Diffusive Motion in Stage-1 and Stage-2 Li-Graphite Intercalation Compounds: Results of β-NMR and Quasielastic Neutron Scattering

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Dedicated to Professor Werner Müller-Warmuth on the occasion of his 65th birthday

Investigations of Li diffusion in stage-1 and stage-2 Li graphite intercalation compounds with neutron time-of-flight and backscattering techniques and β-radiation detected nuclear magnetic resonance/relaxation (β-NMR) with the nucleus ^{8}Li ($T_{1/2} = 0.8$ s) are reviewed and compared. Depending on temperature, the spin-lattice relaxation-rate T_1^{-1} of ^{8}Li is governed by different processes. Above 300 K, $T_1^{-1}(T)$ shows maxima induced by long-range Li$^+$ diffusion. Jump correlation times are estimated. Inspection of the B field dependence of T_1^{-1} revealed two-dimensional diffusion behaviour. The neutron spectra showed a quasielastic line broadening above 500 K, which was used to obtain diffusion coefficients and to trace jump vectors of the in-plane motion. The diffusion parameters observed with both techniques are compared, and differences that show up are discussed. In addition, the low-temperature spin-lattice relaxation rates, being due to coupling to conduction electrons, are used to explore electronic properties.

1. Introduction

The large variety of structures resulting from donor and acceptor insertion makes graphite intercalation compounds (GICs) one of the most extensively studied family of guest-host materials. Many properties of practical and theoretical interest, such as electronic transport and structure, ionic motion, magnetic structure and lattice dynamics, may be tailored by inserting appropriate guest species (the intercalate) into more or less well defined sites between the host layers. Additional variation derives from staging, i.e. the occupation of a periodic subset of the planes between the graphite layers. The number of graphite planes between the guest layers denotes the stage of the compound.

These features have stimulated a large part of the research activity dealing with GICs as model systems for studies of phase transitions, magnetism, electronic transport, ion dynamics etc. in two-dimensional (2D) systems, and comprehensive reviews are available now [1, 2].

Alkali-GICs are of particular interest since they provide simple guest species and exhibit nevertheless a variety of in-plane structures. These range from commensurate long-range ordered ones with every guest site occupied, to discommensurate and dilute high-stage compounds.

The Li-GICs are a peculiar system due to the existence of the ordered stage-1 and stage-2 compounds, LiC$_6$ and LiC$_{12}$ respectively, which differ only in the additional C-layer in the stage-2 compound. In both cases the Li atoms form a 2D hexagonal $(\sqrt{3} \times \sqrt{3})$ R 30° superstructure with direct registry, i.e. the Li atoms sit directly above each other. Comparison of LiC$_6$ and LiC$_{12}$ thus offers the possibility to study phenomena for different interlayer coupling; a difference in in-plane Li density has not to be considered. It should also be mentioned that Li$_x$C$_6$ compounds are used as anode materials for rechargeable Li-ion batteries [3].

The main issue addressed in this contribution is the diffusive motion of Li and its dimensionality. Considering the small size of the Li ion it has been argued that diffusion jumps across the graphene sheets cannot be ruled out a priori as in the case of the heavy alkalis [4]. The direct registry of the carbon layers would provide such a diffusion path through the hexagon centres. Here the investigation and comparison of the stage-1 and stage-2 compounds is related to the question whether such a deviation from pure 2D

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diffusion, which should be more pronounced in the former, can be traced. Identical in-plane structures are therefore essential.

A further peculiarity of the Li-GICs is the existence of two distinct stage-2 phases: besides the ordered compound LiC_{12}, which transforms above about 500 K to stage-1 with no long-range in-plane order [5], there exists a dilute compound, labeled LiC_{16}, which has no long-range order already at room temperature [5, 6]. The stage-2 compounds thus offer the possibility to examine the role of in plane ordering in diffusion. Concerning the stage-1 compound, the superstructure of LiC_6 disappears at 715 K [7, 8], thus exhibiting a disordered phase too, however in a restricted temperature range due to formation of lithium carbide above 750 K.

The spectroscopic tools used for the investigations reviewed here are spin-lattice relaxation (SLR) and quasielastic neutron scattering (QENS). The former are performed with the method of β-radiation detected NMR (β-NMR) with the probe nucleus $^8Li(T_{1/2}=0.8$ s) on LiC_6 and LiC_{12}. For the stage-2 compounds LiC_{12} and LiC_{16} neutron scattering data were obtained with time-of-flight (TOF) and backscattering (BS) spectrometers; data for the stage-1 compound LiC_6 were taken from the literature for comparison. Both, neutron-scattering and β-NMR data, are used for the investigation of diffusive Li motion, and the combination of them allows to cover a wide range of jump frequencies. Furthermore the SLR results give access to electronic properties of the materials.

The paper is organised as follows. In the next chapter the samples, the spectrometers, and the techniques employed are briefly described. Then the results for each part, β-NMR and neutron scattering, are shown and discussed separately. In the last section the data concerning the diffusive behaviour of Li will be compiled and discussed.

2. Experimental

2.1 Samples

All samples were prepared from highly oriented pyrolytic graphite (HOPG) and isotopically pure ^7Li metal in order to avoid parasitic neutron absorption by ^6Li in both, the β-NMR and the neutron-scattering experiments. The samples were characterized by neutron diffraction for stage purity and c-axis mosaic spread. The stage-2 admixture of the LiC_6 samples was smaller than 3%, for the stage-2 samples a stage-1 admixture below 10^{-4} was achieved. The c-axis mosaic spread was about 8° full width at half maximum for all samples. The LiC_{12} samples used in the β-NMR investigation had a 15% admixture of the dilute stage-2 phase LiC_{16}. The stage-1 samples were prepared at the Materials Research Laboratory, University of Illinois at Urbana, the stage-2 samples were provided by the Laboratory for Research of the Structure of Matter, University of Pennsylvania at Philadelphia.

2.2 β-Radiation Detected NMR

The versatility of nuclear magnetic resonance/relaxation techniques for the investigation of both, structural and dynamic properties of intercalation compounds has been shown in, e.g., [9]. In this contribution β-radiation detected nuclear magnetic resonance/relaxation is used for the investigation of diffusion processes. Although comprehensive reviews on the β-NMR technique [10] and its application to the study of ion dynamics [11] are available, the method will briefly be described and its special features for the study of GICs will be discussed. In β-radiation detected NMR the β-radiation asymmetry of short-lived β-emitters in a sample is used to measure the nuclear polarization. Any changes of the nuclear polarization are observed via changes of the β-asymmetry.

The measurement proceeds in two steps: (*i*) generation of the short-lived radioactive nuclei in the sample and (*ii*) observation of the β-radiation asymmetry. Here for (*i*) the capture of polarized thermal or cold neutrons by ^7Li nuclei in the sample is used. The observation of the β-radiation asymmetry is performed in a time-differential mode after neutron-activation pulses or under quasi-continuous activation condition by chopping the neutron beam fast compared to the β-lifetime. In the time-differential mode the decay behaviour of the nuclear polarization is observed directly, and the spin-lattice relaxation time T_1 can be obtained. Under quasi-continuous activation conditions resonance signals can be recorded.

Special features of the β-NMR technique for SLR measurements in GICs are the following. Since the nuclear polarization is created in a nuclear reaction, no Boltzmann factor is involved. Low values of the external $\boldsymbol{B}$ field are easily accessible. Further, the

probe spins are extremely diluted and may be regarded as isolated spins with no spin temperature established. Mutual spin flips are suppressed, and the probes relax independently. Relaxation due to paramagnetic impurities does not contribute. Since the measurement of the SLR time does not require any radiofrequency irradiation, skin effect problems with the samples showing metallic conductivity do not arise. So metal single crystals can be used.

A limitation of the β-NMR method is the time window of accessible SLR times T_1 to the approximate range $0.1\,T_{1/2} \leq T_1 \leq 10\,T_{1/2}$ around the nuclear half life $T_{1/2}$ of the probe nucleus. Furthermore, large samples of several cm³ are necessary in order to achieve sufficiently high count rates in the neutron activation experiment, a problem also encountered in the neutron scattering measurements.

The measurements were performed with the in-beam β-NMR spectrometer S6 [10, 11] at a thermal neutron guide of the high-flux reactor of the ILL Grenoble on LiC₆, and with the β-NMR spectrometer at the DIDO reactor of the KFA Jülich [12] on the LiC₁₂ sample. The cold neutron beam available at the latter compensates for the lower reactor power, yielding roughly the same measuring conditions.

2.3 Quasielastic Neutron Scattering

The neutron backscattering and the time-of-flight measurements on the stage-2 compounds were performed with the IN10 and the IN6 spectrometers of the ILL. The scattering plane was always chosen perpendicular to the c-axis, thus probing in-plane diffusive motion. In both cases the momentum transfers Q covered the range $Q = 3\,\mathrm{nm}^{-1} \ldots 20\,\mathrm{nm}^{-1}$, and the energy resolution was about 1 µeV for the BS and 70 µeV for the TOF measurements.

In both, the BS and the TOF spectra, the quantity of interest here is the broadening of the elastic line of the incoherent scattering function $S_{\mathrm{inc}}(Q,\omega)$ due to translational diffusion of the scatterer. With the usual approximations [13] the incoherent scattering functions reads

$$S_{\mathrm{inc}}(Q,\omega) = \frac{1}{\pi}\frac{\Gamma}{\Gamma^2+\omega^2}. \qquad (1)$$

For liquidlike diffusion of the scatterer with the diffusion constant D, the width Γ is given by

$$\Gamma = 2\hbar D Q^2. \qquad (2)$$

For jumplike particle motion the width depends on the mean residence time τ_c between jumps

$$\Gamma = \frac{2\hbar}{\tau_c}f(Q), \qquad (3)$$

where $f(Q)$ is a model dependent geometric function given by

$$f(Q) = \frac{1}{n}\sum_{i=1}^{n}[1-\exp(-i\,Q\cdot l_i)]. \qquad (4)$$

The sum is taken over all possible neighbour sites of the particle accessible with a jump vector l_i. Thus inspection of $\Gamma(Q)$ offers, unlike the SLR measurements, direct access to the geometry of the diffusion process.

3. Results and Discussion

3.1 Spin-Lattice Relaxation of ^8Li

3.1.1 Overview

For the stage-2 compound LiC₁₂ the transients of the β-radiation asymmetry showed single-exponential decay behaviour in the entire range of temperatures and of B-field values for both crystal orientations $B\parallel c$ and $B\perp c$. For LiC₆ the same observation was made except in a T range below 300 K, which will be discussed below. Figure 1 gives an overview of $T_1^{-1}(T)$ of ^{8}Li in LiC₁₂ for the two crystal orientations and a single B value. Four regions of different T-dependences may be distinguished: (i) For $T < 100$ K T_1^{-1} shows a linear T dependence and is independent of B and the crystal orientation. The high-temperature extrapolation of this SLR process is indicated by the dotted line in Figure 1. (ii) For $100\,\mathrm{K} < T < 300\,\mathrm{K}$ T_1^{-1} is still independent of the crystal orientation and exceeds the linear T dependence extrapolated from lower temperatures. (iii) For $300\,\mathrm{K} < T < 500\,\mathrm{K}$ T_1^{-1} shows a steep increase and a maximum induced by Li diffusion. The rate depends on the value of B as well as the crystal orientation, as illustrated in Figure 2. (iv) for $T > 500$ K T_1^{-1} does not reduce to the high-T extrapolation of the SLR process observed in the low-T region. Thus a further T_1^{-1} contribution becomes dominant above about 500 K. For the stage-1 compound a similar diffusion induced rate maximum between about 300 K and 500 K, induced by Li diffusion, and an additional SLR process arising above
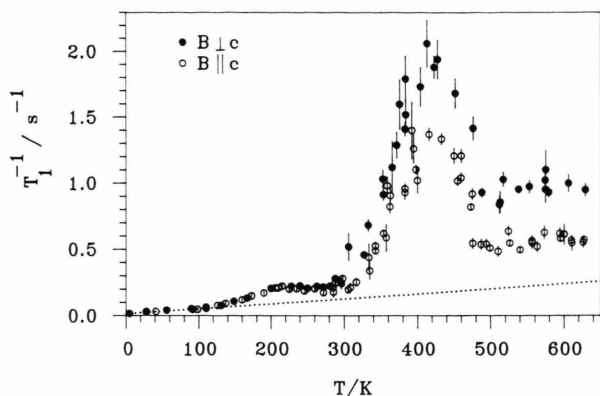
Fig. 1. T dependence of T_1^{-1} of ^{8}Li in LiC$_{12}$ for $B = 37$ mT and two crystal orientations. The dotted line marks the SLR contribution due to coupling to conduction electrons showing up as a background at higher temperatures.
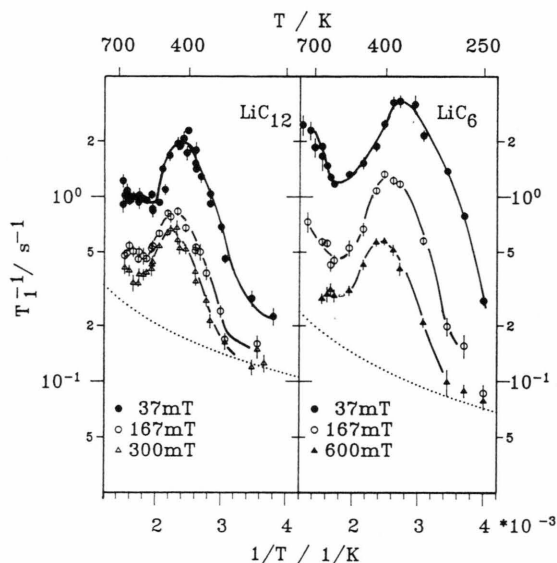

Fig. 2. SLR rate T_1^{-1} of ^{8}Li in LiC$_{12}$ (left) and LiC$_6$ (right) at various B for $B \perp c$. The solid lines are a guide to the eye, the dotted line for LiC$_{12}$ is the high-T extrapolation of the electronic SLR contribution observed below 100 K. The dotted line for LiC$_6$ is the background rate according to $T_{1b}T = 3500$ sK.

500 K similar to the T_1^{-1} behaviour in (iv) showed up [14]. The discussion will mainly be concerned with the long-range Li diffusion dominating T_1^{-1} in region (iii).

3.1.2 Spin-Lattice Relaxation Below 300 K

Since SLR processes being dominant in the T ranges (i) and (ii) might also contribute in the T range

(iii) of the pronounced peak, a short description with emphasis on LiC$_{12}$, which was studied more extensively, will be given here. A more detailed discussion is presented in [15].

The linearly T dependent SLR contribution below 100 K is due to coupling of the ^{8}Li probe spins to conduction electrons. For this contribution the Korringa relation

$$T_1 T K^2 \eta = \frac{\hbar}{4\pi k_B}\left(\frac{\gamma_e}{\gamma_n}\right)^2 = S_0 \tag{5}$$

holds, where γ_e and γ_n are the gyromagnetic ratio of the electron and the probe nucleus, respectively. K denotes the Knight shift. The Korringa-enhancement factor η accounts for deviations of the system from free-electron behaviour. Values $\eta < 1$ usually found in metals are due to electron-electron interaction, values $\eta > 1$ may be ascribed to ion-electron interaction, and values $\eta \gg 1$ are found in low-D electronic systems [16]. Combination of the $T_1 T$ value of ^{8}Li with the Knight shift of ^{7}Li obtained at room temperature for the same LiC$_{12}$ sample [17] yields $\eta \simeq 3.5$. The earlier estimate $\eta \simeq 2$ [15] stems from a higher Knight shift value of a powder sample given in the literature [18] and might be an underestimate. The spread of the η values does, however, not affect the conclusion of a low-D electronic character of LiC$_{12}$.

For the stage-1 compound LiC$_6$, SLR data for T below 100 K are too scarce for a detailed comparison. In the high-T region the SLR contribution due to coupling to conduction electrons does contribute to the experimental T_1^{-1} value in LiC$_6$ as a background rate T_{1b}^{-1} in a similar way as illustrated in Figure 1. In LiC$_6$ the temperature dependence of T_{1b}^{-1} was estimated as $T_{1b}T \approx 3500$ sK [14], in LiC$_{12}$ the T dependent part of the background contribution is described by $T_{1b}T \approx 2600$ sK.

Between 100 K and 300 K SLR contribution in addition to the conduction-electron induced SLR shows up in LiC$_{12}$ as illustrated in Figure 1. The semilogarithmic plot of this additional rate vs. $1/T$ exhibits a linear increase above 100 K and a maximum near 200 K, which both are characteristic of motion induced SLR. The slope on the low-T side of this secondary peak corresponds to an activation energy of about 50 meV. The additional SLR contribution shows a weak B dependence which can be approximated by a power law $B^{-0.5}$. This is weaker than the B^{-2} dependence predicted by the standard model for motion induced SLR by Bloembergen et al. (BPP) [19].

Consequently, the value given for the activation energy is only a lower estimate. It should be noted that similar weak B dependences of the SLR rate were found with ^{7}Li NMR in crystalline β-LiAlSi$_2$O$_6$, which is a Li-ion conductor too [20].

In LiC$_6$ a nonexponential behaviour of the β-asymmetry transients of ^{8}Li for T between 100 K and 270 K was observed which can be described by a double exponential decay law with time constants $T_1^{(1)}$ and $T_1^{(2)}$ ($T_1^{(1)} < T_1^{(2)}$). The B dependence of both, $1/T_1^{(1)}$ and $1/T_1^{(2)}$, is weaker than $\propto B^{-2}$. The T dependence of the SLR rate corresponding to the shorter decay time constant $T_1^{(1)}$ exhibits a peak. From the slope of the low-T side of the peak, in the $\log(1/T_1^{(1)})$ vs. $1/T$ representation an activation energy of 75 meV is estimated, which is as in the case of LiC$_{12}$ only a lower limit.

The mechanisms, whether dipolar or quadrupolar, and consequently the origin of the SLR processes arising additionally to the electron contribution in both, LiC$_6$ and LiC$_{12}$, are not clear. A comparison with ^{7}Li NMR data for LiC$_6$ [21] is hampered by the different B dependences found. Lauginie et al. [21] report a T_1^{-1} value of ^{6}Li at 200 K which is consistent with the conduction-electron induced SLR contribution of ^{8}Li. Due to the small quadrupole moment of ^{6}Li this is a hint that the additional SLR process observed for ^{8}Li in LiC$_6$ is quadrupolar. It might be related to a suggested phase transition at about 200 K ([22] and references therein). In the LiC$_{12}$ sample the SLR behaviour might be influenced by the known phase transition at $T = 248$ K [23] in the minority LiC$_{16}$ phase. The relatively low abundance of the latter, together with a possible translational Li motion during the lifetime of the ^{8}Li probe might effect an averaging over inequivalent probe surroundings and prevent a nonexponential decay of the β-asymmetry of ^{8}Li in the stage-2 sample.

3.1.3 Spin-Lattice Relaxation Above 300 K

In both, LiC$_6$ and LiC$_{12}$, the SLR rate increases drastically with T above 300 K and shows a diffusion-induced rate maximum as illustrated in Fig. 2 in the usual $\log(T_1^{-1})$ vs. $1/T$ representation for the orientation $\boldsymbol{B} \perp \boldsymbol{c}$. For the orientation $\boldsymbol{B} \parallel \boldsymbol{c}$ similar $T_1^{-1}(T)$ peaks are observed. In both compounds the SLR due to coupling to conduction electrons contributes to the observed SLR rate in the T range of the diffusion induced rate maximum and is treated as a background
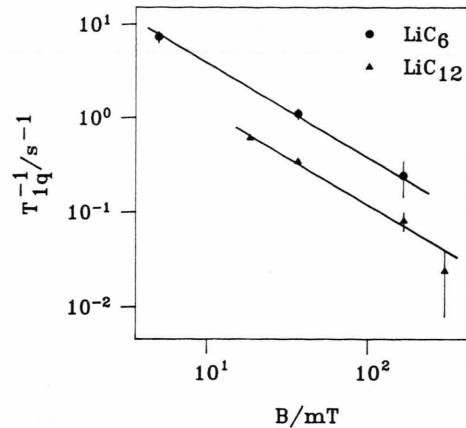

Fig. 3. The SLR contribution T_{1q}^{-1} to the SLR rate of ^{8}Li in LiC$_6$ ($T = 600$ K) and LiC$_{12}$ ($T = 595$ K) as a function of the B field for $\boldsymbol{B} \perp \boldsymbol{c}$ in double-logarithmic representation. The lines represent a B^{-1} dependence.

rate T_{1b}^{-1}. It is given by the dotted lines in Fig. 2 and has to be subtracted from the experimental T_1^{-1} values in order to obtain the diffusion-induced rate T_{1d}^{-1} which will be discussed further.

In the T range (iv) above the high-T side of the rate peaks, T_1^{-1} does not decrease to T_{1b}^{-1} for LiC$_6$ and LiC$_{12}$. A further SLR contribution denoted as T_{1q}^{-1} shows up. It is larger in the stage-1 compound and anisotropic with $(T_{1q}^{-1})_{\boldsymbol{B} \perp \boldsymbol{c}} > (T_{1q}^{-1})_{\boldsymbol{B} \parallel \boldsymbol{c}}$. The anisotropy is larger for LiC$_6$. T_{1q}^{-1} is B dependent as illustrated by Figure 3. The B dependence follows a $T_{1q}^{-1} \propto B^{-1}$ law in LiC$_6$ and LiC$_{12}$. The large anisotropy suggests quadrupolar coupling [24, 25]. The origin of a quadrupolar SLR mechanism is, however, not entirely clear. At the elevated temperatures both compounds contain vacancies in high concentration, and multiple-vacancy diffusion with correlation times larger than those of the low-T phase might be possible.

The high-T SLR behaviour in the Li GICs is qualitatively similar to that in Li intercalated hexagonal TiS$_2$ investigated with ^{7}Li-NMR [26]. A diffusion induced rate maximum and an additional high-T SLR process were observed there, too.

Returning to the diffusion induced rate maxima in LiC$_6$ and LiC$_{12}$, which have been described singly in [14] and [27], the discussion here will concentrate on the comparison of the compounds. For both, the B dependence of the SLR rate showed deviations from the behaviour predicted by standard models for motion induced SLR. On the low-T side of the peak and at the peaks themselves the B dependences were

weaker. On the the high-T side a dispersion of the SLR rate with B was found. Its inspection turned out to be indispensable to elucidate the role of low-D diffusion.

3.1.4 Diffusion Induced Spin-Lattice Relaxation

The evaluation of diffusion parameters from SLR data is achieved by invoking spectral density functions $J(\omega)$ which are the Fourier transforms of the correlation functions $G(\tau)$ describing the motional process. The diffusion induced SLR of ^{8}Li in the temperature range (iii) is caused by fluctuations of the dipole-dipole interaction. Evidence for the relaxation mechanism being dipolar comes from the B dependence on the high-T side of the rate maximum, which is a feature of low-D diffusion. For the case that the diffusion jump rate τ_c^{-1} is large in comparison with the Larmor frequency ω_0 ($\omega_0 \tau_c \ll 1$), which is fulfilled on the high-T side, only in the expression for dipolar SLR spectral density functions with an ω dependence do occur [14, 25]. Further support for a dipolar mechanism comes from a calculation of the lattice sums which determine the peak T_{1d}^{-1} value for dipolar coupling [28]. For both, the ratio of the $(T_{1d}^{-1})_{max}$ values of LiC$_6$ and LiC$_{12}$ and the anisotropy of $(T_{1d}^{-1})_{max}$ for $B \parallel c$ and $B \perp c$, the calculations agree with the experimental values.

The usual way to obtain diffusion parameters from the T_{1d}^{-1} data by fitting spectral density functions $J(\omega)$ from standard models is hampered by the weak $\omega_0 (\hat{=} B)$ dependence on the low-T side of the rate maximum. Here $\omega_0 \tau_c \gg 1$ holds, and the short time behaviour ($\tau \ll \tau_c$) of $G(\tau)$ is probed. The deviation of $G(\tau)$ from single exponential decay behaviour, which is reflected by the ω dependence being weaker than ω^{-2}, can be characterized by a constant $0 < \alpha < 1$ in $G(\tau \ll \tau_c) \propto \exp[-(\tau/\tau_c)^{1-\alpha}]$ [29, 30]. This is equivalent to a modified spectral density function

$$J(\omega) \propto \tau_c (\omega \tau_c)^{-2+\alpha} \quad . \tag{6}$$

The temperature dependence of the characteristic time for motional processes is given by

$$\tau_c = \tau_{c0} \exp[E_A/kT] \tag{7}$$

where E_A is the activation energy. With α determined by the ω dependence, E_A values can be estimated. The low-T side of the $\log(T_{1d}^{-1})$ vs. $1/T$ plots yields 0.6(2) eV for LiC$_6$ and 1.0(3) eV for LiC$_{12}$.

These estimates are supported by the inspection of the SLR-rate maxima. The temperature T_{max} where T_{1d}^{-1} attains its maximum shifts with rising Larmor frequencies to higher temperatures. This shift may be used for another estimate of the activation energy. Regardless of the microscopic details of the diffusion jump mechanism, the spectral density function $J(\omega)$ attains its maximum for $\omega_0 \simeq \tau_c^{-1}$. The shift of T_{max} yields $E_A \approx 0.7$ eV for LiC$_6$ and $E_A \approx 0.9$ eV for LiC$_{12}$. The τ_c values obtained in this way are discussed in Section 3.3. Contrary to E_A the estimate of τ_c values is subjected to a common systematic error, since the exact value of $\omega_0 \tau_c$ at the rate maximum is not known in the present case of non-BPP behaviour.

The observed nonexponential correlation functions are a common feature of superionic conductors [30]. In computer simulations [31] the important role of structural disorder and Coulomb interactions for the deviation of the SLR behaviour from the standard model for diffusion induced SLR was shown. However, in the present case the origin of the observed nonexponential correlation functions is not clear. Inspection of the phonon density of states of LiC$_6$ reveals a strong screening of the Coulomb interaction in comparison with heavy alkali GICs [32], where the Coulombic-force model without screening was more appropriate for the description of the phonon density of states. Further, the compounds investigated here should be well ordered in the discussed T range with the admixture of disordered phases being low. In the frame of the Daumas-Hérold model of small ordered domains [33], disorder effects on diffusion induced SLR might, however, be conceived in case that the diffusion length within a time of the order of T_{1d} exceeds the supposed size of 2 D intercalate "islands".

At temperatures above the rate maximum the condition $\omega_0 \tau_c \ll 1$ holds and the long-time behaviour of $G(\tau \gg \tau_c)$ is probed. The standard model predicts for the spectral density $J \propto \tau_c$ with J independent of ω, which is at variance with the data. Figure 4 shows examples of the B dependence observed in LiC$_6$ and LiC$_{12}$ on the high-T side of the maximum.

Theoretical calculations for a 2 D diffusion process yield for the case $\omega \tau_c \ll 1$ the expression [24]

$$J(\omega \ll \tau_c^{-1}) \propto \tau_c \ln \frac{1}{\omega \tau_c} . \tag{8}$$

Figure 4 is a plot of $T_{1d}^{-1}(B)$ with a logarithmic B scale. The data for both compounds are in accordance with a 2 D process. It should be noted that the calculation
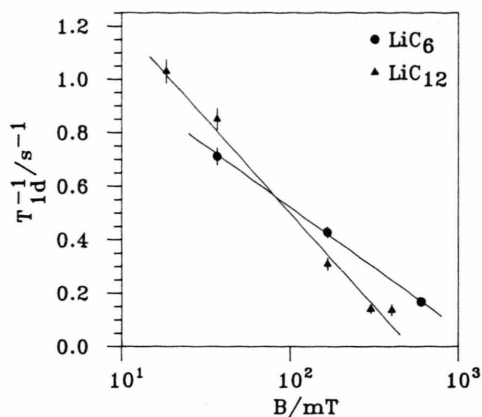
Fig. 4. T_{1d}^{-1} of ^{8}Li in LiC_6 ($T=462$ K, $\boldsymbol{B}\parallel c$) and LiC_{12} ($T=460$ K, $\boldsymbol{B}\parallel c$) as a function of the B field (on logarithmic scale) at temperatures on the high-T side of the rate maximum. The solid lines are fits with (8).

of T_{1d}^{-1} from the experimental T_1^{-1} values involves the subtraction of the SLR contribution due to coupling to electrons denoted as T_{1b}^{-1} as well as a contribution from the high-T SLR process T_{1q}^{-1} at the respective temperature and B value. The procedure is subjected to the uncertainty of this extrapolation, since the origin of T_{1q}^{-1} is unclear. Without this latter correction, intriguingly the data for LiC_6 turned out to be compatible with the $\omega^{-1/2}$ law predicted for 1 D diffusion [14, 22]. As things are, however, the SLR results for LiC_6 as well as for LiC_{12} strongly support the conjecture of 2 D diffusion of the Li ions in their planes between graphite layers, and the logarithmic B dependence of T_{1d}^{-1} was used to obtain values for τ_c according to (8). These will be discussed in Section 3.3.

3.2 Quasielastic Line Broadening of $S_{inc}(Q,\omega)$

In this section neutron time-of-flight and backscattering measurements on the stage-2 Li-GICs LiC_{12} and LiC_{16} will be used for the study of the diffusional Li in-plane motion. For comparison with the stage-1 compound comprehensive reviews on neutron scattering investigations on LiC_6 are available [1, 13].

In backscattering measurements on LiC_{12} no broadening of the quasielastic line was observed but a decrease of the elastic intensity I integrated over the instrumental resolution as the temperature was raised from $T=50$ K to $T>600$ K [34]. The elastic intensity in these fixed-window scans decreases due to the re-

duction of the Debye-Waller factor and the onset of motional processes in the frequency window of the instrumental resolution. In the fixed-window scans of LiC_{12} and LiC_{16} the former results in a weak decrease with T already at low temperatures. Reduction of I due to diffusion is more pronounced and occurs above about 300 K. Thus for LiC_{12} the fixed-window scans give access only to the diffusion process observed by SLR above 300 K. Motional processes between 100 K and 300 K, being discussed in Subsection 3.1.2, are not reflected in decreases of I in the neutron spectra at the same temperatures. Considering the low frequencies of the β-NMR measurements (in the region of 10^6 Hz) and the low activation energies estimated, a signal in the fixed-window measurements (in the 10^9 Hz region) is expected above 350 K, i.e. in the T range where long-range Li diffusion becomes effective.

For the compound LiC_{16}, having no long-range Li order, a quasielastic line broadening showed up in the backscattering spectra. The elastic intensity is evaluated with the usual procedure of convoluting a Lorentzian and a δ function with the instrumental resolution function. The linewidth $\Gamma(Q)$ thus obtained is plotted in the upper part of Figure 5. For the further treatment of $\Gamma(Q)$ in terms of an in-plane jump diffu-
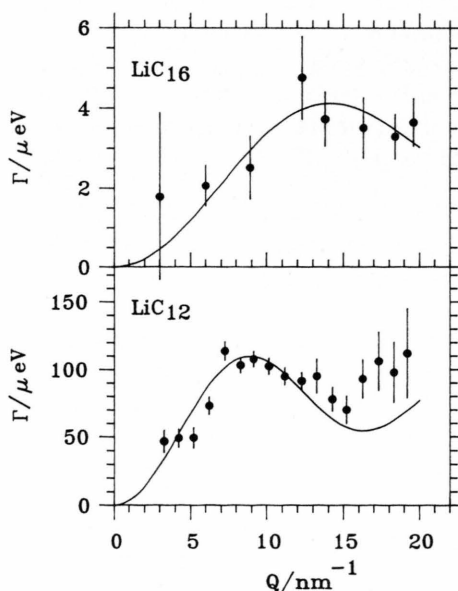

Fig. 5. Linewidths of the quasielastic neutron backscattering and time-of-flight spectra for LiC_{16} ($T=450$ K) and LiC_{12} ($T=650$ K) as functions of the wave vector Q. The solid lines are fits with (9).

sion process according to (4), a proper 2 D average has to be performed in order to account for the orientational randomness of the a or b axes of the crystallites of the HOPG. It yields

$$\Gamma(Q) = \frac{2\hbar}{\tau_c}(1 - J_0(Q\,l)), \qquad (9)$$

where J_0 is the zeroth order Bessel function; τ_c and l are the jump correlation time and the jump length, respectively. The solid line through the data for LiC_{16} in Fig. 5 is a fit with (9) yielding τ_c and l.

The observation of a diffusion induced reduction of the fixed window intensity but of no quasielastic broadening in the case of LiC_{12} is due to the narrow dynamic range of the backscattering spectrometer. This was circumvented by measuring with a time-of-flight spectrometer with a poorer energy resolution but a larger energy range. Quasielastic line broadening data for $T = 650$ K are shown in the lower part of Figure 5. Only for this T a maximum in $\Gamma(Q)$ was observed, allowing the determination of τ_c as well as l. At lower T, maxima in $\Gamma(Q)$ could not be resolved due to the limited statistic accuracy. A $\Gamma \propto Q^2$ behaviour for the low Q range in accordance with (2) was observed and used for the evaluation of diffusion coefficients (see Section 3.3). For LiC_6 and LiC_{12} the measured values for l are close to the distance 0.426 nm of next-nearest neighbour sites in the $(\sqrt{3} \times \sqrt{3}) R 30°$ superstructure [35]. For LiC_{16} l close to the in-plane distance 0.25 nm of hexagon centres, i.e. the distance from a Li site to the site in the centre between adjacent carbon hexagons [34].

3.3 Diffusivity in Stage-1 and Stage-2

In this section, diffusion parameters obtained by the β-NMR and the neutron scattering techniques are summarized. The diffusion coefficients D were obtained directly by fitting (2) to the quasielastic linewidth data when no maximum in $\Gamma(Q)$ was resolved. For the LiC_{16} data and the highest temperature run for LiC_{12}, (9) was fitted to the $\Gamma(Q)$ values, and the diffusion coefficient was calculated from τ_c and l according to the expression for 2 D diffusion
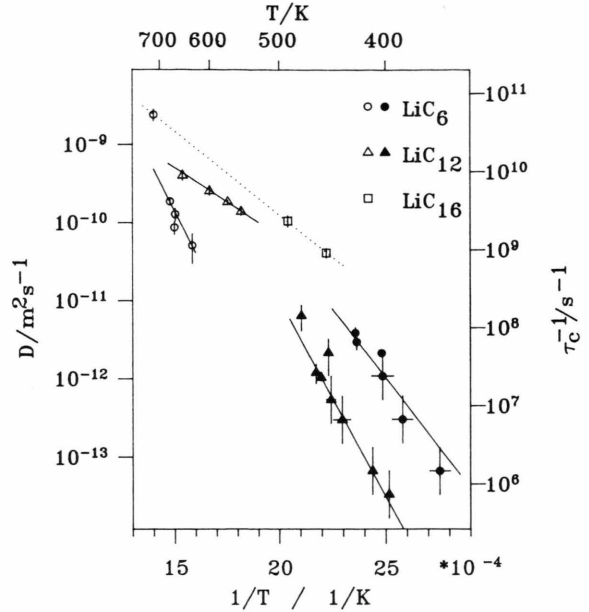
$$D = \frac{l^2}{4\tau_c}. \qquad (10)$$

Fig. 6. Synoptic representation of the temperature dependence of the diffusion coefficient (left-hand ordinate) and jump rate (right-hand ordinate) for the in-plane Li diffusion in various Li-GICs obtained with quasielastic neutron scattering (open symbols) and β-NMR (full symbols). Horizontal error bars refer to the uncertainty of the temperature determination were SLR rate maxima occur, vertical error bars account for the uncertainty of the value of $\omega_0 \tau_c$ at the rate maxima. The QENS data for LiC_6 were taken from [35]. The solid lines correspond to activation energies given in the text. The dotted line corresponds to a common activation energy for LiC_{16} and the disordered phase of LiC_6.

The jump length in LiC_{12} is $l = 0.48(2)$ nm. For LiC_6 a compatible value for l was observed [35], for LiC_{16} the mean value $l = 0.276(14)$ nm was found.

The diffusion coefficients are shown in Fig. 6 together with the jump-correlation rates τ_c^{-1} for LiC_6 and LiC_{12} obtained by the β-NMR measurements. The shift of the scales for D and τ_c^{-1} corresponds to an in-plane jump-distance equal to the next-nearest hexagon centres in (10). This implies that the same 2 D in-plane diffusion mechanism are seen in the QENS and β-NMR measurements. For LiC_6 this scaling results in a discontinuity of the extrapolation from the D values obtained by QENS to the τ_c^{-1} values obtained by β-NMR.

In LiC_6 the quasielastic line broadening yielded an activation energy of 1.0(3) eV [35], the β-NMR data the slightly lower E_A value 0.6(2) eV [14]. In both techniques the T range of the well ordered phase of LiC_6 was covered. Differences in the extracted E_A values

might arise from the different time windows of the spectroscopic methods, which are about three orders of magnitude apart. The β-NMR data showed pronounced deviations from Lorentzian shaped spectral density functions. The evaluation of the quasielastic line broadening of the neutron spectra was, due to the statistics, limited to Lorentzian scattering functions. The D value at 720 K pertains to the disordered state above the in-plane melting temperature of 715 K [7, 8] and shows a dramatic increase of the diffusivity. This illustrates the influence of structural changes on E_A.

For LiC_{12} the TOF spectra yield an activation energy $E_A = 0.35$ eV [34]. This is considerably lower than the E_A value of about 1 eV estimated from the β-NMR data. It is noted that the β-NMR data cover temperatures below the order/disorder transition at about 500 K, while the TOF data cover the disordered phase of LiC_{12}. In Fig. 6 the turn-over of the slope of the $\tau_c^{-1}(T)$ data to that of the $D(T)$ data is located close to the transition temperature. So different jump motions below and above the transition might lead to the difference in E_A. It was already mentioned in the previous section that the QENS spectra at the lower temperatures were not analysed in terms of jump vectors and correlation times, and a change in the jump geometry cannot be traced further within the accuracy of the present data.

For LiC_{16} the data are too scarce for a reliable determination of E_A, and only an estimate can be given. The jump vector agrees with that found in the disordered phase of LiC_6. It should be noted that for LiC_6 and LiC_{16} in their respective disordered states the diffusivities may be described by a common E_A value for which 0.43 eV is estimated. This is close to the value found for the disordered phase of LiC_{12} and is a hint that interplanar couplings play a minor role for the ionic motion in the disordered phase and that the activation energy in the stage-1 compound is reduced upon becoming disordered as supposed earlier [13]. A similar observation was made in diffusion studies in hexagonal Li_xTiS_2. There, upon depletion of the Li layers a reduction of the activation energy was observed [26].

Lattice simulation calculations of the Li in-plane migration for LiC_6 and LiC_{12} reveal the same jump vector as observed in the neutron scattering experiments [36]. The saddle point energy for the migration path is in close agreement with the experimental result for LiC_{12}. But the simulations yield a lower saddle point energy for LiC_6, a finding corresponding to the

β-NMR data. Recent Monte Carlo simulations of the Li diffusion through a graphite lattice based on cluster calculations of the electronic structure also yield energy barriers for the Li^+ migration [37]. For the in-plane diffusion of a single Li atom an activation energy of 0.8 eV is obtained, for the preexponential D_0 the value 10^{-6} m^2 s^{-1} is reported. This is of the order of magnitude found for LiC_{12}. The cluster calculations yield an energy barrier of 13 eV for the diffusion path along the c direction, ruling out motions across the graphene sheets in the intercalation process. The simulations further emphasize the crucial role of the Coulomb interaction of the Li^+ diffusion.

3.4 Summary

Motional processes in stage-1 and stage-2 Li graphite intercalation compounds were investigated in a wide range of temperatures with the β-NMR method and additionally with neutron time-of-flight and backscattering techniques in the high temperature regime.

Below 100 K coupling to conduction electrons dominates the SLR. For LiC_{12}, T_1^{-1} and Knight shift data were used to calculate the Korringa product. An ionic character of Li and low-dimensional electronic properties of the compound in accordance with theoretical considerations were found.

Above 300 K, diffusion induced SLR peaks were observed in LiC_6 and LiC_{12}. The B dependence on the low-T side of the maximum is weaker than predicted by standard models for diffusion induced SLR and was used to estimate activation energies from the slope of the $\log(T_{1d}^{-1})$ vs. $1/T$ representation. The B dependence on the high-T side of the rate maximum is compatible with a 2 D diffusion process. From the shift of the temperature where the rate maximum is attained with B as well as from the B dependence on the high-T side jump correlation times τ_c were estimated. The neutron scattering experiments on the stage-2 compounds were restricted to the high-T regime and yielded in-plane diffusion constants and jump vectors.

The activation energy obtained by β-NMR for LiC_6 is 0.6 eV. This is slightly below the literature value obtained by QENS. The difference may be attributed to the different frequency windows of the methods. For LiC_{12} TOF measurements yielded $E_A = 0.35$ eV, the β-NMR data about 1 eV. This difference is due to

the different phases of LiC_{12} the respective data sets cover. For LiC_{16} and the disordered phase of LiC_6 a common E_A may be established which is close to that of the disordered phase of LiC_{12}.

Comparison with computer simulations of the Li^+ migration confirms the 2 D nature of the motion and consequently the crucial role of in-plane order in diffusion.

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