



THE UNIVERSITY *of* EDINBURGH

Edinburgh Research Explorer

Cow genotyping strategies for genomic selection in a small dairy cattle population

Citation for published version:

Jenko, J, Wiggans, GR, Cooper, TA, Eaglen, SAE, de L Luff, WG, Bichard, M, Pong-Wong, R & Woolliams, JA 2017, 'Cow genotyping strategies for genomic selection in a small dairy cattle population' Journal of Dairy Science, vol. 100, no. 1, pp. 439-452. DOI: 10.3168/jds.2016-11479

Digital Object Identifier (DOI):

[10.3168/jds.2016-11479](https://doi.org/10.3168/jds.2016-11479)

Link:

[Link to publication record in Edinburgh Research Explorer](#)

Document Version:

Peer reviewed version

Published In:

Journal of Dairy Science

General rights

Copyright for the publications made accessible via the Edinburgh Research Explorer is retained by the author(s) and / or other copyright owners and it is a condition of accessing these publications that users recognise and abide by the legal requirements associated with these rights.

Take down policy

The University of Edinburgh has made every reasonable effort to ensure that Edinburgh Research Explorer content complies with UK legislation. If you believe that the public display of this file breaches copyright please contact openaccess@ed.ac.uk providing details, and we will remove access to the work immediately and investigate your claim.



INTERPRETIVE SUMMARY

1
2
3
4
5
6
7
8
9
10

Cow genotyping strategies for genomic selection in small dairy cattle population. *By Jenko et al., page 000.* The benefit of using cow genotypes for building training sets in small dairy populations was examined using the Guernsey breed. Adding genotypes from a single cohort of cows improved the accuracy of prediction substantially over a training set of 200 bulls alone. For this population the genetic correlation for bulls and cows in the training set was <1 . Strategies to improve the cost effectiveness of genotyping can also be beneficial. Genotyping all cows always gave the greatest accuracy, however, genotyping only half, divergently selected, recovered substantial information and was better than genotyping the same number when randomly- or directionally-selected.

11 **COW GENOTYPING STRATEGIES**

12 **Cow genotyping strategies for genomic selection in small dairy cattle population**

13 **J. Jenko^{*1}, G. R. Wiggans[†], T. A. Cooper[†], S. A. E. Eaglen^{*}, W. G. de L. Luff[‡], M.**
14 **Bichard[§], R. Pong-Wong^{*} and J. A. Woolliams^{*}**

15 ^{*}The Roslin Institute and Royal (Dick) School of Veterinary Studies, The University of
16 Edinburgh, Easter Bush, Midlothian, EH25 9RG, Scotland, UK

17 [†]Animal Genomics and Improvement Laboratory, BARC, USDA-ARS, Beltsville,
18 MD 20705, USA

19 [‡]World Guernsey Cattle Federation, The Hollyhocks, 10 Clos des Goddards, Rue des
20 Goddards, Castel GY5 7JD, Guernsey

21 [§]English Guernsey Cattle Society, 12 Southgate Street, Launceston, Cornwall PL15 9DP, UK

22
23 ¹Corresponding author:

24 Janez Jenko

25 ^{*}The Roslin Institute and Royal (Dick) School of Veterinary Studies, The University
26 of Edinburgh, Easter Bush, Midlothian, Scotland, UK

27 +441316519222

28 janez.jenko@roslin.ed.ac.uk

29

30 **ABSTRACT**

31 This study compares how different cow genotyping strategies increase the accuracy of
32 genomic estimated breeding values (EBV) in dairy cattle breeds with low numbers. In these
33 breeds there are few sires with progeny records and genotyping cows can improve the
34 accuracy of genomic EBV. The Guernsey breed is a small dairy cattle breed with
35 approximately 14,000 recorded individuals worldwide. Predictions of phenotypes of milk
36 yield, fat yield, protein yield, and calving interval were made for Guernsey cows from England
37 and Guernsey Island using genomic EBV, with training sets including 197 de-regressed proofs
38 of genotyped bulls, with cows selected from among 1,440 genotyped cows using different
39 genotyping strategies. Accuracies of predictions were tested using 10-fold cross-validation
40 among the cows. Genomic EBV were predicted using four different methods: (i) pedigree
41 BLUP, (ii) genomic BLUP using only bulls, (iii) univariate genomic BLUP using bulls and
42 cows, and (iv) bivariate genomic BLUP. Genotyping cows with phenotypes and using their
43 data for the prediction of single nucleotide polymorphism (SNP) effects increased the
44 correlation between genomic EBV and phenotypes compared to using only bulls by 0.163
45 ± 0.022 for milk yield, 0.111 ± 0.021 for fat yield, and 0.113 ± 0.018 for protein yield, a drop
46 of 0.014 ± 0.010 for calving interval from a low base was the only exception. Genetic
47 correlation between phenotypes from bulls and cows were approximately 0.6 for all yield
48 traits and significantly different from 1. There was only very small change in correlation
49 between genomic EBV and phenotypes when using the bivariate model. It was always better
50 to genotype all the cows but when only half of the cows were genotyped, a divergent
51 selection strategy was better compared to the random or directional selection approach.
52 Divergent selection of 30% of the cows remained superior for the yield traits in 8 of 10 folds.

53 **Keywords:** genomic selection, genotyping cows, cow genotyping strategies, Guernsey

INTRODUCTION

55 Response to selection can be increased by changing the ratio of the accuracy of EBV to the
56 generation interval, and an intermediate age exists where this ratio is maximised so defining the optimum
57 selection age. For conventional evaluations based solely on pedigree and phenotypes the accuracy of
58 parent average EBV are too low, precluding the intense selection of young bulls at birth. For this purpose
59 bulls for widespread use are often selected only after the phenotypes of their first crop daughters are
60 known, at around 5 years of age. A benefit of genomic selection is its potential to increase the accuracy of
61 EBV early in life. To achieve this, a sufficient number of individuals with phenotypes or progeny records
62 needs to be genotyped (Meuwissen et al., 2001). Based on this training set of individuals SNP effects
63 are then estimated. These estimates can then be used for the calculation of genomic EBV of genotyped
64 individuals without phenotypic observations on themselves, or lactating daughters in the case of
65 young bulls. When the accuracy of a genomic EBV is high enough, the optimum selection age for the
66 parents of a future generation can be lowered, reducing the generation interval. This might result in a
67 doubling of the rate of genetic gain in dairy schemes compared with conventional breeding values
68 (Schaeffer, 2006).

69 The accuracy of a genomic EBV will be higher when the number of genotyped
70 individuals with own performance or progeny records is large (Daetwyler et al., 2008, 2010;
71 Goddard, 2009). In large populations, many sires have achieved very accurate progeny tests
72 from large daughter groups, and have been genotyped. This has enabled the successful
73 implementation of genomic selection in large populations of dairy cattle (VanRaden et al., 2009).
74 However, for small cattle breeds genomic selection is still a challenge as their limited resources restricts
75 the prediction accuracy, as either the number of sires with a large number of daughters is too small, or the
76 progeny tests are weak. There are 3 possible solutions to overcome this problem. One is to include
77 genotypes from the same breed but from the other country (Cooper et al., 2016), another is to

78 combine the breed-specific reference population with other breeds (Hayes et al., 2009; Olson et al.,
79 2012; Hozé et al., 2014) and the last is to include cows in the reference population (Pryce et al.,
80 2012; Calus et al., 2013; Cooper et al., 2015).

81 The success of combining the reference population with another breed depends on the genetic
82 distance between them, numbers of genotyped individuals, and SNP chip density. Genomic evaluation
83 requires that the different populations are at least distantly related (Habier et al., 2010). To increase
84 genetic gain the reference population and selection candidates should share recent ancestors (Clark et
85 al., 2012; Pszczola et al., 2012). This relationship is higher when genotypes from cows of the same
86 breed are available compared to individuals from different breeds, but their accuracy is often smaller
87 compared to de-regressed proofs of bulls from large breeds, and are typically expected to add less
88 information per genotyped individual, although this difference depends on the heritability. De Roos
89 (2011) estimated that the addition of 7 cows for a trait with a heritability of 0.1 gives the same gain
90 as adding 1 bull with 100 tested progeny, while for the trait with a heritability of 0.5 this ratio reduced to 2
91 cows per bull. Simulations performed by Jiménez-Montero et al. (2012) showed that not only the
92 number of cow genotypes but also the genotyping design can increase the accuracy of genomic EBV.
93 The accuracy of divergent selection on yield or breeding value deviations was higher than when selecting
94 at random or based on the extreme values in the upper tail.

95 The goal of this study was to estimate the benefit of using cow genotypes for genomic selection
96 in a small dairy cattle population. An additional goal was to determine the effect of different cow
97 genotyping strategies on the accuracy of selection. The Guernsey breed represented by bull and cow
98 genotypes from England and Guernsey Island is a suitable population for this study. Guernsey is one of
99 the smaller dairy breeds with approximately 14,000 recorded individuals worldwide and, of these, 2,000
100 are on Guernsey Island.

101

MATERIALS AND METHODS

102 *Study Samples*

103 A total of 1,637 genotypes from Guernsey cattle were available: 197 from bulls and
104 1,440 from cows. Of the bull samples, 29 were genotyped with the Illumina BovineHD
105 Genotyping BeadChip (777K; Illumina Inc., San Diego, CA) and 168 with the GeneSeek
106 Genomic Profiler HD BeadChip Version 1 (75K; Neogen Corp., Lexington, KY). All of the
107 cow samples were genotyped with the GeneSeek Genomic Profiler for Dairy Cattle Version 3
108 (25K; Neogen Corp., Lexington, KY).

109 Genotyped bulls were part of the artificial insemination program and were born
110 between 1957 and 2013. Except for the most recent ones, they had daughters with records
111 available and were included in genetic evaluations. One bull had both parents genotyped and
112 75 bulls had one parent genotyped. Cows with genotypes were a cohort of Guernsey cows
113 present on the Island in early 2014. They were born between 1997 and 2013 and were
114 included in the milk recording scheme. There were 133 cows with both parents genotyped
115 and 705 cows with one parent genotyped.

116 *Genotype Quality Check*

117 Before the genotypes were checked for quality, three individuals were discovered to
118 have been repeated, and the sample with the higher call rate was kept. For all three chips,
119 SNP were checked for the position and name: 199 SNP had the same name but different
120 positions, or had different names but with the same position as another and these were
121 excluded. The SNP on the sex chromosomes were excluded from all the chips. Individuals
122 were excluded when overall call rate was <0.85 or heterozygosity was outside the interval of
123 mean ± 3 SD calculated for the relevant SNP chip. Altogether, 107 samples from the 25K

124 chip, 1 from the 75K chip and 1 from the 777K chip failed these criteria as shown in
125 Appendix A. Then, SNP loci were excluded if call rate < 0.85 : 546 were excluded for the 25K
126 chip, 1,327 for the 75K chip, and 12,712 for the 777K chip. For imputation, individuals
127 genotyped with 777K were merged with 75K using only 72,679 SNP from the 75K chip.
128 Finally, SNP with Hardy-Weinberg equilibrium test $P < 10^{-6}$ or minor allele frequency
129 (**MAF**) < 0.05 were removed, resulting in the availability of 64,657 and 17,716 SNP on the
130 75K and 25K chip respectively.

131 The pedigree relationship was checked separately for duos and trios using PLINK
132 (Purcell et al., 2007) by comparing the known genotypes of parents and offspring. Parent-
133 offspring duos with more than 1% of opposing homozygosity were identified, and 1 case was
134 discovered and the relationship was set to unrelated. For trios the percentage of opposing
135 homozygous and heterozygous genotypes in the offspring for SNP where both of the parents
136 were homozygous for the same allele was calculated, and if more than 1% were inconsistent,
137 both parent-offspring relationships were set as missing, which occurred in 2 cases. For all the
138 other instances, genotype inconsistencies between parents and progeny were corrected using
139 conflict.f90, which corrects for Mendelian errors and fills missing SNPs using parental
140 genotypes where possible (VanRaden et al., 2015).

141 ***Genotype Imputation***

142 A 2-step imputation process (Figure 1) was conducted using the pedigree and FImpute
143 (Sargolzaei et al., 2014). In the first step, SNP existing only on the 25K chip (5,733 SNP)
144 were excluded and individuals with genotypes on 25K chip were imputed to the SNP existing
145 on the 75K chip (64,657 SNP). After the first step, MAF was reviewed and SNP with MAF $<$
146 0.05 were excluded. Then SNP excluded from the first step were re-introduced giving a total
147 of 69,034 SNP available for the second imputation step, where loci only on the 25K chip

148 were imputed for individuals genotyped only on the 75K chip. After the second step, MAF
149 for all SNP was >0.05.

150 » Figure 1 near here «

151 Imputation accuracy and efficiency were tested on 1,333 cow genotypes with 11,983
152 SNP existing on both 75K and 25K chip using 10-fold cross validation. For each fold 10% of
153 SNP selected at random were set as missing and imputed so that each SNP was imputed
154 exactly once. All of the 1,333 cow genotypes were used in each of the 10 folds. The
155 imputation efficiency and accuracy were calculated as the correlation, genotype concordance,
156 and allele concordance between the imputed and the true genotypes.

157 *Traits for Analysis*

158 The benefits of genotyping cows and different genotyping strategies were analysed
159 for four traits: milk yield (kg), fat yield (kg), protein yield (kg), and calving interval (days).
160 There were 2 types of data obtained: official Predicted Transmitting Abilities (**PTA**) for bulls
161 and cows and daily milk records for cows. Profitable Lifetime Index (**PLI**) and Guernsey
162 Merit Index (**GMI**) were also obtained for bulls and cows for the purpose of creating
163 different selection subsets. The main difference between PLI and GMI is the emphasis put on
164 production and functional traits. While PLI has about 32% weights on production traits and
165 68% on fitness traits, GMI has 60% of weights on production traits and 30% on functional
166 traits. The PTA, PLI, and GMI were obtained from the Interbull evaluation with multiple,
167 across-country data carried out in April 2015. All the data were obtained from EGENES
168 which provides genetic evaluations for UK dairy cattle on behalf of the Agricultural and
169 Horticultural Development Board.

170 Daily milk records from the first five lactations were obtained for milk, fat, and
171 protein yield. They were transformed into standard 305 days lactation records using the test
172 interval method (Sargent et al., 1968). As dry-off days were not available they were
173 approximated: lactation length was set to 305 days when the last milk recording was done 31
174 days or less before the 305 days of lactation; in all the other cases 31 days were added to the
175 last milk recording to get the dry-off day. Lactations shorter than 201 days were discarded.
176 Lactation yield records were corrected for the fixed effects of calving year-season, lactation
177 number, and herd. Calving interval records were available for the first lactation only. They
178 were corrected for the fixed effects of calving year-season and herd. Finally, adjusted
179 phenotypes from cows combined with de-regressed proofs from bulls (see below) were used
180 for the estimation of genomic and conventional breeding values. These values will be called
181 phenotypes. This process resulted in double counting of data from cows that also were
182 daughters of bulls included. After matching genotypes with phenotypes 1,492 individuals
183 (185 bulls and 1,307 cows) remained for yield traits, 1,149 individuals (157 bulls and 992
184 cows) remained for calving interval, and 1,403 individuals (157 bulls and 1,246 cows) had
185 PLI and GMI indexes available. For bull PTA 2.3% of the 28,709 daughters contributing
186 records were found among the genotyped cows, and in the distribution of genotyped cows to
187 daughter contributions among the 185 bulls the median was 0 and the upper quartile was 3%.

188 The PTA were multiplied by 2 to get EBV and de-regressed using the approach
189 described by Garrick et al. (2009). Weights were calculated to allow for the unequal error
190 variances of the de-regressed EBV; for each individual i , the weight w_i was calculated as:
191 $w_i = (1 - h^2) / [(c + (1 - r_i^2) / r_i^2) h^2]$ where c is the genetic variance not assigned to SNP
192 effects and was defined to be 0.2 following the estimate of Daetwyler (2009) for the 50K
193 Illumina SNP chip; h^2 is the trait heritability; and r_i^2 is the reliability of the de-regressed
194 EBV. The value of c was assumed to be the same for all traits. Heritabilities assumed were

195 0.55 for milk yield, 0.47 for fat yield, 0.51 for protein yield, and 0.033 for calving interval,
 196 which are those used for UK evaluations. Weights for repeated lactation milk records of cows
 197 were calculated as: $w_i = (1 - h^2)/[(ch^2 + (1 + (n - 1)t)/n) - h^2]$ where n is the number
 198 of lactations and t is the repeatability used for UK evaluations (0.82, 0.84, and 0.79 for milk,
 199 fat, and protein yield, respectively). The mean w_i for cows were: 0.97 (SD 0.11) for milk
 200 yield, 0.98 (SD 0.09) for fat yield, and 1.01 (SD 0.12) for protein yield. Because calving
 201 interval was available only for the first lactation $w_i = 0.99$ for all the cows. The weights for
 202 bulls were greater: 2.93 (SD 0.74) for milk yield, 4.03 (SD 1.02) for fat yield, 3.44 (SD 0.87)
 203 for protein yield, and 44.2 (SD 22.16) for calving interval.

204 *Prediction of Breeding Values*

205 Two univariate models and one bivariate model were used to calculate EBV using
 206 ASReml software (Gilmour et al., 2009). The 2 univariate models differed in the relationship
 207 matrix used. One used Wright's Numerator Relationship Matrix (**A**) and the other a genomic
 208 (**G**) relationship matrix. The univariate model can be expressed as:

$$209 \quad \mathbf{y} = \mathbf{1}\mu + \mathbf{Z}\mathbf{u} + \mathbf{e}$$

210 where \mathbf{y} is a vector of phenotypes; μ is the overall mean; \mathbf{Z} is the incidence matrix linking the
 211 records from vector \mathbf{y} to vector \mathbf{u} ; \mathbf{u} is a vector of random genetic effects of the animals; \mathbf{e} is
 212 the vector of errors distributed as $N(0, \sigma_e^2 \mathbf{W}^{-1})$ with \mathbf{W}^{-1} diagonal matrix. The diagonal
 213 matrix \mathbf{W} contains the weights w_i for each individual as described above.

214 Depending on the model, the variance of \mathbf{u} was $\text{Var}(\mathbf{u}) = \mathbf{A}\sigma_a^2$, where σ_a^2 is additive
 215 genetic variance, or it was $\text{Var}(\mathbf{u}) = \mathbf{G}\sigma_g^2$, where σ_g^2 is genetic variance associated with **G**.
 216 Matrix **A** was calculated using the known pedigree, and matrix **G** using the whole genome
 217 SNP data following VanRaden (2008):

$$\mathbf{G} = \frac{\mathbf{M}\mathbf{M}'}{2 \sum_j^{N_{snp}} p_j(1 - p_j)}$$

where \mathbf{M} is a matrix of genotypes with elements M_{ij} denoting the number of the counted allele for animal i at SNP j and expressed as the deviation from the SNP mean allele frequency of $2p_j$, and N_{snp} is the number of SNP.

To examine if the correlation between the EBV obtained from bulls' or cows' genotypes was different from one, the following bivariate model was used:

$$\begin{bmatrix} \mathbf{y}_1 \\ \mathbf{y}_2 \end{bmatrix} = \begin{bmatrix} \mathbf{1}' & 0 \\ 0 & \mathbf{1}' \end{bmatrix} \begin{bmatrix} \mu_1 \\ \mu_2 \end{bmatrix} + \begin{bmatrix} \mathbf{Z}_1 & 0 \\ 0 & \mathbf{Z}_2 \end{bmatrix} \begin{bmatrix} \mathbf{u}_1 \\ \mathbf{u}_2 \end{bmatrix} + \begin{bmatrix} \mathbf{e}_1 \\ \mathbf{e}_2 \end{bmatrix}$$

where \mathbf{y}_1 is a vector of bulls' phenotypes with cows' phenotypes set as missing; \mathbf{y}_2 is a vector of cows' phenotypes with bulls phenotypes set as missing; μ_1 and μ_2 are the overall mean values for bulls and cows; \mathbf{Z}_1 and \mathbf{Z}_2 are equal incidence matrices linking the records from vectors \mathbf{y}_1 and \mathbf{y}_2 to vectors \mathbf{u}_1 and \mathbf{u}_2 ; \mathbf{u}_1 and \mathbf{u}_2 are vectors of random genetic effects of the animals; \mathbf{e}_1 and \mathbf{e}_2 are the vector of errors.

The following (co)variance structure for random genetic effects is assumed:

$$var \begin{bmatrix} \mathbf{u}_1 \\ \mathbf{u}_2 \\ \mathbf{e}_1 \\ \mathbf{e}_2 \end{bmatrix} = \begin{bmatrix} \sigma_{g_1}^2 \mathbf{G} & \sigma_{g_{12}} \mathbf{G} & 0 & 0 \\ \sigma_{g_{21}} \mathbf{G} & \sigma_{g_2}^2 \mathbf{G} & 0 & 0 \\ 0 & 0 & \sigma_{e_1}^2 \mathbf{W}^{-1} & 0 \\ 0 & 0 & 0 & \sigma_{e_2}^2 \mathbf{W}^{-1} \end{bmatrix}$$

where $\sigma_{g_1}^2$ and $\sigma_{g_2}^2$ are genetic variances explained with SNP effects estimates from bulls or cows; $\sigma_{g_{12}} = \sigma_{g_{21}}$ is the genetic covariance between SNP effects estimates; $\sigma_{e_1}^2$ and $\sigma_{e_2}^2$ are the residual variances.

235 *Scenarios for Creating Reference Population*

236 In total 10 scenarios were compared using 10-fold cross-validation, with all scenarios
237 tested on each validation set. In each fold 90% of cow records were available for estimating
238 the SNP effects, and the remaining 10% of records used for validation and set to missing.
239 Bulls were always included, as the central question was how to supplement the bull data with
240 routine cow genotyping. Validation sets were created at random by sampling without
241 replacement, so each cow appeared in only one validation set. The weighted correlation
242 between the genomic EBV and phenotypes for the cows in the validation set was calculated
243 within each fold with weights calculated as $w_i = 1/[t + (1 - t)/n]$, where t is the
244 repeatability. Means and approximate standard errors were calculated from the standard
245 deviations across the cross-validation folds of estimates made within folds. An approximate
246 one-tailed sign test was used in some comparisons to assess the significance of the difference
247 in correlation between 2 scenarios. An observed improvement was judged as significant when
248 the correlation was greater in at least 8 out of 10 folds, which has a Type 1 error of 5.5%
249 when compared to Binomial(10,0.5).

250 The 10 scenarios differed in the simulation of cow selective genotyping (Table 1).
251 Within each fold of 10-fold cross-validation test selective genotyping was performed only on
252 the cows for which records were available for estimating the SNP effects. When the cow was
253 not selected to be genotyped her phenotype was set to missing so this cow did not contribute
254 to the SNP effect estimates. In scenario 1 there were no cows genotyped whereas in all the
255 other scenarios different proportion of cows were genotyped. Cows contributing genotypes
256 were selected in four ways: (i) all cows; (ii) a random sample of half of the cows; (iii) cows
257 with extreme phenotypes; and (iv) cows with extreme values in either tail. Selection of cows
258 with extreme phenotypes was based on the: (i) percentage of cows selected for genotyping
259 (50%, 40%, or 30%); and (ii) the trait used for selection of cows to be genotyped. The traits

260 used for selection of cows to be genotyped were: (i) the trait for which EBV was calculated;
261 (ii) milk yield; (iii) PLI; or (iv) GMI.

262 » Table 1 near here «

263 *Quantitative Modelling of Genotyping Strategies.*

264 To validate and generalise the results of the cross-validation outcomes for genotyping
265 strategy, the quantitative models of Daetwyler et al. (2008, 2010) were extended to cover the
266 range of scenarios considered here. This development is described in detail in Appendix B.
267 The predictions obtained were compared with the cross-validation outcomes for the
268 production traits.

269 **RESULTS**

270 *Imputation Accuracy*

271 The correlation between the true and imputed genotypes was 0.952 between
272 individuals and 0.945 between SNP (Table 2). Genotype concordance was 0.961 and allele
273 concordance was 0.980. The concordances were greater than correlations and were the same
274 between individuals or between SNP.

275 » Table 2 near here «

276 *Genotyping Cows*

277 Genotyping cows with phenotypes (scenario 2) and using their data for the prediction
278 of SNP effects increased the correlation between phenotypes and genomic EBV (Table 3)
279 compared to using a training set consisting of the genotyped bulls alone (scenario 1). Benefits
280 were observed across all folds for all yield traits. For milk yield, when using univariate
281 GBLUP, the correlation increased by 0.163 ± 0.022 to 0.376 ± 0.019 and was the highest

282 among all the traits. For fat yield the correlation increased by 0.111 ± 0.021 to 0.347 ± 0.025 ,
283 and for protein yield by 0.113 ± 0.018 to 0.323 ± 0.027 . Calving interval was the exception
284 where the correlation did not increase, it dropped from the low base of GBLUP (0.057
285 ± 0.029) by 0.014 ± 0.010 to 0.042 ± 0.031 . Negative correlations with phenotypic calving
286 interval were observed for 3 out of 10 folds for bulls alone, and 2 out of 10 after adding the
287 cows.

288 The training set of bulls and cows with genomic data using GBLUP improved the
289 accuracy of prediction compared with classical BLUP. The increases in the correlation
290 between GBLUP and BLUP approaches were by 0.060 ± 0.015 for milk, 0.036 ± 0.019 for
291 fat, 0.033 ± 0.015 for protein, and 0.024 ± 0.024 for calving interval. For the yield traits the
292 addition of the cow data to the training set spanned the tipping point so that the bulls'
293 genomic data alone provided less accurate predictions than BLUP, whereas with cows'
294 genomic data predictions were more accurate.

295 The genetic correlation between the phenotypes from bulls and cows in the bivariate
296 model was less than 1 ($P < 0.05$) for all traits except for calving interval where it was not
297 estimable. For milk, fat, and protein yields the estimates were $0.600 (\pm 0.142)$, 0.606
298 (± 0.130) , and $0.628 (\pm 0.144)$, respectively, whilst for calving interval there was a lack of
299 convergence. When the bivariate model was used the correlation between phenotype and
300 genomic EBV for milk yield did not change compared to the univariate model with bulls and
301 cows, and changed only marginally for fat and protein yield.

302 » Table 3 near here «

303 ***Cow Genotyping Strategies***

304 Selecting a subset of cows for genotyping decreased the correlation between the
305 phenotypes and genomic EBV for yield traits as might be expected (see Table 4; scenarios 2
306 cf. 3). The largest decrease when genotyping only half of the cows selected at random was for
307 milk yield where the correlation dropped from 0.376 by 0.055 ± 0.014 when using univariate
308 GBLUP. For fat yield and protein yield these decreases were smaller but notable, 0.033
309 ± 0.012 and 0.036 ± 0.012 . Given the low predictive accuracy obtained for calving interval
310 and the scale of variation in validation sets the detailed results for this trait are not discussed
311 although the results are shown in Table 4.

312 The genotyping strategy was important when using a subset of individuals for
313 training. Genotyping only the 50% of individuals which were in extreme within either tail of
314 phenotypes increased the correlation between the phenotypes and genomic EBV and restored
315 much of the loss in accuracy from genotyping only 50% the cows at random (Table 4;
316 scenarios 5 cf. 3) with increases in accuracy of 0.048 ± 0.016 , 0.026 ± 0.010 , and 0.035
317 ± 0.012 for milk, fat, and protein yields, respectively. The greater accuracy from the
318 divergent selection was observed in at least 8 out of 10 folds for all 3 yield traits. In contrast,
319 genotyping only the 50% of phenotypes in upper tail decreased the correlation between the
320 phenotypes and genomic EBV below that obtained from randomly selecting 50% for all yield
321 traits (Table 4; scenarios 4 cf. 3) by 0.037 ± 0.016 , 0.050 ± 0.013 , and 0.041 ± 0.016 .

322 Reducing the percentage of genotyped cows with extreme phenotypes below 50%
323 decreased the correlation between phenotypes and genomic EBV, but even when only 30% of
324 cows were genotyped and selected from the extremes (scenario 7), the correlations for milk,
325 fat, and protein yield were still higher than in scenario 3 where 50% of phenotypes were
326 genotyped at random. These benefits were observed for at least 8 out of the 10 folds for all
327 yield traits. Averaged over the 3 yield traits, divergent selection of 30%, 40%, and 50% of the

328 cows restored 56%, 72%, and 88% of the loss from selecting 50% of cows at random,
329 compared to genotyping all the available cows.

330 » Table 4 near here «

331 To increase the correlation between the genomic EBV and phenotypes, different
332 criteria were used for selecting cows to be genotyped (Table 5). Results were inconsistent
333 across trait. For fat yield, correlation was the highest when genotyping was done based on
334 GMI ranks (scenario 10), for milk and protein yield when selection was based on milk yield
335 (scenario 8), and for calving interval when ranking was based on PLI (scenario 9). When PLI
336 or GMI were used as selection criterion correlations were always greater than in scenarios
337 where cows were selected at random. The correlations between PLI and yield traits were:
338 0.27 for milk yield, 0.39 for fat, and 0.36 for protein yield. Between GMI and yield traits they
339 were: 0.29 for milk yield, 0.46 for fat yield, and 0.42 for protein yield. For calving interval
340 the correlation with both PLI and GMI was negative (-0.13 and -0.16 , respectively) which is
341 expected as long calving interval is not desired.

342 » Table 5 near here «

343 ***Bias***

344 Table 6 shows the slopes of the regressions of phenotypes on genomic EBV for a range of
345 scenarios, where unbiasedness is indicated by a slope of 1, with under- and over-estimation
346 indicated by slopes >1 and <1 respectively. There is only occasional evidence for
347 underestimation of differences in breeding values: using bulls only for the training set
348 (scenario 1) when predicting fat yield, and using the 50% of cows from the upper tail
349 (scenario 4) when predicting protein yield. However an overview of Table 6 suggests that
350 random selection of cows were less likely to be biased with selection strategies involving

351 only the tails having a trend towards overestimation. This was examined by comparing
352 regression slopes within cross-validation folds for scenarios 3, 4, and 5 where 50% of cows
353 were selected either randomly, from the upper tail only, or from both tails respectively.
354 Reductions in slope of 0.175 ± 0.052 , 0.077 ± 0.034 , and 0.091 ± 0.032 for milk, fat and
355 protein yield, respectively, were observed when 50% of cows from both tails were selected
356 compared to random selection (cf. scenarios 5 and 3). Selection from the upper tail alone
357 increased the trend towards overestimation, particularly for fat and protein yield, by with
358 further reductions in slope of 0.052 ± 0.057 , 0.209 ± 0.041 , and 0.189 ± 0.039 for the same
359 three traits (cf. scenarios 4 and 5). Note that uncertainty in whether or not predictions for
360 scenario 3 are themselves unbiased preclude stating that scenarios 4 and 5 overestimate true
361 differences in breeding values. Regression slopes for calving intervals varied widely.

362 » Table 6 near here «

363 *Predicting Benefits of Genotyping Strategies*

364 Figure 2 shows the relationship between r_p^{-2} , the square of the reciprocal of the values shown
365 in Table 4 and $(n\delta)^{-1}$ where n is the number of records in the training set and δ is the
366 fractional change in genetic variance arising from selection (see Appendix B). The
367 expectation is that the relationship is linear and this was broadly observed. Some biases are
368 evident with the points representing scenarios with selection tending to be less than predicted
369 from the regression and factors contributing to the deviations are discussed below. The model
370 correctly predicts that scenarios 5, 6, and 7 using divergent selection for milk yield, fat yield,
371 and protein yield will be more accurate than scenario 3 with random selection of 50%. The
372 threshold for the equivalence of divergent selection to random selection of 50% depends on
373 the heritability, but for all yield traits the model predicted thresholds between 20% and 30%,
374 with traits of higher heritability having thresholds associated with greater intensity.

375

» Figure 2 near here «

376

DISCUSSION

377

378

379

380

381

382

383

384

385

386

387

388

389

390

391

392

393

394

395

396

There are fewer than 200 progeny tested Guernsey bulls from The Royal Guernsey Agricultural & Horticultural Society and The English Guernsey Cattle Society with genotypes available for use as a training set for initiating genomic evaluations. The results showed that these alone had weaker predictive power than the use of BLUP and in this population lead to biased estimates of breeding values. Whilst genomic information can be combined with the information from pedigree (Legarra et al., 2009; Meuwissen et al., 2011), obtaining substantial increases in accuracy, especially for functional traits such as calving interval will come from increasing the training set size. However, the number of progeny tested bulls per year in the Guernsey is small and their number is not expected to increase significantly in the near future. There are three possible solutions to increase the accuracy of breeding values obtained: (i) to include genotypes of proven bulls from another cattle breed, which to date has met with limited success (Hayes et al., 2009; Olson et al., 2012; Hozé et al., 2014); (ii) to include genotypes from the same breed but from another country (Cooper et al., 2016), or (iii) as tested here, to include genotypes from cows with their own records (Pryce et al., 2012; Calus et al., 2013). The results showed that supplementing the training set with approximately 1,200 genotyped cows was sufficient to boost the accuracy of GBLUP to outperform BLUP by between 11% and 19% and also reduced the bias of the predictions for yield traits. This demonstrates that even for a numerically small commercial dairy breed, genomic approaches have significant potential, and argues for a program of cow genotyping to further increase accuracy by increasing the size of the training set.

397

398

The study provided some support for the proposition of Habier et al. (2010) that genotyping cows is valuable as animals may share more recent relationships and thus have

399 more consistent LD. Support comes from the estimated genetic correlations (r_g) of ~ 0.6
400 between the phenotypes of the training set of bulls and the training set of cows, which was
401 significantly different from 1. The training set of bulls used to predict the Guernsey Island
402 sub-population contained bulls with over 25,000 progeny contributing records for each of the
403 traits considered here, but their dates of birth spanned over 50 years and they come from
404 different sub-populations of the breed. Such differences in age and sub-population would
405 introduce differences in the linkage relationships between the training set of bulls and the
406 Guernsey Island population which provided all the cow data. Nevertheless, other factors may
407 also contribute to the genetic correlations observed, such as differences in trait definitions as
408 daily milk records were used for the prediction of bulls PTA for yield traits, while 305-day
409 lactation records were used for cows. In this data there was very little benefit in from using
410 bivariate models to predict breeding values compared to a univariate model which assumes
411 $r_g = 1$. The explanation lies in 2 opposing effects, when $r_g < 1$ the information content of
412 the bull data is reduced in its predictive value, potentially reducing accuracy, whereas
413 removing the assumption that $r_g = 1$ removes some bias in the estimating the true marker
414 effects in Guernsey Island cows. It would be anticipated that as the training set increases in
415 size the bivariate model would ultimately emerge as the more accurate due to its greater
416 veracity. The imperfect correlation is a further factor to incorporate into the formulae of de
417 Roos (2011) in attempting to provide an exchange rate between the values of cow phenotypes
418 and de-regressed bull proofs.

419 Notwithstanding the value of genotyping cows, a numerically small commercial breed
420 will need to be cost-effective in establishing a genotyping programme and this study showed
421 that both imputation and selective genotyping can play an important role in this. The value of
422 imputation in allowing the routine genotyping to be carried out with low-density chips has
423 been demonstrated in other studies (Cleveland and Hickey, 2013; Boison et al., 2015).

424 However, this is one of the first reports to quantify the value of selective genotyping for
425 genomic selection in dairy cattle in practice, although others e.g. Jiménez-Montero (2012)
426 have suggested benefits from simulations. Compared to genotyping 50% of the cows at
427 random, divergent selection of 50% using extremes at either tail recovered 88% of the
428 information that was lost from not genotyping all the cows. It is important to note that
429 directional selection for genotyping was much worse than divergent selection for genotyping
430 and worse than random selection.

431 In this study random assignment was used for conducting the cross validation and this
432 may be less desirable for predicting the accuracy of selection of young bulls than alternative
433 assignment strategies (Cooper et al., 2015) as it has been reported to lead to higher estimates
434 of accuracy than appropriate (Pérez-Cabal et al., 2012). However the alternative strategies
435 such as forward prediction of young sires or a cut in the study defined by time suggested by
436 Cooper et al. (2015) are difficult to apply in this small population where only cows present in
437 2014 could be genotyped. For example, if young sires with at least 10 daughters were to be
438 used the most recent sample would contain 6 sires born in 2007 and 2008. Whilst these
439 alternative strategies are relevant to prediction accuracy of the young animals in the most
440 recent birth cohort, the comparison of genotyping strategies among the cows might be
441 expected to be more robust to these strategies, with the mean absolute genomic relatedness
442 between the training and validation data sets varying between 0.029 and 0.032 across the
443 different scenarios.

444 The value of creating training sets for the purpose of genomic prediction with
445 increased genetic variance has been explored previously in case-control studies (Daetwyler et
446 al., 2008), and using non-random mating or reproductive technology to increase
447 homozygosity (Nirea et al., 2012). Both studies provided theoretical justification for the
448 benefits in accuracy from increasing the genetic variance in the training set. Here the

449 prediction equation of Daetwyler et al. (2008, 2010) was extended to encompass selection of
450 the phenotypes for genotyping by considering the genetic variance captured in the training
451 set. The predictions were broadly accurate in predicting order and the magnitude of
452 differences. There is sampling variation in the data and the cross-validation which will affect
453 the performance of the predictions through the y-values of Figure 2. However, there are
454 additional potential errors introduced by the use of the UK consensus heritabilities as their
455 relevance to the true heritabilities for this population has not been established, although they
456 are used for the UK genetic evaluations. The predictions derived are dependent on the
457 heritability assumed for a trait in 2 ways: firstly in the de-regression process which affects all
458 scenarios (through the y-values in Figure 2); and secondly, where selection was practiced, in
459 the prediction of genetic variance and consequently in the x-values. The differential impact
460 may explain in part why the scenarios with divergent selection tend to lie beneath the
461 regression lines.

462 **CONCLUSIONS**

463 The study has shown with real data that using cow genotypes selected with divergent
464 strategies can provide a cost effective route for building training sets in small dairy
465 populations. The correlation between the genomic EBV and phenotypes increased when cow
466 phenotypes were used for the prediction of genomic EBV. When half of the population was
467 genotyped, genotyping only individuals with phenotypes in either tail was shown to be better
468 than genotyping them at random or genotyping only individuals with upper tail phenotypes.
469 Genotyping cows with tail phenotype covered on average 88% of the difference between the
470 scenario where all the cows were genotyped or only half of them were genotyped at random.
471 Using GMI for selection of cows for genotyping yields a correlation that was comparable to
472 the correlations obtained in scenarios when cows were selected based on the values for each

473 trait. Genotyping only the individuals from either tail will enable the Guernsey cattle breed in
474 Guernsey Island and United Kingdom to successfully adopt genomic selection and use the
475 available financial resources optimally.

476 ACKNOWLEDGEMENTS

477 The research leading to these results has received funding from the European's Union
478 Seventh Framework Programme for research, technological development and demonstration
479 [G.A. 289592] - Gene2Farm. The valuable comments from two anonymous reviewers are
480 highly appreciated.

481 REFERENCES

- 482 Boison, S.A., D.J.A. Santos, A.H.T. Utsunomiya, R. Carvalheiro, H.H.R. Neves, A.M.P. O'Brien,
483 J.F. Garcia, J. Sölkner, and M.V.G.B. da Silva. 2015. Strategies for single nucleotide
484 polymorphism (SNP) genotyping to enhance genotype imputation in Gyr (*Bos indicus*) dairy
485 cattle: Comparison of commercially available SNP chips. *J. Dairy Sci.* 98:4969–4989.
486 <http://dx.doi.org/10.3168/jds.2014-9213>.
- 487 Bulmer, M.G. 1971. The effect of selection on genetic variability. *Am. Nat.* 105:201–211.
- 488 Calus, M.P.L., Y. de Haas, and R.F. Veerkamp. 2013. Combining cow and bull reference
489 populations to increase accuracy of genomic prediction and genome-wide association
490 studies. *J. Dairy Sci.* 96:6703–6715. <http://dx.doi.org/10.3168/jds.2012-6013>.
- 491 Clark, S.A., J.M. Hickey, H.D. Daetwyler, and J.H. van der Werf. 2012. The importance of
492 information on relatives for the prediction of genomic breeding values and the implications
493 for the makeup of reference data sets in livestock breeding schemes. *Genet. Sel. Evol.* 44:4.
494 <http://dx.doi.org/10.1186/1297-9686-44-4>.
- 495 Cleveland, M.A., and J.M. Hickey. 2013. Practical implementation of cost-effective genomic
496 selection in commercial pig breeding using imputation. *J. Anim. Sci.* 91:3583–3592.
497 <http://dx.doi.org/10.2527/jas.2013-6270>.
- 498 Cooper, T.A., G.R. Wiggans, and P.M. VanRaden. 2015. Short communication: Analysis of
499 genomic predictor population for Holstein dairy cattle in the United States—Effects of sex
500 and age. *J. Dairy Sci.* 98:2785–2788. <http://dx.doi:10.3168/jds.2014-8894>.
- 501 Cooper, T. A., S. A. E. Eaglen, G. R. Wiggans, J. Jenko, H. J. Huson, D. R. Morrice, M. Bichard,
502 W. G. de L. Luff,|| and J. A. Woolliams. 2016 Genomic evaluation, breed identification, and
503 population structure of Guernsey cattle in North America, Great Britain, and the Isle of
504 Guernsey. *J. Dairy Sci.* TBC:1-8. <http://dx.doi.org/10.3168/jds.2015-10445>.
- 505 Daetwyler, H.D., B. Villanueva, and J.A. Woolliams. 2008. Accuracy of predicting the genetic
506 risk of disease using a genome-wide approach. *PLoS ONE.* 3:e3395.
507 <http://dx.doi.org/10.1371/journal.pone.0003395>.

508 Daetwyler, H.D. 2009. Genome-wide evaluation of populations. PhD Thesis. Wageningen
509 Univ., Wageningen, The Netherlands.

510 Daetwyler, H.D., R. Pong-Wong, B. Villanueva, and J.A. Woolliams. 2010. The impact of
511 genetic architecture on genome-wide evaluation methods. *Genetics*. 185:1021–1031.
512 <http://dx.doi.org/10.1534/genetics.110.116855>.

513 Garrick, D.J., J.F. Taylor, and R.L. Fernando. 2009. Deregressing estimated breeding values
514 and weighting information for genomic regression analyses. *Genet. Sel. Evol.* 41:55.
515 <http://dx.doi.org/10.1186/1297-9686-41-55>.

516 Gilmour, A.R., B.J. Gogel, B.R. Cullis, and R. Thompson. 2009. ASReml user guide release 3.0.
517 VSN Int. Ltd Hemel Hempstead UK.

518 Goddard, M. 2009. Genomic selection: prediction of accuracy and maximisation of long term
519 response. *Genetica*. 136:245–257. <http://dx.doi.org/10.1007/s10709-008-9308-0>.

520 Habier, D., J. Tetens, F.-R. Seefried, P. Lichtner, and G. Thaller. 2010. The impact of genetic
521 relationship information on genomic breeding values in German Holstein cattle. *Genet. Sel.
522 Evol.* 42:5. <http://dx.doi.org/10.1186/1297-9686-42-5>.

523 Hayes, B.J., P.J. Bowman, A.C. Chamberlain, K. Verbyla, and M.E. Goddard. 2009. Accuracy of
524 genomic breeding values in multi-breed dairy cattle populations. *Genet. Sel. Evol.* 41:51.
525 <http://dx.doi.org/10.1186/1297-9686-41-51>.

526 Hozé, C., S. Fritz, F. Phocas, D. Boichard, V. Ducrocq, and P. Croiseau. 2014. Efficiency of
527 multi-breed genomic selection for dairy cattle breeds with different sizes of reference
528 population. *J. Dairy Sci.* 97:3918–3929. <http://dx.doi.org/10.3168/jds.2013-7761>.

529 Jiménez-Montero, J.A., O. González-Recio, and R. Alenda. 2012. Genotyping strategies for
530 genomic selection in small dairy cattle populations. *Animal*. 6:1216–1224.
531 <http://dx.doi.org/10.1017/S1751731112000341>.

532 Legarra, A., I. Aguilar, and I. Misztal. 2009. A relationship matrix including full pedigree and
533 genomic information. *J. Dairy Sci.* 92:4656–4663. <http://dx.doi.org/10.3168/jds.2009-2061>.

534 Meuwissen, T.H.E., B.J. Hayes, and M.E. Goddard. 2001. Prediction of total genetic value
535 using genome-wide dense marker maps. *Genetics*. 157:1819–1829.

536 Meuwissen, T. h. e., T. Luan, and J. a. Woolliams. 2011. The unified approach to the use of
537 genomic and pedigree information in genomic evaluations revisited. *J. Anim. Breed. Genet.*
538 128:429–439. <http://dx.doi.org/10.1111/j.1439-0388.2011.00966.x>.

539 Nirea, K.G., A.K. Sonesson, J.A. Woolliams, and T.H. Meuwissen. 2012. Effect of non-random
540 mating on genomic and BLUP selection schemes. *Genet. Sel. Evol.* 44:11.
541 <http://dx.doi.org/10.1186/1297-9686-44-11>.

542 Olson, K.M., P.M. VanRaden, and M.E. Tooker. 2012. Multibreed genomic evaluations using
543 purebred Holsteins, Jerseys, and Brown Swiss. *J. Dairy Sci.* 95:5378–5383.
544 <http://dx.doi.org/10.3168/jds.2011-5006>.

545 Pérez-Cabal, M.A., A.I. Vazquez, D. Gianola, G.J.M. Rosa, and K.A. Weigel. 2012.
546 Accuracy of genome-enabled prediction in a dairy cattle population using different cross-
547 validation layouts. *Livest. Genomics*. 3:27. doi:10.3389/fgene.2012.00027.

548 Pryce, J. E., B. J. Hayes, and M. E. Goddard. 2012. Genotyping dairy females can improve
549 the reliability of genomic selection for young bulls and heifers and provide farmers with new
550 management tools. ICAR Conference, Cork, Ireland. Accessed May 14, 2015.
551 http://www.icar.org/cork_2012/Manuscripts/Published/Pryce%202.pdf

552 Pszczola, M., T. Strabel, H.A. Mulder, and M.P.L. Calus. 2012. Reliability of direct genomic

553 values for animals with different relationships within and to the reference population. *J.*
554 *Dairy Sci.* 95:389–400. <http://dx.doi.org/10.3168/jds.2011-4338>.

555 Purcell, S., B. Neale, K. Todd-Brown, L. Thomas, M.A.R. Ferreira, D. Bender, J. Maller, P.
556 Sklar, P.I.W. de Bakker, M.J. Daly, and P.C. Sham. 2007. PLINK: A tool set for whole-genome
557 association and population-based linkage analyses. *Am. J. Hum. Genet.* 81:559–575.

558 de Roos, A.P.W. 2011. Genomic selection in dairy cattle. PhD Thesis. Wageningen Univ.,
559 Wageningen, The Netherlands.

560 Sargent, F.D., V.H. Lytton, and O.G. Wall Jr. 1968. Test interval method of calculating dairy
561 herd improvement association records. *J. Dairy Sci.* 51:170–179.
562 [http://dx.doi.org/10.3168/jds.S0022-0302\(68\)86943-7](http://dx.doi.org/10.3168/jds.S0022-0302(68)86943-7).

563 Sargolzaei, M., J.P. Chesnais, and F.S. Schenkel. 2014. A new approach for efficient genotype
564 imputation using information from relatives. *BMC Genomics.* 15:478.
565 <http://dx.doi.org/10.1186/1471-2164-15-478>.

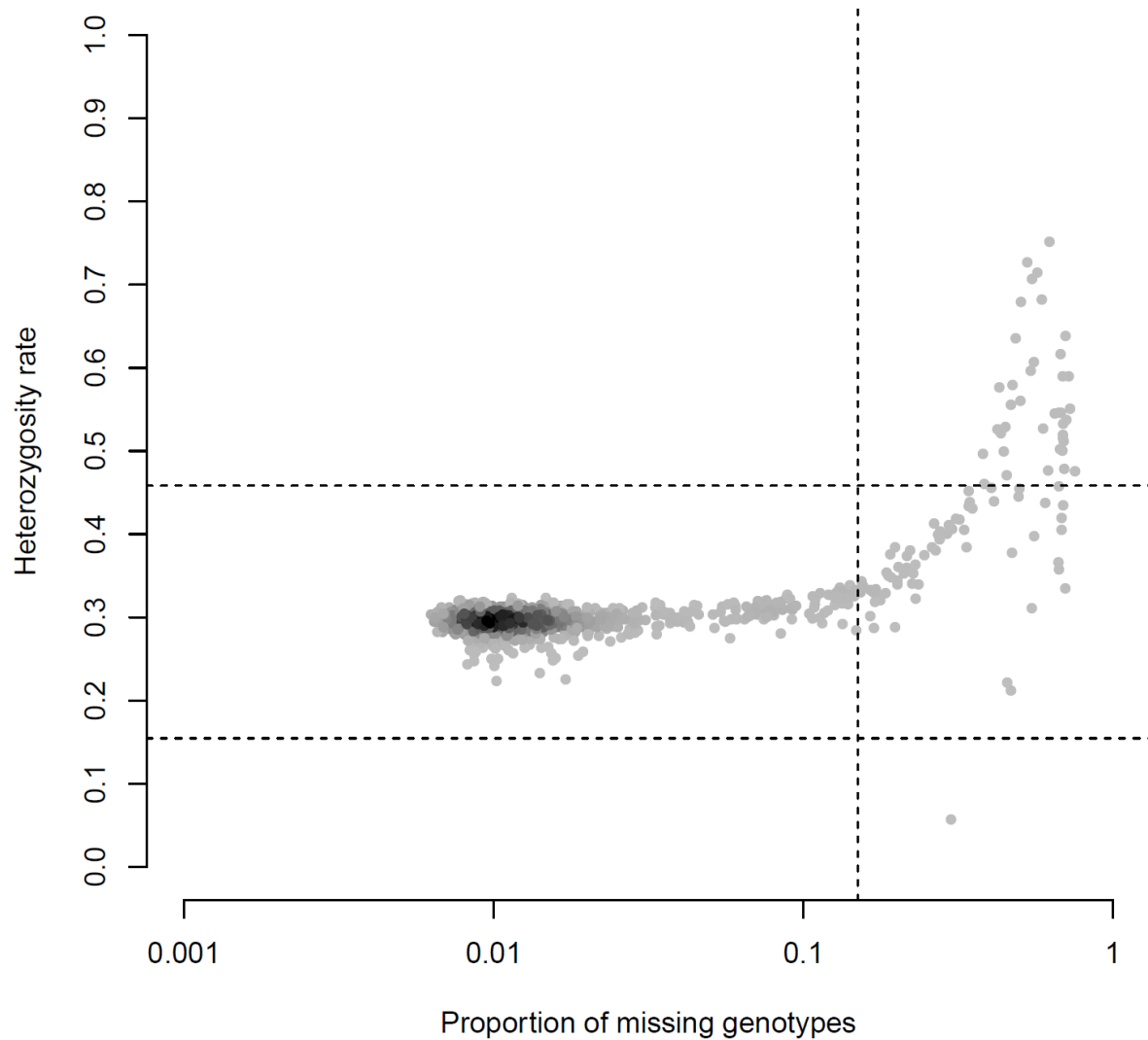
566 Schaeffer, L.R. 2006. Strategy for applying genome-wide selection in dairy cattle. *J. Anim.*
567 *Breed. Genet.* 123:218–223. <http://dx.doi.org/10.1111/j.1439-0388.2006.00595.x>.

568 VanRaden, P.M. 2008. Efficient methods to compute genomic predictions. *J. Dairy Sci.*
569 91:4414–4423. <http://dx.doi.org/10.3168/jds.2007-0980>.

570 VanRaden, P.M., C.P. Van Tassell, G.R. Wiggans, T.S. Sonstegard, R.D. Schnabel, J.F. Taylor,
571 and F.S. Schenkel. 2009. Invited Review: Reliability of genomic predictions for North
572 American Holstein bulls. *J. Dairy Sci.* 92:16–24. <http://dx.doi.org/10.3168/jds.2008-1514>.

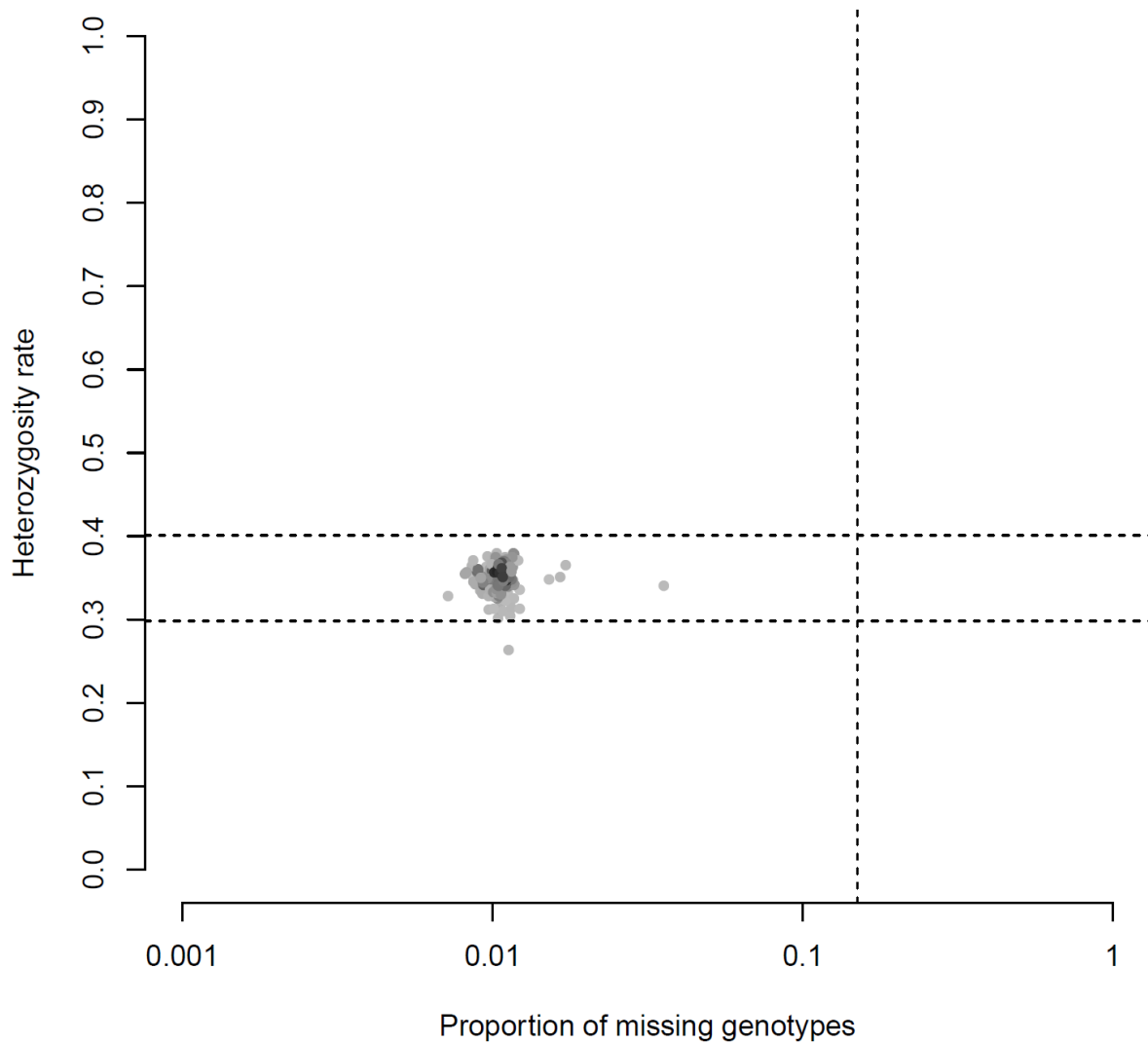
573 VanRaden, P.M., C. Sun, and J.R. O’Connell. 2015. Fast imputation using medium or low-
574 coverage sequence data. *BMC Genet.* 16:82. <http://dx.doi.org/10.1186/s12863-015-0243-7>.

575



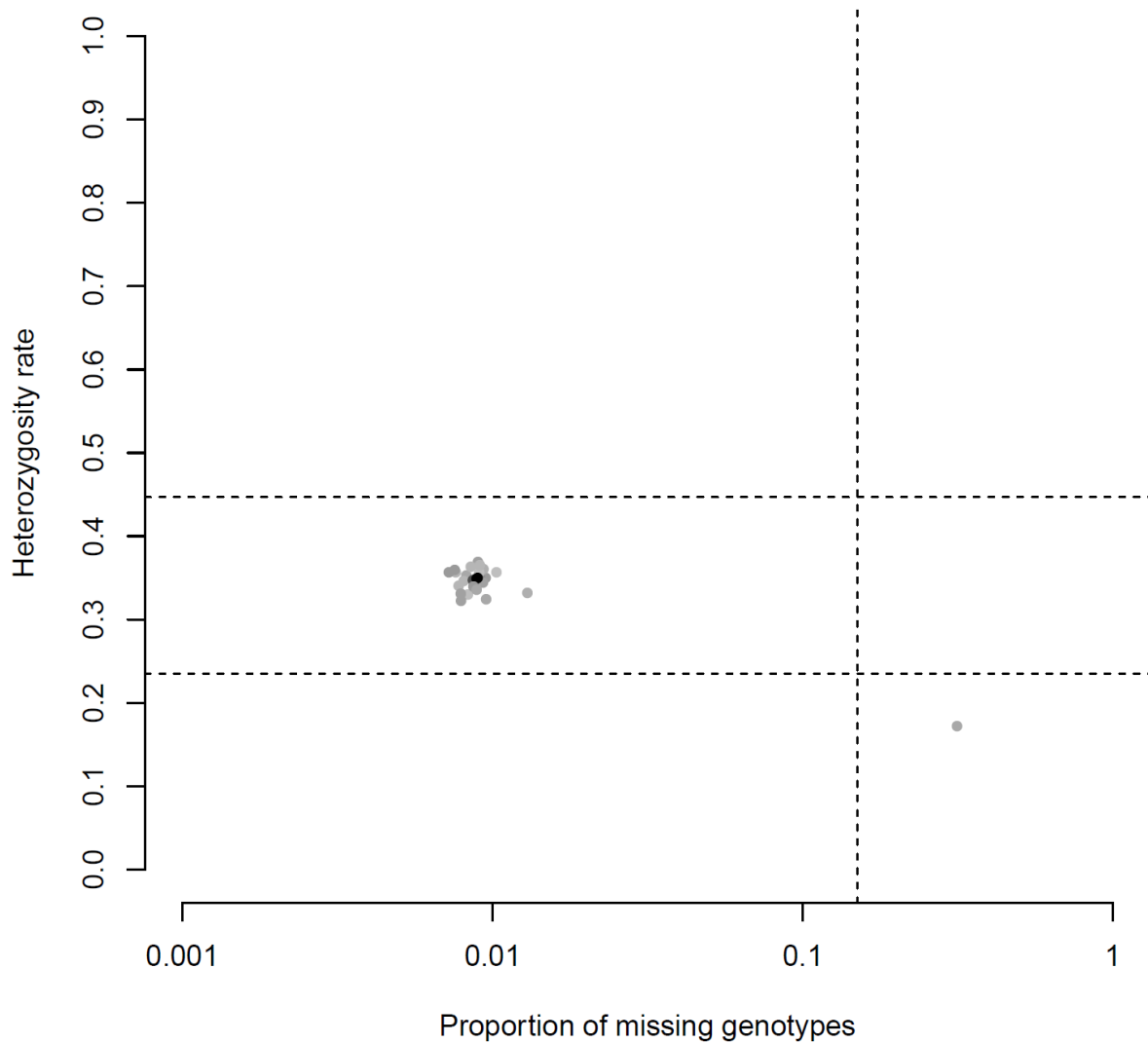
577

578 Figure A1. Heterozygosity rate and proportion of missing genotypes for GeneSeek Genomic
579 Profiler Version 3 chip (left from vertical dashed line there are genotypes with <0.15 of
580 missing genotypes and in-between horizontal lines there are genotypes within the range of
581 ± 3 SD of overall heterozygosity rate).



582

583 Figure A2. Heterozygosity rate and proportion of missing genotypes for GeneSeek Genomic
 584 Profiler HD Version 1 chip (left from vertical dashed line there are genotypes with <0.15 of
 585 missing genotypes and in-between horizontal lines there are genotypes within the range of
 586 ± 3 SD of overall heterozygosity rate).



587

588 Figure A3. Heterozygosity rate and proportion of missing genotypes for Illumina BovineHD
 589 chip (left from vertical dashed line there are genotypes with <0.15 of missing genotypes and
 590 in-between horizontal lines there are genotypes within the range of ± 3 SD of overall
 591 heterozygosity rate).

592

594 The prediction formulae of Daetwyler et al. (2008, 2010) modified for the prediction
595 accuracy of phenotypes by genomic EBV (\hat{g}) is of the form $r_p^2 = h^2 \lambda (\lambda + 1)^{-1}$ where r_p is
596 the accuracy, $\lambda = nh^2/M_e$, n is the number of training records, h^2 is the heritability and M_e
597 is the number of independent segments, a property of the population genome that is assumed
598 not to vary between traits. The derivation involves the ratio of the genetic variances in the
599 validation set and the training set (see Daetwyler et al., 2008), which is 1 when the training
600 set and validation set are random samples from the same population. This can be modified for
601 a selected training set and randomly sampled validation set with the outcome $r_p^2 =$
602 $h^2 \lambda^* (\lambda^* + 1)^{-1}$ where $\lambda^* = nh^{*2}/M_e$ and $h^{*2} = h^2 \text{var}(g^*)/\text{var}(g)$. Therefore, accuracy is
603 predicted to increase as the genetic variance in the training set increases, a conclusion also
604 reached by Nirea et al. (2012). Let $\delta = \text{var}(g^*)/\text{var}(g)$. Daetwyler et al. (2008) explored
605 selection arising from case-control studies but directional or divergent selection on phenotype
606 can also be incorporated. For directional truncation selection, and assuming a normal
607 distribution, $\delta = (1 - k_q h^2)$ where $k_q = i_q (i_q - x_q)$ with i_q the intensity of selection and
608 x_q is the truncation point for $N(0,1)$ for the selection proportion q (Bulmer, 1971). For
609 divergent selection with selection proportion q (assumed $q/2$ upper and lower tail) there are
610 2 sources of genetic variance, between groups and within groups and the total variance is
611 their sum. Within groups the genetic variance is $\text{var}(g) = (1 - k_{q/2} h^2)$ as previously, and
612 between groups is $\text{var}(g) i_{q/2}^2 h^2$, giving the result $\delta = (1 + i_{q/2} x_{q/2} h^2)$ for divergent
613 selection.

614 The prediction accuracy for r_p contains the unknown M_e but the dependence on the selection
615 can be examined by considering $r_p^{-2} = (1/h^2)(1 + \lambda^{*-1})$ which is a linear regression on
616 $(n\delta)^{-1}$ with a slope dependent on h^2 and M_e and intercept inversely related to h^2 . As an

617 example for divergent selection with $q = 1/2$: $x_{q/2} = 0.674$, $i_{q/2} = 1.271$, and $\delta = 1.472$ for

618 $h^2 = 0.55$.

620 **Table 1** Strategies for cow selective genotyping with the number of cows in the reference
 621 population.¹

Scenario	Selection strategy for cows	Cows genotyped (%) ²	Number of cows in the reference population	
			Yield traits	Calving interval
1	None	0	0	0
2		100	1176	893
3	Random	50	588	446
4	Extreme values in upper tail within each trait	50	588	446
5	Extreme values in either tail within each trait	50	588	446
6		40	470	357
7		30	392	268
8	Extreme values from either tail for corrected milk yield	50	588	446
9	Extreme values from either tail for PLI	50	588	446
10	Extreme values from either tail for GMI	50	588	446

622 ¹For divergent selection using either tail, selection is assumed to be equally divided between
 623 the tails.

624 ²From all the cows 10% were used for the purpose of validation and the rest were available
 625 for estimating the SNP effects.

626 **Table 2** Correlation, genotype, and allele concordance between true and imputed genotypes
627 over 10-fold cross-validations.

	Between individuals		Between SNP	
	Mean	SD	Mean	SD
Correlation	0.952	0.033	0.945	0.072
Genotype concordance	0.961	0.024	0.961	0.044
Allele concordance	0.980	0.012	0.980	0.024

628

629 **Table 3** The correlation between genomic estimated breeding values and phenotypes using
 630 different methods of prediction. SE are given in parentheses based on the outcomes from the
 631 10 validation sets.

Trait	Method			
	GBLUP (bulls)	GBLUP (bulls + cows)	Bivariate GBLUP	BLUP (bulls + cows)
Milk yield	0.213 (0.030)	0.376 (0.019)	0.376 (0.020)	0.316 (0.025)
Fat yield	0.236 (0.020)	0.347 (0.025)	0.349 (0.024)	0.310 (0.034)
Protein yield	0.210 (0.026)	0.323 (0.027)	0.327 (0.029)	0.291 (0.032)
Calving interval	0.057 (0.029)	0.042 (0.031)	NA ¹	0.018 (0.044)

632 ¹Convergence was not achieved

633

634 **Table 4** The correlation between genomic estimated breeding values and phenotypes from
 635 different scenarios of selecting cows for genotyping using the univariate GBLUP method. SE
 636 are given in parentheses based on the outcomes from the 10 validation sets.

Trait	Scenario ¹					
	2	3	4	5	6	7
Milk yield	0.376 (0.019)	0.322 (0.021)	0.284 (0.029)	0.369 (0.022)	0.364 (0.021)	0.353 (0.022)
Fat yield	0.347 (0.025)	0.314 (0.021)	0.264 (0.020)	0.340 (0.025)	0.333 (0.024)	0.327 (0.024)
Protein yield	0.323 (0.027)	0.287 (0.023)	0.246 (0.026)	0.322 (0.027)	0.316 (0.027)	0.313 (0.028)
Calving interval	0.042 (0.031)	0.043 (0.032)	0.049 (0.027)	0.040 (0.031)	0.046 (0.030)	0.042 (0.031)

637 ¹Scenarios: 2 - all cows; 3 - 50% selected at random; 4 - 50% from upper tail; 5 - 50% from
 638 either tail; 6 - 40% from either tail; 7 - 30% from either tail.

639

640 **Table 5** Correlation between genomic estimated breeding values and phenotypes with
 641 different criterion for divergent selection of 50% of cows for genotyping using the univariate
 642 GBLUP method. SE are given in parentheses based on the outcomes from the 10 validation
 643 sets.

Trait	Scenario ¹				
	3	5	8	9	10
Milk yield	0.322 (0.021)	0.369 (0.022)	0.369 (0.022)	0.338 (0.028)	0.354 (0.015)
Fat yield	0.314 (0.021)	0.340 (0.025)	0.336 (0.026)	0.328 (0.022)	0.342 (0.013)
Protein yield	0.287 (0.023)	0.322 (0.027)	0.331 (0.016)	0.316 (0.028)	0.326 (0.014)
Calving interval	0.043 (0.032)	0.040 (0.031)	0.051 (0.026)	0.055 (0.032)	0.045 (0.045)

644 ¹Scenarios: 3 - at random; 5 - from either tail for the same trait as the genomic EBV; 8 - from
 645 either tail for milk yield; 9 - from either tail for PLI; 10 - from either tail for GMI.

646

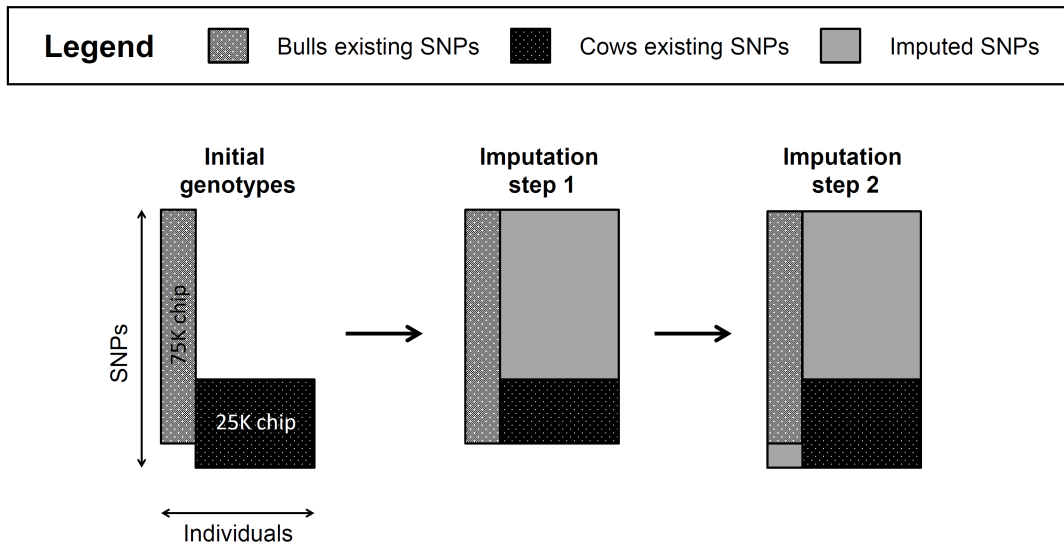
647 **Table 6** Bias expressed as slope of the regression of phenotypes on genomic EBV from
 648 different scenarios of selecting cows for genotyping using the univariate GBLUP method. SE
 649 are given in parentheses based on the outcomes from the 10 validation sets.

Trait	Scenario ¹				
	1	2	3	4	5
Milk yield	0.829 (0.124)	1.081 (0.076)	1.065 (0.099)	0.838 (0.106)	0.890 (0.066)
Fat yield	0.774 (0.066)	1.023 (0.083)	1.011 (0.073)	0.726 (0.063)	0.935 (0.077)
Protein yield	0.840 (0.102)	1.018 (0.102)	1.006 (0.101)	0.726 (0.089)	0.915 (0.088)
Calving interval	1.539 (0.802)	2.300 (1.541)	2.056 (1.556)	2.095 (1.217)	3.390 (2.544)

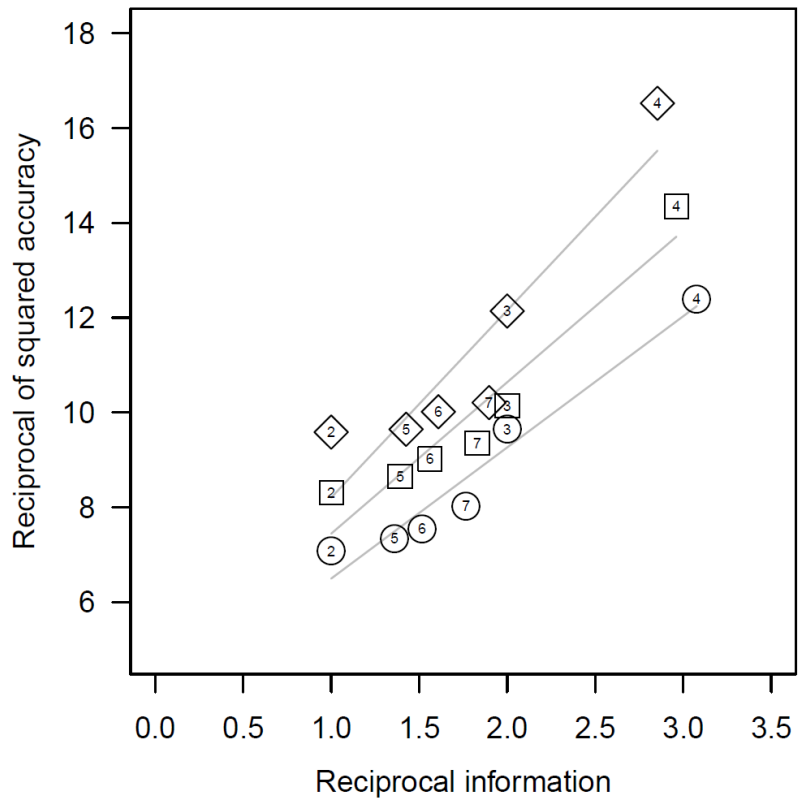
650 ¹Scenarios: 1 - only bulls; 2 - all cows; 3 - 50% selected at random; 4 - 50% from upper tail;
 651 5 - 50% from either tail.

652

FIGURES



Jenko et al., Figure 1



656

657

Jenko et al., Figure 2

658 Figure 1. The 2-step process used for imputation of individuals up to the 75K chip, which
659 was necessitated by a subset of the SNP loci appearing only on the 25K chip.

660

661 Figure 2. The relationship of the reciprocal squared accuracy for predicting phenotypes (r_p^{-2})
662 of milk yield, fat yield, and protein yield for scenarios 2 to 7 inclusive with the reciprocal of
663 information $((n\delta)^{-1}$, see Appendix B), together with their linear trend lines. Milk yield, fat
664 yield, and protein yield are shown with circle, square, and diamond symbols, respectively.
665 The values of n used were 1, 0.5, 0.5, 0.5, 0.4, and 0.3 for scenarios 2 to 7 respectively; $\delta = 1$
666 for scenarios 2 and 3, but depend on the heritability of the trait for all others. For all traits the
667 order of scenarios on the x-axis is (2, 5, 6, 7, 3, and 4).