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Influence of vertical flows in wells on groundwater sampling

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ABSTRACT

Pumped groundwater sampling evaluations often assume that horizontal head gradients predominate and the sample comprises an average of water quality variation over the well screen interval weighted towards contributing zones of higher hydraulic conductivity (a permeability-weighted sample). However, the pumping rate used during sampling may not always be sufficient to overcome vertical flows in wells driven by ambient vertical head gradients. Such flows are reported in wells with screens between 3 and 10 m in length where lower pumping rates are more likely to be used during sampling. Here, numerical flow and particle transport modeling is used to provide insight into the origin of samples under ambient vertical head gradients and under a range of pumping rates. When vertical gradients are present, sample provenance is sensitive to pump intake position, pumping rate and pumping duration. The sample may not be drawn from the whole screen interval even with extended pumping times. Sample bias is present even when the ambient vertical flow in the wellbore is less than the pumping rate. Knowledge of the maximum ambient vertical flow in the well does, however, allow estimation of the pumping rate that will yield a permeability-weighted sample. This rate may be much greater than that recommended for low-flow sampling. In practice at monitored sites, the sampling bias introduced by ambient vertical flows in wells may often be unrecognized or underestimated when drawing conclusions from sampling results. It follows that care should be taken in the interpretation of sampling data if supporting flow investigations have not been undertaken.
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1. Introduction

Groundwater quality observed from the sampling of monitoring wells (or boreholes) is fundamentally controlled by the origin of the groundwater extracted. Sample provenance may depend upon a complex interplay of the scale (e.g. screen length) of the monitoring well, the sampling method and protocol employed and the prevailing local hydrogeological conditions. The latter's influence may prove to be significant between wells even where similar sampling protocols are adopted that are designed to promote consistency in approaches. Variation in the local permeability field (and hence natural groundwater flow regime) may cause traditional well purging approaches advocating removal of three to five or more well volumes (ASTM International, 2013) to exhibit contrasting interactions with the various (hydro)geological units present. Likewise, increasingly adopted, passive zero-purge or low-flow (0.1–0.5 l/min) sampling methods (Puls and Barcelona, 1996), may extract samples significantly influenced by the natural groundwater flow regime that is sensitive to local hydrogeological scenario (and the well's potential perturbation of that regime). Zero purge or low-flow sampling might not always be recommended (US EPA, 2010), but are nevertheless often attractive

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compared to onerous well purging due to their potential benefits of reducing purge volume, minimizing in-well disturbance, reducing mixing with casing water, and shortened sampling times (Barcelona et al., 1994, 2005; Puls and Barcelona, 1996; Stone, 1997). It is hence important that potential influences of the local hydrogeological flow regime upon groundwater samples withdrawn by both modern and established sampling protocols are rigorously assessed to allow more appropriate sampling of wells and interpretation of the groundwater quality data arising.

While the influence of the local permeability field on sample origin is widely recognized through the concept that pumped samples are permeability weighted (i.e., higher permeability layers contribute a greater proportion to the sample obtained (Church and Granato, 1996; Hutchins and Acree, 2000; Puls and Barcelona, 1996)), consideration of local hydraulic, particularly vertical gradients, is often neglected. Critically, the monitoring well may serve as an artificial conduit allowing vertical flows between otherwise unconnected geological units. This can result in unforeseen sample origins that may remain unrecognized in the absence of supporting flow or gradient data. Our primary interest herein is to evaluate the influence of vertical flows in wells on the provenance of the pumped sample and groundwater quality determined.

Our research adds to that undertaken on the provenance of pumped samples from wells. At long time, pump intake position may not be important and the sample origin is directly related to the permeability distribution over the well screen interval (Varlijen et al., 2006). However, it may take a significant time, often longer than the typical sampling time, before this permeability-weighted sample concentration is attained due to the later arrival of groundwater entering the distant ends of the screen farthest from the pump intake (Martin-Hayden, 2000a,b; Martin-Hayden et al., 2014; Reilly and Gibs, 1993). Well casing storage (Barber and Davis, 1987), well screen and sand pack design (Kozuskanich et al., 2012), the partial mixing of inflowing water with water within the well screen during pumping (Martin-Hayden and Wolfe, 2000) and even the purging method (Robbins and Martin-Hayden, 1991) may additionally affect the stabilization time. With increasing screen length in particular, chemical stability may take a very long time to occur, even if pumping rates are increased (Mayo, 2010; Rivett et al., 1990).

Implicit to many groundwater sampling evaluations is the (perhaps unrecognized) assumption that pumping overcomes any ambient vertical gradients and a permeability-weighted sample (also referred to as a flow-weighted average sample or a screen-weighted sample (Church and Granato, 1996; Hutchins and Acree, 2000; Martin-Hayden, 2000a)) is eventually obtained. However, rather than being the exception (Giddings, 1987), ambient vertical flows in wells are expected to be as ubiquitous as vertical flows in aquifers and will occur at least to some degree in all aquifers (Elci et al., 2001). Naturally occurring vertical hydraulic head gradients which may induce significant vertical flows in wells are widely reported in a variety of hydrogeological settings (Brassington, 1992; Church and Granato, 1996; Dumble et al., 2006; Furlong et al., 2011; Ma et al., 2011; Metcalf and Robbins, 2007; Streetly et al., 2002; Taylor et al., 2006). Ambient vertical flows in wells are likely to be greater where well screens are longer and geological layering promotes increased vertical head gradients. Use of shorter screens (low-flow sampling is typically recommended for well screens <3 m (e.g. US EPA, 2010)) may reduce ambient vertical flows, however, ambient vertical flows of 0.015–2.3 l/min have been reported in wells with screens between 3 m and 10 m in length (Elci et al., 2001). It is important to recognize the influence of vertical flows in wells as they may cause aquifer cross-contamination (Lacombe et al., 1995), passive sample concentration bias (Elci et al., 2001; Konikow and Hornberger, 2006), errors in hydraulic head and hydraulic conductivity estimation (Elci et al., 2003; Kaleris et al., 1995) and misinterpretation of tracer test results (Riley et al., 2011). The effect and sensitivities of ambient vertical flows on sampling provenance in pumped groundwater samples has not been systematically mapped out.

Our goal is hence to examine the phenomenon of ambient-flow biased samples and answer the question—can the literature-reported range of vertical flows in wells bias sampling results and lead to samples that are weighted by ambient head gradients in addition to other hydraulic influences? We present herein our numerical modeling study designed to address this question.

2. Materials and methods

2.1. Numerical modeling overview

Numerical flow modeling with particle tracking was used to investigate pumped sample provenance under ambient horizontal head gradients and for increasing vertical gradients for 14 different model scenarios with varying screen lengths, well diameters, pumping rates, aquifer depths, permeability distributions and boundary conditions (Table 1). For each scenario the relative influence of vertical head gradients was varied by varying the position of the monitoring well in the aquifer. Each vertical flow simulation was compared with a corresponding baseline case with the same scenario parameters but no ambient vertical head gradients.

We consider well screen lengths of 3–10 m and pumping rates that vary from those recommended for low-flow sampling through higher pumping rates perhaps adopted in purging. While the lower end of the above screen range is typically recommended for low-flow sampling (e.g. US EPA, 2010), some authors have suggested such sampling can be used with screen lengths >3 m (Barcelona et al., 2005; Metcalf and Robbins, 2007; Varlijen et al., 2006). Indeed, low-flow or zero-purge sampling options are doubtless attractive in longer screen wells as the removal of fixed purge volumes becomes increasingly onerous. From a UK perspective, while well screens <3 m are advocated for monitoring wells (BS ISO, 2010), other guidance suggests that low-flow sampling is most applicable in wells with long screen lengths (BS ISO, 2009). It is recognized that well screen lengths <3 m are becoming more prevalent in contaminated site investigations and that a 10 m well screen may perhaps be perceived to be unreasonably long. However, the use of 10 m, or even longer, well screens still remains significant internationally. For example, within the UK context, they can be used in the monitoring of thick (>c. 100 m) aquifer resource units and low storage aquifers with high amplitude dynamic

Table 1
Summary of model parameters for 14 scenarios.

Scenario	Screen length (m)	Well diameter (cm)	$K_{x,y}$ (m/day)	Anisotropy ratio (K_v:K_h)	$K_{x,y,z}$ (m/day) (Low *K* layer)	Screen K (m/day)	Aquifer depth (m)	Boundary	Pump rate (l/min)
1	6	5	5	1:10	N/A	N/A	30	C.H.	0.3
2	6	5	5	1:1	N/A	N/A	30	C.H.	0.3
3	6	5	0.5	1:10	N/A	N/A	30	C.H.	0.3
4	6	5	0.5 (top 50%) 5 (bottom 50%)	1:10	N/A	N/A	30	C.H.	0.3
5	6	10	5	1:10	N/A	N/A	30	C.H.	0.3
6	6	5	5	1:10	N/A	0.5	30	C.H.	0.3
7	6	5	5	1:10	N/A	0.05	30	C.H.	0.3
8	3	5	5	1:10	N/A	N/A	30	C.H.	0.3
9	10	5	5	1:10	N/A	N/A	30	C.H.	0.3
10	6	5	5	1:10	N/A	N/A	60	C.H.	0.3
11	6	5	5	1:1	0.05 (middle)	N/A	30	C.H.	0.3
12	6	5	5	1:1	0.05 (top)	N/A	30	C.H.	0.3
13	6	5	5	1:10	N/A	N/A	30	Recharge	0.3
14	6	5	5	1:10	N/A	N/A	30	C.H.	0.5

water tables. Also long well screens may be found in older wells/boreholes inherited from long-term monitoring of aquifer resources or, for example, sentinel monitoring at landfill sites where a reasonable thickness of a potentially impacted aquifer may be monitored.

Vertical flow simulations for each scenario were run initially without pumping to assess the induced ambient vertical flows in the well. Pumping at low-flow rates was then simulated to investigate the sampling bias induced by the aquifer vertical gradients. Finally for each scenario, the pumping rate was increased to see if vertical gradients could be overcome and permeability-weighted sampling conditions could be achieved. Several transient simulations were used to investigate the possible variation in flux distribution as drawdown proceeds; in particular, the arrival at the pump intake of water initially in the casing.

The scope of the modeling excluded direct assessment of the implications of water quality variations within a monitored aquifer. The modeling results will assume more importance where concentration variations are significant between different geological (permeability) horizons sampled by the well. Our flow-based assessment underpins such future work.

2.2. Model setup

MODFLOW 2000 (Harbaugh et al., 2000) was used to model the sampling scenarios simulated (Fig. 1). The model's

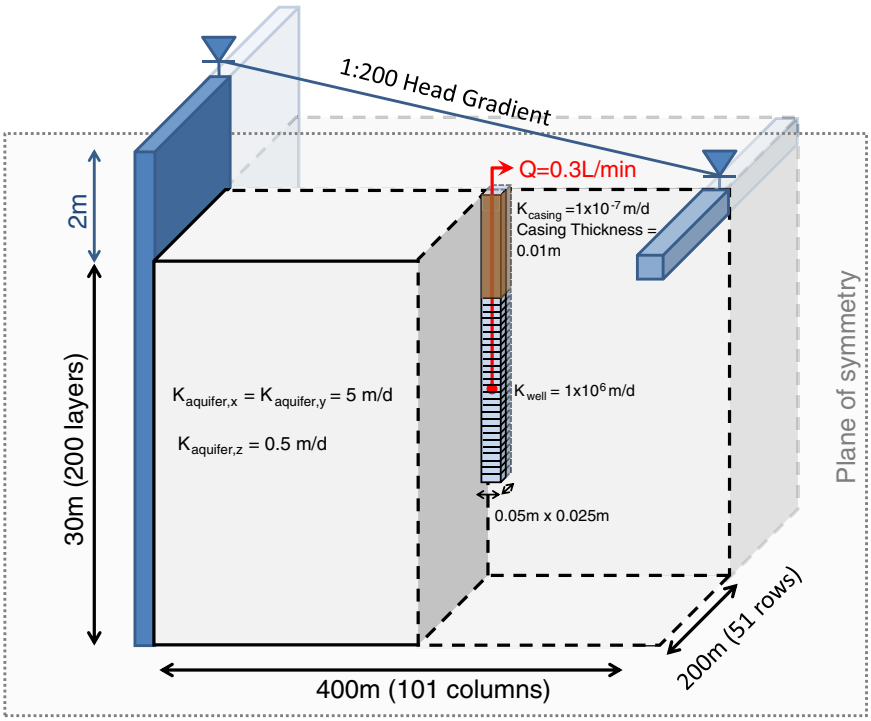

Fig. 1. Summary of model domain and parameters for Scenario 1 with vertical head gradients (not to scale).

finite difference grid was 400 m wide and either 30 or 60 m deep. Variable horizontal grid spacing was used ranging from a minimum as dictated by the borehole diameter to a maximum of 30 m at the inflow boundary. Uniform vertical discretization was used. The existence of a vertical plane of symmetry through the borehole and parallel to groundwater flow allowed half the domain of interest to be simulated.

Head boundaries were specified at the left- and right-hand sides of the model. The remaining boundaries were no flow. For baseline no ambient vertical flow simulations the head gradient between left and right boundaries was uniform with depth in the aquifer. In these simulations, the well was centered both vertically and horizontally in the aquifer. For vertical flow cases, the conceptual model was one of predominantly horizontal regional flow from an aquifer discharging at a surface-water body with vertical gradients increasing as discharging water converges at the outflow point. For these scenarios, the right constant head boundary was specified in the top layer of the model only.

Rather than fixing well inflows/outflows or near well hydraulic gradients, for vertical flow simulations model boundary conditions were specified at a distance from the well. This allowed pumping simulations to affect (and possibly overcome) near well vertical head gradients. For each scenario the influence of vertical gradients on the well was varied by varying the horizontal distance of the well from the outflow boundary.

Initial sensitivity testing demonstrated that increasing the horizontal head gradient between the inflow and outflow boundaries leads to increased vertical head gradients due to the larger volume of water converging on the outflow point. Therefore, the horizontal gradient acted as a control on the magnitude of any in-well vertical flows. A final horizontal hydraulic head gradient of 1:200 was chosen as being both a realistic value, and one able to generate ambient vertical well flow rates that were comparable to those reported in literature.

While possibly important during groundwater sampling at some sites, variation in sample origin due to well dewatering effects was out with the scope of this investigation. In order to prevent well dewatering effects in the unconfined simulations, the model head gradients were specified such that they were above the top boundary of the model. The only exception to this was Scenario 13 where model inflows were derived from recharge alone with no left-hand constant head boundary. In this scenario, recharge was uniformly distributed at a rate of 1.41 mm/day. The recharge value was selected to give model inflows comparable to Scenario 1.

It was hypothesized that any impedance to vertical flow in the aquifer was likely to be important in driving ambient vertical well flows. For this reason, the starting vertical scenario (scenario 1) was that of a permeable (5 m/day) aquifer with a 1:10 vertical to horizontal anisotropy ratio. Aquifer hydraulic properties in subsequent scenarios were chosen to represent a non-exhaustive range of alternatives: an isotropic aquifer (Scenario 2); a lower permeability aquifer (Scenario 3); a two-layer aquifer (Scenario 4); and an isotropic aquifer with a single 1.5 m low-K layer intersecting the middle (Scenario 11) or top of the well (Scenario 12).

For all scenarios, a single column of high-conductivity cells was used to simulate the water column both in the screened and cased sections of the well. During initial sensitivity testing with the MT3D code (Zheng and Wang, 1999) for transport simulation using MODFLOW velocity data, the influence of the in-well hydraulic conductivity (K_{well}) on transport to the pump intake was investigated in an aquifer with hydraulic conductivity of 5 m/day. Simulated flow and transport to the pump intake was simulated for various K_{well} values and compared against an analytical solution (Martin-Hayden, 2000a). The analytical solution described the temporal variation in pumped sample concentration given a formation concentration that varied linearly from high concentration adjacent to the screen near the pump intake to low concentration at the far end of the screen. A K_{well} value of at least 10^6 m/day was required to provide a close match to both early and late time analytical data (Fig. 2) and account for the delayed arrival of stream lines originating at a distance from the pump intake. A K_{well} value of 10^6 m/day was used for all further scenarios. This value is comparable with K_{well} estimates using Poiseuille's law (e.g. (Martin-Hayden, 2000a; Reilly and Gibs, 1993)); assuming fresh water at 12 °C, equivalent conductivities for 5 cm and 10 cm diameter wells are calculated as 5.4×10^7 m/day and 2.1×10^8 m/day respectively.

Well casing above the open interval was simulated using MODFLOW's wall boundary condition with a very low K value (1×10^{-7} m/day) to simulate the impermeable casing with a thickness of 0.01 m. This value was found to be sufficiently low to provide an effectively impermeable barrier with negligible flow observed through the casing relative to the screened interval of the well.

Lower conductivity screens have been shown to have a homogenizing effect on well inflows in a heterogeneous aquifer under pumping conditions (Houben and Hauschild, 2011). Scenarios 6 and 7 were used to investigate the effect of a low-K well screen on well inflows under ambient vertical gradients. Screen conductivity values were chosen arbitrarily to be lower than the surrounding aquifer and were explicitly modeled using MODFLOW's wall boundary condition. Values of 0.5 and 0.05 m/day were chosen for Scenarios 6 and 7 respectively. In all other cases head loss across the screen was assumed negligible and the screen was not modeled.

A single cell within the well screen interval was specified as a well boundary condition to represent the pump intake. The initial pumping rates were either 0.3 or 0.5 l/min (within the range of 0.1–0.5 l/min recommended for low-flow pumping (Puls and Barcelona, 1996)). Unless otherwise specified, the

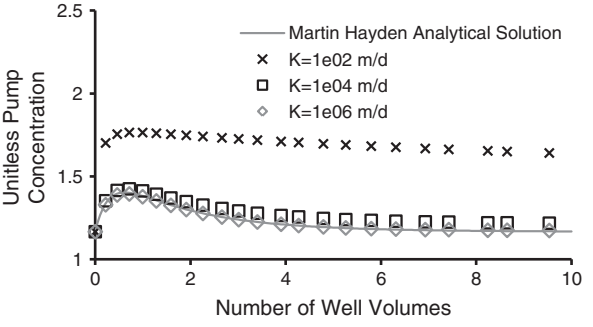

Fig. 2. Comparison of MT3D transport results with Martin-Hayden's (2000a) analytical solution for increasing K_{well} values.

pump was located in the center of the well screen. During vertical flow simulations, pumping rates were incrementally increased until ambient vertical flows were overcome. The maximum pumping rate used was 36 l/min. Actual modeled pumping rates were half of those stated above due to simulation of half of the model domain.

2.3. Flow simulation

The groundwater flow equations were solved using the PCG2 package of MODFLOW. In order to minimize mass balance errors and artificial oscillations due to very high-K well cells, head-change and residual-convergence-criteria values were set to 1×10^{-6} m and 0.001 m^3/day respectively. Cell-by-cell well in-flows and outflows were obtained directly from the MODFLOW CBB files. Constant-head and volumetric fluxes across the right, front and lower faces of each well grid cell were recorded for each timestep. These flows, in addition to the flows from the right face of the cell immediately to the left of the well cell, allowed the total inflows/outflows in the well to be calculated for each vertical layer. The inflows/outflows were multiplied by two as only half the well was modeled.

Steady-state flows were simulated when comparing well inflows and outflows under unpumped and pumped conditions. Limited transient flow simulations were used to investigate the possible variation in flux distribution as drawdown proceeds and particularly the arrival at the pump intake of water initially in the casing. The 12-h duration of the transient flow simulations was chosen to be significantly longer than the completion of groundwater sampling using well pumping methods (low-flow, or traditional 3–5 well volumes). During the transient simulations, the specific yield was set to 0.1 in the aquifer and 1 in the well. Specific storage was specified as 1×10^{-4} 1/m.

2.4. Particle tracking

Particle tracking using the MODPATH 5 (Pollock, 1994) code in time series mode and transient MODFLOW velocity data was used to investigate the temporal variation in the well's capture zone. The relatively low pumping rates and the partially penetrating screens form capture zones that extended only a few meters from the screen. Consequently, particles did not need to be distributed throughout all layers of the model. Particles were placed in up-gradient and down-gradient of the well in layers 10–145 (layers numbered top to bottom). Particles were placed in row 1 on the cell face at the top edge of the model along the plane of symmetry. Particles were released at the onset of pumping and were removed from the model upon arrival at the pump intake. Six particles were placed in each cell (evenly distributed in two rows) in order to provide sufficient resolution for early time (<1 h) capture zones. During particle tracking, porosity within the well was 1 and outside the well 0.25.

2.5. Quantifying the bias to sampling

To allow comparison between vertical flow scenarios it was necessary to quantify the vertical flow induced sample bias. For a particular vertical flow scenario, the bias was calculated by finding the percentage inflow from each layer and then summing the difference between this and the percentage inflow from each layer under baseline horizontal gradient conditions:

$$\%Bias = \sum_{i=1}^{n} \left| \frac{Q^{v}_{in,i}}{Q^{v}_{T}} - \frac{Q^{h}_{in,i}}{Q^{h}_{T}} \right| \times 100 \quad (1)$$

where $Q_{in,i}$ is the volumetric inflow for the well cell in layer i, Q_T is the total volumetric inflow to the well over all layers, n is the number of layers intersected by the well and the superscripts v and h indicate vertical flow and ideal horizontal flow conditions respectively.

3. Results and discussion

3.1. Origin of pumped sample water from wells with no ambient vertical flows

Under horizontal head gradients, flow converges vertically to the well screen since the well is partially penetrating in these scenarios (Fig. 3g–i). This explains the higher influxes at the top and bottom of the well screen during pumping (Fig. 3a–c). However, while the long-time pumping capture zone encapsulates the entire well screen (Fig. 3g–i), the time to reach this state depends on the volume of water within the well screen (Fig. 3d–f). For Scenario 1 it takes 2 h to purge all well screen and casing water (Fig. 3d) and achieve a sample comprising 100% formation water. In Scenario 5 it takes over 3 h (Fig. 3e). Even for a well with a 3 m screen, for the low-flow pumping rate used, it takes just over 1 h (Fig. 3f) to purge all non-formation water. In all three cases, to achieve a sample comprising 100% formation water requires purging the equivalent of several screen volumes. However, stabilization of drawdown to within 95% of steady-state drawdown was achieved within 10 min.

After groundwater from the entire screen has reached the pump intake, the pump intake location may not affect the zone of the screen sampled. However, the time to reach this position depends on the well screen volume. In wells with longer screens it can be inferred that prolonged pumping may be required to collect water from the entire screen interval. Until then, pump intake position, pumping rate and pumping duration will play an important role in determining the origin of the water sampled and therefore the sample concentration, even without vertical flows. This result compares well to the modeling of Martin-Hayden et al. (2014) who found that purging of at least two screen volumes was required to obtain a sample consisting of 94% formation water. For the cases considered, well drawdown was not a good indicator of pumping capture zone stabilization across the screen interval.

Some casing water will always be purged due to the drawdown induced by pumping (Fig. 3d–f). The location of the pump intake determines the arrival time of the casing water at the pump intake. The farther the pump intake is located from the top of the screen, the later the casing water will arrive at the pump intake. While the volume of casing water is small and possibly well mixed with other water flowing towards the pump intake, the influence of the casing water may be an additional consideration when siting the pump intake for various types of sampling with a pump.

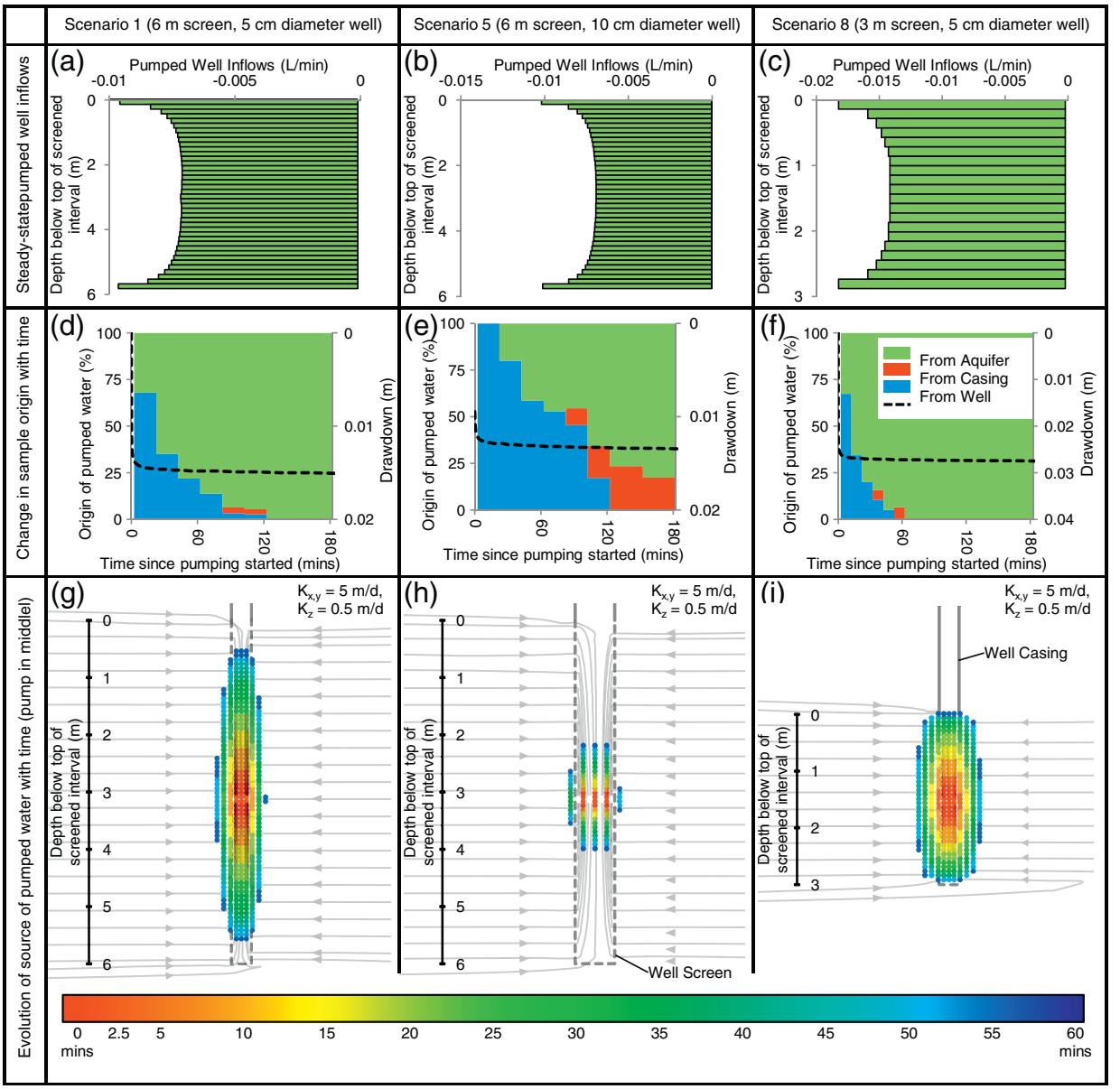

Fig. 3. Simulated pumped sample origin for Scenarios 1, 5 and 8 under ambient horizontal gradients. The first row shows the steady-state pumped well inflows. The second row shows the variation in pumped water origin with time compared with the simulated drawdown. The third row shows the temporal evolution of sample origin with the pump intake located at the middle of the screen. In all cases the pumping rate is 0.3 l/min. Particle color indicates time, arrowed lines indicate long-time pumping capture zone.

3.2. Ambient vertical-flow simulations

3.2.1. Sensitivity of ambient vertical flows in unpumped wells to aquifer and well properties

The following observations are made on the vertical flow simulations (and therefore the likelihood of vertical flows occurring in wells) during unpumped conditions (Fig. 4):

1) The farther the well is from the outflow boundary, the smaller the induced vertical flow in the well. In the main body of the aquifer, groundwater flow is predominantly horizontal; upward flows are only seen near the outflow boundary due to convergence of groundwater flow from deeper in the aquifer. A flow reversal is seen at a distance from the outflow boundary in Scenario 13 where recharge drives downward flow in the well.
2) In the discharge zone, simulated ambient vertical flows are within the observed range reported in the literature for well screens between 3 m and 10 m in length; in fact in the 3 m well the flows are much less than the maximum reported (a simulated value of 0.05 l/min compared with 0.3 l/min observed).
3) Anisotropy/heterogeneities provide a strong control on the degree of vertical flow simulated within the well. Under isotropic conditions, significant vertical flows are not seen until very close to the outflow boundary.

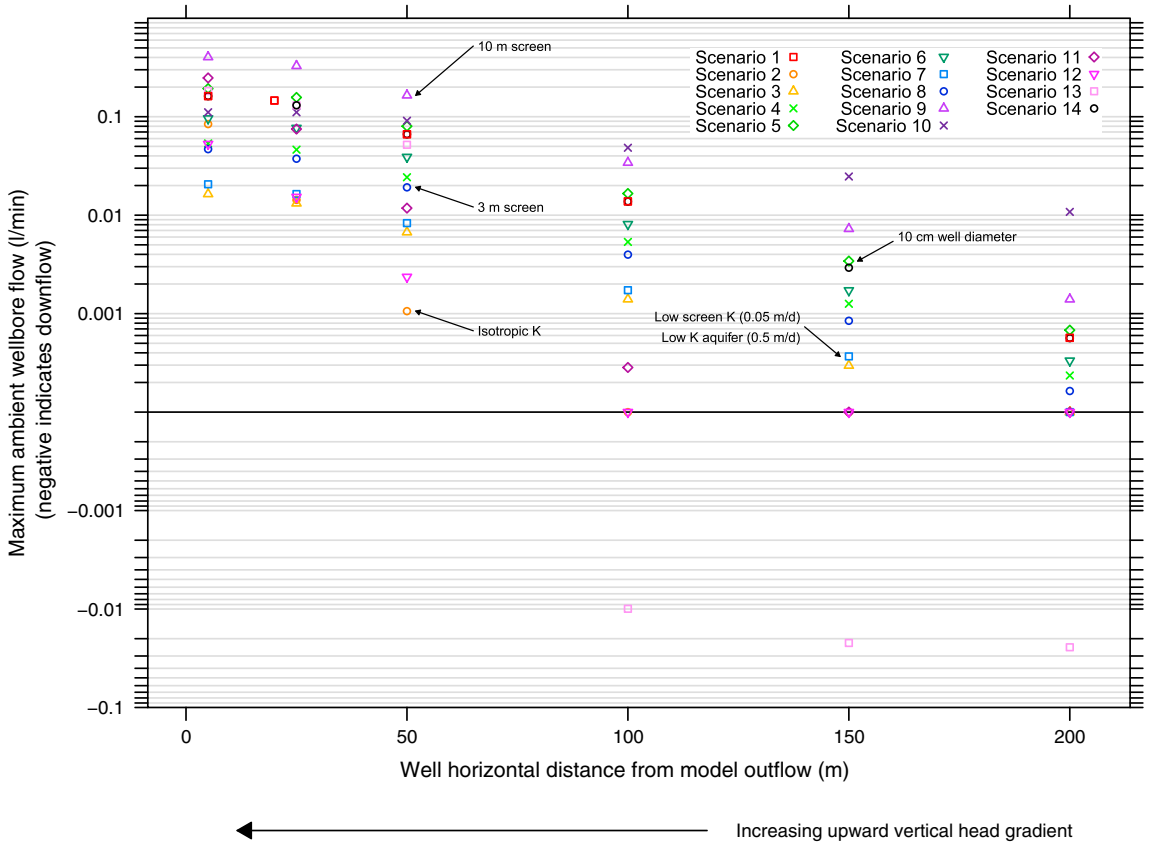

Fig. 4. Change in simulated maximum ambient upflow in the well with distance from the model specified head outflow boundary for all vertical flow scenarios.

4) Increasing well volume (length or diameter) increases the magnitude of vertical flows, with screen length having a greater effect as the head difference between opposite ends of the screen is greater.
5) Lower aquifer *K* values reduce flows into and out of the well and hence decrease vertical flows in the well. Reducing screen *K* has a similar effect. However, care should be taken if undertaking pumped sampling in low permeability settings or with a low *K* screen in order to prevent excessive drawdown.

Typical ambient vertical flow patterns in the well were similar to those noted by others (Konikow and Hornberger, 2006; Reilly et al., 1989; Segar, 1993), with inflows biased towards the region of highest head intersected by the well screen (the bottom of the well in this case) and outflows towards that of lowest head (the top of the well screen) (Fig. 5a). A gradual reduction of inflows and increase of outflows is observed between these two points. If the hydraulic conductivity distribution is not homogenous, inflows and outflows may still be biased towards zones of higher conductivity intersected by the well screen (Fig. 5b).

3.2.2. Origin of pumped sample water from wells with ambient vertical flows

With increasing vertical flows, pumping may not be able to counteract the vertical head gradients that generate ambient upflow in the well. The sample origin becomes biased towards the ambient inflowing zones in the well (e.g., results from Scenario 1, 5 and 8, Fig. 6).

For Scenario 8 (3 m screen) pumping at 0.3 l/min is sufficient to partially overcome the ambient vertical head gradients generating a maximum ambient upflow in the well of 0.05 l/min (Fig. 6c, f). Like the baseline case (Fig. 3i), at long times the sample is drawn from the entire screen interval and is independent of the pump intake position. However, it requires over 60 min of pumping to reach this position. Unlike the baseline case, the sample origin does not depend only on the formation hydraulic conductivity distribution. The sample remains partially biased towards the zone of highest head intersected by the screen with a greater portion of the sample being drawn from the bottom of the screen interval.

In Scenario 1, with maximum ambient upflow in the well of 0.16 l/min, pumping at 0.3 l/min is insufficient to overcome the ambient vertical head gradients (Fig. 6a, d). Even after extended pumping, the pumped sample is drawn entirely from the bottom half of the screen interval. Like Scenario 8 (Fig. 6c, f), at long times the origin of the sample in the screen interval is independent of the pump intake position. During pumped sampling, ambient upflow, driven by the ambient vertical head gradient, continues in the upper portion of the screened interval of the well. This water bypasses the pump intake entirely; even if mixing with casing water were to occur, there will be no bias to the sample in this case.

Unlike the two previous cases, for Scenario 5, with ambient upflow in the well of 0.19 l/min, pump intake

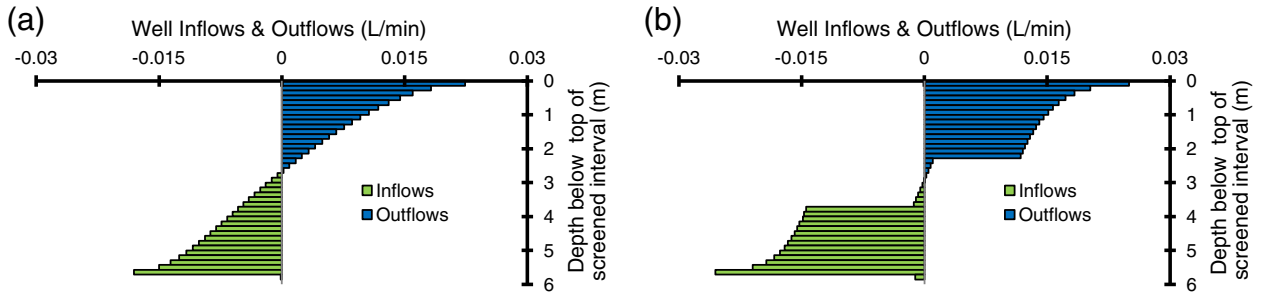

Fig. 5. Simulated ambient well inflows/outflows under vertical head gradients for: (a) Scenario 1 (6 m well screen, 1:10 anisotropy) and, (b) Scenario 11 (6 m well, 1.5 m thick low *K* layer intersecting the middle of the well) with the well located 5 m from the outflow boundary.

position is important even after extended pumping. Different portions of the aquifer are sampled when the pump intake is positioned in the middle (Fig. 6b) or the bottom of the screen interval (Fig. 6e). With the pump intake located at the bottom of the screen interval (the zone of the screen with highest inflow), the pumped sample is drawn from only the bottom third of the well. Any ambient flows entering farther up the well screen bypassing the pump intake entirely

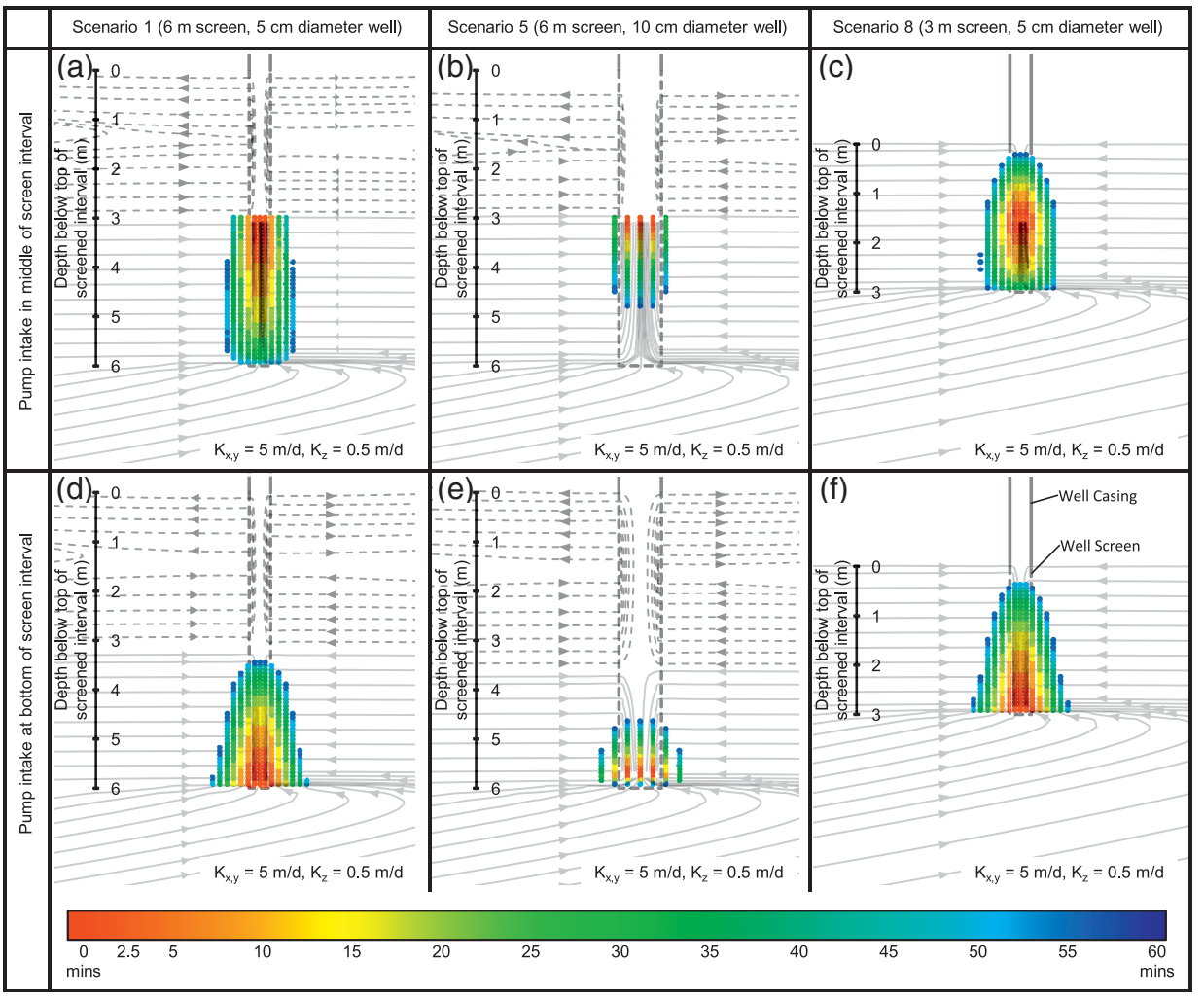

Fig. 6. Simulated change in pumped sample origin with time for Scenarios 1, 5 and 8. The first row shows the evolution in sample origin with the pump intake located in the middle of the screen interval. The second row shows the evolution in sample origin with the pump intake located at the bottom of the screen interval. In all cases the pumping rate is 0.3 l/min. Maximum ambient upflow in the well are 0.16, 0.19 and 0.05 l/min for Scenarios 1, 5 and 8 respectively. Particle color indicates time, solid arrowed lines indicate long-time pumping capture zone, and dashed lines indicate flows in the well that bypass the pump intake.

(Fig. 6e). Moving the pump intake to the middle of the well screen (Fig. 6b), the zone of the well with highest flow, allows a mixture of the entire inflowing zone of the screen to be sampled. This maximizes the portion of the aquifer sampled but gives a more mixed sample.

The pump intake position has very little effect on the well inflows and outflows during pumping (Fig. 7a). The difference in sample composition due to the pump intake location is clearer when considering the patterns of vertical flows in the well during pumping (Fig. 7b). When the pump intake is located in the middle of the screened interval, 0.045 l/min of groundwater entering the well through the lower half of the screen interval flows past the pump intake during pumping. The volume of water not captured by the pump depends on the rate of ambient vertical flows in the well.

As suggested by (Greswell et al. (in press)), in wells with high ambient vertical flows, pumped sampling at low rates can be thought of as almost analogous with taking a passive sample when compared with the volumes of groundwater flowing passed the pump intake. Groundwater not captured by pumping will exit the well higher up in the screen interval. The pumped sample composition will depend on the degree of in-well mixing between streamlines originating from different screen intake points. If lateral dispersion and mixing between streamlines in the well are low, sampling may only draw from a subset of upward flowing streamlines. If the pumped sample does not represent a fully mixed snapshot then horizontal position of the pump intake in the well becomes important in sample origin and sample repeatability. It can be inferred that dispersion and mixing are also important if the pump intake is located at the top of the well. The sample origin will depend on what water is carried to the pump intake, what water exits the well screen lower down, and the degree of mixing between waters of different origin moving upwards in the screen interval. If full mixing between streamlines can be assured, taking multiple samples at different depths in the screened portion of the well may be a way of assessing vertical changes in water quality from different screen inflow points.

3.2.3. The transition from baseline conditions to vertical ambient head gradient biased samples

As ambient upflow increases, a transition from permeability-weighted sampling conditions to vertical head gradient biased conditions occurs. The sample becomes increasingly biased towards the zone of the screen intersecting the region of highest head (Fig. 8a). For a fixed pumping rate, sample origin depends on the rate of ambient upflow in the well. However, sample bias does not occur only when ambient vertical flows in the well are much greater than the pumping rate. For example, considering Scenario 1 (Fig. 8a), the sample origin begins to become biased towards the zone of highest head intersecting the screen for ambient vertical flows in the well of only 0.01 l/min. Once the maximum ambient flow in the well reaches 0.07 l/min the inflow to the well is zero at the top of the screen during pumping. As the maximum ambient upflow increases to 0.15 l/min (50% of the pumping rate) the sample origin is dominated by the ambient vertical hydraulic gradient and the sample is drawn from the bottom half of the screen interval only.

Comparing the percentage bias to the pumped sample due to ambient vertical flows (Eq. (1)) against the maximum ambient upflow in the well, a similar pattern is observed for all scenarios (Fig. 8b). As the maximum ambient upflow in the well increases from 0% to 50% of the pumping rate the percentage bias increases. A transition between baseline sampling conditions and vertical head gradient biased conditions occurs. Within this transition zone sample origin is very sensitive to ambient upflow rates. If ambient vertical flows in the well vary (e.g. seasonally), sample origin during pumped sampling will differ even if fixed sampling procedures are used. A similar conclusion is drawn by Riley et al. (2011) for tracer testing in the presence of vertical flows.

As the maximum ambient upflow in the well increases beyond 50% of the pumping rate, the percentage bias to sampling levels off. The well inflows are determined by the ambient vertical head gradients with pumping having little ability to counteract vertical flows in the well. Changes in ambient vertical flow rates become less important to the sample origin, pump position becomes important even at long times and pumped sampling becomes increasingly analogous to a passive sample.

3.2.4. Overcoming ambient vertical flow bias via increased pumping

If a well sampling is undertaken at higher pumping rates, vertical gradients can be overcome and the sample can be drawn from the entire screen interval. For Scenario 1, with

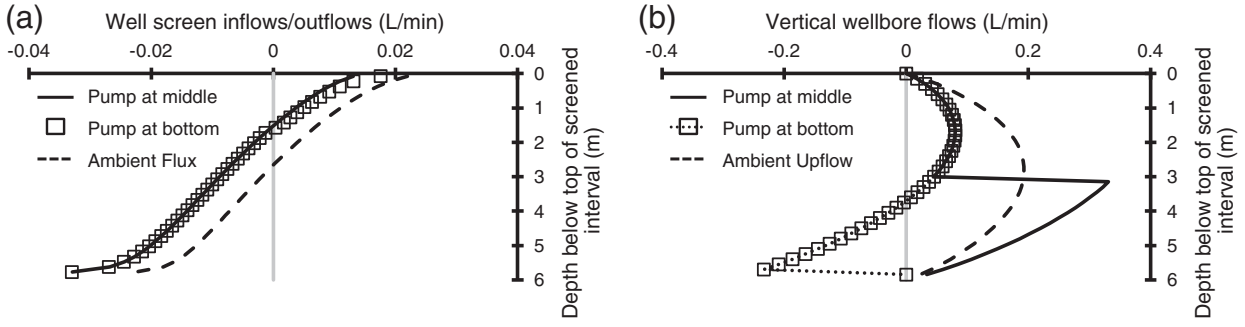

Fig. 7. Comparison of well flows for Scenario 5 under ambient vertical head gradients with pump intake located at the bottom and middle of the screen. (a) Inflows and outflows in the well screen under ambient and pumping conditions (negative indicates inflow), and (b) vertical flows in the well under ambient and pumping conditions (negative indicates downward flow). Maximum ambient upflow in the well is 0.19 l/min.

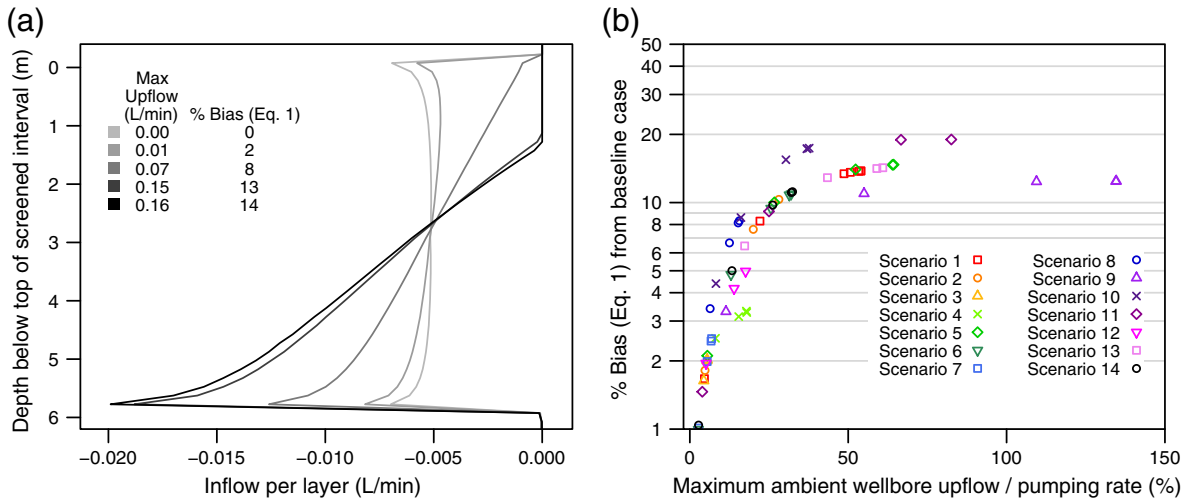

Fig. 8. Departure from no vertical flow baseline as a function of ambient upflow in the well: (a) deviation from baseline (Eq. (1)) and variation in pumped influxes for Scenario 1 (Q = 0.3 l/min), (b) deviation from baseline conditions for all scenarios.

maximum ambient upflow in the well of 0.16 l/min, pumping at 0.3 l/min results in vertical flow bias of 14% (Fig. 9). Increasing the pumping rate to 2 l/min reduces the ambient vertical flow induced bias to <10%. However, achieving a 10% bias does not provide a sample drawn from the entire screen interval (Fig. 8a). The pumping rate has to be increased to 10 s·l/min to approach 0% bias and achieve a permeability-weighted sample unbiased by ambient vertical head gradients. The pumping rate required to fully overcome vertical head gradients is many tens of times the vertical head gradient driven ambient upflow in the well.

Using the simulated maximum ambient upflow in the well to compare all scenarios, a linear relationship exists between the maximum ambient upflow simulated in the well and the pumping rate required to overcome the vertical gradient induced bias. For example, to reduce the ambient vertical flow induced sampling bias to 3% (Eq. (1)) it is necessary to pump at 11.5 times the maximum ambient upflow rate in the well (Fig. 10a). Similar linear relationships exist for other percentage biases (Fig. 10b). As observed for Scenario 1 (Fig. 9), it is necessary to use a pumping rate of tens of times the ambient vertical flow rate in the well to fully overcome ambient vertical head gradients and achieve a bias approaching zero. Hence, for the modeling scenarios considered, knowledge of the maximum ambient upflow in the well is enough to estimate the pumping rate required to overcome the in-well vertical flows. Detailed knowledge of the flow distribution was not required.

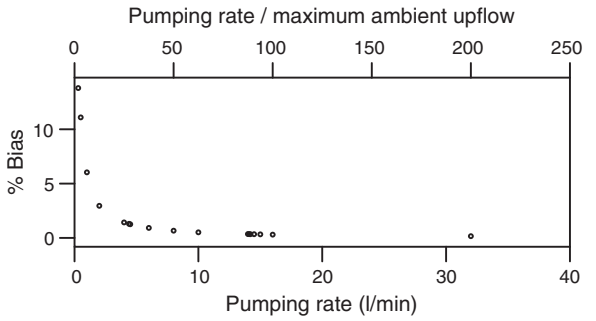

Fig. 9. Variation in sample bias (Eq. (1)) with increasing pumping rate under ambient vertical head gradients (Scenario 1, maximum ambient vertical flow in the well = 0.16 l/min).

The implication for groundwater sampling in wells with maximum ambient upflow in the range observed by (Elci et al., 2001) (0.015–2.3 l/min) is that low-flow sampling will be biased towards the zones of highest head intersecting the screen. Increasing the pumping rates to several liters per minute may not fully overcome the ambient vertical head gradients observed. To obtain a permeability-weighted sample from across the screen interval during pumped sampling in these wells the pumping rate may need to be tens of liters per minute or higher.

4. Conclusions

Numerical modeling to evaluate the effect of ambient vertical flows on groundwater sampling using pumps has demonstrated that naturally occurring vertical flows of the magnitude reported in literature may be a key control on sample origin even in wells with screens <10 m in length. If permeability-weighted sampling from across the screen interval is the goal it may be necessary to pump at rates many times the ambient vertical flow rate in the well. Purging at low pumping rates such as those recommended for low-flow sampling would not be sufficient. Ambient vertical flows in the wellbore are increased by:

1) greater aquifer hydraulic conductivity and greater aquifer depth;
2) greater proximity to discharge (or recharge) zones;
3) greater well volume (well diameter and length), screen hydraulic conductivity;
4) and greater vertical/horizontal hydraulic conductivity anisotropy (including the presence of discrete layers of low permeability).

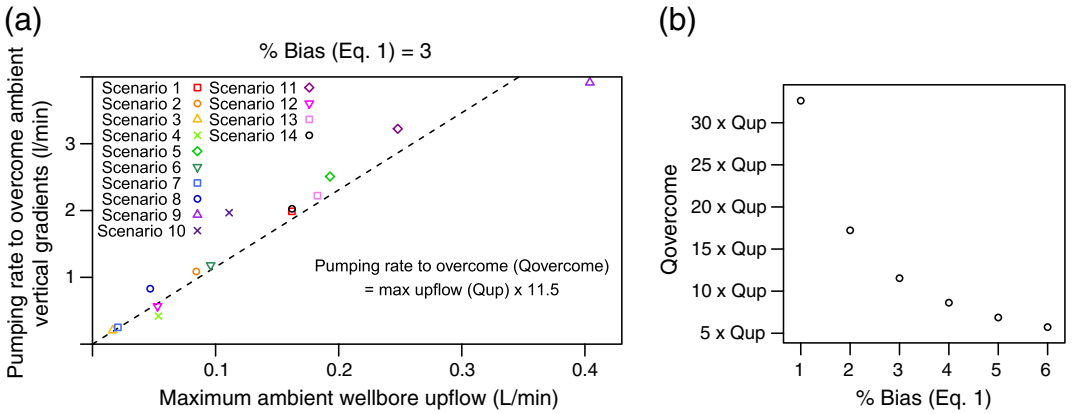

Fig. 10. Pumping rate required to overcome ambient vertical head gradients as a function of ambient well upflow: (a) maximum ambient well upflow versus pumping rate required to reduce sample bias (Eq. (1)) to 3% (all scenarios), and (b) pumping rate to overcome vertical head gradients versus % bias (all scenarios).

For situations where the maximum ambient upflow in the well is <5% of the pumping rate the numerical modeling undertaken here has demonstrated that:

1) it is possible to overcome ambient vertical gradients, even with low-flow pumping, and achieve a sample drawn from the entire screen interval;
2) pumping rate and time (which can be significant in sampling terms) are important controls on sample origin (this is the case even without vertical flows);
3) and during early pumping the sample origin will depend on pump intake position but at long times may be pump independent.

As ambient upflow in the well increases towards 50% of the pumping rate, a transition occurs. The sample becomes increasingly biased towards the zone of highest head intersecting the screen. In these cases:

1) water may not be drawn from the entire saturated screen interval even with extended pumping times;
2) if ambient vertical flow rates vary (e.g. seasonally), the sample origin may vary even if pump intake position, pump rate and pump time are fixed;
3) pump intake position is important in determining the sample origin, this may be the case even after an extended pumping period;
4) targeting the zone of the well with maximum vertical flow maximizes the vertical extent of aquifer sampled.

For wells with ambient upflow rates much greater than the pumping rate the sample is entirely biased towards the zone of highest head. The pumped sample becomes analogous to a passive sample. In these cases:

1) pumping rate and time are not important;
2) pump intake position is the key control on the sample origin
3) sampling from the base of a borehole provides a more discrete sample from that inflow zone, and through appropriate choice of sampling location might enable level-determined sampling
4) however, quantitative predictions of water quality variation with depth will depend on assessing the degree of dispersion and mixing as water of different origins enters and exits the well screen

Vertical flows can introduce considerable uncertainty when attempting to relate sample concentration to in-aquifer conditions, even in wells with screens <10 m in length. Knowledge of the ambient vertical flow rate in the well can be used, in conjunction with sampling objectives, to guide decisions on pumping rate, pumping duration and pump intake location. From a practitioner community viewpoint, sampling objectives will determine if a detailed knowledge of sample origin is required. If this detailed knowledge is required then supporting vertical flow investigations are recommended.

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