

Purdue University Purdue e-Pubs

International Compressor Engineering Conference

School of Mechanical Engineering

2012

Simulation Analysis of a Two Rolling Piston Expander Replacing Throttling Valve in Conventional Refrigerant Heat Pump System

Li Zhao yoouer@tju.edu.cn

Minxia Li

Yitai Ma

Zhongyan Liu

Follow this and additional works at: http://docs.lib.purdue.edu/icec

Zhao, Li; Li, Minxia; Ma, Yitai; and Liu, Zhongyan, "Simulation Analysis of a Two Rolling Piston Expander Replacing Throttling Valve in Conventional Refrigerant Heat Pump System" (2012). *International Compressor Engineering Conference*. Paper 2100. http://docs.lib.purdue.edu/icec/2100

Complete proceedings may be acquired in print and on CD-ROM directly from the Ray W. Herrick Laboratories at https://engineering.purdue.edu/ Herrick/Events/orderlit.html

This document has been made available through Purdue e-Pubs, a service of the Purdue University Libraries. Please contact epubs@purdue.edu for additional information.

Simulation analysis of a two rolling piston expander replacing a throttling valve in a conventional refrigerant heat pump system

ZhaoLi¹, LiMinxia¹*, MaYitai¹, LiuZhongyan¹

¹Key Laboratory of Medium-Low Temperature Energy Efficient Utilization of Ministry of Education, Department of Thermal Engineering, Tianjin University, Tianjin, China *022-27890041, 022-87401539, tjmxli@tju.edu.cn

ABSTRACT

An expander is employed to replace a throttling valve in a heat pump system of the conventional refrigerant in order to further improve the efficiency of the system by recovering partial expansion work to decrease energy consume of the system. Due to large expansion ratios of conventional refrigerants, a two-rolling piston one-stage expander was proposed and designed. Simulation analysis was developed by analyzing irreversible losses in the expansion work process. The simulation results show that, friction losses of a conventional refrigerant expander are 80.2% of total losses, which are the main factors to influence the efficiency of expander. Then the measures of reducing friction losses are presented, which would be expected to improve the expander efficiency efficiently.

1. INTRODUCTION

In recent years, refrigeration and heat pump units have been widely applied in China with the development of national economy and improvement of people's living standards, which also led to huge energy consumption simultaneously. Under the background of global energy shortage, it is of great importance to heighten system efficiency to save energy and meet the increasingly stringent national energy efficiency standards.

Many efficient efforts have been investigated to improve system efficiency, including the design and analysis of cycle principle, high efficient compressors (screw, centrifugal etc.), throttle mechanism, high efficient heat exchanger etc[N. Stosic, 2003]. For example, isentropic efficiency of a medium-sized compressor by optimizing study can be higher than 80%[DORIN, 2011]. The heat transfer coefficient of a plate heat exchanger can reach up to 2000W/(m²·K)[Anjun Li, 2008]. And the control of system has been described to be close to perfect[Craig CordelL, 2003]. While, in comparison with those designations, expansion part is to be considered less[Yitai Ma, 2008].

Based on the thermodynamic calculation of R22 cycle COPs (coefficient of performance) of a system with various efficiency of expander are shown in Figure 1. The calculation condition is that the evaporation temperature and condensation temperature are 7.2°C/54.4°C, with a superheat and supercooling of 11.1 $^{\circ}C/8.3^{\circ}C$. When the expander efficiency reaches 50%, the COP of a system with an expander can get an amplification of 6.84% compared with the system with a throttling valve, and the recovering work of expander is equal to 5.03% of input work of a compressor. When the expander efficiency reaches 70%, the system COP increases by 9.79% and the expander recovering work is equivalent to 7.05%, of input work of a compressor. Therefore, using an expander to replace a throttling



Figure 1 variations of system COP and expansion work ratio to expander efficiency

valve can improve COP of a refrigeration system. The key technology is to develop a high-efficient expander.

The expansion ratios of traditional refrigerants are 20-30 in common and are much larger than compression ratio. The structure of an expander with such large expansion ratio is difficult to design. Considering the large expansion ratio of conventional refrigerants, authors considered that a two-rolling piston expander is proper type

expander to develop, which is proposed by some researchers (Katsumi et al. 2006) for a CO_2 expander. In this paper, theoretical analysis and simulation calculation was carried out to investigate internal losses of conventional refrigerant expander in order to find the main factors which affect the efficiency of expander.

2. BRIEF INTRODUCTION OF TWO-ROLLING PISTON EXPANDER

2.1 Structure of Expander

A two-rolling piston expander of conventional refrigerant is equivalent to two sets of single rolling piston expander system, each of which includes a slide, a rolling piston, a cylinder, a eccentric wheel etc[Ma Guoyuan, 2003]. Its basic structure is shown in Figure 2. The left side is the first stage cylinder system, and the right is the second stage. There is an angle between two slides. A connecting pipe connects the outlet of first stage cylinder and the inlet of second stage cylinder. The first stage cylinder acts as an inlet control device. As the first stage cylinder is always connected with inlet pipe, the inside pressure fluctuation can be reduced, and the pressure during inlet process is stable. When the first stage piston rotates one circle, a suction process ends. Meanwhile, the fluid begins to expand. Expansion process completes when the second stage piston rotates to the outlet. The second rolling piston continues to run one circle to accomplish the exhaust process. Therefore, in order to complete one work cycle, the first rolling piston whirls one circle and the second rolling piston whirls two circles. The two-rolling piston one-stage expansion structure is one of effective methods to solve large expansion ratio of conventional refrigerant.



Figure 2 Conventional refrigerant two-rolling piston expander1-cylinder2-rolling piston3-eccentric wheel4-slide5-connecting pipe6-inlet port7-outlet port8-cylinder wallα-end of inlet angleβ-start of outlet angle

2.2 Movement Characteristics of Expander

There are some characteristic angles of expander, including: $1\alpha_i$: the inlet rear edge angle of the first cylinder, $2\beta_i$: the outlet front edge angle of the first cylinder, $3\alpha_i$: the inlet rear edge angle of the second cylinder, $4\beta_i$: the outlet front edge angle of the second cylinder, $5\alpha_i$: the angle between two slides, 6δ : the sharing angle of inlet channel. The inlet and outlet angles are shown in Figure 2.

This expander is equivalent to two sets of expander system, and the movements are more complicated. A complete working cycle includes suction process, expansion process and exhaust process. Base on that, the movements of expander have been analyzed and diagramed as shown in Figure 3.

In Figure 3(a), the rotation angle is $(\alpha_1-\delta)$, which represents the begin of suction process of the 1st cylinder of this cycle.

In Figure 3(b), the rotation angle is $(360-\beta_1)$. At this moment, the connecting pipe begins to connect the working chambers of two cylinders and the suction process of 2^{nd} cylinder of this cycle begins.



Figure 3 movements of the conventional refrigerant expander

In Figure 3(c), the rotation angle is $(360+\alpha_1)$. Right now, the whole suction process finishes, and the expansion process begins.

In Figure 3(d), the rotation angle is $(720-\beta_2-\alpha)$, which represents the finish of expansion process and the start of exhaust process of this cycle.

In Figure 3(e), the rotation angle is $(1080-\beta_2-\alpha)$, which represents the finish of whole exhaust process of this cycle. At this moment, a whole working process has been completed.

In Figure 3(f), the rotation angle is (1080- β_1), which represents the start of suction process of the 2nd cylinder of the next cycle. The next working process is going on.

2.3 P-V Diagram of the Ideal Expansion Process

Considering the ideal expansion process, the variation of pressure and volume in working chamber is shown in Figure 4. Figure 4 shows the whole working process of expander. During the suction process, pressure keeps constant, when the piston run around one



volume in working chamber of ideal expansion process

circle, the expansion process starts, the pressure decreases quickly with the increase of volume. The area enclosed by the curve is the ideal expansion work of the expander.

3. FORCE ANALYSIS OF EXPANDER MAIN COMPONENTS

The main components of expander include a slide (sliding valve), a rolling piston, and an eccentric wheel. In the calculation of the friction losses of expander, frictions between main components are considered through the force analysis.

Basing on the reference of Rotary compressor[Ma Guoyuan, 2003], forces and pressure distributions on a slide is shown in Figure 5. Forces on the slide include: 1)the elastic force F_k of spring at the end of slide, which's direction is along the slide centerline to cylinder center; 2)the inertial force F_{iv} , representing the resultant force of slide;3)positive pressure F_{rl} , F_{r2} on both sides of slide and the friction F_{rtl} , F_{rt2} between the slide and slide grooves, in which friction is opposite to the moving direction of slide, and change to the reverse every 180 degrees of rolling piston; 4)positive pressure and friction force between slide and rolling piston, in which positive pressure Fs is along the connect line of connect point(slide end and rolling piston) and rolling piston center pointing to slide, while friction force F_t is opposite to the speed direction of connect point; 5)differential pressure force F_c at both ends of slide and 6)force F_h on the part of slide which inserted into cylinder caused by pressure difference between the suction chamber and expansion chamber. The direction of this force points to low pressure side from high pressure side.



Figure 5 force analysis diagram of slide

Figure 6 leakage analysis within expander

4. LOSSES ANALYSIS IN EXPANSION PROCESS

4.1 Friction Losses of Expander

On base of the relative moving components of expander, the friction losses of conventional refrigerant expander include: $1)L_1$, the loss between main shaft and bearing, $2)L_2$, the loss between eccentric wheel and cylinder end covers, $3)L_3$, the loss between eccentric wheel and rolling piston, 4) L_4 , the loss between rolling piston and cylinder wall, 5) L_5 , L_6 , the loss between rolling piston and the upper and lower end caps of cylinder, 6) L_7 , the loss between rolling piston and slide and 7) L_8 , the loss between slide and slide grooves.

So, all friction losses of cylinder are:

$$W_{fric} = L_1 + L_2 + L_3 + L_4 + L_5 + L_6 + L_7 + L_8 \tag{1}$$

4.2 Leakage Losses of Expander

According to the relative motion between components during expansion process, leakage positions can be obtained, which mainly include 1)gap between slide and slide groove δ_1 , 2)gap between the two sides of slide and cylinder end covers (referred as slide side gap) δ_2 , 3)gap between rolling piston outer surface and cylinder inner wall of the cut point (referred as radial gap) δ_3 , 4)gap between rolling piston and cylinder end covers (referred as end face gap) δ_4 , and 5)gap between slide end and rolling piston δ_5 , as shown in Figure 6.

In general, as the position of slide and slide grooves are relatively fixed, the gaps δ_1 between them do not vary with external environment, and can be treated as fixed clearances. Slide side gap, δ_2 , *results* in leakage between two working chambers, and gas refrigerant leaks from high pressure chamber to low pressure chamber through this gap. In addition, radial gap, δ_3 , changes slightly with the rotation of rolling piston. The existence of this gap causes the gas refrigerant leaking from high pressure working chamber to low pressure chamber. Rolling piston

end gap, δ_4 , may cause lubricant leakage within the bearing leaking to the working chamber. This gap changes little and is considered as a fixed value in the calculation. At the contact of slide and rolling piston, δ_5 , existing lubricant film can decrease the leakage greatly, which means the leakage there is very small and can be ignored. The expander leakage characteristics are shown in Table 1.

Table 1 leakage characteristics of different gaps					
Leakage rate	Leakage gap	Gap characteristics	Leakage characteristics	leakage model	
m_1	Gap between slide and slide grooves δ_1	Fixed gap	Mainly lubrication oil	Liquid leakage model	
\dot{m}_2	Slide side gap δ_2	Fixed gap	Mainly gas refrigerant	Gas leakage model	
\dot{m}_3	Racial gap δ_3	Change with the moving of rolling piston	Mainly gas refrigerant	Gas leakage model	
m_4	End face gap δ_4	Fixed gap	Mainly lubrication oil	Gas leakage model	
m_5	Gap between slide and rolling piston δ_5	Small, can be ignored	Mainly gas refrigerant	Liquid leakage model	

The leakage rate of liquid leakage model is:

$$m = \left(\frac{\Delta p \delta^3}{12\mu l} + \frac{1}{2} v_x \delta\right) H \rho_0 \tag{2}$$

The leakage rate of gas leakage model is:

$$m = \varphi_0 A g \tag{3}$$

$$g(p_{in}, \rho_{in}, \rho_{out}) = \begin{cases} \sqrt{p_{in} \rho_{in} \left(\frac{2}{k+1}\right)^{\frac{k+1}{k-1}}} & \left(\frac{p_{out}}{p_{in}}\right) < \left(\frac{2}{k+1}\right)^{\frac{k}{k-1}} & \left(\frac{2}{k+1}\right)^{\frac{k$$

The leakage mass flow rates can be calculated through corresponding model. The corresponding leakage losses are generally caused by enthalpy changes. So, the leakage loss is the product of leakage mass flow rate and enthalpy difference. And the total leakage loss is:

$$W_{leak} = LL_1 + LL_2 + LL_3 + LL_4 + LL_5$$
(5)

4.3 Other Losses of Expander

For a rolling piston expander, when a exhaust process is completed and rolling piston turns over the outlet port, a small amount of refrigerant between rolling piston and slide cannot be discharged completely, which would do negative work to expander. In the design of an expander, it is necessary to adjust the angle between discharge point and the slide to make it as small as possible to get smaller clearance volume loss.

In addition, the connection pipe would be filled with working fluid all the time, while a part of refrigerant in this pipe cannot be discharged. The size and length of connection pipe is designed based on the location of two cylinders. And it cannot be too short or small for the probably throttling loss.

4.4 The Total Losses and Efficiency Calculations of Expander

Above all, the expander losses W_t is:

$$W_t = W_{fric} + W_{leak} + W_{else} \tag{6}$$

Expander adiabatic efficiency η can be calculated as follows:

$$\eta = \frac{W_e - W_t}{W_e} \tag{7}$$

International Compressor Engineering Conference at Purdue, July 16-19, 2012

Where, W_e represents the ideal recovering power (W), W_{else} is other losses (W).

5. SIMULATION RESULTS AND ANALYSIS

The simulation involves the suction and expansion process of a R22 expander. The inlet and outlet condition of expander is 40° C/1.53MPa and 0° C/0.498MPa. The radius and height of two cylinders are 55.5/28mm and 82.5/107mm. And the eccentricity of two cylinders is 4.4/11mm.

5.1 Friction Losses of Expander

Figure 7 shows the variations of friction forces against rotation angle of two slides. The first slide suffers less friction force, while the second slide suffers more. To the first slide, friction forces between slide and slide grooves F_{rt1} , F_{rt2} change in the range of 2N, and that between slide and rolling piston F_t changes within 5N. To the second slide, friction force between slide and rolling piston F_t has a maximum of 800N. Friction force between slide and the right slide groove F_{rt2} is within the range of 200~400N, and differs large to the force between slide and the left groove F_{rt1} , which mainly results from the rotation direction of rolling piston(clockwise). In addition, the breakpoints at 180° in Figure 6 are caused by the moving direction change of slide.



Figure 8 and Figure 9 are the changes of friction losses with rotation angle of two cylinders respectively. Besides the fixed losses of bearings, the larger share of friction losses distributes between slide and rolling piston L_7 and between slide and slide grooves L_8 . As the moving direction change of slide at 180° and the beginning of expansion process at 52°, relative turning points appeared in the figures.



In the first cylinder, maximum friction loss between a slide and slide grooves reaches 1.5W, and that between the slide and the rolling piston gets 5.2W. Besides, friction loss caused by the movement between main shaft and bearings, that between eccentric wheel and cylinder end covers, and that between eccentric wheel and rolling

piston are fixed values of 5.0W, 6.4W, 2.4W respectively. The total friction loss of first cylinder is less then 20W.

In the second cylinder, maximum friction loss between slide and slide grooves is of 1.01KW, and that between slide and rolling piston gets 1.8KW, which are caused by the large friction forces on them. In addition, friction losses between main shaft and bearings, that between eccentric wheel and cylinder end covers, and that between eccentric wheel and rolling piston are 0.1KW, 54W, 11W respectively. While losses in other parts are close to zero.



Base on the above, proportions of different friction losses to the total friction losses can be obtained, as shown in Table 2. It is obvious that the friction losses between slide and slide grooves and that between slide and rolling piston are large. Among them, the friction loss between slide and rolling piston of second cylinder is about 65.9% of the total friction losses, which means that reducing this part of loss would significantly improve expander efficiency.

Desition of function loss	First cylinder		Second cylinder	
Position of friction loss	Loss (W)	Proportion (%)	Loss (W)	Proportion(%)
Between main shaft and bearings	5.02	19.3	107.4	6.02
Between eccentric shaft and cylinder end covers	6.27	24.1	29.59	1.66
Between eccentric shaft and rolling piston	2.53	9.74	53.28	2.99
Between rolling piston and inner cylinder	0.512	1.97	13.64	0.764
Between rolling piston and lower end cover	0.120	0.462	8.345	0.468
Between rolling piston and upper end cover	0.193	0.743	14.63	0.820
Between rolling piston and slide	7.62	29.3	1175.9	65.9
between slide and slide grooves	3.71	14.3	382.1	21.4
The total friction losses	25.98	100	1784.9	100

Table 2 proportions of different friction losses to the total friction losses

5.2 Leakage Losses of Expander

Figure 10 is the changes of leakage rates with rotation angle of first cylinder. The leakage rates of first cylinder are small. Among them, leakage rate between rolling piston and inner cylinder m_3 is larger, which have a maximum of 0.0072kg/s and almost linear decrease with the increase of rotation angle.

Figure 11 is the changes of leakage rates with rotation angle of second cylinder. The leakage rates between

rolling piston and inner cylinder is larger. That leakage rate mainly results from the changes of pressure in expansion chamber and gets a maximum at the beginning of expansion process(52°) as the maximum pressure difference of two working chambers. And rapidly decrease with the increase of rotation angle occurs till about 150°, and then its decline begins to be smooth, and gradually close to zero, which is mainly caused by the changes of pressure in expansion chamber. The leakage rate of end face gap, m_4 , increases greatly from the beginning of expansion process to 120° and then change gently to 280° where get a slight increase. The maximum of that leakage rate is 0.018kg/s. The leakage through the gap between slide and slide grooves from back pressure chamber, m_1 , also increases with the increase of rotation angle, and has a maximum leakage rate of 0.015kg/s. In addition, the leakage rate through slide side gap decreases with the pressure difference of two chambers, and gets a maximum rate of 0.0023kg/s at the beginning of expansion process.



rotation angle of first cylinder

rotation angle of second cylinder

Figure 12 is the changes of leakage losses with rotation angle of two cylinders. For the first cylinder, the mainly loss is caused by racial gap, and is within 1W. This is also the reason why the pressure changes little in the working chamber of first cylinder. For the second cylinder, the site of main loss is also through racial gap, and its biggest loss is close to 80W, which reduces rapidly with the increase of rotation angle. This part of leakage is caused by the pressure difference between expansion chamber and discharge chamber, which gradually reduces during the expansion process. The leakage loss through gap between slide and slide grooves and end face gap change similarly. And that of slide side gap keeps constant and its value is also small.



As shown in Table 3, the proportion of leakage losses to the total leakage losses is cleared up. Leakage loss caused by racial gap is serious both in two cylinders.

Position of lookage loss	First cylinder		Second cylinder	
r osition of leakage loss	Loss (W)	Proportion (%)	Loss (W)	Proportion (%)
Gap between slide and slide grooves	0.00746	1.12	72.05	21.0
Slide side gap	0.00562	0.845	28.85	8.39
Racial gap	0.481	72.3	142.5	41.4
End face gap	0.171	25.7	100.4	29.2
The total leakage losses	0.665	100	343.8	100

Table 3 proportion of leakage losses to the total leakage losses

5.3 Discussions on Expander Efficiency

The total losses and expander efficiency are shown in Table 4. The simulation calculated expander efficiency is 48.5%. From Table 4 it can be seen obviously, that the friction loss is a very important factor affecting expander efficiency. The friction loss takes 41.3% of total ideal expansion work and about 80% of total losses.

item	value (W)	proportion (%)
Ideal expansion work	4188.0	100
Total loss	2156.0	51.5
Friction loss	1728.4	41.3
Leakage loss	344.47	8.23
Other irreversible losses	83.762	2.00
Real recover work	2032.0	48.5

Through the above analysis and simulation calculation, we find that the friction loss is about 41.3% of ideal expansion recovery work, while leakage loss and other irreversible loss are relatively small. To improve expander efficiency, reducing the friction losses between slide and piston and between slide and slide grooves are the key. The followings are some practical methods applied in the expander to reduce friction losses.

In order to decrease the friction loss caused by the movement between slide and slide grooves, rolling-needles are considered to add to join the slide and slide grooves which would change sliding friction to rolling friction and reduce their friction and friction loss. As rolling friction coefficient is far less then sliding friction coefficient and rolling-needles are lubricated well, the friction loss between slide and slide grooves could be decreased by 90.4%. For the decreasing of the friction loss between slide and rolling piston, the mainly measure is to improve the end part of slide, and make it to have well lubrication and sealing. Then, the friction loss of this part is decreased by 67.8%. Lubrication between these components has a good work to reduce this loss, It is considered that a designed independent lubrication system of expander can improve the lubrication of main shaft, piston, eccentric wheel and other parts and the friction losses between these parts have a certain extent diminution separately. In final, the total friction losses now can be decreased by 63.7% compared with the previous value in Table 4.

In addition, in order to improve the sealing of expander, O-ring seal can be used to reduce expander external leakage and a higher machining accuracy can help to control the internal leakage. And these measures could decrease the leakage losses by 20% at least.

So, after these efficient measures, the expander efficiency could be increased greatly and has a theoretical value of 76.0%.

6. CONCLUSIONS

1. A two-rolling piston one-stage expander has been designed to fit for the large expansion ratio of conventional refrigerants. Besides, this structure can eliminate an additional suction control system and is able to ensure the inlet pressure stability.

2. Irreversible losses analysis and simulation calculates have been carried out by analyzing the moving parts of expander,. The results show that friction losses are accounting for about 80.2% of the total expander losses, and leakage losses are about 16.0%.

3. Improvement measures were discussed which would be efficient to improve expander efficiency. The friction losses decrease by 63.7%, and the simulation calculated expander efficiency increase greatly to 76.0%.

NOMENCLATURE

The nomenclature referred in this paper is shown in the following:

α	end of inlet angle	(°)	Subscripts	
β	start of outlet angle	(°)	1	the first cylinder
δ	sharing angle of inlet channel/the leakage gap	(°/m)	2	the second cylinder
ρ	density	$(kg \cdot m^{-3})$	in	the inlet status
m	leakage rate	$(kg \cdot s^{-1})$	out	the outlet status
W	power	$(W/J \cdot s^{-1})$		
F	force	(N)		
m	leakage rate	$(kg \cdot s^{-1})$		
W	power	$(W/J \cdot s^{-1})$		
k	adiabatic coefficient	(-)		

REFERENCES

N. Stosic, I. K. Smith, A. Kovacevic. Optimization of screw compressors. Applied Thermal Engineering. 2003,23(10):1177-1195

DORIN, DANFOSS, BITZER. The menu of compressor products

- Yitai Ma etc. The current situation and development of the refrigeration and air conditioning energy efficiency standards of China. Refrigeration and Air Conditioning. 2008,8(3):5-11
- Anjun Li, Guiju Xing, Liwen Zhou. The research on enhancement technology of heat changer. Energy for Metallurgical Industry. 2008,27(1):50-54
- Craig Cordell. ASHRAE Presentation-Modern Refrigeration Controls. ASHRAE SEMINAR of 2003, Chicago
- Katsumi Sakitani, Michio Moriwaki, Masakazu Okamoto, et al. Development of two-phase flow expander for CO₂ heat pump and air-conditioners[C], Proceeding of International Heat Pump Conference in 2006, Alaska, U.S.A.

Ma Guoyuan, Li Hongqi. Rotary compressor. Beijing: machine industrial publishor.2003

ACKNOWLEDGEMENT

This study was sponsored by the project 51076111of National Science Fund of China.