}}{(v' \prod_{j \in \mathcal{M}} v_j)^{r''}} = sk_{S^*, 1}.$$

Recall that  $\sigma_4 = sk_{S^*, 2}$ . So adversary  $\mathcal{A}_{II}$  knows the sender's full private key  $sk_{S^*} = (sk_{S^*, 1}, sk_{S^*, 2})$ . With  $sk_{S^*}$ , adversary  $\mathcal{A}_{II}$  can certainly forge signcryption on behalf of this sender, and thus can always win game IV.

Therefore, Liu et al.'s scheme is not existential unforgeable against chosen-message attacks.

## 5. Conclusion

In this paper, we indicated that Liu et al.'s certificateless signcryption scheme [15] is neither semantically secure against chosen ciphertext attacks nor existentially unforgeable against chosen message attacks. We demonstrated this by giving concrete attacks according to their security model.

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