

# FIREFLY (Fitting ItERatively For Likelihood analYsis): a full spectral fitting code

David M. Wilkinson, Claudia Maraston,<sup>★</sup> Daniel Goddard, Daniel Thomas<sup>★</sup>  
and Taniya Parikh

*Institute of Cosmology and Gravitation, University of Portsmouth, Portsmouth PO1 3FX, UK*

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## ABSTRACT

We present a new spectral fitting code, FIREFLY, for deriving the stellar population properties of stellar systems. FIREFLY is a chi-squared minimization fitting code that fits combinations of single-burst stellar population models to spectroscopic data, following an iterative best-fitting process controlled by the Bayesian information criterion. No priors are applied, rather all solutions within a statistical cut are retained with their weight. Moreover, no additive or multiplicative polynomials are employed to adjust the spectral shape. This fitting freedom is envisaged in order to map out the effect of intrinsic spectral energy distribution degeneracies, such as age, metallicity, dust reddening on galaxy properties, and to quantify the effect of varying input model components on such properties. Dust attenuation is included using a new procedure, which was tested on Integral Field Spectroscopic data in a previous paper. The fitting method is extensively tested with a comprehensive suite of mock galaxies, real galaxies from the Sloan Digital Sky Survey and Milky Way globular clusters. We also assess the robustness of the derived properties as a function of signal-to-noise ratio (S/N) and adopted wavelength range. We show that FIREFLY is able to recover age, metallicity, stellar mass, and even the star formation history remarkably well down to an S/N  $\sim 5$ , for moderately dusty systems. Code and results <sup>★</sup>are publicly available.<sup>1</sup>

**Key words:** methods: data analysis – methods: numerical – galaxies: evolution – galaxies: fundamental parameters – galaxies: stellar content.

## 1 INTRODUCTION

The comparison of model spectra to observed galaxy and star clusters spectra is essential to the interpretation of galaxy evolution problems and for determining the gravitational potential of galaxies via velocity dispersion estimates. Models at an increasingly high spectral resolution are now available (e.g. Bruzual & Charlot 2003; Vazdekis et al. 2010, Thomas, Maraston & Johansson 2011, Maraston & Strömbäck 2011), which also contain sophisticated prescriptions of stellar evolution. As the models grow in complexity and precision, we are increasingly able to derive more robust stellar evolution histories of galaxies. In the recent past, several algorithms for matching models to observed spectra have been published (e.g. PPF by Cappellari & Emsellem 2004; Sarzi et al. 2006, STARLIGHT by Cid Fernandes et al. 2005, STECKMAP by Ocvirk et al. 2006b, VESPA by Tojeiro et al. 2007, NBURSTS by Chilingarian et al. 2007,

CIGALE by Noll et al. 2009; Conroy, Graves & van Dokkum 2014, BEAGLE by Chevallard & Charlot 2016).

In this paper, we introduce a new full spectral fitting code called FIREFLY (Fitting ItERatively For Likelihood analYsis), designed to tackle many specific challenges in the interpretation of model spectra into galaxy properties. We shall now summarize these challenges before we introduce the specifics of our code.

The problem of degeneracies is one that pervades the study of spectra, especially at optical wavelengths (e.g. Worthey 1994). Three main parameters are particularly degenerate with respect to each other, namely age, metallicity, and dust. These degeneracies are inherent to theoretical spectra and can be difficult to disentangle even at high spectral resolution and accuracy. Due to this, many local minima (in a chi-squared sense) may exist across the multidimensional parameter space, which arise from the inherent spectral degeneracies in physical properties. It is therefore important to ‘map out our ignorance’ when providing an estimate of physical properties and have algorithms in place to avoid becoming

<sup>★</sup>E-mail: [claudia.maraston@port.ac.uk](mailto:claudia.maraston@port.ac.uk) (CM); [daniel.thomas@port.ac.uk](mailto:daniel.thomas@port.ac.uk) (DT)

<sup>1</sup> [www.icg.port.ac.uk/firefly](http://www.icg.port.ac.uk/firefly)

‘trapped’ into local maxima in likelihood. In a galaxy, multiple stellar populations co-exist and so the degeneracies become even more difficult to break. Nearby globular clusters, whose stars we can individually resolve, can provide sanity checks on the modelling of galaxies by allowing us to check the results of spectral fitting with the properties determined independently through techniques such as colour–magnitude–diagram (CMD) fitting.

More technically, model spectra do not vary smoothly as a function of a given stellar population property such as age or metallicity, due to short-lived stellar phases contributing in different ways to the total spectral energy distribution (SED) at various wavelengths. What this means is that we use as a fitting tool, a discrete set of model spectra which correspond to a grid which may or may not be a regular. In principle, given a fine enough grid of models in parameter space, one should in theory be able to use a spectral fitting code to approximately recover any possible star formation history (SFH) in a galaxy, no matter how complex the observed SED. Modern stellar population models allow this to be possible to high precision, typically having very fine grids of SEDs, especially in age, corresponding to sets of hundreds of SEDs, each corresponding to a unique stellar population age, metallicity (e.g.  $[Z/H]$ ), and initial mass function (IMF), with properties like dust content and emission lines typically added at the end of the computation.

In practice, a perfect decomposition is not possible in astrophysics as stellar light is emitted inversely proportional to time and strongly non-linear with stellar mass, which means that the most luminous components are those that might be the less relevant in a mass budget. For a recent discussion of this problem, see Maraston et al. (2010), who define it as the ‘iceberg effect’. This effect means that even without setting priors and using an arbitrarily fine model grid, some stellar components may remain outshined by the latest stellar generations. In addition to this, spectral fitting at high spectral resolution involves a significant amount of computational time. Ideally, one would wish to obtain the full posterior distribution of all possible SFHs, for example via Monte Carlo Markov Chain (MCMC) methods. However, the time taken to undertake MCMC for hundreds of possible model spectra (i.e. dimensions) in combination is completely impractical for even the most powerful modern computing clusters. Problems tackled by such approaches (e.g. Acquaviva, Gawiser & Guaita 2011; Panter, Heavens & Jimenez 2003; Nilsson et al. 2007; Sajina et al. 2006; Johnson et al. 2013; Serra et al. 2011) typically have no more than 10 dimensions. CPU time can be reduced to manageable levels at the same time as covering adequate parameter space using a variety of methods when producing a spectral fitting code. We will briefly summarize these here and direct the reader to Section 3 for more details of how these are overcome in this work.

First, one may opt to use a reduced (in number) set of base models, thus reducing the dimensionality of the problem. This can be done by summing models together, either by grouping base models that are spectrally similar (as in e.g. `STEC(K)MAP` Ocvirk et al. 2006b), or by constructing a set of base models with layers of complexity that are used as the data require it (e.g. as in the fitting code `VESPA`, Tojeiro et al. 2007). Most of these methods have the advantage that the physical intuition of the solutions are retained, but reduces the accuracy of the solutions and requires an input prior on the possible SFHs, which is a non-trivial choice. Secondly, one may use an automated procedure for dimensionality reduction, such as principal component analysis (PCA, as in e.g. Chen et al. 2012), before using a simple fitting method. This has the advantage of being extremely quick to fit once the base model components are chosen, but the solutions are difficult to interpret when converting

back into measurable galaxy physical properties. Finally, one may choose to use the full set of base models available, but restrict the exploration of parameters, such that the posterior probability is calculated over a smaller area or to a lower precision. `STARLIGHT` (Cid Fernandes et al. 2005) does this by compressing the stellar population parameters to a coarser grid after fitting using the full available grid, choosing the coarse grid through simulations. This approach is robust but may not exploit the full precision able to be achieved with modern advancements in wavelength resolution both in models and data. `PPXF` (Cappellari & Emsellem 2004) uses a similar approach, in which penalty terms are applied to the residuals found from least-squares fitting, in order to bias the solutions to a Gaussian shape around the best-fitting values. The output of this approach is therefore a best-fitting combination of base models, with errors estimated from Gaussian exploration around this best fit. Optionally, `PPXF` can also preferentially choose solutions with smooth SFHs. In either case however, this approach can be prone to falling into local minima in chi-squared space, which can be prolific when attempting to recover complex SFHs. Thus, the full range of possible spectral degeneracies cannot be explored without applying Monte Carlo simulations on the input data.

In this paper, we describe the development of a new analysis tool, `FIREFLY`, that follows the latter approach described in the previous paragraph, i.e. a posterior distribution of galaxy physical properties is estimated by comparing to data a large set of model stellar populations in linear combinations. Our procedure employs a chi-squared minimization approach, but to avoid the problem of falling into local minima we use liberal parameter searching with a convergence test. This choice becomes more important as the number of models used in linear combination increases. We are then able to derive a large set of plausible SFHs that cover a large portion of parameter space. As we will demonstrate in this paper, trusting the best fit over all other solutions can be misleading when applied to galaxy data, especially since spectral degeneracies in the models are often prominent. We take the point of view that is preferable to explore model degeneracies rather than avoid them.

Model SEDs depend on their input stellar spectra. In this work, we fit observational data using models by Maraston & Strömback (2011) which are calculated keeping the energetics fixed and varying the input stellar spectra, using three different empirical libraries, namely medium-resolution Isaac Newton Telescope library of empirical spectra (MILES) (Sánchez-Blázquez et al. 2006), `STELIB` (Le Borgne et al. 2003), and `ELODIE` (Prugniel et al. 2007). This way we can assess the effect of stellar spectra on the final result on galaxy evolution (Section 2).

In order to validate our modelling technique, we perform extensive testing making use of observed spectra of simple Milky Way populations (e.g. globular clusters), mock galaxies with well-defined properties known in advance, involving both simple and complex SFHs, and galaxy data which have been analysed previously in the literature.

The paper is structured as follows. In Section 2, we describe the stellar population models used in this work. Section 3 provides the details of the `FIREFLY` algorithm, the treatment of reddening and the visualization of results and output format. Section 4 briefly compares the `FIREFLY` procedure to those of other widely used codes. The comprehensive testing with globular clusters data and mock galaxies is found in Section 5. The testing with the Sloan Digital Sky Survey Data Release (SDSS DR7) galaxy survey (Abazajian et al. 2009) and comparisons to results obtained with other codes are shown in Section 6. In Section 7, we provide a discussion and present our conclusions.

## 2 INPUT STELLAR POPULATION MODELS

FIREFLY can be used to fit any set of stellar population models to observational SEDs. Here, we use the stellar population models of Maraston & Strömbäck (2011), hereafter **M11**, which are calculated for several input stellar spectra.<sup>2</sup> In this paper, we experiment with models based on three empirical stellar libraries,<sup>3</sup> namely MILES (Sánchez-Blázquez et al. 2006), STELIB (Le Borgne et al. 2003), and ELODIE (Prugniel et al. 2007). The **M11** models make the same assumptions as Maraston (2005) with regards to the fuel consumption in the post-main sequence and stellar tracks and energetics, and the contribution from thermally pulsating asymptotic giant branch (TP-AGB) stars. We summarize the differences between the models based on the stellar libraries here, but refer the reader to **M11** for a more detailed description.

Models based on the MILES stellar library have the largest range and sampling of the stellar population parameter grid (in terms of age and metallicity), of all three models, and a high spectral resolution of 2.54 Å (Beifiori et al. 2011). In particular, **M11**–MILES models have coverage of both low- and very low-metallicity populations ( $[Z/H] = 0.3$  and  $-2.3$  respectively), albeit only for old ages (due to the Milky Way stellar age distribution at low- $Z$ ). The wavelength coverage encompasses the range 3500–7429 Å, and as discussed in **M11** and Maraston et al. (2009), have a somewhat lower flux upwards of 6400 Å compared to STELIB- and ELODIE-based models. This is due the differences in the assumed temperature scales for RGB-bump stars (see **M11**). **M11** also published a version of MILES-based models where the temperature assigned was changed following other libraries and as a result it has a higher near-infrared (near-IR) flux which matches the models based on other libraries (see **M11**, Appendix A).

Models based on the STELIB stellar library cover three metallicities, half-solar, solar, and twice-solar, and lack some of the younger ages present in other models. However, they boast the largest wavelength range of 3200–7900 Å, and for solar metallicity 3200–9300 Å, with a resolution of  $\sim 3$  Å. To keep the wavelength range consistent when comparing models at different metallicities, we limit the wavelength range of the spectral fit to 3200–7900 Å.

Lastly, models based on the ELODIE (v3.1) stellar library have a fair age and metallicity coverage, extending down to ultra-low metallicities ( $[Z/H] = -2.3$ ), but lacking the low-metallicity ( $[Z/H] = -1.3$ ) stellar populations compared to MILES-based ones. They contain the youngest stellar populations among the models used in this paper, down to just 3 Myr for solar metallicity, though older for non-solar metallicities. The observed stellar spectra used to calculate these very young populations can suffer from unknown dust reddening however, so fitting solutions containing these ages should be checked with care. ELODIE-based models have an exceptionally high resolution of 0.55 Å, but in exchange have a fairly low wavelength coverage of 3900–6800 Å, and a somewhat too flat continuum shape at the edges (see **M11**, fig. 3).

The use of empirical libraries to calculate stellar population models comes with some drawbacks (see **M11** for a detailed discussion). Specifically, there is a lack of M-type dwarf stars, limiting the coverage of temperature and surface gravity in the dwarf tail of the main sequence. To mitigate this, **M11** used theoretical dwarf spectra from the MARCS library (Gustafsson et al. 2008), smoothed to

match the resolution of the specific empirical spectra. In addition, all these libraries lack Carbon- and Oxygen-rich stars, necessary to model the TP-AGB stellar phase. To represent this phase, **M11** use interpolated versions of low-resolution spectra from Lançon & Wood (2000), as was used in Maraston (2005), which still provides enough resolution to identify the broad features from the component AGB stars in the resulting SEDs.

An additional caveat to the use of empirical libraries is that the element abundance ratios encoded in the observed stars are usually not known for all stars, making the element abundance ratio of the integrated model uncertain (see Milone, Sansom & Sánchez-Blázquez 2011 for an attempt to derive all chemical abundance ratios for the MILES stars). Elemental abundance ratios are probably solar-scaled at high-metallicity and  $\alpha$ -enhanced at low metallicity, following the pattern of chemical evolution known for the Milky Way (see extensive discussion in Thomas, Maraston & Bender 2003). Furthermore, the flux calibration may carry additional uncertainties. The relative flux calibration of each empirical library has been qualitatively assessed in **M11**, finding, in summary, that the most significant difference is that cool stars are bluer, and hot stars are redder, in the MILES library compared with STELIB and ELODIE. We noted already that our method of dust and flux calibration treatment described in Section 3.3 should minimize flux calibration issues, as demonstrated in Wilkinson et al. (2015).

The base stellar population model is referred to as simple stellar population (SSP), a model describing a coeval population of stars with a given age and chemical composition. In nature, globular clusters are generally well represented by a single SSP and even those showing evidence of so-called multiple generations (e.g. Piotto et al. 2007) remain simpler in terms of SFH than galaxies. Hence, globular clusters provide a good ‘sanity check’ on the combination of stellar population models and a fitting procedure. We shall fit globular cluster data in Section 5. In Fig. 1, we have plotted the SSP spectra for the **M11** empirical models at various ages, as a function of stellar library for a visual comparison. Each model clearly gives different SEDs, the differences of which change as a function of age and metallicity. In Section 6, we describe how the differences in SEDs propagate to diverse galaxy properties.

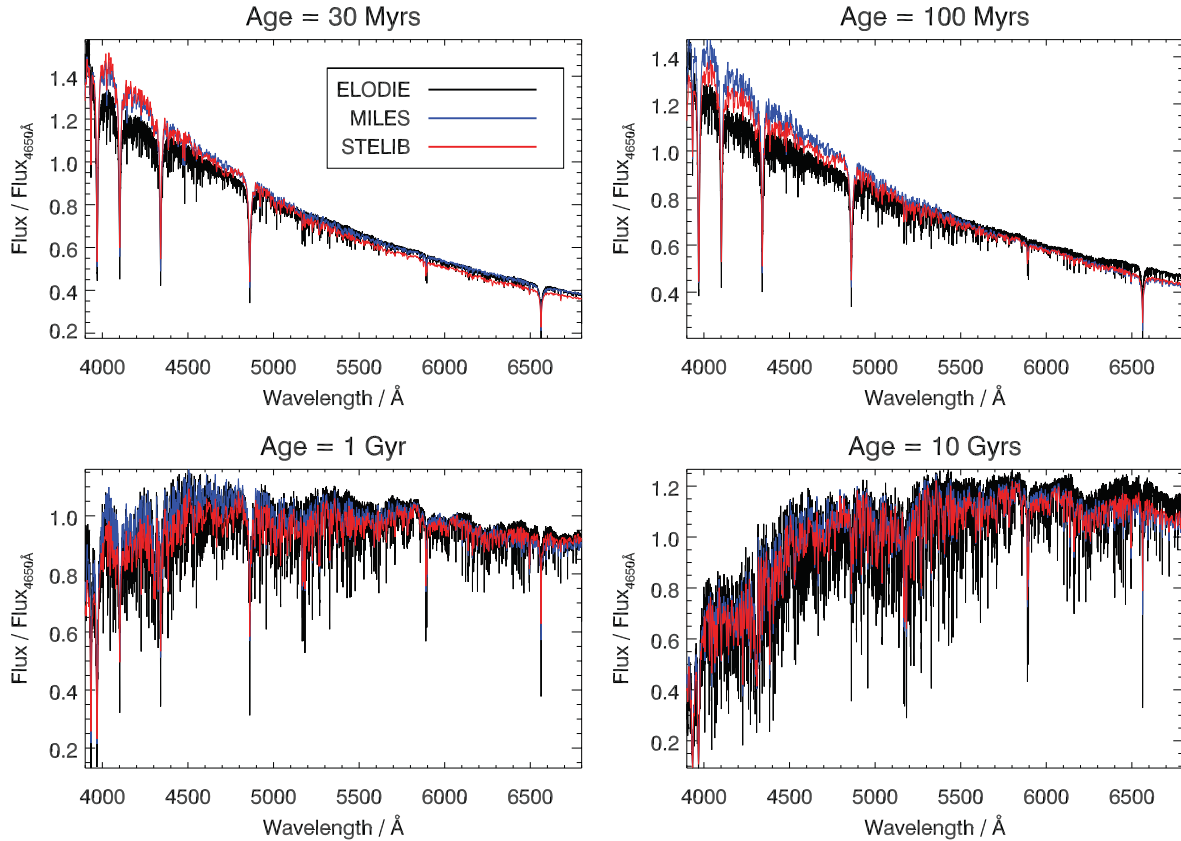
Lastly, we comment on the IMF, which is a model input. The **M11** models used in this paper are calculated for three IMFs for describing the distribution of stellar masses at birth, namely ‘Salpeter’ (Salpeter 1955), ‘Kroupa’ (Kroupa 2001), and ‘Chabrier’ (Chabrier 2003). Since Kroupa and Chabrier IMFs have lower amounts of low-mass stars, they have lower mass-to-light ratios, e.g. in the SDSS ‘ $i'$ ’-band Kroupa and Chabrier mass-to-light ratios are different by a factor  $\sim 0.6$  and  $\sim 0.55$  compared to Salpeter, respectively. However, other than the scaling factor the impact on the SED fit is restricted to only some small changes in certain absorption features. In tests with models based on different IMFs, we did not measure any difference on the recovered SED fits greater than 0.1 per cent in any of the properties. As Kroupa IMFs are often used in the literature, in this paper, we only show results from using models with a Kroupa IMF.

## 3 FITTING METHOD

FIREFLY is a full spectroscopic fitting code of models to data, based on  $\chi^2$ -minimization with treatment of the inherent spectral degeneracies and uncertainties in the data. FIREFLY finds physical parameters, such as age ( $t$ ), metallicity ( $[Z/H]$ ), and dust ( $E(B - V)$ ) by minimizing the  $\chi^2$  values of models with respect to data. Models are arbitrary combinations of individual bursts. The SFH is reconstructed

<sup>2</sup> Models are available at [www.maraston.eu/M11/](http://www.maraston.eu/M11/).

<sup>3</sup> **M11** also publish a set of models based on the theoretical stellar library MARCS, see detail in **M11**. The theoretical version of **M11** models are also a standard input of FIREFLY.



**Figure 1.** Comparison of stellar population model spectra for different ages, 30 Myr, 100 Myr, 1 Gyr, and 10 Gyrs, respectively, for a Kroupa IMF (Kroupa 2001) and solar metallicity, from the stellar population models of Maraston & Strömbäck (2011).

at the end of the procedure and the stellar mass is calculated. In addition to the ‘best fit’, the code also outputs many other solutions and their associated values of  $\chi^2$ . Thus, it gives a likelihood surface with many maxima across a large amount of parameter space. Full details of the algorithm are given in Section 3.2.

The main motivations driving the design of our code were the following:

- (i) Be able to map out the inherent degeneracies in the spectra, and how they propagate into degeneracies in physical properties;
- (ii) Be fast enough to analyse millions of galaxy spectra at high spectral resolution spanning a large wavelength range in a reasonable time frame;
- (iii) Allow a comparison of the different models to be conducted easily;
- (iv) Have a method that visualizes the parameters obtained conveniently so that improvements can be made incrementally;
- (v) Work relatively well also in low signal-to-noise (S/N) regimes;
- (vi) Makes as few assumptions regarding SFH and other parameters as possible, within the constraints of the available models.

In Section 3.1, we explain the rationale for the first requirement in this list, using as an example case the Milky Way old open cluster M67. In Section 3.2, we detail the generalized method, with descriptions of how we treat additional complications in the spectra, including dust, complex SFHs, emission lines, and variable wavelength ranges. In Section 3.6, we discuss how we obtain galaxy properties such as the average age, metallicity, and total stellar mass. In Section 3.9, we describe the statistics of the fits obtained

and how these lead to visualization of physical properties. Lastly, in Section 4, we compare our procedure with other fitting codes in the literature.

### 3.1 The age–metallicity–stellar library degeneracy

Maraston & Strömbäck (2011) performed a fit of their models to the optical spectrum of the Milky Way old open cluster M67 (Schiaffon et al. 2005). M67 is an ideal object for the purpose of model calibration, because it is a simple stellar system, with age and metallicity determinations from fitting stellar models to the CMD. A current measure of M67 age is 3.5–4 Gyr (see Sarajedini, Dotter & Kirkpatrick 2009). M67 is also a desirable object for these models because it is approximately solar in metallicity and has got solar-scaled element abundance ratios, which matches with the models (see discussion in M11, and their fig. 21). Using MILES- and STELIB-based models, M11 find that different solutions corresponded to the minimum  $\chi^2$ , namely 9 Gyr,  $0.5 Z_{\odot}$  for M11–MILES and 3 Gyr,  $Z_{\odot}$ , for M11–STELIB. The quality of fits in terms of absolute  $\chi^2$  was the same. As the energetics and the code are identical for the two sets of models, the difference was attributed to the effect of the input stellar library. The effect quantitatively mimics the well-known age–metallicity degeneracy (e.g. Worthey 1994), hence we may worry about a complicated ‘age–metallicity–stellar library’ degeneracy. The M11 test was based on a simpler code and looked only at the minimum  $\chi^2$ . In this paper, we shall re-address this problem comprehensively in Section 5.2.1.

For a first test of our fitting code, we use FIREFLY to repeat the M11 test and fit the M67 observed spectrum. We additionally use also

the ELODIE-based M11 models. We restrict the fit to single-SSP solutions (see Section 3.2 for the general algorithm), since M67 is shown from CMD fitting to be very well represented by a simple population (Sarajedini et al. 2009). The wavelength range used for the best fits is the maximum used by the data (3650–5350 Å) or the models. The spectra in this case are normalized to 4600–4700 Å because this region is relatively free of absorption lines and matches the work of M11. Note that, in general, we normalize to as large a wavelength range as possible so that we do not need to worry about absorption features in particular regions, and so that this method still works when we are missing data from portions of the wavelength region (see Section 5.2).

Fig. 2 shows the results. All fits are visually very good, and their  $\chi^2$ 's lie within 0.1 percent of each other, but the recovered properties do vary. The age and metallicity of M67 are 9, 3, and 10 Gyr at half-solar, solar, and half-solar metallicity, for MILES-, STELIB-, and ELODIE-based models, respectively. Our results for MILES and STELIB are fully consistent with the M11 ones, with the STELIB-based models matching the CMD-derived results well, whereas MILES-based results suffer from the age-metallicity degeneracy, which places their lowest  $\chi^2$  values at a higher age, but a lower metallicity. ELODIE-based models behave similarly to MILES-based ones.

Fig. 2 demonstrates yet another problem in spectral model degeneracy, namely that the physical properties derived for stellar systems vary as a function of just one model ingredient, the input stellar library, and paint a different picture of the galaxy's current properties and SFH.

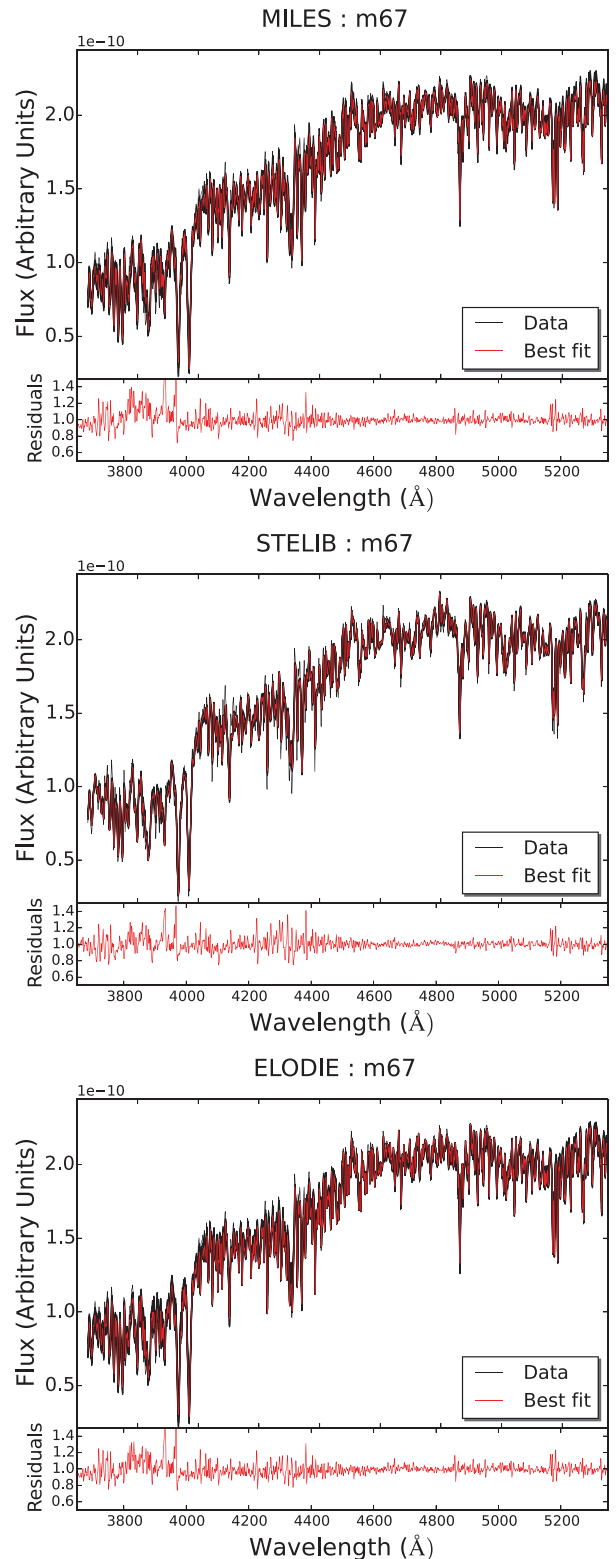
In principle, the STELIB–M11 solution is the one matching the CMD solution, hence it should be retained as the only one physical. On the other hand, there is also a statistical problem, namely: is the solution for the minimum  $\chi^2$  the only one we should consider? Indeed, it is easy to find combinations of age and metallicity that give very similar chi-squared values. In writing our code, we explore all solutions and retain those within a statistical significance from the best fit.

### 3.2 Algorithm

When using a  $\chi^2$ -minimization technique, as demonstrated here, in Maraston et al. (2010) and M11, depending on input model ingredients, the ‘best’ solution may not always correspond to the most realistic or precise galaxy properties. Clearly, this method of finding the physical parameters of a galaxy is inadequate, especially given the close proximity of the chi-squared values of many combinations of parameters. With this in mind, we have developed our fitting code to give the additional information of not only the minimal chi-squared solution, but also a good sample of other solutions.

Fig. 3 describes our general procedure for fitting an object spectrum with a set of model spectra. A step-by-step visualization of the fitting process of the full spectrum of an example SDSS galaxy is shown in Fig. 4 for a subset of the model SEDs used. By using this parallel fitting approach, we can obtain many combinations of SSPs, often giving on order 1000 solutions. The assumptions in this approach are:

(i) We are able to find good solutions by working in the basis of the SSPs (i.e. assuming the *individual* solutions can be modelled with a bursty SFH). However, if we use a finely sampled in time grid of SSPs then we are able to obtain SFHs that are effectively continuous;



**Figure 2.** Best fits for the star cluster M67, all of which are visually excellent. The top panel shows the fit using models based on the MILES library (M11–MILES), whereas the middle and the bottom plots show the fits using M11–STELIB and M11–ELODIE, respectively. Each individual sub-panel shows the residual of the data and model. For the three models M11–MILES, M11–STELIB, and M11–ELODIE, we obtain 9, 3, and 10 Gyr and a half-solar, solar, and half-solar metallicity, respectively. These results match well with those obtained in M11.

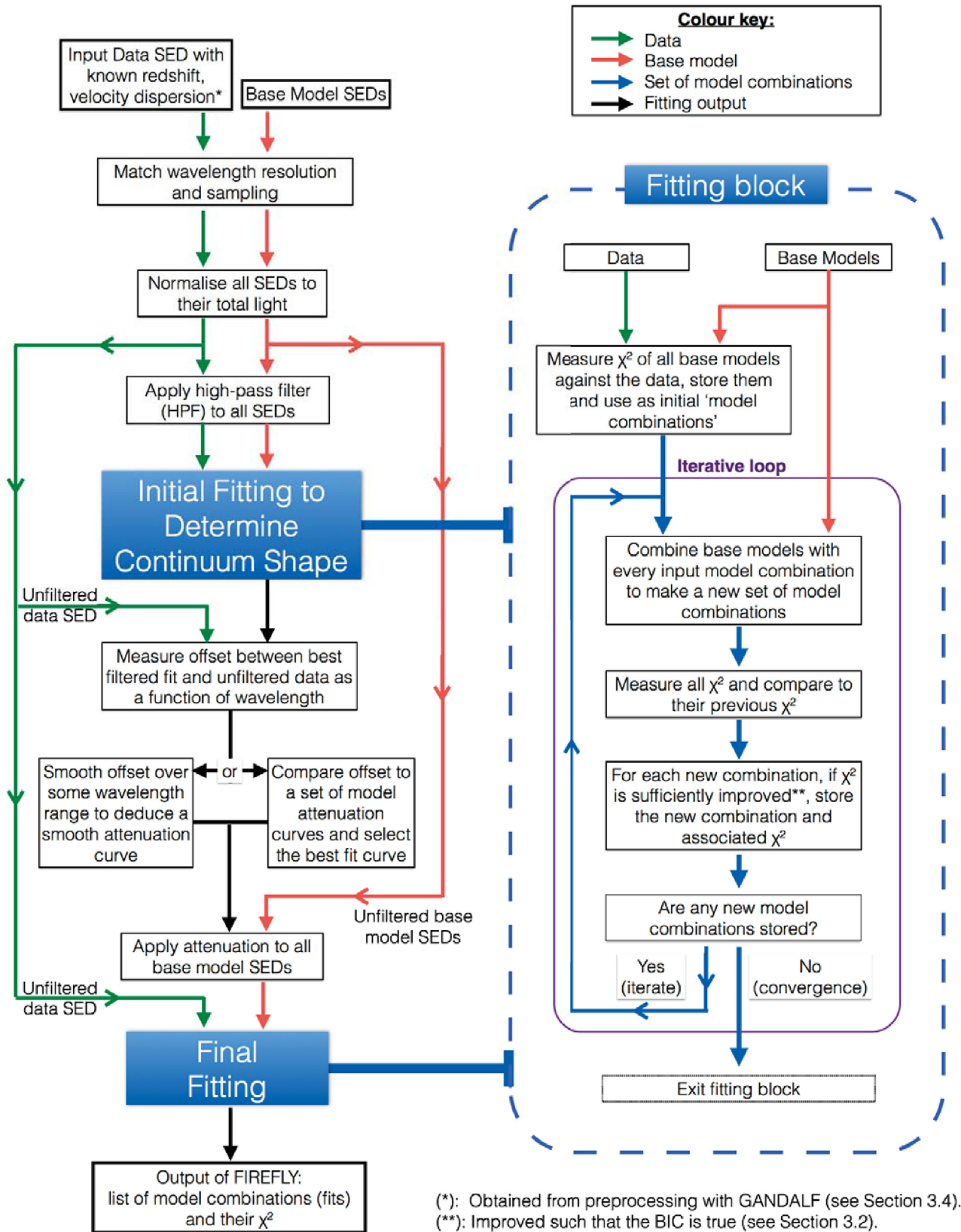
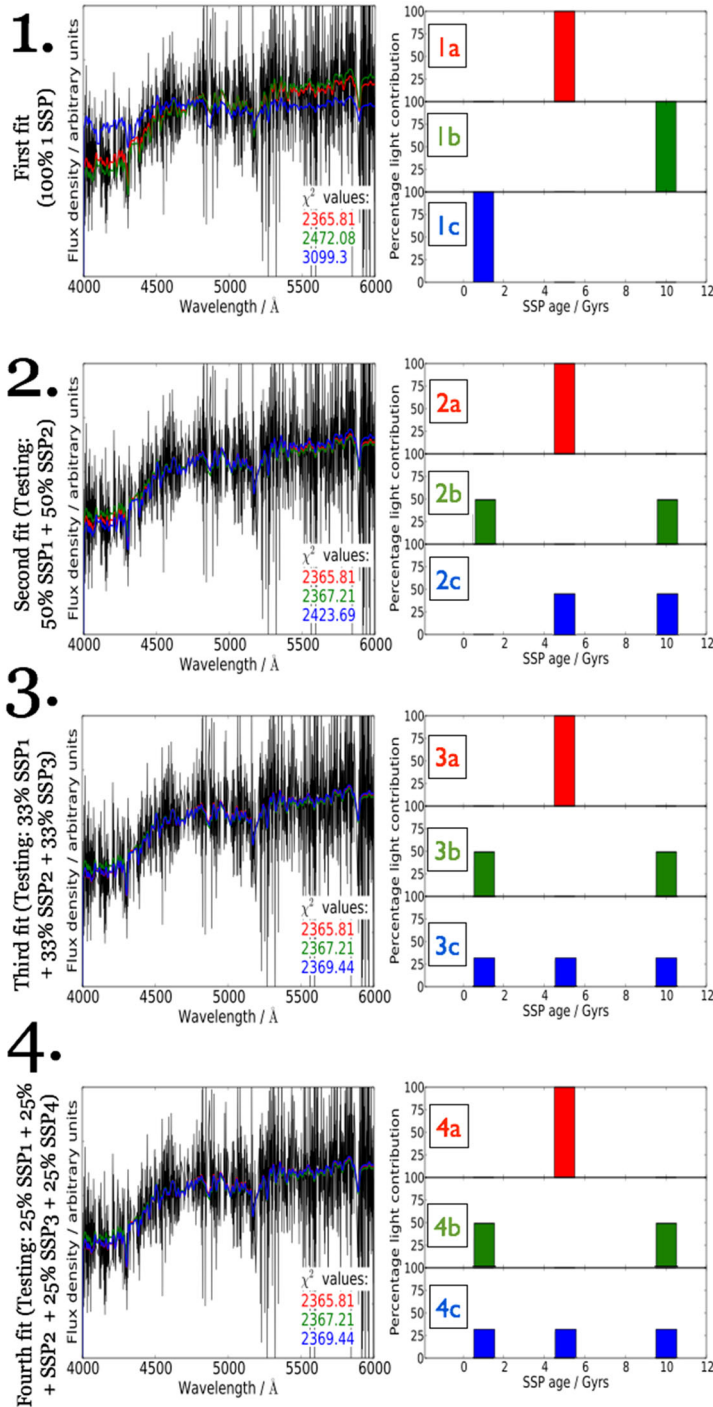


Figure 3. Schematic description of FIREFLY.



**Figure 4.** Step-by-step example of running the FIREFLY fitting block on an SDSS galaxy, using a reduced set of base SSPs for clarity.

(ii) We are able to first find a suitable SSP-based fit and then hone our overall composite SFH by adding smaller proportions of other SSPs to this fit;

(iii) Solutions can be combined via  $\chi^2$  likelihoods to give a physically realistic sum SFH.

We first discuss the fitting block of the code in Fig. 3. The main component of this code is the iterative loop over equal weights of base model SSPs. At each iteration of the loop, we progressively increase the size of the linear combinations used in the fits. To give

**Step One:** Initially each of the SSPs are fit to the data. In this example fitting process to a sample galaxy we only use 3 SSPs:

1 Gyr, 5 Gyrs, and 10 Gyrs, all at solar metallicity.  
**1a** = 5 Gyr SSP, **1b** = 10 Gyr SSP, **1c** = 1 Gyr SSP.

**Step Two:** For each SSP fit in step one, we add all possible combinations of an additional SSPs such that both SSPs contribute 50% of the total light each.

*i.e.* New fit = 50% new SSP + 50% initial (step one) SSP. Each combination must improve the BIC to be included, otherwise only the fit from the previous step is included. All combinations are saved and the top three plotted (left). This is an explanation of each of the fits in order:

- **2a** is the same as **1a**, where any further SSPs added to the initial 5 Gyr SSP did not improve the BIC.

**100% 5 Gyr.**

- **2b** came from **1b** with the addition of a 1 Gyr SSP to the initial 10 Gyr SSP. **50% 1 Gyr + 50% 10 Gyr.**

- **2c** came from **1b** with the addition of a 5 Gyr SSP to the initial 10 Gyr SSP. **50% 5 Gyr + 50% 10 Gyr.**

**Step Three:** The previous step is repeated, adding another SSP if the BIC is improved.

*i.e.* New fit = 33% new SSP + 33% step two SSP + 33% step one SSP

This is an explanation of each of the fits in order:

- **3a** is the same as **2a**, again where any further SSPs added to the initial 5 Gyr SSP did not improve the BIC.

**100% 5 Gyr.**

- **3b** is the same as **2b**, where any further SSPs added to the previous SSP combination did not improve the BIC.

**50% 1 Gyr + 50% 10 Gyr.**

- **3c** came from **2c**, with the addition of a 1 Gyr SSP with the total light of the initial SSP. **33% 1 Gyr + 33% 5 Gyr + 33% 10 Gyr.**

**Step Four:** Each of the top three combinations remain unchanged, due to every possible SSP contribution not improving their BIC values. Generally, solutions tend to converge like this at around steps three to five. We save each new model combination (*i.e.* SSP weights) and their associated  $\chi^2$  values at every step, **including the step one 100% SSP weights**. For the full set of model SSPs, this can be on the order 1000 solutions, all of which are then output.

a concrete example, suppose a 10 Gyr, solar metallicity SSP (Fit<sub>1</sub> =  $M_{10 \text{ Gyr}, Z_{\odot}}$ ) has a  $\chi^2$  value that may be reduced by adding a 3 Gyr, half-solar metallicity component, thus creating a linear combination of SSPs as a fit to the data as Fit<sub>2</sub> =  $\frac{1}{2}M_{10 \text{ Gyr}, Z_{\odot}} + \frac{1}{2}M_{3 \text{ Gyr}, 0.5 Z_{\odot}}$ . Each of the possible combinations of two SSPs are checked for improvement on the one-SSP fits, and all fits from both one- and two-SSP fits are saved for the next iteration. This continues until convergence, see below.

It is important to note that even if the initial combinations use equal weights to start with, not all combinations will pass the

goodness threshold (see below) and the survivors will get recombined. Hence, at the end solutions can have arbitrary proportions of the initial grid of SSPs.

With our approach, we obtain a very large number of components, i.e. linear combinations of SSPs. This number is  $N_{\text{baseSSP}} * (N_{\text{baseSSP}} - 1)^{N_{\text{iterations}} - 1}$ . So, for example for M11–MILES containing 159 base SSPs and 4 iterations, the number of components is:  $6.2 \times 10^8$ . In practice, the majority of these components will not survive the iterations, because they will not lead to an improvement of the fit (see below). After a few iterations, the typical number of components is of the order of thousands.

In order to avoid overfitting and allow for convergence of solutions, we employ the Bayesian information criterion (BIC). The BIC quantifies the likelihood of the set of parameter values found given the goodness of the spectral fit (in our case, the  $\chi^2$  value) and includes a penalty term that increases as the number of parameters used increases; see Liddle (2007) for a discussion on the BIC and other information criteria. In order to iteratively improve our fits, we require that the BIC must be improved (reduced) at each iteration of the fit in order for a new SSP contribution to be added. The BIC is defined as follows:

$$\text{BIC} = \chi^2 + k \ln(n), \quad (1)$$

where  $k$  is number of fitting parameters used (in our case, the number of SSPs added in combination to make a fit), and  $n$  is the number of observations (in our case, the number of flux points used in the fit). Therefore, at each iteration step, the  $\Delta_i \text{BIC}$  must be less than zero (where we take  $\Delta_i x$  to mean the value of  $x$  at step  $i$  minus the value at step  $i - 1$ , hence  $\Delta_i k = 1$ ), which means that for a single iteration

$$\Delta_i \chi^2 < \ln(n) \quad (2)$$

must hold in order to contribute to the fit. This prevents extremely unimportant contributions to the SFH from extending the fitting process, and hence prevents wasting CPU time for no tangible benefit to any of the physical properties obtained.

We ensure that we cover adequate parameter space in order to avoid over investigating local minima in  $\chi^2$  at each iteration by allowing any combination that improves the fit beyond the median value of  $\chi^2$  computed at the previous stage. This means that as more solutions get more precise, this median value converges.

We see that the solutions converge at around the fourth step of the iterative process, and for the vast majority of SDSS DR7 galaxies (as in Section 6), we find that solutions converge between the third and fifth iterations with the BIC employed. From this procedure, we obtain a range of fits, each of which has a record of the linear combination of their SSP contribution, the luminosity of which is given by

$$L(\lambda) = \sum_i^{n_{\text{SSP}}} a_i L_{\text{SSP}_i}(\lambda), \quad (3)$$

where  $a_i$  are the weights to the base models  $\text{SSP}_i$ , which has luminosity  $L_{\text{SSP}_i}$  and  $n_{\text{SSP}}$  is the number of SSPs used in the fit. In the next sub-sections, we describe key steps of the fitting procedure more in-depth.

The sampling of a galaxy SFH we can reach with this approach is just the number of entry SSPs (i.e. the base SSPs) as we do not interpolate between ages. So for example for the M11–MILES models the sampling is of 159 ages between 6 Myr and 15 Gyr.

Another interesting quantity is the smallest SSP fraction. Assuming the final solution contains 1000 components, the minimum

weight an SSP can have after four iterations is  $1/4/1000 = 0.004$ , hence of the order  $10^{-3}$ . This is the smallest SSP fraction in this case. This smallest fraction varies according to the input grid, the number of iterations (which will also depend on the data), and how well the model fits the data. For SDSS-DR7 galaxies fitted with M11–MILES, we find  $10^{-4}$ – $10^{-3}$ .

### 3.3 Interstellar reddening

FIREFLY takes into account both interstellar reddening of the object observed, and foreground reddening due to the Milky Way’s interstellar material. We take account of the foreground reddening due to dust in the Milky Way by applying the attenuation law of Fitzpatrick (1999) and using the  $E(B - V)$  values from the Schlegel’s maps (Schlegel, Finkbeiner & Davis 1998), using the input right ascension and declination of each object. As shown in Fig. 3, there are two methods used to fit for dust attenuation, both of which involve pre-processing the data and base models. This is described in detail in Wilkinson et al. (2015), where we found that without a sophisticated method for treating dust attenuation, we were unable to retrieve physically realistic values for the dust properties in the case of high dust column density, and/or in data with flux calibration problems. However, this method is applicable in general to measure dust attenuation accurately, so we summarize it in the following section.

Note that in principle the stellar population properties of the stellar system under analysis could already be derived when performing the fit for dust. The reason for re-applying the fitting procedure to determine stellar population properties rather than using the results obtained from fitting the filtered data is that we are adding in the additional prior of assuming a smooth attenuation curve, as deduced in the fourth step of the process above. This helps us better constrain the stellar population properties, as we have the smoothed attenuation curve working as a prior. Hence, the final properties we provide are those obtained by fitting again, now with the intrinsic knowledge of the attenuation curve (loop called ‘Fitting Block’ in Fig. 3).

#### 3.3.1 Producing attenuation curves from the data

We use an analytical function across all wavelengths to rectify the continuum before deriving the stellar population parameters. This function is called a High-Pass Filter (HPF). An HPF applied to SEDs is able to remove the long-wavelength modes of the data, such as continuum shape and dust extinction, through the use of a window function applied to the Fourier transform of the spectra as follows:

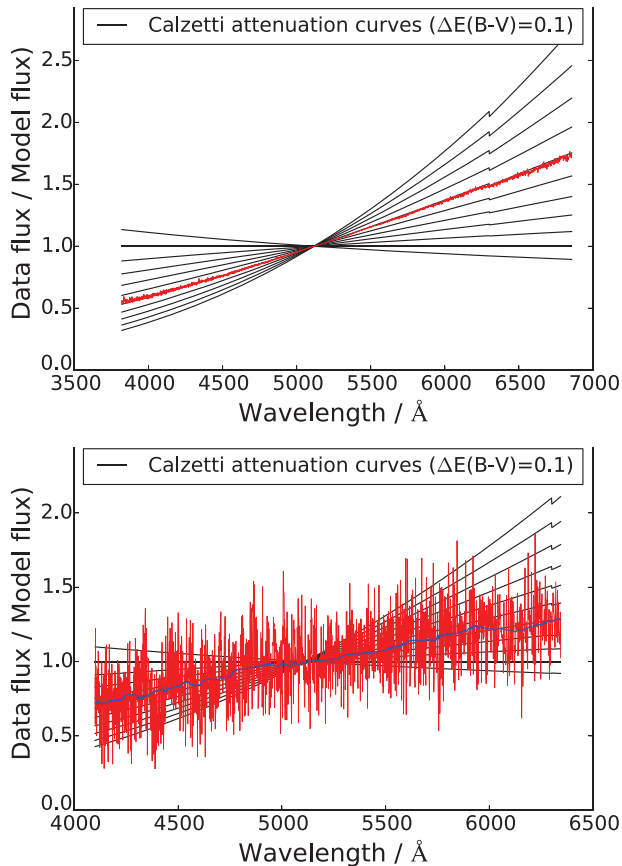
$$\text{Flux}_\lambda^{\text{output}} = \text{Flux}_\lambda^{\text{input}} \otimes W_\lambda, \quad (4)$$

where this is the convolution in wavelength space, and the window function  $W_\lambda = \mathcal{F}^{-1} W_k$  describes which modes,  $k$ , are removed. This window function is given by:

$$W_k = \begin{cases} 0 & k \leq k_{\text{crit}} \\ 1 & \text{otherwise,} \end{cases} \quad (5)$$

where we have parametrized the form of the window function by a single value used in the filter, called  $k_{\text{crit}}$ . This parameter relates to masking features on wavelength scales greater than  $\sim$  number of wavelength points in the spectrum divided by  $k_{\text{crit}}$ . Hence, an SED with 4000 wavelength points between 3000 and 7000 Å and a  $k_{\text{crit}}$  of 40 will remove all wavelength modes greater than 100 Å in size. In Wilkinson et al. (2015), we used a fixed value of  $k_{\text{crit}}$ ,





**Figure 5.** Attenuation arrays derived from FIREFLY’s fitting method of filtered data, as described in Section 3.3. The top panel shows the method applied to a mock galaxy spectrum consisting of a 100 Myr old SSP with an input extinction of  $E(B - V) = 0.5$  and  $S/N = 50$ . The bottom panel refers to an example SDSS DR7 galaxy (see Section 6) with  $S/N \sim 5$ . The deduced attenuation is in red, the smoothed one, which is then applied to the models for refitting (see Section 3.3.1) is in blue. Calzetti et al.’s law curves for  $E(B - V) = -0.1$  to 1.0, in steps of 0.1 are shown in black. Note that in the upper panel, there is no blue line as smoothing was unnecessary.

since the data always had the same wavelength range and sampling, but for a general application, we set  $k_{\text{crit}}$  to the number of flux points/100, which masks any modes greater than  $100 \text{ \AA}$  in size. This approximately corresponds to that used in Wilkinson et al. (2015) and the tests done on the consistency of solutions when varying  $k_{\text{crit}}$  are the same.

We then use the parameters measured from this fit in the unfiltered models and data, dividing the best model fit by the data to give a residual attenuation curve. This is then smoothed over a wavelength range of at least  $100 \text{ \AA}$  depending on the features one wishes to try to capture. Once one has fit the filtered model SEDs to the filtered data SED, the fitting block returns a measured attenuation array, which is smoothed over the wavelength scales one is trying to assess, i.e.  $100 \text{ \AA}$  in our application. Then, in our default approach, we measure the closest fit to a set of model attenuation curves to obtain an estimate of the extinction that is output by the code as a single number ( $E(B - V)$ ), but apply the full derived attenuation array to all model SEDs and the data are refit assuming this attenuation.

In Fig. 5, we show two examples of fitting SEDs using this method. The returned attenuation arrays are shown in red, its smoothed version in blue. To guide the comparison, we also plot Calzetti et al. (2000, see next sub-section) attenuation curves from

$-0.1$  to  $1.0$  in  $E(B - V)$ , in steps of  $0.1$ , where the zero value of extinction corresponds to a constant value of  $1.0$ .

In the top panel of Fig. 5, we have used a mock galaxy spectrum, consisting of a 100 Myr old SSP, to which we applied a Calzetti-type attenuation law with input  $E(B - V) = 0.5$ . The  $S/N$  of this mock is 50. The recovery of the input Calzetti curve with  $E(B - V) = 0.5$  is excellent as the recovered attenuation function lies almost exactly along a Calzetti’s curve corresponding to  $E(B - V) = 0.5$ . In the lower panel, we show the same exercise for an example galaxy from SDSS/DR7 galaxy (see Section 6) with a median  $S/N$  of  $\sim 5$ . The noise is clearly seen in the raw attenuation array in red. Once smoothed however (blue curve), we can see that the Calzetti law represents the function derived from the data reasonably well, suggesting that it models the data well. In this case, the method described here and in the next section are equivalent. However, as shown in Wilkinson et al. (2015), the method described in this section offers significant advantages when the flux calibration is uncertain.

### 3.3.2 Fitting attenuation using general curves

The other method for including dust extinction in spectral fitting is to use general attenuation curves, which were derived independently of the data under analysis. Here, we adopt the Calzetti law as in Calzetti et al. (2000), using a range of values of  $E(B - V)$  from  $0.0$  to  $1.0$ . This law has been shown to be generally applicable to good accuracy to many different types of galaxies such as those from the SDSS surveys used in this work (Chevallard et al. 2013; Pacifici et al. 2012). We assume that a dust screen is uniform across the whole galaxy and thus is applied to the SSP combinations equally. This method may be used over the default HPF method of determining the attenuation curve when one wishes to assume a known law such as the Calzetti’s one. Should any user of FIREFLY wish to use a different extinction law for reddening, or use different parameters, the extinction law can be easily changed via swapping out the attenuation module. In both cases, the attenuated SEDs are then refit to the data.

We tested both dust methods on  $S/N > 5$  mock spectra, finding good agreement between the two, with results within  $0.02$  dex for average age, metallicity, and stellar mass. However, since the HPF method can be applied more generally (see Fig. 5) when the attenuation law is unknown and/or the flux calibration is uncertain, we set this as default in this paper.

### 3.4 Emission lines

FIREFLY can in principle fit any spectrum either including emission lines or not, depending on the input models. As the M11 models do not include emission lines, to fit emission-line galaxies one should either mask out regions of emission, or find the strength of emission features and remove them before the fitting.<sup>4</sup> Although our code can work under both circumstances, the latter method should be preferable because including as much of the SED as

<sup>4</sup> For emission-line removal of SDSS galaxy spectra, we use the emission and absorption-line fitting code called Gas AND Absorption Line Fitting (GANDALF; Sarzi et al. 2006), equipped with the same M11 stellar population models as described in Thomas et al. (2013). GANDALF accurately fits the emission lines of a galaxy, providing an emission-line model spectrum. This can then be used to subtract the emission lines from the observed galaxy spectrum, to provide us with an emission-line free spectrum which we can then fit.

possible should allow an increased precision in the fits, except for cases of poor wavelength calibration (e.g. Koleva et al. 2008). This hypothesis is tested in Section 5.

In order to gain an idea on how critical the emission-line removal is, in Appendix A, we performed the exercise of fitting a set of galaxy spectra in which emission lines were removed or left. We find a surprisingly good agreement between the ages and metallicities derived in both cases. These results lead us to conclude that full spectral fitting of a wide enough portion of a galaxy spectrum is relatively robust to the presence of a few narrow emission lines.

### 3.5 Broadening of the spectrum

The combined effects of the galaxy intrinsic velocity dispersion and of the instrumental resolution broaden absorption features in the spectra. Models have their specific spectral resolution, which varies between models and maybe different from data. FIREFLY needs as input the velocity dispersion of the data, such that models can be adapted to this resolution. In this study, we use a combination of GANDALF and PPF codes (Cappellari & Emsellem 2004) as in Thomas et al. (2013) to measure stellar and gas kinematics.

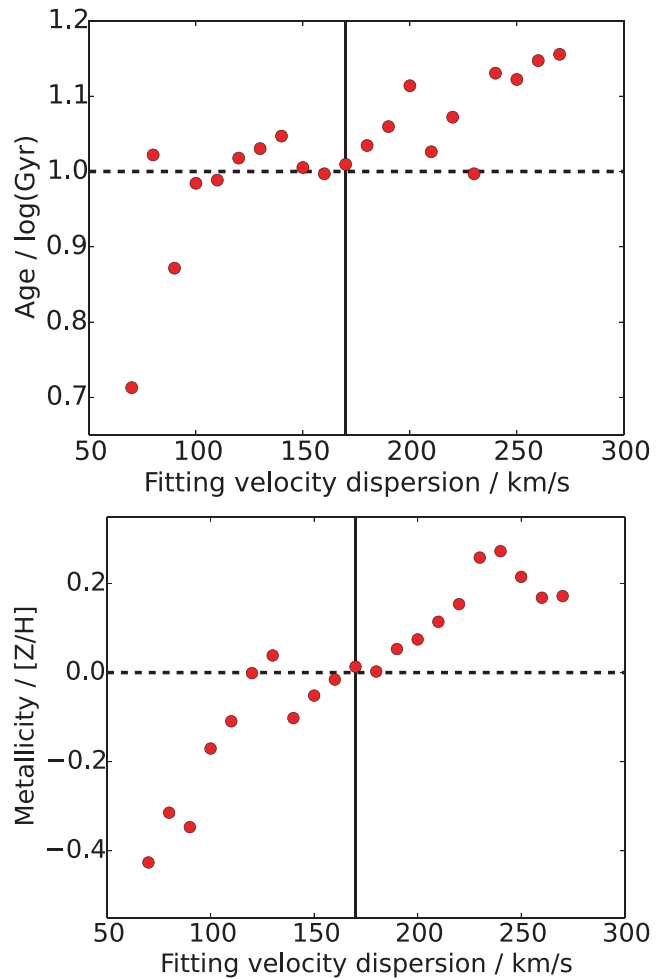
Panter et al. (2007) argue that with  $3 \text{ \AA}$  spectral resolution models and data, there is only negligible effects of velocity dispersions on their model fitting. Hence, their fitting code VESPA (see Section 4.4.3) assumes a typical galaxy velocity dispersion of  $170 \text{ km s}^{-1}$  (for the SDSS data) and downgrades models to this resolution accordingly (Tojeiro et al. 2009). However, our models use somewhat higher spectral resolution and we may in the future apply our code to even higher spectral resolution data, so this assumption should be carefully tested.

To this end, we constructed a ‘mock’ galaxy spectrum consisting of a 10 Gyr, solar metallicity SSP with a velocity dispersion of  $170 \text{ km s}^{-1}$  from MILES-based M11 models. We then run FIREFLY using 21 sets of the same M11 models, but assume velocity dispersions from 70 to  $270 \text{ km s}^{-1}$ , in  $10 \text{ km s}^{-1}$  intervals. Fig. 6 shows the corresponding age and metallicity recovered when using each of these sets of models. Both panels of the figure show an underestimate in the age and metallicity recovered when using a model velocity dispersion lower than the true one from the data, and an overestimate in the age and metallicity recovered when using a model velocity dispersion higher than the true velocity dispersion of the data. The effect in age is somewhat small in a  $\pm 50 \text{ km s}^{-1}$  range around the correct value, but beyond this varies by about 0.1 dex for every  $20 \text{ km s}^{-1}$  offset, going some way to support the argument of Panter et al. (2007). However, the effect on metallicity is much more pronounced, with no clear stable region of correct metallicity recovery and instead a  $\sim 0.1$  dex displacement for every  $30 \text{ km s}^{-1}$  offset from the true input value. This effect on metallicity was also found in Koleva et al. (2008) and Sánchez-Blázquez et al. (2011), where it was described as the ‘metallicity–velocity dispersion degeneracy’.

From these tests, we conclude that taking into account the true velocity dispersion is required to within  $10 \text{ km s}^{-1}$  velocity dispersion accuracy in order to avoid a  $\sim 0.03$  dex systematic error in metallicity, although this requirement is less strict for accurate age determination. This result makes intuitive sense, as one of the main effects of velocity dispersion is broadening metallic absorption lines.

### 3.6 Comparing multiple solutions of a fit

Models are fit to data by comparing fluxes at the same wavelength. To test the goodness of each of the model fits to the data at each



**Figure 6.** Recovery of age and metallicity of a 10 Gyr, solar metallicity SSP mock galaxy with  $170 \text{ km s}^{-1}$  velocity dispersion, using a range of input model velocity dispersions.

stage of our fitting procedure, we use a chi-squared test, given by:

$$\chi^2(\text{model}_i | \text{data}) = \sum_{\lambda} \frac{(F_{\text{data}}(\lambda) - F_{\text{model}_i}(\lambda))^2}{\sigma(\lambda)^2}, \quad (6)$$

where  $F$  represents the flux of the data or of model, and  $\sigma$  represents the error at the wavelength point  $\lambda$ . Using our method, we obtain a range of fits with chi-squared values that are usually close to each other (typically within a few per cent of the minimum chi-squared value), which are represented by the bottom set of fits in the schematic of Fig. 4. For our set of models, we typically have of order 1000 of these fits, all expressed as a linear combination of SSPs, as in equation (3). To compare these fits in a statistically meaningful way for individual galaxies, we must compute the cumulative likelihood function of the chi-squared probability distribution, given by:

$$P(X = \chi_o^2) = \int_{\chi_o^2}^{\infty} \frac{1}{2^{(k/2)} \Gamma(\frac{k}{2})} X^{(k/2)-1} e^{-X/2} dX, \quad (7)$$

where  $\Gamma$  is the Gamma function,  $\chi_o^2$  is the value of chi-squared we are using to find the probability density.  $k$  is the degrees of freedom, which can be expressed as  $k = N - \nu - 1$ , where  $N$  is the number of (independent) observations, and  $\nu$  is the number of fitting parameters. Hence, for our method,  $N$  is the number of data flux points that we are fitting model fluxes to (of order 1000 for typical resolution and wavelength coverage of SDSS observations), and  $\nu$  is the number of SSPs,  $n_{\text{SSP}}$ , used in linear combination to

**Table 1.** Parameter space of the set of Maraston & Strömbäck (2011) stellar population models used in this paper. For a given IMF, M11–MILES, M11–STELIB, and M11–ELODIE collect 159, 85, and 132 SSP models, respectively. These and other models are available at <http://www.maraston.eu/M11>.

Model	Wavelength coverage (min – max)/Å	Age coverage (min – max)/Gyr	Age grid <i>N</i> ages	Metallicity [Z/H]	HB morphology
M11–MILES	3500–7429	5–15	11	[–2.3]	Red
		5–15	11	[–2.3]	Blue
		2–15	14	[–1.3]	Red
		2–15	14	[–1.3]	Blue
		0.055–15	34	[–0.3]	Red
		0.0065–15	50	[+0.0]	Red
M11–STELIB	3201–7900	0.2–15	24	[–0.3]	Red
		0.03–15	39	[+0.0]	Red
		0.4–15	22	[+0.3]	Red
		3201–7900			
M11–ELODIE	3900–6800	6–15	10	[–2.3]	Red
		6–11	6	[–2.3]	Blue
		0.055–15	34	[–0.3]	Red
		0.003–15	57	[+0.0]	Red
		0.1–15	25	[+0.3]	Red

obtain our fit (which will vary according to the model library and any prior on which SSPs to include, cf. Table 1).

This method relies on two assumptions. First, that the fluxes and their errors are independent. This is not true for most spectroscopic surveys, such as SDSS, as fluxes from nearby pixels and their errors are somewhat correlated. Fortunately, this effect is small, on the order of the full-width at half-maximum of the instrument plus detector (see Bolton & Schlegel 2010, who also show how modern calibration methods could reduce this effect further). This means that the  $\chi^2$  values computed from model fitting are approximately statistically correct. In any case, in FIREFLY we will only output the probabilities relative to the best fit, which will be affected much less than the absolute  $\chi^2$  values. Therefore, we can safely neglect this effect, especially because we use a spectrum covering a wide wavelength range. Secondly, we assume that our method explores the parameter space close to the position of the minimum  $\chi^2$  value well, and this can be readily demonstrated by calculating the probabilities of similar fits.<sup>5</sup>

The flux of the final solution of the spectral fit of the galaxy is the sum of all the fluxes of the solutions weighted by their likelihoods as:

$$F(\lambda) = \sum_i^{\text{fits}} \frac{P(\chi^2(i))F_i(\lambda)}{\sum_i P(\chi^2(i))}, \quad (8)$$

where  $F_i(\lambda)$  is the flux of an individual solution as described in equation (3). This can then be plotted as a complete spectral fit.

### 3.7 Galaxy properties and confidence intervals

We provide best-fitting physical properties and their confidence intervals for each object. For each SED analysed, we recover the likelihood distributions of galaxy properties. The best fit for each property is the peak of its distribution, with confidence intervals determined by the range of values within a given likelihood value. For example, 68 per cent confidence intervals in age are extracted by finding the minimum and maximum values of age that have at least 68 per cent likelihood, relative to the best solution. Consider

for example, the lower plots of Fig. 7, in which we show likelihood as a function of age. The 68 per cent confidence interval in this case encloses all ages with that likelihood or higher, which in this case is about 9.7–10.0 in  $\log(t/\text{yr})$ . We provide the best fit and its 68 per cent, 95 per cent, and 99.7 per cent confidence intervals for all stellar population properties as default in FIREFLY’s output.

We note that the estimated error is based on a single SED rather than a Monte Carlo simulation based on many realizations of the SED, which is much more computationally expensive. Our method provides a fast way of measuring the spectral degeneracies between the stellar population properties based on the input data SED errors, in addition to the best-fitting set of properties based on this single SED. The exception to this method of evaluating model degeneracies is the dust calculation, hence the  $E(B - V)$  values, as computed in Section 3.3, are not folded into these error estimates. In the next section, we explain which types of average galaxy properties we determine and make available.

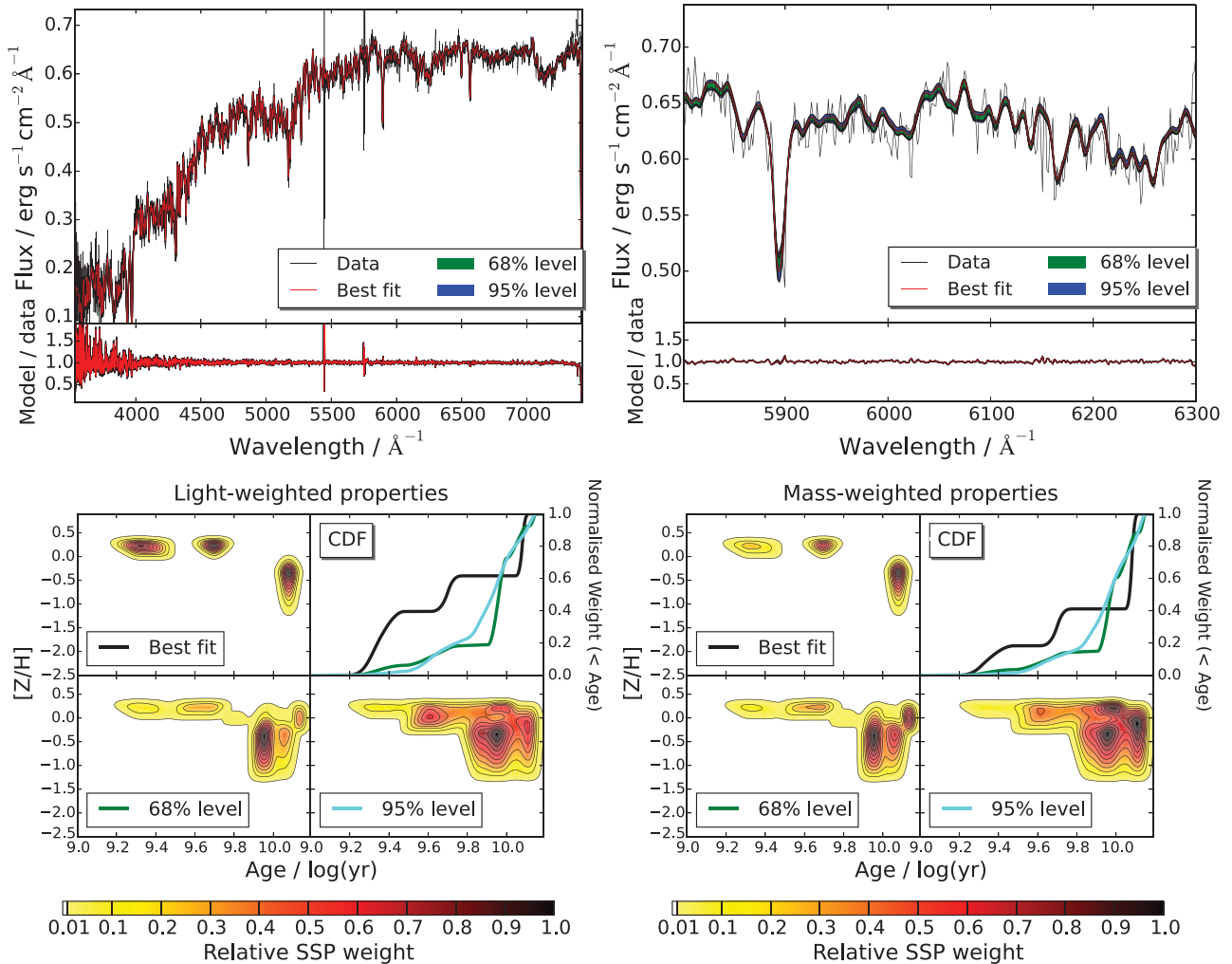
#### 3.7.1 Light- and mass-weighted properties

In the process of finding the contributions of stellar generations to an overall galaxy spectral fit, we normalize data and model fluxes before fitting and only fit for the spectral shape and features. Therefore, the contributions of SSP models initially obtained after a FIREFLY fit are ‘flux-weighted’ or ‘light-weighted’, which we shall identify as  $w_i^L$ ,<sup>6</sup> where  $i$  is the  $i$ th SSP contribution. This is a common procedure among fitting methods (see e.g. STARLIGHT; Cid Fernandes et al. 2005 and STECKMAP; Ocvirk et al. 2006b). Light-weighted contributions are converted back into mass-weighted contributions after fitting as we know the relative fluxes of the models (in units of luminosity per stellar mass) compared to the data, which are the normalization factors of models to data.

We derive both mass- and light-weighted properties since they can both be useful and complement each other well, identifying different processes more clearly. For example, recent star formation will dramatically reduce the light-weighted stellar age due to

<sup>5</sup> See David. M. Wilkinson PhD thesis, University of Portsmouth.

<sup>6</sup> We adopt *light* as this is generally used, but it is important to understand that light here refers to the SED shape, and not to the amount of  $\text{erg s}^{-1}$ .



**Figure 7.** Top panels: example total fit (red) of a typical SDSS DR7 galaxy SED (black) with 68 per cent and 95 per cent confidence intervals in shaded green and blue, respectively, with the residuals plotted underneath. In the left-hand panel, we show the entire spectral range, and in the right-hand panel, to aid visualization of the confidence intervals, we zoom in to the 5800–6300 Å region. Bottom panels: light- and mass-weighted age–metallicity maps, each containing the best-fitting solution, and the sum of solutions within the 68 per cent and 95 per cent confidence intervals. Darker contour regions correspond to higher weights of the base model SSPs found in the fits. We also apply some interpolation of the order of the sampling scale in age and metallicity of the SSPs. The age–metallicity degeneracy is visible in the spread of SSP weight contours, particularly in the island of low age, high-metallicity solutions away from the dominant ones around half-solar metallicity. This is especially visible in the spread of solutions at higher confidence intervals. In the top right sub-panels of the contours, we show the cumulative distribution function of stellar age for each of the solution sets by marginalizing the contour plots over metallicity. All plots in this figure are based on FIREFLY’s fits using M11–MILES models with a Kroupa IMF on the same SDSS galaxy.

the high luminosity of massive stars, even when it pertains to a very small mass component. Conversely, small or negligible differences in light- and mass-weighted properties will testify a small age difference between the various stellar generations, ultimately approaching a single burst of star formation. Moderate differences can therefore be interpreted as more or less extended episode(s) of star formation.

Mass-weighted properties are calculated from the light-weighted properties by the normalization factors that were used initially to match models on to data. Data fluxes are measured in units proportional to  $[\text{erg s}^{-1} \text{Å}^{-1} \text{cm}^{-2}]$ , whereas model fluxes are actually luminosities hence are measured in  $[\text{erg s}^{-1} \text{Å}^{-1} M_{\odot}^{-1}]$ , and scaled to  $1 M_{\odot}$ .<sup>7</sup> Hence, the contribution of each of the SSP fits in terms

of stellar mass will be calculated using the normalization factors of models on to data obtained before fitting (see Fig. 3). We save the values of the normalization in FIREFLY for each SSP in the model library, which we shall henceforth call ‘ $N_{M/D}$ ’:

$$N_{M/D}^{\text{SSPi}} = \frac{\sum_{\lambda} L[\text{SSPi}]}{\sum_{\lambda} \phi[\text{Data}]}, \quad (9)$$

where  $L[\text{SSPi}]$  is the  $i$  – SSP (model) luminosity and  $\phi[\text{Data}]$  is the observed flux. The units of  $N_{M/D}$  are therefore  $[\text{cm}^2 M_{\odot}^{-1}]$ .<sup>8</sup> Note that the summation corresponds to adding up fluxes or luminosities for all available wavelength data points between a defined upper and lower limit. Where possible, these wavelength limits should also be consistent when comparing models such that any systematic effect of changing the wavelength range on the stellar mass determination

<sup>7</sup> Scaling to 1 solar mass is true for the standard output of the Maraston’s models, other models may use different units.

<sup>8</sup> For example, the specific units for SDSS are  $[10^{17} \text{cm}^2 M_{\odot}^{-1}]$ .

is reduced (see Pforr, Maraston & Tonini 2012). The mass-weighted contribution of each SSP will then be:

$$w_i^M = \frac{w_i^L}{N_{\text{SSPi}}^{M/D}} = w_i^L \times \frac{\sum_\lambda \phi[\text{Data}]}{\sum_\lambda F[\text{SSPi}]}, \quad (10)$$

where the  $w_i^M$  and  $w_i^L$  are the mass and light weights, respectively. This expression will therefore be in units of  $[M_\odot \text{ cm}^{-2}]$ . The flux from the data can be converted to a luminosity knowing the object's redshift hence, assuming a cosmological model, its luminosity distance  $D_L$  (in centimetres), via  $L = 4\pi D_L^2 \times \phi$ . Hence, we can now convert the luminosity-weighted contributions into mass-weighted contributions as:

$$\begin{aligned} M_{\text{SSPi}} &= w_i^M \times 4\pi D_L^2 \\ &= 4\pi D_L^2 \times w_i^L \frac{\sum_\lambda \phi[\text{Data}]}{\sum_\lambda L[\text{SSPi}]}, \end{aligned} \quad (11)$$

which is in units of  $[M_\odot]$ .

### 3.7.2 Total stellar mass and mass contributions

At the end of the fitting procedure we provide global properties, such as the total mass. The total mass (stellar plus gas) is simply given by the sum of all the SSP weightings:

$$\begin{aligned} M_{\text{stellar}}^{\text{tot}} &= \sum_i M_{\text{SSPi}} \\ &= \sum_i (w_i^M) \times 4\pi D_L^2 \\ &= 4\pi D_L^2 \sum_i \left( w_i^L \frac{\sum_\lambda \phi[\text{Data}]}{\sum_\lambda L[\text{SSPi}]} \right). \end{aligned} \quad (12)$$

In addition to this, we also breakdown the total mass into more detailed segments, such as the contribution from living stars, stellar remnants, and the gas that was ejected via stellar mass losses. This information is provided in tables by the models used in this work (at <http://www.maraston.eu>). The contributions depend on the assumed IMF (see next section) and on the analytical prescriptions relating the initial stellar mass and their product remnant. They also depend on age, and little on metallicity (see Maraston 1998, 2005).

## 3.8 Input and output of FIREFLY

In order to run FIREFLY, the following needs to be provided as input quantities:

- (i) Object's spectrum;<sup>9</sup>
- (ii) Object's velocity dispersion ( $\sigma$ );
- (iii) Object's redshift;
- (iv) Input stellar population models;
- (v) Wavelength range for the fit.

The models will be downgraded to the actual object's (galaxy) velocity dispersion ( $\sigma$ ) after being downgraded, if necessary, to the data spectral resolution (i.e. the combination of the specific instrument resolution and intrinsic object's dispersion) using a routine developed in Thomas et al. (2013). Average fitting times for a single spectrum are  $\sim 1$  min on a standard computer. The default output of FIREFLY is:

- (i) Input model and fitting parameters (stellar library, IMF, wavelength range, etc.), galaxy's  $\sigma$  and redshift;
- (ii) Light weights of each SSP entering the average solution;
- (iii) Mass weights of each SSP entering the average solution;
- (iv) Light- and mass-weighted averaged age and errors;
- (v) Light- and mass-weighted averaged metallicity and errors;
- (vi) Best-fitting spectrum;
- (vii)  $\chi^2$  of the average solution;
- (viii)  $E(B-V)$  (with the adapted method described in Section 3.3.1) of the average solution;
- (ix) Total stellar mass, its fractions in stellar remnants, mass in gas.

The above outputs provide a large amount of information which should be useful in robustly determining galaxies SFHs.

## 3.9 Visualization of spectral fits and physical properties

Fig. 7 visualizes the full spectral fitting result. The final fit is a composite model containing the galaxy properties we need to know to perform galaxy evolution studies. Given the large number of contributing solutions, we need an effective way to extract them and visualize them. In the left-hand panel, we show the total fit, i.e. the weighted sum of all contributions (red line) overplotted to the empirical spectrum (black line), for an SDSS typical galaxy (see Section 6). The total fit includes all possible solutions as in equation (8), in this case  $\sim 2000$ . The right-hand panel is a zoomed-in version in the 5800–6300 Å region. In the bottom panels, we show the light- and mass-weighted age–metallicity maps, each containing the best-fitting solution, and the sum of solutions within the 68 per cent and 95 per cent confidence intervals. Darker contour regions correspond to higher weights of the base model SSPs found in the fits.

The age–metallicity degeneracy is visible in the spread of SSP weight contours, particularly in the island of low age, high-metallicity solutions away from the dominant ones around half-solar metallicity. This is especially visible in the spread of solutions as one considers higher confidence intervals. In the top right-hand sub-panels of the contours, we show the cumulative distribution function of stellar age for each of the solution sets by marginalizing the contour plots over metallicity. The main difference between light- and mass-weighted contributions is the emphasis of the former towards the youngest population ages, which provide substantial light even when in negligible mass proportions.

## 4 COMPARISON TO OTHER FITTING CODES

In this section, we compare the methodology of FIREFLY to that of other popular SED fitting codes. We reserve a comparison of results to Section 6. As mentioned in the Introduction, there are other fitting codes that could be described in this section, however our focus here is on widely used codes which have publicly available results for SDSS galaxies.

### 4.1 STARLIGHT

STARLIGHT (Cid Fernandes et al. 2005) is a  $\chi^2$ -minimization full spectral fitting code that, as FIREFLY, uses a base of SSPs as its input. However, rather than iteratively adding SSP contributions directly, STARLIGHT explores the parameter space by finding an approximation to the minimum  $\chi^2$  solution, further fine-tunes the result, and then projects the base SSPs into coarser components. Since we save a large range of fits and weight them by their final likelihood, we

<sup>9</sup> Note that if the object contains emission lines and the models do not, the spectral fit may not be able to accurately recreate the data. This effect is discussed in Appendix A. FIREFLY allows for the masking of emission lines as an input keyword.

effectively smooth out our SFHs across all of the fits, and so instead of requiring this base projection in order to get a realistic and stable combined fit we effectively sum over all possible solutions. Cid Fernandes et al. (2005) also test their procedures with mock galaxies, which are tuned to match SDSS data and so reach low S/N as ours do. They test the recovery of light- and mass-weighted age and metallicity, total stellar mass, stellar velocity dispersion, and dust extinction. They report a broadly good recovery, but find it difficult to resolve the individual stellar population components, compared to our approach which works well down to an S/N of 5. We compare with the results of STARLIGHT for SDSS DR7 in Section 6.

#### 4.2 STECKMAP

STECKMAP (Ocvirk et al. 2006a,b) is a matrix inversion code also using SSPs as their base and including a penalty-based method for avoiding overfitting in a similar way to our use of the BIC. STECKMAP retrieves likelihoods similar to FIREFLY, but instead of combining a range of fits, performs smoothness over its solutions until robustness is achieved. This method is capable of achieving very precise recovery of sub-populations for high S/N data. The ability of the code to recover parameters successfully was shown in Ocvirk et al. (2006b), where a detailed analysis of single- and double-burst mock galaxies was conducted. Although the strengths of STECKMAP lie in its ability to recover parameters accurately from high S/N data, there have been studies using the code at SDSS-like S/N (see Sánchez-Blázquez et al. 2014). However, since most of their work is much more tuned for high S/N objects, and different stellar population models are used, a deeper comparison between FIREFLY and STECKMAP would prove difficult to make.

#### 4.3 VESPA

VESPA (Tojeiro et al. 2007, 2009) is an iterative  $\chi^2$ -minimization full spectral fitting code, whose stellar population model input includes both the Bruzual & Charlot (2003) and the Maraston (2005) and the M11 models. Fitting solutions are retrieved through the use of age bins that are larger than our single bursts. The age bins use a combination of continuous star formation rate models and exponentially declining star formation rate models. They also test dual-burst models, but find them to give inferior results in general. The resolution of the age bins varies depending on the number of parameters required to fit below the noise level, and thus the results strongly depend on the S/N of the data. This process is used to avoid overfitting in a similar way to FIREFLY's use of the BIC. The result of convergence in FIREFLY is to return linear combination of SSPs, and include them in many other fits (weighted by likelihood) summed together to build a SFH, whereas VESPA will return a combination of flux contributions corresponding to its age bins. Additionally, they convolve a constant  $\sigma = 170 \text{ km s}^{-1}$  stellar velocity dispersion with the Bruzual & Charlot (2003) models, compared to our approach of fitting for  $\sigma$  separately. In Section 3.5, we show the effect such an approximation has on the derived age and metallicity across a range of simulated velocity dispersion objects.

Tojeiro et al. (2007) tested VESPA using mocks obtained with exponentially declining SFH models ( $\tau$  models) with  $\tau = 0.3 \text{ Gyr}$ . They test the effect of using two different wavelength ranges (1000–9500 and 3200–9500 Å), two different S/N cases (20 and 50), and a range of dust values. It is important to note that for this value of  $\tau$ , our parameter recovery in FIREFLY is similarly very good,

even for low S/N of 5. We compare our results to those of VESPA for SDSS DR7 in Section 6.

## 5 TESTING THE FITTING METHOD

To test the validity and stability of the results obtained from FIREFLY, we run a comprehensive set of tests on two types of data; mock galaxies (with both simple and complex SFHs) and real astronomical data, comprising both globular clusters and galaxies. We use these data to assess the effect of S/N, adopted wavelength range in the fitting and SFH, and to evaluate how realistic ages, metallicities, and stellar masses derived via FIREFLY are. We push this testing to also investigate the recovery of the input SFH and reddening.

The testing using SDSS galaxies is placed in Section 6 for clarity. This latter testing allows us to compare our results with those obtained from other fitting codes in the literature and to test the effect of the input stellar library on the resulting model fit. We test both the accuracy and the precision, in terms of error, of the recovery of stellar population properties. Our work matches for full high-resolution spectral fitting the tests by Pforr et al. (2012) for broad-band spectral fitting. Throughout the next section, we show a combination of both light- and mass-weighted properties depending on which is more relevant to the data set in question. Also note that in the following, we consider the wavelength range spanned by the M11–MILES models (cf. Table 1), but we know that the extension of the SED in wavelength especially towards the near-IR matters on improving the recovery of stellar population properties (e.g. Pforr et al. 2012).

### 5.1 Effect of signal-to-noise, dust reddening, and star formation history

To test the effect of S/N, and its relation to the assumed SFH and dust reddening, we determine the recovery of stellar population properties from two types of mock galaxies based on model spectra which we have perturbed to simulate a range of S/N ratios.

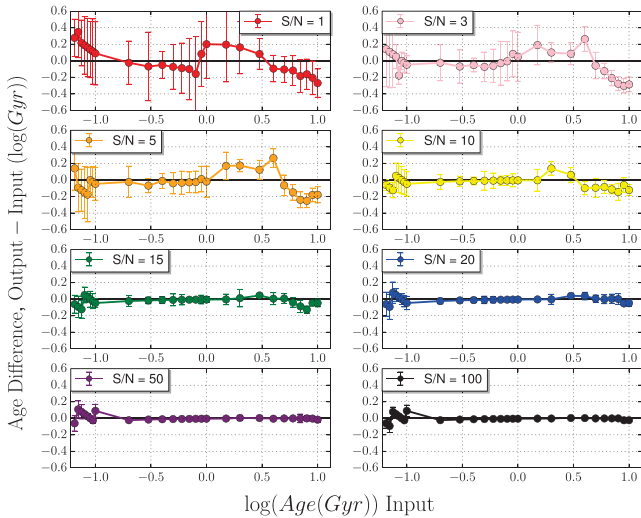
#### 5.1.1 Simple stellar populations

In the first set of tests, we use mock galaxies made from the same SSP templates used to fit to them. We adopt the M11–MILES set, since it has the largest metallicity coverage, and use the full-wavelength range available (see Table 1). We apply a Gaussian perturbation to each flux point with a flat S/N, as described by:

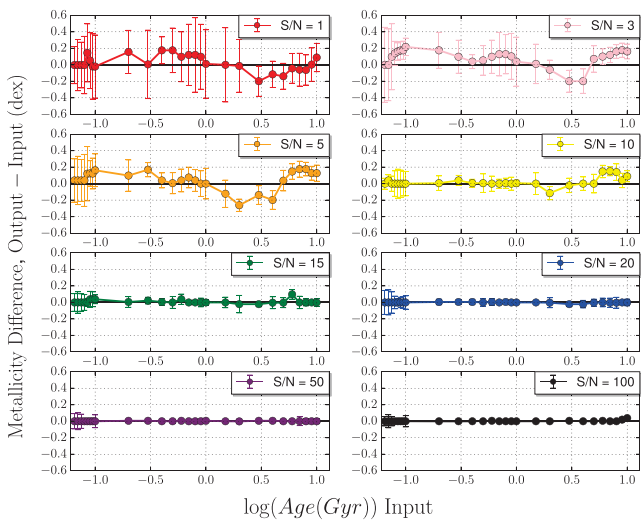
$$F_{\text{Mock}}(\lambda_i) = N \left( F_{\text{SSP}}(\lambda_i), \left( \frac{\phi_{\text{SSP}}}{S/N} \right)^2 \right), \quad (13)$$

where  $F_{\text{Mock}}(\lambda_i)$  is the individual flux point  $i$  of the mock galaxy,  $F_{\text{SSP}}(\lambda_i)$  is the flux point  $i$  of the input SSP,  $N(x, \sigma^2)$  is the normal distribution with mean  $x$  and variance  $\sigma^2$ ,  $\phi_{\text{SSP}}$  is the mean flux over the whole wavelength range of the spectrum, and S/N is the input signal-to-noise ratio. We explore S/N of 1, 3, 5, 10, 15, 20, 50, and 100. The 1–100 range covers the vast majority SDSS galaxies with higher values usually corresponding to stacked spectra. The highest S/N value case allows us to measure the intrinsic model degeneracies. For this first test, we do not include dust, which will be considered in the next section when we use composite models.

We create a Monte Carlo simulation of 100 realizations by applying these Gaussian perturbations 100 times to each SSP for each S/N bin. In Figs 8–10 we plot the age, metallicity, and stellar mass recovered as a function of SSP age for each S/N bin. Each point represents the average value of 100 realizations of that SSP, with



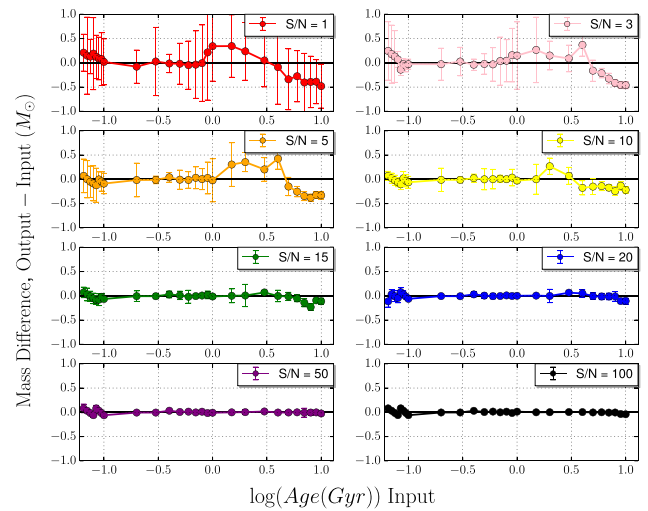
**Figure 8.** Recovery of light-weighted ages of single-burst models perturbed as to mimic eight different S/N values. Each point is the median fitted value for the 100 Monte Carlo realizations, with errors plotted as the 68 percentile (i.e.  $1\sigma$ ). Tests refer to MILES-based M11 models at the full available wavelength range available, solar metallicity and no dust.



**Figure 9.** As Fig. 8, for metallicity.

the errors measured from the standard deviation of the fitted ages. The line drawn at  $y = 0$  visualizes where the fitted property matches the input one.

Figs 8–10 report the results, for age, metallicity, and stellar mass, respectively. The recovery of the input properties is excellent for all properties, down to  $S/N = 5$ . It remains acceptable down to  $S/N = 3$  at intermediate ages, while towards old ages ( $t > 1$  Gyr), the age–metallicity degeneracy kicks in and leads to underestimating age, overestimating metallicity, and underestimating stellar mass. These results are very encouraging for our code because the code fits combinations of SSPs with dust and such a remarkable agreement for a single SSP with no dust is not trivial. We also note that when fitting the mock spectra, we always find negligible reddening, consistent with the input. However, these plots are not shown for brevity. These results will support the use of our code for low



**Figure 10.** As Fig. 8, for stellar mass.

$S/N$  populations such as those of galactic haloes or high-redshift galaxies.

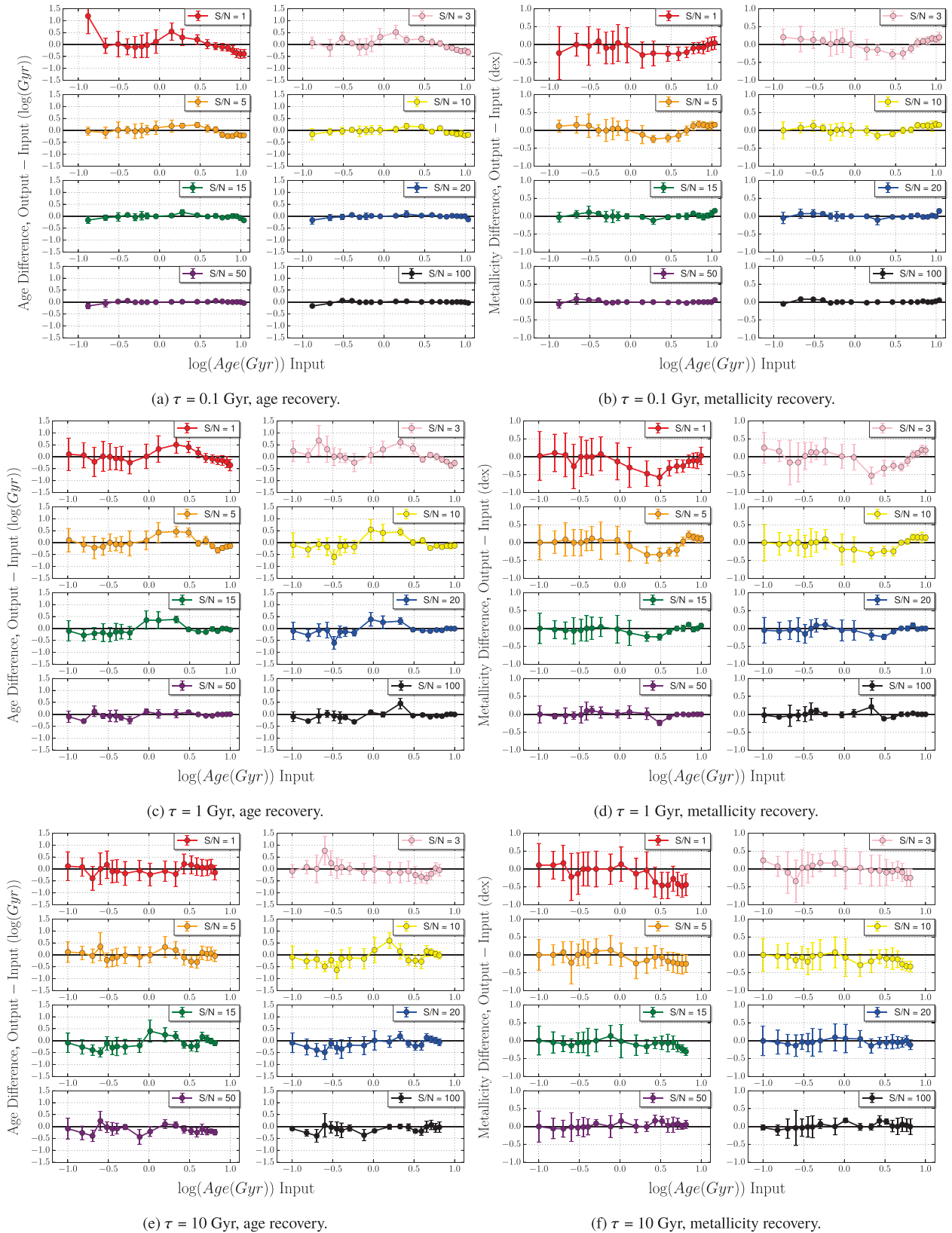
Chen et al. (2012) note that stellar masses of SDSS-III galaxies obtained by full spectral fitting of spectra with  $S/N \sim 5$  were larger than the stellar masses calculated for the same galaxies, but using broad-band spectrophotometry (as in Maraston et al. 2013). Chen et al. (2012) show that as the  $S/N$  ratio increases, the stellar mass derived from their full spectral fitting tends to approach the one they derive from broad-band photometry fitting. Our results from full spectral fitting seem more optimistic in that even at low  $S/N$ , the stellar mass is well recovered. We should note that the spectral fitting method by Chen et al. (2012) employs PCA and is overall different from the one we take here.

### 5.1.2 Extended star formation histories

In the second set of tests, we use composite models obtained with a range of exponentially declining SFHs (known as  $\tau$  models, Bruzual 1983). In  $\tau$  models, the star formation rate,  $\Phi(t, \tau)$ , is described as  $\Phi(t, \tau) \propto e^{-t/\tau}$  for  $t > 0$ , where  $t$  is the time coordinate, with star formation beginning at  $t = 0$  and  $\tau$  is the characteristic decay time. These models are commonly used in the literature for fitting to a variety of galaxy data (e.g. Longhetti & Saracco 2009; Lee et al. 2010) as a realistic mode of star formation. We investigate these models for every combination of: a range of decay times;  $\tau = 0.1, 1, 10$  Gyr, a range of times  $t$  after star formation began (24 values spanning from  $t = 0.01$  to 10 Gyr), and a range of reddening, obtained using the Calzetti’s law with dust extinction values  $A_v = 0, 0.4, 1, \text{ and } 3$ . We consider the same  $S/N$  values (from 1 to 100) as in Section 5.1.1 and we experiment with 100 Monte Carlo simulations of each single mock for the same set of  $S/N$  to test the robustness of property recovery.

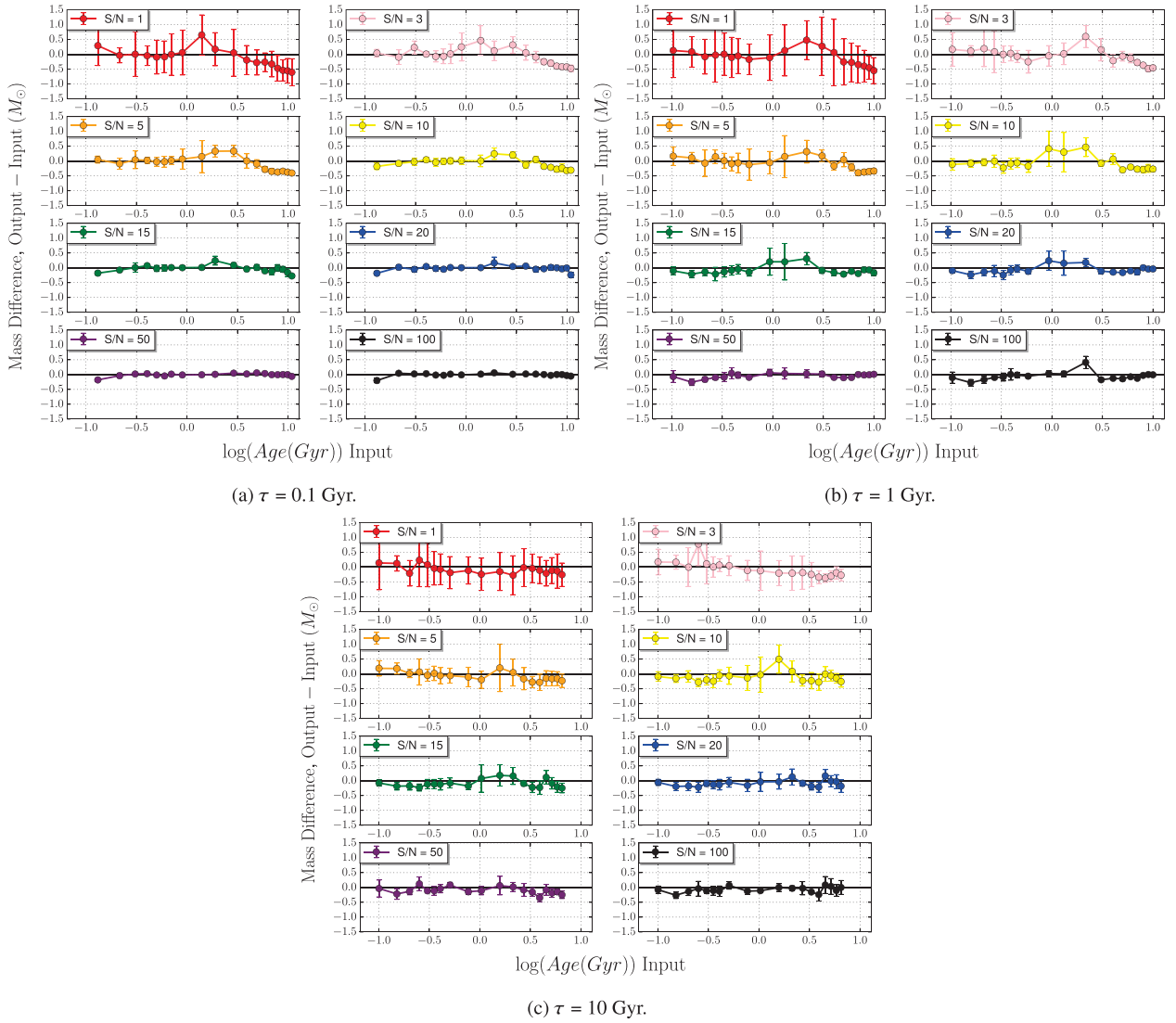
First, we show the case where the mocks do not contain intrinsic reddening in Figs 11 and 12. The results for the mocks with dust are in Figs 13–17. It is important to note that in all cases we use FIREFLY in its full mode, e.g. we fit for reddening as well. We determine the accuracy of the fitting procedure by analysing the output in terms of age, metallicity, and stellar mass, and also SFH and dust reddening.

Fig. 11 shows the recovered mass-weighted ages and metallicities (left-hand and right-hand plot series, respectively) compared to the



**Figure 11.** Recovered mass-weighted ages and metallicities (left- and right-hand plot series, respectively) from fitting mock spectra of composite stellar populations. Their input SFHs have exponentially declining star formation rates given by  $\Phi(t, \tau) \propto e^{-t/\tau}$ , for  $t > 0$ , where  $t$  is the time, since the onset of star formation and  $\tau$  is the star formation decay time or  $e$ -folding time (0.1, 1, and 10 Gyr, from top to bottom). Solutions are plotted at different of S/N ratios (from 1 to 100).





**Figure 12.** As in Fig. 11, for the recovered stellar mass.

input mass-weighted ages, as a function of S/N, from 1 to 100, for the three  $\tau$ -models with  $\tau = 0.1, 1,$  and 10 Gyr (from top to bottom).

We find that FIREFLY is able to recover remarkably well both ages and metallicities, down to low S/Ns ( $S/N \sim 5$ ) and for a wide range of extended SFHs. The recovered metallicity shows some scatter, well within 0.2 dex at  $S/N > 10$ . As in case of single-burst populations, old ages at low S/N are the most difficult to recover, with ages getting overestimated (around 1 Gyr), then underestimated (after  $\sim 3$  Gyr), with an opposite trend displayed by metallicity, i.e. an overestimation of age is generally accompanied by an underestimation of metallicity. No exact quantitative correspondence should be sought between the two offsets because of the additional parameter (reddening) which is considered in the fitting.

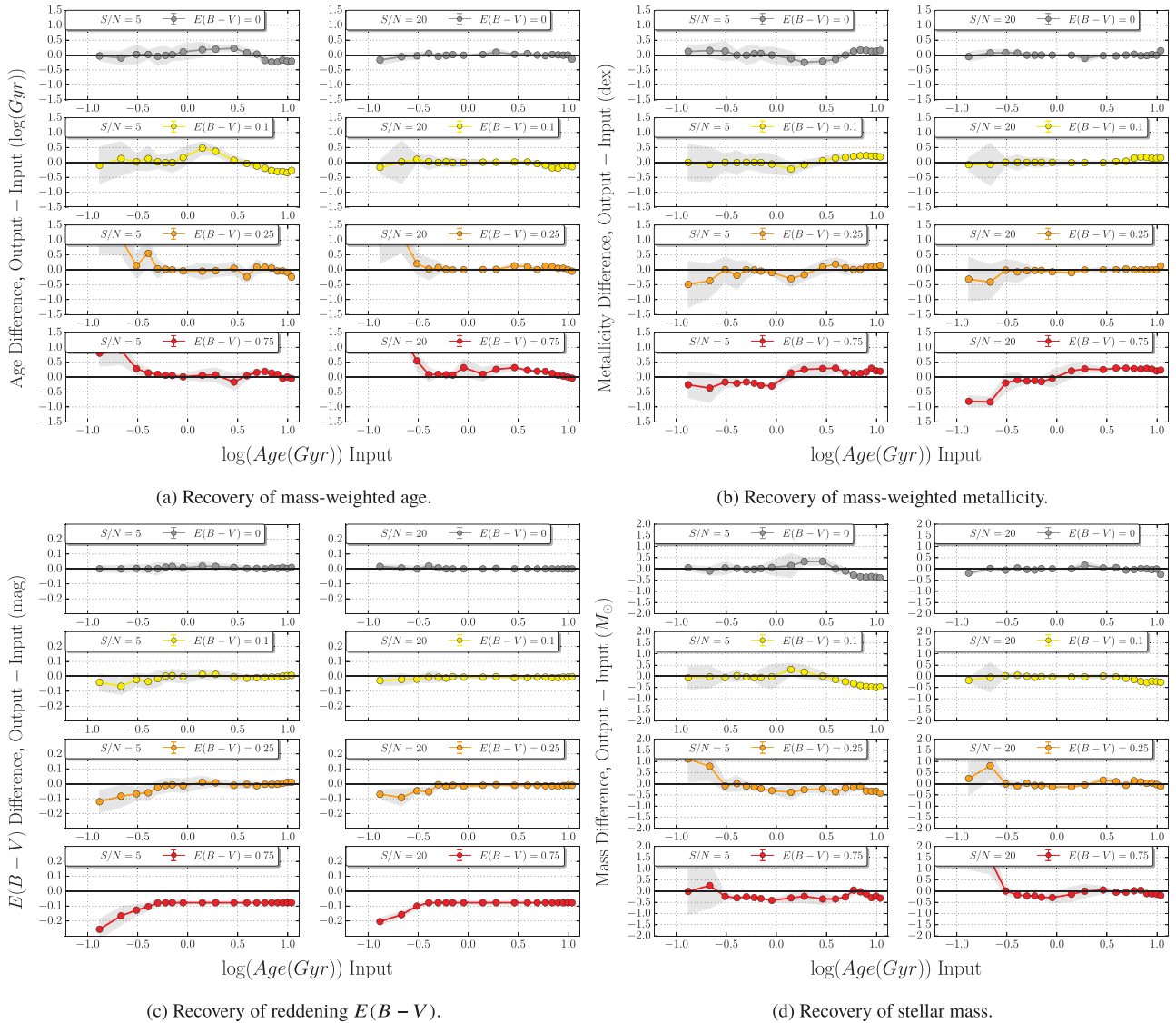
As  $\tau$  increases, we find a larger scatter in the recovered properties (larger error bars around the median). This is expected as more extended SFHs allow more room for degeneracies to creep in and hence properties become more difficult to recover.

Fig. 12 shows the recovery of stellar mass, in terms of the difference between input and output stellar masses (y-axis), as a function of the mass-weighted age (x-axis), for the same models and S/N ra-

tios as in Fig. 11. The recovery of stellar mass in this case of mocks without reddening is remarkably good down to low S/N ratios. Trends in mass are primarily mirroring those in age, due to the age evolution of the mass-to-light ratio.

Figs 13–15 show the recovery of mass-weighted age and metallicity, dust reddening, and stellar mass, for each of the three  $\tau$ -models (ordered as 0.1, 1, and 10 Gyr), two values of S/N (5 and 20), and four values of  $E(B - V)$  (0, 0.1, 0.25, and 0.75). Note that while the no-reddening case was already shown in previous figures, we keep it here to allow a fast evaluation of reddening effects.

We see that at the highest  $S/N = 20$ , all properties are recovered well nearly independently of  $\tau$  and reddening, with the shortest  $\tau$  and the lowest reddening being the most favourable cases, as one may expect. This is nonetheless, a remarkable result. At the highest  $E(B - V) = 0.75$ , with the more extended SFH, the accuracy of recovered properties, especially age and reddening, degrades, with for example the youngest ages being overestimated and the reddening underestimated (the well-known age–dust degeneracy). Considering that such a high reddening is pretty rare in nature, these results are not generally a concern, but it is important to understand the limitations of the procedure.



**Figure 13.** Recovered mass-weighted age, metallicity, reddening  $E(B - V)$ , and stellar mass, for input composite stellar populations including intrinsic reddening, with  $E(B - V) = 0, 0.1, 0.25,$  and  $0.75$ , for two median  $S/N$  of 5 (LHS) and 20 (RHS). This figure refers to a  $\tau = 0.1$  exponentially declining SFH.

Metallicity seems to be the most robust among all properties, although this might also be due to the fact that our mocks are calculated for a single (solar) metallicity, followed by mass, whose accuracy primarily depends on the accuracy of age. We note that reddening seems systematically underestimated, at the lowest ages. We shall investigate this event in future developments of FIREFLY, by allowing reddening to be fit as a free parameter.

At lower  $S/N = 5$  properties are recovered well in the regime of low-reddening ( $E(B - V) < 0.25$ ), whilst at this value and above scatter up to 0.5 dex is observed, for example with age overestimated and reddening underestimated. These effects compensate each other in most cases such that the stellar mass remains pretty well determined even in these less favourable regimes.

Last, we consider the recovery of the SFH in Figs 16 and 17. Here, we plot our reconstructed SFHs in terms of SSP weights as a function of the mass-weighted age, and we overlay the input SFH as a smooth curve (red dashed lines). Each sub-figure contains results for the shortest  $\tau$  (0.1 Gyr) in the upper row, and the longest  $\tau$  (10 Gyr) in the lower row, for three reddening values, increasing

from left to right. Each double plot refers to a different  $S/N$ , namely 5, 20, and 50.

Fig. 16 reports the case where the mock spectra are viewed 1 Gyr after the start of star formation, hence one should expect to find only populations younger than this limit in the ideal case. Fig. 17 refers to 10 Gyr after the starting of star formation, hence one should expect a larger spread in ages at the largest  $\tau$ .

These trends are exactly found in the plots. The recovery of the input SFH is very good at  $S/N = 20$  for both short and long  $\tau$  and for a range of reddening. At  $S/N = 50$ , the recovery is basically perfect for the shortest  $\tau$  independently of reddening and formation epoch. Note also the shift in the fitted ages passing from the 1 to the 10 Gyr start of star formation, as in the input SFH. The fraction of SSPs formed are not in precise agreement with the smooth curve in the case of the long  $\tau$ , but the range of possible ages is generally well matched and one should also note that such a long  $\tau$  is a quite complicated case.

In conclusions, these tests give us confidence on a good to excellent performance of FIREFLY in simple or complex cases, down to a

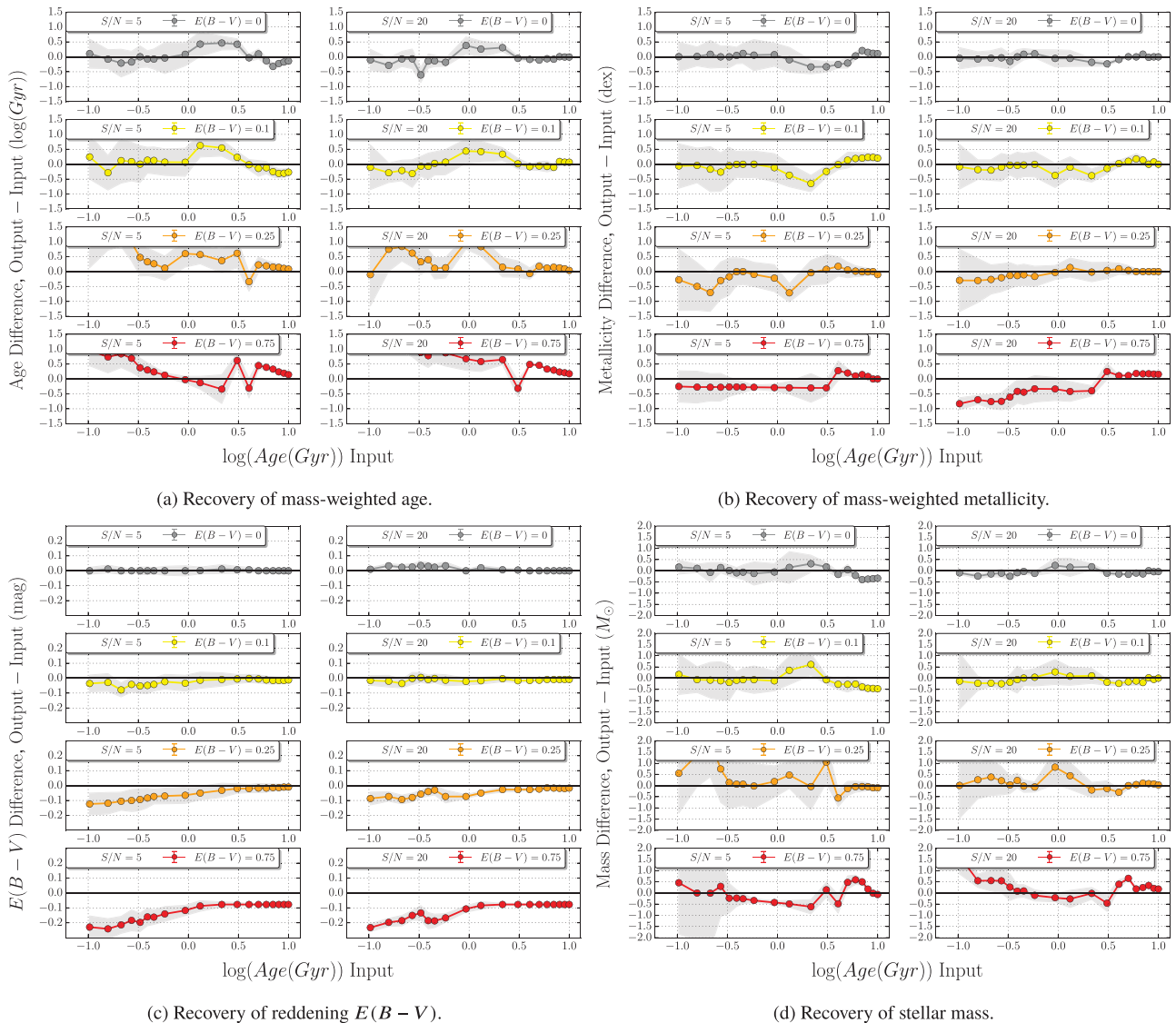


Figure 14. As in Fig. 13 for a  $\tau = 1$  Gyr exponentially declining SFH.

remarkably low S/N and also in presence of reddening. Particularly good is the recovery of the SFH.

## 5.2 Effect of wavelength range

Here, we test the effect of the wavelength range adopted in the fitting procedure on the derived properties, focusing on age and metallicity. These tests are useful to directly probe the degeneracies of the model components and calibrate the fitting setup. We use as test populations the spectrum of the M67 star cluster, whose age is independently known, and mock galaxies as in the previous sections, whose ages and metallicity are a well-defined input.

### 5.2.1 M67

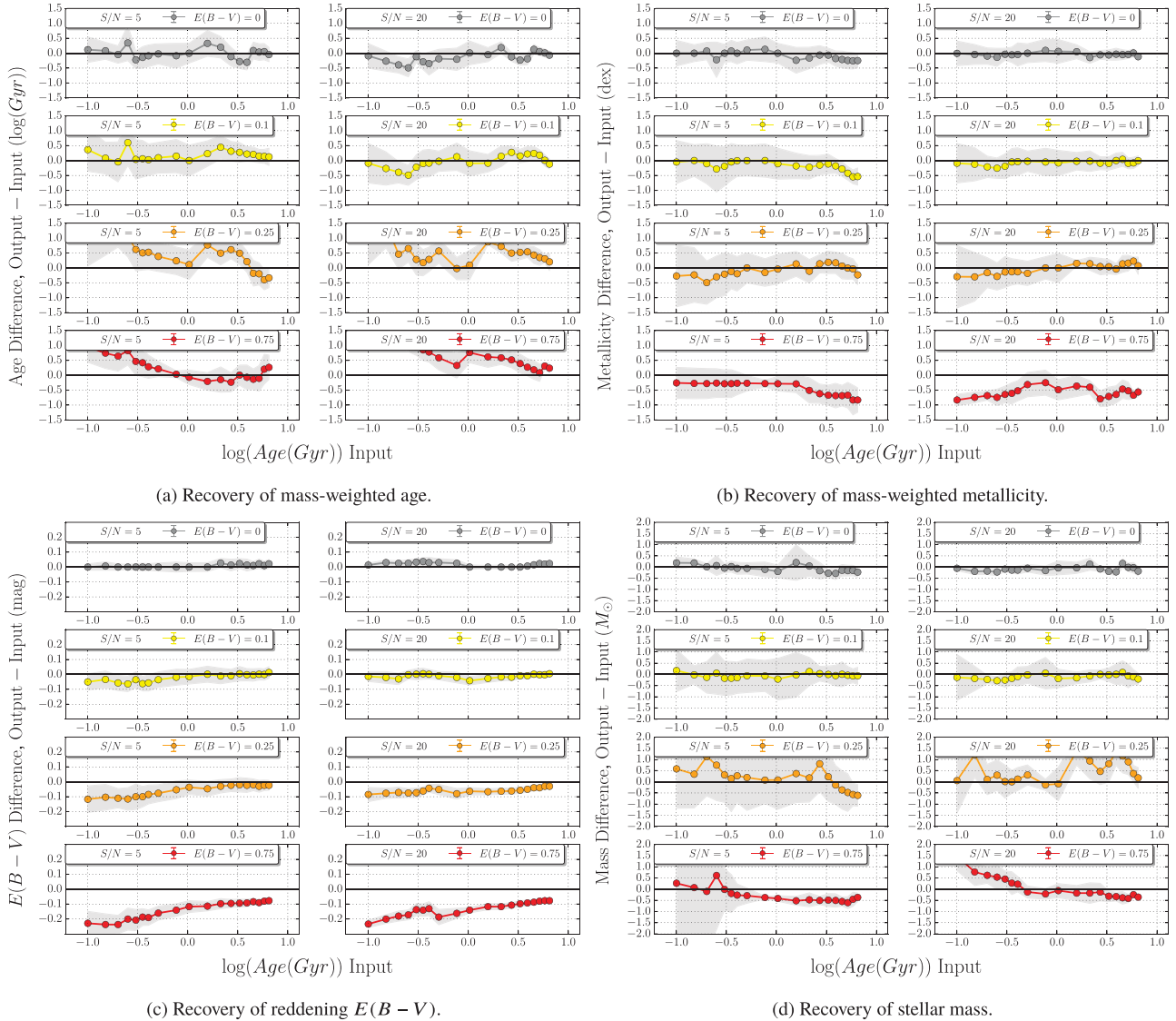
The wavelength range used for the best fits in Fig. 2 was the maximum used by the data (3650–5350 Å) or the models. Here, we test the effect on the derived age of choosing a smaller wavelength range, and we also study the effect as a function of the model input empirical stellar library. We focus on age as it is independently

known from CMD fitting. The results are shown in Fig. 18, where we have fitted with full freedom of SSPs and combinations of fits. CMD-consistent ages are those plotted in light yellow (cf. vertical colour bars).

Looking first at the whole wavelength spanned, MILES-based models give most often the most accurate solutions, finding that for many regions of the figure, the age determined is exactly correct, with about 0.1 dex spread in values for large wavelength ranges. STELIB-based models have more variance in the ages recovered, about 0.2 dex, but generally find accurate solutions. ELODIE-based models generally overestimate the age by about +0.2 dex.

The following features related to wavelength are noted:

- (i) STELIB-based models release the most consistent fits that are also CMD-consistent when using a relatively small, blue wavelength range (around 3900–4300 Å): this is the well-known D-4000 Å break (see below);
- (ii) MILES- and ELODIE-based models release CMD-consistent ages when a large wavelength range is used, but fails to do so when



**Figure 15.** As in Figs 13 and 14 for a  $\tau = 10$  Gyr exponentially declining SFH.

not taking account of the lower wavelength ranges (approximately below 4300 Å);

(iii) All models release ages that are too high (which correspond to metal-poor solutions) when cutting out the blue part of the spectrum (up to  $\sim 4300$  Å). In general, the models are more sensitive to the minimum wavelength range set, clearly showing that the models can discriminate the age much more clearly at low wavelengths, for SSPs such as in M67.

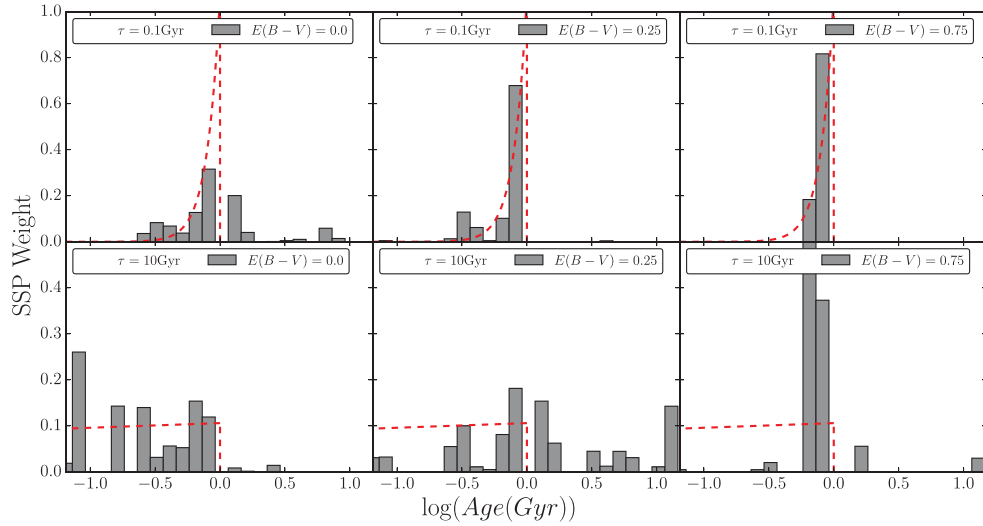
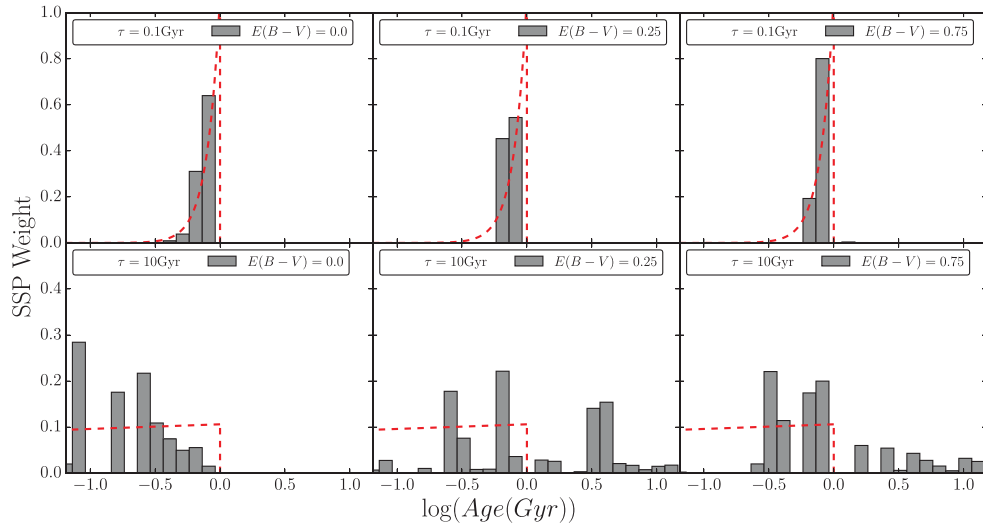
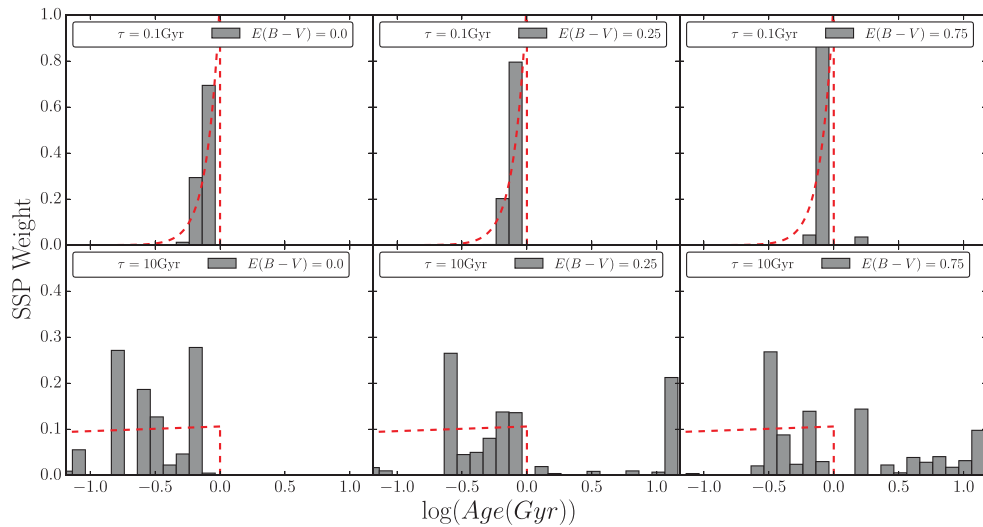
The dominant effect on the age accuracy as a function of wavelength range is the sampling of the ‘D(4000)’ (or the 4000 Å break, defined and described in Bruzual 1983), which is a spectral break generated by the onset of photospheric opacities, due to a variety of elements heavier than Helium in various stages of ionization, shortward 4000 Å. Hence, the strength of the break depends on temperature, which can be related to the age of the population, and metallicity. Therefore including this region in the analysis explains why this is a necessary wavelength region to fit in order to accurately determine the age of M67. This shows that in order to accurately trace the age of intermediate-age stellar populations, we must use

this wavelength region in any spectral fit where these stars are dominant.

### 5.2.2 Mock galaxies

To complement the above tests on a real star cluster as M67, we carry out an investigation of the effect of varying the wavelength range used to fit to the spectra, both as a function of input model SSP age and S/N. For brevity, we display only the ages and metallicities obtained from fitting solar metallicity SSPs with no dust component, using an S/N of 5 and MILES-based models. Two representative cases are shown in Fig. 19 for SSP mocks, with a very young (55 Myr) and an old (7 Gyr) input age, in the top and bottom panels, respectively.

From Fig. 19, we see two different cases of age–metallicity degeneracy. For the very young 55 Myr mock, we see that in general, the recovered ages are overestimated ( $\sim 0.3$  dex), while the metallicities are very well determined, being only slightly underestimated ( $\sim 0.01$  dex). These effects worsen when the wavelength range is smaller. Conversely, the 7 Gyr mock shows that as long as one


 (a) Simulations at  $S/N = 5$ .

 (b) Simulations at  $S/N = 20$ .

 (c) Simulations at  $S/N = 50$ .

**Figure 16.** Recovery of SFH, for input mocks with  $\tau=0.1$  and 10 Gyr (upper and lower rows, respectively), 1 Gyr after the starting of star formation, as a function of reddening, increasing from left to right, for three  $S/N$  ratios. Red, dashed lines show the input SFHs as smooth curves.

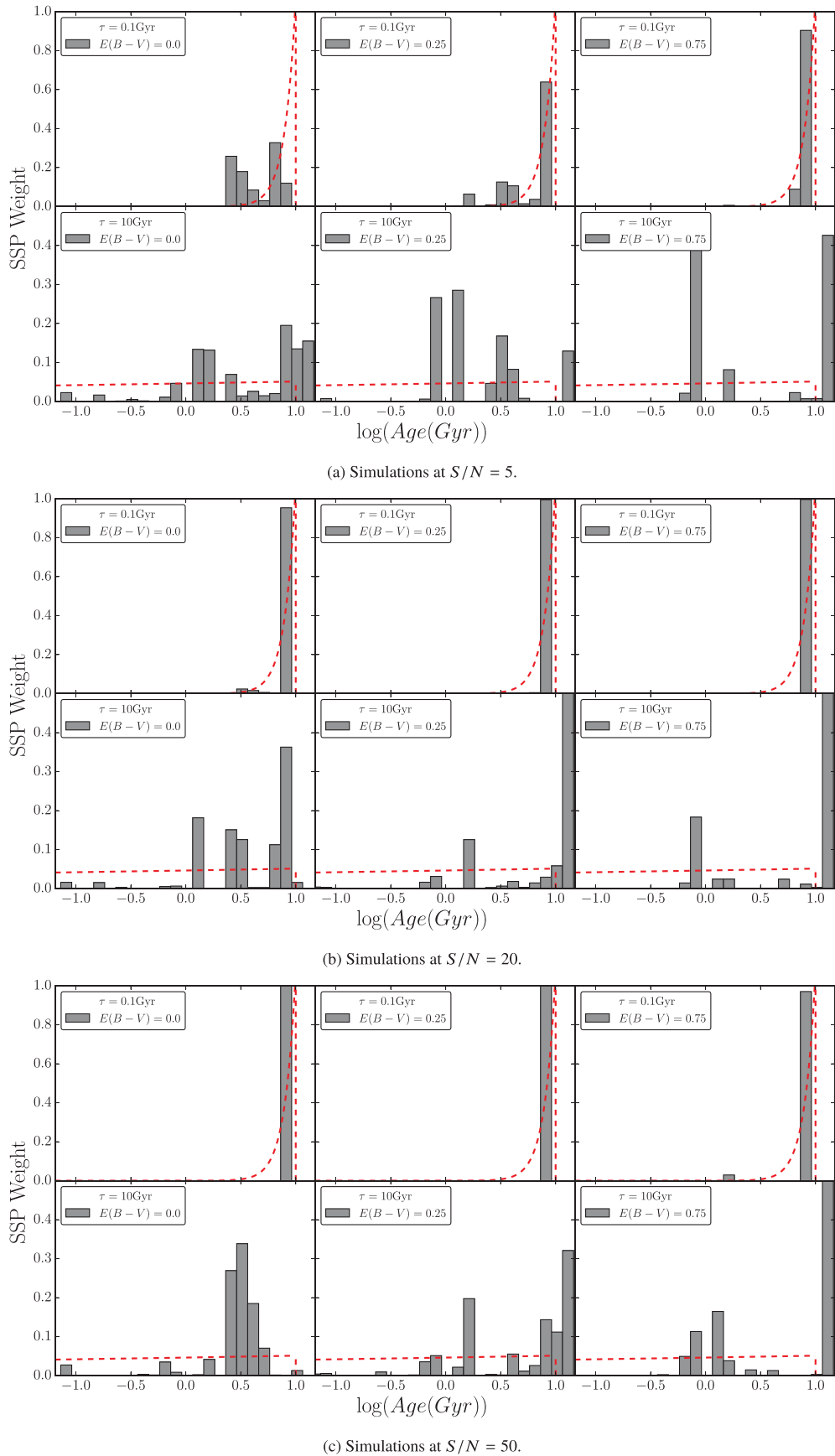
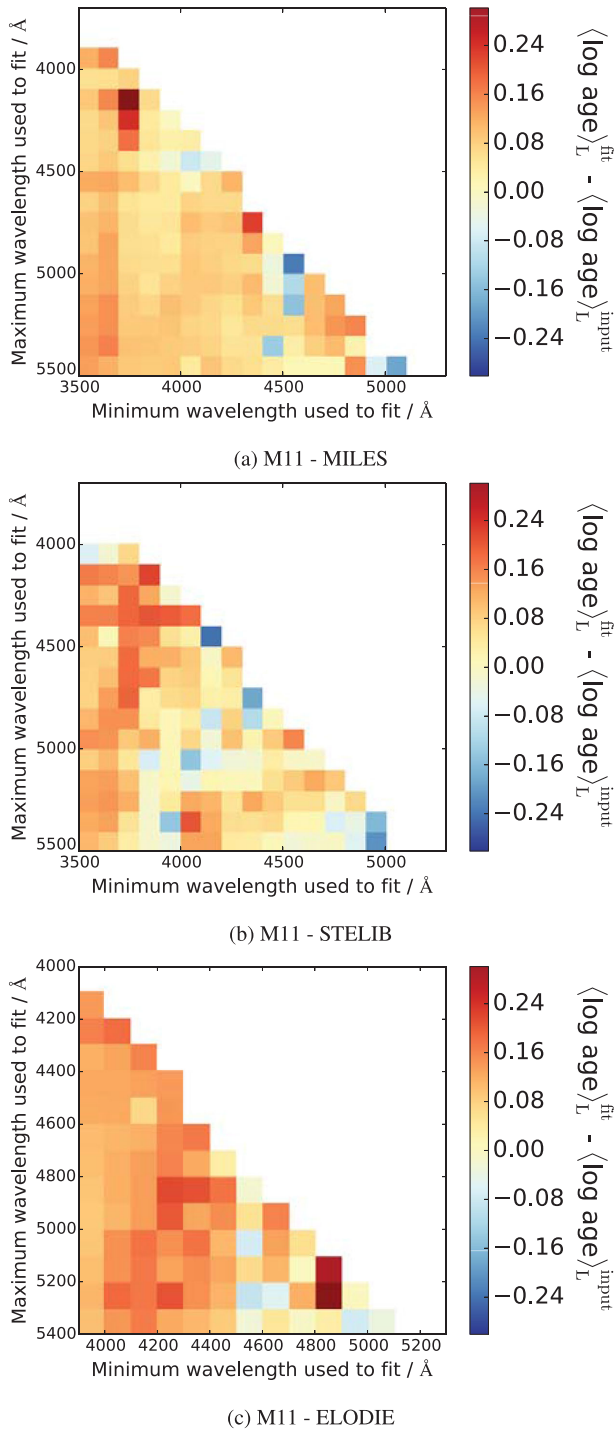


Figure 17. As in Fig. 16, but 10 Gyr after the starting of star formation.



**Figure 18.** How age determinations for the star cluster M67 obtained with M11–MILES–/STELIB–/ELODIE–based models, respectively, depend on the wavelength range fitted over. Coloured squares show the average age determination for that range of wavelengths fitted across. Ages consistent with the CMD one (4 Gyr, Chaboyer 1999; Sarajedini et al. 2009) are shown in colour close to yellow. The top right of the plots are empty, since those regions cover a negative, and hence non-existent, wavelength range.

includes a wavelength fitting region below 4100 Å, ages and metallicities are well estimated. However, once the region is removed, then the solutions tend towards younger (by up to 0.5 dex), generally more metal-rich ( $\sim 0.01$  dex) solutions. This was the case also when fitting M67. Together, these plots show that wider wavelength ranges give more ability to overcome the effects of age–metallicity degeneracy, as also concluded in Pforr et al. (2012), and confirms that for intermediate to old age solutions, the 4000 Å region is essential for precise age determinations.

### 5.3 Testing of age and metallicity derivation with globular clusters

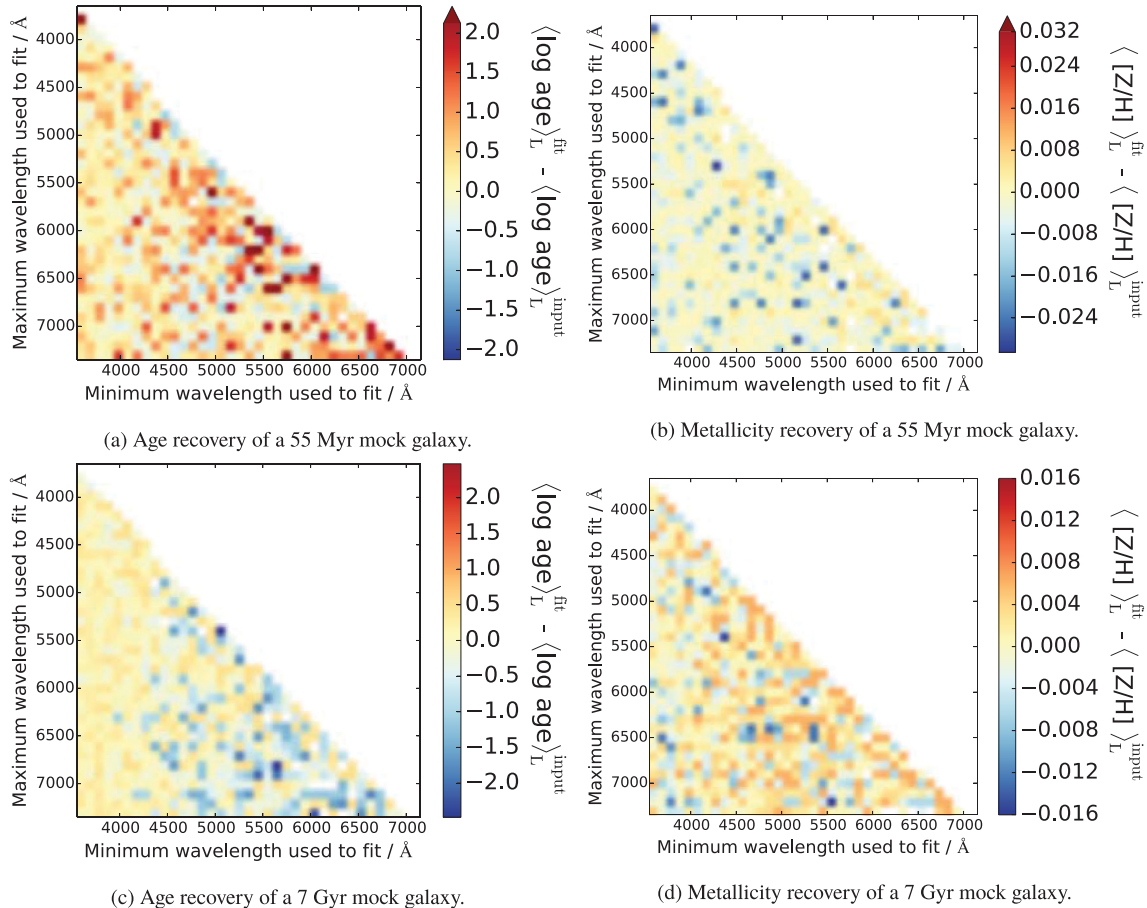
As stated in the Introduction, globular clusters, especially those in the Milky Way or Magellanic Clouds, are invaluable for calibration of methods using stellar population models, since we can compare our fitted ages with their independent determinations based on either fitting CMD fit for ages or stellar spectroscopy for chemical abundances (Renzini & Fusi Pecci 1988).<sup>10</sup> Star clusters provide the ‘simplest’ form of stellar populations in nature, i.e. approximately a single coeval and mono-metallicity population of stars, something we can assess with FIREFLY. In this section, we use globular cluster data from Schiavon et al. (2005), as also used in M11. In Fig. 20, we show two examples of FIREFLY’s fits to a metal-poor and metal-rich globular clusters, respectively.

We see that the metal-poor globular cluster NGC 5286 is well represented by nearly a single group of SSPs at high age and low metallicity, whereas NGC 6528, a more metal-rich cluster, is fitted by an old component of metallicity approx half-solar. The average values of age and total metallicity derived with the full spectral fitting with M11–MILES models are:  $t = 11.8$  Gyr,  $[Z/H] = -1.80$  for NGC 5286 and  $t = 11.2$  Gyr,  $[Z/H] = -0.33$  for NGC 6528 in remarkable agreement with the independent determinations based on CMD, namely  $t \sim 12$  Gyr,  $[Z/H] \sim -1.73$  for NGC 5286 and  $t \sim 10$  Gyr,  $[Z/H] \sim -0.2$  for NGC 6528. This is an important test that a fitting code plus a set of models has to pass. The dispersion in solutions might be testifying the presence of multiple generations very close in age and with a metallicity spread, although an extreme horizontal branch (HB) not included in our library or a fraction of blue stragglers could induce subtle effects in the fitting. One caveat here is that NGC 6528 is metal-rich and enhanced in  $\alpha$  elements (e.g. Thomas et al. 2003), whereas the M11 models are most likely solar-scaled at high metallicity (see discussion in Section 2). We shall investigate in the future whether the hints towards multiple populations is indeed a real effect.

In Fig. 21, we compare all our light-weighted ages and metallicities to those derived in the literature, as tabulated by Koleva et al. (2008). In cases where a CMD age has been measured, we use this value, and for others, we use the value derived in Koleva et al. (2008) from their full spectral fitting code *NBURSTS* (Chilingarian et al. 2007) based on the Pegase–HR models (Le Borgne et al. 2004). Since the models and code are different, we just provide a qualitative comparison of the results.

Very pleasingly, the ages derived from FIREFLY are close to those from CMD isochrone fitting (blue symbols) within 0.1 dex, for the vast majority of cases. Those for which the two determinations are not in agreement could either host blue HBs (we have used

<sup>10</sup> It should be noted, as discussed in M11, that the CMD fit depends somewhat on the tracks adopted for the fitting, which in turn are also a basic ingredient of stellar population models.



**Figure 19.** Light-weighted age (LHS) and metallicity (RHS) recovery of SSP-based mock galaxies as a function of wavelength range used for the fitting (at 100 Å intervals). The top panel shows results for a 55 Myr, solar metallicity SSP and the bottom panel shows results for a 7 Gyr, solar metallicity SSP. All use MILES-based models to fit to MILES-based mocks. The top right of the plots are empty, since those regions cover a negative, and hence non-existent, wavelength range.

M11–MILES with red HB for this test), or multiple populations. We refer to a future project for studying in detail globular clusters with FIREFLY.

Metallicity is compared in the right-hand panel. The blue points refer to determinations based on stellar spectroscopy. As these are generally tied to the so-called Carretta & Gratton’s scale (1997, Gratton, private communication), they refer to iron abundance [Fe/H] rather than to the total metallicity [Z/H] determined via FIREFLY. In order to make a meaningful comparison, we shifted the GCs values by +0.3 dex, which corrects [Fe/H] to [Z/H] for a  $\alpha$ -enhancement value around  $[\alpha/\text{Fe}] \sim 0.3$ , using the scaling by Thomas et al. (2003). The metallicity recovery is generally good.

The CMD ages are in better agreement with FIREFLY than the values derived from fitting in Koleva et al. (2008), where they seem to give lower ages than the CMD ones. This mismatch may originate in the combination of fitting procedures and adopted models. Overall, the comparisons show that FIREFLY is capable of correctly matching the properties of globular clusters derived from CMD fitting and stellar spectroscopy.

## 6 TESTING WITH SDSS DR7

We focus on spectra from the SDSS DR7 and 9 in this presentation paper because this is a very large sample which covers a range of galaxy types and which has been widely used in the literature.

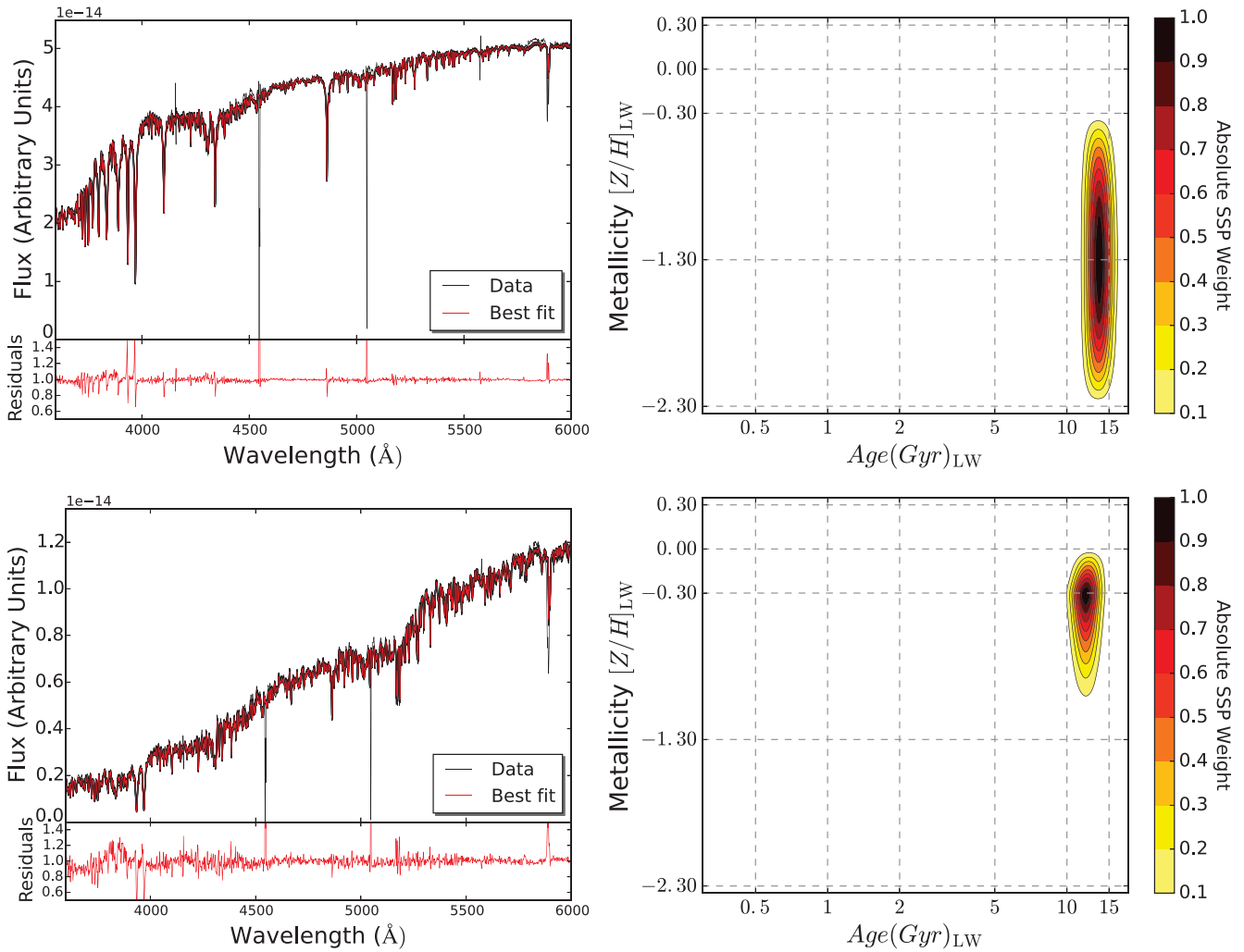
Obviously, our fitting code can be applied to any spectra. For example, in Wilkinson et al. (2015) we have analysed integral field unit spectroscopy data from SDSS-IV/Mapping Nearby Galaxies at Apache Point Observatory (MANGA) survey and in a forthcoming work we shall use it to fit the spectra of the most massive galaxies across a redshift range, from the SDSS-III Baryon Oscillation Spectroscopic Survey Data Release 12 (Dawson et al. 2013). The observed galaxy spectra that we have used in this work come from the SDSS II DR7. Equipped with two multi-object spectrographs, SDSS acquired spectra of more than 0.93 million galaxies in its ‘Legacy’ survey of a very large area of sky across a large wavelength range, covering 9380 sq. deg. at 3800–9200 Å at a spectral resolution of  $\sim 3$  Å, across a redshift range of  $0.0 \leq z \leq 0.5$ .

### 6.1 Data pre-processing

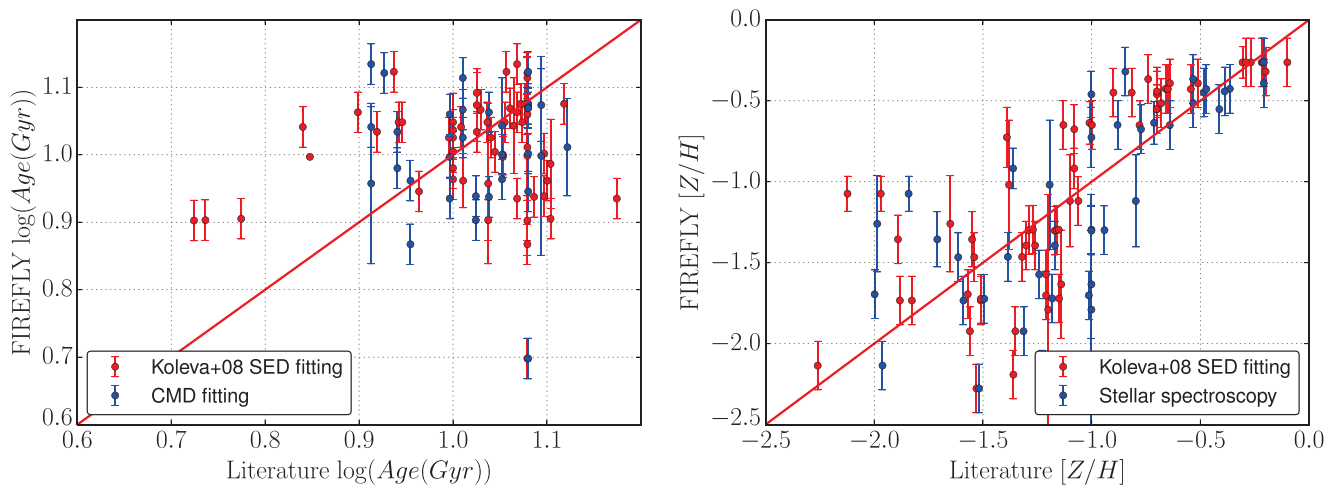
When analysing DR7 SEDs, some important considerations need to be made to ensure good recovery of galaxy physical parameters. In FIREFLY, these considerations become features in the code that can make the analysis more versatile and robust. We list these considerations and features here:

(i) We always use the actual velocity dispersion (in our case as output by GANDALF and PPF) to downgrade the resolution of our models as described in Section 3.4. This routine also provides us

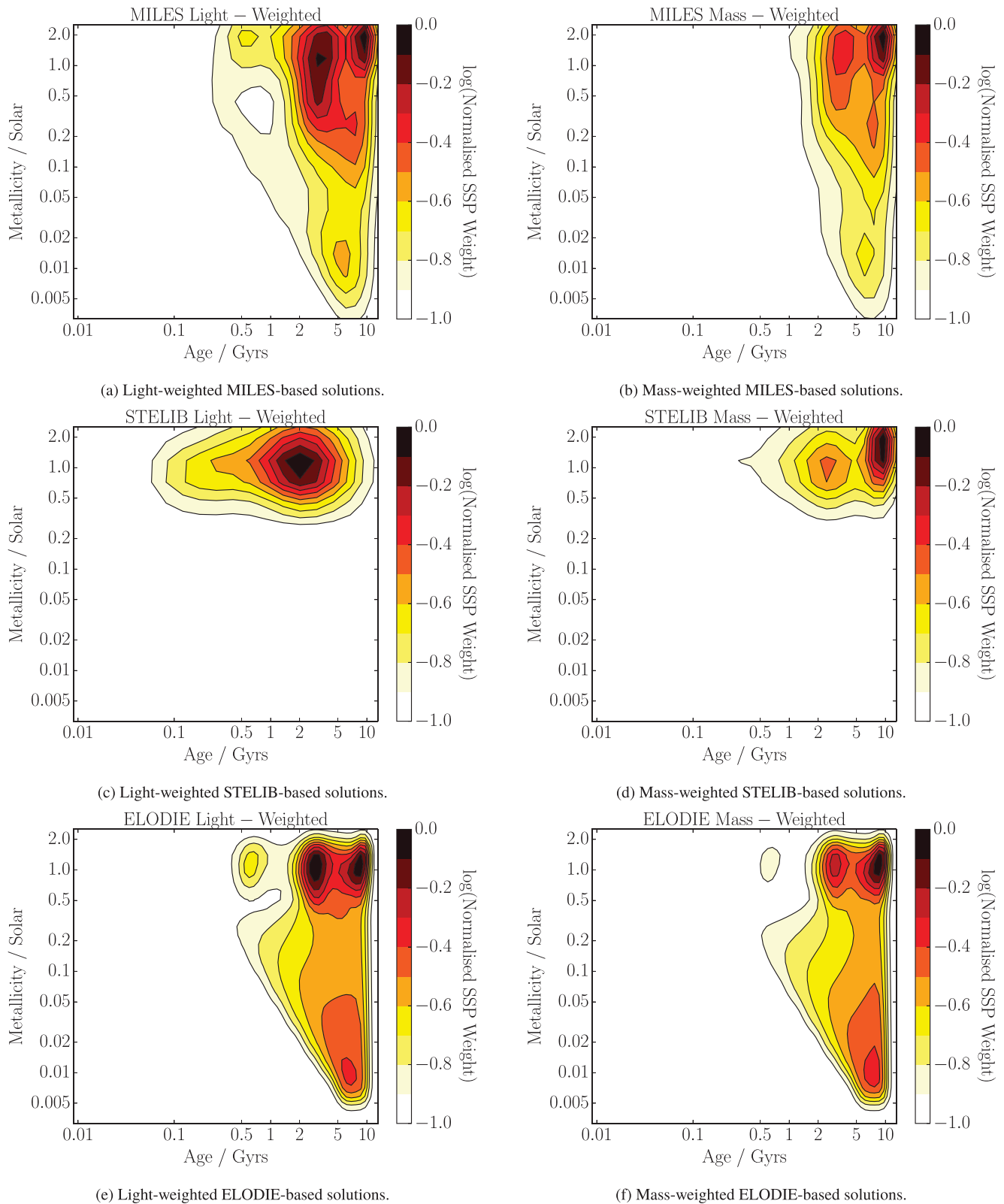




**Figure 20.** Fits and stellar population contours of two example globular clusters, NGC 5286 and NGC 6528 from Schiavon et al. (2005). Measurements from CMD fitting show NGC 5286 is very metal poor, whereas NGC 6528 is approximately half-solar in  $[Z/H]$ . FIREFLY using M11–MILES is able to reproduce their properties remarkably well.



**Figure 21.** Light-weighted age and metallicity derived from FIREFLY with M11–MILES models compared to results obtained with another spectral fitting code (red points, from Koleva et al. 2008) or to literature values which are independent of SED fitting procedures (blue points). The latter refer to CMD isochrone fitting in case of ages (left-hand panel), or stellar spectroscopy in the case of metallicity (right-hand panel).



**Figure 22.** The likelihood-weighted sum of all SSP contributions from all galaxies in the SDSS DR7 survey, as a function of empirical stellar library model ingredient, by light (i.e. flux) (LHS) or by stellar mass (RHS). Each contour represents the fractional weight of stellar population solutions in that part of age–metallicity space. An interpolation algorithm has been used to smooth the distributions.

with emission-cleaned spectra that we use to fit each of the galaxies used in this paper. As described in Section 3.3, we pre-process the data SEDs for Milky Way extinction by assuming a Fitzpatrick (1999) reddening law, and de-reddening the data;

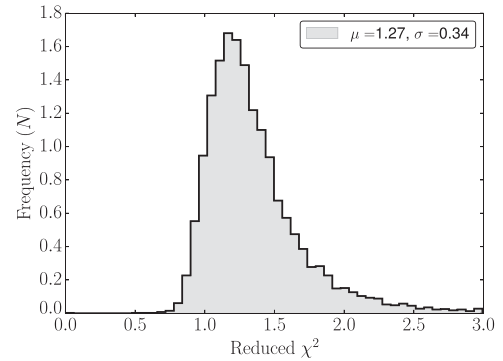
(ii) All SDSS data sets include quality flags (known as the ‘good-pixel array’) on each data point that signify if it is untrustworthy. For example pixels can show extreme residuals or very low S/N that can arise from artefacts in the data, or high amounts of sky flux. These points are removed from the analysis and shown in the spectral fits as if that part of the wavelength space had no data. Additionally, skylines from atmospheric scattering occur at 5577, 6200, and 6363 Å (in the observed frame) – these points are similarly removed with 5 Å masks to ensure they are not part of the spectral fits in their corresponding galaxy rest frame;

(iii) Occasionally, these flags can miss poorly processed fluxes, which would bias our fitting by weighting the chi-squared values obtained towards them. To prevent this, we use sigma-clipping of points at every measurement of chi-squared as used in many popular codes such as PPF (Cappellari & Emsellem 2004).

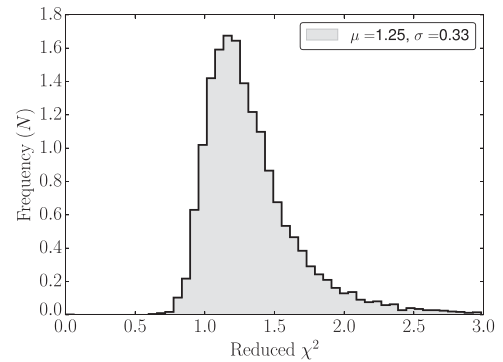
## 6.2 Results from DR7

In this section, we show the application of FIREFLY to SDSS DR7 and construct the SFH of full DR7 data set by summing the contributions from all the likelihood-weighted fits. An example fit to a typical DR7 galaxy was shown in Fig. 7. We use the full range of age, metallicity, and wavelength coverage available from each of the MILES-, STELIB-, and ELODIE-based M11 models since we want to assess the ability of each of the models to recover galaxy properties to their fullest extent. The light- and mass-weighted ages versus metallicities derived for DR7 galaxies are shown in Fig. 22. We note that we have computed a full set of stellar population properties including mass- and light-weighted average ages and metallicities, dust, mass, and chi-squared as a function of stellar library, but the plots shown are representative of the full set of possible plots. The calculated properties are publicly available.<sup>11</sup>

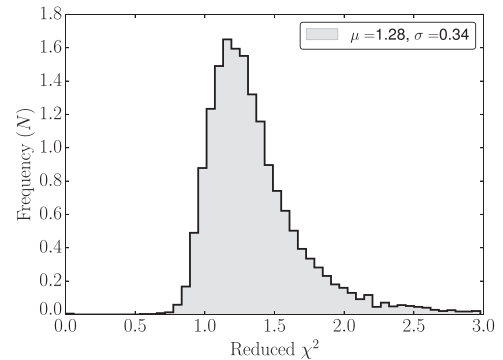
We now briefly analyse the distributions of Fig. 22. For all three models, we see that DR7 galaxies are dominated in mass-weighted contributions (right-hand panels) by a major component with old age,  $\sim 12$  Gyr and high metallicity (solar or above), plus minor components at younger ages (for MILES- and STELIB-based models) or low metallicity (for ELODIE-based models). Differences due to the input stellar library become more evident in the light-weighted contributions (left-hand panels). M11–MILES and M11–ELODIE solutions display a bimodality in light-weighted ages, with a group of galaxies with low ( $\sim 3$  Gyr) ages. STELIB-based models is more consistent with a unimodal, broader distribution with somewhat intermediate ages. Results based on this model flavour lack the extension to low metallicity because the library lacks low-metallicity models (cf. Table 1). Probably as a consequence of a narrow span in metallicity, the STELIB-based solutions show a wider spread in age, compared to the other models whose solutions are more compressed towards older ages. MILES-based models show the greatest number of solutions with high metallicity, both at high  $\sim 10$  Gyr and intermediate  $\sim 2$  Gyr ages. STELIB-based models are similar, but to a lesser extent. ELODIE-based solutions cluster around solar metallicity. Hence, the input stellar library affect both the recovered ages and metallicities, mostly in a light-weighted sense.



(a) MILES-based models.



(b) STELIB-based models.



(c) ELODIE-based models.

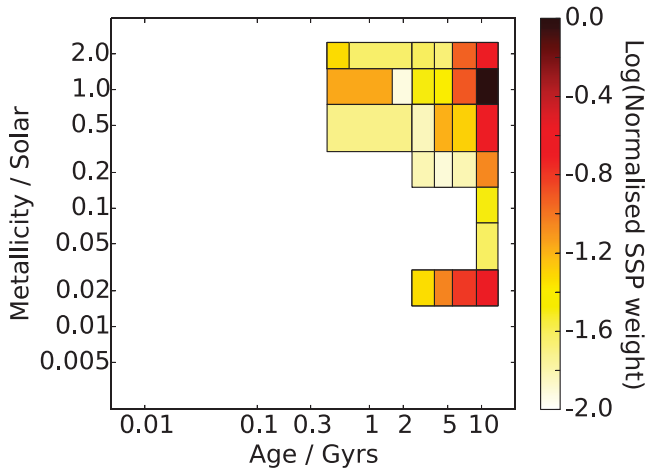
**Figure 23.** Reduced chi-squared distribution of fitting all DR7 galaxies with MILES-, STELIB-, and ELODIE-based models, which have corresponding mean averages of 1.13, 1.10, and 1.19, respectively.

The chi-squared distributions for the three explored models are shown in Fig. 23. The distributions are very similar with median reduced chi-squared values of 1.27, 1.25, and 1.28 for MILES-, STELIB-, and ELODIE-based models, respectively. The differences are driven by a small number of galaxies (with no clear pattern for what characterizes these galaxies) fitting somewhat more poorly for ELODIE-based models compared to the others, and STELIB-based models having slightly more galaxies with lower reduced chi-squared. Clearly, the  $\chi^2$  would not work as discriminator for which model one should use.

## 6.3 Comparisons with the literature

We compare the results of FIREFLY applied to SDSS DR7 galaxies with the results of two popular full spectral fitting codes, the

<sup>11</sup> [www.icg.port.ac.uk/firefly](http://www.icg.port.ac.uk/firefly)



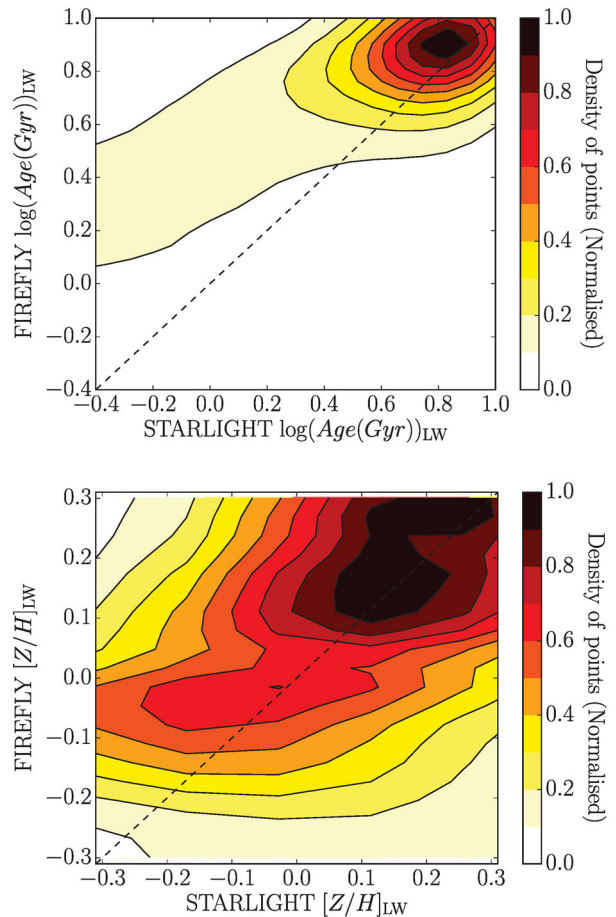
**Figure 24.** Stellar population mass contributions for DR7 galaxies obtained with *VESPA* and M05 models. The *VESPA* plot has age–metallicity bins as defined in Tojeiro et al. (2009), with the colours representing the total weighted mass in that bin, compared to *FIREFLY*’s weights based on the total mass of SSPs in that region of the plot. This plot should be compared to the right-hand panels of Fig. 22.

methodologies of which are described in Section 4. These codes have publicly accessible and published data bases of fitting results from DR7. We note that these data bases use different sets of stellar population models, although one of them (*VESPA*) provides also Maraston-type of models. Hence there is a degeneracy between codes and models which is difficult to separate. None the less, these are still useful comparisons to make.

First, we compare our results to *VESPA* using their DR7 data base (Tojeiro et al. 2009).<sup>12</sup> In Fig. 24, we show the results of summing the stellar populations found in all DR7 galaxies for the stellar population models of Maraston (2005) (M05) after *VESPA* fitting. This distribution should be compared to the ones showed in the right-hand panels of Fig. 22. The adopted models use the same evolutionary population synthesis code and the same prescriptions for stellar evolution, the only difference being the input stellar library. We note that M11 has greater spectral resolution compared to M05, potentially leading to resolving greater details in galaxies’ SFHs. On the other hand, M05 has a larger extension in wavelength and metallicity. In addition, we note that *VESPA* is written to give solutions with lower resolution in parameter space than *FIREFLY*.

Taking all this into account, the distributions are broadly speaking quite similar, displaying a major peak of galaxies at old ages and high metallicity. The *VESPA*–M05 distribution is closer to the *FIREFLY*–MILES or ELODIE-based results because of the more similar metallicity coverage. Looking in more detail, the plots show the different priors made in the fitting codes. *FIREFLY* allows for more contributions from individual SSPs compared to *VESPA*’s more strict allowance of introducing more complex SFHs, hence the age/metallicity distributions are somewhat broader in the *FIREFLY* case. Additionally, *FIREFLY* finds the major, old age contribution at high, super-solar metallicity, while the one in *VESPA* lies at solar metallicity.

Nonetheless, qualitatively the results agree on an old, high-metallicity stellar component being dominant for the DR7 sample, hence the galaxy evolution picture from both codes would probably



**Figure 25.** Comparison of the light-weighted average ages and metallicities obtained with *STARLIGHT* and *FIREFLY*. *STARLIGHT*’s results are obtained using BC03 models, and *FIREFLY*’s are obtained with M11 models, but both models are based on the STELIB library.

be similar. The fact that we use the same underlying population model here certainly makes a large part of this consistency.

Secondly, we compare our results with the analysis of the DR7 performed by *STARLIGHT* (Cid Fernandes et al. 2005),<sup>13</sup> which is based on BC03 STELIB-based models. Given the flexibility of our models, we can compare with M11–STELIB, which should help reducing the differences due to the input models. Unlike *VESPA*’s data base, a full breakdown of stellar population components is not available; instead they provide mass- and light-weighted average properties, hence we shall compare to those. In Fig. 25, we plot the light-weighted properties, which, by spanning a larger range of values, enable a more distinctive comparison. We plot density contours of the  $\sim 1$  million points from directly plotting *STARLIGHT* results against *FIREFLY* results.

We see that – in spite of different procedure and input model – the main density of age and metallicity points are very similar between *STARLIGHT* and *FIREFLY*, clustering around 8 Gyr in age and 0.1 to 0.3 dex in  $[Z/H]$ . Hence for the total sample, the codes agree very well. Some differences are visible however. First, in the age plot, the extension down to low ages is flatter in *FIREFLY* compared to *STARLIGHT*, suggesting either that *STARLIGHT* is more sensitive to small star formation episodes in the star-forming sample, or that the

<sup>12</sup> Available at <http://www-wfau.roe.ac.uk/vespa/>.

<sup>13</sup> Available at <http://casjobs.starlight.ufsc.br/casjobs/>.

BC03 models fit for younger ages compared to our models. Only running `STARLIGHT` with our models, which is beyond our scope here, could choose between one of these hypotheses. Secondly, also in the metallicity plot, we see a flatter profile from `FIREFLY` out to low metallicity. In Goddard et al. (2017), we present an extensive comparison of stellar population properties obtained with `FIREFLY` and `STARLIGHT`, and swap stellar population models between the codes to be able to pin down the interplay of fitting procedure and model.

In conclusion, despite differences in the details of the minor stellar population components, we conclude that we have good qualitative agreement with the literature on full spectral fitting of DR7 galaxies even when different stellar population models are used.

## 7 SUMMARY AND CONCLUSIONS

We presented `FIREFLY`, a full spectral fitting code designed to recover the stellar population properties, such as light- and mass-weighted ages, metallicity, reddening, and the SFH, of stellar systems – galaxies and star clusters – from stellar population model fitting to observed spectra. `FIREFLY` employs a chi-squared minimization procedure that fits combinations of single-burst stellar population models to spectroscopic data, following an iterative best-fitting process controlled by the BIC. No priors are applied, rather all solutions within a statistical cut are retained with their weight. Moreover, no additive or multiplicative polynomials are employed to adjust the spectral shape. This fitting freedom without adjustments is envisaged in order to map out intrinsic degeneracies and explore the effect of changing models and their components. It is a code written from a modeller perspective.

In addition, we explore an innovative method for including the effects of dust attenuation. In this method reddening is not treated as an additional adjustable free parameter, rather it is determined prior to the fitting by comparing the large modes of data and models. This method was studied in a previous paper (Wilkinson et al. 2015) using integral field unit data in which dust regions were easily spotted. We plan nonetheless to experiment with different options in future developments of the code.

We check the performances of our code through comprehensive testing, using a large suite of mock galaxies, representing both simple and complex populations, as well as a sample of well-studied Milky Way globular clusters and galaxies from the SDSS.

We use Monte Carlo simulations to measure and quantify how offsets and errors in age, metallicity, and mass vary as a function of S/N of the data, which is a crucial information to plan new observations, and input model parameters. We show that the code is able to recover stellar population properties such as age, metallicity, and stellar mass, and even the SFH, down to an S/N  $\sim 5$ , for moderately dusty systems. At S/N  $\sim 20$ , the recovery of the SFH is remarkably good independently of reddening, unless the star formation is very extended ( $\sim 10$  Gyr). Even in the latter case, though, in spite of a lower precision, we find that the code releases multiple generation components, hence it is still able to discriminate between short and extended formation histories.

For a sample of Milky Way GCs, we find a very good match of their ages and metallicities as independently determined via CMD fit and stellar spectroscopy. We plan to use `FIREFLY` to investigate the event of multiple populations in extragalactic globular clusters.

Lastly, we have run `FIREFLY` on  $\sim 1$  million galaxies from SDSS DR7 and compared the results with previous analysis based on other fitting codes, such as `STARLIGHT` (Cid Fernandes et al. 2005) and `VESPA` (Tojeiro et al. 2007, 2009). We find generally consistent ages

and metallicities for the bulk population of SDSS galaxies. Using SDSS galaxies, we have also analysed the effect of input stellar library in the population model. We find that the overall effect is small, although interesting differences in some regions of the age/metallicity diagram emerge, with MILES-based models giving the largest number of old ages and high (super-solar) metallicity, whereas ELODIE-based models are more consistent with a bulk solar metallicity and a metallicity spread. Codes, input files, and other results are publicly available at: [www.icg.port.ac.uk/firefly](http://www.icg.port.ac.uk/firefly).

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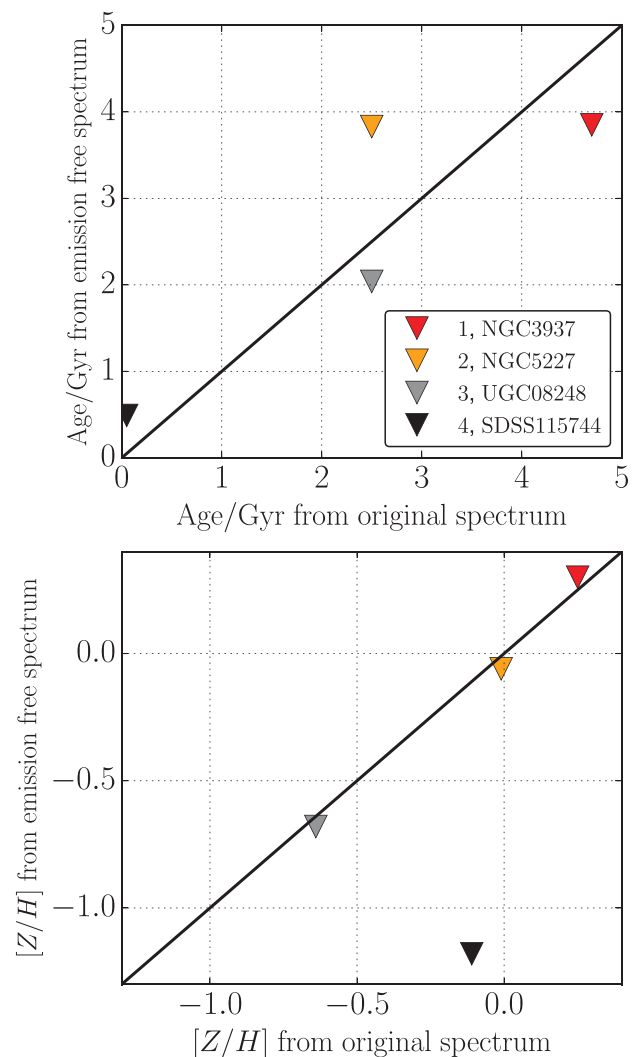
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## APPENDIX A: EFFECT FROM EMISSION LINES

To explore the impact of emission lines on the observed spectrum to be fitted with FIREFLY, we carried out the following exercise. We ran FIREFLY on the original observed spectra and on the same after removal of the strongest emission lines, and compared the resulting ages and metallicities. Emission lines have been removed using a version of the SDSS-IV MANGA Data Analysis Pipeline (Westfall et al. in preparation), which is based on the code PPF. This analysis was done on four galaxies from the SDSS covering a range of

morphological types and emission-line strengths, namely: a quiescent elliptical (NGC3937, 1), a spiral galaxy bulge (NGC5227, 2), a dusty star-forming galaxy (UGC08248, 3), and an H II star-forming dwarf (SDSS115744, 4). The results are reported in Fig. A1. Overall, there appears to be no systematic offset in the age and metallicity derived between the original and emission-line free spectrum, which is very interesting. The derived metallicity in particular is remarkably robust independent of emission lines. It seems that the full spectral fitting by modelling a large number of flux points gives results that are not too dependent on the presence of narrow emission lines randomly distributed along the spectrum. Not surprisingly, the most affected object is the emission-line dominated dwarf (4). These results performed on four objects only should be regarded as indicative, and should be obtained for a larger number of objects in the future.



**Figure A1.** Light-weighted ages and metallicities for the four different galaxies, labelled as in the text [1 = quiescent elliptical (red), 2 = spiral galaxy bulge (orange), 3 = dusty star-forming galaxy (grey), 4 = H II star-forming dwarf (black)], as derived from the original spectrum inclusive (x-axis) or not (y-axis) of emission lines.

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