# NONLINEAR BIAS CORRECTION FOR SATELLITE DATA

# ASSIMILATION USING TAYLOR SERIES POLYNOMIALS

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#### **ABSTRACT**

Output from a high-resolution ensemble data assimilation system is used to assess the ability of an innovative nonlinear bias correction (BC) method that uses a Taylor series polynomial expansion of the observation-minusbackground departures to remove linear and nonlinear conditional biases from all-sky satellite infrared brightness temperatures. Univariate and multivariate experiments were performed in which the satellite zenith angle and variables sensitive to clouds and water vapor were used as the BC predictors. The results showed that even though the bias of the entire observation departure distribution is equal to zero regardless of the order of the Taylor series expansion, there are often large conditional biases that vary as a nonlinear function of the BC predictor. The linear 1st order term had the largest impact on the entire distribution as measured by reductions in variance; however, large conditional biases often remained in the distribution when plotted as a function of the predictor. These conditional biases were typically reduced to near zero when the nonlinear 2nd and 3rd order terms were used. The univariate results showed that variables sensitive to the cloud top height are effective BC predictors especially when higher order Taylor series terms are used. Comparison of the statistics for clear-sky and cloudy-sky observations revealed that nonlinear departures are more important for cloudy-sky observations as signified by the much larger impact of the 2nd and 3rd order terms on the conditional biases. Together, these results indicate that the nonlinear BC method is able to effectively remove the bias from all-sky infrared observation departures.

## 1. Introduction

The ability to generate accurate cloud and water vapor (WV) analyses suitable for numerical weather prediction (NWP) models is perhaps the most challenging aspect of modern data assimilation (DA) systems because they typically assume Gaussian error statistics and that linear relationships exist between the observations and model state variables. Cloud processes, however, are inherently nonlinear with complex interactions occurring between different cloud hydrometeor species and the local thermodynamic environment at spatial and temporal scales that are typically much smaller than those represented by NWP models. Likewise, WV content can change rapidly in space and time and can influence the evolution of the cloud field in nonlinear ways. These and other factors can make it very challenging to effectively assimilate information from cloud and WV sensitive observations.

Remotely sensed observations obtained using geostationary and polar-orbiting satellites provide
the only reliable source of high-resolution cloud and WV information covering large geographic
domains. Sophisticated visible, infrared, and microwave sensors onboard various satellite platforms provide information about the spatial distribution and characteristics of the cloud and WV
fields. For regional-scale NWP, observations from geostationary satellites are especially useful
because their continuous viewing of the same area with high temporal and spatial resolution allow
them to more easily constrain the evolution of rapidly changing weather features (Vukicevic et al.
2006; Errico et al. 2007). Satellite observations, however, often exhibit biases when compared to
their model equivalents computed using the NWP model background; therefore, bias correction
(BC) methods are typically required to assimilate these observations (Eyre 2016).

Observation-minus-background (OMB) biases can occur for a variety of reasons and can differ for clear and cloudy observations. For example, biases can arise from calibration errors in a satel-

lite sensor or to instrument "drift" as a sensor ages. Biases can also be introduced by deficiencies in the forward radiative transfer models used to compute the model equivalent brightness temper-61 atures. For clear-sky observations, biases may result from errors in the specification of surface emissivity, simplifications in the radiative transfer model equations, inadequate vertical resolution or a low model top in the NWP model, or the misspecification or absence of atmospheric constituents (such as aerosols) observed by some satellite bands. In the context of clear-sky DA, biases can also be introduced by incomplete cloud screening procedures that allow some cloudaffected observations to pass quality control and thereby incorrectly enter the DA system. Indeed, most existing quality control methods were originally designed to remove all cloud-affected observations; however, these constraints are being relaxed as operational modeling centers move toward all-sky DA (e.g., Okamoto et al. 2014; Zhu et al. 2016). Exclusion of cloud-affected brightness temperatures has the undesirable consequence of removing observations that could have been used 71 to improve the model initialization in cloudy areas of the model domain. 72

Additional uncertainties regarding the specification of cloud properties arise when assimilating cloud-affected infrared brightness temperatures. Though forward radiative transfer modeling for cloudy scenes has become more accurate in recent years, deficiencies remain, especially for ice clouds. Simulation of absorption and scattering properties for liquid clouds is relatively straightforward because the droplets are assumed to be spherical. However, there are larger uncertainties with ice cloud bulk optical properties because there is some dependence in the infrared on the shape of the ice particles (Yang et al. 2013). For example, an ice particle may take the form of a hexagonal plate, solid or hollow column, bullet rosette, or an aggregate of some form, and impact the bulk microphysical and optical properties that result from integration of the individual particle properties over the assumed size and habit distributions (Baum et al. 2014). In addition, the ice water path is related to both the cloud optical thickness and the cloud particle effective diameter.

When computing simulated brightness temperatures, these diameters should be computed using the particle size distribution and cloud property assumptions made for each cloud species by a given microphysics scheme (e.g. Otkin et al. 2009; Cintineo et al. 2014; Thompson et al. 2016). 86 Biases in the OMB departures can also be caused by systematic errors in the NWP model fore-87 casts that result from deficiencies in the parameterization schemes or other characteristics of the NWP model. It is well known that model forecasts containing large biases influence the behavior of BC methods and can degrade the performance of DA systems (Dee 2005; Dee and Uppala 2009; Eyre 2016). Biases can be especially large for model variables for which few observations are available to constrain their evolution, such as root zone soil temperature and moisture (Mahfouf 2010), or variables such as clouds and water vapor that are strongly influenced by parameterization schemes accounting for sub-grid scale processes. For example, uncertainties in microphysical parameters controlling cloud generation and decay processes can lead to systematic errors in the spatial extent, optical thickness, and height of the clouds, which in turn impacts the simulated satellite brightness temperatures (Otkin and Greenwald 2008; Cintineo et al. 2014; Eikenberg et al. 2015). Ideally, a BC method would not remove the bias in the OMB departures associated with deficiencies in the NWP model because the observations should be used to correct such systematic errors. In the absence of a perfect reference analysis, however, it can be very difficult to 100 determine whether a bias originates in the observations or forward radiative transfer model, both 101 of which should be corrected, or in the model background (Dee 2005). Because of this uncertainty 102 in bias attribution, all BC methods functionally act to correct the bias in the "observations" regardless of the true sources of the bias (Dee and Uppala 2009). Though this outcome is not desirable 104 because it will limit the ability of the observations to reduce systematic errors in the analysis, it 105 does satisfy the requirement by most DA methods that the observations are unbiased. In addition, the bias corrected observations can still be used to reduce random errors in the analysis. Eyre

the NWP model state relaxes back toward its own climatology after the assimilation update. If an NWP model quickly returns to its preferred state, then the analysis errors will continue to be large even if the model bias can be removed prior to computing the BC coefficients. This points toward the need to fix the bias at its source within the NWP model. The impact of model bias on a BC method can be reduced when high quality "anchor" observations with little or no bias are available; however, it is not apparent that such observations exist for water vapor and clouds.

BC methods can be broadly categorized into two types (Eyre 2016). The first type uses depar-115 tures between the observations and their model equivalents accumulated over long time periods 116 outside of the DA system to estimate and remove the bias from the observations prior to their assimilation. These so-called "static" BC methods typically use the satellite scan angle along with several atmospheric variables, such as the geopotential thickness over some layer, as the BC pre-119 dictors. The BC coefficients for each satellite sensor and band are then computed using linear 120 least squares regressions between the predictors and the observations. In practice, however, these 121 "static" BC coefficients are regularly updated to account for changes in the model background due 122 to changes in the NWP model or DA system, the addition of new observations, and upgrades to 123 the forward radiative transfer model. Frequent retuning of a static BC method can be beneficial because it makes it more adaptable to changes in the models and observations. More detailed de-125 scriptions of static BC methods can be found in Eyre (1992), Harris and Kelly (2001), and Hilton 126 et al. (2009).

With the second type of BC method, known as variational BC (VarBC), the BC coefficients are updated simultaneously with the control vector during each DA cycle using the same set of observations and an augmented control vector (Derber et al. 1991; Parrish and Derber 1992; Derber and Wu 1998; Dee 2005; Auligne et al. 2007; Dee and Uppala 2009; Zhu et al. 2014). Like static BC

methods, VarBC typically uses the satellite scan angle and several variables describing the atmospheric state as the predictors, with the total BC treated as a linear combination of all predictors.

The BC coefficient for each predictor is computed during the minimization of the variational cost function. With an incremental DA approach with multiple outer loops, the BC coefficient increments evolve during each iteration of the inner loop and are updated at the end of each outer loop, which allows the coefficients to adjust with time and capture changes in observation quality. The state space augmentation approach used by VarBC also requires an estimate of the background covariances of the augmented state vector. For simplicity, most schemes assume that the error for a given BC parameter is uncorrelated with errors in other parameters for other satellite sensors and bands and with errors in the model background (Derber and Wu 1998; Dee 2005).

Most BC methods have been developed for use in variational or hybrid DA systems; however, 142 several studies have also explored BC in ensemble DA systems. Fertig et al. (2009) developed a 143 BC method for ensemble DA that is similar to VarBC in that it uses state augmentation to estimate the biases during the assimilation step. They showed that their method was able to reduce both the observation bias and the analysis error in perfect model experiments. Similar methods have also 146 been used successfully in real data experiments assimilating microwave brightness temperatures 147 (Szunyogh et al. 2008; Aravequia et al. 2011; Miyoshi et al. 2011). In high-resolution observing system simulation experiments assimilating infrared brightness temperatures, Cintineo et al. 149 (2016) found that the analysis and forecast accuracy was improved when a simple fixed-value BC 150 was applied to the clear-sky observations similar to that used by Stengel et al. (2009, 2013) in a variational DA system. Cintineo et al. (2016), however, did not bias-correct the cloudy obser-152 vations prior to their assimilation because their bias was too complex to properly handle using a 153 simple fixed-value BC applied uniformly to all cloudy observations. Zhu et al. (2016) handled biases in all-sky microwave observations by computing the BC coefficients using only cases where both the model background and the observations were either clear or cloudy. By doing this, they
were able to reduce errors associated with mismatched cloud fields, while still preserving clouddependent information in the matched observations. Together, these results provide evidence that
more sophisticated BC methods that can account for changes in cloud properties are necessary to
effectively remove biases in the OMB departures.

In this study, we present a new BC method that can be used to diagnose and remove biases in 161 all-sky infrared brightness temperatures using a Taylor series polynomial expansion of the OMB 162 departures. This approach can diagnose both linear and nonlinear bias components through use of higher order Taylor series terms and a set of BC predictors. For example, with a 3rd order 164 approximation, the 0th and 1st order terms represent the constant and linear bias components, 165 whereas the 2nd (quadratic) and 3rd (cubic) order terms represent nonlinear bias components. We use this nonlinear BC (NBC) method to remove the bias from Scanning Enhanced Visible and 167 Infrared Imager (SEVIRI) infrared brightness temperatures that were passively monitored during 168 high-resolution ensemble DA experiments. The paper is organized as follows. The DA framework is described in Section 2, with a mathematical description of the NBC method presented in Section 170 3. Statistics obtained using the NBC method are shown in Section 4, with conclusions and a 171 discussion presented in Section 5. 172

## 173 2. Experimental Design

#### a. SEVIRI Satellite Datasets

The SEVIRI sensor onboard the Meteosat Second Generation satellite provides accurate topof-atmosphere radiance measurements across 12 visible and infrared spectral bands with a nadir resolution of 3 km for all infrared bands (Schmetz et al. 2002). The utility of the NBC method was

evaluated using brightness temperatures from the 6.2  $\mu$ m and 7.3  $\mu$ m bands sensitive to WV over broad layers of the upper and middle troposphere, respectively, when skies are clear, while also 179 being sensitive to clouds when they are present. Under clear conditions, the weighting functions 180 that depict how much radiation from a given atmospheric height reaches the top of the atmosphere 181 peak near 350 hPa (500 hPa) for the 6.2  $\mu$ m (7.3  $\mu$ m) bands, and then decrease to zero in the 182 lower troposphere. When clouds are present, however, the weighting functions are truncated near 183 the cloud top, which means that a larger portion of the top-of-atmosphere radiation originates at 184 higher (e.g. colder) altitudes than would occur under clear-sky conditions. Their dual sensitivity to clouds and WV means that observations from these bands provide valuable information about 186 the atmospheric state that is typically not available with conventional observations. Another mo-187 tivation for using these bands is the expectation that their OMB departure statistics will be more Gaussian than would occur with infrared "window" bands because there will be a smoother tran-189 sition between the brightness temperatures in adjacent clear and cloudy areas. 190

Cloud top height retrievals made using SEVIRI observations were also obtained using software 191 provided by the EUMETSAT Nowcasting Satellite Applications Facility and will be used as one 192 of the BC predictors. The cloud top height for each satellite pixel was estimated by computing 193 simulated clear-sky 10.8 µm brightness temperatures using the RTTOV radiative transfer model (Saunders et al. 1999) and temperature and humidity profiles from the global GME model (Majew-195 ski et al. 2002), and then inserting a cloud at successively higher levels until a best fit is obtained 196 between the observed and simulated brightness temperatures (Derrien and Le Gleau 2005; Le Gleau 2016). To reduce the data volume and minimize the impact of spatially correlated errors 198 in the observation departures, the cloud top height retrievals and SEVIRI brightness temperatures 199 were horizontally thinned by a factor of 5 in the zonal and meridional directions. This reduces their horizontal resolution to  $\sim$ 20-25 km across the model domain, and is  $\sim$ 8 times coarser than the NWP model resolution. The cloud top height retrievals have a vertical resolution of 200 m; however, their uncertainty is larger, especially for semi-transparent clouds (Le Gleau 2016).

## 204 b. KENDA Data Assimilation System

Ensemble DA experiments in which conventional observations were actively assimilated and 205 SEVIRI brightness temperatures were passively monitored were performed using the Kilometerscale Ensemble Data Assimilation (KENDA) system (Schraff et al. 2016) developed by the 207 Deutscher Wetterdienst (DWD). The KENDA system is based on the local ensemble transform 208 Kalman filter method described by Hunt et al. (2007) and uses the Consortium for Small-scale Modeling (COSMO) model (Baldauf et al. 2011) as the NWP model. During this study, ra-210 diosonde, surface, wind profiler, and aircraft observations, were actively assimilated using a 1-h 211 assimilation window, whereas SEVIRI 6.2  $\mu$ m and 7.3  $\mu$ m brightness temperatures were passively monitored. With KENDA, 4-D assimilation capabilities are obtained through inclusion of the ob-213 servation operators within the COSMO model so that the model equivalents can be computed at the exact observation times during the forward integration of the ensemble. Temporally and spatially varying covariance inflation values are obtained at each grid point through a combination 216 of multiplicative covariance inflation based on Anderson and Anderson (1999) and the relaxation 217 to prior perturbations approach described by Zhang et al. (2004). Covariance localization is performed by updating the analysis at each grid point using only those observations located within 219 a specified distance of the grid point. The vertical localization scale is fixed, but increases with 220 height, whereas the horizontal scale is determined adaptively. For more detailed information about 221 the KENDA system, the reader is referred to Schraff et al. (2016). 222

This study uses output from ensemble DA experiments that were performed on the COSMO-DE domain covering all of Germany and parts of surrounding countries with 2.8 km horizontal grid

spacing. Lateral boundary conditions were obtained at hourly intervals from the 7-km resolution COSMO-EU domain run at the DWD, which in turn is driven by boundary conditions provided 226 by the Icosahedral non-hydrostatic (ICON) model (Zangl et al. 2015). The COSMO-DE domain 227 covers approximately 1200 x 1200 km and contains 50 vertical levels that are terrain-following in the lower troposphere and become horizontally flat in the upper troposphere and stratosphere. The 229 model top is located at 22 km (i.e. about 40 hPa). The DA experiments employed 40 ensemble 230 members along with a deterministic run that is initialized by applying the Kalman gain matrix from 231 the assimilation update to the deterministic model background. The ensemble and deterministic runs were initialized at 00 UTC on 16 May 2014 and then updated at hourly intervals during a 233 5-day period ending at 00 UTC on 21 May 2014.

Atmospheric prognostic variables in the COSMO model include the horizontal and meridional 235 wind components, temperature, pressure, and the mixing ratios for water vapor, cloud water, rain-236 water, pristing ice, snow, and graupel. Cloud microphysical processes, such as autoconversion, 237 accretion, and self-collection, are represented using a simplified version of the Seifert and Beheng (2001) double-moment microphysics scheme that was reduced to a single-moment scheme 239 for computational efficiency. Cloud formation and decay processes are parameterized based on 240 the work of Lin et al. (1983). Heating rates due to radiative effects are updated at 15-min intervals using the  $\delta$ -2-stream method developed by Ritter and Geleyn (1992). Deep convection 242 is explicitly resolved whereas shallow convection is parameterized using a simplified version of 243 the Tiedtke (1989) mass-flux scheme. A 2.5 order turbulent kinetic energy scheme developed by Raschendorfer (2001) is used to predict turbulence. 245

After an initial 12-h spin-up period, simulated SEVIRI brightness temperatures were generated for each ensemble member and the deterministic run at hourly intervals during a 4.5-day period from 13 UTC 16 May 2014 to 00 UTC 21 May 2014 using first-guess model output from 1-h

COSMO-DE forecasts. The model profiles were interpolated to the thinned SEVIRI observation locations, and then simulated 6.2  $\mu$ m and 7.3  $\mu$ m brightness temperatures were computed using 250 version 10.2 of the RTTOV radiative transfer model (Saunders et al. 1999). RTTOV includes an 251 enhanced cloud-scattering module that enables the use of cloud profiles located on the NWP model vertical grid (Matricardi 2005; Hocking et al. 2011). When computing cloudy brightness temper-253 atures, RTTOV requires vertical profiles of liquid water content, ice water content, and fractional 254 cloud cover. These quantities were computed using the COSMO model output and empirical rela-255 tionships developed by Kostka et al. (2014). The default maximum-random cloud overlap scheme in RTTOV based on Raisanen (1998) was used during this study. RTTOV also includes several 257 options to diagnose the ice particle effective diameters from the forecast ice water content based on relationships developed by Wyser (1998), Ou and Liou (1995), and McFarquhar et al. (2003) 259 along with two ice crystal shape options (aggregates and randomly-oriented hexagonal crystals) 260 that together are used to compute the ice radiative properties. For this study, we assume hexagonal 261 ice crystals and compute the particle diameters using the McFarquhar et al. (2003) method. These settings were chosen because they provided the smallest overall bias during the 108-h study pe-263 riod based on six sensitivity experiments using the various ice crystal diameter and shape options. 264 The mean brightness temperature for ice clouds between the best and worst options differed by 265 approximately 1 K for the 6.2  $\mu$ m band and 2.5 K for the 7.3  $\mu$ m band during the entire study 266 period (not shown), which illustrates the large uncertainty associated with the ice cloud property 267 lookup tables in RTTOV.

# 3. Nonlinear Bias Correction (NBC) Method

Traditional BC methods remove biases between a given set of observed and model-equivalent satellite brightness temperatures through use of a set of BC predictors that describe the atmospheric

state or characteristics of the satellite data. Both static and VarBC methods typically assume that a linear relationship exists between the departure bias and a given set of predictors or that a global 273 constant can be added to the observations. This linear BC approach has been shown to work well 274 for clear-sky observations possessing Gaussian error characteristics for which a set of constant and linear BC coefficients are sufficient to remove the bias; however, their use will be sub-optimal if the observation bias varies as a nonlinear function of some predictor. For satellite observations, 277 nonlinear error dependencies are more likely to occur when cloudy observations are assimilated 278 given the prevalence of nonlinear processes in clouds that could lead to complex errors in the forecast cloud field and the possibility that nonlinear error sources could be introduced by the forward 280 radiative transfer model used to compute the model-equivalent brightness temperatures. For example, with infrared brightness temperatures, it is possible that increased uncertainty simulating ice 282 radiative properties in forward radiative transfer models could lead to biases that are a nonlinear 283 function of some cloud property, such as cloud top height. Thus, given the increased interest in all-sky DA, it is desirable to develop BC methods that can remove both linear and nonlinear bias 285 components from the innovations. 286

One method that can be used to account for nonlinear error dependencies in a set of observations
is a Taylor series polynomial expansion that includes higher order terms that can capture nonlinear
features of the error distribution if they exist. For a given set of observed and model-equivalent
brightness temperatures corresponding to a specific satellite sensor and band, the observation departure vector is defined as:

$$\mathbf{dy} = \mathbf{y} - H(\mathbf{x}),\tag{1}$$

where **y** is the observation vector, **x** is the NWP model state vector, and  $H(\mathbf{x})$  is the observation operator that is used to compute the model equivalent brightness temperatures. If we assume that the bias in the observation departures can be described by a real function f(z) of a single variable

(e.g., predictor) that is infinitely differentiable around a real number c, Eqn. 1 can be decomposed into an N order Taylor series expansion:

$$\mathbf{dy} = \left( f(c) + \frac{f'(c)(z^{(i)} - c)}{1!} + \frac{f''(c)(z^{(i)} - c)^2}{2!} + \frac{f'''(c)(z^{(i)} - c)^3}{3!} + \dots + \frac{f^{(n)}(c)(z^{(i)} - c)^n}{n!} \right)_{\substack{i=1,\dots,m \\ (2)}}$$

where  $\mathbf{dy}$  is the m x 1 observation departure vector and m is the number of observations,  $f^{(n)}(c)$  is
the nth derivative of f evaluated at the point c, and  $z^{(i)}$  is the predictor value for the ith observation.

The i=1,...,m notation outside the parentheses indicates that the Taylor series approximation is
computed separately for each element of the  $\mathbf{dy}$  vector using the equation within the parentheses.

The variable used as the predictor is chosen based on its ability to capture some aspect of the
observation departure bias, whereas the value  $z^{(i)}$  of that variable for a given observation can be
obtained from a variety of sources, such as the model background or a satellite retrieval. The
constant c can be set to any value because  $c + \delta c$  simply moves c to another constant value;
therefore, for convenience, we define c to be the mean of the predictor values:

$$c = \frac{\sum_{i=1}^{m} z^{(i)}}{m} \tag{3}$$

It is readily apparent from Eqn. 2 that the higher order terms represent nonlinear components because the exponents are  $\geq 2$ , with the  $(z-c)^2$  and  $(z-c)^3$  polynomials representing the quadratic and cubic terms, respectively.

The single variable case shown in Eqn. 2 can subsequently be generalized to be a function of more than one predictor:

$$\mathbf{dy} = \left( f(a_1, \dots, a_d) + \sum_{j=1}^d \frac{\partial f(a_1, \dots, a_d)}{\partial x_j} (x_j^{(i)} - a_j) \right)$$

$$+ \frac{1}{2!} \sum_{j=1}^d \sum_{k=1}^d \frac{\partial^2 f(a_1, \dots, a_d)}{\partial x_j \partial x_k} (x_j^{(i)} - a_j) (x_k^{(i)} - a_k)$$

$$+ \frac{1}{3!} \sum_{i=1}^d \sum_{k=1}^d \sum_{l=1}^d \frac{\partial^3 f(a_1, \dots, a_d)}{\partial x_i \partial x_k \partial x_l} (x_j^{(i)} - a_j) (x_k^{(i)} - a_k) (x_l^{(i)} - a_l) + \dots \right)$$

$$+ \frac{1}{3!} \sum_{j=1}^d \sum_{k=1}^d \sum_{l=1}^d \frac{\partial^3 f(a_1, \dots, a_d)}{\partial x_i \partial x_k \partial x_l} (x_j^{(i)} - a_j) (x_k^{(i)} - a_k) (x_l^{(i)} - a_l) + \dots \right)$$

which can be written more compactly as:

$$\mathbf{dy} = \left(\sum_{n_1=0}^{d} \cdots \sum_{n_d=0}^{d} \left(\frac{\partial^{(n_1+\cdots+n_d)} f}{\partial x_1^{n_1} \cdots \partial x_d^{n_d}}\right) (a_1, \cdots, a_d) \frac{(x_1^{(i)} - a_1)^{n_1} \cdots (x_d^{(i)} - a_d)^{n_d}}{n_1! \cdots n_d!}\right)_{i=1,\dots,m}, \quad (5)$$

where d is the number of predictors,  $f^{(n_d)}(a_d)$  denotes the nth partial derivative of f evaluated at the point  $a_d$ , and  $x_d^{(i)}$  is the ith value for a given predictor  $x_d$ .

For illustrative purposes, if we assume a single variable, third order Taylor series expansion for a single satellite sensor and band, and define the BC coefficients such that  $b_n = \frac{f^{(n)}(a)}{n!}$ , Eqn. 2 can be written as:

$$\mathbf{dy} = \left(b_0 + b_1(z^{(i)} - c) + b_2(z^{(i)} - c)^2 + b_3(z^{(i)} - c)^3\right)_{i=1,\dots,m}$$
(6)

or alternatively in matrix notation as:

$$\mathbf{dy} = \mathbf{Ab} \tag{7}$$

where  $\mathbf{dy}$  is the  $m \times 1$  observation departure vector,  $\mathbf{A}$  is an  $m \times n$  matrix containing the n Taylor series terms  $(z^{(i)}-c)^l$  for each ith observation, where l=0,...,n-1, and  $\mathbf{b}$  is an  $n \times 1$  vector containing the BC coefficients. This is an overdetermined system of m linear equations in n unknown coefficients because m > n. The first column of  $\mathbf{A}$  contains ones, with the remaining columns containing the linear and higher order Taylor series terms. Because this kind of system typically does not have an analytic solution, we instead want to find the coefficients  $\mathbf{b}$  that best fit the equations by solving the quadratic minimization problem  $\hat{b} = \min_{b} S(b)$ , where the objective function S is

given by:

$$S(b) = \sum_{i=1}^{m} |dy_i - \sum_{i=1}^{n} A_{ij}b_j|^2 = \|\mathbf{dy} - \mathbf{Ab}\|^2$$
 (8)

and  $\|\cdot\|$  is the Euclidean norm. Because most real-world phenomena act as a low pass filter in the forward direction where **A** maps **b** to **dy**, the inverse mapping will operate as a high-pass filter that amplifies noise and can therefore lead to a poorly conditioned problem. Preference, however, can be given to smaller norms by adding a Tikhonov regularization term,  $\|\Gamma \mathbf{b}\|^2$ , to Eqn. 8, which is a standard approach when solving inverse problems (Nakamura and Potthast, 2015). For simplicity, we choose a matrix that is a multiple of the identity matrix ( $\Gamma = \alpha I$ ), such that:

$$\hat{S}(b) = \|\mathbf{dy} - \mathbf{Ab}\|^2 + \alpha \|I\mathbf{b}\|^2 \tag{9}$$

Sensitivity tests showed that  $\alpha$  could be set to a very small value  $(10^{-9})$  when one variable was used in the regression; however, a slightly larger value  $(10^{-6})$  was found to work better for the multivariate regressions. These values were used for the univariate and multivariate experiments presented in Section 4. The least squares solution can then be found by differentiating  $\hat{S}$  with respect to b, and equating to 0, such that:

$$\frac{\partial \hat{S}}{\partial b} = \mathbf{A}^T \mathbf{dy} - (\alpha I + \mathbf{A}^T \mathbf{A}) \mathbf{b} = 0, \tag{10}$$

or alternatively, after rearranging and multiplying both sides of Eqn. 10 by  $(\alpha I + \mathbf{A}^T \mathbf{A})^{-1}$ , we can solve for the b vector containing the BC coefficients using:

$$\mathbf{b} = (\alpha I + \mathbf{A}^T \mathbf{A})^{-1} \mathbf{A}^T \mathbf{dy}$$
 (11)

where  $(\alpha I + \mathbf{A}^T \mathbf{A})$  is a symmetric, square matrix with dimensions  $n \times n$ . The small dimensions of this matrix make it easy to compute its inverse, thereby making it feasible to include higher order Taylor series terms, additional predictors, and a large OMB departure dataset when computing the BC coefficients. After solving for  $\mathbf{b}$ , which is done separately for each satellite band and sensor,

the BC coefficients can then be applied to **dy** to remove the linear and nonlinear conditional bias components from the observations.

## 4. Results

In this section, the ability of the NBC method to remove biases from all-sky satellite infrared 346 brightness temperatures is assessed using OMB departure statistics accumulated at hourly intervals during a 4.5 day period in which conventional observations were actively assimilated and SEVIRI observations were passively monitored. Figure 1 shows the evolution of the observed SEVIRI 6.2 349 μm brightness temperatures during this time period. At the start of the period on 16 May (Fig. 350 1a), an area of cold upper level clouds associated with a band of precipitation was located across the eastern half of the domain. This weather feature slowly weakened over Germany during the 352 next two days (Fig. 1b, c), with the brightness temperatures becoming warmer as the convective clouds were replaced by cirrus and mid-level clouds. Generally clear skies characterized by warm brightness temperatures were also present across parts of the domain during this time period, with 355 clear skies prevailing across most of the region on 19 May (Fig. 1d). A large area of convection with very cold upper-level clouds then moved into the western half of the domain on 20 May (Fig. 1e). Overall, it is evident that the study period contains a wide range of atmospheric conditions 358 and cloud types that supports a realistic assessment of the NBC method during the warm season. 359

#### a. Univariate Bias Correction Results

To explore the ability of individual predictors to remove the bias from all-sky infrared observations, univariate NBC experiments were performed using the satellite zenith angle and various predictors sensitive to clouds and WV, such as the brightness temperature, cloud top height, and integrated water content over some vertical layer. This section presents results from a subset of

these experiments that remove the bias from all-sky SEVIRI 6.2  $\mu$ m observations. The impact of each predictor is assessed using OMB departure distributions normalized by the standard deviation in a given sample and with 2-D probability distributions of the departures plotted as a function of a given predictor. The results are evaluated separately for the original departure distribution and for distributions for which the bias has been removed using either a 0th (constant), 1st (linear), 2nd (quadratic), or 3rd (cubic) order Taylor series polynomial expansion.

### 1) Observed Brightness Temperature Predictor

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As shown by the probability distributions in Fig. 2, the observed 6.2  $\mu$ m brightness temperatures 372 are an excellent predictor of their own bias, especially when higher order Taylor series terms are 373 used. The horizontal magenta line in each panel depicts the mean bias of the entire distribution, 374 whereas the shorter horizontal black lines depict the conditional bias in each column and will be used to assess how the bias varies as a function of the predictor value. This terminology is 376 being used to differentiate biases conditioned on the predictor value from the bias of the overall 377 distribution. For example, though each distribution except for the original distribution will have zero overall bias, this obscures the fact that the conditional bias could potentially vary as a function 379 of the predictor value. Inspection of Fig. 2a reveals a nonlinear pattern in the conditional biases, 380 with a tendency for the simulated brightness temperatures to be too warm (cold) when the observed brightness temperatures are colder (warmer) than 235 K. Though the mean bias of the distribution 382 is relatively small (-0.83 K), the nonlinear pattern in the conditional biases means that constant 383 and linear BC terms alone will be unable to remove all of the bias. For example, even though the constant BC term removes the mean bias from the distribution (Fig. 2b), its shape remains the 385 same and therefore large conditional biases remain throughout the distribution. Likewise, the 1st 386 order BC term removes the linear departure component by raising (lowering) the cold (warm) end

of the distribution, which reduces the conditional biases for the coldest brightness temperatures,
but turns a positive bias into a negative bias for the warmest brightness temperatures (Fig. 2c).

Removal of the constant and linear bias components exposes an asymmetric arch shape in the
conditional biases that is largely removed when the 2nd order quadratic term is used (Fig. 2d),
except for nonzero biases that remain at the cold and warm ends of the distribution. Finally, when
the 3rd order cubic term is used, the general shape of the distribution is unchanged; however, it
is evident that subtle improvements were made to it given that most of the conditional biases are
now close to zero. Together, these results show that even though each BC distribution has zero
mean bias, that the conditional biases in the distribution are much smaller when the higher order,
nonlinear BC terms are applied to the observations.

Normalized OMB departure histograms computed using the original observations and the con-398 stant, 1st, 2nd, and 3rd order BC observations are shown in Fig. 3a-e. Each histogram is nor-399 malized based on its variance, with the curved red line on each panel representing a Gaussian 400 distribution with zero mean and a variance equal to that of the sample. Overall, the variance and 401 root mean square error (RMSE) are greatly reduced when the 1st order BC coefficients are ap-402 plied to the observations (Fig. 3c), which is primarily due to the smaller departures for the colder 403 brightness temperatures (e.g. Fig. 2c). The variance was further reduced when the 2nd order BC was used, with only minimal changes occurring when this was expanded to a 3rd order BC (Figs. 405 3d, e). The fact that the higher order terms only had a small impact on these statistics while simul-406 taneously having a large positive impact on the conditional biases in Fig. 2 illustrates that more detailed analysis methods such as 2-D probability distributions can provide additional insight into 408 the characteristics of the OMB departure distributions. Comparison of the histograms also shows 409 that the negative skewness in the original distribution (Fig. 3a) changes to positive skewness after the BC terms are applied. This behavior primarily results from a conditional positive skewness for brightness temperatures < 230 K that is evident in Fig. 2a by the tendency for the conditional bias in each column to be located above the bin with the maximum probability. Because the same BC is applied to a given brightness temperature regardless of its OMB departure, the positive skewness in the conditional distributions is preserved as they are shifted upward, thereby leading to a positive skewness in the full BC distributions.

### 17 2) CLOUD TOP HEIGHT PREDICTOR

Because infrared observations are very sensitive to the vertical distribution of clouds, an experi-418 ment was performed using the NWC SAF cloud top height retrievals as the BC predictor to better isolate the impact of clouds. To provide complete domain coverage, the clear-sky observations 420 were assigned a height equal to the model terrain elevation. Overall, the conditional biases in the 421 original distribution (Fig. 4a) are close to zero for cloud top heights < 7 km; however, the biases increase for clouds above this level and peak near -6 K for cloud top heights > 10 km. This is a 423 complex error pattern that a constant BC scheme is unable to fix (Fig. 4b). Indeed, the upward shift 424 of the distribution to remove the mean bias actually worsens the conditional biases for cloud top heights < 7 km, while leading to only minor improvements for the upper-level clouds. The linear 426 correction (Fig. 4c) slightly improves the conditional biases for lower and upper-level clouds, but 427 worsens the bias for mid-level clouds, which together slightly reduces the variance in the overall distribution (Fig. 3f). Use of the 2nd order quadratic term substantially improves the distribution 429 by removing the arch in the conditional bias pattern by decreasing the magnitude of the positive 430 (negative) OMB departures for cloud tops located in the middle (upper) troposphere (Fig. 4d). 431 These changes resulted in a much smaller variance in the histogram (Fig. 3g). As was the case in 432 the previous section, the 3rd order BC led to slightly smaller conditional biases across most of the 433 distribution (Fig. 4e), but had minimal impact on the statistics of the overall distribution (Fig. 3h).

Though the cloud top height predictor was unable to reduce the variance of the full distribution
as much as the brightness temperature predictor did, the NBC method was still able to greatly
improve the distribution by decreasing the conditional biases. Its use also led to a more symmetric
OMB departure distribution (Fig. 3h). These results show that cloud top height information can
be used to remove the bias from all-sky infrared observations if higher order Taylor series terms
are used.

#### 441 3) VERTICALLY-INTEGRATED WATER CONTENT PREDICTOR

In this section, the impact of using a BC predictor that depicts the total water content over a 442 vertical layer is assessed. Numerous experiments were performed using different vertical layers; 443 however, for brevity, results are only shown for the predictor that encapsulates the total water 444 content between 100 and 700 hPa because that is the portion of the atmosphere where 6.2  $\mu$ m brightness temperatures are most sensitive. Unlike the previous predictors, this predictor is com-446 puted using model output. The total water content is calculated for each ensemble member by converting the WV and all cloud hydrometeor mixing ratios in each model layer into mm and then integrating over the 100-700 hPa layer. Inspection of Fig. 5a shows that this predictor has 449 a less complex OMB departure pattern than occurred when the cloud top height and brightness 450 temperatures were used as the predictors. There are however slightly larger biases on both ends of the distribution, with a small upward slope in the maximum probabilities as the total water content 452 increases. This linear error trend is removed by the linear bias correction term (Fig. 5c), which 453 reduces the conditional biases when the total water content is < 7 mm, but increases it elsewhere. The subtle arch in the conditional biases is subsequently removed after applying the 2nd order 455 quadratic term (Fig. 5d), with only minor changes occurring after the 3rd order term is used (Fig. 456 5e). Comparison of the histograms (Figs. 3i-k) shows that the total water predictor had only a

small impact on the variance of the full distribution; however, the scatterplots showed that it still
improved the conditional bias across most of the distribution. Even so, this predictor still had
a much smaller impact than the previous predictors that were directly sensitive to the cloud top
height, which indicates that the location of the cloud top rather than the vertically integrated cloud
and WV content is a more effective BC predictor for all-sky infrared brightness temperatures.

## 4) SATELLITE ZENITH ANGLE PREDICTOR

Given that the satellite zenith angle is widely used in operational BC methods, an additional 464 experiment was performed using it as the BC predictor. After adjusting for the mean bias in the 465 original distribution, the conditional biases are close to zero across the entire distribution, with only a slight downward trend in the bias for zenith angles  $> 48^{\circ}$  (Fig. 6b). Application of the 467 1st to 3rd order BC terms (Figs. 6c-e) eliminated most of these conditional biases; however, the 468 impact of this predictor on the statistics of the entire distribution was negligible according to the histograms (Figs. 31-n). These results indicate that the bias in the observations is only very weakly 470 related to the satellite zenith angle; however, the small improvements made to the conditional 471 biases by the 2nd to 3rd order terms also show that there is a small nonlinear bias component that can be removed when using this predictor. 473

## b. Clear and Cloudy Sky Error Evaluation

Next, the relative impact of the linear and nonlinear BC terms on the clear and cloudy-sky observations is examined more closely using a subset of the  $6.2 \mu m$  brightness temperatures for which both the model background and a given observation were identified as being clear or cloudy. Each observation was classified as clear or cloudy based on the NWC SAF cloud mask dataset whereas each model grid point was deemed to be clear (cloudy) if the sum of all cloud hydrometeor mixing

ratios over the entire vertical profile was less (greater) than  $10^{-6}$  kg kg<sup>-1</sup>. The 2-D probability 480 distributions for the clear-sky matched observations are shown in Fig. 7, with the corresponding histograms shown in Fig. 8. The observed 6.2  $\mu$ m brightness temperatures were used as the BC 482 predictor. Inspection of Fig. 7a reveals that the original distribution contains both a systematic 483 bias and a large linear trend where mostly negative OMB departures for the colder brightness temperatures transition into mostly positive departures for the warmer brightness temperatures. The 485 linear trend indicates that the WV field in the model background is more uniform than observed 486 such that the model tends to be too wet (dry) in regions where the observations indicate less (more) WV. Overall, most of the bias is removed from the clear-sky observation departures using only the 488 constant and 1st order terms, with little or no impact due to the higher order terms (Figs. 7b-e). 489 This behavior is consistent with existing BC schemes that use constant and linear corrections to remove the bias from clear-sky observation departures. 491

For the cloud-matched observations shown in Figs. 9 and 10, the NWC SAF cloud top height 492 retrievals were used as the predictor. The OMB departure pattern and conditional biases for these 493 observations are very similar to that shown in Fig. 4 when both clear and cloudy-sky observations 494 were included in the regression. This includes the generally positive departures for mid-level 495 clouds and the transition to large negative departures for the upper-level clouds (Fig. 9a). Large departures remained in the distribution for all cloud top heights after the constant and linear BC 497 terms were applied to the observations (Fig. 9c). It is only when the 2nd and 3rd order terms are 498 used that the conditional biases become close to zero throughout the entire distribution (Figs. 9d, e). The histograms in Fig. 10 also reveal that the quadratic and cubic terms had a much larger impact on the overall statistics than occurred for the clear-sky matched observations. These results 501 provide further evidence that the nonlinear conditional biases evident in the all-sky scatterplots in Section 4.1 primarily result from biases associated with the cloudy observations. It also shows

that the NBC method is an effective method to remove both linear and nonlinear biases from allsky infrared brightness temperature departures if a suitable cloud-sensitive variable is used as the predictor.

#### or c. Multivariate Bias Correction Results

In addition to the univariate NBC experiments discussed in previous sections, multivariate ex-508 periments were performed to assess the impact of using more than one predictor to remove the ob-509 servation bias. For a 3rd order polynomial expansion using two variables, it is necessary to solve 510 for seven coefficients in Eqn. 11, whereas 22 coefficients are computed when three predictors are used. Because a direct approach is used to simultaneously estimate all of the BC coefficients, it 512 is not possible to determine the individual contribution of each predictor on the OMB departures; 513 however, the total contribution of all of the predictors within a given Taylor series order (e.g., 1st, 2nd, and 3rd) can still be inferred through comparison of the results obtained using different order 515 expansions. Though using more than one variable greatly increases the size of the A matrix, it is 516 still computationally efficient to solve for the inverse of  $A^TA$  given its small dimensions.

Numerous experiments using different predictor combinations and a 2nd or 3rd order polyno-518 mial expansion were performed; however, for brevity, this section only includes results from the 519 combination that had the largest impact on the OMB departure distributions. This particular configuration employed a 3rd order expansion with the satellite zenith angle, 100-700 hPa total water 521 content, and observed brightness temperatures for a given satellite band used as the BC predic-522 tors for that band. A separate multi-variate experiment (not shown) that employed the cloud top 523 height rather than the brightness temperature as the third predictor revealed that it had a smaller 524 impact, similar to what occurred with the univariate experiments shown earlier. There may be 525 some overlap between the brightness temperature and satellite zenith angle predictors; however, this should be minimal because the zenith angle predictor primarily accounts for potential biases in the radiative transfer model associated with the path length through the atmosphere, whereas the brightness temperature predictor is being used as a proxy for the cloud top height given its strong sensitivity to the cloud top. Unlike the previous sections that focused exclusively on the 6.2  $\mu$ m band, this section presents results from experiments that removed the bias from both of the SE-VIRI WV-sensitive bands (e.g., 6.2  $\mu$ m and 7.3  $\mu$ m). All observations, both clear and cloudy-sky, were used during these experiments.

### 1) SEVIRI 6.2 μM EXAMPLE

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Figure 11 shows the OMB departure distributions for the 6.2  $\mu$ m multivariate NBC experiment, 535 with the corresponding normalized histograms shown in Figs. 3o-q. Comparison to Fig. 2 shows 536 that the departure distributions for the multivariate case are similar to those from the univariate case employing only the observed brightness temperature as the BC predictor. This is not sur-538 prising given that the experiments employing the satellite zenith angle and total water content 539 predictors both had a much smaller impact on the distributions (Figs. 5, 6). Overall, the shape of the distribution is improved after the linear term is used; however, there are still large condi-541 tional biases at both ends of the distribution (Fig. 11c). The arch pattern in the conditional bias 542 was subsequently removed after the quadratic term was applied (Fig. 11d), with slightly smaller (larger) biases occurring at the warm (cold) end of the distribution after using the 3rd order cubic 544 term (Fig. 11e). Though the distributions are similar to those shown in Fig. 2, it is evident that the 545 width of the conditional distribution is less for all predictor values. This is encouraging because it shows that even though the impact of the satellite zenith angle and total water content predic-547 tors was relatively small when used individually, they still provided new information that further 548 reduced the OMB departures when used in combination with the observed brightness temperature

predictor. Inspection of the histograms (Figs. 3o-q) shows that the variance was greatly reduced compared to the univariate experiments; however, each of the distributions had a large positive skewness similar to that seen in Figs. 3c-e when the brightness temperature was used as the BC predictor. It is important to note however that quality control measures could potentially be used to reduce the skewness in the distribution after the BC terms are applied. This topic will be explored in a future study.

# 56 2) SEVIRI 7.3 μM EXAMPLE

In this section, we assess the ability of the multivariate NBC method to improve the observation 557 error characteristics of the 7.3  $\mu$ m band. As discussed in Section 2.1, observations from this band 558 are sensitive to WV and clouds in the middle and upper troposphere, with a weighting function that 559 peaks near 500 hPa in clear sky scenes. Overall, each of the OMB departure distributions (Fig. 12) have shapes that are similar to the corresponding 6.2  $\mu$ m distributions (Fig. 11); however, 561 their error range is larger because the weighting function for this band peaks at a lower level 562 in the troposphere, thereby leading to potentially larger departures due to mismatched clouds in the observations and model background. Though the linear BC term substantially improves the 564 distribution by making the departures less negative for colder brightness temperatures, non-zero 565 conditional biases remain across most of the distribution, with negative (positive) biases occurring for brightness temperatures colder (warmer) than 230 K (Fig. 12c). As occurred in the previous 567 experiments, the conditional biases are almost eliminated after the 2nd order BC term is used, 568 with minimal changes occurring due to the 3rd order term (Figs. 12d, e). The negative skewness present in the original histogram (Fig. 13a) switches to a large positive skewness after the linear 570 BC term is used (Fig. 13c). Inspection of the OMB departure distributions shows that the positive 571 skewness developed in response to the large upward shift in the conditional distributions for the

colder brightness temperatures (Fig. 12a) that exposed the conditional positive skewness in the original distribution for warmer brightness temperatures that was being masked in the overall 574 histogram by the large negative OMB departures. Another notable feature of the histograms is 575 that their peaks are higher and narrower than the 6.2  $\mu$ m histograms (Figs. 30-q). This strongly non-Gaussian behavior was already present in the original histogram and is likely due to the large percentage of clear-sky observations containing small departures combined with fatter tails due 578 to cloud displacement errors. Even so, these results show that the NBC method improved the distribution such that the variance was much lower and the conditional biases were reduced to near zero across most of the distribution. Also, as was the case with the 6.2  $\mu$ m band, the linear 581 BC term had the largest impact on the overall statistics; however, the variance was also reduced when using the higher order nonlinear BC terms. 583

#### 5. Discussion and Conclusions

In this study, output from a high-resolution, regional-scale ensemble DA system was used to 585 explore the ability of an innovative method to remove the bias associated with all-sky satellite 586 infrared brightness temperatures using a Taylor series polynomial expansion of the OMB depar-587 tures. This so-called NBC method uses OMB statistics accumulated over some period of time to 588 remove linear and nonlinear conditional biases in a distribution through use of higher order Taylor series terms and a set of BC predictors. Nonlinear conditional biases can be identified using 2nd 590 (quadratic) and 3rd (cubic) order terms (and even higher order terms if desired), whereas the con-591 stant and linear bias components can be diagnosed using the 0th and 1st order terms, respectively. The ability of the NBC method to effectively remove the bias associated with all-sky SEVIRI 593 infrared brightness temperatures was assessed using output from high-resolution ensemble DA 594 experiments performed using the KENDA system. OMB departure statistics for the 6.2 and 7.3 μm bands sensitive to clouds and WV in the upper and middle troposphere, respectively, were accumulated at hourly intervals during a 108-h period from 16-21 May 2014 using output from the COSMO-DE domain that covers Germany and surrounding areas with 2.8-km horizontal grid spacing. Conventional observations were actively assimilated, whereas the SEVIRI observations were passively monitored and therefore did not affect the analyses during the hourly assimilation cycles. Model-equivalent brightness temperatures were computed for each observation and ensemble member using the RTTOV radiative transfer model. The study period contained both clear-sky areas and a wide range of cloud types that together promoted a realistic assessment of the NBC method during the warm season.

Univariate and multi-variate NBC experiments were performed using the satellite zenith angle 605 and other predictors sensitive to clouds and WV, with their impact on the conditional bias and other aspects of the OMB departure distributions assessed using normalized histograms and probability 607 distributions plotted as a function of the predictor. Overall, the results revealed that there are often 608 strongly nonlinear conditional bias patterns in the OMB probability distributions that cannot be removed using only constant and linear BC terms. Though the overall bias of each distribution is 610 equal to zero regardless of the order of the Taylor series expansion, there are often large conditional 611 biases that vary as a function of the BC predictor. Because each SEVIRI band had a relatively small systematic bias, the constant BC term only had a small impact on the distributions. The 613 linear 1st order term generally had the largest impact on the statistics of the entire distribution 614 as measured by reductions in the variance; however, conditional biases often remained across much of the distribution. These conditional biases were typically reduced to near zero across 616 the entire distribution only after the nonlinear 2nd and 3rd order terms were applied to the OMB 617 departures. Indeed, the conditional bias patterns often exhibited an arch shape for which the 2nd order quadratic term is ideally suited to remove. The tendency for the nonlinear terms to have a small impact on the variance of the entire distribution while simultaneously having a large
positive impact on the conditional biases also illustrates that detailed analysis methods such as 2-D
probability distributions provide valuable insight into the behavior of the BC method that is not
possible using traditional 1-D error histograms.

Inspection of the univariate NBC results showed that the variance of the BC distributions was 624 smallest when the brightness temperature observations were used as the BC predictor. The vari-625 ance was also substantially reduced when the NWC SAF cloud top height retrievals were used as 626 the predictor. Both of these predictors were able to diagnose and remove nonlinear biases associated with the cloudy observations. For example, large positive conditional biases for mid-level 628 clouds transitioned into large negative conditional biases for upper-level clouds. Though not examined during this study, the different signs of the conditional biases for these clouds could be 630 related to the ability of the COSMO model and RTTOV to properly simulate ice and mixed-phase 631 cloud properties. The experiments using the satellite zenith angle or vertically-integrated water 632 content showed that these BC predictors had a much smaller impact on the variance of the overall distribution. This behavior indicates that variables sensitive to the cloud top height are more 634 effective BC predictors for all-sky infrared brightness temperatures, especially when higher order 635 Taylor series terms are included. Even so, the multivariate experiments showed that though the 636 zenith angle and total water content predictors only had a relatively small impact on the departure 637 histograms when used individually, they still provided new information that greatly reduced the 638 variance of the distribution when used in combination with the observed brightness temperature predictor. 640

Additional univariate NBC experiments were performed to examine the influence of linear and nonlinear components on the OMB departure distributions for clear- and cloudy-sky observations using a subset of the 6.2  $\mu$ m brightness temperatures for which both a given observation and the

corresponding model grid point were identified as being clear or cloudy. Overall, comparisons of the statistics for the clear-sky and cloudy-sky matched observations revealed that nonlinear error 645 sources are much more important for cloudy sky observations as signified by the much larger 646 impact of the 2nd and 3rd order Taylor series terms on the variance and the conditional biases in the distributions. For the clear-sky observations, the conditional biases could be effectively removed using only the 0th and 1st order terms, which is consistent with existing operational BC 649 methods that typically remove the bias from clear-sky satellite observations using a set of constant 650 and linear BC coefficients. These results show that the nonlinear conditional bias patterns evident in the all-sky OMB departure distributions primarily resulted from nonlinear biases in the cloudy-652 sky infrared brightness temperatures. They also show that the NBC method can effectively remove both linear and nonlinear conditional biases from all-sky infrared brightness temperatures provided that a suitable cloud-sensitive variable is used as one of the predictors. 655

Future work includes running cycled DA experiments using the KENDA system to assess the 656 impact of the NBC method on the forecast accuracy when assimilating clear- and cloudy-sky infrared brightness temperatures. Additional experiments will be necessary to explore the ability of 658 the method to remove biases from the OMB departures when the simulated brightness tempera-659 tures and cloud top heights are used as the BC predictors rather than their observed counterparts. 660 Preliminary results indicate that predictors derived from the NWP model cloud field rather than the 661 observations have a smaller impact on the overall statistics as measured by reductions in variance; 662 however, they were still able to effectively remove the conditional biases across most of the distribution when higher order Taylor series terms were used. These results also indicate that it may 664 be necessary to use up to a 4th order polynomial to remove the bias if the NWP-derived quantities 665 are used rather than their observed counterparts. A more detailed assessment of this sensitivity is currently underway. Additional experiments will also be necessary to explore the ability of the

NBC method to remove biases from infrared bands that are sensitive to the land surface or other atmospheric constituents such as ozone, as well as for all-sky microwave and visible radiances.

Though the NBC method used in this paper was implemented as a static, off-line method, it 670 could also be incorporated into online methods such as VarBC through inclusion of additional nonlinear predictors. For example, the VarBC system at the Met Office uses Legendre polynomial 672 predictors to remove residual scan biases and Fourier predictors to correct complex orbital biases 673 in some satellite sensors (Cameron and Bell, 2016). Higher order predictors, such as the quadratic form of the temperature lapse rate and 4th order polynomial of the satellite angle bias, are also widely used in operational VarBC systems. Zhu et al. (2015) recently showed that inclusion of 676 a quadratic aircraft ascent/descent term reduced the bias when assimilating aircraft temperature observations. Results from the current study could be used to help inform the development of 678 operational DA systems as they continue to expand into all-sky satellite DA. Finally, many of the 679 all-sky OMB departure distributions exhibited narrow peaks and fat tails that could potentially be 680 better represented using a Huber norm (Huber 1972) representation, which has been shown to lead to improved quality control and more observations being assimilated (Tavolato and Isaken 2015). 682 Further research is necessary to determine if using a Huber norm in combination with the NBC 683 method can improve existing quality control methods by identifying erroneous observations after the nonlinear conditional biases have been removed from the distribution. This approach could 685 potentially preserve more cloud-affected observations where nonlinear biases are more prevalent, 686 thereby leading to additional observations being assimilated in sensitive areas of the domain.

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## **7. Figure Captions**

- Fig. 1. Observed SEVIRI 6.2  $\mu$ m brightness temperatures (K) valid at 18 UTC on (a) 16 May, (b) 17 May, (c) 18 May, (d) 19 May, and (e) 20 May 2014.
- Fig. 2. Probability distributions of 6.2  $\mu$ m observation-minus-background departures plotted as a function of the observed 6.2  $\mu$ m brightness temperatures (K) for the (a) original data, and the (b) constant, (c) 1st order, (d) 2nd order, and (e) 3rd order bias corrected observations when the observed 6.2  $\mu$ m brightness temperature is used as the predictor. The horizontal black line segments represent the conditional bias in each column. Data were accumulated at hourly intervals during a 108-h period from 13 UTC on 16 May 2014 to 00 UTC on 20 May 2014.
- Fig. 3. Probability density function of normalized 6.2  $\mu$ m observation-minus-background departures for the (a) original and (b) constant bias correction distributions. The corresponding 1st, 2nd, and 3rd order bias correction error distributions when the (c-e) observed 6.2  $\mu$ m brightness

- temperatures, (f-h), NWC SAF cloud top heights, (i-k) model-simulated total integrated water content (IWC) in the 100-700 hPa layer, (l-n) satellite zenith angle, or (o-q) observed 6.2  $\mu$ m
- brightness temperatures, satellite zenith angle, and IWC are used as the predictors are also shown.
- Data were accumulated at hourly intervals during a 108-h period from 13 UTC on 16 May 2014 to 00 UTC on 20 May 2014.
- Fig. 4. Same as Fig. 2 except for showing probability distributions plotted as a function of the NWC SAF cloud top height retrieval (km) when this quantity is also used as the BC predictor.
- Fig. 5. Same as Fig. 2 except for showing probability distributions plotted as a function of the vertically-integrated total water content (mm) over the 100-700 hPa layer when this quantity is also used as the BC predictor.
- Fig. 6. Same as Fig. 2 except for showing probability distributions plotted as a function of the satellite zenith angle (o) when this quantity is also used as the BC predictor.
- Fig. 7. Same as Fig. 2 except for showing probability distributions for clear-sky matched observations plotted as a function of the observed brightness temperature (K) when this quantity is also used as the BC predictor.
- Fig. 8. Probability density function of normalized clear-sky matched 6.2  $\mu$ m observation-minus-background departures for the (a) original data, and the (b) constant, (c) 1st order, (d) 2nd order, and (e) 3rd order bias corrected observations when the observed 6.2  $\mu$ m brightness temperature is used as the predictor. Data were accumulated at hourly intervals during a 108-h period from 13 UTC on 16 May 2014 to 00 UTC on 20 May 2014.
- Fig. 9. Same as Fig. 2 except for showing probability distributions for cloudy-sky matched observations plotted as a function of the NWC SAF cloud top height retrieval (km) when this quantity is also used as the BC predictor.

- Fig. 10. Probability density function of normalized cloudy-sky matched 6.2  $\mu$ m observationminus-background departures for the (a) original data, and the (b) constant, (c) 1st order, (d) 2nd
  order, and (e) 3rd order bias corrected observations when the NWC SAF cloud top height retrieval
  is used as the predictor. Data were accumulated at hourly intervals during a 108-h period from 13
  UTC on 16 May 2014 to 00 UTC on 20 May 2014.
- Fig. 11. Same as Fig. 2 except for showing probability distributions plotted as a function of the observed 6.2  $\mu$ m brightness temperatures when the observed 6.2  $\mu$ m brightness temperature, satellite zenith angle, and vertically-integrated total water content from 100-700 hPa are used as the BC predictors.
- Fig. 12. Probability distributions of 7.3  $\mu$ m observation-minus-background departures plotted as a function of the observed 7.3  $\mu$ m brightness temperatures (K) for the (a) original data, and the (b) constant, (c) 1st order, (d) 2nd order, and (e) 3rd order bias corrected observations when the observed 7.3  $\mu$ m brightness temperature, satellite zenith angle, and model-integrated total water content from 100-700 hPa are used as the predictors. Data were accumulated at hourly intervals during a 108-h period from 13 UTC on 16 May 2014 to 00 UTC on 20 May 2014.
- Fig. 13. Probability density function of normalized 7.3  $\mu$ m observation-minus-background departures for the (a) original data, and the (b) constant, (c) 1st order, (d) 2nd order, and (e) 3rd order bias corrected observations when the observed 7.3  $\mu$ m brightness temperatures are used as the predictor. Data were accumulated at hourly intervals during a 108-h period from 13 UTC on 16 May 2014 to 00 UTC on 20 May 2014.

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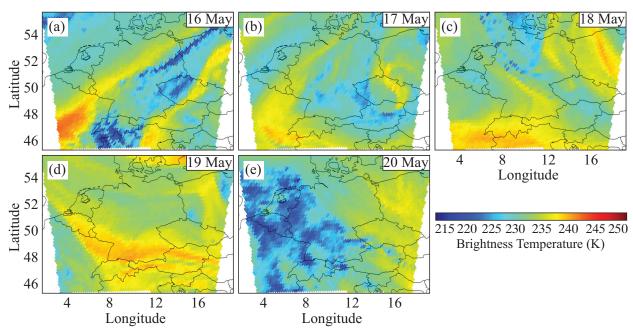


Fig. 1. Observed SEVIRI 6.2 µm brightness temperatures (K) valid at 18 UTC on (a) 16 May, (b) 17 May, (c) 18 May, (d) 19 May, and (e) 20 May 2014.

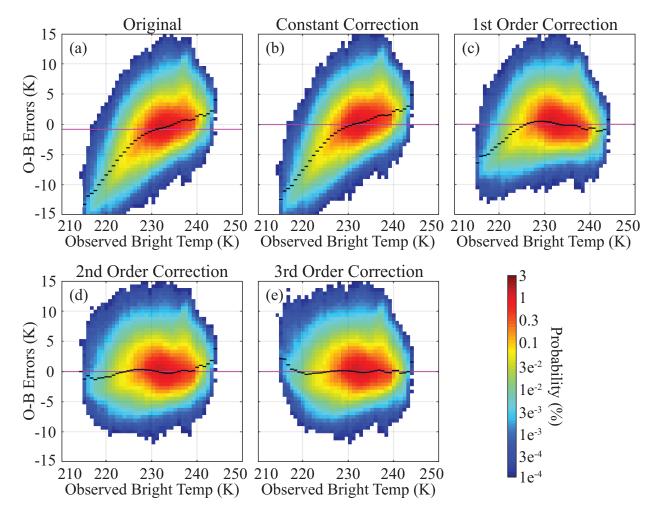


Fig. 2. Probability distributions of 6.2  $\mu$ m observation-minus-background departures plotted as a function of the observed 6.2  $\mu$ m brightness temperatures (K) for the (a) original data, and the (b) constant, (c) 1st order, (d) 2nd order, and (e) 3rd order bias corrected observations when the observed 6.2  $\mu$ m brightness temperature is used as the predictor. The horizontal black line segments represent the conditional bias in each column. Data were accumulated at hourly intervals during a 108-h period from 13 UTC on 16 May 2014 to 00 UTC on 20 May 2014.

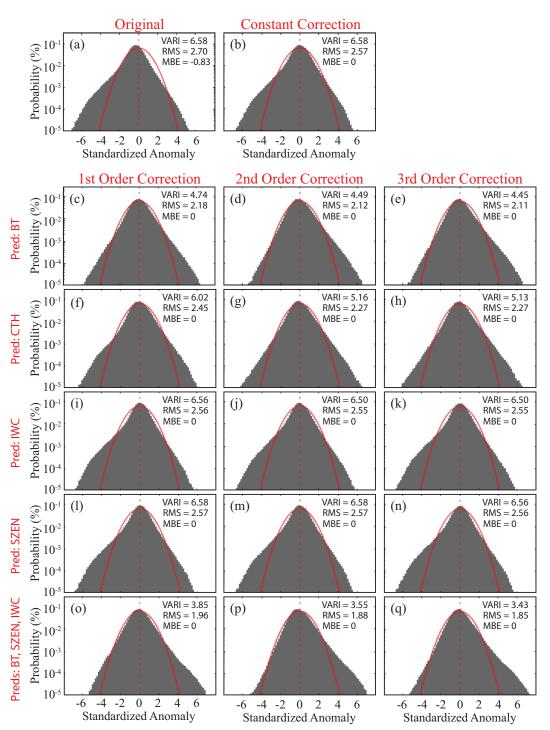


Fig. 3. Probability density function of normalized 6.2  $\mu$ m observation-minus-background departures for the (a) original and (b) constant bias correction distributions. The corresponding 1st, 2nd, and 3rd order bias correction error distributions when the (c-e) observed 6.2  $\mu$ m brightness temperatures, (f-h), NWC SAF cloud top heights, (i-k) model-simulated total integrated water content (IWC) in the 100-700 hPa layer, (l-n) satellite zenith angle, or (o-q) observed 6.2  $\mu$ m brightness temperatures, satellite zenith angle, and IWC are used as the predictors are also shown. Data were accumulated at hourly intervals during a 108-h period from 13 UTC on 16 May 2014 to 00 UTC on 20 May 2014.

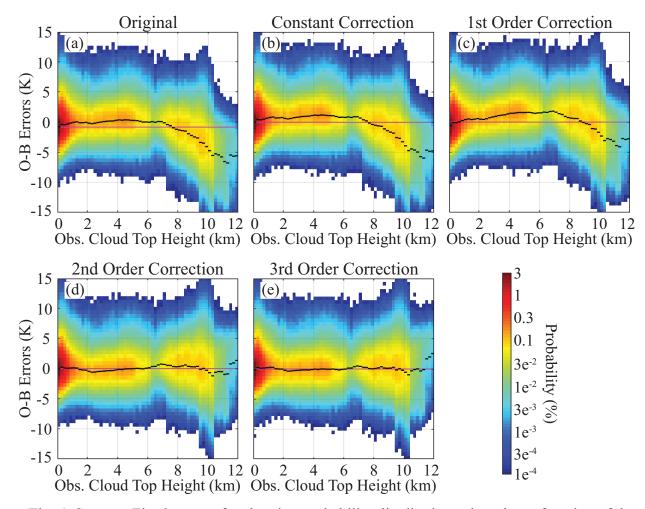


Fig. 4. Same as Fig. 2 except for showing probability distributions plotted as a function of the NWC SAF cloud top height retrieval (km) when this quantity is also used as the BC predictor.

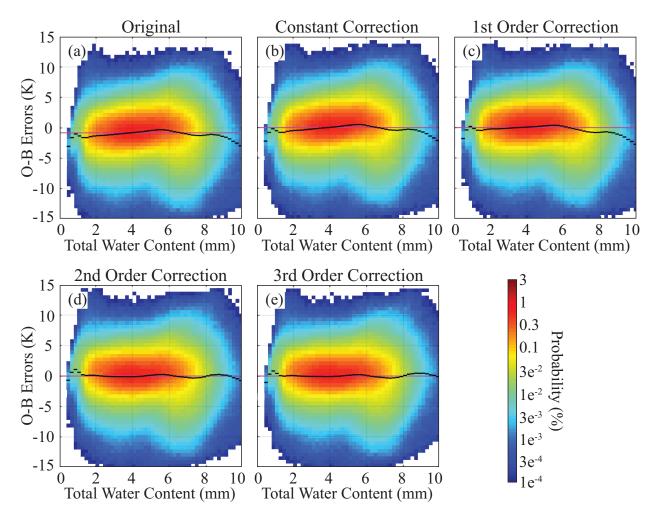


Fig. 5. Same as Fig. 2 except for showing probability distributions plotted as a function of the vertically-integrated total water content (mm) over the 100-700 hPa layer when this quantity is also used as the BC predictor.

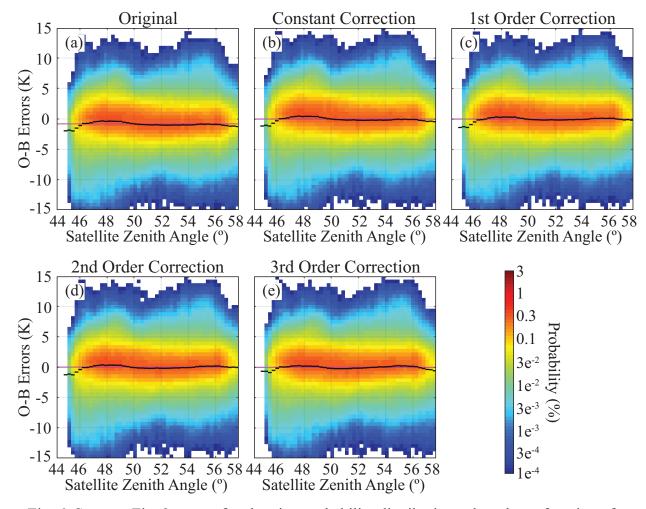


Fig. 6. Same as Fig. 2 except for showing probability distributions plotted as a function of the satellite zenith angle (°) when this quantity is also used as the BC predictor.

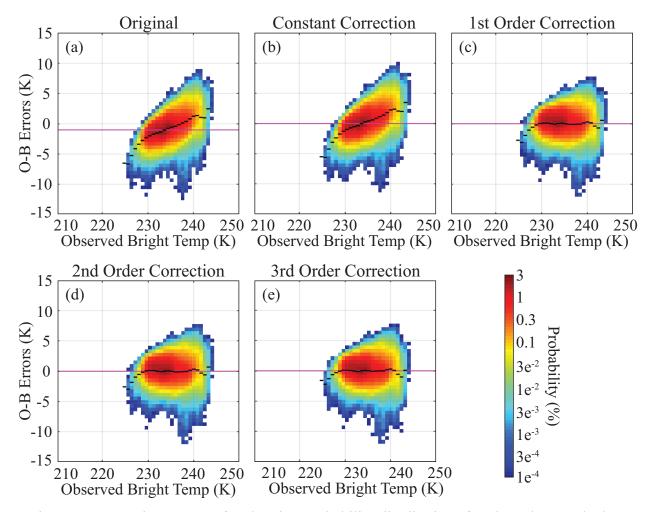


Fig. 7. Same as Fig. 2 except for showing probability distributions for clear-sky matched observations plotted as a function of the observed brightness temperature (K) when this quantity is also used as the BC predictor.

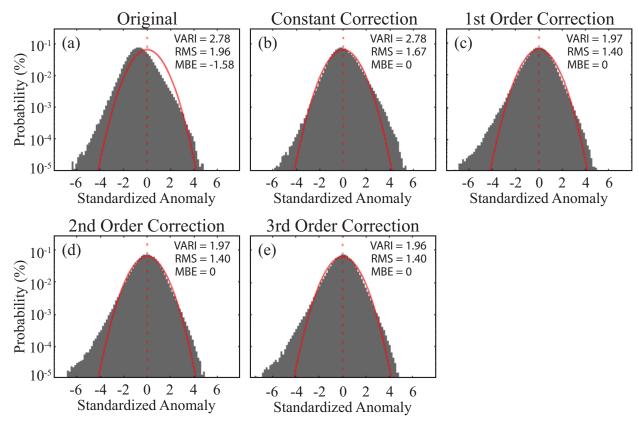


Fig. 8. Probability density function of normalized clear-sky matched 6.2  $\mu$ m observation-minus-background departures for the (a) original data, and the (b) constant, (c) 1st order, (d) 2nd order, and (e) 3rd order bias corrected observations when the observed 6.2  $\mu$ m brightness temperature is used as the predictor. Data were accumulated at hourly intervals during a 108-h period from 13 UTC on 16 May 2014 to 00 UTC on 20 May 2014.

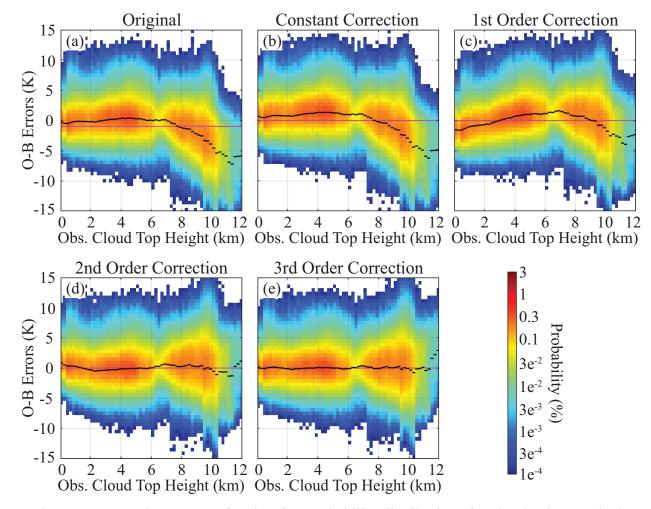


Fig. 9. Same as Fig. 2 except for showing probability distributions for cloudy-sky matched observations plotted as a function of the NWC SAF cloud top height retrieval (km) when this quantity is also used as the BC predictor.

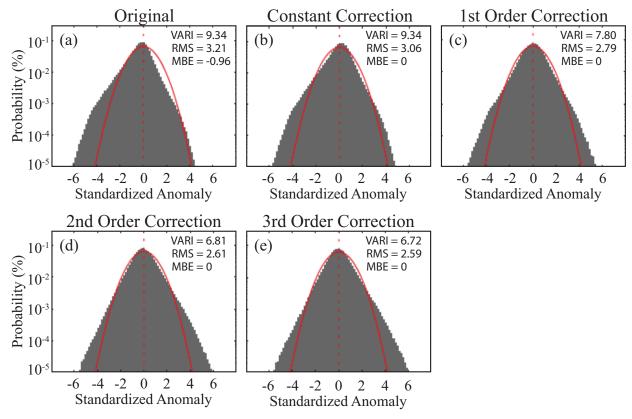


Fig. 10. Probability density function of normalized cloudy-sky matched 6.2 μm observation-minus-background departures for the (a) original data, and the (b) constant, (c) 1st order, (d) 2nd order, and (e) 3rd order bias corrected observations when the NWC SAF cloud top height retrieval is used as the predictor. Data were accumulated at hourly intervals during a 108-h period from 13 UTC on 16 May 2014 to 00 UTC on 20 May 2014.

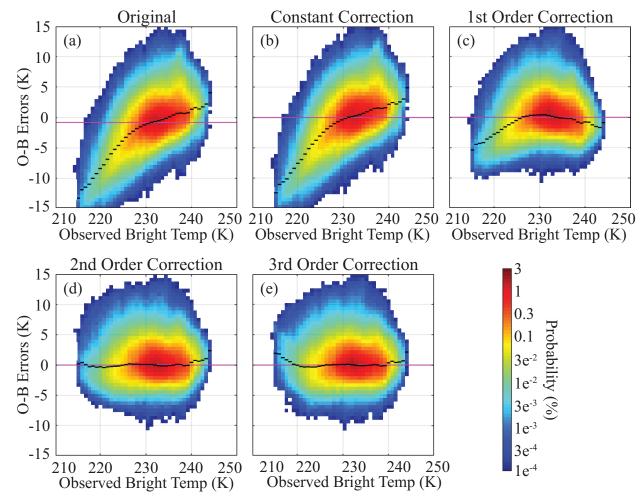


Fig. 11. Same as Fig. 2 except for showing probability distributions plotted as a function of the observed  $6.2~\mu m$  brightness temperature, when the observed  $6.2~\mu m$  brightness temperature, satellite zenith angle, and vertically-integrated total water content from 100-700~hPa are used as the BC predictors.

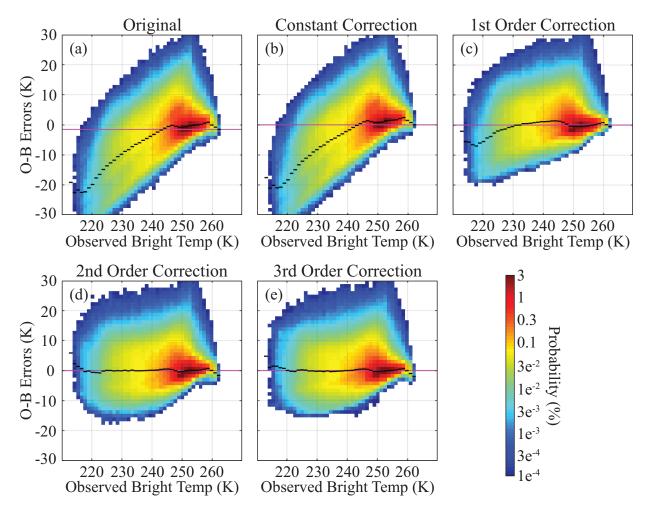


Fig. 12. Probability distributions of 7.3 µm observation-minus-background departures plotted as a function of the observed 7.3 µm brightness temperatures (K) for the (a) original data, and the (b) constant, (c) 1st order, (d) 2nd order, and (e) 3rd order bias corrected observations when the observed 7.3 µm brightness temperature, satellite zenith angle, and model-integrated total water content from 100-700 hPa are used as the predictors. Data were accumulated at hourly intervals during a 108-h period from 13 UTC on 16 May 2014 to 00 UTC on 20 May 2014.

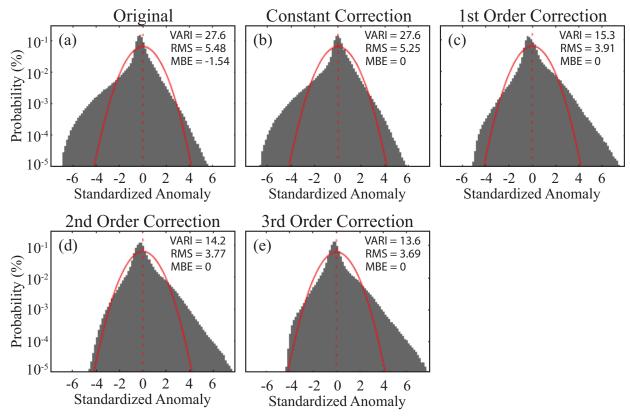


Fig. 13. Probability density function of normalized 7.3 µm observation-minus-background departures for the (a) original data, and the (b) constant, (c) 1st order, (d) 2nd order, and (e) 3rd order bias corrected observations when the observed 7.3 µm brightness temperatures are used as the predictor. Data were accumulated at hourly intervals during a 108-h period from 13 UTC on 16 May 2014 to 00 UTC on 20 May 2014.