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Sunil K. Agrawal<br>University of Windsor

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## SUNIL K. AGRAWAL, B.E., M.E.

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## TO MY PARENTS, SUSHMA AND SHIVANI

## ABSTRACT

A modified approach to design various treatment units handing particles in suspension or in settled form in water and wastewater treatment is proposed. The recommended method of design is based on the concept of critical shear stress. It is shown that the design of different treatment units based on critical shear stress is more rational and can be used to optimize the performance of the units.

This study was conducted in four parts. The first part consisted of the experiments on different sizes of grit and gravel particles in a laboratory flume to obtain the critical bed shear stress necessary to initiate the motion. Grit samples, collected from the West Windsor Pollution Control plant were washed and sieved. Some larger gravel particles were included also in the study. The information gathered through these experiments have been used to determine the minimum bed shear stresses required in various water and wastewater treatment units, where the deposition of inert particles is undesirable. These critical bed shear stress values can also be used to design treatment units, where the deposition of inert particles is desired.

In the second part critical bed shear stresses, necessary to initiate the motion of different types of sludge
particles in the laboratory flume, were obtained. Sludge samples were collected from water and wastewater treatment plants in Windsor, Amherstburg and Chatham. Five different types of sludge samples were analyzed; biological wastewater sludge, physico-chemical wastewater sludge, alum sludge from water treatment plant, secondary digested sludge and a mixture of primary and secondary biological sludge. These experiments allowed a determination of the minimum shear stress required in various water and wastewater treatment units where the deposition of these sludge particles is undesirable.

The third part was concerned with the rheological properties of all five types of sludges, both before and after settling. The yield stress values obtained in the laboratory using viscosity meters are recommended for use in the design of treatment units where the settling and shearing of sludge particles or flocs is not permitted. The value of yield stress is the maximum shear that can be allowed in a treatment unit or in a mixing chamber without breaking the flocs or particles and also keeping them in suspension.

In the fourth part an empirical model of an aeration tank was formulated based on the actual experimental velocity distribution data. The horizontal velocities at different depths in an aeration tank were measured under a range of different operating conditions. The developed model is based
on the horizontal velocity, 25 mm above the tank bottom, under different operating conditions such as air flow rate, diffuser submergence, liquid depth and tank width. The information on horizontal velocites close to the tank bottom is important in the design of an aeration tank in which the settling of floc particles is not allowed.

Typical applications of the proposed design methods are presented. These methods can be used in the design of grit chambers, both conventional and aerated, storm and sanitary sewers, flocculation chambers, settling tanks, aeration tanks and mixing chambers.

## ACKNOWLEDGEMENTS

The author expresses his heartful gratitude to his advisor, Dr. J. K. Bewtra. He, with his continued guidance, generous financial support, untiring efforts and constructive input provided much needed encouragement during the completion of this work.

The author is also extremely grateful to Dr. J. A. McCorquodale, for his invaluable advice in the completion of this work. Acknowledgements are also due to Dr. Carl C. St. Pierre, Dr. S.P. Chee, and Dr. N. Biswas for their input in this research.

Special thanks go to Dr. D. Dekee for his advice on the flow behaviour of non-Newtonian fluids and allowing me to use his equipment for the analysis work.

Thanks are due to Frank Kiss for his help in setting up the lab for experimental work. Thanks also to all unmentioned friends who provided much needed help during this research.

The author would also like to acknowledge Erica Berndt for her assistance in putting this thesis together and to Rama Rao v. Cherukuri for his support and encouragement during the final stages of this work.

Acknowledgement is also due to the Natural Science and Engineering Research Council of Canada for their financial assistance for this research.

Finally, many thanks go to my wife Sushma for her moral support and patience throughout the completion of this work.

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## Chapter I

## INTRODUCTION

### 1.1 General

Both raw water and wastewaters contain settleable and suspended particles with different settling characteristics. In certain treatment units, these particles are removed by gravity, with or without the use of chemical coagulants, whereas in some other units, it becomes necessary to keep these particles in suspension. For example, the grit Chambers are designed to remove only the inert grit particles from the wastewater while keeping the decomposable organic solids in suspension, whereas the sedimentation tanks are designed to remove all the settleable particles. On the other hand, mixing chambers, flocculators and aeration tanks are designed to keep such particles and flocs in suspension all the time.

Air agitated tanks and channels are among the most power consuming units in water and wastewaters treatment plants. The diffused air in these treatment units serves one or more of the following functions:

1. Mix the contents of the tank
2. Provide dissolved oxygen to satisfy biological and/or chemical oxygen demands
3. Provide sufficient circulating velocities to keep the settleable flocs or particles in suspension
4. Allow heavier inert particles to settle while keeping the lighter organic particles in suspension

Although a great deal of field and laboratory data are available on the design of mechanically agitated tanks, the information available on the design of air agitated tanks and channels is limited. Most of the research work with air agitated tanks has been directed towards mass transfer of oxygen and air requirement to satisfy biological and/or chemical oxygen demand. Only a limited amount of information is available on the air requirement to keep the particles in suspension under specified conditions or to allow heavier particles to settle while keeping lighter particles in suspension.

It has been reported [103] that, in aeration tanks for conventional domestic wastewater treatment plants, the amount of air required to keep the floc in suspension is higher than that needed to satisfy biochemical oxygen demand, BOD. Thus, if the aeration tank is designed to keep the flocs in suspension all the time, then the oxygen demand would also be satisfied. However, most of designs have been based mainly on oxygen requirement. It should be recognized that while keeping the floc in suspension in an aeration tank, it should not be sheared to an extent that it would not settle efficiently in the settling tank.

### 1.2 Objectives

The purpose of this research was to develop a better approach for the design of various treatment units which handle particles in suspension or in settled form in water and wastewater treatment practices. The modified method for the design is based on the concept of critical shear stresses required to initiate particle motion and on yield stresses. This research was divided into four parts:

1. Determine the scouring velocities for different sizes of grit particles in a flume in order to calculate the shear stress required to initiate the motion of particles and use this information in the design of both conventional and aerated grit chambers.
2. Determine the scouring velocities for different types of sludge particles in a flume in order to calculate the minimum shear stress required in an aeration unit to prevent settling of particles.
3. Determine the yield stress of different types of sludges to obtain the upper limit for shear stress that can be permitted in an aeration unit without shearing the floc.
4. Develop a model to predict horizontal velocity near the bottom of an aeration tank under different operating conditions.

## Chapter II

## IITERATURE REVIEW AND HISTORICAL BACKGROUND

### 2.1 Aeration Process

### 2.1.1 General

The aeration process is of great importance for its wide range of applications in the treatment of water and wastewaters. Diffused air is used most widely in the aeration basins, but it is also used in grit chambers, equalization basins, aerated lagoons, air stripping columns, and mixing chambers. Raw wastewaters are often aerated for short periods prior to conventional treatment to increase the efficiency of subsequent operations. Flotation with air is used for grease removal. Aeration is also used for flocculation purposes in the wastewater treatment. Recently, there has been renewed interest in the potentialities of forced instream aeration as a supplemental means for water quality control [96] ${ }^{\text {l }}$.

[^0]
### 2.1.2 Preaeration Basins

A careful study and review of the subject of preaeration reveals that, despite its versatile, extentive and beneficial use, probably no other single step of modern sewage treatment practice has received so little attention [74]. Preaeration is defined by the Glossary-Water and Wastewater Control Engineering [37] as 'a preparatory treatment of wastewater consisting of aeration to remove gases, add oxygen, promote flotation of grease, and aid coagulation'.

Early use of preaeration of raw sewage was for the purpose of odor control and/or prevention of septicity. Generally short aeration periods, ranging from 15 min. down to less than 1 min., were used. Additional benefits of grease separation and flocculation of solids became evident as the period of aeration was increased. The later benefits now are considered the major objectives of the process. An additional benefit, where the preaeration tank is adjacent to settling units, is to provide uniform distribution of flow and solids to settling tank inlets. Within the last few years preaeration has been used successfully for grit separation and this unit is called an aerated grit chamber.

Obvious benefits of preaeration, as reported by consulting engineers and plant operators, can be summarized as follows [42]:

1. Increase in reduction of $B O D$ and suspended solids in primary treatment units
2. Increase in grease removal in primary treatment units
3. Sweetening of stale sewage
4. Reduction of odors
5. Prevention of septic primary tanks during periods of low flow
6. Treatment of digester supernatant
7. Improved flocculation for chemical precipitation
8. Removal of undesirable gases from the wastewaters

Preaeration of raw wastewater is normally practised prior to primary sedimentation unit. The detention period in preaeration basins is generally less than 20 min. [92].

Hatfield [40] discussed the operation of preaeration unit at Decatur, IL in 1931. The results of two years of study and testing indicated that 2.5 hours aeration could reduce the BOD from $30-40$ percent and that the settled, aerated effluent could be successfully applied to trickling filters at three times the rate of unaerated sewage. Currie [19] discussed the improvement in the performance of several sewage treatment plants in the United States, after preaeration was introduced in the process and followed by primary sedimentation unit.

The design criteria and air requirement for preaeration basins, suggested by different researchers, are given in Table 2.1. It is expected that these air flow rates will

```
both satisfy the oxygen demand and prevent the particles
from settling.
```

Table 2.1 - DESIGN CRITERIA FOR PREAERATION UNITS

| REFERENCE | DESIGN PARAMEIER | RANGE |
| :---: | :---: | :---: |
| Metcalf \& Eddy (60) | Tank depth | 3-6m |
|  | Detention time | 10-45 min. |
|  | Air Requirements | $0.075-0.30 \mathrm{~m}^{3} / \mathrm{m}^{3}$ of wastewater (typical $0.20 \mathrm{~m}^{3} / \mathrm{m}^{3}$ of wastewater) $0.02-0.05 \mathrm{~m}^{3} / \mathrm{min} .-\mathrm{m}$ of length (for aerated channel) |
| Steel \& McGhee (80) | Detention time | About 30 min . |
|  | Aeration rate | 0.01 to $0.05 \mathrm{~m}^{3} / \mathrm{m}^{3}$ of wastewater |
|  | Dimensions | Same as for aerated grit chambers |
| Viessman \& Harmer (91) | Detention time | Less than 20 min . |
|  | Air Requirements | 0.37 to $1.49 \mathrm{~m}^{3} / \mathrm{m}^{3}$ of wastewater <br> 10.05 to 0.20 ft .3 qal . of wastewater |
| Kappe \& Neighbor (42) | Detention time | 30 min . |
|  | Velocity | $0.61 \mathrm{~m} / \mathrm{s}$ ( $2 \mathrm{ft} . / \mathrm{s}$ ) is necessary to prevent deposition of solids |
|  | Air requirements | Mininum $0.7392 \mathrm{~m}^{3} / \mathrm{m}^{3}$ of wastewater ( $0.1 \mathrm{ft.}^{3} /$ gal. of wastewater) or amount necessary to maintain tank circulation |

### 2.1.3 Aerated Equalization Basins

The proper operation of both in-line and off-line equalization basins require proper mixing and sufficient dissolved oxygen. Mixing is provided to blend the contents of the tank and to prevent deposition of solids in the basin. Grit removal facilities should precede equalization basin, wherever possible, to minimize mixing requirements. Compressed air aeration system can provide both the mixing and the oxygen to prevent the wastewater from becoming septic [60]. The other method of providing both mixing and aeration is through the use of mechanical aerators. Properly designed equalization facilities reduce wide fluctuations in waste-stream characteristics, and provide a system that is less susceptible to upsets and consistently provides a better quality effluent than an unequalized system [7]. Also it has been proven that the operating power requirements of the equalized system can be appreciably lower than that of an unequalized system [7]. Proper mixing can make the volume of an equalization basin much smaller than a poorly mixed basin, at the same time providing better results at reduced capital investment and operating costs.

The design criteria for equalization basins, as given by various researchers are given in Table 2.2.

Table 2.2 - DESIGN CRIIERIA FOR AERATED EQUALIZATION BASINS

| REFERENCE | DESIGN PARAMEIER | RANGE |
| :---: | :---: | :---: |
| Metcalf \& Eddy (60) | Air Requirement to Maintain <br> Aerobić Conditions in Aerated <br> Equalization Basins | 0.01 to $0.015 \mathrm{~m}^{3} / \mathrm{m}^{3}-\mathrm{min}$. |
| Metcalf \& Eddy (60) | Power Requirement to Blend a <br> Medium-Strength Municipal <br> Wastewater | 4 to $8 \mathrm{w}^{3} \mathrm{~m}^{3}$ of storage |

### 2.1.4 Aeration Basins in Biological Treatment of Wastewater

Air is used for two purposes in the biological treatment process: first to supply metabolic oxygen requirements of micro-organisms and second to provide proper mixing within the reactor to keep the biological flocs in suspension. The most common method of aeration in biological treatment processes is diffused bubble aeration. The cost of compressing air constitutes the largest portion of the operating cost in an activated sludge process. Therefore, any improvement in the efficiency of the aeration process would certainly reduce these operating costs[57].

The process of diffused aeration is in the form of small air bubbles introduced through small openings into the liquid. These openings or outlets are usually located near the bottom and along one side of the tank. Because of the resulting low density of the air water mixture above the air outlets, as well as the direction of liquid flow, a rising, circulating, spiral motion of the mixture results throughout the entire tank as shown in Figure 2.1. This circulatory motion keeps the activated sludge flocs in suspension. The air bubbles also provide necessary oxygen needed by the biological suspension in the system[57].

There are various methods of supplying oxygen to the aeration basin but the two most common means are by mechanical or surface aeration and by diffused bubble


Figure 2.1: Cross-Section of a Typical Diffused Air, Spiral
Flow, Conventional Activated Sludge Aeration Tank
aeration. The latter can be further divided into fine bubble and coarse bubble aeration. However, despite higher efficiencies generally associated with fine bubble diffusers, they have limitations in practice due to their tendency to clog: both internally from the impurities in compressed air and externally from the wastes in the aeration basins. The coarse bubble aeration process, commonly employed in different wastewater treatment units, has been the object of many extensive investigations for improving the transfer of oxygen into wastewater [57]. Substantial amount of work has been done in recognizing and improving the factors affecting the rate of oxygen transfer [9,20,30,31,57]. However, limited literature is available on the mixing aspects of aeration to keep the biological solids in suspension without shearing them. Mixing in aeration basins is discussed in detail later in this chapter.

### 2.2 Grit Chambers

It is a common practice to remove grit in such a way as to avoid the inclusion of excessive amount of decomposable organic solids with the removed grit. Grit includes sand, silt, coal dust, coffee grounds, fruit seeds, egg shells etc. For design purposes of a grit chamber, grit is defined as fine sand of 0.2 mm or larger in diameter with a specific gravity of 2.65 [18,92]. Grit is removed in municipal wastewater treatment to protect mechanical
equipment and pumps from abnormal abrasive wear, to prevent pipe clogging by grit deposition, to maintain the capacities of settling tanks, digesters etc. [92], and to prevent the cementing effects on the bottom of sludge digesters and primary sedimentation tanks [73]. Grit chambers may be located ahead of all other units in treatment plants where removal of grit would facilitate operations. However, the installation of mechanically cleaned bar racks or comminutors ahead of grit chambers makes the operation of grit removal and cleaning facilities easier. Table 2.3 shows the advantages and disadvantages of having a grit removal facility installed at different locations [73].

Most grit chambers are designed to maintain a certain mean velocity depending on particle characteristics, as shown in Table 2.4. It is expected that at this velocity only decomposable organic particles will be resuspended.

The conventional type chamber has a two-fold function (i) to remove the grit from the sewage, and (ii) to separate the grit from the decomposable particles so that it may be disposed of without nuisance. The mechanism of this removal process has not been well understood in practice and has generally been referred to as 'differential settling'. There are in fact two processes at work: (a) settling of both grit and organics which is 'differential' only in the sense that grit settles faster than most of the organic particles and (b) 'scour' or 'bed load movement' of the settled solids

Table 2.3 - COMPARISON OF VARIOUS LOCATIONS OF GRIT REMOVAL FACIIITY, Qasim (73)

| LOCATION | ADVANTAGES | DISADVANIAGES |
| :--- | :--- | :--- |
| Ahead of lift station | Maximum protection of pumping <br> equipment. | Frequently deep in the ground, <br> high construction cost, not <br> easily accessible, and difficult <br> raising the grit to ground level. |
| After pumping station | Ground level structure. Ac- <br> cessible and easy to operate. | Some abnommal wear to pumps. |
| pegritter in conjunction with |  |  |
| primary sludge | Usually low capital and opera- <br> tion and maintenance costs. <br> Cleaner and drier grit. | Pumping equipment not adequately <br> protected. |

Table 2.4 - RECOMMENDED MEAN DESIGN VELOCITIES IN GRIT CHAMBERS

| REFERENCE | PARIICTE CHARACTERISTICS | FLOW CONDITIIONS | VELOCITY RANGE |
| :---: | :---: | :---: | :---: |
| Kappe \& Neighbor (42) | Sand particles, 0.2 mm size | Move along the tank bottom. | $\begin{aligned} & 0.23 \mathrm{~m} / \mathrm{s} \\ & (0.75 \mathrm{ft} . / \mathrm{s}) \end{aligned}$ |
| Kappe \& Neighbor (42) | Sand particles, 0.2 mm size | Start an upward vertical movement coupled with the additional resistance caused by the sharp turn at the tank edge. | $\begin{aligned} & 1.83 \mathrm{~m} / \mathrm{s} \\ & (0.6 \mathrm{ft} . / \mathrm{s}) \end{aligned}$ |
| Kappe \& Neighbor (42) | Lighter organic particles | Stay in suspension. | $\begin{aligned} & 0.61 \mathrm{~m} / \mathrm{s} \\ & (2.0 \mathrm{ft} . / \mathrm{s}) \end{aligned}$ |
| Harremoes (38) \& Pallasch (69) | Grit particles | Bottom velocity that would deposit grit particles but not the organic matter in aerated grit chambers. | $0.3 \mathrm{~m} / \mathrm{s}$ |
| Lodholze \& Pentz (52) | Organic particles | Keep organic particles in the removed grit at a minimum level. | $\begin{aligned} & 0.23 \text { to } 0.37 \mathrm{~m} / \mathrm{s} \\ & \text { ( } 0.75 \mathrm{to} 1.2 \mathrm{ft} . / \mathrm{s} \end{aligned}$ |
| Hardenbergh \& Rodie (39) | Sewage | Just enough to permit the particles with greater specific gravity to settle out while the organic material is carried away. | $\begin{aligned} & 0.3 \mathrm{~m} / \mathrm{s} \\ & (1.0 \mathrm{ft} . / \mathrm{s}) \end{aligned}$ |
| Camp (18) | Grit particles | For American-type qrit chambers. | $\begin{aligned} & 0.15 \text { to } 0.37 \mathrm{~m} / \mathrm{s} \\ & 10.5 \text { to } 1.2 \mathrm{ft} . / \mathrm{s} \\ & \hline \end{aligned}$ |

Table 2.4 - RECOMMENDED MEAN DESIGN VELOCITIES IN GRIT CHAMBERS (cont'd)

| REFERENCE | PARTICLE CHARACIERISTICS | FLOW CONDITIONS | VELOCITY RANGE |
| :---: | :---: | :---: | :---: |
| Konicek \& Pardus (46) | Grit particles | Critical velocity in a grit chamber without baffle. | $0.30 \mathrm{~m} / \mathrm{s}$ |
| Viessman \& Harmer (91) | Grit particles, 0.2 mm size, 2.65 specific gravity | Prevent scouring. | $\begin{aligned} & 0.30 \mathrm{~m} / \mathrm{s} \\ & (1.0 \mathrm{ft} . / \mathrm{s}) \end{aligned}$ |
| Steel \& McGhee ( 80 ). | Grit and organics | Horizontal velocity to remove grit, without removing organic material. | $\begin{aligned} & <0.056 \mathrm{~m} / \mathrm{s} \text { and } \\ & >0.23 \mathrm{~m} / \mathrm{s} \end{aligned}$ |
| Steel \& MCGhee (80) | Grit and organics | Recommended velocity to allow deposition of grit while scouring out organics. | $\begin{aligned} & 0.23-0.38 \mathrm{~m} / \mathrm{s} \\ & \text { (preferred } 0.3 \mathrm{~m} / \mathrm{s} \text { ) } \end{aligned}$ |
| Hardenbergh \& Rodie (39) | Particles of specific gravity 2.65 | For grit removal. | $\begin{aligned} & 0.3 \mathrm{~m} / \mathrm{s} \\ & (1.0 \mathrm{ft} . / \mathrm{s}) \end{aligned}$ |
| Qasim (73) | Grit particles | Typical design value for a grit chamber. | $0.3 \mathrm{~m} / \mathrm{s}$ |
| MOP \#8 (58) | Grit | Average design value. | $\begin{aligned} & 0.3 \mathrm{~m} / \mathrm{s} \\ & (1.0 \mathrm{ft} . / \mathrm{s}) \end{aligned}$ |
| Metcalf \& Eddy (60) | Grit | Horizontal desion velocity. | $0.25-0.40 \mathrm{~m} / \mathrm{s}$ |

which is more effective in separating the organics than settling [18]. In a properly designed grit chamber the full advantage of both"processes is taken. Camp [18] had developed an equation to calculate the mean scouring velocity in a grit chamber by utilizing the theoretical study and extensive experimental work done by Shields [81] on the movement of granular materials in a flowing stream. Proposed Camp Shields equation for scouring velocity [18]:

$$
\begin{aligned}
& v_{c}=\sqrt{\frac{2 \beta}{f} g\left(S_{s}-1\right) d} \\
& \text { Where } v_{C}= \text { critical velocity required to start } \\
& \text { scour of particles whose size is } d \\
& \text { and specific gravity is } \mathrm{Ss}, \mathrm{~m} / \mathrm{s} \\
& \mathrm{~g}= \text { acceleration due to gravity, } \mathrm{m} / \mathrm{s}^{2} \\
& f= \text { Weisbach-Darcy friction factor which } \\
& \text { may be considered equal to about } 0.03 \text { for } \\
& \text { grit chambers } \\
& \beta= \text { an experimental constant }
\end{aligned}
$$

The value of experimental constant, $\beta$, was found by Shields to be approximately 0.04 for unigranular material. For non-uniform and sticky material, like grit, a value of about 0.06 is probably safe for design. According to this equation the depth does not influence scour, although it does affect settling.

There are two general types of grit chambers : (a) horizontal flow and (b) aerated. In a horizontal flow type, the flow passes through the chamber in a horizontal direction and the straight line velocity of flow is controlled by the dimensions of chamber or by the use of special weir sections at the effluent end. In case no velocity control is provided, settled particles have to be washed to separate the decomposable organic particles from grit. The aerated grit chamber consists of a spiral flow aeration tank where the spiral velocity is controlled by the dimensions and the quantity of air supplied to the unit [60]. Different kinds of horizontal flow type grit chambers are in use in wastewater treatment and selection depends on the amount of grit in the wastewater, size of the plant and cost. Standard systems include : (a) channel shaped grit chamber, and (b) clarifier type units with mechanical scraping arms [29,60].

In practice the length of the tank is up to 50 percent larger than theoretically required to allow for turbulence and inlet and outlet disturbances [58]. The design criteria for grit chambers as suggested by various researchers are given in Table 2.5.

Table 2.5 - DESIGN CRITERIA FOR HORIzONTAL FLOW GRIT CHAMBERS

| REFERENCE | DESIGN PARAMETER | RANGE |
| :---: | :---: | :---: |
| Metcalf \& Eddy (60) | Detention time | 45-90 s |
|  | Horizontal mean velocity | 0.25-0.4 m/s |
|  | Settling Velocity for the removal of: <br> 65 mesh material ( 0.21 mm ) <br> 100 mesh material ( 0.15 mm ) | 1.0 to $1.3 \mathrm{~m} / \mathrm{min}$. <br> 0.6 to $0.9 \mathrm{~m} / \mathrm{min}$. |
|  | Head loss in control section as percentage of depth in channel | 30 to 40\% |
|  | Allowance for inlet and outlet turbulence | $2 \times$ maximum depth of grit chamber <br> 0.5 x theoretical length of grit chamber |
| Viessman \& Harmer (91) | Settling velocity for the removal of 0.2 mm diameter particles with specific gravity of 2.65 | $0.023 \mathrm{~m} / \mathrm{s}$ |
|  | Horizontal mean velocity | $0.3 \mathrm{~m} / \mathrm{s}$ |
| Steel \& McChee (80) | Length of grit chamber | Depends upon the trajectory of slowest settling particles and the depth of flow. Length $\simeq 12 \mathrm{x}$ depth of flow. |
| Qasim (73) | Detention time | 60 s |
|  | Horizontal mean velocity | $0.3 \mathrm{~m} / \mathrm{s}$ |
|  | Settling velocity for 65 mesh ( 0.21 mm ) particles | $1.15 \mathrm{~m} / \mathrm{min}$. |
|  | Head loss | 30 to $40 \%$ of the maximum water depth in the channel |

Table 2.5 - DESIGN CRIIERIA FOR HORIZONIAL FLOW GRIT CHAMBERS (cont'd)

| REFERENCE | DESIGN PARAMETER | RANGE |
| :--- | :--- | :--- |
| Camp (18) | Horizontal mean velocity | $0.15-0.3 \mathrm{~m} / \mathrm{s}$ |
|  | Detention time | 1 min. |
|  | Settling velocity for 0.2 mm <br> sand | $0.023 \mathrm{~m} / \mathrm{s}$ |
| Eckenfelder (29) | Horizontal mean velocity | $0.23-0.38 \mathrm{~m} / \mathrm{s}$ |
|  | Chamber length | Based on horizontal mean velocity and <br> settling velocity of particles |
|  | Cross-sectional area | Based on flow rate and horizontal mean <br> velocity |

### 2.2.1 Aerated Grit Chambers

Conventional grit chambers are incorporated in water pollution control plants to remove sand and other abrasive or inert materials which could be detrimental to the proper operation of the mechanical equipment and treatment units. Aerated grit chambers are finding general application because they exhibit certain advantages in operation and design over conventional grit chambers. These advantages are $[1,73]$ are listed below:

1. The sewage is freshened (kept more aerobic) by oxygen in air
2. Low hydraulic head loss is required in the design
3. The controllable air-induced water velocity enhances the removal of grit with a low organic content
4. Grit larger than desired size can be preferentially removed, assuming a constant specific gravity for all the grit involved
5. The grit removal efficiency can be maintained over a large flow range
6. Comparatively clean grit can be obtained.
7. An aerated grit chamber can also be used for chemical addition, mixing and flocculation ahead of primary treatment
8. Grease removal may be achieved if skimming is provided At design conditions, the normal flow retention time in an aerated grit chamber is small (a matter of a few
minutes): therefore, the freshening of the sewage may be minimal. However, if the aerated grit chamber is incorporated with a preaeration unit, the dual benefits of grit removal and sewage freshening can be achieved.

The hydraulic head loss in an aerated grit chamber is kept small because a simple horizontal overflow weir may be employed. This compares with the relatively large head loss associated with Sutro or other constant velocity weirs often used with conventional grit chambers. Complex constant velocity weirs are not required with aerated grit chambers because the air-induced water velocity, rather than the flow through velocity, control the grit removal process. This control, maintained by the air-induced velocity, also explains why grit removal efficiencies can be maintained over the entire designed flow range.

The aerated grit chamber has been developed to provide a system of grit removal which can be installed ahead of comminutors, raw sewage pumps, and other mechanical equipment. Maximum protection may be given to these units by removing clean washed grit that will be useable for filling without causing any nuisance. Aerated grit chambers are normally rectangular in cross-section with an aeration header on each side, or only on one side, creating a rolling action to separate the lighter organic material from the grit particles. The grit drops to the bottom of the tank and rolls to the collection hopper while the organics remain in suspension [53].

In application, an aerated grit chamber is similar to a standard spiral flow aeration tank with air diffusion tubes located on one side, approximately 0.61 m . ( 2 ft. ) above the bottom of the tank. Hoppers are provided beneath the swing diffusers for collecting the grit. Swing diffusers are preferred because of their accessibility for servicing and other advantages over submerged fixed diffuser system. The velocity of roll or agitation governs the size of particles of a given specific gravity that will be removed. If the velocity is too high, grit will be carried out of the chamber: if it is too small, organic material will be removed with the grit. Grit chambers traditionally have been designed to remove inorganic material of minimum 0.2 mm size at the design flow rate [36].

A study has shown that the performance of an aerated grit removal system can be substantially improved by adjusting aeration rate and distribution [36]. An optimum rate can decrease operational problems in distribution channels, digesters and other areas by reducing the amount of grit, rags, sticks, and plastics passing through the grit removal system into those areas from which they must be removed manually. Further tapered aeration equalizes loading on grit pumping and dewatering equipment. The Renton Treatment Plant at Seattle [35] improved grit removal by adjusting the air flow rate in its aerated grit chamber to the optimum rate. This resulted in a decrease in operational problems in
distribution channels, digesters and other areas. Aerated grit chambers are normally designed on the basis of detention time [52]. The air requirements in aerated grit chambers suggested by various researchers are shown in Table 2.6.

The design criteria for aerated grit chambers recommended by various researchers are given in Table 2.7. It can be seen that very little work has been done on aerated grit chambers, especially on the critical location of diffusers, effect of depth of liquid on velocity, and effect of tank geometry on velocity.

Table 2.6 - AIR REQUTREMENT IN AERATED GRIT CHAMBERS

| REFERENCE | PARTICTE CHARACTERISTICS | DESIGN CONDITITONS | AIR REQUIREMENT |
| :---: | :---: | :---: | :---: |
| Kappe \& Neighbor (42) | Organic material | Develop a velocity of $0.6 \mathrm{~m} / \mathrm{s}$ ( $2 \mathrm{ft} . / \mathrm{s}$ ) to hold particles in suspension | $\begin{aligned} & 0.28 \mathrm{~m}^{3} / \min . / \mathrm{m}\left(3 \mathrm{ft}_{.}^{3} /\right. \\ & \min . / \mathrm{ft} .) \text { of } \operatorname{tank} \text { length } \end{aligned}$ |
| Bewtra (8) | Grit particles | Design factor in aerated grit chamber | $\begin{aligned} & 0.28 \text { to } 0.465 \mathrm{~m}^{3} / \mathrm{min} . / \mathrm{m} \\ & \left(3 \text { to } 5 \mathrm{ft.}^{3} / \mathrm{min} . / \mathrm{ft} .\right) \text { of } \\ & \text { tank length } \end{aligned}$ |
| Steel \& McGhee (80) | Grit and organic particles | Prevent scouring of grit while keeping organics in suspension | 0.3 to $0.5 \mathrm{~m}^{3} / \mathrm{min}$. $/ \mathrm{m}$ of tank length. Detention time is usually less than 3 min . |
| Metcalf \& Eddy (60) | Grit and organic particles | Settle grit while keeping organics in suspension | $0.15-0.45 \mathrm{~m}^{3} / \mathrm{min} . / \mathrm{m}$ of length. <br> Typical <br> value $=0.3 \mathrm{~m}^{3} / \mathrm{min} . / \mathrm{m}$ Detention time at peak flow $=2.5 \mathrm{~min}$. |
| pasim (73) | Grit particles | Typical design value for the design of aerated grit chamber | $4.6-12.4 \mathrm{~L} / \mathrm{s} / \mathrm{m}$ of tank length. <br> Detention time at peak flow $=2.5 \mathrm{~min}$. |

Table 2.7 - DESIGN CRITERIA FOR AERATED GRIT CHAMBERS

| REFERENCE | DESIGN PARAMEIER | RANGE |
| :---: | :---: | :---: |
| Metcalf \& Eddy (60) | Depth | 2-5m |
|  | Width | $7.5-20 \mathrm{~m}$ |
|  | Length | $7.5-20 \mathrm{~m}$ |
|  | Width to depth ratio | 1:1-5:1 |
|  | Detention time at peak flow | 2-5 min. |
|  | Air flow rate | $0.15-0.45 \mathrm{~m}^{3} / \mathrm{min} .-\mathrm{m}$ of tank length |
|  | Depth of grit hopper (with steep sloping sides) | 0.9 m |
|  | Location of diffuser | $0.45-0.60 \mathrm{~m}$ (above the normal plane of bottom) |
|  | Tank geametry | Wastewater should be introduced in the direction of roll. |
| Albrecht (1) | Chamber geametry | Depth to width ratio of 1:1 with side slopes at 45 degrees. The collection channel size is based on anticipated amount of grit. A long and narrow tank minimizes short-circuiting. |
| Rappe \& Neighbor (42) | Location of diffusers | 0.6 m (2ft.) above the bottom of tank |
|  | Recormended kind of diffusers | Swing |
|  | Velocity | $0.6 \mathrm{~m} / \mathrm{s}$ ( $2 \mathrm{ft} . / \mathrm{s}$ ) |
|  | Detention time | 1.1 min. at peak flow |
|  | Depth | Up to 4.6 m ( $15 \mathrm{ft}$. ) |
|  | Width | Up to 9.2 m ( 30 ft.$)$ |
|  | Typical tank size | 6.25 m ( 20.5 ft .) wide $\times 3.50 \mathrm{~m}$ (11.5 ft. deep) $\times 15.25 \mathrm{~m}$ ( $50 \mathrm{ft}$. ) long for 100 MGD plant. For 200 MGD plant: 9.15 m ( 30 ft .) wide $\times 4.60$ ( 15 ft .) deep $\times 21.35 \mathrm{~m}$ ( 70 ft. ) long. |
|  | ir flow rate | $0.28 \mathrm{~m}^{3} / \mathrm{min} . / \mathrm{m}$ of tank length |

Table 2.7 - DESIGN CRITERIA FOR AERATED GRIT CHAMBERS
(cont'd)

| REFERENCE | DESIGN PARAMETER | RANGE |
| :---: | :---: | :---: |
| Steel \& McGhee (80) | Air flow rate | 0.3-0.5 $\mathrm{m}^{3} / \mathrm{min}-\mathrm{m}$ of tank length |
|  | Detention time | Less than 3 min. |
|  | Depth | 70 to 100 percent of width ( 3 to 5 m ) |
| Qasim (73) | Depth | 2-5m |
|  | Length | 7.5-20m |
|  | Width | 2.5-70 m |
|  | Width to depth ratio | 1:1-5:1 |
|  | Length to width ratio | 2.5:1-5:1 |
|  | Transverse velocity at surface | 0.6-0.8 m/s |
|  | Detention time at peak flow | 2-5 min. |
|  | Air flow rate | 4.6-12.4 L/s/m of tank length (3-8 cim/ft. of tank length) |
|  | Inlet and outlet structure | Must be such as to prevent short-circuiting and turbulence. |
|  | Baffles | Longitudinal and transverse baffles improve qrit removal efficiency. |
|  | Chamber geametry | Location of air diffusers, sloping tank bottam, grit hopper, and accamodation of grit collection and removal equipments should all be given consideration in chamber geanetry. |
| Neighbor \& Cooper (62) | Location of diffusion equipment | 0.6 m ( 2 ft .) above the sloping tank bottam |
|  | Air supply | $0.28 \mathrm{~m}^{3} / \mathrm{min} . / \mathrm{m}$ of tank length ( $3 \mathrm{~cm} /$. ft. of tank length) |
|  | Surface velocity | 0.46-0.6 m/s (1.5-2 ft. $/ \mathrm{s}$ ) |

Table 2.7 - DESIGN CRITERIA FOR AERATED GRIT CHAMBERS (cont'd)

| REFERENCE | DESIGN PARAMEIER | RANGE |
| :---: | :---: | :---: |
| Neighbor \& Cooper (62) | Detention time | 1.5-2 min. |
|  | Shape | Longer, narrower tanks produce grit of better quality. |
|  | Inlet and outlet structures. | Must minimize short-circuiting. |
|  | Baffles | Transverse baffles are desirable on larger tanks. Longitudinal baffles and effluent baffles improve performance. |

### 2.3 Mixing in Water and Wastewater Treatment

### 2.3.1 General

Mixing is defined as the intermingling of two or more dissimilar portions of materials, resulting in the attainment of a desired level of uniformity, either physical or chemical, in the final product.

Mixing operations have a considerable importance in water as well as wastewater treatments. The term 'mixing' has been used to describe processes which tend to reduce nonuniformities or gradients in composition of material in bulk [89]. As an example, mixing is employed (i) in aeration tanks to keep the biological solids in suspension and also to keep the conditions aerobic, and (ii) in high rate digesters to prevent separation of solids and to maintain homogeneous conditions of raw sludge and seed sludge, and also to provide an even temperature throughout the tank. Another very common and important purpose served by mixing is to bring together different molecular species in order to have a reaction. Mixing may also be used to disperse a variety of chemicals such as coagulants, coagulant aids, or to contact substances such as activated carbon.

Different kinds of mixing devices.. are in use depending upon the purpose of mixing, volume, cost, extent of desirable uniformity and operating conditions. The common mixing devices are [82]: (a) gravitational, (b) pneumatic, and (c) mechanical. The baffled channel and hydraulic-jump
mixers are examples of gravitational mixers. Impellers such as paddles, turbines and propellers are generally used for mechanical mixing. In pneumatic mixing, compressed air is diffused in the liquid content which generates mass circulation of liquid and turbulence [33,80]. Pneumatic mixing has been the least investigated of all the types of mixing.

### 2.3.2 Mixing in Air Agitated Tanks

In wastewater treatment as well as in other mixing operations, two types of air agitated tanks are in use: continuous and batch operated. Despite the widespread use of these units, there is limited literature available on either the theoretical or the practical aspects of designing these tanks [3].

Most of the reported work is on continuous air agitated tanks in which air agitation is used to achieve oxygen transfer from diffused air to the liquid content of the tank. Some fundamental research work on mixing characteristics of continuous air agitated tanks has been reported by Thomas and Mckee [88], Murphy and Timpany [56] and Murphy and Boyko [59]. All their studies were confined to fixed geometry tanks and fixed location of diffusers. None of them studied the effect of geometry or location of diffusers on the mixing or the horizontal velocities near the tank bottom.

For batch air-agitated tanks, the nature of mixing has not been studied extensively. Kaufman [44] has suggested various amounts of air for various intensities of agitation, referring specifically to the petroleum industry. According to him the following quantities of air per unit of tank cross-sectional area may be used to obtain an acceptable degree of agitation in a liquid depth $\mathrm{m}_{\perp}^{3} / \mathrm{min} / \mathrm{m}_{\mathrm{ll}}^{2}\left(\mathrm{ft}_{\perp}^{3} / \mathrm{min} / \mathrm{ft}\right)^{2}$
Moderate Agitation
Complete Agitation
Violent Agitation

$$
\begin{aligned}
\mathrm{m}^{3} / \mathrm{min} / \mathrm{m}^{2} & \left(f t^{3} / \mathrm{min} / \mathrm{ft}\right)^{2} \\
0.183 & (0.6) \\
0.396 & (1.3) \\
0.945 & (3.1)
\end{aligned}
$$

Szabo [82],studied the mixing characteristics of a small scale batch mixing tank. Air was diffused through a pipe located either at the center or the periphery of the tank. Based on the experimental results, szabo developed the following correlations relating the performance of the mixing time with the tank geometry and the air flow rate.

$$
\begin{align*}
& \log t_{\max }=1.19+0.34 \frac{\mathrm{D}}{\mathrm{H}}+0.35 \log _{\overline{\mathrm{Q}}}^{\mathrm{Fl}}  \tag{2.2}\\
& V_{\text {sur }}=\frac{Q_{\mathrm{al}}}{\mathrm{C}+\mathrm{mQ}_{\mathrm{al}}} \tag{2.3}
\end{align*}
$$

$$
\begin{aligned}
& \text { Where } t_{\max }=\text { mixing time, } s \\
& \qquad \begin{aligned}
& \mathrm{D}=\text { diameter of tank, } \mathrm{m} \\
& \mathrm{H}= \text { liquid depth, } \mathrm{m} \\
& Q_{\mathrm{al}}= \text { air flow rate under atmospheric } \\
& \text { pressure and at } 20^{\circ} \mathrm{C}, \mathrm{~m}^{3} / \mathrm{min} \\
& \forall= \text { volume of fluid in tank, } \mathrm{m}^{3} \\
& V_{\text {sur }}=\text { surface velocity, } \mathrm{m} / \mathrm{s}
\end{aligned} \\
& \mathrm{c} \text { and } \mathrm{m}=\text { correlation constants }
\end{aligned}
$$

The successful operation of an air agitated tank in waste treatment system is dependent on the degree of mixing in the system. Function of mixing include [67]:

1. Gross mixing of the waste influent with the biological solids
2. Mixing of the incoming waste with the bulk liquid present in the aeration basin (extent depending on the degree of 'complete mixing' desired)
3. Mixing to cycle deoxygenated liquor to the aerators
4. Mixing turbulence to maintain biosolids in suspension
5. Mixing to produce small scale turbulence for promoting the mass transfer of dissolved oxygen and substrate into the cell mass

The mathematical description of mixing is useful for directing the designer toward the provision of adequate mixing in activated sludge systems, but application of these principles alone does not permit the completion of a design
for a system. Parameters such as power input per unit volume, aerator pumping capacity per unit volume, and velocity measurements have been employed as guides to ensure adequate mixing $[67,28,43,51,68]$. In most cases, design has centered around obtaining the desired oxygen transfer capacity [67,28,51].

Power input is generally regarded as a poor criterion since a number of combinations of impeller diameter and rotational speed, in the case of a surface aerator, can result in the same power consumption with markedly different mixing characteristics. The same argument could be applied in the case of diffused aeration systems. However, in systems with similar geometries this parameter can still be very useful [68].

Aerator pumping capacities have been correlated with radius of influence for dispersion of dissolved oxygen and suspension of solids in activated sludge systems. Again these correlations have been keyed to particular types of equipment, and therefore representative values cannot be cited [67]. Velocities have been widely employed as guides for estimating the extent of mixing required to keep the biosolids in suspension.

The most common type of air agitated tanks are 'spiralflow' aeration tanks and aerated grit chambers, in which air is usually released near the bottom of one side of the tank resulting in a spiral bulk flow of the contents. The bulk
rotation of the fluid in a rectangular tank, combined with the mixing effects of the rising air bubbles, results in a high degree of turbulent mixing. This mixing can be influenced by variations in many factors including [56]:

1. temperature
2. air flow rate
3. type of air injectors
4. mean residence time
5. tank geometry
6. solids level
7. entrance and exit conditions

Price et al. [67] have given an excellent description of surface aerators and submerged turbine aerators, discussing for example the spacing of aerators and extent of mixing. The minimum power requirement to suspend the biological solids given in the literature $[28,67]$ is $7.9 \mathrm{~W} / \mathrm{m}^{3}(0.04 \mathrm{hp} /$ 1000 U.S. gal) of mixed liquor. The velocities required to keep the biological solids in suspension, given by different researchers, are shown in Table 2.8.
:Table 2.8 - VELOCITIES REQUIRED IN ACTIVATED SLUDGE AERATION TANKS

| REFERENCE | PARTICLE <br> CHARACTERISTICS | FLOW CONDITIONS | VELOCIIY RANGE |
| :--- | :--- | :--- | :--- |
| Eckenfelder, et al (28) <br> Kumke, et al (43) | Activated sludge | Minimum velocity for sus- <br> pending biomass | $0.15 \mathrm{~m} / \mathrm{s}$ <br> $(0.5 \mathrm{ft} . / \mathrm{s})$ |
| Harremoes (38) | Mixed liquor suspended <br> solids | To keep biamass in suspen- <br> sion, bottam velocity | $0.3 \mathrm{~m} / \mathrm{s}$ |
| Price, et al (67) | Biosolids | Minimum velocity to sus- <br> pend biosolids | $0.15 \mathrm{~m} / \mathrm{s}$ <br> $(0.5 \mathrm{ft} / \mathrm{s}$.$) up to$ <br> biosolid concentra- <br> tion of $5,000 \mathrm{mg} / \mathrm{L}$ |

### 2.4 Initiation of Motion of Particles

Very little theoretical and experimental work has been done on the design of grit chambers based on the initiation of motion of grit and organic particles. The only theoretical approach, found in the literature, has been taken by Camp [18], who considered the theory of sediment transportation by Shields [81] and made use of it in the design of grit chambers. Grit chambers can be treated as small channels with a light sediment load. Excellent background is available in the field of sediment transport which can be used in a rational design of grit chambers.

Water flowing over a bed of particles exerts forces on the grains and tends to move or entrain them. The forces that resist the entraining action of the flowing water differ according to the grain size and grain size distribution of the sediments. For coarse sediments, e.g. sands and gravels, the forces resisting motion are caused mainly by the weight of the particles. Finer sediments that contain appreciable fractions of silt or clay, or both, tend to be cohesive and resist entrainment mainly by cohesion rather than by weight of the individual grains. Critical or threshold conditions are said to have been reached, when the hydrodynamic forces acting on a grain of sediment or on particles of cohesive sediments has reached a value, that, if increased even slightly will put the grain or aggregate into motion [83].

### 2.4.1 Sediment Properties

The fundamental properties of sediment particles have been studied quite intensively by two separate professions, geology and engineering. The geologists are concerned mainly with ancient sediments and they have studied the properties of sediment particles to find clues to the nature and movement of the transporting agent. The hydraulic engineers emphasize the interaction between the fluid and the particles, as they are primarily interested in the movement and deposition of sediments. The entrainment, transportation and subsequent deposition of a sediment depend not only on the characteristics of the flow involved, but also on the properties of the sediment itself [75].

### 2.4.1.1 Size

The most important property of a sediment particle or grain is its size. In many studies average size alone has been used to describe the sediment as a whole. Particle size may be defined by its volume, diameter, weight, fall velocity, or by sieve mesh size. With the exception of volume, the definitions are generally influenced by the shape or density of the particle. The following definitions taken from the the U.S. Inter-Agency Committee on Water Resources, Subcommittee on Sedimentation [90], are used to describe the particle size:

1. Nominal diameter- diameter of sphere having the same volume as the particle.

Sieve diameter- the diameter of a sphere equal to the length of the side of a square sieve opening through which measured quantities (by weight) of a sample will pass. As an approximation the sieve diameter is equal to the nominal diameter.

Sedimentation diameter- diameter of a sphere of the same fall velocity and same specific gravity as the particle in the same fluid under the same conditions.
4. Fall diameter or Standard fall diameter- diameter of a sphere that has a specific gravity of 2.65 and also has the same terminal uniform settling velocity as the particle when each is allowed to settle alone in quiescent, distilled water of infinite extent at a temperature of $24^{\circ} \mathrm{C}$.

The sieve and sedimentation diameters obviously have come into common use because of the convenience in measuring them. The sedimentation diameter is actually a fictitious size that enables the calculation of the settling velocity. For this reason, it has greater physical significance in sediment transportation than the other diameters [83]. Sieving has two definite disadvantages: (a) the lower sieve limit corresponds to approximately the midpoint of the size range of hydraulic interest; (b) sieve data are biased by particle shape, because the nominal sieve size is that size of square mesh through which a group of particles will just pass in a given interval of time, regardless of the extent to which they depart from the ideal spherical shape [10].
2.4.1.2 Shape

The size of a sediment particle alone is usually not sufficient to describe it. Generally speaking, shape refers to the overall geometric form of a particle regardless of size or composition. The most pertinent shape parameter has been known as sphericity which is defined [45,98] as the ratio of surface area of a sphere having the same volume as the particle to the surface area of the particle. Sphericity should be distinguished from roundness, which is defined as the ratio of the average radius of curvature of the edges to the radius of a circle inscribed in the maximum projected area of the particle [10]. The shapes of the particles have been expressed by a shape factor, SF , given by [83]:

$$
S F=\frac{c}{\sqrt{a b}}
$$

in which $a, b$, and $c$ are, respectively, the lengths of the longest, intermediate, and shortest mutually perpendicular axes of the particles.

### 2.4.1.3 Specific Weight of Sediment Particles

Specific weight is the dry weight per unit volume of the sediment. Most of the sediments whether borne by wind or water have their origin in rock material, and all constituents of the parent material can usually be found in the sediment. Quartz, because of its great stability, is the
commonest mineral found in sediments or grit. The average specific gravity of sand is very close to that of quartz i.e. 2.65, and this value is used often in calculation and analysis dealing with the grit. The specific gravity of particles in sediment transport is an important quantity and is used in many calculations.

### 2.4.1.4 Fall Velocity

The relative motion between sediment particles and the surrounding fluids under various conditions of entrainment, transportation, and deposition appears to depend upon essentially the same factors as the velocity at which the particles would fall through the fluid under their own weight. As a result, fall velocity has come to represent a characteristic of considerable practical as well as analytical value[10].

For a sphere of diameter $d$, the fall velocity $V_{S}$, for values of Reynolds number less than approximately 0.1 is given by Stokes law:

$$
\begin{equation*}
v_{s}=-\frac{g d^{2}}{18 v}-\left(s_{s}-1\right) \tag{2.5}
\end{equation*}
$$

$$
\begin{aligned}
\mathrm{R}_{\mathrm{e}}= & \mathrm{V}_{\mathrm{s}} \mathrm{~d} \\
\text { in which } v & =\text { kinematic viscosity of the fluid, } \mathrm{m}^{2} / \mathrm{s} \\
\mathrm{~g} & =\text { acceleration due to gravity, } \mathrm{m} / \mathrm{s}^{2} \\
\mathrm{~S}_{\mathrm{s}} & =\text { specific gravity of the sphere } \\
\mathrm{V}_{\mathrm{s}} & =\text { settling or fall velocity, } \mathrm{m} / \mathrm{s} \\
\mathrm{~d} & =\text { diameter of a sphere, } \mathrm{m}
\end{aligned}
$$

The fall velocity over the entire range of Reynolds number in terms of the drag coefficient, $\bar{C}_{d}$, is given by:

$$
\begin{equation*}
v_{s}=\sqrt{\frac{4}{3} \frac{g d}{c_{d}}\left(s_{s}-1\right)} \tag{2.7}
\end{equation*}
$$

Although fall velocity is a complex function of the Reynolds number, shape, and concentration, the fact remains that it is the relative behaviour of the particle rather than the exact correlation of size, shape and fall velocity which is of paramount importance in the hydrodynamics of sediment movement. To utilize the actual fall velocity as the significant particle characteristics, expressing this in terms of size when necessary through use of the Sedimentation Diameter, i.e. the diameter of a quartz sphere having the same terminal velocity of fall in the same fluid [10]. In some suspensions, electrochemical forces tend to hold particles together once they come into contact.

### 2.4.2 Mechanism of Entrainment

For many years, efforts have been made to express analytically the resultant force acting upon a typical sediment particle at the moment of its entrainment by the flow [47,99]. However, application of this rational approach to sediment particles in the aggregate on the stream bed becomes very complex statistically. For more than two centuries, workers have attempted to formulate the conditions of incipient motion. One of the earliest expressions is due to Brahms [11] which gives the critical velocity of water near the bed as:

$$
\begin{aligned}
& \mathrm{V}_{\mathrm{C}}=\mathrm{k} \mathrm{~W}_{\mathrm{g}}^{1 / 6} \\
& \text { Where } \mathrm{V}_{\mathrm{c}}=\text { critical velocity of water } \\
& \mathrm{k}=\text { an empirical constant } \\
& \mathrm{W}_{\mathrm{g}}=\text { weight of the grain }
\end{aligned}
$$

This equation is also called the Sixth Power Law.
Airy and Law $[4,53]$ rediscovered this law by equilibrium consideration. Wisner [100] pointed out that the factor of proportionality in the Sixth Power Law is likely to vary with the shape of the cross-section. Assuming that weight is proportional to the third power of a 'characteristic' grain diameter, Sternberg [84] showed that for incipient motion critical velocity varies with the square root of grain diameter. Sternberg's theory is close to the present usage where the weight of the grains is rarely used since it is easier to measure grain diameter (by sieving).

Shields [8l], published a paper in 1936 on this subject which has become a standard reference. It basically confirms the Sixth Power Law for large Reynolds Number [75]. A significant achievement by Shields was the dimensionless presentation of his results, which are illustrated in Figure 2.2. During the last four decades a number of papers have been published, most of them more or less intensive variations of the original Shields publications. These papers seemed to originate from what became known as the Shields diagram. The research efforts were almost exclusively directed toward uniform grain size material. Shields avoided the initial attempt at rationality by making certain gross assumptions and then confirmed and supplemented the analysis experimentally. Similar, though more involved, procedures were followed by Einstein[32] and Kalinske[47].

For the specific case of a level bed of uniform particle size investigated by Shields, he came up with a relationship


Figure 2.2: Analysis by Shields of the Entrainment Function [10].

$$
\begin{aligned}
& \frac{\gamma_{f}\left(S_{S}-1\right) d}{\gamma_{O}}=\phi-\frac{d U_{*}}{v} . \\
& \text { Where } \tau_{o c}=\text { critical tractive force, } N / \mathrm{m}^{2} \\
& g=\text { acceleration due to gravity, } \mathrm{m} / \mathrm{s}^{2} \\
& v=\text { kinematic viscosity of fluid, } \mathrm{m}^{2} / \mathrm{s} \\
& S_{S}=\text { specific gravity of particles } \\
& \mathrm{d}=\text { particle size, m } \\
& \gamma_{\mathrm{F}}=\text { specific weight of fluid, } \mathrm{N} / \mathrm{m}^{3} \\
& y=\text { depth of flow, } m \\
& \text { s = slope } \\
& U_{*}=\text { friction or shear velocity, } \mathrm{m} / \mathrm{s} \\
& -\frac{{ }^{\tau}{ }_{\gamma_{f}}\left(S_{S^{-1}}^{-1}\right)}{}=\text { critical entrainment function } \\
& \text { d U*_ =particle Reynolds number } \\
& v
\end{aligned}
$$

The critical entrainment function and particle Reynolds number are plotted in Shields diagram, Figure 2.2.

Novak and Nalluri[63] have developed equations for critical values of velocities, shear stresses and particle Froude numbers for incipient motion of sediment particles over fixed beds. They concluded that for single particle
resting on a smooth bed, the critical velocity or shear stress is a function of the particle size, shape, and density and the depth of flow; for grouped particles, in addition to the above, the space between the particles and the mode of grouping influences the result. In case of rough fixed beds, the size of the roughness and its relation to the particle size is an important parameter.

Neil[64] has presented experimental data on incipient motion of uniformalized. bed materials. These data are correlated with comparable data obtained by previous investigators including Shields, to develop a dimensionless expression for scour of coarse uniform material. He presented a design nomogram, relating competent mean velocity to grain size, specific gravity of sediment particles and depth of flow.

$$
\begin{aligned}
\mathrm{v}_{\mathrm{mc}}= & \text { function of }\left(\rho_{f}, \rho_{s}, \mu, \mathrm{~d}_{\mathrm{g}}, \mathrm{y}, \mathrm{~g}\right) \\
\text { Where } \mathrm{v}_{\mathrm{mc}}= & \text { competent mean velocity for first } \\
& \text { displacement of bed material, } \mathrm{m} / \mathrm{s} \\
\rho_{f}= & \text { fluid mass density, } \mathrm{kg} / \mathrm{m}^{3} \\
\rho_{s}= & \text { bed material mass density, } \mathrm{kg} / \mathrm{m}^{3} \\
\mu= & \text { fluid dynamic viscosity, } \mathrm{N} . \mathrm{s} / \mathrm{m}^{2} \\
\mathrm{~d}_{\mathrm{g}}= & \text { effective diameter of bed } \\
& \text { grains, } m \\
\mathrm{y}= & \text { depth of flow, } \mathrm{m} \\
g= & \text { acceleration due to gravity }
\end{aligned}
$$

It may be argued from physical considerations that since the flow is uniform, and since incipient motion is basically a question of static equilibrium, neither $g$ nor $\rho_{s}$ can be relevant as independent characteristic parameters. They can only occur in the combination $g\left(\rho_{s}-\rho_{f}\right)$, the specific weight of the bed material in the fluid, denoted $\gamma_{s}^{\prime \prime}$. If this view is adopted, and $\mu$ is replaced by $\nu=\mu / \rho$, the revised statement becomes:

$$
v_{\mathrm{mc}}=\text { function of }\left(\rho_{f}, \gamma_{S}^{\prime}, v_{i} d, y\right)---[2.12]
$$ This results in,

$$
\begin{equation*}
-\frac{\rho_{1} V_{\text {ma }}^{2}}{\gamma_{s}: \frac{d}{d}}=2.50-\frac{d}{y}-0.20 \tag{2.13}
\end{equation*}
$$

The results obtained using his approach were comparable with the results obtained by many other researchers including Shields.

### 2.5 Concept of Critical Shear Force and Critical Shear Velocity

When water flows in a channel, a force is developed that acts in the direction of flow on the channel bed. This force, which is simply the pull of water on the wetted area, is known as the shear force or tractive force. The critical shear force on a sediment particle is defined as the minimum shear force necessary for the initiation of motion of a particle [104]. The critical shear stress was determined by

Shields as the value of the stress for zero sediment discharge obtained by extrapolating a plot of observed sediment discharge versus shear stress [81].

In an uniform flow, the shear force, $F$, is apparently equal to the effective component of the gravity force acting on the body of water, parallel to the channel bottom and can be written as:

$$
\begin{aligned}
& F=\gamma_{f} A L s \\
& \text { Where } \gamma_{f}=\text { unit weight of water } \\
& A=\text { wetted area } \\
& L=\text { length of channel reach } \\
& s=\text { slope of channel }
\end{aligned}
$$

Thus, the average value of the shear force per unit wetted area is also called unit tractive force, ${ }^{\tau}{ }_{o}$ ([17] or simply shear stress and is equal to:

$$
\begin{aligned}
& \tau_{0}=\frac{\gamma_{E} A L s}{P_{e}^{L}}=\gamma_{f} R s \\
& \text { Where } P_{e}=\text { wetted perimeter } \\
& R=\text { hydraulic mean radius }
\end{aligned}
$$

The shear or friction velocity, $U_{\star}$, can be obtained from Eq. 2.15 as follows:

$$
\text { Where } p=\text { density of fluid }
$$

Under critical conditions, the shear stress becomes critical shear stress and the shear or friction velocity at this point is called critical shear or friction velocity, $\mathrm{U}_{\mathrm{*}_{\mathrm{C}}}$. Thus,

$$
\begin{align*}
U_{*_{C}} & =\sqrt{\frac{L_{0} \underline{\rho}}{\rho}}  \tag{2.17}\\
& \text { Where } \tau_{\rho c}=\text { critical shear stress }
\end{align*}
$$

The critical.shear stress of a sediment particle is defined as the minimum boundary shear stress necessary to initiate the motion of the particle [17]. Its magnitude depends on a number of factors including:

1. densities of the particle and the fluid
2. . size of the particle
3. viscosity of the fluid, which in turn varies with the fluid temperature

Critical shear stress is normally determined by laboratory experiments. However, for naturally occurring particles, such as sand, empirical formulae and experimental graphs are available for estimating their values in a
limited range [104]. An observation of a large area of sediment bed, when subjected to a shear stress near the critical value, will show that the incidence of gusts of sediment motion appears to be random in both time and space. This suggests, as observed by Shields[81], that the process of initiation of motion is statistically random in nature. Einstein [32] was the first to develop a transport relation based on statistical concepts. Because of the statistical nature of the entrainment process, there is no truly critical condition for initiation of motion for which motion begins suddenly as the condition is reached [83].

White[99] concluded that the true critical shear stress required to move a particular grain has a fixed value and this value is obtained from the experiments with laminar flow. His equation of critical bed shear ( $\tau_{o c}$ ) for sediment in a horizontal bed is:

$$
\begin{equation*}
\tau_{o c}=0.18\left(\gamma_{s}-\gamma_{f}\right) d_{s} \tan \theta \tag{2.18}
\end{equation*}
$$

in which the constant was obtained from the experiment with laminar flow, and

$$
\begin{aligned}
\tau_{O C} & =\text { critical bed shear } \\
\gamma_{S} & =\text { specific weight of sediment } \\
\gamma_{f} & =\text { specific weight of fluid } \\
d_{S} & =\text { particle mean size } \\
\theta & =\text { angle of repose }
\end{aligned}
$$

If it is assumed that initiation of motion is determined by $\tau_{o c}\left(\gamma_{s}-\gamma_{f}\right), d_{s}, \rho_{f}$ and $\mu$, then the dimensional analysis yields [83]:

$$
\begin{equation*}
\frac{\tau}{\left(\gamma_{s}-\gamma_{f}\right) d_{s}}=£\left(-\frac{U_{*} c_{-} d_{s}}{\nu}\right) \tag{2.19}
\end{equation*}
$$

The same equation was obtained by Shields by analysis of experimental data.

The value of $\tau_{o c}$. recommended by Lane[54] for the coarse material, is given by:

$$
\begin{aligned}
& \tau_{o c}=0.0164 d_{75} \\
& \text { in which } d_{75}= \text { size for which } 75 \% \text { of the bed } \\
& \text { material is finer, mm } \\
& \tau_{o c}= \text { critical bed shear in pounds } \\
& \text { force per square foot }
\end{aligned}
$$

### 2.5.1 Critical Shear Stress of Grit Particles Found in <br> Wastewaters

In designing grit chambers, the normal criterion is complete removal of particles with a specific gravity of 2.65 and a size of 0.2 mm [33] or greater. This size, however, represents only the lower limit and some grit particles larger than 0.2 mm are also removed. Table 2.9 presents the critical shear stresses for grit particles of 0.2 mm and l mm in size under different entrainment
conditions, estimated from the Shields diagram and methods suggested by other researchers [104]. The water temperature is assumed to be $20^{\circ}$. It is important to note in Table 2.9 that the critical shear stress increases appreciably with the content of colloidal or sediment particles in water [104]. For domestic sewage, the sum of the concentration of suspended and colloidal particles is often less than $0.1 \%$ [34], which is far less than $2.5 \%$ indicated in the Russian literature. However, considering the high solid load in the initial period of stormwater runoffs, the critical shear stresses given in Table 2.9 for high solid contents could be significant for storm sewer design. Otherwise, grit particles are the dominating consideration in designing the grit chambers and self cleansing domestic wastewater sewers.

Table 2.9 - CRITICAL SHEAR STRESS FOR 1 mm and 0.2 mm SAND PARTICLES (103)

| REFERENCE | CONDITTION | CRITICAL SHFAR STRESS |  |
| :---: | :---: | :---: | :---: |
|  |  | 1 mm | 0.2 mm |
| Shields diagram (23) | Packed bed flume | $\begin{aligned} & 3.063 \mathrm{~N} / \mathrm{m}^{2} \\ & \left(0.064 \mathrm{lb} . / \mathrm{ft}^{2}{ }^{2}\right) \end{aligned}$ | $\begin{aligned} & 1.149 \mathrm{~N} / \mathrm{m}^{2} \\ & \left(0.024 \mathrm{lb} . / \mathrm{ft}^{2}{ }^{2}\right) \end{aligned}$ |
| Russian results (78) | Clear water | $\begin{aligned} & 9.573 \mathrm{~N} / \mathrm{m}^{2} \\ & \left(0.20 \mathrm{lb} . \mathrm{ft.}^{2}\right) \end{aligned}$ | $\begin{aligned} & 2.393 \mathrm{~N} / \mathrm{m}^{2} \\ & \left(0.05 \mathrm{lb} . / \mathrm{ft}^{2}\right) \end{aligned}$ |
| Lane (78) | Canals with sand bed (clear water) | $\begin{aligned} & 9.573 \mathrm{~N} / \mathrm{m}^{2} \\ & \left(0.20 \mathrm{lb} . / \mathrm{ft} .{ }^{2}\right) \end{aligned}$ | $\begin{aligned} & 7.179 \mathrm{~N} / \mathrm{m}^{2} \\ & \left(0.15 \mathrm{lb} . / \mathrm{ft} .^{2}\right) \end{aligned}$ |
| PuBoys and Straub (79) | Packed bed flume | $\begin{aligned} & 7.658 \mathrm{~N} / \mathrm{m}^{2} \\ & \left(0.16 \mathrm{lb} . / \mathrm{ft}^{2}{ }^{2}\right) \end{aligned}$ | $\begin{aligned} & 3.829 \mathrm{~N} / \mathrm{m}^{2} \\ & \left(0.08 \mathrm{lb} . / \mathrm{ft}^{2}\right) \end{aligned}$ |
| Lane (78) | Concrete canals with low sediments | $\begin{aligned} & 13.880 \mathrm{~N} / \mathrm{m}^{2} \\ & \left(0.29 \mathrm{lb} . / \mathrm{ft}^{2}\right) \end{aligned}$ | $\begin{aligned} & 11.487 \mathrm{~N} / \mathrm{m}^{2} \\ & \left(0.24 \mathrm{lb} . / \mathrm{ft} .{ }^{2}\right) \end{aligned}$ |
| Russian results (78) | 2.5\% colloids | $\begin{aligned} & 18.666 \mathrm{~N} / \mathrm{m}^{2} \\ & \left(0.39 \mathrm{lb} . / \mathrm{ft}^{2}\right) \end{aligned}$ | $\begin{aligned} & 7.179 \mathrm{~N} / \mathrm{m}^{2} \\ & \left(0.15 \mathrm{lb} . / \mathrm{ft} .{ }^{2}\right) \end{aligned}$ |
| Fortier and Scobey (78) | With colloids | $\begin{aligned} & 18.666 \mathrm{~N} / \mathrm{m}^{2} \\ & \left(10.39 \mathrm{lb} . / \mathrm{ft} .{ }^{2}\right) \end{aligned}$ | $\begin{aligned} & 18.666 \mathrm{~N} / \mathrm{m}^{2} \\ & \left(0.39 \mathrm{lb} . / \mathrm{ft}^{2}\right) \end{aligned}$ |

### 2.5.2 Shear Stress Distribution

The shear stress distribution in a steady two-dimensional flow of a real and homogeneous fluid, having a free surface varies linearly with depth of flow and it becomes zero at the free surface. In fluid mechanics, it is normally assumed that, in a general case of turbulent flow, the total shear stress $\tau$ at any depth $y$ can be expressed as a sum of two components:

$$
\begin{aligned}
\tau= & \tau_{\ell}+\tau_{t} \\
\text { Where } \tau_{\ell}= & \text { laminar or viscous shear stress }=\text { shear } \\
& \text { stress due to molecular viscosity, } \mu \\
\tau_{t}= & \text { turbulent shear stress }
\end{aligned}
$$

The Laminar Shear Stress, $\tau_{\ell}=\mu-\frac{d u}{d y}$

$$
\text { where } \quad \frac{d u}{d y}=\text { Velocity gradient at a depth } y
$$

The component $\tau_{t}$ is the apparent shear stress due to turbulent fluctuations,ie,

$$
\begin{equation*}
\tau_{t^{\prime}}=-\rho \overline{u^{\prime} v^{\prime}} \tag{2.23}
\end{equation*}
$$

Where $u$ 'v' is the time average value of the product $u^{\prime} \cdot v^{\prime}$, the multipliers $u^{\prime}$ and $v^{\prime}$ being the components of the fluctuating velocity in $x$ and $y$ directions respectively. In terms of the time average velocity $u$, the magnitude of the turbulent shear stress $\tau_{t}$ can be given by the following expression of Prandtl [71].

$$
\begin{align*}
& \tau_{t}=\rho \ell^{2} \frac{d u}{\left(\frac{-}{d y}\right)^{2}}  \tag{2.24}\\
& \text { Where } \ell=\text { Prandtl mixing length } \\
& \ell=X y
\end{align*}
$$

Where X = proportionality factor known as Von Karman Constant. The accepted numerical value of this constant is 0.4

### 2.6 Velocity Distribution and Surface Roughness

### 2.6.1 General

When water enters a channel, the velocity distribution across the channel cross-section, owing to the presence of boundary roughness, will vary with the distance over which the water travels in the channel. If the flow is uniform and stable and if the channel is prismatic and of constant roughness, the velocity distribution will eventually reach a definite pattern. For simplicity of discussion, the following assumptions are made[17]:

1. The flow entering the channel is laminar and of uniform velocity distribution
2. No restriction exists at the entrance that will cause abrupt disturbance of the water surface and velocity distribution
3. Depth of flow is indefinitely large, so the depth of flow can be considered constant as the water enters the channel

In Figure 2.3 [17], the effect of velocity distribution due to boundary roughness is indicated by the line ABC. Outside the surface represented by $A B C$, the velocity distribution is practically uniform. Near the channel bottom and within the region $A B C$, velocity varies according to the distance from channel bottom. The region inside ABC though not distinctive is known as the boundary layer [84] and its thickness is designated by $\delta$. Since the boundary layer is not distinctive, its thickness has been defined arbitrarily in various ways. A very common definition is that the thickness $\delta$ is the magnitude of the normal distance from the boundary bottom or bed at which the velocity $u$, is equal to $99 \%$ of the limiting velocity $u_{0}$.
The effect of the boundary layer in Figure 2.4 [17], on the flow is equivalent to a fictitious upward displacement of the channel bottom to a virtual position by an amount equal to the so-called displacement thickness $\delta *$. The value of the displacement thickness generally varies from one-eighth to one-tenth of the thickness of the boundary layer, depending upon the magnitude of the Reynolds number [17].

At the beginning of the flow in the channel, the flow is entirely laminar and a laminar boundary layer is developed along the channel bed as shown by the curve $A B$, Figure 2.3. The velocity distribution in this layer is approximately parabolic. As the water travels farther along in the channel, the flow in the boundary layer will eventually



Figure 2.4: $\begin{aligned} & \text { Distribution of Velocity Over a Smooth Channel } \\ & \text { Surface [17] }\end{aligned}$
change to turbulent. The point where the change takes place is indicated by B. Downstream from B, a turbulent boundary layer is developed, as shown by $B C$. The velocity distribution in this layer can be shown analytically to be approximately logarithmic.

If the channel bottom is relatively smooth, the velocity close to the channel bottom is low; thus a very thin stable film of flow known as the laminar sublayer will be developed on the bottom. Within the laminar sublayer the flow is kept laminar. If the conditions for uniform flow exist throughout the channel, the turbulent boundary layer will be fully developed at section $C D$; thereafter the velocity distribution will have a definite pattern.

In a laboratoray channel or flume, the laminar boundary layer can be eliminated easily by placing a roughness element at the entrance. Thus, the turbulent boundary layer will be developed at the very beginning of the channel, and the total length of this zone for the full development of boundary layer can be shortened [17].

### 2.6.2 Concept of Surface Roughness

The concept of existence of a laminar sublayer in the turbulent boundary layer offers an appropriate explanation of the behaviour of bottom or bed roughness. When the bottom or bed profile of a channel is enlarged, it can be seen that the bottom or bed is composed of irregular peaks and valleys. The effective height of the irregularities forming
the roughness elements is called the roughness height, $k_{s}$. The ratio of the roughness height to the hydraulic radius, $k_{s} / R$, is known as the relative roughness.

If the roughness height is less than a certain fraction of the thickness of the laminar sublayer, the bottom or bed irregularities will be so small that all roughness elements will be entirely submerged in the laminar sublayer. Under this condition, the roughness has no effect upon the flow outside the laminar sublayer and the bottom or bed is said to be hydraulically smooth.

In connection with flow in pipes or on flat plates, Schlichting [84] and Yalin[105] have given the following conditions for a bottom or bed to be hydraulically smooth or rough :

1. Turbulent flow given by the condition $U_{\star} k_{5} / \nu \leqq 5$ is called hydraulically smooth flow. Hydraulically smooth flow is distinguished by the fact that its velocity distribution does not depend upon the size and nature of roughness, provided $k_{s} \ll$ depth of flow.
2. Turbulent flow given by the condition $U_{\star} k_{s} / v \geqq 70$ is called fully developed turbulent flow or rough turbulent flow. Rough turbulent flow is distinguished by the fact that the velocity distribution does not depend upon the viscosity $\mu$ or $V$. If the thickness of the viscous sublayer is small in comparison to the size of the roughness, then the elements of roughness
are almost totally exposed to the turbulent fluid motion. This means that the turbulence has penetrated even into the flow between the elements of roughness and hence the fully developed turbulent flow conditions exist.
3. Turbulent flow given by the condition $5 \leqq U_{*} k_{S} / v \leqq 70$ is said to be in the transitional regime and the velocity distribution is dependent on both viscosity and roughness.

### 2.6.3 Velocity Distribution

Keulegan [48] had attempted to apply the work of Prandtl [71], Karman [49] and Nikuradse $[65,66]$ to the problem of turbulent flow in open channel, mainly for the purpose of developing formulas for resistance or for mean flow velocity in forms similar to those obtained for circular pipes. Keulegan [48] developed a set of equations for velocity distribution both for the smooth walls and for rough walls. Yalin [105] simplified these equations as shown below:

For smooth walls, i.e., when $U_{\star} k_{s} / v \leqq 5$

$$
\begin{aligned}
\frac{u}{U_{*}}= & 5.75 \log \left(-\frac{Y}{k_{s}}\right)+B s \\
& B s=5.75 \log -\underbrace{U_{i}}_{v} n_{s}+5.5
\end{aligned}
$$

For Rough Walls, i.e., when $U_{*} k_{s} / \nu \geqq 70$

$$
\begin{aligned}
\frac{\mathrm{u}}{\mathrm{U}_{*}}= & 5.75 \log \left(\frac{\mathrm{y}}{\mathrm{k}_{\mathrm{s}}}\right)+\mathrm{Bs} \\
\mathrm{Bs}= & 8.5 \\
\text { where } \mathrm{u}= & \text { velocity at a distance } y \text { from the channel } \\
& \text { bed } \\
\mathrm{k}_{\mathrm{s}}= & \text { size of roughness, which can be taken } \\
& \text { equal to the particle, size } \\
\mathrm{U}_{*}= & \text { friction or shear velocity } \\
\mathrm{Bs}=^{=} & \text {a dimensionless property of the flow in } \\
& \text { the vicinity of the bed. In general, it } \\
& \text { is a function of particle Reynolds } \\
& \text { number, } \mathrm{U}_{\star} \mathrm{k}_{\mathrm{s}} / v
\end{aligned}
$$

Turbulent flow given by the condition $5 \leqq U_{*}{ }_{s} / v \leqq 70$ is said to be in the transitional regime. In the transitional regime, the velocity distribution is dependent on both viscosity and roughness. For this case the value of Bs cannot be given analytically and it must be estimated from the plot shown in Figure 2.7 [105].


Figure 2.5: Relationship Between Particle Reynolds Number and Bs [104]

### 2.7 Physical Characteristics of Sludges

The characteristics of sludges produced in water and wastewater treatments can vary greatly, due to the tremendous difference in types of wastewaters and chemicals used during treatment processes. It is important to be able to measure some of the characteristics that can be used in design and operation of water or/and wastewater treatment plants. Because of the complex nature of sludge, basic parameters are of limited value, and it, has been necessary to develop some operational parameters which can be used in practice. Some of the physical characteristics of sludges which have been used in the operation and design of a treatment plant are listed below [93]:

1. Specific Gravity: specific gravity is defined as the ratio of the weight of the material to that of an equal volume of water. Most sludges have a specific gravity of almost 1.0.
2. Solid Concentration: the relative solid and liquid fractions of a slurry are most commonly described by solids concentration, .expressed as $\mathrm{mg} / \mathrm{L}$ or percent solids. There are three types of solids (A) total (B) dissolved (C) suspended. Normally suspended solids concentration is used to describe the physical properties of sludges.
3. Settling Characteristics: sludge often can be characterized by how well the particles settle.

Settling velocity of a specific sludge is an inverse function of sludge solids concentration.
4. Particle Size: sludge particles vary not only in size but also in consistency and shape. Thus it is extremely difficult to characterize sludges by particle size, although this has been attempted by several researchers. Not only is sludge composed of many different sized particles, but these sizes change with time and test conditions.
5. Rheology: all fluids can be classified in terms of their flow properties. This field of water and wastewater engineering, has not received much attention. Although researchers have started to realize the importance of rheological properties of sludges in designing different waste treatment units, it will take time before proper design parameters are established. This physical characteristic of sluage is discussed in detail in the following section.

### 2.7.1 Rheology of Different Kinds of Sludges

Rheology is the science of the deformation and flow of matter [24]. Extensive use has been made of rheological measurements in studying the fundamental properties of suspensions such as the size and shape of particles, degree of hydration, state of aggregation, rigidity of particles, and forces acting between particles[24]. However, very few of these applications have been in the field of water and wastewater engineering.

### 2.7.1.1 Types of Fluids

Real fluids can be divided into two categories:

1. Newtonian Fluids
2. Non-Newtonian Fluids

Newtonian Fluids: Pure single - phase liquids characteristically demonstrate Newtonian behaviour, that is the shearing stress, $\tau$, is directly proportional to the rate of shear or velocity gradient, $d u / d x$, in laminar flow conditions:

$$
\begin{array}{cc}
\tau \propto & \frac{d u}{d x}  \tag{2.28}\\
\tau=\mu & \frac{d u}{d x} \\
\tau=-
\end{array}
$$

The constant of proportionality, $\mu$, for a given liquid at a given temperature is a characteristic physical constant and is known as absolute or dynamic viscosity or Newtonian viscosity. The Newtonian viscosity, $\mu$, depends only on temperature and pressure. Therefore the diagram relating shear stress and rate of shear for Newtonian fluids, the socalled 'flow-curve', is a straight line of slope $\mu$ as shown in Figure 2.6. This single constant completely characterizes the fluid [101]. Newtonian behaviour is exhibited by fluids in which the dissipation of viscous energy is due to the collision of comparatively small molecular species. All gases, liquids and solutions of low molecular weight come
into this category. Notable differences are observed in colloidal suspensions and polymeric solutions where the molecular species are large. The flow curve for such suspensions show considerable changed behaviour. from Newtonian behaviour [101].

Non-Newtonian Fluids: Non-Newtonian fluids are those for which the flow curve is not linear, i.e. the viscosity of a non-Newtonian fluid varies not only with temperature and pressure but also depends on other factors such as the rate of shear in the fluid, the apparatus in which the fluid is contained or even on the previous history of the fluid.

The real non-Newtonian fluids can be classified into two major categories:

1. Time independent non-Newtonian fluids
2. Time dependent non-Newtonian fluids

Each of these categories can be further subdivided into different types.
A. Time Independent Fluids

Time independent fluids are those fluids whose properties are independent of time. Most of the sludges fall in this category. Time independent fluids may conveniently be subdivided into three distinct types depending on the nature of their fiow curve:
i. Bingham plastic fluids
ii. Pseudoplastic fluids
iii. Dilatant fluids


Figure 2.6: Typical Flow Curves for Different Fluids

Typical flow curves for these three fluids are shown in Figure 2.6.
B. Time Dependent Fluids

Time dependent fluids are those fluids whose properties change with time when a shear force is applied. These fluids may be divided into two classes according to shear stress increase or decrease with time when the fluid is sheared at a constant rate
i. Thixotropic fluids
ii. Rheopectic fluids

### 2.7.2 Sludge as a Non-Newtonian Fluid

The classic work of Babbitt and Caldwell [12,13] is apparently the basis on which the sewage sludge is classified as a Bingham plastic. However, their conclusions were based on digested sludge. Behn [14] has summarized the work of other workers in wastewater and the weight of evidence indicates that the digested sludge behaves as a Bingham plastic. Bokil and Bewtra [15] also found the behaviour of digested sludge to be very close to Bingham plastic. Dick $[24,25]$ has done considerable work on different kinds of sludges recently, and found the sludges to behave very close to non-Newtonian, especially a Bingham plastic. Very limited work has been done with raw wastewater sludges. No information could be found in the literature on the behaviour of sludges such as alum sludge, sludge from chemically treated wastewater, primary sludge, etc.

### 2.7.3 Use of Rheological Informations

The obvious application of rheological information has been the head loss calculations when sludge is pumped and piped. However, there are other applications which might be equally useful [25]:

1. Rheological measurements provide a fundamental description of flow and deformation properties of sludges.
2. The performance of many processes for separating and treating activated sludge solids depends on physical properties of sludge. Therefore, the rheological measurements may be useful in developing an understanding of process performance.
3. Dick [26] has shown that the deviation of the thickening behaviour of activated sludge from the ideal thickening properties, as defined by Kynch [50], could be related to the yield strength of the sludge as determined by a coaxial cylinder rotational viscometer.
4. Wood and Dick [102] have demonstrated that in dissolved air pressure floatation of activated sludge, the rise rate and float concentration are related to the rheological properties of the sludges. It is reported that high yield strength values interfere with effective performance of floatation.
5. Campbell, et al. [21] have noted that due to the polymer conditioning of activated sludge, yield stress increased with polymer dose until the optimum dosage was reached.
2.7.4 Rheological Models to Represent Behaviour of Different Fluids

Bingham and Green [16] proposed the following model for a plastic material, which has come to be known as Bingham plastic:

$$
\begin{align*}
\tau=\tau_{y} & +\mu_{p} \frac{d u}{d x}  \tag{2.30}\\
\text { where } \tau & =\text { shear stress } \\
\tau_{y} & =\text { yield stress } \\
\mu_{p} & =\text { plastic viscosity } \\
\frac{d u}{d x} & =\text { rate of shear }
\end{align*}
$$

Intermediate in behaviour between plastic materials or Bingham plastic materials and dilute suspensions with altered Newtonian viscosity are suspensions displaying pseudoplastic behaviour. Because size and other characteristics of flocculent particles are influenced by the rate of shear, the effect of the particles on flow behaviour of the suspension varies with the rate of shear. The resulting shear-thinning (pseudoplastic) behaviour has
been described by Van Wazer, et al. [94] by the power function as shown below:

$$
\begin{equation*}
\tau=k_{1}\left(\frac{d u}{d y}\right)^{n} \tag{2.31}
\end{equation*}
$$

where $k_{1}=a$ constant with dimensions of viscosity $\mathrm{n}=\mathrm{a}$ dimensionless constant with a value less than one

Improved models are now available in the literature, especially in the chemical engineering field, to describe those real fluids which behave somewhere between Bingham plastic and pseudoplastic. In fact, most of the water and wastewater sludges in higher concentrations show this kind of behaviour.

The Herschel Bulkley model [27], which has been used successfully and extensively in chemical engineering to represent behaviour of several foodstuff data, is a 3 parameter model as shown below:

$$
\begin{equation*}
\mu^{\prime} \frac{d u}{(--)}=y\left(\frac{d u}{d x}\right)^{-1}+m\left(\frac{d u}{d x}\right)^{n-1} \tag{2.32}
\end{equation*}
$$

$$
\begin{aligned}
& \text { where } \begin{aligned}
\mu^{\prime}\left(\frac{d u}{d x}\right) & =\text { non-Newtonian viscosity at shear rate } \\
& \text { of } d u / d x
\end{aligned} \\
& \text { n and } m=\text { constants } \\
& \quad{ }^{\tau} y=\text { yield stress }
\end{aligned}
$$

An improvement to the Herschel Bulkley model was proposed by De Kee and Turcotte [27], with another 3 parameter model as shown below:

$$
\begin{aligned}
& -t_{1}\left(\frac{d u}{d x}\right) \\
& \mu^{\prime} \underset{(--)}{d x}={ }_{\tau_{y}}\left(\frac{d u}{d x}\right)^{-1}+\mu_{1}^{\prime} e \\
& \text { where } \\
& t_{I}=\text { time parameter } \\
& u^{\prime}=\text { viscosity parameter } \\
& { }^{\tau}{ }_{y}^{1}=\text { yield stress } \\
& \mu^{\prime}\left(\frac{d u}{d x}\right)=\text { non-Newtonian viscosity at shear rate } \\
& \text { of } d u / d x
\end{aligned}
$$

The 3 unknown parameters in this model are $\tau_{y}, t_{1}$ and $\mu_{i}^{\prime}$. This model appears to be more interesting since it contains a time constant, which may be useful in the study of materials showing time dependent behaviour.

## Chapter III

## APPARATUS AND EQUIPMENT

This experimental work was carried out in several steps using different sizes of grit particles and different types of sludge particles collected both from water and wastewater treatment plants. A laboratóry scale model of a diffused air aeration tank and a recirculating rectangular flume were used during the experiments to measure various parameters. This chapter briefly describes the details of each equipment used during the experimental work.

### 3.1 Experiments With Laboratory Flume

The flume was used during the experiments to establish critical values for the initiation of motion of different sizes of grit particles and for different types of sludges.

### 3.1.1 Description of Flume

The flume was $2.74 \mathrm{~m}(9.00 \mathrm{ft})$ long, $0.31 \mathrm{~m}(1.00 \mathrm{ft})$ deep and $0.15 \mathrm{~m}(0.50 \mathrm{ft})$ wide. A recirculation tank $0.61 \mathrm{~m}(2.00$ $f t)$ wide and $0.61 \mathrm{~m}(2.00 \mathrm{ft})$ deep was located at the bottom of the flume. This recirculation tank was used to collect and recirculate the discharge from the flume. A flow adjuster (gate valve) was provided to adjust both the depth
and the rate of flow in the flume. At the begining of the flume a constant head tank $0.91 \mathrm{~m}(3.00 \mathrm{ft})$ deep, 0.15 m ( 0.50 ft ) wide and $0.61 \mathrm{~m}(2.00 \mathrm{ft})$ long was provided. A honeycomb was placed at the entry point of the flume to stream-line the flow. The flume and the constant head tank were made of plexiglass and angle iron, whereas the recirculation tank was made of steel plates. The details of the flume are shown in Figure 3.1 and the photographs are shown in Figure 3.2.

### 3.1.2 Measurement of Velocity in the Flume

A small current meter model \# MINIFLO-PROBE 265-3 as shown in Figure 3.3, made by Kent Lea was used to measure the velocity of flowing water close to the bed during the critical conditions of entrainment. The measuring range of the equipment was from $0-1.3 \mathrm{~m} / \mathrm{s}$ with an accuracy of $\pm 2 \%$. At the upper limit, however, at a lower velocity range a higher error is expected. This current meter was calibrated against March McBirney Electromagnetic current meter, which is discussed in detail in section 3.3.4.


Figure 3.1: Flume Used for Experiments



### 3.2 Determination of Rheological Properties of Different Types of sludges

A Brookfield Synchro-Lectric Viscometer was used to determine the rheological properties of different types of sludges both before and after thickening by settling. Some of the results obtained using the Brookfield Viscometer were rechecked by Rheomat 30 Viscosity Meter.

### 3.2.1 Viscosity Meters

The rheological properties of both wäter and wastewater sludges were determined using Brookfield Synchro-Lectric Viscometer Model \# LVF, Figure 3.4. It was a four speed, 60, 30, 12 and 6 rpm , rotational co-axial type viscosity meter with four different types of spindles. This equipment worked on the principle of measuring the force required to rotate a spindle with a constant known speed, RPM, in a fluid, and this force value was used to calculate the viscosity. The speed of the spindle gave the rate of shear in $1 / s$, and the force required to rotate the spindle in that fluid gave the shear stress. Out of the four spindles equipped with the Brookfield Viscometer, only spindle \#l was used for all the tests. This spindle was a cylindrical shaped with 9.421 mm (0.371 in.) radius and 74.93 mm (2.95 in.) effective length.

Some of the tests were repeated by using a very sophisticated and sensitive viscosity meter made by Contraves (Switzerland), Model \# Rheomat 30, to check the


Ficure 3.4: Brcokfield Synchro-Lectric Viscometer


## Figure 3.5: Contraves, Model \# Rheomat 30 Viscosity Meter

accuracy of the Brookfield Viscometer. This viscosity meter Figure 3.5, also was a rotational co-axial type with many options. The range for the rate of shear obtained by this equipment was fairly wide and eight different rates of shear were used. The calibration procedure of the Brookfield Viscometer is presented in Appendix A.

### 3.2.2 Water Bath

A water bath, Figure 3.6, was used to maintain a constant temperature of the sample during the experiments to determine the rheological properties of sludges using viscosity meters. Since rheological properties are very sensitive to temperature, it was made sure that the temperature of the samples remained at $20^{\circ} \mathrm{C}$ during these experiments.


Ficure 3.6: Water Eath Used during Experiments on Sludces

### 3.3 Experiments With Aeration Tank Model

A laboratory scale tank was used to obtain velocity profile and mixing behaviour under various operating conditions of air agitation.

### 3.3.1 Aeration Tank Model

The model tank was rectangular in shape with a line diffuser placed along the length of the tank, Figure 3.7. Photographs showing different mixing conditions are shown in Figure 3.8. The Aeration tank was $2.4 \overline{4} \mathrm{~m}(8.00 \mathrm{ft})$ wide, $0.69 \mathrm{~m}(2.25 \mathrm{ft})$ long and $1.22 \mathrm{~m}(4.00 \mathrm{ft})$ high. The width of the tank was altered by using a movable partition made of iron plate. The tank itself was made of 12.5 mm ( 0.5 in. ) thick plexiglass segments reinforced with iron frame. The diffuser consisted of 25 mm (1.0 in.) diameter copper pipe $0.69 \mathrm{~m}(2.25 \mathrm{ft})$ long, with fourteen 3 mm (1/8 in.) diameter orifices 50 mm (2 in.) apart and facing the surface of the tank. The diffuser covered the entire length of the tank:


Figure 3.7: Aeration Tank Model Used for Experiments



Figure 3.9: Safeguard Rotameter Model No: 5-HCFXB and Float No: 3/4-EGNV-4

### 3.3.2 Measurement of Air Flow Rate

The air flow to the tank was monitored by using a Safeguard Rotameter Model No: 5-HCFXB and Float No: 3/4-HGNV-4, supplied by S.K. Instruments. The scale of rotameter was precalibrated for air at STP (14.7 psia and $70^{\circ}$ F) in Standard Cubic Feet Per Minute, SCFM, in the range of 0-20 SCFM with an accuracy of $\pm 1 \%$. The picture of rotameter is shown in Figure 3.9.

### 3.3.3 Measurement of Air Pressure

The pressure of air diffused into the aeration tank through line diffusers was measured using a Bourdon-Tube type pressure gauge, supplied by Thermo Gauge. This pressure gauge was calibrated for the pressure range of $0-30$ psig. The air pressure in the aeration tank was held steady using a constant pressure control valve in the air supply line. The picture of pressure gauge is shown in Figure 3.10.


Figure 3.10: Air Pressure Gauge Used during Experiments

### 3.3.4 Measurement of Velocity

The accurate measurement of horizontal velocity was necessary in the development of the model. The velocity was measured at the middle of the tank width at different depths in order to develop velocity profiles. Two different types of velocity meters were used for this purpose as described below:

1. Detflow Ultrasonic Velocity Meter
2. Marsh McBirney Electromagnetic Current Meter
3. Detflow Ultrasonic Velocity Meter: A Detflow Ultrasonic Velocity Meter model \# 3 CM was used for the velocity measurement. This meter was designed on Ultrasonic Doppler Principle. The velocity measuring range of this meter was $0-3 \mathrm{~m} / \mathrm{s}$. The expected error in the measurement of velocity was $\pm 2 \%$ of the actual velocity at the upper range and as high as $\pm 20 \%$ in the lower range of velocities. This meter had a cylindrical shaped probe which was placed facing the direction of flow at the required depth and position at which the velocity measurement was desired. The meter was precalibrated by the manufacturer for the velocity measurement in water. Precaution was taken to keep the probe clean of any kind of deposit, oil and grease. A picture of the Detflow Ultrasonic Velocity Meter is shown in Figure 3.11.


## Figure 3.11: Detflow Ultrasonic Velocity Meter

Marsh McBirney Electromagnetic Current Meter: A Marsh McBirney Electromagnetic Current Meter, Model \# 201M was used for the velocity measurement. This meter worked on the principle of Faraday's Law. When water, as a conductor, moved in a magnetic field, a voltage was produced which was linearly proportional to the water velocity. The velocity range was $0-3 \mathrm{~m} / \mathrm{s}$. The accuracy of this velocity meter was expected to be $\pm$ $2 \%$ in the upper range; however, in the lower range of velocities, this error could go as high as $\pm 20 \%$. This meter had a conical shaped probe which was placed at the required depth and position facing the direction of flow. The probe was mounted on a clamp made of plexiglass (non-magnetic material) to avoid any kind of.interference in the magnetic field formed by the probe. The probe was protected from getting damaged and kept clean of any kind of deposit, oils, grease etc.. The meter was calibrated by the manufacturer to measure the velocity directly in water. The picture of Marsh McBirney Electromagnetic Current Meter is shown in Figure 3.12 .

Velocities were measured using both the meters at the same time to compare the readings.


Figure 3.12: Marsh McBirney Electromagnetic Current Meter

## Chapter IV

## EXPERIMENTAL PROCEDURE

The experimental work was divided into four major parts as described below:
a. Measurement of velocity during critical conditions for the initiation of motion of different sizes of grit particles in a flume.
b. Measurement of velocity during critical conditions for the initiation of motion of different kinds of sludge particles in a flume. c. Determination of rheological properties of different kinds of sludges.
d. Measurement of velocity in the aeration tank under different operating conditions.

### 4.1 Experiments in Laboratory Flume with Grit Particles

The experiments in the laboraotry flume were conducted to measure horizontal velocities at different locations and at different depths during the critical conditions.

### 4.1.1 Preparation of Grit Samples

The grit samples were collected from the West Windsor Pollution Control Plant. The grit was cleaned several times with water to wash off all the decomposable organic matter and then dried in the oven. The washed grit was sieved and separated into various sizes. Some bigger size gravel particles were also included in the experiments to extend the scope of this study. Information on different grit and gravel sizes used in these experiments are provided in Table 4.1 and Table 4.2.

Table 4.1 - SIZE CLASSIFICATION OF GRIT USED DURING THE EXPERIMENTS

| PASSED |  | RETAINED |  | $\begin{aligned} & \text { GEDMEIRIC MEAN } \\ & \text { SIZE, mm } \end{aligned}$ | GEDMEIRIC MEAN PARTICLE SIZES USED IN EXPERINENIS, m |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Sieve No. | Sieve Opening, mm | Sieve No. | Sieve Opening, mm |  |  |
|  |  | 8 | 2.380 |  |  |
| 8 | 2.380 | 10 | 2.000 | 2.1817 |  |
| 10 | 2.000 | 14 | 1.400 | 1.6733 | 1.6733 |
| 14 | 1.400 | 16 | 1.180 | 1.2853 |  |
| 16 | 1.180 | 18 | 1.000 | 1.0860 | 1. 0860 |
| 18 | 1.000 | 20 | 0.850 | 0.9220 |  |
| 20 | 0.850 | 25 | 0.710 | 0.7770 | 0.7770 |
| 25 | 0.710 | 30 | 0.600 | 0.6527 |  |
| 30 | 0.600 | 35 | 0.500 | 0.5477 | 0.5477 |
| 35 | 0.500 | 40 | 0.425 | 0.4610 |  |
| 40 | 0.425 | 45 | 0.355 | 0.3880 | 0.3880 |
| 45 | 0.355 | 50 | 0.300 | 0.3263 |  |
| 50 | 0.300 | 60 | 0.250 | 0.2739 | 0.2739 |
| 60 | 0.250 | 80 | 0.180 | 0.2121 | 0.2121 |
| 80 | 0.180 |  |  |  |  |

Table 4.2 - SIZE CLASSIFICATION OF GRAVEL USED DURING EXPERIMENTS

| PASSED |  | RETAINED |  | GEOMEIRIC MEAN SIZE, mm | GEOMEIRIC MEAN PARTICLE SIZES USED IN EXPERIMENTS, mm |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Sieve No. | Sieve Opening, mm | Sieve No. | Sieve Opening, mm |  |  |
| 3/4" | 19.050 | 5/8" | 15.875 | 17.40 | 17.40 |
| 5/8" | 15.875 | 1/2" | 12.700 | 14.20 | 14.20 |
| 1/2" | 12.700 | 7/16" | 11.633 | 12.20 | 12.20 |
| 7/16" | 11.633 | 3/8" | 9.525 | 10.50 | 10.50 |
| 3/8" | 9.525 | 5/16" | 7.925 | 8.70 | 8.70 |
| 5/16" | 7.925 | 4 | 4.750 | 6.10 |  |
| 4 | 4.750 | 8 | 2.380 | 3.40 | 3.40 |

### 4.1.2 Determination of Specific Gravity of Grit and Gravel Particles

The specific gravity of the grit particles collected from the waste treatment plant and larger size gravel particles, was determined by measuring the volume of water displaced by the known mass of grit and gravel particles. For both types of particles, experiments were repeated five times and the average values were used for subsequent calculations.

### 4.1.3 Measurement of Velocity During Critical Conditions

A laboratory flume, Figure 3.1, was used to establish the critical conditions for initiation of the motion of particles. The flume was completely levelled during the experiments and a water depth of 150 mm to 175 mm was maintained in the flume. Since the flume length was short, the flume bed was roughened with the same size of particles as were used for scouring during the experiment, in order to develop the flow fully. However, in the middle of the flume, about 650 mm test section was not roughened and this section was used to observe the movement of particles. The loose grit particles were placed uniformly in this test section for determining the critical conditions to initiate the motion of the particles. The sizes of all grit and gravel particles used in the experiments are listed in Table 4.1 and Table 4.2. It was assumed that the critical conditions had been established when the particles just started moving.

For each size of particle, the experiment was repeated at least twice to confirm the established critical conditions. The velocities at different depths and at different locations along the length of the flume were measured. The Kent Lea current meter was used to measure the velocities in the flume. The velocity along the length of the flume was measured at two locations, $1.83 \mathrm{~m}(6.00 \mathrm{ft})$ and $2.13 \mathrm{~m}(7.00$ ft) from the reservoir. Along the depth, velocities were measured at 7.6 mm and at 38 mm above the bed, and subsequent readings were taken at 38 mm intervals.

### 4.2 Experiments in Laboratory Flume with Sludge Particles

Experiments were conducted to measure the horizontal velocity in the laboratory flume at different locations and depths during the critical conditions for the initiation of motion of the sludge particles. Different types of sludges, Table 4.3. were studied. Only the settled sludge particles were used in the experiment. Before starting the experiment, the flume was filled with tap water and a low velocity was maintained in the flume by adjusting the valve so that the sludge particles would not be washed away. Then a layer of sludge was spread on the flume bed. The velocity of water in the flume was slowly increased by opening the valve until the sludge flocs started to move. At this critical condition, the velocity of flow was measured at different locations along the length of the flume and also along the
depth of the flow. Each set of experiment was repeated at least twice to make sure that a true critical condition had been achieved. The Kent Lea Current Meter was used for the measurement of velocity. The flume was completely levelled during the experiment and a constant water depth of 150 mm to 175 mm was maintained in the flume. The velocity along the length of the flume was measured at two locations, 1.83 $\mathrm{m}(6 \mathrm{ft})$ and $2.134 \mathrm{~m}(7 \mathrm{ft})$ from the reservoir. Along the depth, velocities were measured at 7.6 mm and at 38 mm above the bed, and subsequent readings were taken at 38 mm intervals.

Table 4.3 - TYPES OF SLUDGES USED AND THEIR SOURCES

| SLUDGE TYPE | WATER/WASTENATER TREATMENT PLANT | IOCATION/SOURCE |
| :--- | :--- | :--- |
| Mixed liquor, biological sludge | Little River Pollution Control Plant, Windsor | Aeration tank |
| Alum sludge | Water Treatment Plant, Amherstburg | Clarifier underdrains |
| Physico chemical sludge | West Windsor Pollution Control Plant, Windsor | Secondary clarifiers |
| Physico chemical sludge | West Windsor Pollution Control Plant, Windsor | Secondary clarifier <br> underdrains |
| Secondary digested sludge | Wastewater Treatment Plant, Chatham | Secondary digester <br> underdrains |
| Mixture of primary and secondary |  |  |
| sludges | Wastewater Treatment Plant, Chatham | Primary clarifier <br> underdrains |

### 4.3 Determination of Properties of Sludges

The following properties of all types of sludges were determined during each experiment:
a. suspended solids concentration
b. zone settling rate
c. rheological properties of sludge

### 4.3.1 Suspended Solid Concentration

The total suspended solid concentration in all sludge samples, both before and after thickening by settling, were determined using the procedure given in the Standard Methods [86]. A 10 to 15 mL well mixed sludge sample was filtered through a glass fibre filter paper, Whatman \# 541. The filter paper with the retained material was dried at 103 to 105 degrees $C$ for at least 1 hour and then the residue was weighed to calculate the suspended solids concentration.

### 4.3.2 Zone Settling Rate

In order to study the settling properties of sludges, the zone settling rate for all types of sludges was determined in a settling column using the procedure given in the Standard Methods [86]. At high concentrations of suspended solids, suspensions settle in zone settling regime. This type of settling takes place under quiescent conditions and is characterized by a distinct interface between the supernatant liquor and sludge zone. The height of this distinct interface was measured with time.

### 4.3.3 Rheological Properties of Sludges

The rheological properties of all types of sludges were determined using a Brookfield Viscometer with spindle \#l (cylindrical shaped). Both the rate of shear and the torque input to maintain that rate of shear were obtained with the viscosity meter. Then these two parameters were used to calculate other characteristics of sludges. Since rheological properties of any non-Newtonian fluid are sensitive to change in temperature, a constant temperature was maintained by using a water bath for each sample during the experiment. Since sludge suspensions have a tendency to form a layer of supernatant and sludge flocs, all samples were stirred periodically using a glass stirrer. The Brookfield Viscometer Model \# LVF is a four speed viscosity meter; therefore, only four readings could be obtained for each sample. Each set of experiment was repeated at least twice, and the average values were used for further calculations.

### 4.4 Experiments With Aeration Tank Model

The experiments in the aeration tank filled with the tap water were carried out by measuring the velocity under different operating conditions. The operating conditions which were varied during the experiments are listed below:
a. Location of line diffuser in the liquid depth
b. Air flow rate
c. Tank Width
d. Liquid depth in the tank

Different combinations of these variables were used, as shown in Table 4.4. and the horizontal velocities at different depths were measured so that the velocity profile could be developed. Two different types of velocity meters were used simultaneously to measure and compare the velocity readings. Visual observations on circulations patterns were also recorded under different operating conditions.
Table 4.4 - DIFFERENT OPERATING CONDITIONS USED DURING EXPERIMENTS WITH AERATION TANK


Table 4.4 - DIFFERENT OPERATING CONDITIONS USED DURING EXPERIMENTS WITH AERATION TANK (cont'd)

| WATER DEPTH, $m$ | DIFFUSER SUBMERGENCE, $m$ | AIR FIOW RATE <br> (Rotameter Reading) <br> SCFM | TANK WIDTH, m |
| :---: | :---: | :---: | :---: |
| 1.10 | 1.016 | 14.2 | 2.44 |
|  | 0.955 | 10.8 | 2.21 |
|  | 0.828 | 8.1 | 1.98 |
|  | 0.795 | 3.2 | 1.75 |
|  | 0.694 |  | 1.52 |
|  | 0.617 |  | 1.29 |

## Chapter V

## THEORY AND COMPUTATIONAL PROCEDURES

The theory and computational procedures used in this research are discussed in this chapter.

### 5.1 Concept of Critical Shear Stress for the Design of Grit Chamber

Grit particle characteristics are the most important parameters in the design and operation of grit chambers in wastewater treatment plants. Generally, the grit chambers are designed to remove all grit particles that are retained on a $65-$ mesh screen ( 0.21 mm opening), and have a specific gravity of 2.65. However, many grit chambers have been designed to remove grit particles that are retained on a 100-mesh screen ( 0.15 mm opening).

The design of gravity type grit chamber is generally based upon the concept of discrete particle settling under ideal conditions. It is assumed that (i) all particles settle in accord with Newton's law, (ii) liquid velocity is the same in all parts of the chamber, and (iii) there are no eddies in the flow stream. However, in an actual chamber the velocity is not uniform and also there are eddies present due to turbulence. These eddies retard settling. An increase
in chamber velocity increases the scour of the settled material. Therefore, it is the scouring process and not the settling process which determines the design flow velocity for grit chambers.

Camp [18] proposed the following equation for mean critical scouring velocity,$V_{C}$. It was based on experimental and theoretical studies by Shields [81] on the movement of granular particles in flowing streams.

$$
\begin{equation*}
v_{c}=\sqrt{-\frac{8 \beta}{f}-g\left(s_{s}-1\right) d} \tag{5.1}
\end{equation*}
$$

It is apparent from this Equation that the depth of flow in the channel has no influence on the critical mean scouring velocity. This is not quite true because, even if the mean velocity of flow in a channel remains the same for different depths of flow, the velocity profile will change with depth. . Consequently, the scouring velocity on the channel bed is influenced by the depth of flow. Therefore, a new approach to design grit chambers has been developed on the concept of critical bed shear stress rather than critical mean velocity.

The bed shear stress in a fully developed flow is lower than the bed shear stress in an under developed flow for the same mean velocity, which again justifies the use of the concept of bed shear stress rather than mean velocity for grit chambers design.

The critical bed shear stress of a sediment particle is defined as the minimum boundary shear stress necessary to initiate the motion of that particle. Its magnitude depends on a number of factors including:
a. densities of particle and fluid
b. size of particle
c. viscosity of fluid, which in turn varies with the fluid temperature

### 5.1.1 Shear or Friction Velocity

In a uniform flow, the shear force, $F$, is equal to the effective component of the gravity force acting on the body of water, parallel to the channel bottom and can be written as [17]:

$$
\begin{aligned}
& F=\gamma_{f} A L s \\
& \text { Where } \gamma_{f}=\text { unit weight of water } \\
& A=\text { area of cross-section } \\
& L=\text { length of channel reach } \\
& s=\text { slope of channel }
\end{aligned}
$$

Thus the average value of the shear force per unit wetted area or simply shear stress, $\tau{ }^{\prime}$, is equal to:

$$
\begin{align*}
& \tau_{0}=-\gamma_{f}^{P_{e}}{ }^{\text {ALs }}=\gamma_{f} R s  \tag{5.3}\\
& \text { Where } P_{e}=\text { wetted perimeter } \\
& \quad R=\text { hydraulic mean radius }
\end{align*}
$$

The shear or friction velocity, $U_{*}$, is defined as:

$$
\begin{align*}
& U_{*}=\sqrt{-\frac{\tau}{\rho_{f}}}=\sqrt{\frac{Y_{f}^{R S}}{\rho_{f}}}=\sqrt{g R s}  \tag{5.4}\\
& \text { Where } \rho_{f}=\text { density of fluid }
\end{align*}
$$

Under critical condition to initiate particle movement, the shear stress becomes critical shear stress and the shear or friction velocity at this point is called critical shear or friction velocity, $U_{*_{C}}$.

$$
\begin{align*}
U_{*_{C}} & =\sqrt{\frac{\tau_{-}}{\rho_{f}}}  \tag{5.5}\\
& \text { Where } \tau_{o c}=\text { critical shear stress }
\end{align*}
$$

The value of shear or friction velocity, $U_{*}$, changes with wall friction. Therefore, to calculate the value of $U_{*}$, the equations of velocity distribution in an open channel flow have to be obtained as discussed in the following section.

### 5.1.2 Velocity Distribution in Grit Chamber

Generally, the grit chambers have long and narrow rectangular sections and resemble open channels. The flow in a grit chamber is generally found to be fully developed turbulent flow. In a fully developed turbulent flow, the velocity distribution is logarithmic and is influenced by the regime of flow. Whether the regime of flow is
hydraulically smooth or rough turbulent, is determined by the particles Reynolds number, $U_{*}{ }^{\prime} k_{s} / v$, using the following conditions:
a. Turbulent flow with $U_{*} k_{s} / \nu \leqq 5$ is called hydraulically smooth flow. Hydraulically smooth flow is distinguished by the fact that its velocity distribution does not depend upon the size and nature of roughness, provided $k_{s} \ll$ depth of flow.
b. Turbulent flow with $U_{\star} k_{S} / v \geq 70$ is called hydraulically rough turbulent flow or fully developed turbulent flow Rough turbulent flow is distinguished by the fact that the velocity distribution does not depend upon the viscosity $\mu$ or $V$. If the thickness of the viscous sublayer is small in comparison to the size of the roughness, then the elements of roughness are almost totally exposed to the turbulent fluid motion. This means that the turbulence has penetrated even into the flow between the elements of roughness and hence the fully developed turbulent flow conditions exist.
c. Turbulent flow given by the condition $5 \leqq U_{*} k_{S} / v$ $\leqq 70$ is said to be in the transitional regime and the velocity distribution is dependent on both viscosity and roughness.

The equations which have been used for the determination of velocity distribution are shown below:

For Smooth Walls, i.e., when $U_{\star} k_{s} / v \leqq 5$

$$
\begin{aligned}
& \frac{u}{u_{\star}}=5.75 \log \left(-\frac{y}{\mathrm{k}_{\mathrm{s}}}\right)+\mathrm{Bs} \\
& \text {----[5.6.a] }
\end{aligned}
$$

$$
\begin{aligned}
& \text { [5.6.b] }
\end{aligned}
$$

For Rough Walls, i.e., when $U_{*} k_{s} /: v \geqq 70$

$$
\begin{array}{rlr}
-\frac{\mathrm{u}}{\mathrm{U}_{*}^{*}} & =5.75 \log \left(\frac{\mathrm{Y}}{\mathrm{k}_{\mathrm{s}}}\right)+\mathrm{Bs} & --[5.7 . \mathrm{a}] \\
& \mathrm{Bs}=8.5 & ---[5.7 . \mathrm{b}]
\end{array}
$$

where $u=$ velocity at a distance $y$ from the channel bed
$k_{s}=$ size of roughness, which can be taken to be equal to the particle size
$U_{*}=$ friction or shear velocity
Bs $=$ a dimensionless property of the flow in the vicinity of the bed. In general it is a function of particle Reynolds number ( $U_{*} k_{s} / \nu$ )

Turbulent flow with $5 \leqq U_{*} k_{S} / v \leqq 70$ is said to be in the transition regime. In the transition regime, the velocity distribution is dependent on both viscosity and roughness. For this case the value of Bs cannot be obtained analytically and must be estimated.

Using Equations 5.6 and 5.7 , the value of shear or friction velocity, $U_{*}$, can be calculated, provided a point velocity, $u$, at a given depth, $y$, from the bed is known. The constant, Bs, can be obtained by calculating the value of particle Reynolds number for different grit particles.

### 5.1.3 Mean Velocity

The value of mean velocity can be calculated if the location of mean velocity along the depth, i.e. distance from channel bed, $Y$, is known. The location of the mean velocity in a channel flow can be obtained both for hydraulically smooth and rough turbulent regimes using Equations 5.6 and 5.7 as shown below [105]:
5.1.3.1 For Hydraulically Smooth Regime, $u_{\star} k_{s} / v \leqq 5$

Eq. 5.6 can be written as:

$$
\begin{equation*}
\frac{u}{\bar{u}_{*}}=2.5 \ln \left[9.0 \frac{U_{*} Y}{v}\right] \tag{5.8}
\end{equation*}
$$

The value of the mean or average velocity is given by:

$$
\begin{equation*}
u_{m}=-\frac{1}{(y-\delta)} \int_{\delta}^{y} u d y \tag{5.9}
\end{equation*}
$$

$$
\text { Where } \begin{aligned}
u_{m} & =\text { mean or average velocity } \\
\delta & =\text { laminar layer thickness } \\
y & =\text { depth of water } \\
u & =\text { point velocity }
\end{aligned}
$$

Substituting the value of $u$ from Eq. 5.8 into Eq. 5.9 and solving it with the assumption that $\delta \ll y$, (ratio $\delta / y$ would even be smaller and can be neglected), gives

$$
\frac{\mathrm{U}_{\mathrm{m}}}{\mathrm{U}_{*}}=2.5 \ln \left[9.0 \frac{\mathrm{U}_{\star} \mathrm{Y}}{v}\right]-2.5
$$

$$
---[5.10]
$$

$$
\begin{equation*}
\frac{u_{\underline{m}}}{U_{\ddot{\star}}}=2.5 \ell n\left[3.32 \frac{U_{\star} Y}{v}\right] \tag{5.11}
\end{equation*}
$$

From Equations 5.8 and 5.11, the value of depth, $Y$, can be calculated at which the point velocity will be equal to the mean velocity, $u_{m^{\prime}}:$

$$
\begin{equation*}
Y_{m}=0.368 \mathrm{y} \tag{5.12}
\end{equation*}
$$

5.1.3.2 For Rough Turbulent Regime, $U_{*} k_{S} / \nu \geqq 70$ Eq. 5.7 can be written as:

$$
\begin{equation*}
\frac{\dot{\mathrm{u}}}{\mathrm{U}_{*}}=2.5 \ln \left(30.0 \frac{\mathrm{Y}}{\mathrm{k}_{\mathrm{s}}}\right) \tag{5.13}
\end{equation*}
$$

The value of the mean or average velocity is given by:

$$
\begin{equation*}
u_{m}=-\frac{1}{\left(y-k_{s}\right)} \int_{k_{s}}^{y} u d y \tag{5.14}
\end{equation*}
$$

Where $k_{s}=$ size of roughness, which can be taken equal to the particle size

Substituting the value of $u$ from Eq. 5.14 into Eq. 5.15 and solving it with the assumption that $k_{s} \ll y$, (ratio $k_{s} / y$ would even be smaller and can be neglected), gives:

$$
\begin{align*}
& \frac{u_{m}}{u_{*}}=2.5 \ln \left[30.0-\frac{y_{-}}{k_{s}}\right]-2.5  \tag{5.15}\\
& \text { or } \quad \frac{u_{m}}{U_{*}}=2.5 \ln \left[11.0-\frac{y_{-}}{k_{s}}\right] \tag{5.16}
\end{align*}
$$

From Equations 5.13 and 5.16, the value of depth, $y$, can be calculated at which the point velocity will be equal to the mean velocity, $u_{m^{\prime}}$ :

$$
\begin{equation*}
\underset{\mathrm{m}}{\mathrm{y}}=0.368 \mathrm{y} \tag{5.17}
\end{equation*}
$$

Therefore, from the above derived equations, it is concluded that the location of mean velocity is the same relative to the depth of flow, $y$, both in hydraulically smooth or rough turbulent regimes.

### 5.1.4 Application

The application of the above concept of critical shear stress in practice is discussed below:
a. Knowing a point velocity, $u$, at any depth, $Y_{1}$, obtained from a channel or a flume during critical conditions of entrainment, the shear or friction velocity, $U_{*}$, can be estimated from Equation 5.6 or 5.7.
b. Using this value of shear or friction velocity, $U_{*}$, and the known total depth of flow, $y$, in a channel or flume, the mean or average velocity, $u_{\dot{m}^{\prime}}$ can be obtained from Equation 5.6 or 5.7 for $Y_{m}=0.368 \mathrm{Y}$.
c. The critical shear stress value for this particular kind of particle can be obtained from Eq. 5.4, where density of fluid (water), $\rho_{f}$, is known.
d. These mean velocity and critical shear stress values can be used for design of grit chambers.

### 5.2 Concept of Critical Shear Stress Applicable to Sludge

In the design of different water and wastewater treatment units, the knowledge of the characteristics of flocs or sludge particles is very important. Generally, the aeration tank in wastewater treatment and the flocculator in the water treatment are designed to enhance the size and the density of flocs without shearing or breaking them. These treatment units should not allow the settling of these flocs. All the settling and removal of flocs takes place in a settling or sedimentation tank. Therefore, in the aeration tank or in the flocculator, it can be assumed that the bed is smooth and the flow regime is turbulent. The shearing stress close to the bed of these treatment chambers has to be higher than the critical bed shear required to keep all the flocs in suspension all the time. Eqs. 5.6 and 5.5 can be applied to obtain the critical bed shear stress for different types of sludge particles, using the point velocity obtained in the flume close to the bed. Combining Eqs. 5.6.a and 5.6.b yield:

$$
\begin{equation*}
\frac{u}{U{ }_{* C}}=5.5+5.75\left(-\frac{Y_{\star_{C}}}{v}\right) \tag{5.18}
\end{equation*}
$$

$$
\text { Where } \begin{aligned}
v & =\text { kinematic viscosity, } \mathrm{m}^{2} / \mathrm{s} \\
& =1.01 \times 10^{-6} \mathrm{~m}^{2} / \mathrm{s} \text { at } 20^{\circ} \mathrm{C}
\end{aligned}
$$

### 5.3 Rheological properties of Sludge

In this section, the analysis of the rheological properties of different types of sludges and their use in obtaining shear stress values required in various water and wastewater treatment units is discussed. Generally this shear stress should be just enough to keep the sludge flocs in suspension without shearing them. Appropriate models to calculate yield stress for non-Newtonian fluids are also discussed.

### 5.3.1 Devolopment of Equation for the Rate of Shear and Shearing Stress

At least two experimental measurements are necessary on any non-Newtonian fluid in order to define its rheological properties, whereas a Newtonian fluid requires only one measurement, namely the viscosity. The rheological properties for any fluid can be determined by the direct relation between shear stress, $\tau$, and shear rate, $d u / d x$, by subjecting the fluid sample to a uniform rate of shear in a suitably designed instrument and measuring the corresponding shear stress. Viscometers using this principle are usually rotational instruments of the coaxial cylinder type.

The principle of operation of the coaxial-cylinder viscometer is shown in FIGREF REFID=F501.. The fluid is confined between long vertical coaxial cylinders, one of which can be rotated at different speeds, while the torque, $M$, on the other is measured. The variation of torque, $M$,
with speed, $w$, can be interpreted to give the relation between shear stress, $\tau$, and rate of shear, $d u / d x$.

Following are the assumptions made in this approach [94]:
a. Liquid is incompressible
b. Motion of liquid is laminar
c. Streamlines of flow are circles on the horizontal plane perpendicular to the axis of rotation (i.e. the velocity is a function only of radius; radial and axial flows are assumed to be equal to zero)
d. Motion is steady - all time derivatives in the equations of continuity and motion are zero e. There is no relative motion i.e. no slippage between the surface of the cylinders and the fluid in immediate contact with the cylinders f. Motion is two dimensional
g. System is isothermal

Assumption 3, implies that centrifugal forces are neglected, an assumption that is valid for small values of angular velocity.

Assumption 6, means neglecting the edge and end effects. This assumption also neglects normal forces ( cross-viscosity, Weissenberg effect, etc.).

The relationship between angular velocity, $\omega$, and linear velocity, $v$, is used to obtain the velocity gradient. It has been assumed that the inner cylinder or bob is rotating at an angular velocity, w.


## Figure 5.1: Principle of Operation of Coaxial-Cylindrical Visccsity Meter

The linear velocity, $v$, at any distance, $r$, from the axis given by:
$v=\mathbf{r} \omega$
----[5.19]

Similarly, the linear velocity, (v+dv), at a distance, $d r$, from , $r$, when the angular velocity at that point becomes ( + d ) is given by:
$(v+d v)=(\omega+d \omega)(r+d r) \quad-\cdots-[5.20]$
Solving Eq. 5.20, after neglecting the second order term:
$\frac{d v}{d r}=\omega+r \frac{d \omega}{\frac{d r}{d r}}$

In this Equation the first term, $\omega$, is the angular velocity of all the apparatus if no shearing takes place. Therefore, the internal stresses are derived from the second term $r(d \omega / d r)$ :

By definition, the relation between shear stress and rate of shear in Newtonian fluid is:

$$
\begin{equation*}
\tau=\mu\left(-\frac{d v}{d r}\right)=\mu\left(-\frac{d u}{d x}\right) \tag{5.22}
\end{equation*}
$$

$$
\begin{equation*}
\tau=\mu\left(-r \frac{d \dot{\omega}}{d r}\right) \tag{5.23}
\end{equation*}
$$

Torque $M=$ Shearing Stress $x$ Surface Area of Bob

$$
\mathbf{x} \text { Radius of the Bob }
$$

$$
\begin{equation*}
=\tau \times 2 \pi r h \times r \tag{5.24}
\end{equation*}
$$

Substituting the value of $\tau$ from Eq. 5.22 and solving it for $d \omega$ :

$$
-d \omega=\frac{M}{2 \pi h \mu} \frac{d r}{(r)^{3}}
$$

The angular velocity is equal to zero at the wall of the outer cylinder for the condition of no slippage.

If the radius of the outer cylinder (container) $=R_{c}$ and the radius of the inner cylinder $(b o b)=R_{b}$ then:
integration between $\omega=0$ and $\omega=\omega$, for $r=R_{c}$ and $r=R_{b}$, yields
$\int_{0}^{\omega}-\mathrm{d} \omega=\int_{R_{c}}^{R_{b}} \frac{M}{2 . \pi h \mu} \quad-\frac{d r}{r^{3}}$
$-\omega=-\frac{M}{4 \pi h \mu} \frac{1}{\left.R_{b}{ }^{2}-\frac{1}{R_{c}^{2}}\right]}$ :
$\mu=-\frac{M}{4 \pi \cdot h \omega} \frac{R_{b}{ }^{2}-R_{c}^{2}}{R_{b}^{2}{ }^{2}{ }_{c}^{2}}$

Since $\mu=$ shear stress/ rate of shear $=\tau /(d v / d r)$, therefore, Eq. 5.28 can be divided into two parts:

The rate of shear is given by
$-\frac{d v}{d r}=\frac{-2 \omega}{r^{2}}\left(\frac{R_{b}^{2} R_{c}^{2}}{R_{c}^{2}}-\frac{R_{b}}{2}\right)$
and the shear stress is given by

$$
\begin{equation*}
\tau=\frac{--M}{2 \pi r^{2} h} \tag{5.30}
\end{equation*}
$$

In case of plastic fluids such as sludges, the observed shear stress, $\tau$, becomes [94]:

$$
\begin{align*}
& =\mu_{p} \frac{d v}{d r}+\tau_{y}  \tag{-}\\
& \text { Where } \tau_{y}=\text { yield stress }
\end{align*}
$$

and viscosity for plastic fluids, $\mu_{p}$, is called plastic viscosity or apparent viscosity.

In practice the rate of shear is determined at the surface of the bob (spindle). Therefore, $r$, becomes equal to $R_{b}$ and Eq. 5.29 for rate of shear is reduced to

$$
\begin{equation*}
\frac{d v}{d r}=2 \omega \quad\left(\frac{R_{c}^{2}}{R_{c}^{2}-R_{b}^{2}}\right) \tag{5.32}
\end{equation*}
$$

and the Eq. 5.30 for Shear Stress becomes

$$
\begin{equation*}
\tau^{\prime}-\tau_{y}=-\frac{M}{2 \pi R_{b}^{2}} \bar{L}^{---} \tag{5.33}
\end{equation*}
$$

Where $L=$ effective length of the spindle

All above mentioned equations are developed based on Newtonian fluids' theory. However, the validity of these equations for non-Newtonian fluids also has been proved [87].
5.3.1.1 Computation of Rate of Shear and Shear Stress The rate of shear and shear stress using the Brookfield Viscometer were calculated with the help of Eq. 5.32 and Eq. 5.33 as shown below:

Rate of Shear

In Eq. $5.32, \omega=\frac{2 \pi n}{60}$

Where $n=$ speed of the spindle, rpm

$$
\begin{aligned}
& R_{b}=9.4211 \mathrm{~mm} \text { (provided by the } \\
& \text { manufacturer) }
\end{aligned}
$$

After substituting these values in Eq. 5.32, the rate of shear, $\mathrm{dv} / \mathrm{dr}=0.217 \mathrm{n} \mathrm{sec}{ }^{-1^{-}}---[5.34]$

Shear stress

In Eq. 5.33, $M=\frac{673.7 \text { Dial }}{100}$
Where $R_{b}=9.421 \mathrm{~mm}$

$$
L=74.93 \mathrm{~mm} \begin{gathered}
\text { (provided by the } \\
\text { manufacturer) }
\end{gathered}
$$

After substituting these values in Eq. 5.33, the shear stress, $\tau=16.1227$ Dial dynes/cm ${ }^{2}--[5.35]$ where Dial= dial gauge reading for torque $M=$ torque in full scale, 673.7 dynes/cm (Dial)

### 5.3.2 Model for Sludges

Among several models available to represent the nonNewtonian behaviour of different fluids and suspensions in the field of chemical engineering and food technology, the Dekee model [27] was found to be more flexible with the potential to use it beyond the purpose for which it was developed. The Dekee model [27] has been used successfully in determining the rheological properties of different types of biofluids and suspensions which show behaviour of pseudoplastic fluids with a yield stress. Since the behaviour of sludges was found to be very close to the biofluids and suspensions, it was decided to use the Dekee's model to fit the experimental viscosity data of different types of sludges.

### 5.3.2.1 Dekee Model

This model is an empirical 3 parameter model as shown below:

$$
\mu^{\prime}\left(\frac{d u}{d x}\right)={ }^{\tau}{ }_{y}\left(\frac{d u}{d x}\right)^{-1}+\mu^{\prime} e^{-t}\left(\frac{d u}{d x}\right)
$$

where $\quad t_{I}=$ time parameter

$$
\begin{aligned}
& \mu^{\prime}=\text { viscosity parameter } \\
&{ }^{1} \\
&{ }_{y}=\text { yield stress }
\end{aligned}
$$

$$
\begin{aligned}
\mu^{\prime} & \left(\frac{d u}{d x}\right)= \\
& \text { non-Newtonian viscosity at shear } \\
& \text { rate, } d u / d x
\end{aligned}
$$

A non-linear regression was performed using the SAS statistical package called NLIN to fit the experimental viscosity data to the Dekee model. A Taylor series expansion around these points was done and resulting linear equations were normalized. These normalized equations were then solved by Gauss Elimination Method using the initial values of the parameters, obtained by the experimental viscosity data as discussed in the following paragraphs. This method is called the Modified Gauss-Newton Method. The newly obtained values of the parameters became the initial value for the next iteration. The iterations were continued until convergence criteria were satisfied. The values of the parameters obtained in the last iteration were used as the corrected and final values.

Evaluation of the Parameters: The initial values of the parameters for each type of sludge were determined using the experimental viscosity. data for non-linear regression as discussed below

Time Parameter and Viscosity Parameter: For a very high rate of shear, the yield stress term became very small which can be neglected and Eq. 5.36 reduces to Eq. 5.37.

$$
\begin{align*}
& \mu^{\prime}\left(\frac{d u}{d x}\right)=\mu_{1}^{\prime} e^{-t}\left(\frac{d u}{d x}\right) \\
& \text { taking } \ell \text { n of both sides, } \\
& \text { ln } \mu^{\prime}\left(\frac{d u}{d x}\right)=\ln \mu_{1}^{\prime}-t_{1}^{(--)} d x \\
& \text { which is similar to an equation for a stright line, } \\
& Y=m x+C \tag{5.38}
\end{align*}
$$

When this relationship between rate of shear and nonNewtonian viscosity is plotted on a semilog graph paper; the slope of the straight line portion of the curve at very high rate of shear will give the initial value of time parameter and the intercept of this straight line on the $Y$ axis, i.e. non-Newtonian viscosity at zero rate of shear will give the initial value of viscosity parameter.

Yield Stress: For many pseudoplastic fluids with a yield value, flow properties can be successfully characterized by means of the Casson Equation [22]. However, Asbeck [5] emphasized the applicability of the Casson Equation in the
high shear region by employing an alternate form as shown below:

$$
\begin{aligned}
& \mu_{1}=\underset{\mu_{L}}{1 / 2}+\tau_{y}^{1 / 2} \underset{(--)}{\mathrm{du}}-1 / 2 \\
& \text { Where }{ }_{1}^{\mu}=\text { non-Newtonian viscosity } \\
& \mu_{L}=\text { limiting viscosity, i.e. independent of } \\
& \text { shear rate } \\
& \tau_{y}=\text { yield stress }
\end{aligned}
$$

If Eq. 5.39 is multiplied by ( du/dx) , one obtains

$$
\begin{equation*}
\tau^{1 / 2}=\mu_{1}^{1 / 2}\left(\frac{d u}{d x}\right)^{1 / 2}+\tau_{y}^{1 / 2} \tag{5.40}
\end{equation*}
$$

Which is a useful form for a low shear viscometer and represents a linear relationship.

Therefore, if the square root of shear stress, $\tau^{1 / 2}$, is plotted against the square root of rate of shear, $(d u / d x)^{1 / 2}$, a straight line analogous to a Bingham plastic fluid [77] will be obtained. The intercept of this straight line on the $Y$ axis for zero rate of shear will give the square root of the initial value of yield stress. The slope of this straight line will give the value of limiting viscosity.

### 5.4 Development of Model for the Aeration Tank

A dimensional analysis was carried out to develop an empirical model, which will be able to predict the horizontal velocity, $u$, in the tank close to the tank bottom. In this dimensional analysis all the possible variables on which the horizontal velocity in an aeration tank could depend were considered. The units and dimensions of all variables involved in the development of the model are shown below:

```
u =f (P,L,W,g, \rhof, (,H,X,h)
----[5.41]
    Where u = horizontal velocity close to the tank bottom
    P = rate of power consumption
    L = tank length
    W = tank width
    g = acceleration due to gravity
    \rho
    \mu = liquid viscosity
    H = water depth in the tank
    X = distance of diffuser from the sidewall
        of the tank
        h = depth of water above the diffuser
        (submergence)
```

$$
\begin{aligned}
& L T^{-1}=f\left[L^{(2 A+B+C+D-3 E-F+G+I+J)} M_{M}^{(A+E+F)}{ }_{T}^{(-3 A-2 D-F)}\right]-[5.43]
\end{aligned}
$$

Comparing the exponents on each side in Eq. 5.43
For $L \quad I=2 A+B+C+D-3 E-F+G+I+J$
----[5.44]
For $T \quad-1=-3 A-2 D-F$
----[5.45]
For $M \quad 0=A+E+F$

Using the Buckingham II Theorem [76], the number of independent dimensionless groups of variables (dimensionless parameters) needed to correlate the variables in this system is equal to $10-3=7$, where 10 is the number of total variables involved and 3 is the number of basic dimensions. Therefore it was decided to substitute the values of $E, F$, and $G$ in terms of other exponents to reduce the number of dimensionless groups to 7, as shown below:

From Eq. 5.45
$F=1-3 A-2 D$
----[5.47]
Substituting this value of $F$ in Eq. 5.46
$0=A+E+1-3 A-2 D$
or $\quad E=2 A+2 D-1$
Substituting the values of $E$ and $F$ from Equations 5.47 and 5.48 into Eq. 5.44, gives
$I=2 A+B+C+D-3(2 A+2 D-1)-(1-3 A-2 D)+G+I+J$
$1=B+C-A-3 D+G+I+J+2$
$G=-B-C+A+3 D-I-J-1$
Substituting the values of $E, F$, and $G$ from Eqs. 5.47, 5.48 and 5.49 into Eq. 5.42, gives



A few modifications and deletion were made in the Eq. 5.51 as described below:
a. The $D$ powered term is called a depth factor and in order to show the effect of water depth directly, this term was changed in the form of $H$ instead of $\mathrm{H}^{3}$ by taking the cube root of all the variables in this dimensionless group.
b. In a rectangular aeration tank the diffusers are generally placed along the length of the tank. Since, the length of the tank ( 0.69 m ) was not changed during experiments, it was decided to drop the length factor ( $L / H$ ) from the Eq. 5.51. The width of the tank was changed during the experiments.
c. The distance of diffuser from the sidewall of the tank was not changed during the experiments, because it was observed that a small change in this distance made no significant change in the velocity distribution, it was decided to eliminate factor $\mathrm{X} / \mathrm{H}$ from Eq. 5.51. Therefore:

Where $\left.\begin{array}{rl}\left(-\frac{u_{\rho} H}{\mu}\right.\end{array}\right)=$ Reynold number or velocity factor,

$$
\begin{aligned}
& \left.\begin{array}{l}
P_{\rho}^{2} H \\
\mu^{3}
\end{array}\right)=\text { Power number } X \text { Reynold number }{ }^{3} \\
& \text { or power factor, F2 } \\
& \frac{W}{H}=\text { width factor, } F 3
\end{aligned}
$$

 $\underset{H}{(-)}=$ submergence factor, $F 5$

Surface tension played an insignificant role in the experimental aeration tank due to its size. Surface tension is important in the formation and movement of bubbles in liquid. However, in this dimensional analysis, the details of air bubbles in the aeration tank was not considered. Therefore, the effect of surface tension on this analysis was neglected.

The variables and their values that were held constant during experiments on aeration tank are listed below:

Tank length, $L=0.69 \mathrm{~m}$
Fluid density, $\rho=998 \mathrm{Kg} / \mathrm{m}^{3}$ at $20^{\circ} \mathrm{C}$
Fluid viscosity, $\mu=1.0 \times 10^{-3} \mathrm{~N} . \mathrm{s} / \mathrm{m}^{2}$ at $20^{\circ} \mathrm{C}$
Acceleration due to gravity, $g=9.8 \mathrm{~m} / \mathrm{s}^{2}$
Room temperature $=20^{\circ} \mathrm{C}$

The velocity observations in the aeration tank were made for horizontal velocity for the entire depth. However, horizontal velocity, 25 mm above the tank bottom was considered for the development of model. Therefore, this model will predict the horizontal
velocity at 25 mm above the tank bottom under different operating conditions.

### 5.4.1 Calculation of Different Dimensionless Factors <br> The calculation of various parameters used in different dimensionless factors are described below:

### 5.4.1.1 Reynolde Number or Velocity Factor, F1

Velocity Factor, $F 1=\frac{u \rho H}{\mu^{-}}$

This factor was calculated for the horizontal velocity, u, at a distance 25 mm above the tank bottom for different depths of water and operating conditions. The values of other parameters considered. in the calculation were kept constant as discussed earlier.
5.4.1.2 Power Factor, F2

Power Factor, $F 2=\left(\frac{\rho_{\rho}^{2} H}{\mu^{3}}\right)$
A. The theoretical rate of power consumption, $P$ is calculated using the following formula [80] based upon the assumption of adiabatic conditions.

$$
\begin{equation*}
\mathrm{P}=\frac{W R_{g} \mathrm{~T}}{8.41} \underset{\{(--)}{\mathrm{P}_{1}} \quad 0.283 \tag{5.53}
\end{equation*}
$$

Where $P=$ rate of power consumption, $k w$

$$
\begin{aligned}
\mathrm{w} & =\text { air mass flow rate, } \mathrm{kg} / \mathrm{s} \\
\mathrm{R}_{\mathrm{g}} & =\text { gas constant, } 8.314 \mathrm{~J} / \mathrm{g} \cdot \mathrm{~mol} .{ }^{\circ} \mathrm{K} \\
\mathrm{~T}_{\mathrm{i}} & =\text { inlet temperature of air, }{ }^{\circ} \mathrm{K}
\end{aligned}
$$

$P_{1}=a b s o l u t e$ inlet pressure, atmosphere $P_{2}=a b s o l u t e$ outlet pressure, atmosphere
B. The useful power based on the isothermal expansion of the air at the outlet has been given by the Fair and Geyer [33] by the following equation:

$$
\begin{equation*}
\left.\left.P=3891.26 Q \quad \log \frac{h+10.36}{10.36}\right)\right\} \tag{5.54}
\end{equation*}
$$

Where $P$ = useful power dissipated, watts
$Q=$ air flow rate, $\mathrm{m}^{3} / \mathrm{min}$
$h=$ submergence of outlet port, m

The air flow rate is calculated for the standard conditions, i.e. $20^{\circ} \mathrm{C}$ temperature and $101.3 \mathrm{kN} / \mathrm{m}^{2}$ pressure.
C. The useful power available at the outlet or diffuser can be calculated by modifying Eq. 5.53. The outlet pressure term, $P_{2}$, can be replaced by $(h+10.36) \quad$ m, inlet pressure
term, $P_{1}$, can be assumed to be equal to atmospheric pressure of 10.36 m , and h is the submergence of outlet port or diffusers in $m$. The modified equation for useful power available at the outlet becomes:

$$
\begin{equation*}
P=\frac{W R Q^{T} i}{8.41}\left[\left(\frac{10.36+h}{10.36}\right)^{0.283}-1\right] \tag{5.55}
\end{equation*}
$$

This value of power, $P$, ignores all the losses in the delivery system, in the fittings, at the diffusers, efficiency of the compressor and therefore is equal to the useful power available at the outlet. For all further calculations, this value of power, $P$, has been used. The air flow rates were obtained from a rotameter which was calibrated for air flow rate under standard conditions, STP.
D. In practice, standard conditions seldom exist at the outlet port. Therefore the air flow rate measured by the rotameter should be corrected for the operating conditions to obtain the air flow rate under standard conditions, using the following Equation:

$$
\begin{align*}
& \left(\mathrm{P}_{\text {STP }}\right) \quad\left(\mathrm{T}_{\text {ope }}\right) 1 / 2 \tag{5.56}
\end{align*}
$$

```
Where \(Q_{S T P}=\) air flow rate under standard STP 3 conditions, \(\mathrm{m}^{3} / \mathrm{sec}, 20^{\circ} \mathrm{C}\) and 101.3 \(\mathrm{kN} / \mathrm{m}^{2}\) or \(\mathrm{cfm}, 20^{\circ} \mathrm{C}\) and 14.7 psia
``` Q \(=\) observed air flow rate (reading from rota rotameter), \(\mathrm{m}^{3} / \mathrm{s}\) or cfm

Q = actual air flow rate under operating a conditions, \(\mathrm{m}^{3} / \mathrm{sec}\) or cfm

P \(\quad=\) pressure for which the rotameter was rota calibrated, \(101.3 \mathrm{kN} / \mathrm{m}^{2}\) or 14.7 psia \(\mathrm{p}_{\text {gage }}=\) pressure gauge reading, \(\mathrm{kN} / \mathrm{m}^{2}\) or psig gage
\(\begin{aligned} P_{\text {atm }}= & \text { atmospheric pressure, } 101.3 \mathrm{kN} / \mathrm{m}^{2} \\ & \text { or } 14.7 \mathrm{psia}\end{aligned}\)
\(T_{\text {ope }}=\) operating temperature, \({ }^{\circ} \mathrm{K}\)
\(T=s t a n d a r d\) temperature for which the rotameter was calibrated, \(293.15^{\circ} \mathrm{K}\)

The actual air flow rate from diffuser, \(Q_{a}, m^{3} / \mathrm{s}\) or cfm, corresponding to temperature, Tope' and diffuser submergence, \(h\), can be obtained from [61]:

5.4.1.3 Width Factor, F3

Width Factor, \(\mathrm{F} 3=\frac{\mathrm{W}}{\mathrm{H}}\)

This factor was calculated for different widths, W, 2.44 \(\mathrm{m}, 2.21 \mathrm{~m}, 1.98 \mathrm{~m}, 1.75 \mathrm{~m}, 1.52 \mathrm{~m}, 1.29 \mathrm{~m}\) and 1.06 m of the aeration tank and for different depths of water, \(H, 0.50 \mathrm{~m}\), \(0.65 \mathrm{~m}, ~ 0.80 \mathrm{~m}, ~ 0.95 \mathrm{~m}\) and 1.10 m in the aeration tank.

\subsection*{5.4.1.4 Depth Factor, F4}

Depth Factor, \(\mathrm{F} 4=\left(\frac{\mathrm{g}^{1 / 3}}{\mu^{2 / 3}} \frac{2 / 3}{2 / 3}\right)\)

In calculating the depth factor, all parameters except depth of water, \(H\), in the aeration tank, such as density of water, \(\rho\), viscosity of water, \(\mu\) and acceleration due to gravity, \(g\), were kept constant at \(20^{\circ} \mathrm{C}\). The various depths of water used in the experiment were \(0.50 \mathrm{~m}, 0.65 \mathrm{~m}, 0.80 \mathrm{~m}\), 0.95 m and 1.10 m .

\subsection*{5.4.1.5 Submergence Factor, F5}

Submergence Factor, \(F 5=\frac{h}{H}\)

This factor was calculated for different submergences, \(h\), of the diffuser and for different depths of water, \(H\), in the aeration tank.

\subsection*{5.4.2 Correlation Between Dimensionless Factors}

An empirical model for the aeration tank to predict the horizontal velocity close to the tank bottom ( 25 mm above the floor) under various operating conditions was developed using the method of linear regression. A correlation was established between different dimensionless factors.

The statistical analysis of data was carried out using a standard statistical package program called Linear Regression [41]. Since Eq. 5.58 is in exponential form it was reduced to a linear form by taking log of both sides.
\[
\begin{aligned}
& F 1=f(F 2)^{A}(F 3)^{B}(F 4)^{D}(F 5)^{J} \\
& \text { Where } F 1=\text { Reynolds number or velocity factor } \\
& F 2=\text { power factor } \\
& F 3=\text { width factor } \\
& F 4=\text { depth factor } \\
& F 5=\text { submergence factor }
\end{aligned}
\]
```

or }\operatorname{log}(F1)=\operatorname{log}(f)+A\operatorname{log}(F2)+B log(F3)

```
\[
\begin{equation*}
D \log (F 4)+J \log (F 5) \tag{5.59}
\end{equation*}
\]

The values of unknown multiplying constants such as \(f\), \(A\), \(B, D\), and \(J\) were determined by applying a linear regression statistics to develop a correlation between the dependent variable, Fl, and the independent variables F2, F3, F4, and F5 or any combinations of two or more of these independent variables. During the process of this analysis, any independent variable that had little or no influence on the dependent variable was discarded. The extent of influence of independent variables on dependent variable was identified by calculating different statistical parameters and they are listed below:

R - SQUARE Value - Coefficient of Determination
F Test Value
PR >F - Significance Probability
T FOR HO: PARAMETER=0 - Student's t test
\(P R>|T|\)

\section*{Chapter VI}

\section*{RESULTS AND ANALYSIS}

Results obtained through theoretical and experimental analyses are presented in this chapter.

\subsection*{6.1 Velocity Distribution in the Laboratory Flume}

In this study, the Eqs. 5.6 and 5.7 have been used to calculate the critical shear or friction velocity, \(U_{*_{c}}\) These equations are derived from 'Prandtl-von Karman Universal Velocity Distribution Law', which has been verified by many investigators [95]. This logarithmic law means that, during a turbulent flow when the boundary layer is fully developed, the velocity distribution is logarithmic. The experiments conducted in the laboratory flume indicate a striking similarity between observed and computed velocity distribution, Figure 6.1, and, therefore offer a reasonable justification for use of this logarithmic law in the analysis of data.


Figure 6.1: Observed and Computed Velocity Distribution in the Flume

\subsection*{6.2 Experiments in Laboratory Flume with Grit Particles}

The experiments were conducted in a laboratory flume to determine the critical shear stress required to move grit particles of different sizes. For this purpose, velocity profiles were determined at different locations along the length of the flume. Since the length of the flume was short, the bed was roughened to develop the flow fully, with the same size of grit particles as were used for scouring during the experiment. The grit partiicles were separated into eight different geometric mean sizes, ranging from 2.1817 mm to 0.2121 mm . In order to widen the scope of this investigation, some larger gravel particles, ranging in size from 3.4 mm to 17.4 mm , were also included in the experiment.

All the velocity readings obtained at different locations and depths were used to verify whether the flow was fully developed during critical conditions for the initiation of the motion for different grit and gravel particles. Some typical velocity profiles for different grit and gravel particles during critical conditions are shown in Figure 6.2 and Figure 6.3. The velocity profile obtained at the end of the flume was neglected because exit conditions distorted the velocity profile.

From the velocity profile for the entire depth of flow, only the point velocity close to the bed, 7.6 mm above bed, was considered for further analysis to obtain critical shear

Grit Size \(=1.6733 \mathrm{~mm}\)
Depth of Water \(=17.5 \mathrm{~cm}\)
\[
\text { Location }=1.83 \mathrm{~m}(6 \mathrm{ft})
\]
\[
\text { Location }=2.134 \mathrm{~m}(7 \mathrm{ft})
\]


Fig. 6.2. Typical Velocity Profiles in Flume During Critical Conditions for Grit Particles


Fig. 6.3. Typical Velocity Profiles in Flume During Critical Conditions for Gravel Particles.
stresses. This point velocity was then converted to critical shear or friction velocity, \(U_{* c^{\prime}}\) using Eq. 5.6 or 5.7. This critical shear or friction velocity was used to obtain the values for critical bed shear stress, \(\tau\) oc' using Eq. 5.5. The calculated shear velocities and corresponding particle Reynolds number, for different particles sizes and critical bed shear stress, are tabulated in Table 6.1 and Table 6.2. Since none of the velocity readings, except the point velocity, \(u\), close to the bed of the flume, was used directly in further analysis, it was considered unnecessary to include all these data in these tables.

The particle sizes and the corresponding values of shear stress are plotted on log log scales in Figure 6.4. This plot shows that the curve is a straight line in the hydraulically smooth flow regime and becomes curvilinear for rough turbulent flow conditions. In the transitional state, the plot begins to change from straight line to a curve. This plot can be used directly in finding the critical bed shear stress required to initiate the motion of any size of grit particles. This will also indicate the regime of flow in a channel whose bed is made up of uniform size grit or gravel particles.

A linear regression analysis was performed, using a SAS statistical package called GLM, General Linear Models, to establish a correlation between the particle size in mm and the corresponding value of critical bed shear stress in

Table 6.1 - PARTICLE CHARACIERISTICS AND CORRESPONDING CRITICAL SHEAR OR FRICIION VELOCITY
\begin{tabular}{|c|c|c|c|c|c|}
\hline TYPE OF PARTICLES & \[
\underset{\substack{\text { PARTICLE } \\ \mathrm{k}_{\mathrm{s}} \\ \mathrm{~mm}}}{\text { SIZE }}
\] & POINT VELOCITY u at 7.6 mm above the bed \(\mathrm{m} / \mathrm{sec}\) & ```
CRITICAL SHEAR
    OR FRICTION
    VELOCITY,
        \(\mathrm{U}_{\mathrm{*}_{\mathrm{C}}}\)
        \(\mathrm{m} / \mathrm{sec}\)
``` & PARTICLES REYNOLD NUMBERS
\[
U_{*} c_{s}^{k} / v
\] & REGIME OF FLOW \\
\hline Gravel & 17.40 & 0.3350 & 0.05210 & 898 & Rough Turbulent \\
\hline Gravel & 14.20 & 0.3080 & 0.04440 & 624 & Rough Turbulent \\
\hline Gravel & 12.20 & 0.2680 & 0.03660 & 442 & Rough Turbulent \\
\hline Gravel & 10.50 & 0.2550 & 0.03310 & 344 & Rough Turbulent \\
\hline Gravel & 8.70 & 0.2410 & 0.02950 & 254 & Rough Turbulent \\
\hline Gravel & 3.40 & 0.2140 & 0.02040 & 69 & Close to Turbulent \\
\hline Grit & 2.1817 & 0.2010 & 0.01690 & 37 & Transitional \\
\hline Grit & 1.6733 & 0.2010 & 0.01550 & 26 & Transitional \\
\hline Grit & 1.0860 & 0.1940 & 0.01330 . & 14 & Transitional \\
\hline Grit & 0.7770 & 0.1870 & 0.01230 & 9 & Transitional \\
\hline Grit & 0.5477 & 0.1810 & 0.01130 & 6 & Transitional \\
\hline Grit & 0.3880 & 0.1670 & 0.01016 & 4 & Hydraulically Smooth \\
\hline Grit & 0.2739 & 0.1540 & 0.00947 & 3 & Hydraulically Smooth \\
\hline Grit & 0.2121 & 0.1410 & 0.00877 & 2 & Hydraulically Smooth \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|c|}
\hline \multicolumn{4}{|l|}{Table 6.2 - PARTICLE CHARACTERISTICS AND CORRESPONDING CRITICAL BED SHEAR STRESS} \\
\hline TYPE OF PARIICLES & \[
\underset{\substack{\text { PARTICLE SIZE } \\ \mathrm{k}_{\mathrm{s}} \\ \mathrm{~mm}}}{ }
\] & CRITICAL SHEAR OR FRICTION VELOCITY, \(\mathrm{U}_{\mathrm{*}_{\mathrm{C}}}\) \(\mathrm{m} / \mathrm{sec}\) & CRITICAL BED SHEAR STRESS
\[
\begin{gathered}
{ }^{\tau_{\alpha C}}=\mathrm{U}_{\mathrm{*}_{\mathrm{c}} \cdot \rho}^{2} \cdot \mathrm{~N} / \mathrm{m}^{2}
\end{gathered}
\] \\
\hline Gravel & 17.40 & 0.05210 & 2.710 \\
\hline Gravel & 14.20 & 0.04440 & 1.970 \\
\hline Gravel & 12.20 & 0.03660 & 1.340 \\
\hline Gravel & 10.50 & 0.03310 & 1.100 \\
\hline Gravel & 8.70 & 0.02950 & 0.870 \\
\hline Gravel & 3.40 & 0.02040 & 0.420 \\
\hline Grit & 2.1817 & 0.01690 & 0.290 \\
\hline Grit & 1.6733 & 0.01550 & 0.240 \\
\hline Grit & 1.0860 & 0.01330 & 0.177 \\
\hline Grit & 0.7770 & 0.01230 & 0.151 \\
\hline Grit & 0.5477 & 0.01130 & 0.127 \\
\hline Grit & 0.3880 & 0.01016 & 0.103 \\
\hline Grit & 0.2739 & 0.00947 & 0.090 \\
\hline Grit & 0.2121 & 0.00877 & 0.077 \\
\hline
\end{tabular}


Figure 6.4: Relationship Between Particle size and Critical Bed Shear Stress
\(\mathrm{N} / \mathrm{m}^{2}\). The selection of best fit model was done on the basis of following statistical parameters.

R - SQUARE Value - Coefficient of Determination
F Test Value
PR >F - Significance Probability
T FOR HO: PARAMETER=0 - Student's t test
\(P R>|T|\)

The following best fit equation has been developed for the plot shown in Figure 6.4.
\[
\begin{gathered}
\log \left(\tau_{o c}\right)=0.611 \log \left(k_{s}\right)+0.244\left[\log \left(k_{s}\right)\right]^{2}-0.779--[6.1] \\
\text { Where } \tau_{o c}=\text { critical bed shear, } \mathrm{N} / \mathrm{m}^{2} \\
\mathrm{k}_{\mathrm{S}}=\text { particle size, } \mathrm{mm}
\end{gathered}
\]

The plot overlapping the measured value and estimated value of critical bed shear stresses using Eq. 6.1 is shown in Figure 6.5.

\section*{PLOT OF CRITICAL SHEAR STRESS AND PARTICLE SIZE}


Figure 6.5: Measured and Estimated Values of Shear Stresses

\subsection*{6.3 Experiments on Sludges}

Experiments on different kind of sludges were run in the flume. The Brookfield viscometer was employed to determine the rheological properties of sludges. The results obtained are presented below:

\subsection*{6.3.1 Laboratory Flume with Sludge Particles}

Experiments in the flume were run to obtain the values of critical bed shear stress necessary to initiate the motion of sludge particles for different kinds of sludges. The depth of water in the flume was kept between 0.15 m and 0.175 m during these experiments. After establishing the critical conditions for the initiation of motion of particles, the horizontal velocites of flow in the flume were measured at different locations and depths.

The velocity profiles for the entire depth of flow and at different locations were obtained to check whether or not the regime of flow was fully developed. Some typical velocity profiles for critical conditions to initiate motion of different sludge particles are shown in Figure 6.6.

Since sludge particles are not supposed to settle in the aeration tank, it is assumed that the bed will be smooth and flow will be turbulent in calculating different parameters. Eq. 5.6 was used to calculate the critical shear or friction velocity, \(U_{*_{C}}\), and Eq. 5.5 was used to obtain the value of critical bed shear, \(\tau_{o c} \quad\) The point velocity, \(u\), close to the bed and calculated values of critical shear or friction

Physico-Chemical Sludge
Depth of Water \(=25.0 \mathrm{~cm}\)


Fig. 6.6. Typical Velocity Profiles in Flume During Critical Conditions for Sludge Particles.
velocity and critical shear stress are shown in Table 6.3. Since none of the velocity readings, except the point velocity close to the bed of the flume, \(u\), was used in any other calculation, it was considered unnecessary to include all the velocity readings in this table.

Table 6.3 - CRITICAL SHEAR STRESS VALUES FOR DIFFERENT TYPES OF SLIDGES
\begin{tabular}{|c|c|c|c|c|}
\hline \multirow[t]{2}{*}{SLUDGE TYPE} & \multirow[t]{2}{*}{VELOCITY, u at \(y=7.6 \mathrm{~mm}\) above the bed \(\mathrm{m} / \mathrm{sec}\)} & \multirow[t]{2}{*}{CRITICAL SHEAR OR FRICTION VELOCITY, \(\mathrm{U}_{\mathrm{*}_{\mathrm{C}}}\) \(\mathrm{m} / \mathrm{sec}\)} & \multicolumn{2}{|l|}{CRITICAL SHEAR STRESS, \({ }^{\tau} \mathrm{y}\)} \\
\hline & & & \[
\mathrm{N} / \mathrm{m}^{2}
\] & dynes/cm \({ }^{2}\) \\
\hline Biological Sludge (from aeration tank) & 0.064 & 0.00445 & 0.01976 & 0.1976 \\
\hline Biological Sludge & 0.066 & 0.00457 & 0.02084 & 0.2084 \\
\hline Biological Sludge & 0.064 & 0.00445 & 0.01976 & 0.1976 \\
\hline Biological Sludge & 0.064 & 0.00445 & 0.01976 & 0.1976 \\
\hline Biological Sludge & 0.066 & 0.00457 & 0.02084 & 0.2084 \\
\hline Biological Sludge & 0.069 & 0.00475 & 0.02252 & 0.2252 \\
\hline Alum Sludge & 0.080 & 0.00539 & 0.02899 & 0.2899 \\
\hline Alum Sludge & 0.084 & 0.00562 & 0.03152 & 0.3152 \\
\hline Alum Sludge & 0.084 & 0.00562 & 0.03152 & 0.3152 \\
\hline Alum Sludge & 0.082 & 0.00550 & 0.03019 & 0.3019 \\
\hline Alum Sludqe & 0.080 & 0.00539 & 0.02899 & 0.2899 \\
\hline Alum Sludge & 0.075 & 0.00510 & 0.02596 & 0.2596 \\
\hline Physico-Chenical shudge from underdrains) & 0.070 & 0.00481 & 0.02309 & 0.2309 \\
\hline Physico-Chemical Sludge & 0.075 & 0.00510 & 0.02596 & 0.2596 \\
\hline Physico-Chemical Sludge (from clarifiers) & 0.061 & 0.00427 & 0.01820 & 0.1820 \\
\hline Physio-Chemical sludge & 0.070 & 0.00481 & 0.02309 & 0.2309 \\
\hline Physico-Chemical Sludge & 0.058 & 0.00409 & 0.01669 & 0.1669 \\
\hline Physico-Chemical Sludge & 0.061 & 0.00427 & 0.01820 & 0.1820 \\
\hline
\end{tabular}
\(\underset{(\text { cont'd) }}{\text { Table }} \mathbf{~ - ~ C R I T I C A L ~ S H E A R ~ S T R E S S ~ V A L U E S ~ F O R ~ D I F F E R E N T ~ T Y P E S ~ O F ~ S L U D G E ~}\)
\begin{tabular}{|c|c|c|c|c|}
\hline \multirow[t]{2}{*}{SLUDGE TYPE} & \multirow[t]{2}{*}{VEIOCITY, u at \(y=7.6 \mathrm{~mm}\) above the bed \(\mathrm{m} / \mathrm{sec}\)} & \multirow[t]{2}{*}{\[
\begin{gathered}
\text { CRITICAL SHEAR } \\
\text { OR FRICTION } \\
\text { VEIOCITY, } \\
\text { U }_{* c} \\
\text { m/sec }
\end{gathered}
\]} & \multicolumn{2}{|l|}{CRITICAL SHEAR STRESS, \({ }^{\tau} \mathrm{y}\)} \\
\hline & & & \(\mathrm{N} / \mathrm{m}^{2}\) & dynes/cm \({ }^{2}\) \\
\hline Diluted Secondary Digested Sludge & 0.075 & 0.00510 & 0.02596 & 0.2596 \\
\hline Diluted Secondary Digested
Sludge & 0.070 & 0.00481 & 0.2309 & 0.2309 \\
\hline Mixture of Primary and Secondary Sludge & 0.055 & 0.00391 & 0.01526 & 0.1526 \\
\hline Mixture of Primary and Secondary Sludge & 0.065 & 0.00451 & 0.02030 & 0.2030 \\
\hline
\end{tabular}

\subsection*{6.3.2 Determination of Rheological Properties of Sludges \\ by Viscometer}

A Brookfield Viscometer with cylindrical shaped spindle \#l was used to determine the rheological properties of the sludges. The spindle speed, rpm, and the torque required to maintain constant angular velocity were then used to calculate the rate of shear, \(d v / d r\), and the shear stress, \(\tau\), using Eqs. 5.33 and 5.34. For each type of sludge, both raw and settled, the experiments were repeated at least twice or thrice depending upon the volume of sample available for the analysis. At each spindle speed or rate of shear, at least four torque readings were taken and the average of these readings was used for further analysis. Since it was considered unnecessary to include all the raw data, only the average values of shear stress for each rate of shear and for each set are shown in Appendix B, for different types of sludge samples analyzed.

\subsection*{6.3.2.1 Determination of Yield Stress, \(T_{Y}\)}

The yield stress, \(\tau_{y}\), values for all types of sludges and at different concentrations of suspended solids were obtained using the following two methods:
a. Graphical Method
b. Dekee Model
1.Graphical Method: The rate of shear and shear stress values were plotted to obtain the value of yield stress for each type of sludge. Some of the
typical plots between the rate of shear and the corresponding shear stress for different types of sludges, flow curves, are shown in Figure 6.7, Figure 6.8, Figure 6.9, Figure 6.10, Figure 6.11, Figure 6.12, Figure 6.13, Figure 6.14, Figure 6.15, Figure 6.16, Figure 6.17, Figure 6.18, Figure 6.19, Figure 6.20, Figure 6.21, and Figure 6.22. The yield stress, \(\tau_{Y}\), was obtained by joining the first two points at lower rate of shear in the flow curve and extending this line to the \(Y\) axis drawn at zero rate of shear. This intercept on the \(Y\) axis was taken to be equal to the yield stress for that particular type of sludge at that concentration of suspended solids. By following the same procedure, the yield stress values of all type of sludges, raw sludge and settled sludge, were obtained. The results are shown in Table 6.4, Table 6.5, Table 6.6, Table 6.7, and Table 6.8.



Figure 6.9: Observed Flow Curve for Biological Sludge (Mixed Liquor)








\footnotetext{
Observed. Flow Curve for Physico-Chemical
Sludge (Unsettled)
Observed. Flow Curve for Physico-Chemical
Sludge (Unsettled)
Observed. Flow Curve for Physico-Chemical
Sludge (Unsettled)
Figure 6.16:
}



Figure 6.18: \(\begin{aligned} & \text { Observed Flow Curve for Physico-Chemical } \\ & \text { Sludge (Settled) }\end{aligned}\)



Figure 6.20: Observed Flow Curve for Secondary Digested



Figure 6.22: Observed Flow Curve for Mixture of Primary and Secondary sluage (Diluted)

Table 6.4 - SUMMARY OF YIEID STRESS VALUES FOR BIOLOGICAL SLUDGES (GRAPHICAL MEIHOD)
\begin{tabular}{|c|c|c|c|}
\hline SLUDSE TYPE & SUSPENDED SOLIDS CONCENIRATION \(\mathrm{mg} / \mathrm{L}\) & \multicolumn{2}{|l|}{\[
\begin{gathered}
\text { YIELD STRESS, }{ }^{\tau} y \\
{\text { dynes } / \mathrm{cm}^{2}}^{\mathrm{N} / \mathrm{m}^{2}}
\end{gathered}
\]} \\
\hline Mixed Liquor (Biological) & 2,491 & 0.0200 & 0.0020 \\
\hline Mixed Liquor (Biological) & 2,909 & 0.0400 & 0.0040 \\
\hline Mixed Liquor (Biological) & 2,387 & 0.0100 & 0.0010 \\
\hline Settled Mixed Liquor (Activated Sludge) & 9,258 & 0.7500 & 0.0750 \\
\hline Mixed Liquor (Biological) & 1,908 & 0.0175 & 0.00175 \\
\hline Mixed Liquor (Biological) & 2,708 & 0.0500 & 0.0050 \\
\hline Settled Mixed Liquor (Activated Sludge) & 8,531 & 1.300 & 0.1300 \\
\hline Settled Mixed Liquor (Activated Sludge) & 8,538 & 1.1000 & 0.1100 \\
\hline Mixed Liquor (Biological) & 3,787 & 0.13 & 0.0130 \\
\hline Mixed Liquor (Bioloqical) & 3,851 & 0.14 & 0.0140 \\
\hline Settled Mixed Liquor (Activated Sludge) & 11,969 & 2.30 & 0.230 \\
\hline Settled Mixed Liquor (Activated Sludge) & 11,967 & 2.95 & 0.295 \\
\hline
\end{tabular}

Table 6.5 - SUMMARY OF YIELD STRESS VALUES FOR ALUM SLUDGES FROM WATER TREATMENT PLANT (GRAPHICAL MEIHOD)
\begin{tabular}{|c|c|c|c|}
\hline SLUDGE TYPE & SUSPENDED SOLIDS CONCENTRATION \(\mathrm{mg} / \mathrm{L}\) & \multicolumn{2}{|l|}{\[
\begin{aligned}
& \text { YTELD STRESS, }{ }^{\tau} y \\
& \text { dynes } / \mathrm{cm}^{2} \quad \mathrm{~N} / \mathrm{m}^{2}
\end{aligned}
\]} \\
\hline Alum Sludge & 3,099 & 0.070 & 0.0070 \\
\hline Alum Sludge & 3,097 & 0.075 & 0.0075 \\
\hline Settled Alumi Sludge & 12,688 & 4.200 & 0.4200 \\
\hline Settled Alum Sludqe & 13,362 & 3.900 & 0.3900 \\
\hline Alum Sludge & 2,985 & 0.075 & 0.0075 \\
\hline Alum Sludge & 3,128 & 0.070 & 0.0070 \\
\hline Settled Alum Sludge & 11,447 & 3.400 & 0.3400 \\
\hline Settled Alum Sludge & 11,613 & 3.250 & 0.3250 \\
\hline Alum Sludge & 2,732 & 0.030 & 0.0030 \\
\hline Alum Sludge & 2,697 & 0.040 & 0.0040 \\
\hline Settled Alum Sludge & 11,573 & 3.700 & 0.3700 \\
\hline Settled Alum Sludge & 11,493 & 4.300 & 0.4300 \\
\hline
\end{tabular}

Table 6.6 - SUMMARY OF YIELD SIRESS VALUES FOR PHYSICO-CHEMICAL WASTENATER SLUDGES (GRAPHICAL METHOD)
\begin{tabular}{|c|c|c|c|}
\hline SLUDGE TYPE & SUSPENDED SOLIDS CONCENIRATION \(\mathrm{mg} / \mathrm{L}\). & \[
\begin{array}{r}
\text { YIELD } \\
\text { dynes/cm }
\end{array}
\] & \(T_{y}\)
\[
\mathrm{N} / \mathrm{m}^{2}
\] \\
\hline Diluted Physico-Chemical Sludge from Underdrain & 3,557 & negligible & \\
\hline Diluted Physico-Chemical Sludge from Underdrain & 1,640 & negligible & \\
\hline Physico-Chemical Sludge from Underdrain & 42,309 & 2.9 & 0.2900 \\
\hline Physico-Chemical Sludge from Underdrain & 42,396 & 3.1 & 0.3100 \\
\hline Physico-Chemical Sludge from Clarifier & 675 & negligible & --mm \\
\hline Physoci-Chemical Sludge from Clarifier & 784 & negligible & ----- \\
\hline Settled Physico-Chemical Sludge from Clarifier & 13,818 & 0.625 & 0.0625 \\
\hline Settled Physico-Chemical Sludge from Clarifier & 11,493 & 0.425 & 0.0425 \\
\hline Physico-Chemical Sludge from Clarifier & 5,255 & negligible & - \\
\hline Physico-Chenical Sludge from Clarifier & 5,897 & negligible & \\
\hline Settled Physico-Chemical Sludge from Clarifier & 14,766 & 0.7750 & 0.0775 \\
\hline Settled Physico-Chemical Sludge from Clarifier & 12,596 & 0.25 & 0.025 \\
\hline
\end{tabular}

Table 6.7 - SUMMARY OF YIEID STRESS VALUES FOR SECONDARY DIGESTED SLUDGES (GRAPHICAL MEIHOD)
\begin{tabular}{|c|c|c|c|}
\hline SLUDGE TYPE & SUSPENDED SOLIDS CONCENIRATION \(\mathrm{mg} / \mathrm{L}\) & \multicolumn{2}{|l|}{\[
\begin{gathered}
\text { YIEID STRESS, }{ }^{\tau} \mathrm{Y} \\
\text { dynes } / \mathrm{cm}^{2} \quad \mathrm{~N} / \mathrm{m}^{2}
\end{gathered}
\]} \\
\hline Diluted Secondary Digested Sludge & 24,537 & 5.2 & 0.520 \\
\hline Diluted Secondary Digested Sludge & 26,693 & 5.95 & 0.595 \\
\hline Diluted Secondary Digested Sludge & 18,837 & 2.00 & 0.200 \\
\hline Diluted Secondary Digested Sludge & 22,040 & 3.60 & 0.360 \\
\hline
\end{tabular}

Table 6.8 - SUMMARY OF YIEID STRESS VALUES FOR MIXTURES OF PRIMARY AND SECONDARY SLUDGES (GRAPHICAL MEIHOD)
\begin{tabular}{|c|c|c|c|}
\hline SLUDGE TYPE & SUSPENDFD SOLIDS CONCENTRATION mg/L & \multicolumn{2}{|l|}{\[
\begin{gathered}
\text { YIELD STRESS, }{ }^{\tau} \mathrm{y} \\
\text { dynes } / \mathrm{cm}^{2} \quad \mathrm{~N} / \mathrm{m}^{2}
\end{gathered}
\]} \\
\hline Mixture of Primary and Secondary Sludge & 20,586 & 2.4 & 0.240 \\
\hline mixture of Primary and Secondary Sludge & 20,820 & 2.3 & 0.230 \\
\hline
\end{tabular}
2.Dekee Model: The values of yield stress for different types of sludges were determined by applying the Dekee model with the help of a non-linear regression technique using a SAS statistical package called NLIN. The initial values of different parameters in Dekee model were obtained using various approaches as discussed in the next paragraph and the final values or the corrected values of parameters including yield stress were obtained by using the nonlinear regression technique.

The initial values of yield stress for all types of sludge samples were obtained using the Casson Equation as discussed in Chapter 5. The square root of shear stress and square root of rate of shear were plotted on a regular graph paper. For pseudoplastic fluids with a defined yield stress, this plot gave a straight line. By extending this straight line to \(Y\) axis at zero rate of shear and this intercept was considered as initial value of the yield stress. Some of the typical plots used for obtaining the initial value of yield stress are shown in Figure 6.23, Figure 6.24, Figure 6.25, Figure 6.26, and Figure 6.27. The initial values of yield stress for different types of sludges are presented in Table 6.9.

The initial values of time parameter and viscosity parameter were obtained using the method discussed in


Figure 6.24: Plot to Estimate Initial Value of Yield Stress in Dekee Model for Alum Sludges


Figure 6.25: Plot to Estimate Initial Value of Yield Stress


Figure 6.26: Plot to Estimate Initial Value of Yield Stress in Dekee Model for Secondary Digested Sludges

Figure 6.27:
Plot to Estimate Initial Value of Yield Stress in Dekee Model for Mixture of Primary and Secondary Sludges

Table 6.9 - INITIAL VALUES OF PARAMETERS FOR DEKEE MONEL FOR DIFFERENT TYPES OF SLIJGGES
\begin{tabular}{|c|c|c|c|c|}
\hline \multirow[t]{2}{*}{TYPE OF SLJDGE} & \multirow[t]{2}{*}{SUSPENDED SOLIDS CONCENTRATION \(\mathrm{mg} / \mathrm{L}\)} & \multicolumn{3}{|c|}{INITIAL VALUE} \\
\hline & & \[
\begin{aligned}
& \text { YIELD STRESS } \\
& \mathrm{t}_{\mathrm{y}}, \text { dynes } / \mathrm{cm}^{2}
\end{aligned}
\] & \[
\begin{aligned}
& \text { VISCOSITY } \\
& \text { PARAMETER } \\
& \mu_{1}^{\prime} \text {, poise }
\end{aligned}
\] & \[
\begin{gathered}
\text { TIME PARAMETER } \\
\mathrm{t}_{1}, \mathrm{~S}
\end{gathered}
\] \\
\hline Biological Sludge & \[
\begin{array}{r}
9,258 \\
8,538 \\
11,969 \\
11,967
\end{array}
\] & \[
\begin{aligned}
& 0.6006 \\
& 0.6400 \\
& 1.5625 \\
& 2.0306 \\
& \hline
\end{aligned}
\] & \[
\begin{aligned}
& 0.77 \\
& 0.70 \\
& 1.30 \\
& 1.50 \\
& \hline
\end{aligned}
\] & \[
\begin{aligned}
& 0.0380 \\
& 0.0340 \\
& 0.0465 \\
& 0.0586 \\
& \hline
\end{aligned}
\] \\
\hline Alum Sludge & \[
\begin{aligned}
& 12,688 \\
& 13,362 \\
& 11,447 \\
& 11,573 \\
& 11,613 \\
& 11,493
\end{aligned}
\] & \[
\begin{aligned}
& 4.0000 \\
& 4.1006 \\
& 2.6406 \\
& 2.8900 \\
& 2.7225 \\
& 3.5156 \\
& \hline
\end{aligned}
\] & \[
\begin{aligned}
& 2.15 \\
& 2.25 \\
& 1.65 \\
& 1.80 \\
& 1.50 \\
& 1.85 \\
& \hline
\end{aligned}
\] & \[
\begin{aligned}
& 0.0760 \\
& 0.0805 \\
& 0.0617 \\
& 0.0673 \\
& 0.0554 \\
& 0.0726
\end{aligned}
\] \\
\hline Physico-Chemical Sludqe & \[
\begin{aligned}
& 42,309 \\
& 42,396 \\
& 13,818 \\
& 11,493 \\
& 14,766 \\
& 12,596 \\
& \hline
\end{aligned}
\] & \[
\begin{aligned}
& 2.0306 \\
& 2.2500 \\
& 0.4556 \\
& 0.2627 \\
& 0.5439 \\
& 0.2500 \\
& \hline
\end{aligned}
\] & \[
\begin{aligned}
& 1.45 \\
& 1.45 \\
& 0.42 \\
& 0.30 \\
& 0.48 \\
& 0.34 \\
& \hline
\end{aligned}
\] & \[
\begin{aligned}
& 0.0560 \\
& 0.0571 \\
& 0.0533 \\
& 0.0393 \\
& 0.0472 \\
& 0.0740
\end{aligned}
\] \\
\hline Secondary Digested Sludge & \[
\begin{aligned}
& 24,537 \\
& 26,693 \\
& 22,040 \\
& 18,837 \\
& \hline
\end{aligned}
\] & \[
\begin{aligned}
& 4.1006 \\
& 4.9506 \\
& 2.9327 \\
& 1.5625 \\
& \hline
\end{aligned}
\] & \[
\begin{aligned}
& 2.40 \\
& 3.00 \\
& 1.78 \\
& 1.17 \\
& \hline
\end{aligned}
\] & \[
\begin{aligned}
& 0.0763 \\
& 0.0822 \\
& 0.0729 \\
& 0.0718 \\
& \hline
\end{aligned}
\] \\
\hline Mixture of Primary and Secondary Sludge & \[
\begin{array}{r}
20,820 \\
20,586 \\
\hline
\end{array}
\] & \[
\begin{array}{r}
2.0664 \\
2.1025 \\
\hline
\end{array}
\] & \[
\begin{array}{r}
1.40 \\
1.52 \\
\hline
\end{array}
\] & \[
\begin{aligned}
& 0.0613 \\
& 0.0669 \\
& \hline
\end{aligned}
\] \\
\hline
\end{tabular}

Chapter 5. The rate of shear and non-Newtonian viscosity values were plotted on a semi-log graph paper. For pseudoplastic fluids, this curve became a straight line at a high rate of shear. By extending this straight line part of the curve to the viscosity, Y, axis at zero rate of shear, the value of viscosity parameter was obtained. The slope of this straight line portion of the curve was used as the initial value of the time parameter. The same procedure was repeated for all sludge samples. The typical plots are shown in Figure 6.28, Figure 6.29, Figure 6.30, Figure 6.31, and Figure 6.32. The initial value of time and viscosity parameters for different types of sludges are presented in Table 6.9.

The initial values for all 3 parameters along with the experimental viscosity data were fed into the computer program for non-linear regression to fit the Dekee model. The corrected values of yield stress for all types of sludges are shown in Table 6.10, Table 6.11, Table 6.12, Table 6.13, and Table 6.14. The Dekee model was applied to only those sludge samples which exhibited a pseudoplastic behaviour with a yield stress, and not to those samples which showed a behaviour of Bingham plastic fluids.

The observed behaviour for different types of sludges is presented in Table 6.15.


Figure 6.28: Plot to Estimate Initial Values of Time and Viscosity Parameters in Dekee Model for Biological Sludges



Figure 6.30: Plot to Estimate Initial Values of Time and Physico-Chemical Sludges



Table 6.10 - SUMMARY OF YIELD STRESS VALIES FOR BIOLOGICAL SLUDGES (DEKEE MODEL)
\begin{tabular}{|c|c|c|c|}
\hline SLUDCE TYPE & SUSPENDED SOLIDS CONCENIRATION mg/L & \[
\begin{gathered}
\text { YIELD S } \\
\text { dynes/cm²}
\end{gathered}
\] & \[
\begin{gathered}
\text { SS, }{ }^{\tau}{ }_{y}{ }^{2} / \mathrm{m}^{2}
\end{gathered}
\] \\
\hline Mixed Liquor (Biological) & 2,491 & 0.0200 & 0.0020 \\
\hline Mixed Liquor (Biological) & 2,909 & 0.0400 & 0.0040 \\
\hline Mixed Liquor (Biological) & 2,387 & 0.0100 & 0.0010 \\
\hline Settled Mixed Liquor (Activated Sludge) & 9,258 & 0.7688* & 0.0767 \\
\hline Mixed Liquor (Biological) & 1,908 & 0.0175 & 0.00175 \\
\hline Mixed Liquor (Biological) & 2,708 & 0.0500 & 0.0050 \\
\hline Settled Mixed Liquor (Activated Sludge) & 8,538 & 1.0330* & 0.1033 \\
\hline Mixed Liquor (Biological) & 3,787 & 0.13 & 0.0130 \\
\hline Mixed Liquor (Biological) & 3,851 & 0.14 & 0.0140 \\
\hline Settled Mixed Liquor (Activated Sludge) & 11,969 & 2.3144* & 0.2314 \\
\hline Settled Mixed Liquor (Activated Sludge) & 11,967 & 2.9370* & 0.2937 \\
\hline \multicolumn{4}{|l|}{*Only these values were estimated using the Dekee Model; the rest were from the graphical method.} \\
\hline
\end{tabular}

Table 6.11 - SUMMARY OF YIELD STRESS VALUES FOR ALUM SLUDGES FROM WATER TREATMENT PLANT (DEKEE MODEL)
\begin{tabular}{|c|c|c|c|}
\hline SLUDGE TYPE & SUSPENDFD SOLIDS CONCENIRATION \(\mathrm{mg} / \mathrm{L}\) & \[
\begin{array}{r}
\text { YIELD S } \\
\text { dynes/cm }
\end{array}
\] & \[
\begin{gathered}
\text { SS, } \quad{ }^{\tau} \mathrm{Y} \\
\mathrm{~N} / \mathrm{m}^{2}
\end{gathered}
\] \\
\hline Alum Sludge & 3,099 & 0.0700 & 0.0070 \\
\hline Alum Sludge & 3,097 & 0.0750 & 0.0075 \\
\hline Settled Alum Sludge & 12,688 & 4.0090* & 0.4000* \\
\hline Settled Alum Sludge & 13,362 & 3.7100* & 0.3710* \\
\hline Alum Sludge & 2,985 & 0.0750 & 0.0075 \\
\hline Alum Sludge & 3,128 & 0.0700 & 0.0070 \\
\hline Settled Alum Sludge & 11,447 & 3.3553* & 0.3355* \\
\hline Settled Alum Sludge & 11,613 & 3.0881* & 0.3088* \\
\hline Alum Sludge & 2,732 & 0.0300 & 0.0030 \\
\hline Alum Sludge & 2,697 & 0.0400 & 0.0040 \\
\hline Settled Alum Sluage & 11,573 & 3.6175* & 0.3618* \\
\hline Settled Alum Sludqe & 11,493 & 4,3261* & 0.4326* \\
\hline \multicolumn{4}{|l|}{*Only these values were estimated using the Dekee Model; the rest were from the graphical method.} \\
\hline
\end{tabular}

Table 6.12 - SUMMARY OF YIELD STRESS VALUES FOR PHYSICD-CHEMICAL WASTEWATER SLUDGES (DEKEE MODEL)
\begin{tabular}{|c|c|c|c|}
\hline SLUDGE TYPE & SUSPENDED SOLIDS CONCENIRATION \(\mathrm{mg} / \mathrm{L}\) & \multicolumn{2}{|l|}{\[
\begin{gathered}
\text { YIELD STRESS, }{ }^{\tau} \mathrm{y} \\
\text { dynes } / \mathrm{cm}^{2} \quad \mathrm{~N} / \mathrm{m}^{2}
\end{gathered}
\]} \\
\hline Diluted Physico-Chemical Sludge from Underdrain & 3,557 & negligible & - \\
\hline Diluted Physico-Chemical Sludge from Underdrain & 1,649 & negligible & - \\
\hline Physico-Chemical Sludge from Underdrain & 42,309 & 2.7466 & 0.2747 \\
\hline Physico-Chemical Sludge from Underdrain & 42,396 & 3.0903 & 0.3090 \\
\hline Physico-Chemical Sludge from Clarifier & 675 & negligible & - \\
\hline Physico-Chemical Sludge from Clarifier & 784 & negligible & \\
\hline Settled Physico-Chemical Sludge from Clarifier & 13,818 & 0.5940 & 0.0594 \\
\hline Settled Physico-Chemical Sludge from Clarifier & 11,493 & 0.4247 & 0.0425 \\
\hline Physico-Chemical Sludge from Clarifier & 5,255 & negligible & ----- \\
\hline Physoci-Chemical Sludge from Clarifier & 5,897 & negligible & ---- \\
\hline Settled Physico-Chemical Sludge from Clarifier & 14,766 & 0.7818 & 0.0782 \\
\hline Settled Physion-Chemical Sludge fram Clarifier & 12,596 & 0.2116 & 0.0212 \\
\hline
\end{tabular}

Table 6.13 - SUMMARY OF YIELD STRESS VALUES FOR SECONDARY DIGESTED SLUDGES (DEKEE MODEL)
\begin{tabular}{|c|c|c|c|}
\hline SLUDGE TYPE & SUSPENDED SOLIDS CONCENIRATION mg/L & \multicolumn{2}{|l|}{\[
\begin{gathered}
\text { YIELD SIRESS, }{ }^{\tau} \mathrm{Y} \\
\text { dynes } / \mathrm{cm}^{2} \quad \mathrm{~N} / \mathrm{m}^{2}
\end{gathered}
\]} \\
\hline Diluted Secondary Digested Sludge & 24,537 & 5.0701 & 0.5070 \\
\hline Diluted Secondary Digested Sludge & 26,693 & 5.8247 & 0.5825 \\
\hline Diluted Secondary Digested Sludge & 18,837 & 1.9707 & 0.1971 \\
\hline Diluted Secondary Digested Sludge & 22,040 & 3.5574 & 0.3557 \\
\hline
\end{tabular}

Table 6.14 - SUMMARY OF YIELD STRESS VALUES FOR MIXIURE OF PRIMARY AND SECONDARY SEITLED SLUDGES
\begin{tabular}{|c|c|c|c|}
\hline SLUDGE TYPE & SUSPENDED SOLIDS CONCENIRATION \(\mathrm{mg} / \mathrm{L}\) & \multicolumn{2}{|l|}{\[
\begin{gathered}
\text { YIELD STRESS, }{ }^{\mathrm{T}} \mathrm{y} \\
\text { dynes } / \mathrm{cm}^{2} \quad \mathrm{~N} / \mathrm{m}^{2}
\end{gathered}
\]} \\
\hline Mixture of Primary and Secondary Settled Sludge & 20,586 & 2.2232 & 0.2223 \\
\hline Mixture of Primary and Secondary Settled Sludge & 20,820 & 2.2017 & 0.2202 \\
\hline
\end{tabular}

Table 6.15 - OBSERVED BEHAVIOUR OF DIFFERENT SLUDGES
\begin{tabular}{|ll|}
\hline \multicolumn{1}{|c|}{ SLUDGE TYPE } & \multicolumn{1}{c|}{ BEHAVIOUR } \\
\hline Mixed Liquor & Bingham Plastic \\
Settled Mixed Liquor & Pseudoplastic with Yield Stress \\
Alum Sludge & Bingham Plastic \\
Settled Alum Sludge & Pseudoplastic with Yield Stress \\
Diluted Physico-Chemical Sludge (from Underdrains) & Close to Dilatant Fluid \\
Physico-Chemical Sludge (fram Underdrains) & Pseudoplastic with Yield Stress \\
Physico Chemical: Sludge (fram Clarifiers) & Close to Dilatant Fluid \\
Settled Physico-Chemical Sludge (fram Clarifiers) & Pseudoplastic with Yield Stress \\
Diluted Secondary Digested Sludge & Pseudoplastic with Yield Stress \\
Mixture of Primary and Secondary Sludge & Pseudoplastic with Yield Stress \\
\hline
\end{tabular}

\subsection*{6.3.2.2 Relationship Between Yield Stress and Suspended Solid: Concentration}

When the suspended solids concentration and corresponding yield stress value for each type of sludge sample was plotted on a logarithmic graph paper, it was noticed that a straight line relationship between suspended solids concentration and yield stress existed. Plots between 'log of suspended solids concentration and log of yield stress' for different types of sludges are" shown in Figure 6.33, Figure 6.34, Figure 6.35, Figure 6.36, and Figure 6.37 for results obtained using graphical method and in Figure 6.38, Figure 6.39, Figure 6.40, Figure 6.41, and Figure 6.42 for results obtained using the Dekee Model. A correlation between these two parameters was developed using a linear regression analysis as discussed in section 6.1. Therefore, two sets of equations for each type of sample have been developed. One set of equations correlates the values of yield stress obtained using the graphical method, and the other set of equations correlates the values estimated using the Dekee model. Since the Dekee model was not applied to those sludge samples which exhibited Bingham plastic flow Characteristics, the same yield stress values obtained using the graphical method were also used in developing the second set of equations using values estimated by the Dekee model. All these equations developed for the respective sludge samples to estimate the yield stress for different types of
sludges by knowing their suspended solids concentration are shown in Table 6.16. Plots overlapping the obtained values of yield stress from graphical method and estimated value of yield stress from the least square equation for different types of sludges are shown in Figure 6.43, Figure 6.44, Figure 6.45, Figure 6.46. Similarly plots of calculated values of yield stress from Dekee model and estimated values from least square equation are shown in Figure 6.47, Figure 6.48, Figure 6.49, and Figure 6.50.


\footnotetext{
Figure 6.33: Relationship Between Yield
Suspended Solids Concentration Stress and for Biological Sludges (Graphical Method)
}


Figure 6.34: \(\left.\begin{array}{l}\text { Relationship Between Yield Stress and } \\ \text { Suspended Solids Concentration for Alum } \\ \text { Sludges (Graphical Method) }\end{array}\right)\).

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\section*{PHYSICO CHEMICAL WASTEWATER SLUDGE (USING GRAPHICAL METHOD)}


Figure 6.35: \(\begin{aligned} & \text { Relationship Between Yield Stress and } \\ & \text { Suspended Solids Concentration for Physico- } \\ & \text { Chemical Sludges. (Graphical Method) }\end{aligned}\)


Figure 6.36: Relationship Between Yield Stress and Suspended Solids Concentration for Secondary Digested Sludges (Graphical Method)


Figure 6.37: Relationship Between Yield Stress and Suspended Solids Concentration for Mixture of Primary and Secondary Sludges (Graphical Method)

\title{
BIOLOGICAL MIXED LIQUOR (USING DEKEE MODEL)
}


Figure 6.38: Relationship Between Yield Stress and Suspended Solids Concentration for Biological Sludges (Dekee Model)

\section*{alum sludge from water treatment plant (USING DEKEE MODEL)}

\(\begin{array}{ll}\text { Figure 6.39: } & \begin{array}{l}\text { Relationship Between Yield Stress and } \\ \text { Suspended Solids Concentration for Alum } \\ \text { Sludges (Dekee Model) }\end{array}\end{array}\)


Figure 6.40: Relationship Between Yield Stress and Suspended Solids Concentration for PhysicoChemical Sludges (Dekee Model)

SECONDARY DIGESTED SLUDGE, DILUTED (USING DEKEE MODEL)


Figure 6.41: Relationship Between Yield Stress and Suspended Solids Concentration for Secondary Digested Sludges (Dekee Model)

\section*{MIXTURE OF PRIMARY AND SECONDARY SLUDGE, DILUTED (USING DEKEE MODEL)}

- Figure 6.42: Relationship Between Yield Stress and Suspended Solids Concentration for Mixture of Primary and Secondary Sludges (Dekee Model)
table 6.16. equations CORRELATING yield stress and suspended solids concentration
\begin{tabular}{|c|c|c|c|}
\hline No. & SLUDGE TYPE & GRAPHICAL METHOD & DEKEE MODEL \\
\hline 1 & Biological Mixed Liquor & Log (Yield Stress) \(=2.9116\) Log (SS) - 11.4546 & Log (Yield Stress) \(=2.9170\) Log (SS) - 11.4739 \\
\hline 2 & Alum Sludge from Water Treatment plant & Log (Yield Stress) \(=2.9922\) Log (SS) - 11.6296 & Log (Yield Stress) \(=2.9704\) Log (SS) - 11.5540 \\
\hline 3 & Physico-Chemical Wastewater Sludge & Log (Yield Stress) \(=1.5992\) Log (SS) - 6.9124 & Log (Yield Stress) \(=1.6218\) Log (SS) - 7.0284 \\
\hline 4 & Secondary Digested Sludge & Log (Yield Stress) \(=3.2135\) Log (SS) - 13.4194 & \({ }^{\prime}\) Log (Yield Stress) \(=3.1855\) Log (SS) - 13.3055 \\
\hline 5 & Mixture of Primary and Secondary Sludge & Insufficient Data & Insufficient Data \\
\hline
\end{tabular}

Note: \(\quad\) SS = Suspended solid concentration, mg/L
Yield Stress, dynes/cm²

\section*{BIOLOGICAL MIXED LIQUOR \\ (USING GRAPHICAL METHOD)}


Figure 6.43: Observed Values of Yield Stress By Graphical Method and Estimated Values By Developed Equation for Biological Sludges

\section*{ALUM SLUDGE FROM WATER TREATMENT PLANT (USING GRAPHICAL METHOD)}


Figure 6.44: Observed Values of Yield Stress By-Graphical Method and Estimated Values By Developed Equation for Alum Sludges

\section*{PHYSICO CHEMICAL WASTEWATER SLUDGE} (USING GRAPHICAL METHOD)


Figure 6.45: Observed Values of Yield Stress By Graphical Method and Estimated Values By Developed Equation for Physico-Chemical Sludges

\section*{SECONDARY DIGESTED SLUDGE, DILUTED (USING GRAPHICAL METHOD)}


Figure 6.46: Observed Values of Yield Stress By. Graphical Method and Estimated Values By Developed Equation for Secondary Digested Sludges


Figure 6.47: Calculated Values of Yield Stress By Dekee Model and Estimated Values By Developed Equation for Biological Sludges

\section*{ALUM SLUDGE FROM WATER TREATMENT PLANT (USING DEKEE MODEL)}


Figure 6.48: Calculated Values of Yield Stress.By Dekee Model and Estimated Values By Developed Equation for Alum Sludges


Figure 6.49: Calculated Values of Yield Stress.By Dekee Model and Estimated Values By Developed Equation for Physico-Chemical Sludges


\footnotetext{
Figure 6.50: Calculated Values of Yield Stress By Dekee Model and Estimated Values By Developed Equation for Secondary Digested Sludges
}

\subsection*{6.4 Model for Aeration Tank}

A model, which optimizes the energy requirement in an aeration tank, was developed by correlating the various parameters which influence the process of mixing and affect the horizontal velocity close to the tank bottom. Experiments were run in a laboratory size aeration tank to identify various parameters. All the experimental data collected during the experiments, calculated parameters and dimensionless factors are shown in the following sections:

\subsection*{6.4.1 Experimental Data}

Details of the experimental setup and equipment used to measure different parameters have been provided in the previous chapters.

Experiments were run to measure the horizontal velocities at different points along the water depth during different operating conditions. During the experiment, the length of the tank, \(L\), was kept constant at 0.69 m , whereas the width of the tank, \(W\), was changed to \(2.44 \mathrm{~m}, 2.21 \mathrm{~m}, 1.98 \mathrm{~m}, 1.75\) \(\mathrm{m}, 1.52 \mathrm{~m}, 1.29 \mathrm{~m}\) and 1.06 m . For each width, the depth of water, H , was changed to \(0.50 \mathrm{~m}, 0.65 \mathrm{~m}, 0.80 \mathrm{~m}, 0.95 \mathrm{~m}\) and 1.10 m . For each depth of water and each width of the tank, both the submergence of the diffuser and the air flow rate were changed. The velocity profiles obtained for different operating conditions in the aeration tank are tabulated in Appendix \(C\). Since the development of model was based on the horizontal velocity, \(u\), 25 mm above the tank bottom, only
these velocity values at different operating conditions are provided in Appendix \(D\).

\subsection*{6.4.2 Rate of Power}

The theoretical rate of power, useful rate of power based on isothermal expansion of the air at the outlet or diffuser and useful power based on adiabatic conditions, available at the outlet or diffuser, as described in Chapter 5, were calculated and are summarized in Appendix E. The corresponding air flow rates for standard conditions, STP, and actual operating conditions, are also given in these Tables.

\subsection*{6.4.3 Dimensionless Factors}
Different dimensionless factors relating various
operating conditions as described in Chapter 5 were
calculated for each operating condition separately. The
operating conditions for which the dimensionless factors
were calculated are summarized in Appendix F, and
corresponding dimensionless factors are provided in Appendix
G.

\subsection*{6.4.4 Development of Model}

In the development of the model the linear regression techniques on were employed as described in Chapter 5. The basic model Eq. 5.58 was in non-linear form; therefore, this equation was linearized first to get the values of the coefficients. The values of different coefficients and
constant were obtained using a SAS statistical package called REG. Before the final model was decided to predict the value of horizontal velocity, \(u\), at 25 mm above the aeration tank floor under various operation conditions, different statistical parameters as they are listed below, were considered and then the best model was obtained.

R - SQUARE Value - Coefficient of Determination
F Test Value
PR > F - Significance Probability
T FOR HO: PARAMETER \(=0\) - Student's \(t\) test
\(P R>|T|\)

The selected model involving all the five dimensionless factors to predict the horizontal velocity, \(u\), is shown below:


\section*{Chapter VII}

\section*{DISCUSSION OF RESULTS}

The results shown in the previous chapter are discussed in this section.

\subsection*{7.1 Critical Bed Shear}

The critical bed shear force on a particle is defined as the minimum shear force necessary for the initiation of particle motion. Since the direct measurement of bed shear force or shear stress is a complex and elaborate procedure, normally it is estimated through other experimental parameters which are simpler to measure. The accuracy of the results depends upon the boundary conditions and the assumptions made during the development of theory. Several procedures have been proposed in the literature to estimate the bed shear stress during critical conditions for the initiation of the motion of particles. In this study, Eqs. 5.6 and 5.7 were used to calculate the critical shear or friction velocity, \(U_{*_{C}}\). After calculating the shear or friction velocity from the laboratory flume data, the critical bed shear stress, \(\tau\), , values were estimated using Eq. 5.5. The point velocity, \(u\), observed close to the bed in the laboratory flume was used as a basic parameter to
estimate the values of critical bed shear for different types of particles.

\subsection*{7.1.1 Grit and Gravel Particles}

The grit samples were collected from the West Windsor Pollution control plant, washed several times to remove decomposable organic matter and then dried in an oven. The dried grit was sieved into eight geometric mean sizes, ranging from 0.2121 mm to 2.1817 mm , Table 4.1 . In order to widen the scope of this investigation, some larger gravel particles, ranging in size from 3.4 mm to 17.4 mm were also included in these experiments as shown in Table 4.2.

A laboratory flume was used to measure point velocities during critical conditions to initiate the motion of these particles. For these observations, the flow had to be fully developed before any measurements of point velocity were made. The development of flow (boundary layer) was done by covering the bed of the flume by the same size of the particles used for the experiment, except a 0.65 m long stretch at the middle of the flume was left smooth to observe the movement of particles. The accuracy of the critical bed shear stress value depends on how close to the bed is the point velocity measured. Due to the restrictions imposed by the velocity meters, point velocities closer than 7.6 mm above the flume bed were not measured.

A grit chamber resembles closely in shape and hydraulic characteristics to typical channels used in hydraulics
engineering. Therefore, the equations developed for open channels can also be applied in the study of grit chambers.

The current design practice of gravity type grit chambers is generally based upon the concept of a discrete particle settling under ideal conditions - assuming that all particles settle in accord with Newton's Law, liquid velocity is the same in all parts of the chamber, and there are no eddies [18]. However, in an actual chamber the yelocity is not uniform and there are eddies present due to turbulence which retard settling. An increase in chamber velocity increases the scour of the settled material. Therefore, it is the scouring process and not the settling process which determines the design flow velocity for grit chamber. Using the Shields' findings of the scouring of bed material, Camp [18] came up with a relationship as shown in Eq. 2.1. Camp also proposed the use of parabolic channel. It is apparent from Eq. 2.1 for scour velocity that the depth of flow in the channel has no influence on the critical mean velocity. This is not quite true because, even if the mean velocity of flow in a channel remains the same for different depths of flow, the velocity profile still changes with depth. Consequently, the scouring velocity on the channel bed is influenced by the depth of flow. Therefore, it is not justified to ignore the influence of flow depth in the grit chamber design while calculating the critical scouring velocity. For example, two different channels may have flat
beds of identical particles and therefore will require the same bed shear stress to move the particles. Assuming a similar velocity distribution profile, the velocities at any given distance above the bed should also be the same in these two channels. However, since the mean velocity occurs at \(y\) equal to a constant fraction of the depth, Eq. 5.17, the deeper flow depth will have a higher mean velocity.

A new approach has been suggested to design a grit chamber using the concept of critical shear. stress rather than a critical mean velocity. The advantage of using shear stress to specify the critical scouring conditions is that only one quantity is enough, whereas if mean velocity is used, one must also consider the depth of flow and location along the depth at which the mean velocity is observed or computed.

The observed mean values of point velocity, \(u\), at 7.6 mm above the bed for critical conditions are shown in Table 6.1 These values are the average of data obtained at two locations in the flume, \(A\) and \(B\), as shown in Figure 3.1. The calculated critical shear velocities, \(U_{*_{C}}\), and corresponding particle Reynolds number, regime of flow for different sizes of grit and gravel particles are also shown in Table 6.1. The particle sizes and corresponding values of critical bed shear stress are shown in Table 6.2. The particle sizes and the corresponding values of shear stress are plotted on LogLog scale in Figure 6.4. This plot shows that in the
hydraulically smooth flow regime, particle Reynolds number, \(U_{*} k_{s} / v \leqq 5\) the influence of fluid viscosity is predominant and the curve is a straight line. It means that the particles of sizes 0.4 mm or smaller will keep the flow hydraulically smooth. However, for rough turbulent flow conditions, particle Reynolds number, \(\quad U_{*} k_{s} / V \geqq 70\), the influence of bed roughness becomes more significant. During this regime of flow, the plot between particle sizes and corresponding shear stress values becomes curvilinear, and the influence of viscosity on the value of critical shear stress is negligible. The shape factor for the grit and gravel particles also had an effect on the nature of relationship in the turbulent region. It has been reported [10] that the influence of shape factor on the drag coefficient increases with an increasing Reynolds number. In the transitional state, \(5 \leqslant U_{*} k_{s} / v \leqq 70\), the influence of both viscosity and roughness are dominating the shear stress and the plot changes from a straight line to a curve. This plot can be used directly in finding the critical bed shear stress required to initiate the motion of any size of grit particle within specified conditions. This will also indicate the regime of flow in a channel whose bed is made up of uniform size of grit or gravel particles.

The best fit equation, Eq. 6.1, developed for the plot between particle sizes and corresponding values of shear stress was tested for different statistical parameters as
discussed in Section 6.1. The value of most important statistical parameter, i.e. coefficient of determination for this equation was 0.994. This implies that \(99.4 \%\) of the variation in critical shear stress is accounted by the model. The values of the other statistical parameters as discussed in Chapter 6 were also favourable.

Substantial amount of work on the relationship between particle size and critical shear has been done in the field of hydraulics engineering, but most of the work is applicable to river channels [55,91] and packed bed laboratory flumes'[81]. The two popular curves for critical bed shear were given by U.S.B.R. [91] and Shields [81]. The critical bed shear values obtained from these curves are higher than those obtained in this investigation. The data reported in Table 6.2 and Figure 6.4 are for the operating conditions normally encountered in grit chambers i.e., a bed made up of scattered grit particles. In a typical grit chamber, the accumulation of grit particles is not permitted. Therefore, the grit chamber bed can neither be considered as a packed bed as used by Shields nor as a river channel or canal with a higher content of fine sediment as used by U.S.B.R. and Lane \([54,55]\).

\subsection*{7.1.2 Sludge Particles}

Some units in the treatment of water and wastewaters are designed to keep all the particles in suspension, whereas some other units are designed to allow the settling of these particles. For example, aeration tanks, flocculation chambers and mixing chambers are designed to keep all the particles in suspension all the time. On the other hand, settling tanks are designed to allow the settling of all settleable particles. Similarly gritt chambers are designed to allow the removal of heavy inert particles keeping all the decomposable organic particles in suspension.

The experiments with sludge particles were conducted to determine the critical bed shear stress, \(\tau_{o c}\), required to initiate the motion of settled particles in treatment units. Different types of sludge samples were collected both from water and wastewater treatment plants as shown in Table 4.3. Those sludge samples, which were not settled when collected, were allowed to settle for 3 to 4 hours and the settled sludge was used in the flume to run the scouring experiments. The settled sludge was more representative of the actual field conditions, because it is the settled sludge particles that have to be moved in a treatment unit or mixing chamber.

With a very low velocity of flow in the flume, the sludge flocs were poured and uniformly spreaded over the flume bed. Then the velocity of flow was increased slowly till the
settled sludge started scouring. During this critical condition of the motion of sludge particles, the velocity profiles were obtained along the depth of flow at two locations, \(A\) and \(B\), Figure 3.1, along the length of the flume. The horizontal point velocity, \(u, 7.6 \mathrm{~mm}\) above the bed, was used as the basic parameter to estimate the value of critical bed shear stress for different types of sludge samples. Due to the restrictions imposed by the velocity meters, the point velocity any closer to the bed could not be measured. This point velocity, \(u\), was used in Eq. 5.6 to Obtain the critical shear or friction velocity, \(U_{*_{C}}\). Then Eq. 5.5 was used to estimate the critical bed shear stress value. All the estimated critical shear stress values are shown in Table 6.3, for different types of sludge samples analyzed. In most of the treatment units and mixing chambers, except sedimentation tanks, the particles are not allowed to settle, if the units are designed properly. Therefore, it is reasonable to assume that the bed of such treatment unit is smooth.

Once the sludge particles had settled down in the flume, the thickness of the layer on the bed did not seem to make a significant difference in the value of critical bed shear stress. The top layer of the sludge scoured first, followed by the next layer and eventually all the sludge particles were in suspension. The physical characteristics of the sludge particles, such as floc strength, are expected to, but not significantly, influence the critical shear stress.

The critical shear stress value for a given sludge indicates the minimum bed shear stress necessary that must be provided in the treatment unit in which the settling of similar particles is not permitted. The horizontal velocity close to the bed will have to be kept higher than the velocity needed to achieve the critical shear stress.

\subsection*{7.2 Yield Stress of sludges}

It has been long recognized, also confirmed in this investigation, that the sludge samples behave more closely to the non-Newtonian fluid than to the Newtonian. Therefore, all the sludge samples were treated as non-Newtonian fluids. The yield stress, \(\tau^{\tau}{ }^{\prime}\) ' is defined as the stress which must be exceeded before any flow starts. A fluid or suspension at rest contains a three dimensional structure of sufficient rigidity to resist any stress less than the yield stress, \({ }^{\tau} y\). For Bingham plastic fluids, if this stress is exceeded, the structure completely disintegrates and the system behaves as a Newtonian fluid due to a shear stress, \(\tau-{ }^{\tau} y\). It is therefore suggested that the maximum shear allowed in the aeration tank or in any other unit, where the shearing of the flocs or particles is unwanted, should always be less than yield stress value for that suspension. If the applied shear through diffused aeration, mechanical aeration or other means exceeds the yieldstress, then the floc or particles would start shearing. The settling properties of
the particles will deteriorate and the removal efficiency of these flocs or particles in settling units will decrease.

Yield stress values for different sludges were obtained with Brookfield Viscometer as described in Chapters 5 and 6 and presented in Tables 6.4-6.8. Flow curves for different sludge samples, Figs. 6.7-6.22, were found to represent characteristics of different types of sludges. The observed behaviour of different types of sludges are shown in Table 6.15.

Babbitt and Caldwell [12,13], Behn [14], Bokil and Bewtra [15] and Dick [24,25] have shown sludges to behave as Bingham plastic fluid. However the results obtained in this study were different. For mixed liquor and alum sludge (water treatment plant) the flow curves were close to Bingham plastic fluids. But when these samples were allowed to settle and analyzed again, they behaved like pseudoplastic fluids with certain yield stress. The physico chemical sludge (wastewater treatment plant) collected from the secondary clarifier behaved altogether differently. At low concentrations; the flow curves were similar to those for dilatant fluids without any yield stress. When these samples were allowed to settle and settled sludge was analyzed, the flow curves became similar to those for pseudoplastic fluids with certain yield stress. When the physico-chemical sludge was collected from the underdrains which take the sludge to the dewatering facility for the
same plant and diluted, it also behaved close to dilatant fluid without any yield stress, whereas the same sludge in concentrated form behaved as pseudoplastic fluid with a yield stress value. Other sludges such as secondary digested sludge, mixture of primary and secondary sludges, also behaved as pseudoplastic fluids with yield stress values. Therefore, it can be said that the behaviour of sludges changes with the concentration of suspended solids and the physical state of the sample, - suspended or settled. Suspended sludge samples do behave more closely to the Bingham plastic fluids as found by other researchers also, but the behaviour of settled sludge changes to pseudoplastic fluid with a certain yield stress.

The change in the behaviour of sludge samples with suspended solids concentration may be due to the flocculent nature of the solid particles. Dilute concentrations of sludge particles disrupt fluid stream lines and increase the viscosity without imparting non-Newtonian behaviour. As the concentration of the solid phase increases, an opportunity for more complex rheological behaviour exists. Not only do particle-liquid interactions exist, but also, particleparticle interactions and particle deformation can occur. A pronounced change in rheological behaviour takes place when the volumetric concentration of solids increases to the extent that a continuous solid phase can exist. Now instead of deforming continuously in response to an applied stress,
the suspension can resist deformation until sufficient stress is applied to exceed the yield strength of the solid phase. Then the suspension assumes properties more like a fluid. In case of lower concentration of suspended solids, a weak continuous solid phase did seem to exist, which resulted in Bingham plastic type fluid behaviour. However, in higher concentration of suspended solids in different sludges, particle-particle interaction resulted in a pronounced change in behaviour of "sludge samples and they exihibited pseudoplastic behaviour with a yield stress value. However, the behaviour of sludge makes no difference in the value of yield stress, which is the most important design parameter for different treatment units.

\subsection*{7.2.1 Relationship Between Yield Stress and Suspended}

\section*{Solids Concentration}

When \(\log (s u s p e n d e d\) solids concentration) and corresponding log(yield stress) values were plotted, they showed a straight line relationship, Figs. 6.33-6.37. This relationship was true with all types of sludge samples analyzed. Therefore, these plots can be used directly to obtain the value of yield stress at different suspended solids concentration. It is shown in Figs. 6.7-6.22, the behaviour and flow curve of sludges may be different at different suspended solids concentrations, but the yield stress values do not change with the behaviour.

Equations correlating the log(yield stress) and \(\log (s u s p e n d e d\) solids concentration) also have been developed using linear, regression technique, Table 6.16. These equations were tested for different statistical parameters for reliability of the model. The most important parameter during the evaluation of the model was the R-SQUARE, the coefficient of determination. For all the correlations, this value varied between 0.88 and 0.99 , i.e., \(88 \%\) to \(99 \%\) of variations in yield stress are accounted by the selected models. Other statistical parameters as mentioned in Chapter 6 also had favourable values.

Yield stress values were obtained using both graphical method and Dekee model as discussed in Chapters 5 and 6. The set of equations developed using graphical method was considered more reliable than the set of equations developed using the yield stress values obtained by Dekee model. The reason is that the yield stress obtained with Dekee model would be only as good as the basic experimental data used in the model, whereas in the graphical method, one can see the change in the behaviour of fluids and any experimental error can be visualised. However, when only limited data are available and a good flow curve is difficult to obtain, then the use of Dekee model may be appropriate. It is recommended to check the values of yield stress obtained using graphical method with Dekee model.

The plots between log(yield stress) and log(suspended solids concentration) also give the critical suspended solids concentration at which the yield stress value can be considered as negligible, below the accuracy of measurement.

\subsection*{7.3 Model for Aeration Tank}

It is a common practice in the operation of aeration tanks to maintain a certain minimum dissolved oxygen all the time. However, the minimum velocity requirements in the aeration tank to keep the biological flocs in suspension have not been given much consideration. The operating parameters which influence the velocity profiles in the aeration tanks have also not been fully investigated.

In this study, the important controlling parameters in the operation of aeration tanks to maintain a required horizontal velocity were investigated. Experiments were run in the laboratory size aeration tank under different operating conditions and the data were used to develop a dimensionless model using a linear regression technique. Statistical analysis was carried out to select the best model to predict the horizontal velocity close to the tank's floor under different operating conditions.

The details about the experimental setup, instrumentation, operating parameters, raw data and the
dimensionless factors have been provided in Chapters 3, 4, 5 and 6. The parameters which can influence the velocity, \(u\), in the tank are shown below:
a. rate of power consumption
b. tank length (along the diffusers)
c. tank width
d. water depth in the tank
e. depth of water above the diffusers (submergence)
f. distance of the diffusers from the side wall of the tank

The above mentioned parameters, except the length of the tank, were varied during the experiments and the horizontal point velocity, \(u\), along the depth of water in the tank at mid-width was measured for each operating condition. The rate of power consumption was varied by changing the air flow rate and diffuser submergence. The processed data are shown in Appendix B. These data were converted into dimensionless factors as explained in Chapter 5. A dimensional analysis was performed to establish a relationship between different dimensionless factors, Eq. 5.51. The dimensionless factor involving the horizontal velocity, \(u\), was considered as a dependent variable and other factors which influence the velocity were considered as independent variables.

Surface tension played an insignificant role in the experimental aeration tank due to its size. Surface tension is important in the formation and movement of bubbles in liquid. However, in this dimensional analysis, the details of air bubbles in the aeration tank was not considered. Therefore, the effect of surface tension on this analysis was neglected.

During the process of analyzing Eq. 5.51 critically, a few modifications were made in Eq. 5.51 to make this model more effective and reliable in predicting the velocities under different operating conditions. The length factor term was dropped from Eq. 5.51, because length of the tank ( 0.69 m ) was not changed during the experiments. Since the diffusers are conventionally placed along the length of the aeration tank, the length of the tank makes no significant difference in the spiral motion of the liquid and the velocity. Also, the dimensionless factor involving the distance of diffusers from the side wall of the tank, \(X\), was dropped from Eq. 5.51, because it was noticed during the analysis of data, that a small change in \(X\) made no significant difference in the velocity, u. Statistical analysis also showed that this factor made no significant contribution to the model for predicting velocity. In order to determine the effect of water depth, \(H\),
directly, this term was changed in the form of \(H\) instead of \(\mathrm{H} \%\) in depth factor. The final equation, Eq. 5.52, after making above modifications contains five instead of seven factors.

\subsection*{7.3.1 Calculation of Dimensionless Factors}

The calculations for all dimensionless factors except the power factor, are straight forward. In calculating the power factor, values for rate of power, were obtained by using different assumptions. These power factor values are summarized in Appendix E.

When the compressed air is discharged into the tank through the diffusers, the frictional losses in the pipes, fittings, instrumentation, compressor etc. add to the power requirement. This loss of power is variable and depends on individual layout. In order to neglect the effect of these variable power losses in delivery system and compressor, the actual power available at the outlet was used for further calculations. The values of power obtained using Eqs. 5.54 and 5.55 are very close to each other, Appendix E. The small difference in their values is due to different assumptions made in deriving these equations. Eq. 5.54 was derived based on the assumption of isothermal expansion of the air whereas Eq. 5.55 was derived on the assumption of adiabatic conditions.

For the calculation of useful power available at the outlet or diffusers, the actual air flow rate was used to
obtain the air flow rate under standard conditions, Eqs. 5.56 and 5.57.. This air flow rate takes into account the change in the density of air in the rotameter and piping due to outlet conditions.

\subsection*{7.3.2 Determination of Coefficients for Model Equation}

The derived model, Eq. 5.52 , is in non-linear form and it was linearized by taking log of both sides, Eq. 5.59. The values of unknown coefficients such as \(f, A, B, D\) and \(J\) were determined by applying a'linear regression technique [41]. Various possible combinations were evaluated to obtain the best fit model for predicting the horizontal velocity, u, at 25 mm above the tank floor, under different operating conditions. These analyses included the independent variables individually or their different combinations. The evaluation was done in terms of various statistical parameters shown in Chapter 6. The selected best fit model is shown in Eq. 6.2. The values of test statistical parameters and their importance in predicting the horizontal velocity, \(u\), close to the bed are discussed below:

R SQUARE: This statistical parameter predicts how well a multiple regression model fits a set of data. The value of R\% for the selected model was 0.96 . This implies that \(96 \%\) of the variations in velocity, \(u\), about their mean are accounted for by the model. The value of \(R^{2}\) can range between 0 and 1 and the larger the value the better the model fit.

Sometimes \(R^{2}\) is not considered a dependable test for the adequacy of the model. For example, \(R^{2}\) will be equal to 1 when the number of terms in the model is equal to the number of data points or observations.

F Test: The \(F\) test value predicts how well the model contributed information in predicting horizontal velocity, u, i.e it tests how well the model as a whole accounts for the dependent variable's behaviour.

The computed \(F\) value of the model is compared with statistical \(F_{0.05}\) value

Rejection region for null hypothesis ( \(L=0.05\) ),
\(F>F\)
\[
0.05
\]

Total number of data, \(n=819\)
Degree of freedom, \(k=v_{1}=3\)
\(v_{2}=n-(k+1)=815\)
For \(L=0.05, F_{0.05}=2.60\)
\(F\) value of model \(=6052.97\)
Therefore, \(F \gg F\)
0.05

It indicates that the null hypothesis has been rejected and at least one of the coefficient is nonzero. It means that the selected model did contribute significantly in predicting the horizontal velocity, \(u\). \(F\) test is considered to be a more reliable test for evaluating the adequacy of the model. In final selection of the model the use of both tests is recommended.

PR > F: The significance probability labelled as PR >F was 0.0001 for the selected model, which is a very small number. It signified that the probability of getting a greater \(F\) statistic than that observed in the model was very low. In other words it indicats that the contribution of the model in predicting the value of independent variable was significant.

T FOR HO: PARAMETER=0: After confirming that the model was useful in predicting the value of dependent variable, Fl, it was decided to make inferences about particular independent variables that have practical significance. A test of this hypothesis was performed using a student's \(t\) test. The 't' statistic for testing the null hypothesis that the true coefficients are equal to zero appear under column headed 'T FOR HO: PARAMETER=0'. The ' \(t\) ' values for various. terms in the model were compared with the values obtained in the rejection region for a two tailed test with \(L=0.05\).
```

Rejection Region
$t<-t$
$\mathrm{L} / 2 ; \mathrm{n}-(\mathrm{k}+1)$
$t>t$
$L / 2, n-(k+1)$
Where $n=819=$ number of observations
$k=3=$ number of coefficients in the model,
excluding intercept

```
Values of 't' obtained for the selected model are listed
below:
Term
Intercept
F2
F4/F3
F5

All the ' \(t\) ' values obtained for the model are outside the 't' values for the rejection of hypothesis. Therefore, it \(s\) concluded that all the parameters are contributing significantly in predicting the dependent parameter \(F 1\).
\(\underline{P R O B}>|T|: T h e ~ t w o ~ t a i l e d ~ s i g n i f i c a n c e ~ l e v e l s ~ f o r ~ e a c h ~\) 't' values are listed under the column headed \(P R>|T|\). The values of this parameter express the probability that a 't' statistic would obtain a greater absolute value than that Observed in the model, given that the true parameter is zero. Thus a very small value of this probability indicates that the value of the parameter is not likely to equal zero and therefore the independent variabie contributes significantly to the model. In the selected model, it was found for all the independent variables \(P R>|T|\) values were 0.0001. Therefore it is concluded that all the independent
variables used in the model contributed significantly to the model.

The model was also tested after including dimensionless factor, \(\mathrm{X} / \mathrm{H}\), Eq. 5.51. It was found that the value of PR > |T| was very high. Therefore, it reinforces the reason of elimination of this factor from the model.

\subsection*{7.3.3 Physical Evaluation of the Model}

In this section the critical analysis of the model, Eq. 6.2, has been carried out to determine the physical justification of the equation, i.e. if the relationship between the dependent variable and the independent variables is acceptable in actual opertion of the aeration tank.

Eq. 6.2 shows that the dependent dimensionless factor, Fl, increases when the independent dimensionless factor, F2 increases. Factor \(F 2\), is the power factor, and it is quite Obvious that when more power is put into the system, keeping all other operating conditions same, the horizontal velocity close to the tank's floor will increase. The power input to the system, aeration tank, can be increased by increasing air flow rate and diffuser submergence.

The dimensionless factor, Fl, decreases with an increase in the dimensionless factor, \(F 3\), the width factor. The larger the width of the aeration tank, the smaller will be the horizontal velocity. The fluid motion in diffused aeration tanks is spiral, Fig. 2.1. Therefore, the bigger is the size of the spiral loop for the same operating
conditions, larger will be the energy losses and lower will be the velocities.

The velocity factor, Fl, increases with an increase in the depth factor, F4. In depth factor, only the water depth in the aeration tank was varied and other parameters were kept constant. As the depth of water in the tank increases, the horizontal velocity close to the tank bottom also increases for the same operating conditions. It has been Observed that in deeper water, diffused air bubbles tend to stay longer, which allows these air bubbles to transfer more energy to the water. This transfer or dissipation of energy eventually results in higher water velocity. It is also true that longer the air bubbles stay in water, the more will be the oxygen transfer to the liquid content of the tank. Therefore, an optimum depth of liquid to satisfy both the velocity requirements and the oxygen transfer is important in the design of the aeration tank.

The dimensionless factor \(F 1\), increases with an increase in the submergence factor F5. Therefore, when the submergence of the diffusers increases, the horizontal velocity close to the bed also increases. In the case of submergence of diffusers, similar observations were made as for liquid depth in the tank. At the higher values of submergence, a better dissipation of energy through diffused air resulting in \(a\) better spiral flow and higher horizontal velocities, were observed. With low submergence, when the
diffusers were kept close to the surface of water, high superfacial turbulence without or with weak spiral motion, was observed. A stronger and well defined spiral flow always resulted in higher horizontal velocities. Higher submergence will also result in higher oxygen transfer to the liquid content of the aeration tank.

\subsection*{7.3.4 Sensitivity Analysis of the Model}

There are always some chances of getting experimental errors associated with the estimation of model parameters. Therefore, a senstivity analysis was conducted to evaluate the sensitivity of the model to these unforseen errors in the experimental and statistical parameters. If a small variation in an input parameter causes a large difference in the model output or the value of dependent variable, the model is said to be sensitive to that parameter. The exponents of the model were obtained through the statistical analysis and if a small change in one of these exponents causes large change in the overall performance of the model, then that exponent and its parameter are considered to be sensitive. The objective of sensitivity analysis is to know and to be careful about the parameters which will affect the model result significantly by small variations. It also helps to put more effort in the collection and analysis of parameters which are very sensitive.

The sensitivity analysis is divided into two parts. In the first part the sensitivity of the variation in the input
parameters or independent variables to the output variable or dependent variable are discussed. In the second part the sensitivity of small variation in the exponents of the input parameters on the performance of the model are discussed. The overall analysis helps in reinforcing the validity of the selected model for predicting horizontal point velocity, u, close to the tank bottom.

\subsection*{7.3.4.1 Variation in Input Parameters}

The effect of variation in the values of input parameters or independent variables of the model such as F2, F3, F4 and F5 on the output parameter or dependent variable, Fl, is studied and discussed below:
a. Power factor, F2: The power factor is the most important input parameter in the physical sense. However, this parameter is not very sensitive. It is found that by varying the value of F 2 by \(\pm .10 \%\), the change in the value of Fl is only \(\pm 3 \%\). Therefore, in the calculation of power factor, F2, a small error will not change the output parameter, Fl, of the model significantly.
b. Depth Factor, F4: The depth factor, F4, has been found to be most sensitive among all the input parameters. A \(\pm 10 \%\) variation in the value of \(F 4\) caused \(a \pm 6 \%\) change in the value of Fl. This change in the value of output parameter is quite significant. Therefore, no major error in the
measurement of depth of water can be allowed and this measurement should be done very carefully. Also in the design of the aeration tank, the depth of liquid in the tank should be given a serious consideration.
c. Width Factor, F3: The width factor, F3, has also been found to be equally sensitive as the depth factor, F 4 , in the model. A variation of \(\pm 10 \%\) in the value of \(F 3\), resulted in a change of \(\pm 6 \%\) in the value of output parameter Fl. Therefore, the width of the tank should also be measured very carefully. In the design of the aeration tank, the width should be selected carefully.
d. Submergence Factor, F5: The submergence factor, F5, has been found to be least sensitive among all the input parameters. However, in this factor, the depth of water, \(H\), in the tank is involved and it is a sensitive term. In the measurement of submergence, \(h\), some error can be allowed without affecting the value of output parameter, Fl, drastically. It is noticed that a variation of \(\pm 10 \%\) in the value of \(F 5\), caused a change of only \(\pm 1.3 \%\) in the value of \(F 1\).

\subsection*{7.3.4.2 Variation in Exponents of Different Factors}

The sensitivity of the model to the variations in exponent of each input parameter or independent variable is discussed below:
a. Exponent to Power Factor, F2: The exponent to the power factor, \(F 2\), determined by the statistical analysis is 0.310. When this exponent value of 0.310 is changed to 0.3116 , an increment of \(0.5 \%\), there is a corresponding change in the estimated value of Fl using model Eq. 6.2. The number of estimated values of Fl which show an error within \(\pm 20 \%\), when the exponent value is changed from 0.310 to 0.3116 , changes from 738 to 698 out of total 819 obserpations. This change from 738 to 698 is \(-5.4 \%\) of 738 . When the exponent value is varied \(\pm 3.5 \%\), all the estimated values of Fl showed an error of more than \(\pm 20 \%\), many exceeding to \(\pm 40 \%\). Therefore, this exponent is very sensitive and the rounding off of the value obtained through the statistical analysis should be done very carefully.

This analysis also confirms that the exponent value of 0.310 for parameter \(F 2\) is the best value for estimating Fl. In this case, 738 estimated values out of total 819 observations
showed an error within \(\pm 20 \%\) and this was the largest number obtained out of all the exponent values tried in the analysis.
b. Exponent to Width Factor, F3, and Depth Factor, F4: The exponent to the depth factor, F4 and to the width factor, F3, determined statistically, is \(2 / 3\) and \(-2 / 3\) respectively. Since the values of both the exponents are same except their signs, these two factors are grouped together and then analyzed for the sensitivity of the exponent. When this value of exponent is changed by \(0.5 \%\) to \(2.01 / 3\), the variation in the number of estimated values of Fl showing an error within \(\pm 20 \%\) dropped from 738 to 727 out ot total 819 observations. This value represented a change of \(1.5 \%\). When the exponent value is changed by \(\pm 5 \%\), almost all the estimated values show an error of more than \(\pm 20 \%\), most of them exceed \(\ddagger 40 \%\) error. Therefore, it can be concluded that the the model is sensitive to these exponents also, but to a lesser degree as compared to the exponent of power factor, F 2. This analysis also confirms that the exponent value for the ratio of depth factor to width factor, as determined by statistical analysis, is the best value for estimating Fl. In this
case, 738 estimated values show an error within \(\pm 20 \%\), and this was the largest number obtained out of all different exponent value tried in this analysis.
C. Exponent to Submergence Factor, F5: The exponent of the submergence factor, F5, determined by the statistical analysis is \(1 / 4\). When this value of exponent is changed by \(10 \%\) to \(1.1 / 4\), the variation in the number of estimated values showing an error within \(\pm 20 \%\) is only l\%. Even when the exponent value is changed by \(50 \%\) to 1.5/4, the variation in number of estimated values showing an error within \(\pm 20 \%\) is negligible. Therefore, the model is insensitive to this exponent and provides the best estimated values of Fl .

\section*{CONCLUSIONS}

This research has given a new dimension to the design of certain water and wastewater treatment units. At present, the suspension and shearing of particles in treatment units is controlled by maintaining certain lower and upper limits on velocities. It is proposed to use critical bed shear stress and yield stress for a more rational design.

The following conclusions are drawn on the basis of the results obtained in this study:

\subsection*{8.1 Experiments on Grit Particles}
a. The depth of fiow in a conventional grit chamber influences the mean velocity. Therefore; the influence of depth of flow while calculating the critical scouring velocity for grit particles of specific sizes should be taken into consideration.
b. The critical bed shear stress is a more rational parameter for designing a grit chamber as compared to critical mean velocity used as present design parameter.
c. A correlation between the grit particle sizes and corresponding critical bed shear stress values has been established.
d. For fully developed flow conditions and uniform size particles the critical bed shear stress values for a smooth bed are lower than a packed bed.

\section*{8. 2 Experiments on Sludge Particles}
a. Most of the sludges normally encountered in the field of water and wastewater engineering behaved as non-Newtonian fluids, as indicated below:
(a) Unsettled mixed liquor (biological sludge) behaved as Bingham plastic fluid
(b) Settled mixed liquor (biological sludge) behaved as pseudoplastic fluid with a yield stress
(c) Unsettled alum sludge behaved as Bingham plastic fluid
(d) Settled alum sludge behaved as pseudoplastic fluid with a yield stress
(e) Unsettled physico-chemical sludge behaved close to dilatant fluids
(f) Settled physico-chemical sludge behaved close to pseudoplastic fluid with a yield stress
(g) Secondary digested sludge (diluted) behaved as pseudoplastic with a yield stress
(h) Mixure of primary and secondary sludges behaved as pseudoplastic fluid with a yield stress
b. Rheological behaviour of sludges changed with the suspended solids concentration.
c. The yield stress values for different types of unsettled and settled sludges were determined. These are the limiting shear stress values beyond which the suspended particles start disintegrating in water and wastewater treatment units. .
d. A relationship between suspended solids concentration and corresponding yield stress value for different types of sludges has been established..
e. The critical bed shear stress values for different types of sludges were obtained. These are the minimum shear stress values required to prevent the settling of suspended particles.
f. It is recommended that various treatment units in water and wastewater field should be designed taking into consideration the critical bed shear stress and the yield stress values.

\subsection*{8.3 Experiments on Aeration Tank Model}
a. The important parameters, which affect the design and operation of an aeration tank, are identified. An empirical equation correlating these parameters which significantly affect the spiral motion (mixing) in the aeration tank has been developed. This equation predicts the horizontal velocities close to the tank bottom (25 mm above) under different operating conditions.
b. The physical evaluation of the developed equation revealed that:
(a)Increase in the power input in the system would provide higher velocities in the aeration tank.
(b) Increase in tank width would decrease the velocities.
(c)Increase in water depth would result in increased velocities, and
(d)Incrase in diffuser submergence would yield higher velocities.
c. The sensitivity analysis of the model revealed that the power factor was not a sensitive parameter, wherease the depth factor and width factor were found to be very sensitive. Submergence factor was found to be least
sensitive. Therefore, it is recommended to
select the values for all sensitive parameters
more carefully.

\section*{Chapter IX}

\section*{APPLICATION}

This chapter is divided into three major sections and under each section the practical application of the results obtained in this study is discussed.-

\subsection*{9.1 Grit and Gravel Particles}

The experiments conducted with grit and gravel particles in the laboratory flume have provided valuable data and rational design parameters. for grit chambers and sanitary sewers. This approach can also be used in the design of other units in which the accumulation of inert material is either desirable or undesirable.

\subsection*{9.1.1 Design of Grit Chambers Based on Critical Bed Shear Stres8}

The application of the proposed method for designing a grit chamber is recommended using the following steps:
a. Select the smallest particle size to be removed completely in the grit chamber.
b. Determine the critical bed shear stress, \(\tau_{c}\), for this particle size, using Figure 6.4 or Eq. 6.1.
c. Calculate the shear or friction velocity, \(U_{*_{C}}\), using Eq. 5.5.
d. Select the total depth of flow of wastewater to be maintained in the grit chamber.
e. Calculate the corresponding value of \(y\) using Eq. 5.12 or 5.17 , at which the point velocity will be a mean velocity.
f. Obtain the point velocity, \(u\), for the above \(y\) using Eqs. 5.6 or 5.7, depending on the flow regime. This point velocity will be the critical mean velocity, \(u_{m}\).
g. Design the grit chamber, using mean velocity, \(u_{m^{\prime}}\) depth of flow, and the given flow rate of wastewater.

\subsection*{9.2 Different Sludge Particles}

Using data gathered through experimental and theoretical analyses on different types of sludge particles, new methods of designing treatment units and mixing chambers in water and wastewaters treatment are proposed.

\subsection*{9.2.1 Design of Aeration Tank for Activated Sludge Process}

The current practice of designing aeration tank is based on maintaining a certain minimum dissolved oxygen, D.O., concentration. in the unit all the time. In this approach of design, the role of mixing and scouring velocities close to the tank floor are often ignored. The scouring velocity
in the aeration tank is necessary to keep the activated sludge flocs in suspension without shearing them. It is recommended that the aeration tank using diffused aeration should be designed to satisfy both the mixing and the D.O. requirements.

The application of the proposed method to design an aeration tank where the settling of flocs is undesirable, is illustrated with an example in the following steps:
a. Select the mixed liquor suspended solids, MLSS, concentration to be maintained in the reactor. b. Determine the yield stress, \(\tau_{y}\), value for biological sludge for the selected MLSS concentration using Equation given in Table 6.16. or using Figs. 6.33-6.37.
c. Determine the corresponding critical bed shear stress, \(\tau_{o c}\) for biological sludge from Table 6.3
d. The level of shear in the reactor should be kept between these two extreme stress values. Select an appropriate intermediate value of shear stress preferably closer to the yield stress, \({ }^{\tau}{ }^{\prime}\)
e. This will be the amount of shear needed close to the aeration tank floor to keep the sludge flocs in suspension without shearing them and this shear value can be used to determine the operating parameters.
f. Determine the horizontal velocity, 25 mm above the tank floor, needed to provide the above calculated bed shear by using Eg. 6.2.
9. Follow procedure in Section 8.3 to determine the operating parameters to provide the calculated horizontal velocity at 25 mm above tank floor.
h. These operating conditions may have to be modified to satisfy DO requirments.

\subsection*{9.2.2 Design of Flocculation Basins in Water and}

\section*{Wastewaters Treatment}

The flocculation basins are used both in water and wastewater treatment. In water treatment they are used, after rapid mixing of coagulant and coagulant aid, to make the alum flocs bigger and denser. In wastewater treatment, flocculation basins are used in physico chemical treatment. Chemicals are added for various purposes in the raw wastewater and these basins allow the formation of bigger and stronger flocs. The proposed design procedure is given below:
a. Select the type of particles to be flocculated in the basin.
b. Select the suspended solids concentration based on previous experience or given in the literature.
c. Determine the yield stress value, \(\tau y\), for the corresponding sludge and selected suspended solids concentration.
d. Determine the critical bed shear stress, \(\tau_{o c}{ }^{-1}\) for that type of sludge from Table 6.3.
e. Select the extent of shear needed in the basin somewhere between these two stress values. In flocculation basins the value of shear should be above the critical bed shear stress, ' oc' to prevent settling and below yield stress to prevent floc disintegration.
f. Design the basin volume, \(\forall\), to provide the desired detention time for floc formation.
g. Calculate the power input to provide mixing just enough to maintain above calculated shear in the basin.

The power needed for flocculation to generate needed velocity gradient in a rectangular chamber can be calculated as shown below:
\[
\begin{aligned}
& P=Q \gamma h_{f} \\
& \text { where } P=\text { Power input, } W \\
& Q=\text { Flow rate, } \mathrm{m}^{3} / \mathrm{s} \\
& \gamma=\text { Unit weight of liquid, } \mathrm{kg} / \mathrm{m}^{3} \\
& h_{f}=\text { Head loss in the chamber, } \mathrm{m}
\end{aligned}
\]

The bed shear is given by:
\[
\begin{align*}
\tau_{0}= & \gamma R s  \tag{8.2}\\
& \text { where } \tau_{0}=\text { Bed shear stress, } N / m^{2} \\
& R=\text { Hydraulic mean radius of the chamber, } m \\
& s=\text { Slope of chamber }
\end{align*}
\]

Dividing both sides of Eq. 8.1 by length of the chamber ' \(L_{1}\) '
\[
\begin{align*}
& \frac{\mathrm{P}}{\mathrm{~L}_{\mathrm{I}}}=\frac{\mathrm{Q} \gamma \mathrm{~h}_{\mathrm{f}}}{\overline{\mathrm{~L}}_{\mathrm{l}}} \\
& \frac{P}{L_{1}}=Q_{\gamma S} \\
& \text { or } \quad s=-\frac{P}{--}  \tag{8.4}\\
& ----[8.3] \\
& \text { or } \\
& Q \gamma L_{1} \\
& \text { Substituting the value of slope 's' in Eq. } 8.2 \\
& \tau_{o}^{2}=\frac{\gamma R P}{Q_{\gamma} \tau_{1}} \\
& P=\frac{\tau_{0}^{2} Q I_{1}}{R} \tag{8.5}
\end{align*}
\]

\subsection*{9.2.3 Design of Sedimentation Basins in Water and \\ Wastewaters Treatment}

The sedimentation basins or clarifiers are used in all water and wastewaters treatment plant. The design of sedimentation basin is normally done on the basis of overflow rate. However, if the settling characteristics of the particles are good, then the clarifiers can be
overloaded for higher overflow rate. The critical bed shear play a key role to determine the extent of overloading which can be accommodated in the clarifier, without washing away the settled sludge particles and hindering the settling process. The bed shear in the basin due to horizontal velocities close to the bed has to be below the critical bed shear for the particular sludge particles to be removed in the basin. The design procedure for sedimentation basins or clarifiers on the basis of critical bed shear to optimize the capacity is shown in the following steps.

\subsection*{9.3 Aeration Tank Model}

The aeration tank model, Eq. 6.2, can be applied to fix the operating conditions in units where diffused aeration is used as a mean for mixing purposes. This equation provides different options to have a certain predetermined horizontal velocity in the tank at 25 mm above the tank floor. The velocity requirements depend upon the purpose for which the unit is used. Diffused aeration tanks are commonly used in the activated sludge process for wastewater treatment; however, the use of these types of tanks are becoming popular in flocculation chambers, mixing chambers etc.. Aerated grit chamber is another application of diffused aeration in wastewater treatment.

The application of model Eq. 6.2 is described in the following steps:
a. Determine the physical properties of the liquid or suspension to be used in the aeration tank.
b. Fix the horizontal velocity at 25 mm above the tank floor using any of the approaches discussed in the previous sections, depending on the purpose of the unit.
c. Fix the dimensions of the aeration tank based on either detention time or mean cell residence time depending on the objective of the process.
d. Fix the location and submergence of the diffusers based on the convenience of maintenance.
e. Using the above values, calculate different dimensionless factors except power factor, F2.
f. Substitute the values of all calculated factors in Eq. 6.2 to obtain power factor, F2. This power factor value can be used to determine the air flow rate.
g. This air flow rate, as an operational parameter, will control the horizontal velocities in the tank.

If it is not possible to control the air flow rate, then the submergence of diffusers can be used as a operational parameter to control the velocities.

\section*{Appendix A CALIBRATION OF BROOKFIELD VISCOMETER}

The following tests were conducted on the Brookfield Viscometer in order to check its accuracy and performance.
a. Damaged or faulty pivot point or jewel bearing can affect the accuracy and repeatability of the viscometer. The Oscillation Test was performed on the viscometer to evaluate the conditions of pivot point and jewel bearing. This test revealed that they were in good condition.
b. The calibrated viscosity standards were used for final performance check. It was observed that the difference between the standard viscosity values and the observed viscosity values using the spindle \# 1 was within -l5\%. This difference between the standard value and observed values was due to temperature difference.
c. The calibrated viscosity standards were also used for checking the performance of the Rheomat 30 viscometer. The difference between the standard viscosity values and observed visocosity values were in the range of \(\pm 10 \%\).

The difference between the results obtained using the Brookfield Viscometer and Rheomat 30 was due to the wide shearing rate range used in the Rheomat 30 as compared to only four shearing rates used in the Brookfield Viscometer.
\begin{tabular}{c} 
APpendix \(B\) \\
DATA FROM BROOKFIELD VISCOMETER FOR DIFFERENT \\
TYPES OF SLUDGES \\
\hline
\end{tabular}

\section*{B. 1 Biological Sludges}

\section*{FIUID:}

SOURCE:
IOCATION: Little River Pollution Control Plant, Windsor, Ontario
\begin{tabular}{|c|c|c|c|c|c|}
\hline SET \# & \[
\begin{gathered}
\text { SPEFD OF } \\
\text { SPINDLE, } \mathrm{n} \\
\text { IPM }
\end{gathered}
\] & DIAL READING
D
PERCEMIAGE & \begin{tabular}{l}
RATE OF \\
SHEAR, dv/dr \(\sec ^{-1}\)
\end{tabular} & SHEAR STRESS, dynes \(/ \mathrm{cm}^{2}\) & AVERAGE SUSPENLED SOLIDS CONCENIRATION \(\mathrm{mg} / \mathrm{L}\) \\
\hline 1 & \[
\begin{array}{r}
60 \\
30 \\
12 \\
6
\end{array}
\] & \[
\begin{gathered}
0.0465 \\
0.0236 \\
0.011 \\
\text { negligible }
\end{gathered}
\] & \[
\begin{array}{r}
13.02 \\
6.51 \\
2.604
\end{array}
\] & \[
\begin{aligned}
& 0.7497 \\
& 0.3809 \\
& 0.1693
\end{aligned}
\] & 2,491 \\
\hline 2 & \[
\begin{array}{r}
60 \\
30 \\
12 \\
6
\end{array}
\] & \[
\begin{gathered}
0.0492 \\
0.0253 \\
0.0123 \\
\text { negligible }
\end{gathered}
\] & \[
\begin{gathered}
13.02 \\
6.51 \\
2.604
\end{gathered}
\] & \[
\begin{aligned}
& 0.7932 \\
& 0.4071 \\
& 0.1988
\end{aligned}
\] & 2,909 \\
\hline 3 & \[
\begin{array}{r}
60 \\
30 \\
12 \\
6
\end{array}
\] & \[
\begin{gathered}
0.0402 \\
0.0185 \\
0.009 \\
\text { negligible }
\end{gathered}
\] & \[
\begin{aligned}
& 13.02 \\
& 6.51 \\
& 2.604
\end{aligned}
\] & \[
\begin{aligned}
& 0.6481 \\
& 0.3031 \\
& 0.1370
\end{aligned}
\] & 2,387 \\
\hline
\end{tabular}

FLUID: Settled Biological Sludge
SOURCE: Aeration Tank
LOCATION: Little River Pollution Control Plant, Windsor, Ontario


FLUID: Mixed Liquor
SOURCE: Aeration Tank
LOCATION: Little River Pollution Control Plant, Windsor, Ontario


FLUID: Settled Biological Sludge
SOURCE: Aeration Tank
LOCATION: Little River Pollution Control Plant, Windsor, Ontario
\begin{tabular}{|c|c|c|c|c|c|}
\hline SEI \# & \[
\begin{gathered}
\text { SPEED OF } \\
\text { SPINDLE, } \mathrm{n} \\
\text { rpm }
\end{gathered}
\] & DIAL READING D PERCENTAGE & \begin{tabular}{l}
RATE OF \\
SHEAR, \(d v / d r\) \(\sec ^{-1}\)
\end{tabular} & SHEAR STRESS, dynes \(/ \mathrm{cm}^{2}\) & AVERAGE SUSPENIED SOLIDS CONCENIRATION \(\mathrm{mg} / \mathrm{L}\) \\
\hline 1 & \[
\begin{array}{r}
60 \\
30 \\
12 \\
6
\end{array}
\] & \[
\begin{aligned}
& 0.3413 \\
& 0.2050 \\
& 0.1338
\end{aligned}
\] & \[
\begin{gathered}
13.02 \\
6.51 \\
2.604 \\
1.302
\end{gathered}
\] & \[
\begin{aligned}
& 5.5032 \\
& 3.3052 \\
& 2.1565
\end{aligned}
\] & 8,531 \\
\hline 2 & \[
\begin{array}{r}
60 \\
30 \\
12 \\
6
\end{array}
\] & \[
\begin{aligned}
& 0.3650 \\
& 0.2318 \\
& 0.1475 \\
& 0.1050
\end{aligned}
\] & \[
\begin{gathered}
13.02 \\
6.51 \\
2.504 \\
1.302
\end{gathered}
\] & \[
\begin{aligned}
& 5.8848 \\
& 3.7365 \\
& 2.3781 \\
& 1.6929
\end{aligned}
\] & 8,538 \\
\hline
\end{tabular}
\begin{tabular}{ll} 
FLUID: & Mixed Liquor \\
SOURCE: & Aeration Tank \\
LOCATION: & Little River Pollution Control Plant, \\
& Windsor, Ontario
\end{tabular}
\begin{tabular}{|c|c|c|c|c|c|}
\hline SEI \# & \[
\begin{aligned}
& \text { SPEFD OF } \\
& \text { SPINDLE, } \mathrm{n} \\
& \text { rpm }
\end{aligned}
\] & DIAL READING D PERCENIAGE & RATE OF SHEAR, dv/dr \(\sec ^{-1}\) & SHEAR STRESS, dynes \(/ \mathrm{cm}^{2}\) & AVERAGE SUSPENLED SOLIDS CONCENIRATION \(\mathrm{mg} / \mathrm{L}\) \\
\hline 1 & \[
\begin{array}{r}
60 \\
30 \\
12 \\
6
\end{array}
\] & \[
\begin{gathered}
0.0480 \\
0.0296 \\
0.0145 \\
\text { negligible }
\end{gathered}
\] & \[
\begin{gathered}
13.02 \\
6.51 \\
2.604 \\
1.302
\end{gathered}
\] & \[
\begin{aligned}
& 0.7739 \\
& 0.4772 \\
& 0.2338
\end{aligned}
\] & 3,787 \\
\hline 2 & \[
\begin{array}{r}
60 \\
30 \\
12 \\
6
\end{array}
\] & \[
\begin{gathered}
0.0505 \\
0.0292 \\
0.0175 \\
\text { negligible }
\end{gathered}
\] & \[
\begin{gathered}
13.02 \\
6.51 \\
2.604 \\
1.302
\end{gathered}
\] & \[
\begin{aligned}
& 0.8142 \\
& 0.4708 \\
& 0.2822
\end{aligned}
\] & 3,851 \\
\hline
\end{tabular}
\(\begin{array}{ll}\text { FLUID: } & \text { Settled Biological Sludge } \\ \text { SOURGE: } & \text { Aeration Tank } \\ \text { IOCATION: } & \text { Little River Pollution Control Plant, } \\ & \text { Windsor, Ontario }\end{array}\)


\section*{B. 2 Alum Sludges}

FLUID: Alum Sludge
SOURCE: Underdrain of Settling Basin
IOCATION: Water Treatment Plant, Amherstburg, Ontario
\begin{tabular}{|c|c|c|c|c|c|}
\hline SET \# & \[
\begin{gathered}
\text { SPEED OF } \\
\text { SPINDLE, } \mathrm{n} \\
\text { rPm }
\end{gathered}
\] & \begin{tabular}{l}
DIAL READIMG \\
D \\
PERCENTAGE
\end{tabular} & \begin{tabular}{l}
RATE OF \\
SHEAR, \\
\(d v / d r\) \\
\(\mathrm{sec}^{-1}\)
\end{tabular} & SHEAR STRESS, dynes \(/ \mathrm{cm}^{2}\) & AVERAGE SUSPENLED SOLIDS CONCENTRATION \(\mathrm{mg} / \mathrm{L}\) \\
\hline 1 & \[
\begin{array}{r}
60 \\
30 \\
12 \\
6
\end{array}
\] & \[
\begin{aligned}
& 0.044 \\
& 0.0245 \\
& 0.0120 \\
& 0.0073
\end{aligned}
\] & \[
\begin{gathered}
13.02 \\
6.51 \\
2.604 \\
1.302
\end{gathered}
\] & \[
\begin{aligned}
& 0.7094 \\
& 0.3950 \\
& 0.1935 \\
& 0.1169
\end{aligned}
\] & 3,099 \\
\hline 2 & \[
\begin{array}{r}
60 \\
30 \\
12 \\
6
\end{array}
\] & \[
\begin{aligned}
& 0.0455 \\
& 0.0253 \\
& 0.0128 \\
& 0.0070
\end{aligned}
\] & \[
\begin{gathered}
13.02 \\
6.51 \\
2.604 \\
1.302
\end{gathered}
\] & \[
\begin{aligned}
& 0.7336 \\
& 0.4071 \\
& 0.2056 \\
& 0.1129
\end{aligned}
\] & 3,097 \\
\hline
\end{tabular}

FLUID: Settled Alum Sludge
SOURE: Underdrain of Settling Basin
LOCATION: Water Treatment Plant,
Amherstburg, Ontario
\begin{tabular}{|c|c|c|c|c|c|}
\hline SET \# & \[
\begin{gathered}
\text { SPEED OF } \\
\text { SPINDLE, } \mathrm{n} \\
\text { IPM }
\end{gathered}
\] & \[
\begin{gathered}
\text { DIAL READIMG } \\
\text { D } \\
\text { PERCENIAGE }
\end{gathered}
\] & RATE OF SHEAR, \(\mathrm{dv} / \mathrm{dr}\) \(\sec ^{-1}\) & SHEAR STRESS dynes \(/ \mathrm{cm}^{2}\) & AVERAGE SUSPENLED SOLIDS CONCENIRAITION \(\mathrm{mg} / \mathrm{L}\) \\
\hline 1 & \[
\begin{array}{r}
60 \\
30 \\
12 \\
6
\end{array}
\] & \[
\begin{aligned}
& 0.6438 \\
& 0.5113 \\
& 0.4175 \\
& 0.3350
\end{aligned}
\] & \[
\begin{gathered}
13.02 \\
6.51 \\
2.604 \\
1.302
\end{gathered}
\] & \[
\begin{array}{r}
10.3790 \\
8.2428 \\
5.7312 \\
5.4011
\end{array}
\] & 12,588 \\
\hline 2 & \[
\begin{array}{r}
60 \\
30 \\
12 \\
6
\end{array}
\] & \[
\begin{aligned}
& 0.6388 \\
& 0.5250 \\
& 0.4025 \\
& 0.3210
\end{aligned}
\] & \[
\begin{gathered}
13.02 \\
6.51 \\
2.604 \\
1.302
\end{gathered}
\] & \[
\begin{array}{r}
10.2984 \\
8.4644 \\
6.4894 \\
5.1754
\end{array}
\] & 13,362 \\
\hline
\end{tabular}

FLUID: Alum Sludge
SOUREE: Underdrain of Settling Tank
LOCATION: Water Treatment Plant, Amherstburg, Ontario
\begin{tabular}{|c|c|c|c|c|c|}
\hline SET \# & \[
\begin{gathered}
\text { SPEED OF } \\
\text { SPINDLE, } \mathrm{n} \\
\text { rpm }
\end{gathered}
\] & DIAL READING D PERCENTIAGE & RATE OF SHEAR, \(\mathrm{dv} / \mathrm{dr}\) \(\mathrm{sec}^{-1}\) & SHEAR STRESS, dynes/cm \({ }^{2}\) & AVERAGE SUSPENDED SOLIDS CONCENIRATION \(\mathrm{mg} / \mathrm{L}\) \\
\hline 1 & \[
\begin{array}{r}
60 \\
30 \\
12 \\
6
\end{array}
\] & \[
\begin{aligned}
& 0.0485 \\
& 0.0253 \\
& 0.0143 \\
& 0.0095
\end{aligned}
\] & \[
\begin{gathered}
13.02 \\
6.51 \\
2.604 \\
1.302
\end{gathered}
\] & \[
\begin{aligned}
& 0.7820 \\
& 0.4071 \\
& 0.2257 \\
& 0.1532
\end{aligned}
\] & 2,985 \\
\hline 2 & \[
\begin{array}{r}
60 \\
30 \\
12 \\
6
\end{array}
\] & \[
\begin{aligned}
& 0.0483 \\
& 0.0253 \\
& 0.012 \varepsilon \\
& 0.0095
\end{aligned}
\] & \[
\begin{gathered}
13.02 \\
6.51 \\
2.604 \\
1.302
\end{gathered}
\] & \[
\begin{aligned}
& 0.7779 \\
& 0.4071 \\
& 0.2056 \\
& 0.1532
\end{aligned}
\] & 3,128 \\
\hline
\end{tabular}

FLUID: Settled Alum Sludge
SOURCE: Underdrain of Settling Tank
LOCATION: Water Treatment Plant,
Amherstburg, Ontario
\begin{tabular}{|c|c|c|c|c|c|}
\hline SET \# & \[
\begin{aligned}
& \text { SPEED OF } \\
& \text { SPINDLE, } \mathrm{n} \\
& \text { IPM }
\end{aligned}
\] & DIAL READIMG D PERCENTAGE & \begin{tabular}{l}
RATE OF \\
SHEAR, \(\mathrm{dv} / \mathrm{dr}\) \(\mathrm{sec}^{-1}\)
\end{tabular} & \[
\begin{gathered}
\text { SHEAR STRESS, } \\
\tau \\
\text { dynes } / \mathrm{cm}^{2}
\end{gathered}
\] & AVERAGE SUSPENLED SOLIDS CONCENTRATION \(\mathrm{mg} / \mathrm{L}\) \\
\hline 1 & \[
\begin{array}{r}
60 \\
30 \\
12 \\
6
\end{array}
\] & \[
\begin{aligned}
& 0.5975 \\
& 0.4375 \\
& 0.3275 \\
& 0.2675
\end{aligned}
\] & \[
\begin{gathered}
13.02 \\
6.51 \\
2.604 \\
1.302
\end{gathered}
\] & \[
\begin{aligned}
& 9.6333 \\
& 7.0537 \\
& 5.2802 \\
& 4.3128
\end{aligned}
\] & 11,447 \\
\hline 2 & \[
\begin{array}{r}
60 \\
30 \\
12 \\
6
\end{array}
\] & \[
\begin{aligned}
& 0.5900 \\
& 0.4450 \\
& 0.3313 \\
& 0.2625
\end{aligned}
\] & \[
\begin{array}{r}
13.02 \\
6.51 \\
2.604 \\
1.302
\end{array}
\] & \[
\begin{aligned}
& 9.5124 \\
& 7.1746 \\
& 5.3407 \\
& 4.2322
\end{aligned}
\] & 11,613 \\
\hline
\end{tabular}

FLUID: Alum Sludge
SOURCE: Underdrain of Settling Tank
LOCATION: Water Treatment Plant,
Amherstburg, Ontario
\begin{tabular}{|c|c|c|c|c|c|}
\hline SET \# & \[
\begin{gathered}
\text { SPEED OF } \\
\text { SPINDLE, } \mathrm{n} \\
\mathrm{rpm}
\end{gathered}
\] & \[
\begin{gathered}
\text { DIAL READIMG } \\
\text { D } \\
\text { PERCENTAGE }
\end{gathered}
\] & RATE OF SHEAR, \(d v / d r\) \(\mathrm{sec}^{-1}\) & SHEAR STRESS, dynes \(/ \mathrm{cm}^{2}\) & AVERAGE SUSPENLED SOLIDS CONCENTRATION \(\mathrm{mg} / \mathrm{L}\) \\
\hline 1 & \[
\begin{array}{r}
60 \\
30 \\
12 \\
6
\end{array}
\] & \[
\begin{aligned}
& 0.0435 \\
& 0.0208 \\
& 0.0110 \\
& 0.0058
\end{aligned}
\] & \[
\begin{gathered}
13.02 \\
6.51 \\
2.604 \\
1.302
\end{gathered}
\] & \[
\begin{aligned}
& 0.7014 \\
& 0.3346 \\
& 0.1774 \\
& 0.0887
\end{aligned}
\] & 2,732 \\
\hline 2 & \[
\begin{array}{r}
60 \\
30 \\
12 \\
6
\end{array}
\] & \[
\begin{aligned}
& 0.0435 \\
& 0.0215 \\
& 0.0110 \\
& 0.0064
\end{aligned}
\] & \[
\begin{gathered}
13.02 \\
6.51 \\
2.504 \\
1.302
\end{gathered}
\] & \[
\begin{aligned}
& 0.7014 \\
& 0.3467 \\
& 0.1774 \\
& 0.1028
\end{aligned}
\] & 2,697 \\
\hline
\end{tabular}

FLUID: Settled Alum Sludge
SOLRCE: Underdrain of Settling Tank LOCATION: Water Treatment Plant, Amherstburg, Ontario
\begin{tabular}{|c|c|c|c|c|c|}
\hline SET \# & \[
\begin{gathered}
\text { SPEFD OF } \\
\text { SPINDLE, } \mathrm{n} \\
\text { rpm }
\end{gathered}
\] & DIAL READIMG D PERCENTAGE & RAIE OF SHEAR, \(d v / d r\) \(\sec ^{-1}\) & SHEAR STRESS, dynes \(/ \mathrm{cm}^{2}\) & AVERAGE SUSPENIED SOLIDS COICENIRAIIION \(\mathrm{mg} / \mathrm{L}\) \\
\hline 1 & \[
\begin{array}{r}
60 \\
30 \\
12 \\
6
\end{array}
\] & \[
\begin{aligned}
& 0.6078 \\
& 0.4628 \\
& 0.3488 \\
& 0.2875
\end{aligned}
\] & \[
\begin{gathered}
13.02 \\
6.51 \\
2.604 \\
1.302
\end{gathered}
\] & \[
\begin{aligned}
& 9.7986 \\
& 7.4608 \\
& 5.6228 \\
& 4.6353
\end{aligned}
\] & 11,573 \\
\hline 2 & \[
\begin{array}{r}
60 \\
30 \\
12 \\
6
\end{array}
\] & \[
\begin{aligned}
& 0.5788 \\
& 0.4563 \\
& 0.3575 \\
& 0.3140
\end{aligned}
\] & \[
\begin{gathered}
13.02 \\
6.51 \\
2.604 \\
1.302
\end{gathered}
\] & \[
\begin{aligned}
& 9.3310 \\
& 7.3560 \\
& 5.7639 \\
& 5.0625
\end{aligned}
\] & 11,493 \\
\hline
\end{tabular}

\section*{B. 3 PhysicomChemical Wastewater Sludges}

FLUID: Physico-Chemical Wastewater Sludge (Diluted)
SOURCE: Underdrain of Clarifier
LOCATION: West. Windsor Pollution Control Plant, Windsor, Ontario
\(\left.\begin{array}{|c|c|c|c|c|c|}\hline \text { SET \# } & \begin{array}{c}\text { SPEED OF } \\ \text { SPINDLE, } n \\ \text { LPM }\end{array} & \begin{array}{c}\text { DIAL READING } \\ \text { D } \\ \text { PERCENIAGE }\end{array} & \begin{array}{c}\text { RATE OF } \\ \text { SHEAR, } \\ \text { dv/dr } \\ \text { sec }^{-1}\end{array} & \begin{array}{c}\text { SHEAR STRESS, } \\ \tau \\ \text { dynes/cm }\end{array} & \begin{array}{c}\text { AVERAGE SUSPENDED } \\ \text { SOLIDS CONCENTRATION }\end{array} \\ \text { mg/L }\end{array}\right]\)

FLUID: Physico-Chemical Wastewater Sludge SOURCE: Underdrain of Clarifier
LOCATION: West Windsor Pollution Control Plant, Windsor, Ontario


FLUID: Physico-Chemical Mixed Liquor
SOURCE: Clarifier
LOCATION: West Windsor Pollution Control Plant, Windsor, Ontario
\begin{tabular}{|c|c|c|c|c|c|}
\hline SET \# &  & \[
\begin{gathered}
\text { DIAL READING } \\
\text { D } \\
\text { PERCENTAGE }
\end{gathered}
\] & RATE OF SHEAR, \(\mathrm{dv} / \mathrm{dr}\) \(\mathrm{sec}^{-1}\) & SHEAR STRESS, dynes/cm \({ }^{\tau}\) & AVERAGE SUSPENLED SOLIDS CONCENTRAIITON \(\mathrm{mg} / \mathrm{L}\) \\
\hline 1 & \[
\begin{array}{r}
60 \\
30 \\
12 \\
6
\end{array}
\] & \[
\begin{gathered}
0.0260 \\
0.0103 \\
0.0023 \\
\text { negligible }
\end{gathered}
\] & \[
\begin{gathered}
13.02 \\
6.51 \\
2.604 \\
1.302
\end{gathered}
\] & \[
\begin{aligned}
& 0.4192 \\
& 0.1652 \\
& 0.0363
\end{aligned}
\] & 675 \\
\hline 2 & \[
\begin{array}{r}
60 \\
30 \\
12 \\
6
\end{array}
\] & \[
\begin{gathered}
0.0280 \\
0.0105 \\
0.0025 \\
\text { negligible }
\end{gathered}
\] & \[
\begin{gathered}
13.02 \\
6.51 \\
2.604 \\
1.302
\end{gathered}
\] & \[
\begin{aligned}
& 0.4514 \\
& 0.1693 \\
& 0.0403
\end{aligned}
\] & 784 \\
\hline
\end{tabular}

FLUID: Physico-Chemical Settled Sludge
SOURCE: Clarifier
LOCATION: West Windsor Pollution Control Plant, Windsor, Ontario


FLUID: Physico-Chemical Mixed Liquor
SOLRCE: Clarifier
LOCATION: West Windsor Pollution Control Plant, Windsor, Ontario
\begin{tabular}{|c|c|c|c|c|c|}
\hline SET \# & \[
\begin{gathered}
\text { SPEED OF } \\
\text { SPINDLE, } \mathrm{n} \\
\text { rpm }
\end{gathered}
\] & \[
\begin{gathered}
\text { DIAL READIMG } \\
\text { D } \\
\text { PERCENTAGE }
\end{gathered}
\] & RATE OF SHEAR, \(\mathrm{dv} / \mathrm{dr}\) \(\mathrm{sec}^{-1}\) & SHEAR STRESS, dynes \(/ \mathrm{cm}^{2}\) & AVERAGE SUSPENLED SOLIDS CONCENTRATION \(\mathrm{mg} / \mathrm{L}\) \\
\hline 1 & \[
\begin{array}{r}
60 \\
30 \\
12 \\
6
\end{array}
\] & \[
\begin{aligned}
& 0.0358 \\
& 0.0155 \\
& 0.0045 \\
& 0.0020
\end{aligned}
\] & \[
\begin{gathered}
13.02 \\
6.51 \\
2.604 \\
1.302
\end{gathered}
\] & \[
\begin{aligned}
& 0.5764 \\
& 0.2499 \\
& 0.0726 \\
& 0.0322
\end{aligned}
\] & 5,255 \\
\hline 2 & \[
\begin{array}{r}
60 \\
30 \\
12 \\
6
\end{array}
\] & \[
\begin{aligned}
& 0.0365 \\
& 0.0160 \\
& 0.0050 \\
& 0.0023
\end{aligned}
\] & \[
\begin{gathered}
13.02 \\
6.51 \\
2.604 \\
1.302
\end{gathered}
\] & \[
\begin{aligned}
& 0.5885 \\
& 0.2580 \\
& 0.0806 \\
& 0.0363
\end{aligned}
\] & 5,897 \\
\hline
\end{tabular}

FLUID: Physico-Chemical Settled Sludge
SOURCE: Clarifier
LOCATION: West Windsor Pollution Control Plant, Windsor, Ontario
\begin{tabular}{|c|c|c|c|c|c|}
\hline SET \# & \[
\begin{gathered}
\text { SPEED OF } \\
\text { SPINDLE, } \mathrm{n} \\
\text { IPM }
\end{gathered}
\] & DIAL READIMG D PERCENTIAGE & RATE OF SHEAR, dv/dr \(\mathrm{sec}^{-1}\) & SHEAR STRESS, dynes \(/ \mathrm{cm}^{2}\) & AVERAGE SUSPENLED SOLIDS CONCENTRATION \(\mathrm{mg} / \mathrm{L}\) \\
\hline 1 & \[
\begin{array}{r}
60 \\
30 \\
12 \\
6
\end{array}
\] & \[
\begin{aligned}
& 0.2063 \\
& 0.1420 \\
& 0.0945 \\
& 0.0648
\end{aligned}
\] & \[
\begin{gathered}
13.02 \\
6.51 \\
2.604 \\
1.302
\end{gathered}
\] & \[
\begin{aligned}
& 3.3253 \\
& 2.2895 \\
& 1.5236 \\
& 1.0440
\end{aligned}
\] & 14,766 \\
\hline 2 & \[
\begin{array}{r}
60 \\
30 \\
12 \\
6
\end{array}
\] & \[
\begin{aligned}
& 0.1070 \\
& 0.0848 \\
& 0.0468 \\
& 0.0318
\end{aligned}
\] & \[
\begin{gathered}
13.02 \\
6.51 \\
2.604 \\
1.302
\end{gathered}
\] & \[
\begin{aligned}
& 1.7252 \\
& 1.3664 \\
& 0.7538 \\
& 0.5119
\end{aligned}
\] & 12,596 \\
\hline
\end{tabular}

\section*{B. 4 Secondary Digested Sludges}

FLUID: Secondary Digested Sludge (Diluted)
SOURCE: Underdrain
LOCATION: Wastewater Treatment Plant, Chatham, Ontario
\begin{tabular}{|c|c|c|c|c|c|}
\hline SET \# & \[
\begin{gathered}
\text { SPEFD OF } \\
\text { SPINDLEE, } \mathrm{n} \\
\text { rpm }
\end{gathered}
\] & DIAL READING D PERCENTAGE & \[
\begin{aligned}
& \text { RATE OF } \\
& \text { SHEAR, } \\
& \mathrm{dv} / \mathrm{dr} \\
& \mathrm{sec}^{-1}
\end{aligned}
\] & \[
\begin{gathered}
\text { SHEAR STRESS, } \\
\tau \\
\text { dynes } / \mathrm{cm}^{2}
\end{gathered}
\] & AVERAGE SUSPENDED SOLIDS CONCENITRATION \(\mathrm{mg} / \mathrm{L}\) \\
\hline 1 & \[
\begin{array}{r}
60 \\
30 \\
12 \\
6
\end{array}
\] & \[
\begin{aligned}
& 0.7150 \\
& 0.5850 \\
& 0.4350 \\
& 0.3800
\end{aligned}
\] & \[
\begin{array}{r}
13.02 \\
6.51 \\
2.604 \\
1.302
\end{array}
\] & \[
\begin{array}{r}
11.5277 \\
9.4318 \\
7.0286 \\
6.1266
\end{array}
\] & 24,537 \\
\hline 2 & \[
\begin{array}{r}
60 \\
30 \\
12 \\
6
\end{array}
\] & \[
\begin{aligned}
& 0.8288 \\
& 0.6925 \\
& 0.5125 \\
& 0.4438
\end{aligned}
\] & \[
\begin{gathered}
13.02 \\
6.51 \\
2.604 \\
1.302
\end{gathered}
\] & \[
\begin{array}{r}
13.3617 \\
11.1650 \\
8.2629 \\
7.1544
\end{array}
\] & 26,693 \\
\hline
\end{tabular}
(continued)

FLUID: Secondary Digested Sludge (Diluted) SOURCE: Underdrain
LOCATION: Wastewater Treatment Plant, Chatham, Ontario
\begin{tabular}{|c|c|c|c|c|c|}
\hline SEI \# & \[
\begin{gathered}
\text { SPEED OF } \\
\text { SPINDLE, } \mathrm{n} \\
\text { rpm }
\end{gathered}
\] & DIAL READIMG D PERCENTAGE & RATE OF SHEAR, \(\mathrm{dv} / \mathrm{dr}\) \(\mathrm{sec}^{-1}\) & \[
\begin{gathered}
\text { SHEAR STRESS, } \\
\tau \\
\text { dynes } / \mathrm{cm}^{2}
\end{gathered}
\] & AVERAGE SUSPENLED SOLIDS CONCENTRATION \(\mathrm{mg} / \mathrm{L}\) \\
\hline 3 & \[
\begin{array}{r}
60 \\
30 \\
12 \\
6
\end{array}
\] & \[
\begin{aligned}
& 0.3675 \\
& 0.2925 \\
& 0.1963 \\
& 0.1629
\end{aligned}
\] & \[
\begin{aligned}
& 13.02 \\
& 6.51 \\
& 2.604 \\
& 1.302
\end{aligned}
\] & \[
\begin{aligned}
& 5.9251 \\
& 4.7159 \\
& 3.1641 \\
& 2.6260
\end{aligned}
\] & 18,837 \\
\hline 4 & \[
\begin{array}{r}
60 \\
30 \\
12 \\
6
\end{array}
\] & \[
\begin{aligned}
& 0.5550 \\
& 0.4375 \\
& 0.3250 \\
& 0.2753
\end{aligned}
\] & \[
\begin{gathered}
13.02 \\
6.51 \\
2.604 \\
1.302
\end{gathered}
\] & \[
\begin{aligned}
& 8.9481 \\
& 7.0537 \\
& 5.2399 \\
& 4.4378
\end{aligned}
\] & 22,040 \\
\hline
\end{tabular}

\section*{B. 5 Mixture of Primary and Secondary Sludges}

FLUID: Mixture of Primary and Secondary Sludge SOLRCE: Underdrain to Primary Digester LOCATION: Wastewater Treatment Plant, Chatham, Ontario


\section*{Appendix C \\ VELOCITY PROFILES IN AERATION TANK•UNDER VARIOUS \\ OPERATING CONDITIONS}
```

Where Fl = Velocity Factor
F2 = Power Factor
F3 = Width Factor
F4 = Depth Factor
F5 = Submergence Factor
H = Depth of Liquid in the Tank
BH= Distance from Tank Bottom at which the Horizontal
Point Velocities were Measured
Ul= Horizontal Velocity at 2.5 mm Above the Tank Bottom
UBH=Horizontal Velocity at a Distance BH from the Tank
Bottom

```

\section*{C. 1 For Depth of 0.50 m}




\section*{UBH}

\section*{C. 2 For Depth of 0.65 m}





\section*{C. 3 For Depth of 0.80 m}






\section*{C. 4 For Depth of 0.95 m}







\section*{C. 5 For Depth of 1.10 m}



\section*{UBH}

UI





\begin{tabular}{c} 
APPendix.D \\
HORIZONTAI VELOCITIES AT 25 MM ABOVE THE \\
AERATION TANK BOTTOM \\
\hline
\end{tabular}

Where SUBMER = Depth of Water above the Diffusers, \(m\)
\[
\begin{aligned}
\mathrm{U}= & \text { Horizontal Velocity at } 25 \mathrm{~mm} \text { above Tank } \\
& \text { Bottom, } \mathrm{m} / \mathrm{s}
\end{aligned}
\]
\(\mathrm{H}=\) Depth of Water in the Tank, m
\(\mathrm{P}=\) Rate of Power Consumption (Useful) Using Submergence, Watts

X = Distance of Diffusers from the Right Sidewall of the tank, m
\(\mathrm{W}=\) Width of the Tank, m
\(L=\) Length of the Tank (along the diffusers), m
\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|c|c|c|c|}
\hline OBSV & \multicolumn{2}{|l|}{SUBMER} & \multicolumn{2}{|l|}{\(\boldsymbol{u}\)} & \multicolumn{2}{|l|}{H} & \multicolumn{2}{|l|}{\(\boldsymbol{p}\)} & \(\boldsymbol{x}\) & \multicolumn{2}{|l|}{W} & \multicolumn{2}{|l|}{\(L\)} \\
\hline 1 & 0.41605 & 00 & 0.1500 E & 00 & \(0.5000 E\) & 00 & \(0.2768 E\) & 02 & \(0.1100 E 00\) & \(0.2440 E\) & 01 & \(0.6900 E\) & 00 \\
\hline 2 & \(0.4160 E\) & 00 & 0.1300E & 00 & \(0.5000 E\) & 00 & \(0.2090 E\) & 02 & O.1100E 00 & 0.2440 E & 01 & \(0.6900 E\) & 00 \\
\hline 3 & 0.4160 E & 00 & \(0.1100 E\) & 00 & 0.5000E & 00 & 0.1561 E & 02 & \(0.1100 E 00\) & \(0.2440 E\) & 01 & 0.6900 E & 00 \\
\hline 4 & 0.4160 E & 00 & \multicolumn{2}{|l|}{0.7000E-01} & 0.5000E & 00 & 0.8050 E & 01 & \(0.1100 E 00\) & 0.2440 E & 01 & 0.6900E & 00 \\
\hline 5 & \(0.3550 E\) & 00 & \(0.1400 E\) & 00 & 0.5000 E & 00 & \(0.2364 E\) & 02 & \(0.4100 \mathrm{E}-01\) & \(0.2440 E\) & 01 & 0.6900E & 00 \\
\hline 6 & 0.355 OE & 00 & O.1200E & 00 & \(0.5000 E\) & 00 & 0.1783 E & 02 & \(0.4100 E-01\) & 0.2440 E & 01 & 0.6900E & 00 \\
\hline 7 & 0.3550E & 00 & \(0.1000 E\) & 00 & 0.5000 E & 00 & 0.1332E & 02 & \(0.4100 E-01\) & \(0.2440 E\) & 01 & 0.6900E & 00 \\
\hline 8 & 0.3550E & 00 & \multicolumn{2}{|l|}{\(0.6000 E-01\)} & 0.5000 E & 00 & 0.6878E & 01 & \(0.4100 \mathrm{E}-01\) & \(0.2440 E\) & 01 & 0.6900E & 00 \\
\hline 9 & 0.2280E & 00 & \(0.1300 E\) & 00 & 0.5000 E & 00 & 0.1518 E & 02 & \(0.1800 E-01\) & 0.2440 E & 01 & 0.6900E & 00 \\
\hline 10 & \(0.2280 E\) & 00 & \(0.1100 E\) & 00 & 0.5000E & 00 & \(0.1145 E\) & 02 & \[
0.1800 E-01
\] & 0.2440E & 01 & 0.6900E & 00 \\
\hline 11 & \(0.2280 E\) & 00 & \multicolumn{2}{|l|}{\(0.9000 \mathrm{E}-01\)} & \(0.5000 E\) & 00 & \(0.8553 E\) & 01 & \(0.1800 E-01\) & \(0.2440 E\) & 01 & 0.6900E & 00 \\
\hline 12 & 0.5660E & 00 & 0.2400E & 00 & \(0.6500 E\) & 00 & \(0.3765 E\) & 02 & O.1100E OO & \(0.2440 E\) & 01 & 0.6900E & 00 \\
\hline 13 & \(0.5660 E\) & 00 & 0.2100 E & 00 & 0.6500E & 00 & \(0.2843 E\) & 02 & \(0.1100 E 00\) & \(0.2440 E\) & 01 & 0.6900 E & 00 \\
\hline 14 & \(0.5660 E\) & 00 & \(0.1800 E\) & 00 & 0.6500E & 00 & \(0.2124 E\) & 02 & O.1100E 00 & 0.2440E & 01 & 0.6900E & 00 \\
\hline 15 & \(0.5660 E\) & 00 & 0.1400E & 00 & 0.6500E & 00 & \(0.1097 E\) & 02 & \(0.1100 E 00\) & 0.2440E & 01 & 0.6900E & 00 \\
\hline 16 & \(0.5050 E\) & 00 & 0.2200 E & 00 & 0.6500 E & 00 & 0.3361 E & 02 & \(0.4100 \mathrm{E}-01\) & 0.2440 E & 01 & 0.6900 E & 00 \\
\hline 17 & 0.5050 E & 00 & 0.2000 E & 00 & 0.6500E & 00 & 0.2536 E & 02 & \(0.4100 \mathrm{E}-01\) & 0.2440 E & 01 & \(0.6900 E\) & 00 \\
\hline 18 & 0.5050 E & . 00 & 0.1700E & 00 & 0.6500 E & 00 & \(0.1896 E\) & 02 & \(0.4100 E-01\) & 0.2440 E & 01 & 0.6900E & 00 \\
\hline 19 & 0.5050 E & 00 & 0.1300E & 00 & \(0.6500 E\) & 00 & 0.9780 E & 01 & \(0.4100 \mathrm{E}-01\) & 0.2440 E & 01 & \(0.6900 E\) & 00 \\
\hline 20 & 0.3780 E & 00 & 0.1800 E & 00 & 0.6500 E & 00 & \(0.2517 E\) & 02 & \(0.1800 E-01\) & 0.2440 E & 01 & 0.6900 E & 00 \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|}
\hline 앙 & 8 & 앙 & 앙 & 8 & 용 & \(\bigcirc\) & 8 & 앙 & 잉 & \(\bigcirc\) & \(\bigcirc\) & 8 & \(\bigcirc\) & － & 앙 & 8 & 8 & 8 & ㅇ \\
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\(\begin{array}{ll}\infty & 0 \\ 0 & 0\end{array}\) \(\therefore \sim N\)
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\hline & 8 & 8 & 8 &  & 8 & 앙 & 8 & － & \(\bigcirc\) & 8 & \(\bigcirc\) & 잉 & 앙 & 8 & 앙 & 앙 & 8 &  & 앙 &  \\
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\hline \(\bigcirc\) & \(\bigcirc\) & \(\bigcirc\) & \(\bigcirc\) & 0 & \(\bigcirc\) & 0 & 0 \\
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\hline & 앙 & 8 & 8 & 8 & 8 & 앙 & \(\bigcirc\) & 8 & 8 & ： & 8 & 8 & 8 & 잉 & 8 & 8 & 8 & 8 & 8 & － \\
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\hline absv & V SUBMER & \(u\) & H & & \(p\) & & \(x\) & \(w\) & & 4 \\
\hline 221 & 0.6940E 00 & 0.3200 E 00 & O.1100E & 01 & \(0.3244 E\) & 02 & \(0.2500 E-01\) & 0.2210 E & 01 & 0.6900E 00 \\
\hline 222 & 0.6940E 00 & 0.2900 O & 0.1100E & 01 & \(0.2433 E\) & 02 & 0.2500E-01 & 0.2210E & 01 & 0.6900 E 0 \\
\hline 223 & 0.6940E 00 & 0.2200E 00 & 0.1100 E & 01 & \(0.1262 E 0\) & 02 & 0.2500E-01 & O.2210E & 01 & 0.6900E 00 \\
\hline 224 & 0.6940E 00 & 0.2000E 00 & D.1100E 0 & 01 & 0.9010E O & 01 & 0.2500E-01 & 0.2210 E & 01 & 0.6900 E 00 \\
\hline 225 & 0.6170E 00 & 0.3200E 00 & 0.1100 E & 01 & 0.3820 E & 02 & 0.2500E-01 & 0.2210 E & 01 & 0.6900E 00 \\
\hline 226 & 0.6170E 00 & 0.3000E 00 & 0.1100 E & 01 & \(0.2905 E\) & 02 & 0.2500E-01 & 0.2210E & 01 & 0.6900E 00 \\
\hline 227 & 0.617,0E 00 & 0.2800E 00 & 0.1100 E & 01 & 0.2179E 0 & 02 & 0.2500E-01 & 0.2210E & 01 & 0.6900E 00 \\
\hline 228 & 0.6170 O 0 & 0.2100E 00 & 0.1100 E & 01 & 0.1130E 0 & 02 & 0.2500E-01 & 0.2210E & 01 & 0.6900E 00 \\
\hline 229 & 0.6170 E 0 & 0.1900E 00 & 0.1100E & 01 & 0.8070E & 01 & 0.2500E-01 & 0.2210E & 01 & 0.6900E 00 \\
\hline 230 & 0.5410 O 0 & 0.3000E 00 & 0.1100E & 01 & 0.3372 E & 02 & 0.2500E-01 & 0.2210E & 01 & 0.6900 EO \\
\hline 231 & 0.5410E 00 & 0.2800E 00 & 0.1100 E & 01 & 0.2565E & 02 & 0.2500E-O1 & 0.2210E & 01 & 0.6900E 00 \\
\hline 232 & 0.5410 EO & 0.2600E 00 & 0.1100E & 01 & \(0.1924 E 0\) & 02 & 0.2500E-01 & 0.2210E & 01 & 0.6900E 00 \\
\hline 233 & 0.5410 EO & 0.2000E 00 & 0.1100E & 01 & 0.9970E & 01 & \(0.2500 \mathrm{E}-01\) & 0.2210E & 01 & 0.6900E 00 \\
\hline 234 & 0.5410 E 00 & 0.1800E 00 & 0.1100 E & 0.1 & 0.7120E & 01 & \(0.2500 \mathrm{E}-01\) & 0.2210 E & 01 & 0.6900E 00 \\
\hline 235 & 0.4160E 00 & 0.1800E 00 & O.5000E & 00 & 0.2623 E & 02 & 0.1100E 00 & 0.1980E & 01 & 0.6900E 00 \\
\hline 236 & 0.4160E 00 & 0.1600E 00 & 0.5000E & 00 & \(0.1995 E\) & 02 & 0.1100 EO & O-1980E & 01 & 0.6900E 00 \\
\hline 237 & 0.4160E 00 & 0.1400E 00 & 0.5000E & 00 & 0.1496E & 02 & 0.1100E 00 & 0.1980E & 01 & 0.6900E 00 \\
\hline 238 & 0.4160E 00 & 0.8500E-0 1 & 0.5000E & 00 & 0.7760E & 01 & 0.1100 O & 0.1980E & 01 & 0.6900E 00 \\
\hline 239 & 0.3550E 00 & 0.1750E 00 & 0.5000 E & 00 & 0.2251E & 02 & 0.4100E-01 & 0.1980E & 01 & 0.6900E 00 \\
\hline 240 & 0.3550 E 00 & 0.1500E 00 & 0.5000E & 00 & 0.1712E & 02 & 0.4100E-01 & 0.1980 E & 01 & 0.6900E DO \\
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\(0.4100 \mathrm{E}-01\)
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\(\overrightarrow{0}\) & \(\overrightarrow{0}\) & \(\overrightarrow{0}\) & \(\overrightarrow{0}\) \\
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\hline 322 & 0.9550E & 00 & 0.4500 E & 00 & 0.1100 E & 01 & 0.5733 E & 02 & 0.4100E-01 & 0.1980E & 01 & 0.6900E & 00 \\
\hline 323 & 0.9550E & 00 & 0.4200 E & 00 & 0.1100E & 01 & 0.4361 E & 02 & \(0.4100 \mathrm{E}-01\) & 0.1980E & 01 & 0.6900E & 00 \\
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\hline 325 & 0.9550 E & 00 & 0.3200 E & 00 & 0.1100 E & 01 & 0.1696E & 02 & \(0.4100 \mathrm{E}-01\) & 0.1980E & 01 & 0.6900E & 00 \\
\hline 326 & \(0.9550 E\) & 00 & 0.3000E & 00 & 0.1100 E & 01 & \(0.1211 E\) & 02 & \(0.4100 \mathrm{E}-01\) & 0.1980 E & 01 & 0.6900E & 00 \\
\hline 327 & 0.8280E & 00 & 0.4200 E & 00 & 0.1100 E & 01 & 0.5028 E & 02 & \(0.2000 \mathrm{E}-01\) & 0.1980E & 01 & 0.6900E & 00 \\
\hline 328 & \(0.8280 E\) & 00 & 0.4000 E & 00 & 0.1100 E & 01 & 0.3824 E & 02 & \(0.2000 E-01\) & 0.1980 E & 01 & 0.6900E & 00 \\
\hline 329 & 0.8280 E & 00 & 0.3700 E & 00 & 0.1100E & 01 & 0.2868 E & 02 & \(0.2000 \mathrm{E}-01\) & 0.1980 E & 01 & 0.6900 E & 00 \\
\hline 330 & 0.8280E & 00 & 0.3000 E & 00 & 0.1100E & 01 & \(0.1487 E\) & 02 & \(0.2000 \mathrm{E}-01\) & 0.1980E & 01 & 0.6900E & 00 \\
\hline 331 & 0.8280 E & 00 & 0.2800E & 00 & 0.1100 E & 01 & 0.1062E & 02 & \(0.2000 \mathrm{E}-01\) & 0.1980E & 01 & 0.6900E & 00 \\
\hline 332 & 0.7950 E & 00 & 0.4100 E & 00 & 0.1100E & 01 & 0.4842 E & 02 & 0.2500E-01 & 0.1980E & 01 & 0.6900E & 00 \\
\hline 333 & 0.7950E & 00 & 0.3900 E & 00 & 0.1100E & 01 & 0.3683 E & 02 & 0.2500E-01 & \(0.1980 E\) & 01 & 0.6900E & 00 \\
\hline 334 & 0.7950E & 00 & 0.3600E & 00 & 0.1100E & 01 & 0.2762 E & 02 & \(0.2500 \mathrm{E}-01\) & 0.1980 E & 01 & 0.6900E & 00 \\
\hline 335 & 0.7950E & 00 & 0.2900 E & 00 & 0.1100E & 01 & 0.1432 E & 02 & 0.2500E-01 & 0.1980E & 01 & 0.6900E & 00 \\
\hline 336 & 0.7950E & 00 & 0.2700E & 00 & 0.1100E & 01 & 0.1023E & 02 & 0.250 OE-01 & 0.1980E & 01 & 0.6900E & 00 \\
\hline 337 & 0.6940E & 00 & 0.3900 E & 00 & 0.1100E & 01 & 0.4266E & 02 & 0.2500E-01 & 0.1980 E & 01 & 0.6900E & 00 \\
\hline 338 & 0.6940E & 00 & 0.3600E & 00 & 0.1100 E & 01 & 0.3244 E & 02 & 0.2500E-01 & 0.1980 E & 01 & 0.6900E & 00 \\
\hline 339 & 0.6940E & 00 & 0.3300 E & 00 & 0.1100 E & 01 & 0.2433 E & 02 & \(0.2500 \mathrm{E}-01\) & 0.1980E & 01 & 0.6900E & 00 \\
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\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|c|c|c|}
\hline OBS & SUBMER & \(u\) & & H & & P & & \(x\) & W & & \(L\) & \\
\hline 441 & 0.9550 E 00 & 0.4100 E & 00 & 0.1100E & 01 & \(0.3270 E\) & 02 & 0.4100E-01 & 0.1750E & 01 & 0.6900 E & 00 \\
\hline 442 & \(0.9550 E 00\) & 0.3400 E & 00 & 0.1100E & 01 & 0.1696 E & 02 & 0.4100E-01 & 0.1750E & 01 & 0.6900 E & 00 \\
\hline 443 & 0.9550E 00 & 0.3200E & 00 & 0.1100E & 01 & 0.1211E & 02 & 0.4100E-01 & 0.1750E & 01 & 0.6900 E & 00 \\
\hline 444 & 0.8280E 00 & 0.4300E & 00 & 0.1100E & 01 & 0.5028E & 02 & 0.2000E-01 & 0.1750E & 01 & 0.6900 E & 00 \\
\hline 445 & 0.8280 E 00 & 0.4100 E & 00 & 0.1100E & 01 & 0.3824 E & 02 & \(0.2000 \mathrm{E}-01\) & 0.1750E & 01 & 0.6900E & 00 \\
\hline 446 & O.8280E 00 & 0.3800E & 00 & 0.1100E & 01 & 0.2868 E & 02 & \(0.2000 E-01\) & 0.1750 E & 01 & 0.6900E & 00 \\
\hline 447 & 0.8280 E 00 & 0.3200 E & 00 & 0.1100E & 01 & 0.1487E & 02 & \(0.2000 \mathrm{E}-01\) & 0.1750 E & 01 & 0.6900 E & 00 \\
\hline 448 & 0.8280E 00 & 0.3000 E & 00 & 0.1100E & 01 & 0.1062 E & 02 & \(0.2000 \mathrm{E}-01\) & 0.1750 E & 01 & 0.6900E & 00 \\
\hline 449 & 0.7950E 00 & 0.4200 E & 00 & 0.1100 E & 01 & 0.4842 E & 02 & \(0.2500 \mathrm{E}-01\) & 0.1750 E & 01 & 0.6900E & 00 \\
\hline 450 & 0.7950E 00 & 0.4000 E & 00 & 0.1100 E & 01 & 0.3683 E & 02 & 0.2500E-01 & 0.1750E & 01 & 0.6900 E & 00 \\
\hline 451 & 0.7950E 00 & 0.3700 E & 00 & 0.1100E & 01 & 0.2762E & 02 & \(0.2500 \mathrm{E}-01\) & 0.1750 E & 01 & 0.6900 E & 00 \\
\hline 452 & 0.7950E 00 & 0.3000 E & 00 & 0.1100E & 01 & 0.1432 E & 02 & \(0.2500 \mathrm{E}-01\) & 0.1750 E & 01 & 0.6900E & 00 \\
\hline 453 & 0.7950E 00 & 0.2800E & 00 & 0.1100E & 01 & 0.1023 E & 02 & 0.2500E-01 & 0.1750 E & 01 & 0.6900 E & 00 \\
\hline 454 & 0.6940 E 00 & 0.4000 E & 00 & 0.1100E & 01 & \(0.4266 E\) & 02 & \(0.2500 \mathrm{E}-01\) & 0.1750 E & 01 & 0.6900 E & 00 \\
\hline 455 & 0.6940E 00 & 0.3800 E & 00 & \(0.1100 E\) & 01 & 0.3244 E & 02 & \(0.2500 \mathrm{E}-01\) & 0.1750E & 01 & 0.6900E & 00 \\
\hline 456 & 0.6940E 00 & 0.3500 E & 00 & 0.1100 E & 01 & 0.2433 E & 02 & \(0.2500 \mathrm{E}-01\) & 0.1750E & 01 & 0.6900E & 00 \\
\hline 457 & 0.6940 E 00 & 0.2800 E & 00 & 0.1100E & 01 & 0.1262E & 02 & \(0.2500 \mathrm{E}-01\) & 0.1750E & 01 & 0.6900 E & 00 \\
\hline 458 & 0.6940E 00 & 0.2600 E & 00 & 0.1100E & 01 & 0.9010 E & 01 & \(0.2500 \mathrm{E}-01\) & 0.1750 E & 01 & 0.6900 E & 00 \\
\hline 459 & 0.6170 O 0 & 0.3800 E & 00 & 0.1100E & 01 & 0.3820 E & & \(0.2500 \mathrm{E}-01\) & 0.1750E & 01 & 0.6900 E & 00 \\
\hline 460 & 0.6170E 00 & 0.3600 E & 00 & 0.1100E & 01 & 0.2905 E & 02 & \(0.2500 \mathrm{E}-01\) & 0.1750E & 01 & \(0.6900 E\) & 00 \\
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\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|}
\hline & 0 & 8 & 8 & \％ & 앙 &  & 8 & 용 & 잉 &  & 앙 & 0 & 앙 & O & 앙 &  & 8 & 앙 & 8 & \％ \\
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\hline & 0 & \(\stackrel{7}{0}\) & 0 & \(\stackrel{\rightharpoonup}{0}\) & \(\stackrel{-}{0}\) & \(\stackrel{\square}{0}\) & \(\overrightarrow{0}\) & － & 0 & \(\stackrel{7}{0}\) & \(\bigcirc\) & \(\overrightarrow{0}\) & O & \(\overrightarrow{0}\) & 0 & 0 & 0 & 0 & 0 & 0 \\
\hline \(\geqslant\) & \[
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& \stackrel{\rightharpoonup}{\bullet} \\
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& \vdots \\
& 0
\end{aligned}
\] & \[
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& \alpha \\
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\hline & \(\overrightarrow{0}\) & \(\cdots\) & \(\stackrel{\square}{0}\) & \(\stackrel{\rightharpoonup}{0}\) & \(\square\) & \(\stackrel{\square}{0}\) & \(\stackrel{\square}{0}\) & \(\stackrel{\sim}{0}\) & \(\bigcirc\) & \(\bigcirc\) & 앙 & \％ & ㅇ & \(\bigcirc\) & \(\bigcirc\) & \(\bigcirc\) & \(\bigcirc\) & \(\bigcirc\) & 앙 & \(\bigcirc\) \\
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\hline & \(\bigcirc\) & 8 & \[
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\hline & \(\bigcirc\) & 8 & 용 & 8 & 8 & 잉 & 앙 & 8 & 용 & \(\bigcirc\) & 8 & \(\bigcirc\) & 8 & 응 &  & 잉 & 8 & 앙 & － & 앙 \\
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\hline 3 & \[
\] & W
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\hline & N & \(\stackrel{\sim}{\circ}\) & N & N & \(\stackrel{\rightharpoonup}{0}\) & N & N & N & \(\underset{O}{0}\) & \(\overrightarrow{0}\) & N & N & N0 & \(\overrightarrow{0}\) & － & N & N & N & \(\square\) & 0 \\
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\hline & ㅇ & 8 & 8 & 8 & \(\bigcirc\) & 8 & 8 & 앙 & 8 & 8 & \(\bigcirc\) & 8 & 8 & \(\bigcirc\) & 앙 & 앙 & 앙 & 앙 & 8 & \％ \\
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\hline & N & \(\stackrel{\sim}{0}\) & N & N & N & \(\stackrel{N}{0}\) & N & N & \(\stackrel{N}{0}\) & N & N & N & N1 & N & 0 & N & N & N & N & \(\underline{0}\) \\
\hline Q & \begin{tabular}{l}
\(\stackrel{H}{4}\) \\
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\end{tabular} & \[
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& N \\
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& \stackrel{0}{+} \\
& 0 \\
& 0
\end{aligned}
\] & \[
\begin{aligned}
& \text { u } \\
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\end{aligned}
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\(\ddot{7}\)
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\hline & \(\bigcirc\) & \(\bigcirc\) & \(\bigcirc\) & \[
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\therefore
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\therefore
\] & O & \(\bigcirc\) & 8 & \(\bigcirc\) & \％ & 8 \\
\hline Su & \(w_{0}\)
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\begin{aligned}
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\end{aligned}
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\begin{aligned}
& \omega \\
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\begin{aligned}
& \text { u } \\
& 0 \\
& \stackrel{1}{6} \\
& 0 \\
& 0 \\
& 0
\end{aligned}
\] & \[
\begin{aligned}
& \stackrel{\mu}{0} \\
& \stackrel{0}{6} \\
& \vdots \\
& 0
\end{aligned}
\] & \[
\begin{aligned}
& \text { u1 } \\
& \stackrel{\text { n }}{6} \\
& 0 \\
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\end{aligned}
\] & \[
\begin{aligned}
& \text { u } \\
& 0 \\
& \stackrel{0}{6} \\
& \vdots \\
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& \text { u } \\
& \stackrel{0}{0} \\
& \text { \& } \\
& 0 \\
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\end{aligned}
\] & \[
\begin{aligned}
& \text { u } \\
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& i n \\
& \stackrel{0}{+} \\
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\end{aligned}
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& \text { 山 } \\
& \stackrel{0}{0} \\
& \stackrel{+}{0} \\
& 0 \\
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\end{aligned}
\] & \[
\begin{aligned}
& \text { 山 } \\
& \text { of } \\
& \dot{+} \\
& 0 \\
& \vdots
\end{aligned}
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\(\vdots\)
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\hline \[
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\underset{\mathbf{b}}{\overrightarrow{5}}
\] & \[
\begin{gathered}
\underset{\sim}{N} \\
\underset{\delta}{2}
\end{gathered}
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\begin{gathered}
\underset{+}{\mathbf{O}}
\end{gathered}
\] & \[
\stackrel{+}{\Phi}
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& \text { ח } \\
& \underset{\sim}{2}
\end{aligned}
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\underset{\substack{\text { H}}}{( }
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\begin{gathered}
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\begin{aligned}
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& \underset{0}{9}
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\] & 8 \\
\hline
\end{tabular}

\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|}
\hline & 8 & 8 & 8 & \(\bigcirc\) & 앙 & 8 & 8 & 용 & 잉 & \(\bigcirc\) & 앙 & 8 & 앙 &  & 앙 & 8 & 앙 & 앙 & 8 & \％ \\
\hline \(\downarrow\) & \[
\begin{aligned}
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& \text { w } \\
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\begin{aligned}
& \mu \\
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\begin{aligned}
& \text { 山⿱丷⿱口口㇒⿸⿻一丿又寸 } \\
& 0 \\
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\end{aligned}
\] & \[
\begin{aligned}
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\begin{aligned}
& \text { u } \\
& \stackrel{\circ}{\circ} \\
& 0 \\
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& \text { 山 } \\
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& \text { 山 } \\
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\hline & － & \(\overrightarrow{0}\) & \(\stackrel{\square}{0}\) & \(\bigcirc\) & \(\bigcirc\) & 0 & 0 & 0 & 0 & 0 & 0 & 0 & \(\bigcirc\) & 0 & \(\bigcirc\) & \(\bigcirc\) & \(\bigcirc\) & 0 & \(\overrightarrow{0}\) & \(\stackrel{\rightharpoonup}{0}\) \\
\hline 3 & \[
\begin{gathered}
0 \\
\stackrel{0}{N} \\
\underset{\sim}{:} \\
0
\end{gathered}
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\begin{gathered}
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\text { a } \\
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\end{gathered}
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\stackrel{\sim}{\stackrel{1}{*}}
\] & \[
\stackrel{\sim}{\stackrel{N}{0}}
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& \text { 山̈ } \\
& 0 \\
& \stackrel{N}{N} \\
& \stackrel{0}{0}
\end{aligned}
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\stackrel{\text { à }}{\underset{\sim}{\circ}}
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\stackrel{\text { N }}{\stackrel{1}{\sim}}
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\end{gathered}
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& \stackrel{\circ}{0}
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\stackrel{0}{N}
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& \underset{\sim}{N} \\
& \underset{0}{0}
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& \text { ü } \\
& \stackrel{1}{N} \\
& \stackrel{\rightharpoonup}{0} \\
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\begin{aligned}
& \text { 山̈ } \\
& \stackrel{1}{N} \\
& \stackrel{1}{0}
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\begin{aligned}
& \text { ü } \\
& \text { N } \\
& \underset{\sim}{0} \\
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\] & \[
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& \text { 山̈ } \\
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& \stackrel{\mu}{0} \\
& \stackrel{1}{~} \\
& \stackrel{\circ}{0}
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0 & \(0.2500 \mathrm{E}-01\) &  & \(0.2500 \mathrm{E}-01\) & \(\overrightarrow{0}\)
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\end{tabular}

\begin{tabular}{|c|c|c|c|c|c|c|c|c|}
\hline OBSV & SUBMER & \(u\) & H & \(p\) & \(x\) & \(w\) & & \(L\) \\
\hline 721 & 0.5050 E 0 & 0.2900E 00 & 0.6500E 00 & 0.9340E 01 & \(0.4100 \mathrm{E}-01\) & \(0.1060 E\) & 01 & 0.6900E 00 \\
\hline 722 & 0.3780E 00 & 0.360 OE 00 & 0.6500E 00 & \(0.2392 E 02\) & \(0.1800 E-01\) & 0.1060 E & 01 & 0.6900 E 0 \\
\hline 723 & 0.3780E 00 & 0.3200 E 0 & \(0.6500 E 00\) & 0.1819E 02 & 0.1800E-01 & 0.1060 E & 01 & 0.6900E OO \\
\hline 724 & 0.3780E 00 & 0.2900 E 0 & 0.6500 E 0 & \(0.1365 E 02\) & 0.1800E-01 & \(0.1060 E\) & 01 & 0.6900E 00 \\
\hline 725 & 0.3780E 00 & 0.2400E 00 & 0.6500E 00 & 0.7080E 01 & 0.1800E-01 & 0.1060E & 01 & 0.6900E 00 \\
\hline 726 & 0.3450E 00 & 0.3400 E 0 & 0.6500E 00 & 0.2190 E 02 & \(0.2000 \mathrm{E}-01\) & 0.1060 E & 01 & 0.6900 E 00 \\
\hline 727 & 0.3450E 00 & 0.3050 E 0 & 0.6500E 00 & 0.1666E 02 & \(0.2000 \mathrm{E}-01\) & 0.1060 E & 01 & 0.6900 E 00 \\
\hline 728 & 0.3450E 00 & 0.2700 E 0 & 0.6500 E 00 & 0.1249E 02 & \(0.2000 \mathrm{E}-01\) & 0.1060 E & 01 & 0.6900E 00 \\
\hline 729 & 0.3450E 00 & 0.2200E 00 & 0.6500 E 00 & 0.6480E 01 & 0.2000E-01 & 0.1060E & 01 & 0.6900 EO \\
\hline 730 & 0.7160E 00 & 0.5200E 00 & 0.8000E 00 & 0.4392 E 02 & 0.1100E 00 & 0.1060 E & 01 & 0.6900E 00 \\
\hline 731 & 0.7160E 00 & 0.4800 O 0 & 0.8000E 00 & 0.3340 E 02 & 0.1100E 00 & 0.1060E & 01 & 0.6900E 00 \\
\hline 732 & 0.7160 E 00 & 0.4400 E 00 & 0.8000 EO & \(0.2505 E 02\) & 0.1100E 00 & 0.1060E & 01 & 0.6900E 00 \\
\hline 733 & 0.7160E 00 & \(0.3600 E 00\) & 0.8000E 00 & 0.1299E 02 & 0.1100E 00 & 0.1060 E & 01 & 0.6900 E 00 \\
\hline 734 & 0.7160E 00 & 0.3100 EO & 0.8000 E 00 & 0.9280E 01 & 0.1100E 00 & 0.1060 E & 01 & 0.6900E 00 \\
\hline 735 & 0.6550E 00 & 0.4800 EO & 0.8000E 00 & 0.4040 E 02 & \(0.4100 \mathrm{E}-01\) & \(0.1060 E\) & 01 & 0.6900E 00 \\
\hline 736 & 0.6550E 00 & 0.4500 E 00 & 0.8000E 00 & 0.3073E 02 & 0.4100E-01 & 0.1060 E & 01 & 0.6900E 00 \\
\hline 737 & 0.6550E 00 & 0.4000 EO & 0.8000 E 00 & 0.2305E 02 & \(0.4100 \mathrm{E}-01\) & 0.1060E & 01 & 0.6900E 00 \\
\hline 738 & 0.6550E 00 & 0.3300 O 0 & 0.8000E 00 & 0.1195E 02 & 0.4100E-01 & 0.1060 E & 01 & 0.6900E 00 \\
\hline 739 & 0.6550E 00 & 0.3000500 & 0.8000E 00 & 0.8540E 01 & 0.4100E-01 & 0.1060E & 01 & 0.6900E 00 \\
\hline 740 & 0.5280E 00 & 0.4200E 00 & 0.8000E 00 & \(0.3295 E 02\) & 0.1800E-01 & 0.1060 E & 01 & 0.6900E 00 \\
\hline
\end{tabular}

\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|}
\hline & 8 & ㅇ & ㅇ． &  & 용 & 앙 & \％ & 8 & 8 & 앙 & 응 & 8 & \(\bigcirc\) & 용 & 8 & 앙 & \(\bigcirc\) & 앙 & 앙 & 8 \\
\hline \(\downarrow\) & \[
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\hline & 0 & \(\bigcirc\) & \(\stackrel{\sim}{0}\) & 3 & \(\stackrel{7}{0}\) & 0 & \(\stackrel{-0}{0}\) & －10 & \(\bigcirc\) & \(\overrightarrow{0}\) & \(\stackrel{7}{0}\) & \(\xrightarrow{-1}\) & \(\stackrel{-1}{0}\) & 0 & －1 & － & \(\xrightarrow{-1}\) & 3 & \(\overrightarrow{0}\) & \(\stackrel{\rightharpoonup}{0}\) \\
\hline m & \[
\stackrel{0}{0}
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\begin{aligned}
& \text { 山⿱⿵人一口口 } \\
& 0 \\
& 0 \\
& 0 \\
& 0
\end{aligned}
\] & \[
\begin{aligned}
& \text { 山⿱⿵人一口口 } \\
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& 0 \\
& \dot{0}
\end{aligned}
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\hline \(\times\) & \[
\begin{aligned}
& \dot{\omega} \\
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& 0 \\
& \vdots \\
& \dot{0}
\end{aligned}
\] & -0
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\(\vdots\)
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0 & 0
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\(i\)
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\(\vdots\)
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0 & \[
\begin{aligned}
& \ddot{0} \\
& 0 \\
& \mathbf{U} \\
& 0 \\
& 0 \\
& 0 \\
& \vdots \\
& 0
\end{aligned}
\] & \(\overrightarrow{0}\)
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\begin{gathered}
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\end{gathered}
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\(u\)
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0 & \[
\begin{aligned}
& \overrightarrow{0} \\
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& 10 \\
& 0 \\
& 0 \\
& 0 \\
& 0 \\
& 0
\end{aligned}
\] & \[
\begin{aligned}
& 0 \\
& 0 \\
& 1 \\
& \text { u } \\
& 0 \\
& 0 \\
& 0 \\
& 0 \\
& 0
\end{aligned}
\] & \[
\begin{aligned}
& -1 \\
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& 1 \\
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& 0 \\
& 0
\end{aligned}
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\begin{gathered}
\overrightarrow{0} \\
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山 \\
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N \\
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\end{gathered}
\] & \[
\begin{aligned}
& \overrightarrow{0} \\
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& 1 \\
& \hline 0 \\
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& 0 \\
& N \\
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& 0
\end{aligned}
\] & \[
\begin{aligned}
& \overrightarrow{0} \\
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& 1 \\
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& N \\
& \vdots \\
& 0
\end{aligned}
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0 & \(\overrightarrow{0}\)
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\hline & N & N & N & N & N & N & N & N & 0 & N & N & N & N & 0 & N & N & N & N & \(\square\) & N \\
\hline 0 & \[
\begin{aligned}
& n \\
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\end{aligned}
\] & \[
\begin{aligned}
& \dot{\alpha} \\
& \text { N } \\
& \text { N } \\
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\end{aligned}
\] & \[
\begin{aligned}
& u \\
& \alpha \\
& \neq \\
& \underset{\sim}{+} \\
& 0
\end{aligned}
\] & \[
\begin{aligned}
& \mu \\
& \stackrel{\sim}{0} \\
& M \\
& 0 \\
& \stackrel{\circ}{0}
\end{aligned}
\] &  & \[
\begin{aligned}
& \underset{0}{\omega} \\
& \vec{m} \\
& 0
\end{aligned}
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\begin{aligned}
& w \\
& \underset{\sim}{N} \\
& \stackrel{N}{N} \\
& \dot{0}
\end{aligned}
\] & \[
\begin{aligned}
& w \\
& \underset{\sim}{\sim} \\
& N \\
& \underset{\sim}{\sim} \\
& 0
\end{aligned}
\] & \(w\)
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\(\infty\)
\(\infty\)
\(\infty\)
0
0 & \[
\begin{aligned}
& W_{N}^{N} \\
& \infty \\
& \infty \\
& \vdots \\
& \vdots
\end{aligned}
\] &  & \[
\begin{aligned}
& \underset{\sim}{N} \\
& N \\
& N \\
& \underset{N}{N} \\
& 0
\end{aligned}
\] & \[
\begin{aligned}
& \text { U } \\
& \stackrel{\infty}{\star} \\
& \underset{\vdots}{\dot{0}}
\end{aligned}
\] & \(w\)
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\(\vdots\)
\(\infty\)
\(\infty\)
0
0 & \(\mu\)
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0
0
0
0
0 &  &  & \(u\)
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0 & \begin{tabular}{l} 
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0 \\
\multirow{1}{*}{} \\
0 \\
0
\end{tabular} &  \\
\hline & ： & － & \(\bigcirc\) & － & 8 & \(\bigcirc\) & 8 & 8 & O & \[
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\] & 앙 & 앙 & 8 &  & 8 & 8 & 8 & 8 & \(\bigcirc\) & 8 \\
\hline \(\pm\) & \[
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& \text { in } \\
& \dot{0} \\
& \dot{0}
\end{aligned}
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\begin{aligned}
& \bar{\circ} \\
& \text { in } \\
& \dot{0}
\end{aligned}
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on
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0 & 1
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0 & \(u\)
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0 & \(\Perp\)
\(\stackrel{1}{O}\)
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& \text { in } \\
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& 0
\end{aligned}
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\begin{aligned}
& \text { ü } \\
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& 0 \\
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& 0 \\
& 0 \\
& 0
\end{aligned}
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－ \\
\hline & \(\bigcirc\) & \(\bigcirc\) & － & \[
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\] & ㅇ & \(\bigcirc\) & ㅇ & \[
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\] & : & \(\bigcirc\) & \(\bigcirc\) & \(\bigcirc\) & \(\bigcirc\) & \(\bigcirc\) & \(\bigcirc\) & 앙 & 앙 & 8 \\
\hline J & \[
\begin{aligned}
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& + \\
& + \\
& \dot{+}
\end{aligned}
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\begin{aligned}
& 0 \\
& 0 \\
& 0 \\
& 0
\end{aligned}
\] & \[
\begin{aligned}
& \text { w } \\
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& 0 \\
& 0 \\
& 0 \\
& 0 \\
& 0
\end{aligned}
\] & \[
\begin{aligned}
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& 0 \\
& \dot{+} \\
& ! \\
& 0 \\
& 0
\end{aligned}
\] & \[
\begin{aligned}
& \text { ü } \\
& 0 \\
& 0 \\
& 0 \\
& ! \\
& 0 \\
& 0
\end{aligned}
\] & \[
\begin{aligned}
& \text { u } \\
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& \dot{N} \\
& \stackrel{+}{+} \\
& \dot{0}
\end{aligned}
\] & \(u\)
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0
0
0
0
0 & \(w\)
0
ㅇ
N
M
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0 \\
\hline \\
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0
\end{tabular} & \[
\begin{aligned}
& \text { u } \\
& \circ \\
& 0 \\
& \stackrel{~}{+} \\
& + \\
& \vdots
\end{aligned}
\] & \[
\begin{aligned}
& \text { u } \\
& 0 \\
& 0 \\
& 0 \\
& 0 \\
& 0 \\
& 0
\end{aligned}
\] & \[
\begin{aligned}
& \mu \\
& \stackrel{\mu}{O} \\
& \stackrel{1}{\circ} \\
& \stackrel{1}{0} \\
& \dot{0}
\end{aligned}
\] & \[
\begin{aligned}
& \text { w } \\
& 0 \\
& 0 \\
& \stackrel{\rightharpoonup}{7} \\
& 0
\end{aligned}
\] & \[
\begin{aligned}
& u \\
& 0 \\
& 0 \\
& 0 \\
& \stackrel{0}{0} \\
& 0
\end{aligned}
\] & \[
\begin{aligned}
& \text { 山 } \\
& 0 \\
& 0 \\
& 0 \\
& \stackrel{0}{7} \\
& 0
\end{aligned}
\] & 山
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0
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0
\(\vdots\)
0
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0 & 1
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0 \\
\hline & \(\bigcirc\) & 8 & － & ㅇ & : & \[
0
\] & － & O & \[
\therefore
\] & 응 & \(\bigcirc\) & \(\bigcirc\) & \(\bigcirc\) & \(\bigcirc\) & 8 & 8 & － & 8 & 8 & 8 \\
\hline  & \[
\begin{aligned}
& \text { 0 } \\
& 0 \\
& 0 \\
& 0
\end{aligned}
\] & \[
\begin{aligned}
& \text { ng } \\
& 0 . \\
& \infty \\
& 0 \\
& 0
\end{aligned}
\] & \[
\begin{aligned}
& \text { 山̈ } \\
& \text { in } \\
& 0 \\
& \text { 0 } \\
& \dot{0}
\end{aligned}
\] & \[
\begin{aligned}
& \text { n } \\
& 0 \\
& \text { o } \\
& \mathbf{1}
\end{aligned}
\] & \[
\begin{aligned}
& \text { ü } \\
& \stackrel{n}{N} \\
& \stackrel{1}{0} \\
& \dot{0}
\end{aligned}
\] & \[
\begin{aligned}
& \text { in } \\
& \hat{N} \\
& 0 \\
& 0
\end{aligned}
\] & \[
\begin{aligned}
& \text { N } \\
& \stackrel{1}{0} \\
& \vdots \\
& 0
\end{aligned}
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\multirow{1}{1}{} \\
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\end{tabular} & \[
\begin{aligned}
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& \text { in } \\
& 0 \\
& 0 \\
& 0
\end{aligned}
\] & \[
\begin{aligned}
& \text { 山⿱宀八口 } \\
& 0 \\
& 0 \\
& 0 \\
& 0 \\
& 0
\end{aligned}
\] & 18
+
0
0
0
0 & \[
\begin{aligned}
& \text { 山̈ } \\
& \stackrel{0}{0} \\
& \stackrel{0}{0} \\
& \dot{0}
\end{aligned}
\] & \[
\begin{aligned}
& \text { u } \\
& 0 \\
& 0 \\
& \vdots \\
& 0 \\
& 0 \\
& 0
\end{aligned}
\] & \[
\begin{aligned}
& \text { ü } \\
& \text { in } \\
& \underset{\vdots}{0} \\
& \dot{0}
\end{aligned}
\] &  & \(\Psi\)
\(\vdots\)
+
\(\vdots\)
\(\vdots\)
0 &  & 10
0
+
+
\(\stackrel{+}{+}\)
0
0 &  & \[
\begin{aligned}
& \text { Ü } \\
& \stackrel{\rightharpoonup}{0} \\
& 0 \\
& \stackrel{+}{0}
\end{aligned}
\] \\
\hline 品 & \[
\overrightarrow{0}
\] & \[
\begin{aligned}
& \text { N } \\
&
\end{aligned}
\] & \[
\stackrel{\text { N }}{\stackrel{0}{0}}
\] & + & \[
\] & \[
\begin{aligned}
& \circ \\
& \stackrel{\circ}{\circ}
\end{aligned}
\] & \[
\stackrel{\uparrow}{0}
\] & \[
\begin{gathered}
\infty \\
\end{gathered}
\] & \[
\begin{gathered}
\stackrel{a}{\circ} \\
\stackrel{0}{2}
\end{gathered}
\] & \[
\stackrel{\circ}{\mathrm{O}}
\] & \[
\underset{\sim}{*}
\] & \[
\underset{N}{N}
\] & \[
\stackrel{M}{\wedge}
\] & \[
\stackrel{\star}{\uparrow}
\] & \[
\stackrel{N}{N}
\] & \[
\stackrel{\circ}{\stackrel{\circ}{N}}
\] & N & \[
\stackrel{\infty}{\stackrel{\infty}{\uparrow}}
\] & \[
\stackrel{\oplus}{\uparrow}
\] & \(\stackrel{\circ}{\circ}\) \\
\hline
\end{tabular}

\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|c|c|c|c|}
\hline OBSV & SUBME & & \(\boldsymbol{u}\) & & H & & \(P\) & & \(x\) & \(w\) & & \(L\) & \\
\hline 801 & 0.7950E & 00 & \(0.4200 E\) & 00 & 0.1100 E & 01 & \(0.3683 E\) & 02 & \(0.2500 E-01\) & \(0.1060 E\) & 01 & 0.6900E & 00 \\
\hline 802 & 0.7950E & 00 & 0.3900 E & 00 & O.1100E & 01 & \(0.2762 E\) & 02 & \(0.2500 E-01\) & \(0.1060 E\) & 01 & 0.6900E & 00 \\
\hline 803 & 0.7950E & 00 & \(0.3200 E\) & 00 & \(0.1100 E\) & 01 & 0.1432 E & 02 & \(0.2500 E-01\) & \(0.1060 E\) & 01 & 0.6900E & 00 \\
\hline 804 & \(0.7950 E\) & 00 & 0.3000 E & 00 & \(0.1100 E\) & 01 & \(0.1023 E\) & 02 & \(0.2500 E-01\) & 0.1060E & 01 & 0.6900E & 00 \\
\hline 805 & 0.6940E & 00 & \(0.4100 E\) & 00 & 0.1100 E & 01 & \(0.4266 E\) & 02 & \(0.2500 E-01\) & \(0.1060 E\) & 01 & 0.6900 E & 00 \\
\hline 806 & 0.6940E & 00 & \(0.3900 E\) & 00 & 0.1100E & 01 & 0.3244 E & 02 & \(0.2500 E-01\) & \(0.1060 E\) & 01 & 0.6900 E & 00 \\
\hline 807 & 0.6940 E & 00 & 0.3600 E & 00 & 0.1100E & 01 & 0.2433 E & 02 & \(0.2500 E-01\) & 0.1060E & 01 & 0.6900 E & 00 \\
\hline 808 & \(0.6940 E\) & 00 & \(0.3000 E\) & 00 & O.1100E & 01 & \(0.1262 E\) & 02 & \(0.2500 \mathrm{E}-01\) & \(0.1060 E\) & 01 & 0.6900 E & 00 \\
\hline 809 & \(0.6940 E\) & 00 & 0.2800 E & 00 & 0.1100E & 01 & 0.9010 E & 01 & \(0.2500 E-01\) & \(0.1060 E\) & 01 & \(0.6900 E\) & 00 \\
\hline 810 & 0.6170 E & 00 & 0.3900E & 00 & 0.1100E & 01 & \(0.3820 E\) & 02 & \(0.2500 E_{1} 01\) & \(0.1060 E\) & 01 & 0.6900E & 00 \\
\hline 811 & \(0.6170 E\) & 00 & 0.3600 E & 00 & 0.1100E & 01 & \(0.2905 E\) & 02 & \(0.2500 E-01\) & 0.1060E & 01 & \(0.6900 E\) & 00 \\
\hline 812 & 0.6170E & 00 & 0.3400 E & 00 & 0.1100E & 01 & \(0.2179 E\) & 02 & \(0.2500 E-01\) & 0.1060 E & 01 & \(0.6900 E\) & 00 \\
\hline 813 & \(0.6170 E\) & 00 & \(0.2800 E\) & 00 & O. 1100 E & 01 & 0.1130 E & 02 & \(0.2500 E-01\) & 0.1060E & 01 & 0.6900E & 00 \\
\hline 814 & O.6170E & 00 & \(0.2600 E\) & 00 & 0.1100E & 01 & 0.8070 E & 01 & \(0.2500 E-01\) & \(0.1060 E\) & 01 & 0.6900E & 00 \\
\hline 815 & 0.5410E & 00 & \(0.3650 E\) & 00 & \(0.1100 E\) & 01 & 0.3372 E & 02 & \(0.2500 E-01\) & \(0.1060 E\) & 01 & 0.6900E & 00 \\
\hline 816 & \(0.5410 E\) & 00 & 0.3400 E & 00 & \(0.1100 E\) & 01 & \(0.2565 E\) & 02 & \(0.2500 E-01\) & \(0.1060 E\) & 01 & \(0.6900 E\) & 00 \\
\hline 817 & 0.5410 E & 00 & 0.3200 E & 00 & \(0.1100 E\) & 01 & \(0.1924 E\) & 02 & \(0.2500 \mathrm{E}-01\) & 0.1060 E & 01 & 0.6900 E & 00 \\
\hline 818 & 0.5410 E & 00 & 0.2600 E & 00 & \(0.1100 E\) & 01 & 0.9970 E & 01 & \(0.2500 \mathrm{E}-01\) & \(0.1060 E\) & 01 & \(0.6900 E\) & 00 \\
\hline 819 & 0.5410 E & 00 & 0.2400 E & 00 & \(0.1100 E\) & 01 & 0.7120 E & 01 & \(0.2500 \mathrm{E}-01\) & 0.1060 E & 01 & 0.6900 E & 00 \\
\hline
\end{tabular}
\begin{tabular}{c} 
Appendix E: \\
DIFFERENT RATES OF POWER CALCULATED FOR VARIOUS \\
\hline OPERATING CONDITIONS
\end{tabular}

Where, QOPERT=Air Flow Rate at the Operating Temperature and Pressure, \(\mathrm{m}^{3} / \mathrm{s}\)

QNORML=Air Flow Rate af the Standard Temperature and Pressure, \(\mathrm{m}^{3} / \mathrm{s}\)

QNMLI =Air Flow Rate af the Standard Temperature and Pressure, \(\mathrm{m}^{3} / \mathrm{min}\)

POWERI=Theoretical Power (Using Pressure Gauge Reading), KW

POWER2=Theoretical Power (Using Pressure Gauge Reading), Watts

POWER3=Theoretical Power (Using Submergence and Ignoring all the Losses), KW

POWER4=Theoretical Power (Using Submergence and Ignoring all the Losses), Watts

USEPWR=Useful Power, Watts

Note: The rate of power does not vary for different widths of the tank.
\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|}
\hline DBSERV & QOPERT & ONORML & POWER1 & POWER2 & POWER3 & POWER 4 & & ONML 1 & USEPWR \\
\hline 1 & 0.6666E-02 & 0.6935E-02 & 0.7367E-01 & 0.7367 E 02 & 0.2700E-01 & 0.2700E & 02 & \(0.4161 E 00\) & 0.2768E 02 \\
\hline 2 & 0.5033E-02 & 0.5236E-02 & 0.3755E-01 & 0.3755E 02 & 0.2039E-01 & 0.2039 E & 02 & \(0.3142 E 00\) & \(0.2090 E 02\) \\
\hline 3 & 0.3759E-02 & \(0.3911 \mathrm{E}-02\) & 0.2054E-01 & 0.2054E 02 & 0.1523E-01 & \(0.1523 E\) & 02 & \(0.2346 E 00\) & 0.1561 E 02 \\
\hline 4 & 0.1940E-02 & \(0.2018 \mathrm{E}-02\) & 0.6011E-02 & 0.6011 El & \(0.7858 \mathrm{E}-02\) & 0.7858 E & 01 & \(0.1211 E 00\) & 0.8055E 01 \\
\hline 5 & 0.6689E-02 & 0.6919E-02 & 0.7135E-01 & 0.7135E 02 & 0.2304E-01 & 0.2304 E & 02 & 0.4151 E 00 & 0.2364 E 02 \\
\hline 6 & 0.5047E-02 & 0.5220E-0? & 0.3411E-01 & 0.3411E 02 & 0.1738E-01 & 0.1738 E & 02 & 0.3132 EO & 0.1783E 02 \\
\hline 7 & 0.3769E-02. & 0.3899E-02 & 0.1796E-01 & 0.1796E 02 & 0.1298E-01 & 0.1298 E & 02 & 0.2339E 00 & 0.1332E 02 \\
\hline 8 & 0.1946E-02 & 0.2013E-02 & 0.5336E-02 & 0.5336 E 01 & 0.6704E-02 & \(0.6704 E\) & 01 & 0.1208E 00 & 0.6878 E 01 \\
\hline 9 & 0.6729E-02 & 0.6877E-02 & 0.6234E-01 & \(0.6234 E 02\) & 0.1477E-01 & 0.1477 E & 02 & 0.4126E 00 & 0.1518 E 02 \\
\hline 10 & 0.5076E-02 & 0.5188E-02 & 0.2725E-01 & 0.2725E 02 & \(0.1114 \mathrm{E}-01^{\prime}\) & 0.1114 E & 02 & 0.3113 EO & 0.1145 E 02 \\
\hline 11 & 0.3791E-02 & 0.3875E-02 & 0.1281E-01 & 0.1281 E 02 & 0.8322E-02 & \(0.8322 E\) & 01 & \(0.2325 E 00\) & 0.8553 E 01 \\
\hline 12 & 0.6618E-02 & 0.6981E-02 & \(0.8277 \mathrm{E}-01\) & 0.8277E 02 & 0.3680E-01 & 0.3680 E & 02 & 0.4188E 00 & \(0.3765 E 02\) \\
\hline 13 & 0.4997E-02 & 0.5271E-02 & 0.4447E-01 & 0.4447E 02 & 0.2779E-01 & 0.2779E & 02 & 0.3163E 00 & 0.2843E 02 \\
\hline 14 & \(0.3733 \mathrm{E}-02\) & 0.3937E-02 & 0.2573E-01 & 0.2573E 02 & 0.2076E-01 & \(0.2076 E\) & 02 & 0.2362E 00 & 0.2124 E \\
\hline 15 & 0.1927E-02 & 0.2033E-02 & 0.9364E-02 & 0.9364 El & 0.1072E-01 & 0.1072 E & 02 & 0.1220E 00 & 0.1097E 02 \\
\hline 16 & 0.6640E-02 & 0.6965E-02 & 0.8045E-01 & 0.8045 E & 0.3283E-01 & 0.3283 E & 02 & 0.4179E 00 & \(0.3361 E 02\) \\
\hline 17 & 0.5010E-02 & 0.5255E-02 & 0.4102E-01 & 0.4102 E 02 & \(0.2477 \mathrm{E}-01\) & 0.2477E & & 0.3153E 00 & 0.2536E 02 \\
\hline 18 & 0.3745E-02 & 0.3928E-02 & 0.2441E-01 & 0.2441E 02 & 0.1851E-01 & 0.1851 E & 02 & 0.2357E 00 & 0.1896E 02 \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|}
\hline & & N & & & \(\overrightarrow{0}\) & N & N & N & \(\stackrel{\square}{0}\) & N & N & N & N & \(\overrightarrow{0}\) & N & N & \(\bigcirc\) & N & \\
\hline \[
\begin{aligned}
& \frac{w}{3} \\
& \stackrel{y}{2} \\
& \underset{\sim}{w} \\
& 0
\end{aligned}
\] & \[
\] & \[
\begin{aligned}
& \text { 山 } \\
& \stackrel{1}{N} \\
& \stackrel{1}{\circ}
\end{aligned}
\] & \[
\begin{aligned}
& u \\
& \sigma \\
& \boldsymbol{\sigma} \\
& \infty \\
& 0 \\
& 0
\end{aligned}
\] &  &  &  & \[
\begin{gathered}
山 \\
\underset{M}{M} \\
\underset{\sim}{2} \\
\vdots
\end{gathered}
\] &  & \(u\)
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0
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0
0
0 &  & \[
\begin{aligned}
& w \\
& \infty \\
& \text { n } \\
& \text { N } \\
& 0 \\
& 0
\end{aligned}
\] & 1
0
0
0
0
0
0
0 & W
\(\underset{\sim}{\infty}\)
\(\vdots\)
0 &  &  &  & \[
\begin{aligned}
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& \stackrel{0}{n} \\
& \stackrel{+}{0} \\
& \vdots
\end{aligned}
\] & \[
\begin{gathered}
u \\
\infty \\
0 \\
\stackrel{0}{N} \\
\vdots \\
0
\end{gathered}
\] & 374 \\
\hline & \(\bigcirc\) & 앙 & \(\bigcirc\) & 8 & 앙 & 응 & 8 & 앙 & \(\bigcirc\) & \％ & ㅇ & \(\bigcirc\) & \(\bigcirc\) & \(\stackrel{\rightharpoonup}{0}\) & ： & 앙 & \(\bigcirc\) & 앙 & \\
\hline \(\frac{2}{2}\) & \[
\begin{gathered}
\text { 山⿱丷口犬} \\
\stackrel{N}{N} \\
\stackrel{\bullet}{0}
\end{gathered}
\] & \[
\begin{gathered}
\underset{\sim}{\omega} \\
\stackrel{\text { N }}{+} \\
\stackrel{+}{+}
\end{gathered}
\] & \[
\begin{gathered}
\omega \\
\stackrel{\omega}{0} \\
\underset{\sim}{m} \\
\dot{0}
\end{gathered}
\] & \[
\begin{aligned}
& \underset{\sim}{w} \\
& \underset{\sim}{N} \\
& \underset{\sim}{\circ}
\end{aligned}
\] & \[
\begin{gathered}
\text { 山̈ } \\
\stackrel{\rightharpoonup}{\hat{N}} \\
\stackrel{0}{2}
\end{gathered}
\] & \[
\begin{aligned}
& \text { 山⿱⿵人一口⿹丁口欠 } \\
& \stackrel{\text { n }}{0}
\end{aligned}
\] &  & \[
\begin{aligned}
& \mu \\
& \stackrel{\mu}{N} \\
& \underset{N}{N} \\
& \stackrel{1}{0}
\end{aligned}
\] &  & \[
\begin{aligned}
& \text { ש } \\
& 0 \\
& N \\
& + \\
& \dot{+}
\end{aligned}
\] & \[
\begin{aligned}
& w \\
& \underset{\sim}{0} \\
& \stackrel{1}{n} \\
& \stackrel{0}{0}
\end{aligned}
\] &  & \[
\begin{aligned}
& \text { w } \\
& \underset{\sim}{N} \\
& \underset{\sim}{\sim} \\
& \vdots
\end{aligned}
\] & \[
\begin{aligned}
& \dot{1} \\
& \stackrel{1}{a} \\
& \stackrel{\sim}{\infty} \\
& \infty \\
& \dot{0}
\end{aligned}
\] & \[
\begin{aligned}
& \text { u } \\
& 0 \\
& \sim \\
& \sim \\
& + \\
& \vdots
\end{aligned}
\] & \[
\begin{aligned}
& w \\
& \stackrel{w}{0} \\
& \stackrel{\rightharpoonup}{m} \\
& \dot{0}
\end{aligned}
\] &  & \[
\] & \\
\hline & \(\overrightarrow{0}\) & \％ & N & N & \(\square\) & N & \％ & N & \(\square\) & N & N & N & N & \(\square\) & N & N & N & N & \\
\hline  & \[
\begin{aligned}
& \mu \\
& \tilde{N} \\
& 0 \\
& 0 \\
& 0 \\
& \dot{0} \\
& \dot{0}
\end{aligned}
\] & \[
\begin{gathered}
\underset{\sim}{W} \\
\stackrel{\leftrightarrow}{4} \\
\stackrel{+}{4} \\
\stackrel{\circ}{0}
\end{gathered}
\] & \[
\begin{aligned}
& \underset{N}{\underset{N}{n}} \\
& \stackrel{\sim}{\infty} \\
& \stackrel{\vdots}{0}
\end{aligned}
\] & \[
\begin{aligned}
& \underline{\mu} \\
& \stackrel{\rightharpoonup}{\otimes} \\
& \underset{\sim}{0} \\
& \vdots \\
& \hline 0
\end{aligned}
\] & \[
\begin{aligned}
& \underset{\sim}{N} \\
& \underset{\sim}{N} \\
& \vdots
\end{aligned}
\] & 山
N
N
\(\stackrel{1}{N}\)
0 & \[
\begin{aligned}
& 山_{0} \\
& 0 \\
& 0 \\
& \vdots \\
& \vdots \\
& \hline 0
\end{aligned}
\] & \[
\begin{gathered}
\underset{\sim}{w} \\
\stackrel{N}{\sim} \\
\stackrel{\vdots}{\square}
\end{gathered}
\] & \[
\begin{aligned}
& w \\
& 0 \\
& 0 \\
& 0 \\
& 0 \\
& 0
\end{aligned}
\] & \(u\)
W
0
0
\(\stackrel{0}{0}\)
0 & \[
\begin{aligned}
& 山_{N}^{N} \\
& N \\
& N \\
& \underset{\sim}{N} \\
& \dot{0}
\end{aligned}
\] & \[
\begin{aligned}
& \text { 山 } \\
& \underset{\sim}{0} \\
& 0 \\
& \underset{0}{+} \\
& 0
\end{aligned}
\] & \[
\begin{aligned}
& \underset{\sim}{\infty} \\
& \underset{\sim}{\infty} \\
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\] & N & \(\vec{N}\) & N & \(\stackrel{M}{N}\) & \(\stackrel{+}{N}\) & \(\stackrel{\sim}{N}\) & \(\stackrel{0}{\sim}\) & N & \(\stackrel{\infty}{\sim}\) & N & \％ & \(\vec{m}\) & N & M & \(\stackrel{ \pm}{*}\) & n & 0 & \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|}
\hline obSERV & OOPERT & ONORML & POWER1 & POWER2 & POWER3 & POWER 4 & & ONMLI & USEPWR \\
\hline 37 & 0.1370E-02 & 0.1457E-02 & 0.7180E-02 & 0.7180 E 01 & 0.8860E-02 & 0.8860E & 01 & \(0.8739 \mathrm{E}-01\) & 0.9054 El \\
\hline 38 & 0.6630E-02 & 0.6969E-02 & 0.8049E-01 & 0.8049E 02 & \(0.3431 \mathrm{E}-01\) & 0.3431E & 02 & \(0.4181 E 00\) & 0.3513 E 02 \\
\hline 39 & 0.5003E-02 & 0.5259E-02 & 0.4104E-01 & 0.4104 E 02 & 0.2589E-01 & 0.2589E & 02 & 0.3155E 00 & 0.2650E 02 \\
\hline 40 & 0.3739E-02 & 0.393IE-02 & 0.2443E-01 & 0.2443 E 02 & 0.1935E-01 & 0.1935 E & 02 & 0.2358 E 00 & 0.1981E 02 \\
\hline 41 & 0.1930E-02 & 0.2028E-02 & 0.8026E-02 & 0.8026 E O1 & 0.9987E-02 & 0.9987 E & 01 & 0.1217E 00 & 0.1022 E 02 \\
\hline 42 & 0.1377E-02 & 0.1448E-02 & 0.5258E-02 & 0.5258E O1 & 0.7128E-02 & 0.7128 E & 01 & \(0.8686 E-01\) & \(0.7297 E 01\) \\
\hline 43 & 0.6640E-02 & 0.6959E-02 & 0.7823E-01 & 0.7823E 02 & 0.3216E-01 & \(0.3216 E\) & 02 & \(0.4175 E 00\) & \(0.3293 E 02\) \\
\hline 44 & 0.5014E-02 & 0.5254E-02 & \(0.4101 \mathrm{E}-01\) & 0.4101 E 02 & 0.2428E-01 & \(0.2428 E\) & 02 & 0.3152E 00 & 0.2486E 02 \\
\hline 45 & 0.3745E-02 & 0.3924E-02 & \(0.2313 \mathrm{E}-01\) & 0.2313 E 02 & \(0.1814 \mathrm{E}-01\) & 0.1814 E & 02 & \(0.2355 E 00\) & 0.1857E 02 \\
\hline 46 & 0.1934E-02 & 0.2026E-02 & 0.8019E-02 & 0.8019E 01 & 0.9365E-02 \({ }^{\prime}\) & 0.9365E & 01 & \(0.1216 E 00\) & 0.9590E 01 \\
\hline 47 & 0.1379E-02 & 0.1445E-02 & 0.4778E-02 & 0.4778E 01 & 0.6680E-02 & 0.6680E & 01 & \(0.8673 \mathrm{E}-01\) & 0.6840E 01 \\
\hline 48 & 0.6672E-02 & 0.6926E-02 & 0.7143E-01 & 0.7143E 02 & 0.2556E-01 & 0.2556 E & 02 & 0.4156 EO & \(0.2621 E 02\) \\
\hline 49 & 0.5037E-02 & 0.5229E-02 & 0.3584E-01 & 0.3584E 02 & 0.1930E-01 & 0.1930E & 02 & 0.3138 E 0 & 0.1979E 02 \\
\hline 50 & 0.3762E-02 & 0.3906E-02 & 0.1925E-01 & 0.1925E 02 & 0.1442E-01 & 0.1442 E & 02 & 0.2343E 00 & 0.1478E 02 \\
\hline 51 & 0.1941E-02 & 0.2015E-02 & 0.5342E-02 & 0.5342 E 01 & \(0.7438 \mathrm{E}-02\) & 0.7438E & 01 & 0.1209E 00 & 0.7627 El \\
\hline 52 & 0.1386E-02 & 0.1438E-02 & 0.3340E-02 & 0.3340 El & 0.5309E-02 & 0.5309 E & 01 & 0.8631E-01 & 0.5444 E 01 \\
\hline 53 & 0.6524E-02 & 0.7071E-02 & 0.1011E 00 & 0.1011 O & 0.5648E-01 & 0.5648 E & 02 & 0.4243 E 0 & 0.5756 E 02 \\
\hline 54 & 0.4927E-02 & \(0.5340 \mathrm{E}-02\) & \(0.5838 \mathrm{E}-01\) & 0.5838 E 02 & \(0.4265 E-01\) & \(0.4265 E\) & & 0.3204 E 0 & 0.4347 E 02 \\
\hline & - & & & & & & & & \[
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\end{tabular}
\begin{tabular}{ccc} 
ONMLI & USEPWR \\
\(0.2394 E ~ 00\) & \(0.3247 E\) & 02 \\
\(0.1235 E ~ 00\) & \(0.1676 E ~ 02\) \\
\(0.8817 E-01\) & \(0.1196 E\) & 02 \\
\(0.4233 E ~ 00\) & \(0.5354 E\) & 02 \\
\(0.3195 E ~ 00\) & \(0.4040 E\) & 02 \\
\(0.2387 E\) & 00 & \(0.3018 E\) \\
02 \\
\(0.1233 E\) & 00 & \(0.1559 E\) \\
02 \\
\(0.8798 E-01\) & \(0.1113 E\) & 02 \\
\(0.4211 E\) & 00 & \(0.4492 E\)
\end{tabular} 02
\begin{tabular}{ccc} 
POWER3 & POWER4 \\
\(0.3186 \mathrm{E}-01\) & 0.3186 E & 02 \\
\(0.1644 \mathrm{E}-01\) & 0.1644 E & 02 \\
\(0.1174 \mathrm{E}-01\) & 0.1174 E & 02 \\
\(0.5249 \mathrm{E}-01\) & 0.5249 E & 02 \\
\(0.3961 \mathrm{E}-01\) & 0.3961 E & 02 \\
\(0.2959 \mathrm{E}-01\) & 0.2959 E & 02 \\
\(0.1528 \mathrm{E}-01\) & 0.1528 E & 02 \\
\(0.1091 \mathrm{E}-01\) & 0.1091 E & 02 \\
\(0.4397 \mathrm{E}-01\) & \(0.4397 E\) & 02 \\
\(0.3318 \mathrm{E}-01\) & 0.3318 E & 02 \\
\(0.2477 \mathrm{E}-01\) & 0.2477 E & 02 \\
\(0.1279 \mathrm{E}-01\) & 0.1279 E & 02 \\
\(0.9129 \mathrm{E}-02\) & 0.9129 E & 01 \\
\(0.4199 \mathrm{E}-01\) & 0.4199 E & 02
\end{tabular}

POWERI
\(0.3616 E-01\)
\(0.1411 E-01\)
\(0.9602 E-02\)
\(0.9873 E-01\)
\(0.5491 E-01\)
\(0.3356 E-01\)
\(0.1342 E-01\)
\(0.9112 E-02\)
\(0.9182 E-01\)
\(0.4967 E-01\)
\(0.2835 E-01\)
\(0.1072 E-01\)
\(0.7183 E-02\)
\(0.8955 E-01\)
\(0.4794 E-01\)
\(0.2833 E-01\)
\(0.1071 E-01\)
\(0.6703 E-02\)
QNORML
\(0.3989 E-02\)
\(0.2059 E-02\)
\(0.1470 E-02\)
\(0.7056 E-02\)
\(0.5325 E-02\)
\(0.3978 E-02\)
\(0.2054 E-02\)
\(0.1466 E-02\)
\(0.7019 E-02\)
\(0.5296 E-02\)
\(0.3954 E-02\)
\(0.2042 E-02\)
\(0.1457 E-02\)
\(0.7009 E-02\)
\(0.5289 E-02\)
\(0.3951 E-02\)
\(0.2040 E-02\)
\(0.1455 E-02\)
QOPERT
\(0.3681 E-02\)
\(0.1899 E-02\)
\(0.1356 E-02\)
\(0.6545 E-02\)
\(0.4940 E-02\)
\(0.3690 E-02\)
\(0.1906 E-02\)
\(0.1360 E-02\)
\(0.6588 \mathrm{E}-02\)
\(0.4971 \mathrm{E}-02\)
\(0.3711 \mathrm{E}-02\)
\(0.1916 \mathrm{E}-02\)
\(0.1368 \mathrm{E}-02\)
\(0.6597 \mathrm{E}-02\)
\(0.4978 \mathrm{E}-02\)
\(0.3718 \mathrm{E}-02\)
\(0.1920 \mathrm{E}-02\)
\(0.1370 \mathrm{E}-02\)

\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|c|}
\hline OBSERV & QOPERT & ONORML & POWER1 & POWER2 & & POWER3 & POWER 4 & & ONMLI & USEPWR \\
\hline 91 & 0.1891E-02 & 0.2066E-02 & 0.1547E-01 & 0.1547 E & 02 & \(0.1815 E-01\) & 0.1815 E & 02 & 0.1240E 00 & \(0.1847 E 02\) \\
\hline 92 & 0.1350E-02 & 0.1475E-02 & 0.1058E-01 & 0.1058 E & 02 & 0.1295E-01 & \(0.1295 E\) & 02 & 0.8849E-01 & 0.1319E 02 \\
\hline 93 & 0.6536E-02 & 0.7060E-02 & \(0.9879 \mathrm{E}-01\) & 0.9879 E & 02 & \(0.5398 \mathrm{E}-01\) & \(0.5398 E\) & 02 & 0.4236E 00 & 0.5504 E 02 \\
\hline 94 & 0.4936E-02 & 0.5331E-02 & \(0.5664 \mathrm{E}-01\) & 0.5664 E & 02 & 0.4076E-01 & 0.4076 E & 02 & 0.31 g9E 00 & \(0.4157 E 02\) \\
\hline 95 & 0.3685E-02 & 0.3980E-02 & 0.3358E-01 & 0.3358 E & 02 & 0.3043E-01 & 0.3043 E & 02 & 0.2388E 00 & 0.3103 E 02 \\
\hline 96 & 0.1903E-02 & 0.2055E-02 & 0.1343E-01 & 0.1343E & 02 & 0.1572E-01 & 0.1572E & 02 & \(0.1233 E 00\) & 0.1602 E 02 \\
\hline 97 & 0.1358E-02 & 0.1467E-02 & \(0.9118 \mathrm{E}-02\) & 0.9118 E & 01 & 0.1122E-01 & 0.1122 E & 02 & \(0.8803 \mathrm{E}-01\) & 0.1144 E 02 \\
\hline 98 & 0.6541E-02 & 0.7045E-02 & \(0.9430 \mathrm{E}-01\) & 0.9430E & 02 & 0.5177E-01 & \(0.5177 E\) & 02 & \(0.4227 E 00\) & 0.5281E 02 \\
\hline 99 & 0.4940E-02 & \(0.5320 \mathrm{E}-02\) & 0.5321E-01 & 0.5321E & 02 & \(0.3910 \mathrm{E}-01\) & 0.3910 E & 02 & 0.3192 O & 0.3988E 02 \\
\hline 100 & 0.3687E-02 & 0.3971E-02 & 0.3100E-01 & 0.3100E & 02 & 0.2919E-01 \({ }^{\prime}\) & 0.2919 E & 02 & 0.2383E 00 & 0.2977E 02 \\
\hline 101 & 0.1906E-02 & 0.2052E-02 & 0.1275E-01 & 0.1275E & 02 & 0.1508E-01 & 0.1508E & 02 & 0.1231E 00 & 0.1539E 02 \\
\hline 102 & 0.1360E-02 & 0.1465E-02 & 0.8635E-02 & 0.8635E & 01 & 0.1077E-01 & 0.1077E & 02 & 0.8789E-01 & 0.1098 CL \\
\hline 103 & 0.6576E-02 & 0.7017E-02 & \(0.8966 \mathrm{E}-01\) & 0.8966E & 02 & 0.4517E-01 & 0.4517E & 02 & 0.4210E 00 & 0.4614 E 02 \\
\hline 104 & 0.4962E-02 & 0.5296E-02 & \(0.4800 \mathrm{E}-0.1\) & 0.4800E & 02 & 0.3409E-01 & 0.3409 E & 02 & 0.3177E 00 & 0.3432 E 02 \\
\hline 105 & 0.3707E-02 & 0.3956E-02 & 0.2337E-01 & 0.2837E & 02 & 0.2546E-01 & 0.2546 E & 02 & 0.2373E 00 & \(0.2601 E 02\) \\
\hline 106 & 0.1914E-02 & 0.2043E-02 & 0.1073E-01 & \(0.1073 E\) & 02 & \(0.1315 E-01\) & 0.1315 E & 02 & 0.1226E 00 & \(0.1343 \mathrm{E} \mathrm{O2}\) \\
\hline 107 & 0.1365E-02 & 0.1457E-02 & 0.6711E-02 & 0.6711 E & 01 & 0.9379E-02 & 0.9379E & 01 & 0.8742E-01 & 0.9579E 01 \\
\hline 108 & 0.6600E-02 & 0.6994E-02 & 0.8509E-01 & 0.8509 E & & \(0.4013 \mathrm{E}-01\) & 0.4013 E & 02 & \(0.4197 E 00\) & 0.4103 E 02 \\
\hline & - & & & & & & & & & \[
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\begin{tabular}{|c|}
\hline Appendix \(F\) \\
VARIOUS OPERATING CONDITIONS FOR WHICH \\
DIMENSIONLESS FACTORS WERE CALCULATED \\
\hline
\end{tabular}

\title{
Where SUBMER=Depth of Water Above the Diffusers, m QOBSD \(=\underset{\text { SCFM }}{\text { Observed Air Flow Rate (Rotameter Reading), }}\) PRGARD= Observed Pressure Gauge Reading, psig
}

For different widths of the tank, SUBMER, QOBSD and PRGARD readings did not change. Only the horizontal velocities changed along the depth for different widths of the tank.
\begin{tabular}{|c|c|c|c|}
\hline OBSERV & SUBMER & QOBSD & PRGARD \\
\hline 1 & \(0.4160 E 00\) & O.1420E 02 & 0.1650E 01 \\
\hline 2 & \(0.4160 E 00\) & 0.1080E 02 & 0.1100 E 01 \\
\hline 3 & 0.4160 O 0 & 0.8100 O O1 & 0.8000 E 0 \\
\hline 4 & 0.4160 O 0 & \(0.4200 E 01\) & 0.4500 O 0 \\
\hline 5 & 0.3550 E 00 & 0.1420E 02 & 0.1600E 01 \\
\hline 6 & \(0.3550 E 00\) & 0.1080E 02 & O.1000E 01 \\
\hline 7 & \(0.3550 E 00\) & 0.8100 O & 0.7000E 00 \\
\hline 8 & \(0.3550 E 00\) & \(0.4200 E 01\) & \(0.4000 E 00\) \\
\hline 9 & \(0.2280 E 00\) & \(0.1420 E 02\) & 0.1400E 01 \\
\hline 10 & \(0.2280 E 00\) & \(0.1080 E 02\) & 0.8000E 00 \\
\hline 11 & \(0.2280 E 00\) & 0.8100E 01 & \(0.5000 E 00\) \\
\hline 12 & 0.5660E 00 & \(0.1420 E 02\) & \(0.1850 E 01\) \\
\hline 13 & 0.5660E 00 & 0.1080E 02 & 0.1300E 01 \\
\hline 14 & \(0.5660 E 00\) & 0.8100 E 01 & 0.1000E 01 \\
\hline 15 & 0.5660 E 00 & \(0.4200 E 01\) & 0.7000E 00 \\
\hline 16 & 0.5050E 00 & \(0.1420 E 02\) & 0.1800 E 01 \\
\hline 17 & 0.5050e 00 & \(0.1080 E 02\) & 0.1200 O \\
\hline 18 & 0.5050 O 00 & 0.8100 E 01 & 0.9500 E 00 \\
\hline 19 & 0.5050 E 00 & \(0.4200 E 01\) & 0.6000 E 0 \\
\hline 20 & 0.3780 E 00 & \(0.1420 E 02\) & 0.1650 E 01 \\
\hline 21 & \(0.3780 E 00\) & 0.1080 O & 0.1050 E 01 \\
\hline 22 & 0.3780E 00 & 0.8100E O1 & 0.7000500 \\
\hline 23 & 0.3780 O 0 & \(0.4200 E 01\) & 0.4000 O \\
\hline 24 & 0.3450 E 0 & \(0.1420 E 02\) & 0.1600E 01 \\
\hline 25 & 0.3450 E 0 & \(0.1080 E 02\) & 0.1000E 01 \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|c|c|c|c|}
\hline OBSERV & \multicolumn{2}{|l|}{SUBMER} & \multicolumn{2}{|l|}{Q08SD} & \multicolumn{2}{|l|}{PRGARD} \\
\hline 26 & \(0.3450 E\) & 00 & 0.8100 E & 01 & \(0.6500 E\) & 00 \\
\hline 27 & 0.3450 E & 00 & 0.4200 E & 01 & 0.4000E & 00 \\
\hline 28 & 0.7160 E & 00 & 0.1420 E & 02 & 0.2050E & 01 \\
\hline 29 & 0.7160E & 00 & 0.1080E & 02 & 0.1550E & 01 \\
\hline 30 & 0.7160 E & 00 & 0.8100E & 01 & 0.1200E & 01 \\
\hline 31 & 0.7160E & 00 & \(0.4200 E\) & 01 & 0.9000 E & 00 \\
\hline 32 & 0.7160 E & 00 & 0.3000 E & 01 & 0.8000 E & 00 \\
\hline 33 & 0.6550 E & 00 & \(0.1420 E\) & 02 & 0.2000E & 01 \\
\hline 34 & 0.6550E & 00 & \(0.1080 E\) & 02 & 0.1450 E & 01 \\
\hline 35 & 0.6550E & 00 & 0.8100 E & 01 & 0.1100 E & 01 \\
\hline 36 & \(0.6550 E\) & 00 & \(0.4200 E\) & 01 & 0.8000E & 00 \\
\hline 37 & 0.6550E & 00 & \(0.3000 E\) & 01 & 0.7500E & 00 \\
\hline 38 & 0.528 OE & 00 & \(0.1420 E\) & 02 & 0.1800E & 01 \\
\hline 39 & 0.5280E & 00 & 0.1080 E & 02 & 0.1200E & 01 \\
\hline 40 & 0.5280 E & 00 & 0.8100 E & 01 & 0.9500 E & 00 \\
\hline 41 & 0.5280E & 00 & 0.4200 E & 01 & \(0.6000 E\) & 00 \\
\hline 42 & 0.528 OE & 00 & D.3000E & 01 & 0.5500 E & 00 \\
\hline 43 & 0.4950E & 00 & \(0.1420 E\) & 02 & 0.1750E & 01 \\
\hline 44 & 0.4950E & 00 & \(0.1080 E\) & 02 & 0.1200E & 01 \\
\hline 45 & 0.4950E & 00 & 0.8100E & 01 & 0.9000E & 00 \\
\hline 46 & 0.4950 E & 00 & 0.4200E & 01 & 0.600 OE & 00 \\
\hline 47 & 0.4950E & 00 & \(0.3000 E\) & 01 & 0.5000 E & 0.0 \\
\hline 48 & 0.3940 E & 00 & \(0.1420 E\) & 02 & \(0.1600 E\) & 01 \\
\hline 49 & 0.3940E & 00 & 0.1080E & 02 & \(0.1050 E\) & 01 \\
\hline 50 & \(0.3940 E\) & 00 & 0.8100 E & 01 & 0.7500E & 00 \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|c|c|c|c|}
\hline OBSERV & \multicolumn{2}{|l|}{SUBMER} & \multicolumn{2}{|l|}{QOBSD} & \multicolumn{2}{|l|}{PRGARD} \\
\hline 51 & 0.3940 E & 00 & 0.4200 E & 01 & 0.4000E & 00 \\
\hline 52 & 0.394 OE & 00 & 0.3000E & 01 & 0.3500E & 00 \\
\hline 53 & 0.8660E & 00 & \(0.1420 E\) & 02 & \(0.2250 E\) & 01 \\
\hline 54 & \(0.8660 E\) & 00 & 0.1080E & 02 & 0.1700E & 01 \\
\hline 55 & 0.8660 E & 00 & 0.8100 E & 01 & 0.1400 E & 01 \\
\hline 56 & 0.8660E & 00 & 0.4200 E & 01 & \(0.1050 E\) & 01 \\
\hline 57 & \(0.8660 E\) & 00 & 0.30 .00 E & 01 & 0.1000E & 01 \\
\hline 58 & 0.8050 E & 00 & 0.1420 E & 02 & \(0.2200 E\) & 01 \\
\hline 59 & 0.8050 E & 00 & 0.1080 E & 02 & 0.1600 E & 01 \\
\hline 60 & 0.8050E & 00 & 0.8100 E & 01 & 0.1300E & 01 \\
\hline 61 & 0.8050E & 00 & \(0.4200 E\) & 01 & 0.1000E & 01 \\
\hline 62 & 0.8050 E & 00 & 0.3000E & 01 & 0.9500 E & 00 \\
\hline 63 & 0.6750 E & 00 & \(0.1420 E\) & 02 & 0.2050E & 01 \\
\hline 64 & 0.6750E & 00 & \(0.1080 E\) & 02 & 0.1450 E & 01 \\
\hline 65 & 0.6750E & 00 & \(0.8100 E\) & 01 & O.1 I OOE & 01 \\
\hline 66 & 0.6750E & 00 & \(0.4200 E\) & 01 & 0.8000 E & 00 \\
\hline 67 & 0.6750 E & 00 & \(0.3000 E\) & 01 & 0.7500E & 00 \\
\hline 68 & 0.6450E & 00 & \(0.1420 E\) & 02 & \(0.2000 E\) & 01 \\
\hline 69 & 0.6450 E & 00 & 0.1080E & 02 & 0.1400E & 01 \\
\hline 70 & 0.6450E & 00 & 0.8100E & 01 & \(0.1100 E\) & 01 \\
\hline 71 & 0.6450E & 00 & 0.4200E & 01 & \(0.8000 E\) & 00 \\
\hline 72 & 0.6450 E & 00 & \(0.3000 E\) & 01 & 0.7000 E & 00 \\
\hline 73 & 0.5440E & 00 & 0.1420E & 02 & 0.1800E & 01 \\
\hline 74 & 0.5440 E & 00 & 0.1080E & 02 & 0.1250E & 01 \\
\hline 75 & 0.5440E & 00 & 0.8100 E & 01 & \(0.1000 E\) & 01 \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|c|c|c|c|}
\hline OBSERV & \multicolumn{2}{|l|}{SUBMER} & \multicolumn{2}{|l|}{aobso} & \multicolumn{2}{|l|}{PRGARD} \\
\hline 76 & 0.5440 E & 00 & 0.4200 E & 01 & 0.6000 E & 00 \\
\hline 77 & 0.5440 E & 00 & 0.3000 E & 01 & \(0.5500 E\) & 00 \\
\hline 78 & 0.4670 E & 00 & 0.1420 E & 02 & 0.1700E & 01 \\
\hline 79 & 0.4670 E & 00 & 0.1080 E & 02 & 0.1150 E & 01 \\
\hline 80 & 0.4670E & 00 & 0.8100 E & 01 & 0.8000 E & 00 \\
\hline 81 & 0.4670 E & 00 & 0.4200 E & 01 & 0.5000 E & 00 \\
\hline 82 & \(0.4670 E\) & 00 & 0.30 .00 E & 01 & 0.4000 E & 00 \\
\hline 83 & \(0.1016 E\) & 01 & \(0.1420 E\) & 02 & 0.2400E & 01 \\
\hline 84 & 0.1016 E & 01 & 0.1080E & 02 & D. 1900 E & 01 \\
\hline 85 & \(0.1016 E\) & 01 & 0.8100 E & 01 & 0.1550E & 01 \\
\hline 86 & 0.1016 E & 01 & 0.4200 E & 01 & 0.1250E & 01 \\
\hline 87 & 0.1016 E & 01 & \(0.3000 E\) & 01 & 0.1200E & 01 \\
\hline 88 & \(0.9550 E\) & 00 & \(0.1420 E\) & 02 & 0.2350E & 01 \\
\hline 89 & 0.9550E & 00 & O.1080E & 02 & 0.1800 E & 01 \\
\hline 90 & 0.9550 E & 00 & 0.8100 E & 01 & 0.1500 E & 01 \\
\hline 91 & 0.9550 E & 00 & \(0.4200 E\) & 01 & 0.1150 E & 01 \\
\hline 92 & \(0.9550 E\) & 00 & 0.3000 E & 01 & 0.1100 E & 01 \\
\hline 93 & 0.828 OE & 00 & \(0.1420 E\) & 02 & 0.2200E & 01 \\
\hline 94 & \(0.8280 E\) & 00 & \(0.1080 E\) & 02 & 0.1650E & 01 \\
\hline 95 & \(0.8280 E\) & 00 & -0.8100E & 01 & 0.1300E & 01 \\
\hline 96 & 0.8280E & 00 & \(0.4200 E\) & 01 & 0.1000 E & 01 \\
\hline 97 & 0.8280 E & 00 & 0.3000 E & 01 & 0.9500 E & 00 \\
\hline 98 & 0.7950 E & 00 & 0.1420E & 02 & 0.2100 E & 01 \\
\hline 99 & 0.7950 E & 00 & \(0.1080 E\) & 02 & 0.1550E & 01 \\
\hline 100 & 0.7950 E & 00 & 0.8100 E & 01 & 0.1200 E & 01 \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|c|}
\hline OBSERV & SUBMER & QOBSD & PRGARD \\
\hline 101 & 0.7950E 00 & \(0.4200 E 01\) & 0.9500E 00 \\
\hline 102 & 0.7950E 00 & \(0.30000^{01}\) & 0.9000E 00 \\
\hline 103 & 0.6940 E 00 & 0.1420E 02 & \(0.2000 E 01\) \\
\hline 104 & 0.6940E 00 & 0.1080E 02 & 0.1400E 01 \\
\hline 105 & \(0.6940 E 00\) & 0.8100 El & 0.1100 E 01 \\
\hline 106 & 0.6940E 00 & \(0.4200 E 01\) & 0.8000E 00 \\
\hline 107 & 0.6940E 00 & 0.3000E 01 & 0.7000 E 0 \\
\hline 108 & 0.6170 E O & \(0.1420 E 02\) & 0.1900 O \\
\hline 109 & 0.6170 E 0 & \(0.1080 E 02\) & \(0.1300 E 01\) \\
\hline 110 & 0.6170E 00 & 0.8100 O & 0.1000E 01 \\
\hline 111 & 0.6170 O & \(0.4200 E 01\) & 0.6500E 00 \\
\hline 112 & 0.6170E 00 & \(0.3000 E 01\) & 0.6000 E 00 \\
\hline 113 & 0.541 OE 00 & 0.1420E 02 & 0.1800 E 01 \\
\hline 114 & 0.5410 OO & 0.1080E 02 & 0.1200E 01 \\
\hline 115 & 0.5410 O 0 & 0.8100 E 01 & 0.9000 E 00 \\
\hline 116 & 0.5410 O 0 & 0.4200E 01 & 0.6000E 00 \\
\hline 117 & 0.5410 OO & 0.3000 E 01 & 0.5500E 00 \\
\hline
\end{tabular}
\begin{tabular}{c} 
APpendix G \\
VARIOUS DIMENSIONLESS FACTORS FOR DIFFERENT \\
\hline OPERATING CONDITIONS \\
\hline
\end{tabular}
```

Where Fl = Velocity Factor
F2 = Power Factor
F3 = Width Factor
F4 = Depth Factor
F5 = Submergence Factor

```
F 1
F2
F3
F4
F5

1

2

3
\(40.3493 E \quad 05\)
0.4009 E 16
0.1177E 17
\(0.8879 E 16\)
\(0.6633 E 16\)
\(0.3425 E 16\)
\(0.7560 E 16\)
\(0.5702 E 16\)
\(0.4259 E 16\)
\(0.2437 E 17\)
\(0.1841 E 17\)
0.1375 E 17
\(0.1168 E 06\)
\(0.9082 E 05\)
0.7102 E 16
\(0.1427 E 06\)
\(0.2176 E 17\)
\(0.1297 E 06\)
\(0.1642 E 17\)
\(0.1103 E 06\)
\(0.1227 E 17\)
\(0.6332 E 16\)
\(0.8433 E 05\)
0.1168 E 06
0. 1378 E 17 0.1041 E 17
\(0.4880 E \quad 01\)
\(0.4880 E 01\)
\begin{tabular}{llll}
\(0.1069 E\) & 05 & \(0.8320 E\) & 00 \\
\(0.1069 E\) & 05 & \(0.8320 E\) & 00 \\
\(0.1069 E\) & 05 & \(0.832 O E\) & 00 \\
\(0.1069 E\) & 05 & \(0.8320 E\) & 00 \\
\(0.1069 E\) & 05 & \(0.7100 E\) & 00
\end{tabular}
\(0.1069 E 050.7100 E 00\)
\(0.1069 E 05 \quad 0.7100 E 00\)
\(0.1069 E 050.7100 E\) OO
\(0.1069 E 05\) O.4560E 00
\(0.1069 E 050.4560 E 00\)
\(0.1069 E 050.4500 E 00\)
\(0.1390 E 050.8708 E 00\)
\(0.1390 E 050.8708 E 00\)
\(0.1390 E \quad 05 \quad 0.8708 E \quad 00\)
\(0.1390 E 05\) O.8708E 00
O. 1390 E O5 O.7769E 00 0.3754 E 01 0.1390E 05 O. \(0.7769 E 00\) \(0.3754 E 01 \quad 0.1390 E 05\) O.7769E OU 0.3754E 01 O.1390E. O5 O.7769E 00 \(0.3754 E \quad 0\)
O.1390E 05
0.5815 E 00

\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|}
\hline Oesv & F1 & & F2 & & F3 & & F4 & & F5 \\
\hline 41 & 0.1198E & 06 & \(0.8143 E\) & 16 & \(0.3050 E\) & 01 & O.1710E & 05 & 0.6600E 00 \\
\hline 42 & 0.9581E & 05 & 0.5817 E & 16 & 0.3050 E & 01 & 0.1710E & 05 & 0.6600E 00 \\
\hline 43 & 0.1756E & 06 & \(0.2624 E\) & 17 & \(0.3050 E\) & 01 & O. 1710 E & 05 & 0.6187E 00 \\
\hline 44 & 0.1597E & 06 & 0.1981E & 17 & 0.3050E & 01 & 0.1710E & 05 & 0.6187E 00 \\
\hline 45 & \(0.1437 E\) & 06 & 0.1480 E & 17 & 0.3050E & 01 & 0.1710E & 05 & 0.6187E 00 \\
\hline 46 & 0.1118 E & 06 & 0.7641 E & 16 & 0.3050E & 01 & 0.1710E & 05 & 0.6187E 00 \\
\hline 47 & \(0.8782 E\) & 05 & 0.5450E & 16 & 0.3050E & 0.1 & 0.1710E & 05 & \(0.6187 E 00\) \\
\hline 48 & \(0.1597 E\) & 06 & 0.2088 E & 17 & 0.3050E & 01 & O.1710E & 05 & \(0.4925 E 00\) \\
\hline 49 & \(0.1437 E\) & 06 & 0.1577E & 17 & 0.3050E & 01 & 0.1710E & 05 & 0.4925E 00 \\
\hline 50 & 0.1277 E & 06 & 0.1178 E & 17 & \(0.3050 E\) & 01 & 0.1710 E & 05 & \(0.4925 E 00\) \\
\hline 51 & 0.1033 E & 06 & 0.6080E & 16 & 0.3050E & 01 & D. 1710 E & 05 & 0.4925E 00 \\
\hline 52 & 0.7984E & 05 & \(0.4335 E\) & 16 & 0.3050E & 01 & 0.1710E & 05 & 0.4925E 00 \\
\hline 53 & 0.3413E & 06 & \(0.5446 E\) & 17 & 0.2568 E & 01 & 0.2031 E & 05 & 0.9116 E 00 \\
\hline 54 & \(0.3129 E\) & 06 & 0.4113 E & 17 & 0.2568 E & 01 & \(0.2031 E\) & 05 & 0.9116E 00 \\
\hline 55 & 0.2844 E & 06 & \(0.3072 E\) & 17 & 0.2568E & 01 & \(0.2031 E\) & 05 & 0.9116 E 00 \\
\hline 56 & 0.2275E & 06 & 0.1586 E & 17 & 0.2568E & 01 & 0.2031 E & 05 & 0.9116 E 00 \\
\hline 57 & 0.1991 E & 06 & 0.1132 E & 17 & 0.2568E & 01 & 0.2031 E & 05 & 0.9116E 00 \\
\hline 58 & \(0.3224 E\) & 06 & 0.5066E & 17 & 0.2568E & 01 & \(0.2031 E\) & & 0.8474 E 00 \\
\hline 59 & 0.2844 E & 06 & \(0.3823 E\) & 17 & 0.2568E & 01 & O.2031E & & 0.8474 E 00 \\
\hline 60 & \(0.2465 E\) & 06 & 0.2856E & 17 & 0.2568E & 01 & 0.2031E & 05 & \(0.8474 E 00\) \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|}
\hline Oesv & F1 & & F2 & & F3 & & F4 & & F5 \\
\hline 61 & 0.1991E & 06 & \(0.1475 E\) & 17 & 0.2568E & 01 & \(0.2031 E\) & & 0.8474500 \\
\hline 62 & 0.1801 E & 06 & \(0.1053 E\) & 17 & 0.2568E & 01 & 0.2031 E & 05 & 0.3474 E 00 \\
\hline 63 & 0.2844E & 06 & \(0.4250 E\) & 17 & 0.2568 E & 01 & 0.2031 E & 05 & \(0.7105 E 00\) \\
\hline 64 & O.2560E & 06 & \(0.3208 E\) & 17 & 0.2568E & & 0.2031 E & 05 & \(0.7105 E 00\) \\
\hline 65 & 0.2275E & 06 & \(0.2394 E\) & 17 & 0.2568 E & 01 & \(0.2031 E\) & 05 & \(0.7105 E 00\) \\
\hline 66 & 0.1801E & 06 & \(0.1237 E\) & 17 & 0.2568E & 01 & 0.2031 E & 05 & \(0.7105 E 00\) \\
\hline 67 & 0.1517 E & 06 & 0.8828E & 16 & 0.2568E & 01 & \(0.2031 E\) & 05 & \(0.7105 E 00\) \\
\hline 68 & \(0.2655 E\) & 06 & 0.4061E & 17 & \(0.2568 E\) & 01 & 0.2031 E & 05 & 0.6789 E 00 \\
\hline 69 & 0.2465E & 06 & \(0.3116 E\) & 17 & 0.2568E & 01 & \(0.2031 E\) & 05 & 0.6783 E 00 \\
\hline 70 & 0.2181 E & 06 & \(0.2289 E\) & 17 & 0.2568E & 01 & 0.2031 E & 05 & 0.6783 E 00 \\
\hline 71 & 0.1707 E & 06 & 0.1182 E & 17 & 0.2568E & 01 & 0.2031 E & 05 & 0.6789E 00 \\
\hline 72 & \(0.1327 E 0\) & 06 & 0.8431 E & 16 & 0.2568E & 01 & \(0.2031 E\) & 05 & 0.6739E 00 \\
\hline 73 & 0.2560E 0 & 06 & 0.3423E & 17 & 0.2568E & 01 & \(0.2031 E\) & 05 & 0.5726E 00 \\
\hline 74 & \(0.2370 E\) OG & 06 & 0.2585E & 17 & 0. 2568 E & 01 & \(0.2031 E\) & 05 & \(0.5726 E 00\) \\
\hline 75 & D.2086E 0 & 06 & \(0.1932 E\) & 17 & 0. 2568 E & 01 & \(0.2031 E\) & 05 & 0.5726E 00 \\
\hline 76 & 0.1422E 0 & 06 & 0.9964 E & 16 & 0.2563E & 01 & 0.2031 E & 05 & 0.5726E 00 \\
\hline 77 & 0.1138 E & 06 & 0.7115 E & 16 & 0.2568E & 0.1 & 0.2031 E & 05 & 0.5726E 00 \\
\hline 78 & \(0.2465 E 0\) & 06 & \(0.2940 E\) & 17 & 0.2568E & 01 & 0.2031 E & & 0.4916 O \\
\hline 79 & \(0.2275 E\) & 06 & 0.2220E & 17 & 0.2568 E & 01 & \(0.2031 E\) & 05 & 0.4916 E 00 \\
\hline 80 & 0.1896 E & 06 & \(0.1647 E\) & 17 & 0.2568E & 01 & \(0.2031 E\) & & 0.4916 EO \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|c|}
\hline O8sv & F1 & & \(F 2\) & & F3 & & \(F 4\) & & FS & \\
\hline 81 & \(0.1327 E\) & 06 & 0.8554E & 16 & 0. 2568 E & 01 & \(0.2031 E\) & 05 & \(0.4916 E\) & 00 \\
\hline 82 & 0.9481 E & 05 & \(0.6103 E\) & 16 & 0.2568E & 01 & 0.2031 E & 05 & 0.4916 E & 00 \\
\hline 83 & \(0.4281 E\) & 06 & \(0.7391 E\) & 17 & \(0.2218 E\) & 01 & \(0.2352 E\) & 05 & \(0.9236 E\) & 00 \\
\hline 84 & \(0.3952 E\) & 06 & 0.5585E & 17 & \(0 \cdot 2218 E\) & 01 & 0.2352E & 05 & 0.9236 E & 00 \\
\hline 85 & \(0.3623 E\) & 06 & 0.4170 F & 17 & 0.2218E & 01 & \(0.2352 E\) & 05 & 0.9236E & 00 \\
\hline 86 & 0.2854E & 06 & \(0.2154 E\) & 17 & \(0.2218 E\) & 01 & \(0 \cdot 2352 E\) & 05 & 0.9236E & 00 \\
\hline 87 & \(0.2635 E\) & 06 & 0.1537E & 17 & \(0.2218 E\) & 01 & \(0.2352 E\) & 05 & \(0.9236 E\) & 00 \\
\hline 88 & \(0.3952 E\) & 06 & 0.6951E & 17 & 0.2218E & 01 & \(0.2352 E\) & 05 & \(0.8682 E\) & 00 \\
\hline 89 & \(0.3623 E\) & 06 & \(0.5250 E\) & 17 & \(0.2218 E\) & 01 & 0.2352E & 05 & 0.8682E & 00 \\
\hline 90 & \(0.3293 E\) & 06 & \(0.3922 E\) & 17 & 0.2218E & 01 & \(0.2352 E\) & 05 & 0.8682E & 00 \\
\hline 91 & .0.26.35E & 06 & \(0.2024 E\) & 17 & \(0.2218 E\) & 01 & \(0.2352 E\) & 05 & \(0.8682 E\) & 00 \\
\hline 92 & \(0.2305 E\) & 06 & 0.1445E & 17 & 0.2218E & 01 & 0.2352E & 05 & 0.8682E & 00 \\
\hline 93 & \(0.3623 E\) & 06 & 0.6030E & 17 & 0.2218E & 01 & 0.2352E & 05 & \(0.7527 E\) & 00 \\
\hline 94 & \(0.3293 E\) & 06 & \(0.4554 E\) & 17 & 0.2218 E & 01 & \(0.2352 E\) & 05 & 0.7527E & 00 \\
\hline 95 & \(0.2964 E\) & 06 & 0.3400E & 17 & \(0.2218 E\) & 01 & \(0.2352 E\) & 05 & \(0.7527 E\) & 00 \\
\hline 96 & \(0.2196 E\) & 06 & O. 1755 E & 17 & 0.2218 E & 01 & \(0 \cdot 2352 E\) & 05 & 0.7527E & 00 \\
\hline 97 & 0.1866E & 06 & \(0.1253 E\) & 17 & 0.2218E & 01 & \(0.2352 E\) & 05 & 0.7527E & 00 \\
\hline 98 & \(0.3293 E\) & 06 & \(0.5786 E\) & 17 & 0.2218E & 01 & \(0.2352 E\) & 05 & \(0.7227 E\) & 00 \\
\hline 99 & \(0.3074 E\) & 06 & \(0.4369 E\) & 17 & 0.2218 E & 01 & \(0 \cdot 2352 E\) & 05 & \(0.7227 E\) & 00 \\
\hline 100 & \(0.2744 E\) & 06 & \(0.3262 E\) & 17 & 0.2218E & 01 & \(0.2352 E\) & 05 & 0.7227E & 00 \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|c|}
\hline 08sV & F1 & & F2 & & F3 & & F4 & & F5 & \\
\hline 101 & \(0.2086 E\) & 06 & 0.1686 E & 17 & 0.2218 E & 01 & 0.2352E & 05 & 0.72275 & 00 \\
\hline 102 & \(0.1756 E\) & 06 & 0.1203 E & 17 & 0.2213 E & 01 & \(0.2352 E\) & 05 & 0.7227 E & 00 \\
\hline 103 & 0.3184 E & 06 & \(0.5055 E\) & 17 & 0.2218 E & 01 & \(0.2352 E\) & 05 & 0.6309E & OO \\
\hline 104 & 0.2854E & 06 & \(0.3815 E\) & 17 & 0.2218E & 01 & O.2352E & 05 & \(0.6309 E\) & 00 \\
\hline 105 & \(0.2525 E\) & 06 & 0.2850E & 17 & 0.2218E & 01 & O.2352E & 05 & 0.6309 E & 00 \\
\hline 106 & 0.1976E & 06 & \(0.1471 E\) & 17 & 0.2218 E & 01 & 0.2352E & 05 & \(0.6309 E\) & 00 \\
\hline 107 & 0.1647 E & 06 & 0.1050E & 17 & 0.2218 E & 01 & 0.2352E & 05 & \(0.6309 E\) & 00 \\
\hline 108 & 0.2964E & 0.6 & 0.4495E & 17 & 0.2218 E & 01 & \(0.2352 E\) & 05 & \(0.5609 E\) & 00 \\
\hline 109 & 0.2744E & 06 & \(0.3392 E\) & 17 & 0.2218 E & 01 & 0.2352 E & 05 & 0.5609E & 00 \\
\hline 110 & 0.2415 E & 06 & \(0.2534 E\) & 17 & 0.2218 E & 01 & \(0.2352 E\) & 05 & \(0.5609 E\) & 00 \\
\hline 111 & \(0.1756 E\) & 06 & \(0.1307 E\) & 17 & 0.2218E & 01 & 0.2352E & . 05 & \(0.5609 E\) & 00 \\
\hline 112 & \(0.1537 E\) & 06 & 0.9335 E & 16 & 0.2218E & 01 & \(0.2352 E\) & 05 & 0.5609E & 00 \\
\hline 113 & \(0.2744 E\) & 06 & \(0.3942 E\) & 17 & 0.2218E & 01 & 0.2352E & 05 & 0.49185 & 00 \\
\hline 114 & \(0.2525 E\) & 06 & 0.2975E & 17 & 0.2218 E & 01 & \(0.2352 E\) & 05 & 0.4918E & 00 \\
\hline 115 & \(0.2305 E\) & 06 & \(0.2222 E\) & 17 & \(0.2218 E\) & 01 & 0.2352E & 05 & 0.4918 E & 00 \\
\hline 116 & \(0.1537 E\) & 06 & \(0.1147 E\) & 17 & 0.2218E & 01 & 0.2352E & 05 & 0.4918 E & 00 \\
\hline 117 & 0.1317 E & 06 & \(0.8195 E\) & 16 & 0.2218E & 01 & 0.2352E & 05 & 0.4918 E & 00 \\
\hline 118 & \(0.8483 E\) & 05 & 0.1306E & 17 & 0.4420E & 01 & 0.1069E & 05 & 0.8320E & 00 \\
\hline 119 & 0.7485 E & 05 & \(0.9935 E\) & 16 & 0.4420E & 01 & \(0.1069 E\) & 05 & \(0.8320 E\) & 00 \\
\hline 120 & 0.6487 E & 05 & 0.7450 E & 16 & 0.4420E & 01 & \(0.1069 E\) & 05 & \(0.8320 E\) & 00 \\
\hline
\end{tabular}

121 122
\(0.3992 E 05\)
\(0.7984 E 05\)
\(0.6986 E 05\)
\(0.5988 E 05\)
\(0.3992 E 05\)
0.7485 E 05
\(0.6238 E 05\)
\(0.5489 E 05\)
0.1687E 06
\(0.1492 E 06\)
\(0.1362 E 06\)
\(0.1038 E 06\)
\(0.1622 E 06\)
\(0.1427 E 06\)
0.1297E 06
\(0.9730 E 05\)
\(0.1362 E 06\)
\(0.1168 E 06\)
\(0.1038 E 06\)
\(0.7784 E 05\)
\begin{tabular}{|c|c|c|c|c|c|c|}
\hline \(0.3864 E\) & 16 & 0.44 & 01 & \(0.1069 E\) & & \(0.8320 E\) \\
\hline \(0.1121 E\) & 17 & \(0.4420 E\) & 01 & 0.1069E & 05 & 0.7100 e O \\
\hline 0.8526E & 16 & 0.4420 & 01 & \(0.1069 E\) & 05 & 0.7100E 00 \\
\hline 0.6394 E & 16 & 0.4420 & 01 & \(0.1069 E\) & 05 & 0.7100E 00 \\
\hline \(0.3316 E\) & 16 & 0.4420 & 01 & 0.106 & 05 & 0.7100E 00 \\
\hline \(0.7286 E\) & 16 & \(0.4420 E\) & 01 & 0.106 & 05 & \(0.4560 \leq 00\) \\
\hline 0.5543 E & 16 & O.4420E & 01 & 0.106 & 05 & \(0.4560 \leq 00\) \\
\hline 0.4157 E & 16 & \(0.4420 E\) & 01 & 0.106 & 05 & 0.4560E 00 \\
\hline \(0.2278 E\) & 17 & \(3400 E\) & 01 & 0.139 & 05 & 0.3703E 00 \\
\hline 0.1733 E & 17 & 0.3400 er & 01 & 0.1390 E & 05 & 0.8708E 00 \\
\hline 0.1300E & 17 & 0.3400 & 01 & 0.139 & 05 & 0.8708E 00 \\
\hline 0.6739 E & 16 & 0.3400 & 01 & 0.1390 & 05 & 0.8708 O 0 \\
\hline 0.2044 E & 17 & 0.3400E & 01 & 0.1390 & 05 & 0.7769 O 0 \\
\hline \(0.1555 E\) & 17 & \(0.3400 E\) & 01 & 0.1390 & 05 & 0.7769E 00 \\
\hline 0.1167 E & 17 & 0.3400 E & 01 & 0.1390E & 05 & 0.7769E 00 \\
\hline \(0.6047 E\) & 16 & \(0.3400 E\) & 01 & 0.1390 & 05 & 0.7769500 \\
\hline 0.1549 E & 17 & 0.3400E & 01 & 0.13905 & 05 & \(0.5815 E 00\) \\
\hline 0.1178 E & 17 & 0.3400E & 01 & 0.1390E & 05 & \(0.5815 E 00\) \\
\hline \(0.8837 E\) & 16 & 0.3400E & 01 & O.1390E & 05 & \(0.5815 E 00\) \\
\hline \(0.4584 E\) & 16 & 0.34 00E & 1 & 0.1390E & 5 & .5815E \\
\hline
\end{tabular}
\(F 2\)
F3
F4
F 5
\begin{tabular}{|c|c|c|c|c|c|c|c|c|}
\hline \(0.1233 E\) & 06 & 0.1418 E & 17 & 0.3400E & 01 & 0.1390E & 05 & \(0.5308 E 00\) \\
\hline 0.1103 E & 06 & 0.1079E & 17 & 0.3400E & 01 & 0.1390E & 05 & \(0.5308 E 00\) \\
\hline \(0.9082 E\) & 05 & 0.8086E & 16 & 0.3400E & 01 & O. 1390 E & 05 & 0.5308 E 00 \\
\hline 0.5838E & 05 & \(0.4195 E\) & 16 & 0.3400E & 01 & \(0.1390 E\) & 05 & \(0.5308 E 00\) \\
\hline 0.2715 E & 06 & \(0.3500 E\) & 17 & 0.2762E & 01 & O.1710E & 05 & O.8950E 00 \\
\hline \(0.2475 E\) & 06 & \(0.2661 E\) & 17 & \(0.2762 E\) & 01 & 0.1710E & 05 & 0.3950E 00 \\
\hline \(0.2236 E\) & 06 & 0.1996E & 17 & \(0.2762 E\) & 01 & 0.1710E & 05 & 0.3950E 00 \\
\hline \(0.1756 E\) & 06 & 0.1035E & 17 & \(0.2762 E\) & 01 & 0.1710 E & 05 & 0.8950E 00 \\
\hline 0.1517 E & 06 & 0.7394E & 16 & \(0.2762 E\) & 01 & O.1710E & 05 & 0.3950 e 00 \\
\hline \(0.2555 E\) & 06 & 0.3219 E & 17 & 0.2762 F & 01 & 0.1710E & 05 & 0.8187E 00 \\
\hline -0.2236E & 06 & 0.2449 E & 17 & 0.2762E & 01 & 0.1710E & 05 & \(0.3187 E 00\) \\
\hline \(0.1996 E\) & 06 & 0.1837 E & 17 & \(0.2762 E\) & 01 & 0.1710E & 05 & \(0.8187 E 00\) \\
\hline 0.1517 E & 06 & 0.9522E & 16 & 0.2762E & 01 & O.1710E & 05 & \(0.8187 E 00\) \\
\hline \(0.1277 E\) & 06 & 0.6805E & 16 & 0.2762 E & 01 & O.1710E & 05 & \(0.3187 E 00\) \\
\hline 0.2236E & 06 & \(0.2625 E\) & 17 & \(0.2762 E\) & 01 & 0.1710E & 05 & 0.6600E 00 \\
\hline 0.1996 E & 06 & 0.1997E 1 & 17 & \(0.2762 E\) & 01 & 0.1710E & 05 & 0.6600E 00 \\
\hline 0.1677E & 06 & 0.1498E 1 & 17 & 0.2762E & 01 & 0.1710 E & 05 & 0.6600E 00 \\
\hline 0.1277E & 06 & 0.7769E 1 & 16 & 0.2762E & 01 & 0.1710E & 05 & 0.6600E 00 \\
\hline 0.1038 E & 06 & 0.5546E 1 & 16 & 0.2762 E & 01 & 0.1710E & 05 & 0.6600E 00 \\
\hline \(0.2076 E\) & 0 & \(2469 E\) & & . \(2762 E\) & 01 & 0.1710 E & 5 & .ó187E \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|c|c|c|c|c|c|}
\hline Obsv & F1 & F2 & & F3 & & F4 & & F5 \\
\hline 161 & 0.1916 OS & 0.1878 E & 17 & \(0.2762 E\) & 01 & 0.1710E & & \(0.5187 E 00\) \\
\hline 162 & \(0.1597 E 06\) & \(0.1409 E\) & 17 & \(0.2762 E\) & 01 & 0.1710E & 05 & \(0.6187 E 00\) \\
\hline 163 & 0.1198E 06 & 0.7299E & 16 & \(0.2762 E\) & 01 & 0.1710E & 05 & \(0.6187 E 00\) \\
\hline 164 & 0.9581E 05 & \(0.5219 E\) & 16 & \(0.2762 E\) & 01 & 0.1710 E & 05 & \(0.6187 E 00\) \\
\hline 165 & 0.1916 E O6 & \(0.1984 E\) & 17 & 0.2762 E & 01 & 0.1710E & 05 & 0.4925E 00 \\
\hline 166 & 0.1756 E & 0.1509E & 17 & \(0.2762 E\) & 01 & 0.1710E & 05 & \(0.4925 E 00\) \\
\hline 167 & 0.1517E 06 & 0.1131 E & 17 & \(0.2762 E\) & 01 & 0.1710E & 05 & 0.4925E 00 \\
\hline 168 & 0.1118 C 06 & \(0.5864 E\) & 16 & 0.2762E & 01 & O.1710E & 05 & \(0.4925 E 00\) \\
\hline 169 & 0.8782 E & \(0.4191 E\) & 16 & 0.2762E & 01 & 0.17105 & 05 & 0.4925E 00 \\
\hline 170 & \(0.3792 E 06\) & 0.4959E & 17 & 0.2326E & 01 & 0.2031E & 05 & 0.9116 E 00 \\
\hline 171 & 0.3413 E 06 & 0.3772 E & 17 & 0.2326E & 01 & 0.2031 E & 05 & 0.9116 E 00 \\
\hline 172 & 0.3129 E 06 & \(0.2828 E\) & 17 & 0.2326E & 01 & 0.2031 E & 05 & 0.9116E 00 \\
\hline 173 & 0.2560E 06 & \(0.1467 E\) & 17 & \(0.2326 E\) & 01 & 0.2031 E & 05 & 0.9116E 00 \\
\hline 174 & 0.2275E 06 & 0.1047E & 17 & 0.2326E & 01 & \(0.2031 E\) & 05 & 0.9116E 00 \\
\hline 175 & 0.3318 E 06 & 0.4635E & 17 & \(0.2326 E\) & 01 & \(0.2031 E\) & 05 & 0.8474 E 00 \\
\hline 176 & 0.3081E 06 & \(0.3526 E\) & 17 & \(0.2326 E\) & 01 & \(0.2031 E\) & 05 & 0.8474E 00 \\
\hline 177 & \(0.2655 E 06\) & 0.2644E & 17 & 0.2326E & 01 & 0.2031E & 05 & \(0.8474 E 00\) \\
\hline 178 & 0.2181E 06 & 0.1371 E & 17 & 0.2326E & 01 & 0.2031 E & 05 & 0.3474 E 00 \\
\hline 179 & \(0.1991 E 06\) & 0.9793E & 16 & 0.2326E & 01 & 0.2031E & & \(0.8474 E 00\) \\
\hline 180 & \(0.3129 E 06\) & \(0.3932 E\) & 17 & \(0.2326 E\) & & 0.2031 E & 05 & 0.7105E OD \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|}
\hline OBSv & F1 & F2 & & F3 & & F4 & & Fs & \\
\hline 181 & 0.2844E 06 & \(0.2991 E\) & 17 & 0.2326E & 01 & \(0.2031 E\) & 05 & 0.7105E & 00 \\
\hline 182 & \(0.2465 E 06\) & \(0.2243 E\) & 17 & 0. 2326 E & 01 & 0.2031 E & 05 & \(0.7105 E\) & 00 \\
\hline 183 & 0.1991 O 06 & 0.1163 E & 17 & \(0.2326 E\) & 01 & 0.2031 E & 05 & 0.7105 E & 00 \\
\hline 184 & 0.1659E 06 & \(0.8308 E\) & 16 & \(0.2326 E\) & 01 & 0.2031 E & 05 & 0.7105E & co \\
\hline 185 & 0.2987E 06 & 0.3768 E & 17 & \(0.2326 E\) & 01 & O.2031E & 05 & 0.67895 & 00 \\
\hline 186 & 0.2655e Oó & 0.2866 E & 17 & 0.2326E & 01 & 0.2031 E & 05 & 0.678 PE & 00 \\
\hline 187 & \(0.2275 E 06\) & \(0.2150 E\) & 17 & \(0.2326 E\) & 01 & 0.2031 E & 05 & \(0.6789 E\) & 00 \\
\hline 188 & 0.1849 E 06 & 0.1115 E & 17 & \(0.2326 E\) & 0.1 & \(0.2031 E\) & 05 & 0.6789E & 00 \\
\hline 189 & 0.1517E 06 & 0.7958E & 16 & \(0.2326 E\) & 01 & 0.2031 E & 05 & 0.6789E & 00 \\
\hline 190 & 0.2749E 06 & \(0.3208 E\) & 17 & 0.2326E & 01 & \(0.2031 E\) & 05 & \(0.5726 E\) & 00 \\
\hline 191 & 0.2465E 06 & \(0.2439 E\) & 17 & 0.2326E & 01 & \(0.2031 E\) & 05 & 0.5726E & 00 \\
\hline 192 & \(0.2181 E 06\) & \(0.1830 E\) & 17 & 0.2326E & 01 & \(0.2031 E\) & 05 & 0.5726E & 00 \\
\hline 193 & 0.1707E 06 & 0.9490 E & 16 & 0.2326E & 01 & \(0.2031 E\) & 05 & \(0.5726 E\) & 00 \\
\hline 194 & 0.1422E 06 & 0.6775E & 16 & 0.2326E & 01 & \(0.2031 E\) & 05 & 0.5726E & 00 \\
\hline 195 & \(0.2465 E 06\) & 0.2773E & 17 & 0.2326E & 01 & \(0.2031 E\) & 05 & 0.4916 E & 00 \\
\hline 196 & 0.2275E 06 & \(0.2109 E\) & 17 & 0.2326E & 01 & \(0.2031 E\) & 05 & \(0.4916 E\) & 00 \\
\hline 197 & 0.1991 E 06 & 0.1582E & 17 & 0.2326E & 01 & 0.2031E & 05 & \(0.4916 E\) & 00 \\
\hline 198 & 0.1612 O & 0.8204 E & 16 & \(0.2326 E\) & 01 & \(0.2031 E\) & 05 & 0.4916 E & 00 \\
\hline 199 & 0.1327E 06 & 0.5857E & 16 & 0. 2326 E & 01 & 0.2031E & 05 & 0.4916 E & 00 \\
\hline 200 & 0.4940 E 06 & 0.6647 E & 17 & 0.2009E & 01 & \(0.2352 E\) & 05 & \(0.9236 E\) & 00 \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|c|}
\hline OBSV & F1 & & F2 & & F3 & & F4 & & F5 & \\
\hline 201 & \(0.4611 E\) & 06 & 0.5055E & 17 & 0.2009E & 01 & \(0.2352 E\) & 05 & \(0.9236 E\) & 00 \\
\hline 202 & 0.4172 E & 06 & 0.3792 E & 17 & 0.2009E & 01 & \(0.2352 E\) & 05 & 0.9236 E & 00 \\
\hline 203 & \(0.3513 E\) & 06 & 0.1966 E & 17 & 0.2009E & 01 & 0.2352E & 05 & 0.9236E & 00 \\
\hline 204 & \(0.3293 E\) & 06 & \(0.1405 E\) & 17 & \(0.2009 E\) & 01 & 0.2352E & 05 & 0.9236E & 00 \\
\hline 205 & 0.4611 E & 06 & \(0.6281 E\) & 17 & \(0.2009 E\) & 01 & \(0.2352 E\) & 05 & 0.8682 E & 00 \\
\hline 206 & \(0.4281 E\) & 06 & 0.4778E & 17 & 0.2009 E & 01 & \(0.2352 E\) & 05 & 0.8682E & 00 \\
\hline 207 & \(0.3952 E\) & 06 & 0.3583E & 17 & 0.2009E & 01 & \(0.2352 E\) & 05 & 0.8682E & 00 \\
\hline 208 & \(0.3293 E\) & 06 & 0.1858 E & 17 & 0.2009E & 01 & 0.2352E & 05 & 0.8682E & 00 \\
\hline 209 & 0.3074 E & 06 & 0.1327E & 17 & 0. 2009 E & 01 & 0.2352E & 05 & \(0.8682 E\) & 00 \\
\hline 210 & 0.4281E & 06 & 0.5509E & 17 & 0.2009 E & 01 & 0.2352E & 05 & 0.7527E & 00 \\
\hline 211 & 0.3952E & 06 & 0.4190 E & 17 & 0.2009E & 01 & 0.2352E & 05 & 0.7527E & 00 \\
\hline 212 & \(0.3513 E\) & 06 & 0.3142 E & 17 & 0.2009E & 01 & 0.2352E & 05 & 0.7527E & 00 \\
\hline 213 & 0.2744E & 06 & 0.1629E & 17 & 0.2009E & 01 & \(0.2352 E\) & 05 & 0.7527E & 00 \\
\hline 214 & 0.2525E & 06 & \(0.1164 E\) & 17 & \(0.2009 E\) & 01 & 0.2352E & 05 & 0.7527E & 00 \\
\hline 215 & \(0.3952 E\) & 06 & \(0.5305 E\) & 17 & 0.2009E & 01 & 0.2352E & 05 & 0.7227E & 00 \\
\hline 216 & \(0.3623 E\) & 06 & \(0.4035 E\) & 17 & 0.2009E & 01 & \(0.2352 E\) & 05 & 0.7227E & 00 \\
\hline 217 & 0.3293 E & 06 & 0.3026E & 17 & 0. 2009 E & 01 & 0.2352E & 05 & 0.7227E & 00 \\
\hline 218 & \(0.2635 E\) & 06 & 0.1569E & 17 & 0.2009E & 01 & 0.2352E & 05 & 0.7227E & 00 \\
\hline 219 & \(0.2415 E\) & 06 & \(0.1121 E\) & 17 & 0.2009E & 01 & \(0.2352 E\) & 05 & \(0.7227 E\) & 00 \\
\hline 220 & \(0.3733 E\) & 06 & 0.4674 E & 17 & 0.2009E & 01 & 0.2352E & 05 & 0.6309 E & 00 \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|}
\hline Obsy & F1 & & F2 & & F3 & & F4 & & F5 \\
\hline 221 & 0.3513 E & 06 & 0.3554 E & 17 & 0.2009 E & 01 & \(0.2352 E\) & 05 & 0.6309 E \\
\hline 222 & \(0.3184 E\) & 06 & \(0.2666 E\) & 17 & 0.2009E & 01 & \(0.2352 E\) & 05 & 0.6309 E \\
\hline 223 & \(0.2415 E\) & 06 & 0.1383E & 17 & 0.2009E & 01 & 0-2352E & 05 & 0.6309E \\
\hline 224 & 0.2196 E & 06 & 0.9871E & 16 & 0.2009E & 01 & O.2352E & 05 & 0.6309 E \\
\hline 225 & \(0.3513 E\) & 06 & \(0.4185 E\) & 17 & 0.2009E & 0.1 & \(0.2352 E\) & 05 & 0.5609E \\
\hline 226 & \(0.3293 E\) & 06 & 0.3183 E & 17 & 0.2009E & 02 & 0.2352E & 05 & \(0.5509 E\) \\
\hline 227 & 0.3074 E & 06 & 0.2387E & 17 & \(0.2009 E\) & 01 & 0.2352E & 05 & \(0.5609 E\) \\
\hline 228 & 0.2305E & 06 & 0.1238E & 17 & 0.2009E & 01 & 0.2352E & 05 & \(0.5609 E\) \\
\hline 229 & 0.2086E & 06 & 0.8842E & 16 & 0.2009E & 01 & \(0.2352 E\) & 05 & 0.5609E \\
\hline 230 & \(0.3293 E\) & 06 & \(0.3694 E\) & 17 & 0.2009E & 01 & \(0.2352 E\) & 05 & 0.4918 O \\
\hline 231 & 0.3074 E & 06 & 0.2810 E & 17 & 0.2009E & 01 & 0.2352E & 05 & 0.4918 E \\
\hline 232 & \(0.2854 E\) & 06 & 0.2108 E & 17 & 0.2009E & 01 & 0.2352E & 05 & 0.4918 E \\
\hline 233 & \(0.2196 E\) & 06 & 0.1092 E & 17 & 0.2009E & 01 & \(0.2352 E\) & 05 & 0.4913 E \\
\hline 234 & \(0.1976 E\) & 06 & 0.7801 E & 16 & 0.2009E & 01 & 0.2352E & 05 & 0.4913 O \\
\hline 235 & 0.8982 E & 05 & \(0.1306 E\) & 17 & 0.3960E & 01 & 0.1069E & '0s & 0.3320E O \\
\hline 236 & 0.7984 E & 05 & \(0.9935 E\) & 16 & 0.3960E & 01 & 0.1069E & 05 & 0.8320: 0 \\
\hline 237 & 0.6986 E & 05 & 0.7450E & 16 & 0.3960E & 01 & 0.1069E & 05 & \(0.8320 E^{\circ}\) \\
\hline 238 & 0.4241E & & \(0.3864 E\) & & 0.3960E & 01 & \(0.1069 E\) & & 0.8320E O \\
\hline 239 & 0.8733 E & 05 & \(0.1121 E\) & 17 & 0.3960E & 01 & 0.1069E & 05 & 0.7100E OO \\
\hline 240 & \(0.7485 E\) & 05 & 0.8526E & 16 & \(0.3960 E\) & 01 & 0.1069E & 05 & 0.71 OOE OO \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|c|c|c|c|c|c|}
\hline 08sv & F1 & F2 & & F3 & & F4 & & F5 \\
\hline 241 & \(0.6736 E 05\) & 0.6394 E & 16 & 0.3960E & 01 & 0.1069 E & 05 & 0.7100E OD \\
\hline 242 & 0.3992 E & 0.3316 E & 16 & 0.3960E & 01 & 0.1069E & 05 & 0.7100E 00 \\
\hline 243 & \(0.8234 E 05\) & 0.7286E & 16 & \(0.3960 E\) & 01 & 0.1069E & 05 & 0.4560 E 00 \\
\hline 244 & \(0.7235 E 05\) & 0.5543E & 16 & 0.3960E & 01 & 0.1069E & 05 & 0.4560E 00 \\
\hline 245 & \(0.6487 E 05\) & 0.4157E & 16 & 0.3960 E & 01 & 0.1069E & 05 & O.4560E 00 \\
\hline 246 & 0.2011E 06 & 0.2278 E & 17 & 0.3046E & 01 & 0.1390E & 05 & 0.8708 E 00 \\
\hline 247 & \(0.1816 E 06\) & 0.1733 E & 17 & 0.3046 E & 01 & 0.1390E & 05 & 0.8708E 00 \\
\hline 248 & \(0.1557 E 06\) & 0. 1300 E & 17 & \(0.3046 E\) & 01 & O.1390E & 05 & 0.3708E 00 \\
\hline 249 & 0.1168 E 06 & 0.6739 E & 16 & 0.3046E & 01 & 0.1390 E & 05 & 0.8708 O \\
\hline 250 & 0.1816 E6 & 0.2044 E & 17 & 0.3046E & 01 & 0.1390E & 05 & 0.7769 E 00 \\
\hline 251 & \(0.1622 E 06\) & 0.1555E & 17 & 0.3046E & 01 & 0.1390E & 05 & 0.7769E 00 \\
\hline 252 & 0.1427E 06 & \(0.1167 E\) & 17 & 0.3046E & 01 & 0.1390 E & 05 & \(0.7769 E 00\) \\
\hline 253 & \(0.1038 E 06\) & \(0.6047 E\) & 16 & 0.3046E & 01 & 0.1390E & 05 & 0.7769E 00 \\
\hline 254 & 0.1460 E 06 & 0.1549E & 17 & 0.3046E & 01 & 0.1390E & 05 & 0.5815E 00 \\
\hline 255 & \(0.1233 E 06\) & 0.1178 E & 17 & \(0.3046 E\) & 01 & 0.1390E & 05 & 0.5815E 00 \\
\hline 256 & 0.1103 E 06 & 0.8837E & 16 & 0.3046E & 01 & O.1390E & 05 & 0.5815E. 00 \\
\hline 257 & 0.9082 E 05 & 0.4584 E & 16 & 0.3046E & 01 & 0.1390E & 05 & 0.5815E 00 \\
\hline 258 & 0.1297E 06 & 0.1418 E & 17 & \(0.3046 E\) & 01 & 0.1390E & 05 & \(0.5308 E 00\) \\
\hline 259 & 0.1168 E 06 & 0.1079E & 17 & 0.3046 E & 01 & 0.1390E & 05 & O.5308E 00 \\
\hline 260 & 0.1038 E 06 & 0.8086 E & 16 & \(0.3046 E\) & 01 & 0.1390E & & 0.530.3E 00 \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|c|}
\hline OBSV & F 1 & & \(F 2\) & & F3 & & F4 & & F5 & \\
\hline 261 & \(0.7136 E\) & 05 & \(0.4195 E\) & 16 & \(0.3046 E\) & 01 & O.1390E & 05 & \(0.5303 E\) & 00 \\
\hline 262 & \(0.2874 E\) & 06 & \(0.3500 E\) & 17 & \(0.2475 E\) & 01 & 0.1710 E & 05 & 0.8950E & 00 \\
\hline 263 & \(0.2555 E\) & 06 & 0.2661E & 17 & 0.2475E & 01 & \(0.1710 E\) & 05 & O.8950E & 00 \\
\hline . 264 & \(0.2395 E\) & 06 & O.1996E & 17 & \(0.2475 E\) & 01 & \(0.1710 E\) & 05 & 0.8950E & 00 \\
\hline 265 & \(0.1916 E\) & 06 & 0.1035E & 17 & 0. 2475 E & 01 & \(0.1710 E\) & 05 & \(0.8950 E\) & 00 \\
\hline 266 & 0.1597E & 06 & 0.7394 E & 16 & 0.2475E & 01 & \(0.1710 E\) & 05 & 0.8950E & 00 \\
\hline 267 & \(0.2715 E\) & 06 & \(0.3219 E\) & 17 & \(0.2475 E\) & 01 & \(0.1710 E\) & 05 & \(0.8187 E\) & 00 \\
\hline 268 & \(0.2395 E\) & 06 & \(0.2449 E\) & 17 & \(0.2475 E\) & 01 & \(0.1710 E\) & 05 & 0.8187 E & 00 \\
\hline 269 & 0.2236E & 06 & 0.1837E & 17 & \(0.2475 E\) & 01 & O-1710E & 05 & \(0.8187 E\) & 00 \\
\hline 270 & \(0.1756 E\) & 06 & 0.9522E & 16 & 0.2475E & 01 & O.1710E & 05 & \(0.8187 E\) & 00 \\
\hline 271 & 0.1437E & 06 & \(0.6805 E\) & 16 & 0.2475E & 01 & O.1710E & 05 & \(0.8187 E\) & 00 \\
\hline 272 & \(0.2555 E\) & 06 & -0.2625E & 17 & \(0.2475 E\) & 01 & O-1710E & 05 & 0.6600E & 00 \\
\hline 273 & \(0.2315 E\) & 06. & D. \(1997 E\) & 17 & \(0.2475 E\) & 01 & \(0.1710 E\) & 05 & 0.6600E & 00 \\
\hline 274 & 0.2156 E & 06 & 0.1498E & 17 & \(0.2475 E\) & 01 & O. 1710 E & 05 & 0.6600E & 00 \\
\hline 275 & 0.1677E & 06 & \(0.7769 E\) & 16 & 0.2475E & 01 & \(0.1710 E\) & 05 & 0.6600E & 00 \\
\hline 276 & \(0.1357 E\) & 06 & \(0.5546 E\) & 16 & \(0.2475 E\) & 01 & 0.1710 E & 05 & 0.6600E & 00 \\
\hline 277 & \(0.2395 E\) & 06 & \(0.2469 E\) & 17 & \(0.2475 E\) & 01 & 0.1710 E & 05 & 0.6187 E & 00 \\
\hline 278 & \(0.2236 E\) & 06 & 0.1878E & 17 & \(0.2475 E\) & 01 & 0.1710 E & 05 & \(0.6187 E\) & 00 \\
\hline 279 & 0.1996E & 06 & \(0.1409 E\) & 17 & 0.2475E & 01 & \(0.1710 E\) & 05 & \(0.6187 E\) & 00 \\
\hline 280 & 0.1597E & 06 & 0.7299E & 16 & \(0.2475 E\) & 01 & O.1710E & 05 & \(0.6187 E\) & 00 \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|}
\hline Obsv & F1 & & F2 & & F3 & & F4 & & FS \\
\hline 281 & 0.1277 E & 06 & 0.5219 E & 16 & \(0.2475 E\) & 01 & 0.1710E & 05 & 0.6187E 00 \\
\hline 282 & 0.2236 E & 06 & 0.1984E & 17 & 0.2475E & 01 & 0.1710E & 05 & \(0.4925 E 00\) \\
\hline 283 & \(0.2076 E\) & 06 & 0.1509E & 17 & \(0.2475 E\) & 01 & 0.1710E & 05 & 0.4925E 00 \\
\hline 284 & \(0.1916 E\) & 06 & 0.1131 E & 17 & 0.2475E & 01 & 0.1710E & 05 & 0.4925 E 00 \\
\hline 285 & 0.1437E & 06 & \(0.5864 E\) & 16 & \(0.2475 E\) & 01 & 0.1710E & 05 & \(0.4925 E 00\) \\
\hline 286 & 0.1118 E & 06 & 0.4191 E & 16 & \(0.2475 E\) & 01 & O.1710E & 05 & \(0.4925 E 00\) \\
\hline 287 & 0.3887E & 06 & 0.4959E & 17 & 0.2084E & 01 & O.2031E & 05 & 0.9116E 00 \\
\hline 288 & 0.3508 E & 06 & \(0.3772 E\) & 17 & 0.2034 E & 01 & \(0.2031 E\) & 05 & 0.9116 E 00 \\
\hline 289 & \(0.3224 E\) & 06 & 0.2828E & 17 & 0.2084E & 01 & \(0.2031 E\) & 05 & 0.9116 E 00 \\
\hline 290 & 0.2749 E & 06 & \(0.1467 E\) & 17 & 0.2084E & 01 & 0.2031 E & 05 & 0.911 GE OO \\
\hline 291 & \(0.2465 E\) & 06 & \(0.1047 E\) & 17 & 0.2084E & 01 & \(0.2031 E\) & 05 & 0.9116 E 00 \\
\hline 292 & 0.3413 E & 06 & \(0.4635 E\) & 17 & \(0.2084 E\) & 01 & \(0.2031 E\) & 05 & 0.8474E.00 \\
\hline 293 & \(0.3129 E\) & 06 & 0.3526E & 17 & 0.2084E & 01 & 0.2031E & 05 & 0.8474E 00 \\
\hline 294 & 0.2844 E & 06 & \(0.2644 E\) & 17 & 0.2084E & 01 & \(0.2031 E\) & 05 & 0.3474 E 00 \\
\hline 295 & 0.2370E O & 06 & 0.1371 E & 17 & 0.2084E & 01 & 0.2031E & 05 & 0.8474 E 00 \\
\hline 296 & 0.2181 E & 06 & \(0.9793 E\) & 16 & 0.2084E & 01 & 0.2031 E & 05 & 0.8474 E 00 \\
\hline 297 & \(0.3224 E\) & 06 & \(0.3932 E\) & 17 & 0.2084 E & 01 & \(0.2031 E\) & 05 & \(0.7105 E 00\) \\
\hline 298 & \(0.2939 E\) & 06 & \(0.2991 E\) & 17 & 0.2084E & 01 & 0.2031 E & 05 & \(0.7105 E 00\) \\
\hline 299 & 0.2655E O & 06 & 0.2243E & 17 & 0.2084E & 01 & \(0.2031 E\) & 05 & 0.7105E 00 \\
\hline 300 & 0.2086 E & 06 & 0.1163 E & 17 & 0.2084E & 01 & \(0.2031 E\) & 05 & \(0.7105 E 00\) \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|}
\hline OBsy & F 1 & & F2 & & F3 & & F4 & & F5 \\
\hline 301 & \(0.1896 E\) & 06 & 0.8308 E & 16 & 0.2084 E & 01 & 0.2031 E & & \(0.7105 E 00\) \\
\hline 302 & 0.3034E & 06 & \(0.3768 E\) & 17 & 0.2084 E & 01 & 0.2031 E & & 0.6789 E 0 \\
\hline 303 & 0.2844E & 06 & 0.2866E & 17 & 0.2084 E & 01 & 0.2031E & 05 & 0.5789E 00 \\
\hline 304 & 0.2560E & 06 & \(0.2150 E\) & 17 & 0.2084 E & 01 & \(0.2031 E\) & 05 & 0.6789E 00 \\
\hline 305 & \(0.1991 E\) & 06 & \(0.1115 E\) & 17 & 0. 2084 E & 01 & 0.2031E & 05 & 0.6789E 00 \\
\hline 306 & 0.1801E & 06 & 0.7958E & 16 & \(0.2084 E\) & 01 & 0.2031E & 05 & 0.6789 EO \\
\hline 307 & 0.2892 E & 06 & 0.32085 & 17 & 0.2084E & 01 & 0.2031 E & 05 & 0.5726E 00 \\
\hline 308 & 0.2655E & 06 & \(0.2439 E\) & 17 & 0.2084E & 01 & \(0.2031 E\) & 05 & 0.5720E 00 \\
\hline 309 & 0.2465E & 06 & 0.1830E & 17 & 0. 2084 E & 01 & 0.2031E & 05 & \(0.5726 E 00\) \\
\hline 310 & \(0.1801 E\) & 06 & \(0.9490 E\) & 16 & 0.2084 E & 01 & 0.2031 E & 05 & 0.5726E 00 \\
\hline 311 & \(0.1612 E\) & 06 & 0.6775 E & 16 & 0.2084 E & 01 & \(0.2031 E\) & 05 & 0.5726E CO \\
\hline 312 & \(0.2655 E\) & 06 & 0.2773 E & 17 & \(0.2084 E\) & 01 & 0.2031 E & 05 & . 0.4916 E 00 \\
\hline 313 & \(0.2465 E\) & 06 & \(0.2109 E\) & 17 & 0.2084E & 01 & 0.2031 E & 05 & 0.4916 E 00 \\
\hline 314 & \(0.2275 E\) & 06 & 0.1582E & 17 & 0.2084 E & 01 & \(0.2031 E\) & 05 & 0.4916E 00 \\
\hline 315 & \(0.1707 E\) & 06 & 0.8204 E & 16 & 0.2084E & 01 & \(0.2031 E\) & 05 & 0.4916 E 00 \\
\hline 316 & \(0.1517 E\) & 06 & 0.5857E & 16 & 0.2084E & 01 & 0.2031 E & 05 & \(0.4916 E 00\) \\
\hline 317 & 0.5160E & 06 & 0.6647E & 17 & 0. 1800 E & 01 & \(0.2352 E\) & 05 & 0.9236500 \\
\hline 318 & \(0.4940 E\) & 06 & 0.5055E & 17 & 0.1800E & 01 & \(0.2352 E\) & 05 & 0.9236 E 00 \\
\hline 319 & 0.4611 E & 06 & 0.3792E & 17 & 0.1800E & 01 & \(0.2352 E\) & & 0.9236 E 00 \\
\hline 320 & 0.3952 E & 06 & 0.1966 E & 17 & 0.1800E & 01 & \(0.2352 E\) & & 0.9236 E 00 \\
\hline
\end{tabular}

F5
\begin{tabular}{|c|c|c|c|c|c|c|c|c|}
\hline \(0.3623 E\) & 06 & 0.1405 E & 17 & 0.1800E & 01 & 0.2352E & 05 & \(0.9236 E 00\) \\
\hline 0.494 OE & 06 & 0.6281 E & 17 & 0.1800E & 01 & \(0.2352 E\) & 05 & 0.8682 E 00 \\
\hline 0.4611E & 06 & 0.4778 E & 17 & 0.1800E & 01 & 0.2352E & 05 & 0.8682 E 00 \\
\hline \(0.4281 E\) & 06 & \(0.3583 E\) & 17 & 0.1800E & \[
01
\] & \(0.2352 E\) & 05 & 0.8682 E 00 \\
\hline 0.3513 E & 06 & 0.1858E & 17 & 0.1800E & 01 & 0.2352E & 05 & 0.8682 E OO \\
\hline \(0.3293 E\) & 06 & 0.1327E & 17 & 0.1800E & 01 & 0.2352E & 05 & 0.8682 EO \\
\hline 0.4611 E & 06 & 0.5509E & 17 & 0.1800E & 01 & \(0.2352 E\) & 05 & 0.7527E OO \\
\hline 0.4391 E & 06 & 0.4190 E & 17 & 0.1800E & 01. & \(0.2352 E\) & 05 & 0.7527E 00 \\
\hline 0.4062 E & . 06 & 0.3142 E & 17 & 0.1800E & 01 & 0.2352 E & 05 & 0.7527E 00 \\
\hline \(0.3293 E\) & 06 & 0.1629E & 17 & 0.1800E & 01 & 0.2352 E & 05 & 0.7527E 00 \\
\hline 0.3074 E & 06 & \(0.1164 E\) & 17 & 0.1800E & 01 & 0.2352 E & 05 & 0.7527E 00 \\
\hline 0.4501E & 06 & \(0.5305 E\) & 17 & 0.1800E & 01 & \(0.2352 E\) & 05 & 0.7227E 00 \\
\hline 0.4281 E & 06 & \(0.4035 E\) & 17 & 0.1800E & 01 & \(0.2352 E\) & 05 & 0.7227E 00 \\
\hline \(0.3952 E\) & 06 & 0.3026E & 17 & 0.1800E & 01 & \(0.2352 E\) & 05 & 0.7227E 00 \\
\hline 0.3184 E & 06 & 0.1569E & 17 & 0.1800E & 01 & \(0.2352 E\) & 05 & 0.7227E 00 \\
\hline 0.2964E & 06 & 0.1121E & 17 & 0.1800E & 01 & \(0.2352 E\) & 05 & \(0.7227 E 00\) \\
\hline 0.4281E & 06 & 0.4674 E & 17 & 0.1800E & 01 & 0.2352 E & 05 & 0.6309 E 00 \\
\hline 0.3952E & 06 & 0.3554 E & 17 & 0.1800E & 01 & \(0.2352 E\) & 05 & 0.6309 E 00 \\
\hline \(0.3623 E\) & 06 & 0.2666E & 17 & 0.1800E & 01 & 0.2352 E & 05 & 0.6309 E 00 \\
\hline 0.2854E & 06 & 0.1383E & 17 & 0.1800E & 01 & 0.2352E & 5 & 0.6309 O \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|c|}
\hline OBSV & F1 & & F2 & & \(F 3\) & & F4 & & F5 & \\
\hline 341 & 0.2635E & 06 & 0.9871E & 16 & 0.1800E & 01 & 0.2352 E & 05 & 0.5309 E & 0.5 \\
\hline 342 & 0.3952 E & 06 & \(0.4185 E\) & 17 & \(0.1800 E\) & 01 & \(0.2352 E\) & 05 & \(0.5609 E\) & 00 \\
\hline 343 & \(0.3733 E\) & 06 & \(0.3183 E\) & 17 & 0.1800E & 01 & 0.2352E & 05 & \(0.5609 E\) & 00 \\
\hline 344 & 0.3403 E & 06 & \(0.2387 E\) & 17 & 0.1800E & 01 & 0.2352E & 05 & \(0.5609 E\) & 00 \\
\hline 345 & 0.2744E & 06 & \(0.1238 E\) & 17 & O. 1800 E & 01 & 0.2352E & 05 & 0.50゙09E & 00 \\
\hline 346 & 0.2525E & 06 & \(0.8842 E\) & 16 & O. 1800 E & 01 & 0.2352E & 05 & 0.56092 & 00 \\
\hline 347 & \(0.3733 E\) & 06 & \(0.3694 E\) & 17 & 0.1800E & 01 & 0.2352 c & 05 & 0.4918 E & 00 \\
\hline 348 & \(0.3513 E\) & 06 & O. 281 OE & 17 & O.1800E & 01 & 0.2352E & 05 & 0.4918 E & 00 \\
\hline 349 & \(0.3184 E\) & 06 & \(0.2108 E\) & 17 & O.1800E & 01 & O-2352E & 05 & \(0.4918 E\) & 00 \\
\hline 350 & 0.2525E & 06 & 0.1092E & 17 & 0.1800E & 01 & 0.2352E & 05 & 0.49135 & 00 \\
\hline 351 & \(0.2305 E\) & 06 & 0.7801E & 16 & O. 1800 E & 01 & 0.2352E & 05 & \(0.4918 E\) & 00 \\
\hline 352 & 0.1048E & 06 & 0.1306E & 17 & 0.3500E & 01 & 0.1069E & 05 & 0.8320E & 00 \\
\hline 353 & \(0.9481 E\) & 05 & \(0.9935 E\) & 16 & 0.3500E & 01 & 0.1069E & 05 & 0.8320E & 00 \\
\hline 354 & \(0.7235 E\) & 05 & \(0.7450 E\) & 16 & O.3500E & 01 & 0.1069E & 05 & \(0.3320 E\) & 00 \\
\hline 355 & 0.4491 E & 05 & \(0.3864 E\) & 16 & D.3500E & 01 & 0.1069E & 05 & \(0.8320 E\) & 00 \\
\hline 356 & \(0.9980 E\) & 05 & \(0.1121 E\) & 17 & 0.3500E & 01 & \(0.1069 E\) & 05 & 0.7100E & 00 \\
\hline 357 & 0.8982E & 05 & 0.8526E & 16 & 0.3500E & 01 & \(0.1069 E\) & 05 & \(0.7100 E\) & 00 \\
\hline 358 & \(0.6986 E\) & 05 & \(0.6394 E\) & 16 & O.3500E & 01 & 0.1069E & 05 & 0.7100E & 00 \\
\hline 359 & \(0.4241 E\) & 05 & \(0.3316 E\) & 16 & 0.350OE & 01 & 0.1069E & 05 & \(0.7100 E\) & 00 \\
\hline 360 & \(0.8982 E\) & 05 & 0.7286E & 16 & 0.3500E & 01 & 0.1069E & 05 & \(0.4560 E\) & 00 \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|}
\hline 0.7984 E & 05 & 0.5543 E & 16 & 0.3500E & 01 & \(0.1069 E\) & 05 & \(0.4560 E\) & 00 \\
\hline 0.6986E & 05 & \(0.4157 E\) & 16 & 0.3500E & 01 & 0.1069E & 05 & 0.4560 E & 00 \\
\hline \(0.2335 E\) & 06 & 0.2278E & 17 & 0.2692E & 01 & 0.1390E & 05 & 0.87 08E & 00 \\
\hline 0.2011 E & 06 & 0.1733 E & 17 & \(0.2692 E\) & 01 & 0.1390 E & 05 & \(0.3708 E\) & 00 \\
\hline 0.1751 E & 06 & 0.1300 E & 17 & 0.2692 E & 01 & 0.1390E & 05 & 0.8708E & 0 \\
\hline \(0.1362 E\) & 06 & 0.6739E & 16 & \(0.2692 E\) & 01 & 0.1390E & 05 & 0.8708 E & 00 \\
\hline 0.2108 E & 06 & 0.2044 E & 17 & 0.2692E & 01 & 0.1390E & 05 & 0.7769E & 00 \\
\hline 0.1687E & 06 & 0.1555E & 17 & 0.2692E & 01 & 0.1390 E & 05 & 0.7769E & 00 \\
\hline 0.1362E & 06 & 0.1167E & 17 & 0.2692 & 01 & 0.1390E & 05 & 0.7769E & 00 \\
\hline 0.1070E & 06 & 0.6047E & 16 & \(0.2692 E\) & 01 & 0.1390E & 05 & 0.7769E & 00 \\
\hline \(0.1816 E\) & 06 & \(0.1549 E\) & 17 & 0.2692 & 01 & 0.1390E & 05 & 0.5815E & 00 \\
\hline 0.1492 E & 06 & 0.1178 E & 17 & 0.2692 E & 01 & 0.1390 E & 05 & 0.5815E & 00 \\
\hline 0.1297E & 06 & 0.8837 E & 16 & 0.2692 E & 01 & 0.1390E & 05 & 0.5815E & 00 \\
\hline 0.1038 E & 06 & 0.4584 E & 16 & \(0.2692 E\) & 01 & 0.1390E & 05 & 0.5315E & 00 \\
\hline 0.1622E & 06 & 0.1418 E & 17 & \(0.2692 E\) & 01 & 0.1390E & 05 & 0.5308E & 00 \\
\hline 0.1427E & 06 & 0.1079 E & 17 & \(0.2692 E\) & 01 & 0.1390E & 05 & 0.5308 E & 0 \\
\hline \(0.1233 E\) & 06 & 0.8086 E & 16 & \(0.2692 E\) & 01 & 0.1390 E & 05 & 0.5308 E & 00 \\
\hline 0.9730 E & 05 & 0.4195 E & 16 & \(0.2692 E\) & 01 & 0.1390E & 05 & 0.5308 E & 00 \\
\hline 0.3194 E & 06 & 0.3500E & 17 & \(0.2187 E\) & 01 & 0.1710 E & 05 & 0.3950E & 00 \\
\hline \(0.2954 E\) & & . 2661 l & & 1 & 01 & 0.1710E & 05 & 0.8950E & \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|}
\hline Onsv & F 1 & & F2 & & F3 & & F4 & & F5 \\
\hline 381 & \(0.2715 E\) & 06 & \(0.1996 E\) & 17 & \(0.2187 E\) & 01 & O. 1710 D & 05 & 0.8950E 00 \\
\hline 382 & 0.2236E & 06 & 0.1035E & 17 & \(0.2187 E\) & 01 & O.1710E & 05 & 0.8950E 00 \\
\hline 383 & 0.1916 E & 06 & 0.7394 E & 16 & 0.2187E & 01 & 0.1710E & 05 & 0.8950E 00 \\
\hline 384 & \(0.3034 E\) & 06 & \(0.3219 E\) & 17 & \(0.2187 E\) & 01 & O.1710E & 05 & \(0.8187 E 00\) \\
\hline 385 & \(0.2794 E\) & 06 & \(0.2449 E\) & 17 & 0.2187 E & 01 & 0.1710 E & 05 & \(0.8187 E 00\) \\
\hline 386 & \(0.2475 E\) & 06 & 0.1837E & 17 & 0.2187 E & 01 & 0.1710 E & 05 & 0.8187 E OU \\
\hline 3 a & \(0.1996 E\) & 06 & 0.9522E & 16 & 0.2187 E & 01 & 0.1710E & 05 & 0.8187 E 00 \\
\hline 388 & 0.1756 E & 06 & 0.6805E & 16 & \(0.2187 E\) & 01 & 0.1710 E & 05 & \(0.8187 E 00\) \\
\hline 389 & \(0.2914 E\) & 06 & \(0.2625 E\) & 17 & 0.2187E & 01 & 0.1710E & 05 & 0.6600E 00 \\
\hline 390 & 0.2715 E & 06 & \(0.1997 E\) & 17 & \(0.2187 E\) & 01 & 0.1710 E & 05 & 0.6600 E O \\
\hline 391 & \(0.2315 E\) & 06 & 0.1498E & 17 & 0.2187E & 01 & 0.1710 E & 05 & 0.6600E 00 \\
\hline 392 & 0.1916 E & 06 & 0.7769E & 16 & \(0.2187 E\) & 01 & 0.1710E & 05 & . 0.6600 E 00 \\
\hline 393 & \(0.1677 E\) & 06 & 0.5546E & 16 & \(0.2187 E\) & 01 & 0.1710E & 05 & 0.6600E 00 \\
\hline 394 & 0.2794 E & 06 & 0.2469E & 17 & \(0.2187 E\) & 01 & \(0.1710 E\) & 05 & \(0.6187 E 00\) \\
\hline 395 & 0.2555E & 06 & 0.1878E & 17 & \(0.2187 E\) & 01 & 0.1710 E & 05 & \(0.6187 E 00\) \\
\hline 396 & \(0.2236 E\) & 06 & 0.1409 E & 17 & \(0.2187 E\) & 01 & 0.1710E & 05 & 0.6137E OO \\
\hline 397 & \(0.1836 E\) & 06 & 0.7299E & 16 & \(0.2187 E\) & 01 & 0.1710 E & 05 & \(0.6137 E 00\) \\
\hline 398 & 0.1597E & 06 & 0.5219 E & 16 & \(0.2187 E\) & 01 & 0.1710E & 05 & \(0.6187 E 00\) \\
\hline 399 & 0.2635E & 06 & 0.1984 E & 17 & \(0.2187 E\) & 0.1 & 0.1710E & & 0.4925E 00 \\
\hline 400 & \(0.2315 E\) & 06 & 0.1509E & 17 & \(0.2187 E\) & 01 & 0.1710 E & & \(0.4925 E 00\) \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|c|c|c|c|c|c|}
\hline Obsv & \(F_{1}\) & F2 & & F3 & & F4 & & F5 \\
\hline 401 & 0.2076E 06 & 0.1131 E & 17 & \(0.2187 E\) & 01 & O.1710E & 05 & \(0.4925 E 00\) \\
\hline 402 & 0.1677E 06 & \(0.5864 E\) & 16 & \(0.2187 E\) & 01 & 0.1710 E & 05 & 0.4925500 \\
\hline 403 & 0.1517 E 06 & 0.4191 E & 16 & \(0.2187 E\) & 01 & 0.1710 E & 05 & \(0.4925 E 00\) \\
\hline 404 & 0.4172 E 06 & 0.4959E & 17 & 0.1842 E & 01 & \(0.2031 E\) & 05 & 0.9116 E 00 \\
\hline 405 & \(0.3887 E 06\) & 0.3772 E & 17 & 0.1842 E & 01 & 0.2031 E & 05 & 0.9116 E 00 \\
\hline 406 & \(0.3603 E 06\) & 0.2828E & 17 & 0.1842E & 01 & 0.2031 E & 05 & 0.9116 E 00 \\
\hline 407 & \(0.3034 E 06\) & 0.1467E & 17 & 0.1842E & 01 & 0.2031 E & 05 & 0.9116 E 00 \\
\hline 408 & \(0.2702 E 06\) & 0.1047E & 17 & 0.1842E & 01 & 0.2031E & 05 & \(0.9116 E 00\) \\
\hline 409 & \(0.3792 E 06\) & \(0.4635 E\) & 17 & 0.1842E & 01 & 0.2031 E & 0.5 & 0.8474 E 00 \\
\hline 410 & 0.3413 E 06 & \(0.3526 E\) & 17 & 0.1842E & 01 & \(0.2031 E\) & 05 & 0.8474 E 00 \\
\hline 411 & \(0.3129 E 06\) & 0.2644E & 17 & 0.1842 E & 01 & 0.2031 E & 05 & 0.8474 E 00 \\
\hline 412 & \(0.2655 E 06\) & 0.1371E & 17 & 0.1842E & 01 & 0.2031E & 05 & 0.8474 E 00 \\
\hline 413 & 0.2370 E 06 & 0.9793E & 16 & 0.1842E & 01 & 0.2031E & 05 & 0.8474 E 0 \\
\hline 414 & 0.3413 C & \(0.3932 E\) & 17 & 0.1842E & 01 & 0.2031E & 05 & 0.7105E 00 \\
\hline 415 & \(0.3129 E 06\) & 0.2991 E & 17 & \(0.1842 E\) & 01 & \(0.2031 E\) & 05 & 0.7105E 00 \\
\hline 416 & 0.2844 E & 0.2243 E & 17 & 0.1842E & 01 & \(0.2031 E\) & 05 & 0.7105 E 00 \\
\hline 417 & 0.2370E 06 & 0.1163 E & 17 & 0.1842 E & 01 & 0.2031 E & 05 & \(0.7105 E 00\) \\
\hline 418 & O.2181E 06 & 0.8308 E & 16 & 0.1842E & 01 & 0.2031 E & 05 & \(0.7105 E 00\) \\
\hline 419 & 0.3224E 06 & 0.3768E & 17 & 0.1842E & 01 & 0.2031E & 05 & 0.6789E 00 \\
\hline 420 & 0.3034E 06 & \(0.2866 E\) & 17 & 0.1842 E & 01 & \(0.2031 E\) & 05 & 0.6789 OO \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|}
\hline OBSV & F1 & & F2 & & F3 & & F4 & & F5 \\
\hline 421 & 0.2749E & 06 & 0.2150 E & 17 & 0.1842 E & 0.1 & O.2031E & 05 & \(0.6789 E 00\) \\
\hline 422 & 0.2275E & 06 & 0.1115E & 17 & 0.1842 E & 01 & 0.2031E & 05 & 0.6789 O \\
\hline 423 & 0.2086E & 06 & 0.7958E & 16 & 0.1842E & 01 & 0.2031 E & 05 & 0.6789 E 00 \\
\hline 424 & \(0.3034 E\) & 06 & 0.3208 E & 17 & 0.1842E & 01 & \(0.2031 E\) & 05 & \(0.5726 E 00\) \\
\hline 425 & 0.2844E & 06 & \(0.2439 E\) & 17 & 0.1842E & 01 & 0.2031 E & 05 & \(0.5726 E 00\) \\
\hline 426 & 0.2655E & 06 & \(0.1830 E\) & 17 & 0.1842 E & 01 & 0.2031E & 05 & \(0.5726 E 00\) \\
\hline 427 & \(0.2275 E\) & 06 & 0.9490E & 16 & 0.1842E & 01 & 0.2031 E & 05 & 0.5726E 00 \\
\hline 428 & 0.1991 E & 06 & \(0.6775 E\) & 16 & 0.1842E & 01 & 0.2031E & 05 & 0.5726E 00 \\
\hline 429 & 0.2939E & 06 & \(0.2773 E\) & 17 & 0.1842E & 01 & \(0.2031 E\) & 05 & 0.4916 E 00 \\
\hline 430 & 0.2749E & 06 & 0.2109E & 17 & 0.1842E & 01 & 0.2031E & 05 & 0.4916 E 00 \\
\hline 431 & 0.2512E & 06 & 0.1582E & 17 & 0.1842E & 01 & \(0.2031 E\) & 05 & 0.4916 E 00 \\
\hline 432 & 0.2181 E & 06 & 0.8204 E & 16 & 0.1842 E & 01 & \(0.2031 \equiv\) & 05 & 0.4916 E 00 \\
\hline 433 & 0.1896 E & 06 & \(0.5857 E\) & 16 & 0.1842 E & 01 & \(0.2031 E\) & 05 & 0.4916 E 00 \\
\hline 434 & \(0.5379 E\) & 06 & 0.6647E & 17 & 0.1591E & 01 & 0.2352 E & 05 & 0.9235E 00 \\
\hline 435 & 0.5050E & 06 & \(0.5055 E\) & 17 & 0.1591E & 01 & 0.2352E & 05 & 0.9236500 \\
\hline 436 & 0.4721 E & 06 & 0.3792E & 17 & 0.1591E & 01 & \(0.2352 E\) & 05 & 0.9236E 00 \\
\hline 437 & 0.4062E & 06 & \(0.1966 E\) & 17 & 0.1591E & 01 & 0.2352 E & 05 & \(0.9236 E 00\) \\
\hline 438 & 0.3842 E & 06 & 0.1405E & 17 & O. \(1591 E\) & 01 & 0.2352E & 05 & 0.9236E 00 \\
\hline 439 & 0.5050E & 06 & 0.6281E & 17 & 0.1591E & 01 & \(0.2352 E\) & & 0.8682E 00 \\
\hline 440 & 0.4830 E & 0 O & 0.4778 E & 17 & 0.1591E & 01 & \(0.2352 E\) & & 0.8682E 00 \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|c|}
\hline OBSV & F1 & & F2 & & F3 & & F4 & & F5 & \\
\hline 441 & 0.4501 E & 06 & \(0.3583 E\) & 17 & 0.1591E & 01 & \(0.2352 E\) & 05 & 0.8682 E & 00 \\
\hline 442 & 0.3733 E & 06 & 0.1858E & 17 & 0.1591E & 01 & 0.2352 E & 05 & \(0.8682 E\) & Do \\
\hline 443 & \(0.3513 E\) & 06 & \(0.1327 E\) & 17 & 0.1591E & 01 & 0.2352E & 05 & 0.8682E & 00 \\
\hline 444 & 0.4721 E & 06 & 0.5509E & 17 & 0.1591E & 01 & 0.2352E & 05 & 0.7527E & 00 \\
\hline 445 & 0.4501 E & 06 & 0.4190 E & 17 & 0.1591E & 01 & 0.2352E & 05 & 0.7527E & 00 \\
\hline 446 & ,0.4172E & 06 & 0.3142 E & 17 & \(0.1591 E\) & 01 & 0.2352E & 05 & 0.7527E & 00 \\
\hline 447 & \(0.3513 E\) & 06 & \(0.1629 E\) & 17 & 0.1591E & 01 & 0.2352 E & 05 & 0.7527E & 00 \\
\hline 448 & \(0.3293 E\) & 06 & 0.1164 E & 17 & 0.1591E & 01 & 0.2352E & 05 & 0.7527E & 00 \\
\hline 449 & \(0.4611 E\) & 06 & \(0.5305 E\) & 17 & 0.1591E & 01 & 0.2352E & 05 & \(0.7227 E\) & 00 \\
\hline 450 & O.4391E & 06 & 0.4035E & 17 & \(0.1591 E\) & 01 & \(0.2352 E\) & 05 & 0.7227E & 00 \\
\hline 451 & \(0.4062 E\) & 06 & \(0.3026 E\) & 17 & \(0.1591 E\) & 01 & 0.2352 E & 05 & 0.7227E & 00 \\
\hline 452 & \(0.3293 E\) & 06 & \(0.1569 E\) & 17 & 0.1591E & 01 & 0.2352 E & 05 & 0.7227E & 00 \\
\hline 453 & 0.3074 E & 06 & \(0.1121 E\) & 17 & 0.1591E & 01 & \(0.2352 E\) & 05 & 0.7227E & 00 \\
\hline 454 & \(0.4391 E\) & 06 & \(0.4674 E\) & 17 & 0.1591E & 01 & 0.2352 E & 05 & \(0.6309 E\) & 00 \\
\hline 455 & 0.4172 E & 06 & 0.3554 E & 17 & 0.1591E & 01 & 0.2352E & 05 & 0.6309 E & 00 \\
\hline 456 & 0.3842 E & 06 & 0.2666E & 17 & 0.1591E & 01 & 0.2352E & 05 & 0.6309E & 00 \\
\hline 457 & 0.3074 E & 06 & 0.1383 E & 17 & 0.1591E & 01 & 0.2352E & 05 & 0.6309E & 00 \\
\hline 458 & 0.2854E & 06 & 0.9871 E & 16 & \(0.1591 E\) & 01 & \(0.2352 E\) & 05 & 0.5309 E & 00 \\
\hline 459 & 0.4172 E & 06 & \(0.4185 E\) & 17 & 0.1591E & 01 & 0.2352E & 05 & \(0.5609 E\) & 00 \\
\hline 460 & 0.3952 E & 06 & 0.3183 E & 17 & 0.1591E & 01 & \(0.2352 E\) & & 0.5609 E & 00 \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|c|}
\hline Obsy & F 1 & & F2 & & F3 & & \(F 4\) & & F5 & \\
\hline 461 & \(0.3623 E\) & 06 & \(0.2387 E\) & 17 & 0.1591E & 0.1 & \(0.2352 E\) & 05 & \(0.5609 E\) & 00 \\
\hline 462 & 0.2964E & 06 & \(0.1238 E\) & 17 & 0.1591 E & 01 & \(0.2352 E\) & 05 & 0.5609 E & 00 \\
\hline 463 & 0.2744E & 05 & 0.8842 E & 16 & 0.1591E & 01 & \(0.2352 E\) & 05 & 0.5609 E & 00 \\
\hline 464 & \(0.3952 E\) & 06 & \(0.3694 E\) & 17 & 0.1591 E & 01 & \(0.2352 E\) & 05 & 0.4918 E & 00 \\
\hline 465 & \(0.3733 E\) & 06 & 0.2810 E & 17 & 0.1591 E & 01 & 0.2352E & 05 & 0.4918 E & 00 \\
\hline 466 & \(0.3403 E\) & 06 & \(0.2108 E\) & 17 & 0.1591 E & 01 & 0.2352E & 05 & 0.4918E & 00 \\
\hline 467 & 0.2854 E & 06 & 0.1092E & 17 & 0.1591E & 01 & 0.2352E & 05 & 0.4918 E & 00 \\
\hline 468 & 0.2525E & 06 & \(0.7801 E\) & 16 & 0.1591E & 01 & 0.2352E & 05 & 0.4918 E & 00 \\
\hline 469 & 0.1148E & 05 & 0.1306E & 17 & 0.3040E & 01 & 0.1069E & 05 & 0.8320E & 00 \\
\hline 470 & 0.9980E & 05 & \(0.9935 E\) & 16 & 0.3040E & 01 & 0.1069E & 05 & 0.8320E & 00 \\
\hline 471 & \(0.8234 E\) & 05 & 0.7450 E & 16 & 0.3040E & 01 & \(0.1069 E\) & 05 & O.8320E & 00 \\
\hline 472 & 0.6487E & 05 & \(0.3864 E\) & 16 & 0.3040E & 01 & \(0.1069 E\) & 05 & . 0.0320 E & 00 \\
\hline 473 & \(0.1098 E\) & 06 & \(0.1121 E\) & 17 & 0.3040 E & 01 & 0.1069 E & 05 & 0.7100E & 00 \\
\hline 474 & 0.9481E & 05 & 0.8526E & 16 & 0.3040E & 01 & 0.1069E & 05 & 0.7100 E & 00 \\
\hline 475 & 0.7984 E & 05 & \(0.6394 E\) & 16 & 0.3040E & 01 & \(0.1069 E\) & 05 & 0.71005 & 00 \\
\hline 476 & 0.5988 E & 05 & \(0.3316 E\) & 16 & 0.3040E & 01 & \(0.1069 E\) & 05 & 0.7100E & 00 \\
\hline 477 & 0.9980E & 05 & 0.7286E & 16 & \(0.3040 E\) & 01 & 0.1069 E & 05 & O.4560E & 00 \\
\hline 478 & 0.8733 E & 05 & \(0.5543 E\) & 16 & 0.3040E & 01 & \(0.1069 E\) & 05 & \(0.4560 E\) & 00 \\
\hline 479 & 0.5988E & 05 & \(0.4157 E\) & 16 & 0.3040E & 01 & 0.1069E & & 0.4560E & 00 \\
\hline 480 & \(0.2725 E\) & 06 & 0.2278E & 17 & 0.2338 E & 01 & 0.1390E & & 0.8708E & 00 \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|}
\hline OBsv & F1 & & F2 & & F3 & & F4 & & F5 \\
\hline 481 & 0.2400E & 06 & 0.1733 E & 17 & 0.2338E & 01 & \(0.1390 E\) & 05 & \(0.3708 E 00\) \\
\hline 482 & 0.2076 E & 06 & 0.1300 E & 17 & 0.2338E & 01 & 0.1390 E & 05 & 0.3708 ECO \\
\hline 483 & \(0.1622 E\) & 06 & 0.6739 E & 16 & D. 2338 E & 01 & 0.1390E & 05 & 0.8708 E 0 \\
\hline 484 & 0.2335E & 06 & 0. 2044 E & 17 & 0.2338 E & 01 & 0.1390E & 05 & 0.7769E 00 \\
\hline 485 & 0.2076E & 06 & 0.1555E & 17 & 0.2338 E & 01 & \(0.1390 E\) & 05 & 0.7769E 00 \\
\hline 486 & 0.1687E & 06 & 0.1167E & 17 & 0.2338E & 01 & 0.1390E & 05 & 0.7769 E 00 \\
\hline 487 & \(0.1427 E\) & 06 & 0.6047E & 16 & 0.2338 E & 01 & 0.1390E & 05 & 0.7769 E 00 \\
\hline 488 & 0.2011 E & 06 & \(0.1549 E\) & 17 & 0.2338 E & 01 & 0.1390E & 05 & 0.5815E 00 \\
\hline 489 & 0.1816 E & 06 & 0.1178 E & 17 & 0.2338E & 01. & 0.1390E & 05 & 0.5815E CO \\
\hline 490 & 0.1557E & 06 & 0.8837E & 16 & \(0.2338 E\) & 01 & 0.1390 E & 05 & 0.5815E 00 \\
\hline 491 & 0.1168 E & 06 & 0.4584E & 16 & 0.2338E & 01 & \(0.1390 E\) & 05 & \(0.5815 E 00\) \\
\hline 492 & 0.1751E & 06 & 0.1418 E & 17 & 0.2338 E & 01 & 0.1390E & 05 & 0.5308E 00 \\
\hline 493 & 0.1557E & 06 & 0.1079E & 17 & 0.2338E & 01 & 0.1390E & 05 & \(0.5308 E 00\) \\
\hline 494 & \(0.1427 E\) & 06 & 0.8086E & 16 & 0.2338E & 01 & 0.1390E & 05 & 0.5308E 00 \\
\hline 495 & 0.1103 E & 06 & \(0.4195 E\) & 16. & 0.2338 E & 01 & 0.1390E & 05 & 0.5308 E 00 \\
\hline 496 & \(0.3673 E\) & 06 & 0.3500E & 17 & 0. 1900 E & 01 & 0.1710 E & 05 & 0.8950 E 0 \\
\hline 497 & \(0.3353 E\) & 06 & \(0.2661 E\) & 17 & 0.1900E & 01 & O.1710E & 05 & 0.8950E 00 \\
\hline 498 & \(0.3194 E\) & 06 & 0.1996E & 17 & 0.1900E & 01 & 0.1710E & 05 & 0.8950E 00 \\
\hline 499 & \(0.2555 E\) & 06 & 0.1035E & 17 & 0.1900E & & 0.1710 E & & 0.8950 E 00 \\
\hline 500 & 0.2236E & 06 & \(0.7394 E\) & 16 & 0.1900 E & & \(0.1710 E\) & & 0.8950E 00 \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|}
\hline Obsv & F1 & & F2 & & F3 & & F4 & & F5 \\
\hline 501 & 0.3513 E & 06 & \(0.3219 E\) & 17 & 0. 1900 E & 01 & O.1710E & & 0.8187E 00 \\
\hline 502 & \(0.3194 E\) & 06 & 0.2449E & 17 & 0.1900E & 01 & 0.1710E & 05 & \(0.8187 E 00\) \\
\hline 503 & 0.2874 E & 06 & \(0.1837 E\) & 17 & 0.1900E & 01 & 0.1710E & 05 & \(0.8187 E 00\) \\
\hline 504 & 0.2395E & 06 & 0.9522E & 16 & 0.1900E & 01 & 0.1710E & 05 & \(0.8187 E 00\) \\
\hline 505 & \(0.2076 E\) & 06 & 0.6805E & 16 & 0.1900E & 01 & 0.1710E & 05 & \(0.3187 E 00\) \\
\hline 506 & 0.3114 E & 06 & \(0.2625 E\) & 17 & 0.1900E & 01 & 0.1710E & 05 & 0.6600E 00 \\
\hline 507 & 0.2874 E & 06 & \(0.1997 E\) & 17 & 0.1900 E & 01 & 0.1710E & 05 & 0.6600E OO \\
\hline 508 & \(0.2475 E\) & 06 & 0.1498E & 17 & 0. 19 DOE & 01 & 0.1710E & - 05 & 0.6600E 00 \\
\hline 509 & \(0.2076 E\) & 06 & 0.7769E & 16 & 0.1900E & 01 & 0.1710 E & 05 & 0.6600E 00 \\
\hline 510 & 0.1916 E & 06 & 0.5546E & 16 & 0.1900E & 01 & 0.1710E & 05 & 0.660JE 00 \\
\hline 511 & \(0.2954 E\) & 06 & 0.2469E & 17 & O. 1900E & 01 & O.1710E & 05 & 0.6187E 00 \\
\hline 512 & \(0.2715 E\) & 06 & 0.1878E & 17 & 0.1900E & 01 & 0.1710E & & 0.6187 O \\
\hline 513 & \(0.2395 E\) & 06 & 0.1409E & 17 & 0.1900E & 01 & 0.1710E & 05 & 0.6187E 00 \\
\hline 514 & 0.1956 E & 06 & 0.7299E & 16 & 0.1900E & 01 & 0.1710E & 05 & 0.6187E 00 \\
\hline 515 & 0.1796 E & 06 & 0.5219E & 16 & 0.1900E & 01 & 0.1710E & 05 & 0.6187E 00 \\
\hline 516 & \(0.2715 E\) & 06 & 0.1984 E & 17 & 0.1900E & 01 & \(0.1710 E\) & 05 & \(0.4925 E 00\) \\
\hline 517 & \(0.2395 E\) & 06 & 0.1509E & 17 & 0.1900 E & 01 & O. 1710 E & 05 & 0.4925E 00 \\
\hline 518 & \(0.2156 E\) & 06 & \(0.1131 E\) & 17 & 0. 1900 E & 01 & 0.1710E & 05 & 0.4925E 00 \\
\hline 519 & 0.1756 E & 06 & \(0.5864 E\) & 16 & 0. 1900 E & 01 & 0.1710 E & 05 & \(0.4925 E 00\) \\
\hline 520 & 0.1597E & 06 & \(0.4191 E\) & 16 & 0. 1900 E & 01 & 0.1710 E & & \(0.4925 E 00\) \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|}
\hline 08sv & F1 & & F2 & & F3 & & F4 & & F5 \\
\hline 521 & \(0.4361 E\) & 06 & \(0.4959 E\) & 17 & 0.1600E & 01 & 0.2031 E & 05 & 0.9116 E 00 \\
\hline 522 & 0.4077E & 06 & \(0.3772 E\) & 17 & 0.1600E & 01 & 0.2031 E & 05 & 0.9116E 00 \\
\hline 523 & \(0.3792 E\) & 06 & 0.2828 E & 17 & 0.1600E & 01 & \(0.2031 E\) & 05 & \(0.9116 E 00\) \\
\hline 524 & 0.3224E & 06 & \(0.1467 E\) & 17 & 0.1600E & 01 & 0.2031 E & 05 & 0.9116 E 0 \\
\hline 525 & 0.3034 E & 06 & \(0.1047 E\) & 17 & 0.1600E & 01 & 0.2031 E & 05 & \(0.9116 E 00\) \\
\hline 526 & \(0.4077 E\) & 06 & \(0.4635 E\) & 17 & 0.1600E & 01 & 0.2031 E & 05 & 0.8474E 00 \\
\hline 527 & 0.3792E & 06 & \(0.3526 E\) & 17 & 0.1600E & 01 & \(0.2031 E\) & 05 & 0.8474 E 00 \\
\hline 528 & \(0.3508 E\) & 06 & \(0.2644 E\) & 17 & 0.1600E & 01 & 0.2031 E & 05 & 0.8474E 00 \\
\hline 529 & \(0.3034 E\) & 06 & \(0.1371 E\) & 17 & 0.1600E & 01 & 0.2031 E & 05 & 0.8474 E 00 \\
\hline 530 & 0.2844 E & 06 & 0.9793 E & 16 & 0.1600E & 01 & \(0.2031 E\) & 05 & 0.8474E 00 \\
\hline 531 & 0.37 92E & 06 & \(0.3932 E\) & 17 & 0.1600E & 01 & 0.2031 E & 05 & \(0.7105 E 00\) \\
\hline 532 & 0.3603 E & 06 & \(0.2991 E\) & 17 & 0.1600E & 01 & 0.2031E & 05 & \(0.7105 E 00\) \\
\hline 533 & \(0.3224 E\) & 06 & 0.2243E & 17 & 0.1600E & 01 & 0.2031 E & 05 & \(0.7105 E 00\) \\
\hline 534 & 0.2749 E & 06 & 0.1163 E & 17 & 0.1600E & 01 & \(0.2031 E\) & 05 & 0.7105E 00 \\
\hline 535 & 0.2560E O & 06 & \(0.8308 E\) & 16 & \(0.1600 E\) & 01 & 0.2031E & 05 & 0.7105 E 00 \\
\hline 536 & \(0.3603 E\) & 06 & 0.3768 E & 17 & 0.1600E & 01 & 0.2031 E & 05 & 0.6789 E 0 \\
\hline 537 & \(0.3413 E\) & 06 & 0.2866E & 17 & 0.1600E & 01 & 0.2031 E & 05 & 0.6789 EO \\
\hline 538 & \(0.3034 E\) & 06 & \(0.2150 E\) & 17 & 0.1600E & 01 & 0.2031E & 05 & 0.6789 E 00 \\
\hline 539 & 0.2560E & 06 & 0.1115 E & 17 & 0.1600E & 01 & 0.2031 E & & 0.6789E 00 \\
\hline 540 & \(0.2370 E\) O & 06 & 0.7958E & 16 & 0.1600E & 01 & 0.2031 E & & 0.6789 EO \\
\hline
\end{tabular}
OBSV F1 F2 F3 F4 F5
\begin{tabular}{lllllllllll}
\(0.3413 E\) & 06 & \(0.3208 E\) & 17 & \(0.1600 E\) & 01 & \(0.2031 E\) & 05 & \(0.5726 E\) & 00 \\
\(0.3224 E\) & 06 & \(0.2439 E\) & 17 & \(0.1600 E\) & 01 & \(0.2031 E\) & 05 & \(0.5726 E\) & 00 \\
\(0.2939 E\) & 06 & \(0.1830 E\) & 17 & \(0.1600 E\) & 01 & \(0.2031 E\) & 05 & \(0.5726 E\) & 00 \\
\(0.2465 E\) & 06 & \(0.9490 E\) & 16 & \(0.1600 E\) & 01 & \(0.2031 E\) & 05 & \(0.5726 E\) & 00 \\
\(0.2275 E\) & 06 & \(0.6775 E\) & 16 & \(0.1600 E\) & 01 & \(0.2031 E\) & 05 & \(0.5726 E\) & 00 \\
\(0.3129 E\) & 06 & \(0.2773 E\) & 17 & \(0.1600 E\) & 01 & \(0.2031 E\) & 05 & \(0.4916 E\) & 00 \\
\(0.2892 E\) & 06 & \(0.2109 E\) & 17 & \(0.1600 E\) & 01 & \(0.2031 E\) & 05 & \(0.4916 E\) & 00 \\
\(0.2655 E\) & 06 & \(0.1582 E\) & 17 & \(0.1600 E\) & 01 & \(0.2031 E\) & 05 & \(0.4916 E\) & 00 \\
\(0.2275 E\) & 06 & \(0.8204 E\) & 16 & \(0.1600 E\) & 01 & \(0.2031 E\) & 05 & \(0.4916 E\) & 00 \\
\(0.1991 E\) & 06 & \(0.5857 E\) & 16 & \(0.1600 E\) & 01 & \(0.2031 E\) & 05 & \(0.4916 E\) & 00 \\
\(0.5818 E\) & 06 & \(0.6647 E\) & 17 & \(0.1382 E\) & 01 & \(0.2352 E\) & 05 & \(0.9236 E\) & 00 \\
\(0.5599 E\) & 06 & \(0.5055 E\) & 17 & \(0.1382 E\) & 01 & \(0.2352 E\) & 05 & \(0.9236 E\) & 00 \\
\(0.5269 E\) & 06 & \(0.3792 E\) & 17 & \(0.1382 E\) & 01 & \(0.2352 E\) & 05 & \(0.9236 E\) & 00 \\
\(0.4501 E\) & 06 & \(0.1966 E\) & 17 & \(0.1382 E\) & 01 & \(0.2352 E\) & 05 & \(0.9236 E\) & 00
\end{tabular}
\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|}
\hline 0esv & F1 & & F2 & & F3 & & F4 & & F5 \\
\hline 561 & \(0.5160 E\) & 06 & 0.5509E & 17 & 0.1382 E & 01 & \(0.2352 E\) & 05 & 0.7527E 00 \\
\hline 562 & 0.4830 E & 06 & 0.4190E & 17 & 0.1382 E & 01 & 0.2352E & 05 & \(0.7527 E 00\) \\
\hline 563 & 0.4611 E & 06 & 0.3142 E & 17 & 0.1382E & 01 & 0.2352E & 05 & 0.7527E 00 \\
\hline 564 & 0.3842 E & 06 & 0.1629E. & 17 & D. 1382 E & 01 & 0.2352E & 05 & 0.7527E 00 \\
\hline 565 & \(0.3623 E\) & 06 & 0.1164E & 17 & 0.1382E & 01 & 0.2352E & 05 & 0.7527E 00 \\
\hline 566 & 0.4885E & 06 & 0.5305E & 17 & 0.1382E & 01 & 0.2352E & 05 & 0.7227E 00 \\
\hline 567 & \(0.4611 E\) & 06 & 0.4035E & 17 & 0.1382 E & 01 & \(0.2352 E\) & 05 & \(0.7227 E 00\) \\
\hline 568 & \(0.4281 E\) & 06 & 0.3026E & 17 & \(0.1382 E\) & 01 & \(0.2352 E\) & 05 & 0.7227E 00 \\
\hline 569 & \(0.3623 E\) & 06 & \(0.1569 E\) & 17 & 0.1382 E & 01 & \(0.2352 E\) & 05 & 0.7227E 00 \\
\hline 570 & 0.3403 E & 06 & \(0.1121 E\) & 17 & 0.1382E & 01 & \(0.2352 E\) & 05 & 0.7227E 00 \\
\hline 571 & \(0.4721 E\) & 06 & 0.4674E & 17 & 0.1382E & 01 & 0.2352E & 05 & 0.6309E 00 \\
\hline 572 & 0.45012 & 06 & 0.3554 E & 17 & 0.1382E & 01 & 0.2352E & 05 & 0.6309E 00 \\
\hline 573 & 0.4172 E & 06 & 0.2666E & 17 & 0.1382E & 01 & 0.2352E & 05 & 0.6309E 00 \\
\hline 574 & \(0.3513 E\) & 06 & 0.1383E & 17 & 0.1382E & 01 & 0.2352E & 05 & 0.6309 E 00 \\
\hline 575 & \(0.3293 E\) & 06 & 0.9871 E & 16 & 0.1382E & 01 & \(0.2352 E\) & 05 & 0.6309E 00 \\
\hline 576 & 0.4281E & 06 & \(0.4185 E\) & 17 & 0.1382E & 01 & \(0.2352 E\) & 05 & 0.5609E 00 \\
\hline 577 & 0.4062 E & 06 & 0.3183 E & 17 & 0.1382E & 01 & \(0.2352 E\) & 05 & 0.5609 E 00 \\
\hline 578 & 0.3733E & 06 & 0.2387E & 17 & 0.1382E & 01 & O.2352E & 05 & \(0.5609 E 00\) \\
\hline 579 & 0.3074 E & 06 & 0.1238E & 17 & \(0.1382 E\) & 01 & 0.2352 F & 05 & 0.5609E 00 \\
\hline 580 & \(0.2854 E\) & 06 & 0.8842E & 16 & 0.1382 E & 01 & 0.2352E & 05 & 0.5609 E 00 \\
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\end{tabular}
\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|c|}
\hline OBSV & F1 & & F2 & & F3 & & \(F_{4}\) & & F5 & \\
\hline 581 & \(0.4062 E\) & 06 & \(0.3694 E\) & 17 & 0.1382 E & 01 & 0.2352E & 05 & 0.4918 E & 00 \\
\hline 582 & 0.3842 E & 06 & 0.2810E & 17 & 0.1382E & 01 & \(0.2352 E\) & 05 & 0.4918 E & 00 \\
\hline 583 & \(0.3623 E\) & 06 & \(0.2108 E\) & 17 & 0.1382E & 01 & \(0.2352 E\) & 05 & 0.4918 E & 00 \\
\hline 584 & \(0.2964 E\) & 06 & 0.1092E & 17 & 0.1382E & 01 & 0.2352 E & 05 & 0.4918 E & 00 \\
\hline 585 & 0.2744 E & 06 & 0.7801 E & 16 & 0.1382E & 01 & 0.2352 E & 05 & 0.4918E & 00 \\
\hline 586 & 0.1198 E & 06 & 0.1306E & 17 & 0.2580E & 01 & \(0.1069 E\) & 05 & 0.8320E & 00 \\
\hline 587 & 0.1048 E & 06 & 0.9935E & 16 & O.2580E & 01 & \(0.1069 E\) & 05 & 0.8320E & 00 \\
\hline 588 & 0.8982 E & 05 & 0.7450E & 16 & D. 2580 E & 01 & 0.1069E & 05 & \(0.8320 E\) & 00 \\
\hline 589 & \(0.7235 E\) & 05 & \(0.3864 E\) & 16 & 0.2580E & 01 & 0.1069E & 05 & 0.8320E & 00 \\
\hline 590 & 0.1148 E & 06 & 0.1121 E & 17 & 0.2580E & 01 & 0.1069E & 05 & 0.7100E & 00 \\
\hline 591 & 0.9980E & 05 & 0.8526E & 16 & 0.2580E & 01 & \(0.1069 E\) & 05 & 0.7100 E & 00 \\
\hline 592 & 0.8733 E & 05 & 0.6394E & 16 & 0.2580E & 01 & 0.1069E & 05 & 0.7100E & 00 \\
\hline 593 & 0.6986E & 05 & \(0.3316 E\) & 16 & 0.2580E & 01 & \(0.1069 E\) & 05 & 0.7100E & 00 \\
\hline 594 & 0.1098 E & 06 & 0.7286E & 16 & 0.2580E & 01 & -0.1069E & 05 & \(0.4560 E\) & 00 \\
\hline 595 & 0.9481 E & 05 & 0.5543 E & 16 & 0.2580E & 01 & \(0.1069 E\) & 05 & 0.4560 E & 00 \\
\hline 596 & 0.8483 E & 05 & \(0.4157 E\) & 16 & 0.2580E & 01 & 0.1069E & 05 & 0.4560E & 00 \\
\hline 597 & \(0.2854 E\) & 06 & \(0.2278 E\) & 17 & 0.1985E & 01 & 0.1390E & 05 & 0.8708E & 00 \\
\hline 598 & 0.2595E & 06 & 0.1733 E & 17 & 0.1985E & 01 & 0.1390E & 05 & \(0.8708 \pm\) & 00 \\
\hline 599 & \(0.2206 E\) & 06 & 0.1300E & 17 & 0.1985E & 01 & 0.1390E & 05 & 0.8708 E & 00 \\
\hline 600 & 0.1687E & 06 & 0.6739 E & & 0.1985E & 01 & \(0.1390 E\) & & \(0.8708 E\) & 00 \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|c|c|c|c|c|c|}
\hline Oesv & F1 & F2 & & F3 & & F4 & & F5 \\
\hline 601 & 0.2595E 06 & 0.2044 E & 17 & 0.1985E & 01 & 0.1390E & 05 & 0.7769E 00 \\
\hline 602 & O.2335E 06 & \(0.1555 E\) & 17 & 0.1985E & 01 & 0.1390E & 05 & 0.7769E 00 \\
\hline 603 & 0.2076E 06 & 0.1167 E & 17 & 0.1985E & 01 & 0.1390E & 05 & 0.7769E 00 \\
\hline 604 & 0.1687E 06 & 0.6047E & 16 & 0.1985E & 01 & 0.1390E & 05 & 0.7769E 00 \\
\hline 605 & \(0.2141 E 06\) & 0.1549E & 17 & 0.1985E & 01 & 0.1390 E & 05 & 0.5815 E 00 \\
\hline 606 & \(0.1881 E 06\) & 0.1178 E & 17 & 0.1985E & 01 & 0.1390E & 05 & 0.5815E 00 \\
\hline 607 & \(0.1687 E 06\) & 0.8837 E & 16 & 0.1985E & 01 & 0.1390E & 05 & 0.5815E 00 \\
\hline 608 & \(0.1362 E 06\) & 0.4584E & 16 & 0.1985E & 01 & 0.1390E & 05 & 0.5815E 00 \\
\hline 609 & 0.1946 E 06 & 0.1418 E & 17 & 0.1985E & 01 & 0.1390E & 05 & 0.5308E 00 \\
\hline 610 & \(0.1687 E 06\) & 0.1079E & 17 & 0.1985E & 01 & 0.1390E & 05 & 0.5308 O 0 \\
\hline 611 & 0.1557E 06 & \(0.8086 E\) & 16 & 0.1985E & 01 & 0.1390E & 05 & 0.5308E 00 \\
\hline 612 & 0.1233 E 06 & \(0.4195 E\) & 16 & 0.1985E & 01 & 0.1390E & 05 & .0.5308E 00 \\
\hline 613 & \(0.4152 E 06\) & 0.3500E & 17 & \(0.1612 E\) & 01 & 0.1710E & 05 & 0.8950E 00 \\
\hline 614 & \(0.3713 E 06\) & \(0.2661 E\) & 17 & \(0.1612 E\) & 01 & 0.1710E & 05 & 0.3950E 00 \\
\hline 615 & 0.3393 E 06 & 0.1996E & 17 & 0.1612 E & 01 & O.1710E & 05 & 0.8950E 00 \\
\hline 616 & \(0.2754 E 06\) & 0.1035E & 17 & \(0.1612 E\) & 01 & 0.1710E & 05 & O.8950E OO \\
\hline 617 & 0.2555E 06 & \(0.7394 E\) & 16 & 0.1612E & 01 & 0.1710 E & 05 & 0.3950E CO \\
\hline 618 & \(0.3992 E 06\) & 0.3219 E & 17 & 0.1612E & 01 & 0.1710 E & 05 & 0.8187 E 0 \\
\hline 619 & \(0.3513 E 06\) & 0.2449 E & 17 & 0.1612 E & 01 & 0.1710 E & 05 & 0.8187 E 00 \\
\hline 620 & \(0.3194 E 06\) & \(0.1837 E\) & 17 & 0.1612 E & 01 & 0.1710E & 05 & 0.8187E 00 \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|c|}
\hline OBSV & F1 & & F2 & & F3 & & \(F 4\) & & F 5 & \\
\hline 621 & 0.2635E & 06 & \(0.9522 E\) & 16 & \(0.1612 E\) & 01 & 0.1710 E & & \(0.3187 E\) & 00 \\
\hline 622 & \(0.2395 E\) & 06 & \(0.6805 E\) & 16 & 0.1612 E & 01 & 0.1710E & 05 & 0.8187E & 00 \\
\hline 623 & 0.3273E & 06 & \(0.2625 E\) & 17 & 0. 1612 E & 01 & 0.1710E & 05 & 0.6600E & 00 \\
\hline 624 & 0.3034 E & 06 & 0.1997E & 17 & 0.1612 E & 01 & 0.1710E & 05 & 0.6600E & 00 \\
\hline 625 & 0.2555E & 06 & 0.1498E & 17 & 0.1612 E & 01 & 0.1710E & 05 & 0.6600E & 00 \\
\hline 626 & 0.2236 E & 06 & 0.7759 E & 16 & \(0.1612 E\) & 01 & 0.1710 E & 05 & 0.5600E & 00 \\
\hline 627 & \(0.2076 E\) & 06 & 0.5546 E & 16 & 0.1612 E & 01 & 0.1710 E & 05 & O.6600E & 00 \\
\hline 628 & 0.3114E & 06 & 0.2469E & 17 & 0.1612 E & 01 & 0.1710E & 05 & 0.6187 E & 00 \\
\hline 629 & 0.2794 E & 06 & 0.1878E & 17 & 0.1612 E & 01 & 0.1710 E & 05 & \(0.6187 E\) & 00 \\
\hline 630 & 0.2555E & 06 & 0.1409E & 17 & 0.1612 E & 01 & 0.1710E & 05 & \(0.6187 E\) & 00 \\
\hline 631 & \(0.2155 E\) & 06 & 0.7299E & 16 & 0. 1612 E & 01 & 0.1710E & 05 & 0.6187E & 00 \\
\hline 632 & 0.1916 E & 06 & 0.52.19E & 16 & 0.1612 E & 01 & 0.1710E & 05 & .0.6187E & 00 \\
\hline 633 & 0.2794 E & 06 & 0.1984 E & 17 & 0.1612 E & 01 & 0.1710 E & 05 & 0.4925E & 00 \\
\hline 634 & \(0.2475 E\) & 06 & 0.1509E & 17 & \(0.1612 E\) & 01 & O.1710E & 05 & \(0.4925 E\) & 00 \\
\hline 635 & 0.2236E & 06 & 0.1131 E & 17 & 0.1612E & 01 & 0.1710E & 05 & \(0.4925 E\) & 00 \\
\hline 636 & \(0.1916 E\) & 06 & \(0.5864 E\) & 16 & 0.1612 E & 01 & O.1710E & 05 & \(0.4925 E\) & 00 \\
\hline 637 & \(0.1756 E\) & 06 & 0.4191 E & 16 & 0.1612E & 01 & 0.1710E & 05 & \(0.4925 E\) & 00 \\
\hline 638 & 0.5120E & 06 & 0.4959E & 17 & 0.1358 E & 01 & \(0.2031 E\) & 05 & \(0.9116 E\) & 00 \\
\hline 639 & 0.4835 E & 06 & 0.3772 E & 17 & 0.1358E & 01 & \(0.2031 E\) & 05 & 0.9116 E & 00 \\
\hline 640 & 0.4456 E & 06 & \(0.2828 E\) & 17 & 0.1358E & 01 & \(0.2031 E\) & 05 & 0.9116 E & 00 \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|c|}
\hline Obsv & F1 & & F2 & & F3 & & F4 & & F5 & \\
\hline 641 & \(0.3792 E\) & 06 & \(0.1467 E\) & 17 & 0.1358E & 01 & \(0.2031 E\) & 05 & 0.9116 E & 00 \\
\hline 642 & 0.3413 E & 06 & 0.1047E & 17 & 0.1353 E & 01 & \(0.2031 E\) & 05 & 0.9116 E & 00 \\
\hline 643 & 0.4740E & 06 & 0.4635E & 17 & 0.1358 E & 01 & 0.2031 E & 05 & 0.8474 E & 00 \\
\hline 644 & 0.4551E & 06 & 0.3526E & 17 & 0.1358E & 01 & 0.2031 E & 05 & 0.3474 E & 00 \\
\hline 645 & 0.4266E & 06 & 0.2644E & 17 & 0.1358E & 01 & 0.2031 E & 05 & 0.8474E & 00 \\
\hline 646 & \(0.3508 E\) & 06 & \(0.1371 E\) & 17 & O. 1358 E & 01 & 0.2031E & 05 & 0.8474 E & 00 \\
\hline 647 & 0.3318 E & 06 & 0.9793E & 16 & 0.1358E & 01 & 0.2031 E & 05 & 0.8474E & co \\
\hline 648 & 0.4456E & 06 & 0.3932 E & 17 & 0.1358E & 01 & 0.2031 E & 05 & 0.7105E & 00 \\
\hline 649 & 0.4077 E & 06 & \(0.2991 E\) & 17 & 0.1358E & 01 & 0.2031E & 05 & \(0.7105 E\) & 00 \\
\hline 650 & 0.3698E & 06 & \(0.2243 E\) & 17 & 0.1358E & 01 & 0.2031 E & 05 & 0.7105 E & 00 \\
\hline 651 & \(0.3129 E\) & 06 & 0.1163 E & 17 & 0.1358 E & 01 & 0.2031 E & 05 & 0.7105 E & 00 \\
\hline 652 & 0.2344E & 06 & \(0.8308 E\) & 16 & 0.1358E & 01 & 0.2031 E & 05 & \(0.7105 E\) & 00 \\
\hline 653 & 0.4266E & 06 & 0.3768 E & 17 & 0.1358 E & 01 & \(0.2031 E\) & 05 & 0.6789E & 00 \\
\hline 654 & 0.3887E & 06 & 0.2866E & 17 & 0.1358E & 01 & 0.2031 E & 05 & 0.6789E & 00 \\
\hline 655 & 0.3508E & 06 & 0.2150E & 17 & 0.1358E & 01 & 0.2031 E & 05 & 0.6789E & 00 \\
\hline 656 & 0.2939E & 06 & \(0.1115 E\) & 17 & 0.1358 E & 01 & 0.2031 E & 05 & 0.6789 E & 00 \\
\hline 657 & \(0.2655 E\) & 06 & 0.7958E & 16 & \(0.1358 E\) & 01 & 0.2031 E & 05 & 0.6789E & 00 \\
\hline 658 & 0.4077E & 06 & 0.3208E & 17 & 0.1358E & 01 & 0.2031E & 05 & 0.5726E & 00 \\
\hline 659 & \(0.3792 E\) & 06 & \(0.2439 E\) & 17 & 0.13588 & 01 & 0.2031 E & 05 & 0.5726 E & 00 \\
\hline 660 & 0.3413 E & 06 & \(0.1830 E\) & 17 & 0.1358E & 01 & 0.2031E & & 0.5726 E & 00 \\
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\begin{tabular}{|c|c|c|c|c|c|c|c|c|}
\hline OBSV & Fi & F2 & & F3 & & F4 & & F5 \\
\hline 661 & 0.2844 E 06 & \(0.9490 E\) & 16 & 0.1358E & 01 & 0.2031 E & 05 & \(0.5726 E 00\) \\
\hline 662 & 0.2560E 06 & 0.6775 E & 16 & 0.1358E & 01 & \(0.2031 E\) & 05 & \(0.5726 E 00\) \\
\hline 663 & 0.3698 O & 0.2773E & 17 & 0.1358E & 01 & \(0.2031 E\) & 05 & 0.4916 E 00 \\
\hline 664 & 0.3318E O6 & \(0.2109 E\) & 17 & 0.1358 E & 01 & 0.2031 E & 05 & 0.4916 E 00 \\
\hline 665 & 0.2939E 06 & 0.1582E & 17 & 0.1358 E & 01 & 0.2031 E & 05 & \(0.4916 E 00\) \\
\hline 606 & 0.2465E 06 & \(0.8204 E\) & 16 & 0.1358E & 01 & 0.2031 E & 05 & 0.4916 E 00 \\
\hline 667 & 0.2275E 06 & \(0.5857 E\) & 16 & 0.1358E & 01 & \(0.2031 E\) & 05 & 0.4916 E 00 \\
\hline 668 & \(0.5709 \mathrm{O6}\) & \(0.6647 E\) & 17 & 0.1173 E & 01 & \(0.2352 E\) & 05 & 0.9236E 00 \\
\hline 669 & 0.5379 E 06 & \(0.5055 E\) & 17 & 0.1173 E & 01 & 0.2352 E & 05 & \(0.9236 E 00\) \\
\hline 670 & 0.5050E 06 & \(0.3792 E\) & 17 & 0.1173 E & 01 & 0.2352E & 05 & \(0.9236 E 00\) \\
\hline 671 & 0.43.91E 06 & \(0.1966 E\) & 17 & \(0.1173 E\) & 01 & 0.2352E & 05 & 0.9236 E 00 \\
\hline 672 & 0.4172E 06 & 0.1405E & 17 & 0.1173 E & 01 & 0.2352E & 05 & . 0.9236 E 00 \\
\hline 673 & 0.5599E 06 & \(0.6281 E\) & 17 & 0.1173 E & 01 & \(0.2352 E\) & 05 & 0.8682 E 00 \\
\hline 674 & 0.5379E Ó & 0.4778 E & 17 & \(0.1173 E\) & 01 & \(0.2352 E\) & 05 & 0.8682 E 00 \\
\hline 675 & 0.5160E 06 & 0.3583 E & 17 & \(0.1173 E\) & 01 & 0.2352 E & 05 & 0.8682E 00 \\
\hline 676 & 0.4391E 06 & 0.1858E & 17 & 0.1173 E & 01 & 0.2352E & 05 & \(0.8682 \pm 00\) \\
\hline 677 & 0.4172 E 06 & \(0.1327 E\) & 17 & 0.1173 E & 01 & 0.2352 E & 05 & 0.3682 E 00 \\
\hline 678 & \(0.5379 E 06\) & 0.5509E & 17 & \(0.1173 E\) & 01 & 0.2352 E & 05 & 0.7527E 00 \\
\hline 679 & 0.5160E 06 & 0.4190E & 17 & 0.1173 E & 01 & 0.2352E & 05 & 0.7527E 00 \\
\hline 680 & 0.4830E 06 & 0.3142 E & 17 & 0.1173E & 01 & 0.2352E & 05 & 0.7527E 00 \\
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\end{tabular}
\begin{tabular}{llllllllllll}
\(0.4172 E\) & 06 & \(0.1629 E\) & 17 & \(0.1173 E\) & 01 & \(0.2352 E\) & 05 & \(0.7527 E\) & 00 \\
\(0.3952 E\) & 06 & \(0.1164 E\) & 17 & \(0.1173 E\) & 01 & \(0.2352 E\) & 05 & \(0.7527 E\) & 00 \\
\(0.5269 E\) & 06 & \(0.5305 E\) & 17 & \(0.1173 E\) & 01 & \(0.2352 E\) & 05 & \(0.7227 E\) & 00 \\
\(0.5050 E\) & 06 & \(0.4035 E\) & 17 & \(0.1173 E\) & 01 & \(0.2352 E\) & 05 & \(0.7227 E\) & 00 \\
\(0.4721 E\) & 06 & \(0.3026 E\) & 17 & \(0.1173 E\) & 01 & \(0.2352 E\) & 05 & \(0.7227 E\) & 00 \\
\(0.3952 E\) & 06 & \(0.1569 E\) & 17 & \(0.1173 E\) & 01 & \(0.2352 E\) & 05 & \(0.7227 E\) & 00 \\
\(0.3733 E\) & 06 & \(0.1121 E\) & 17 & \(0.1173 E\) & 01 & \(0.2352 E\) & 05 & \(0.7227 E\) & 00 \\
\(0.4940 E\) & 06 & \(0.4674 E\) & 17 & \(0.1173 E\) & 01 & \(0.2352 E\) & 05 & \(0.6309 E\) & 00 \\
\(0.4666 E\) & 06 & \(0.3554 E\) & 17 & \(0.1173 E\) & 01 & \(0.2352 E\) & 05 & \(0.6309 E\) & 00 \\
\(0.4391 E\) & 06 & \(0.2666 E\) & 17 & \(0.1173 E\) & 01 & \(0.2352 E\) & 05 & \(0.6309 E\) & 00 \\
\(0.3733 E\) & 06 & \(0.1383 E\) & 17 & \(0.1173 E\) & 01 & \(0.2352 E\) & 05 & \(0.6309 E\) & 00 \\
\(0.3513 E\) & 06 & \(0.9871 E\) & 16 & \(0.1173 E\) & 01 & \(0.2352 E\) & 05 & \(0.6309 E\) & 00 \\
\(0.4501 E\) & 06 & \(0.4185 E\) & 17 & \(0.1173 E\) & 01 & \(0.2352 E\) & 05 & \(0.5609 E\) & 00 \\
\(0.4281 E\) & 06 & \(0.3183 E\) & 17 & \(0.1173 E\) & 01 & \(0.2352 E\) & 05 & \(0.5609 E\) & 00 \\
\(0.4062 E\) & 06 & \(0.2387 E\) & 17 & \(0.1173 E\) & 01 & \(0.2352 E\) & 05 & \(0.5609 E\) & 00
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\begin{tabular}{|c|c|c|c|c|c|c|c|c|}
\hline \(0.3074 E\) & 06 & \(0.1092 E\) & 17 & 0.1173 E & 01 & 0.2352 E & 05 & 0.4913 E \\
\hline 0.2854E & 06 & 0.7801 E & 16 & \(0.1173 E\) & 01 & \(0.2352 E\) & 05 & 0.4918 E \\
\hline 0.1397E & 06 & 0.1306E & 17 & 0.2120 & 01 & 0.1069E & 05 & 0.3320E \\
\hline 0.1198 E & 06 & 0.9935E & 16 & 0.2120 E & 01 & \(0.1069 E\) & 05 & 0.8320E \\
\hline 0.9980E & 05 & 0.7450 E & 16 & \(0.2120 E\) & 01 & 0. & 05 & 0.8320E \\
\hline 0.7984E & 05 & 0.3864 E & 16 & \(0.2120 E\) & 01 & \(0.1069 E\) & 05 & 0.8320E \\
\hline 0.1297E & 06 & 0.1121 E & 17 & 0.2120 & 01 & \(0.1069 E\) & 05 & 0.7100E \\
\hline 0.1148 E & 06 & \(0.8526 E\) & 16 & 0.2120 E & 01 & 0.1069 & 05 & 0.7100E \\
\hline 0.9481E & 05 & 0.6394E & 16 & \(0.2120 E\) & 01 & \(0.1069 E\) & 05 & 0.7100E \\
\hline 0.7485E & 05 & 0.331 & 16 & \(0.2120 E\) & 01 & \(0.1069 E\) & 05 & 0.71 DOE \\
\hline 0.1198 E & 0ó & 0.7286E & 16 & \(0.2120 E\) & 01 & \(0.1069 E\) & 05 & 0.4560E \\
\hline 0.1048 E & 06 & 0.5543 & 16 & 2120 & 01 & 0.1069 & 05 & . 0.4560 \\
\hline 0.8982E 0 & 05 & \(0.4157 E\) & 16 & 0.2120E & 01 & \(0.1069 E\) & 05 & 0.4560 E \\
\hline \(0.3114 E 0\) & 06 & 0.2278E & 17 & \(0.1631 E\) & 01 & \(0.1390 E\) & 05 & 0.8708 E \\
\hline \(0.2854 E O\) & 06 & \(0.1733 E\) & 17 & 0.1631 E & 01 & 0.13901 & 05 & 0.8708 \\
\hline \(0.2530 E 0\) & 06 & 0.1300E & 17 & 0.1631E & 01 & 0.1390E & 05 & 0.87 08E \\
\hline \(0.2011 E 0\) & 06 & 0.6739E & 16 & \(0.1631 E\) & 01 & 0.1390E & 05 & 0.8708 E \\
\hline 0.2919 O & 06 & 0.2044E & 17 & \(0.1631 E\) & 01 & 0.1390E & 05 & \(0.7769 E\) \\
\hline \(0.2595 E 0\) & 06 & \(0.1555 E\) & 17 & 0.1631E & 01 & 0.1390E & 05 & 0.7769E 0 \\
\hline \(0.2335 E\) & 06 & \(0.1167 E\) & 17 & \(0.1631 E\) & 01 & 0.1390E & 05 & . 776 \\
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\(0.1881 E\)
\(0.2335 E\)
\(0.2066 E\)
\(0.1881 E\)
0.26
\(0.1557 E 06\) \(0.2206 E 06\) \(0.1979 E 06\) \(0.1751 E^{\circ} 06\) \(0.1427 E 06\) \(0.4152 E 06\) \(0.3832 E 06\) \(0.3513 E 06\) \(0.2874 E 06\) \(0.2475 E 06\) \(0.3832 E 06\) \(0.3593 E 06\) \(0.3194 E 06\) \(0.2635 E 06\) \(0.2395 E\) 06 0.3353 E 06
\begin{tabular}{|c|c|c|c|c|c|c|c|}
\hline \(0.6047 E\) & 16 & \(0.1631 E\) & 01 & \(0.1390 E\) & 05 & 0.7769 E & 00 \\
\hline \(0.1549 E\) & 17 & \(0.1631 E\) & 01 & O.1390E & 05 & \(0.5815 E\) & 00 \\
\hline 0.1178E & 17 & 0.1631E & 01 & \(0.1390 E\) & 05 & \(0.5815 E\) & 00 \\
\hline O.8837E & 16 & \(0.1631 E\) & 01 & O.1390E & 05 & \(0.5815 E\) & 00 \\
\hline 0.4584E & 16 & \(0.1631 E\) & 01 & 0.1390E & 05 & 0.5815 E & 00 \\
\hline \(0.1418 E\) & 17 & 0.1631E & 01 & \(0.1390 E\) & 05 & \(0.5308 E\) & 00 \\
\hline 0.1079E & 17 & \(0.1631 E\) & 01 & O.1390E & 05 & \(0.5308 E\) & 00 \\
\hline \(0.8086 E\) & 16 & \(0.1631 E\) & 01 & O.1390E & 05 & \(0 \cdot 5308 \mathrm{E}\) & 00 \\
\hline \(0.4195 E\) & 16 & 0.1631E & 01 & O.1390E & 05 & \(0.5308 E\) & 00 \\
\hline 0.3500E & 17 & 0.1325E & 01 & O.1710E & 05 & O.3950E & 00 \\
\hline 0.2661E & 17 & 0.1325E & 01 & 0.1710 E & 05 & \(0.8950 E\) & 00 \\
\hline 0.1996E & 17 & \(0.1325 E\) & 01 & \(0.1710 E\) & 05 & .0.8950E & 00 \\
\hline D.1035E & 17 & \(0.1325 E\) & 01 & O. 1710 L & 05 & \(0.8950 E\) & 00 \\
\hline 0.7394E & 16 & 0.1325E & 01 & \(0.1710 E\) & 05 & O.8950E & 00 \\
\hline \(0.3219 E\) & 17 & \(0.1325 E\) & 01 & 0.1710 E & 05 & 0.3187E & 00 \\
\hline 0.2449E & 17 & 0.1325E & 01 & 0.1710 E & 05 & 0.3187E & 00 \\
\hline 0.1837E & 17 & \(0.1325 E\) & 01 & 0.1710 E & 05 & 0.8187E & 00 \\
\hline \(0.9522 E\) & 16 & \(0 \cdot 1325 E\) & 01 & O-1710E & 05 & \(0.3187 \equiv\) & 00 \\
\hline 0.6805E & 16 & 0.1325E & 0.1 & O.1710E & 05 & D. \(8187 E\) & 00 \\
\hline 0. \(2625 E\) & 17 & \(0.1325 E\) & 01 & 0.1710 E & 05 & 0.6600E & 00 \\
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\end{tabular}

Obsv F1

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F5
\begin{tabular}{lllllllllllll}
741 & \(0.3114 E\) & 06 & \(0.1997 E\) & 17 & \(0.1325 E\) & 01 & \(0.1710 E\) & 05 & \(0.6600 E\) & 00 \\
742 & \(0.2635 E\) & 06 & \(0.1498 E\) & 17 & \(0.1325 E\) & 01 & \(0.1710 E\) & 05 & \(0.6600 E\) & 00 \\
743 & \(0.2395 E\) & 06 & \(0.7769 E\) & 16 & \(0.1325 E\) & 01 & \(0.1710 E\) & 05 & \(0.6600 E\) & 00 \\
744 & \(0.2236 E\) & 06 & \(0.5546 E\) & 16 & \(0.1325 E\) & 01 & \(0.1710 E\) & 05 & \(0.5600 E\) & 00 \\
745 & \(0.3114 E\) & 06 & \(0.2469 E\) & 17 & \(0.1325 E\) & 01 & \(0.1710 E\) & 05 & \(0.6137 E\) & 00 \\
746 & \(0.2874 E\) & 06 & \(0.1878 E\) & 17 & \(0.1325 E\) & 01 & \(0.1710 E\) & 05 & \(0.6187 E\) & 00 \\
747 & \(0.2635 E\) & 06 & \(0.1409 E\) & 17 & \(0.1325 E\) & 01 & \(0.1710 E\) & 05 & \(0.6187 E\) & 00 \\
748 & \(0.2236 E\) & 06 & \(0.7299 E\) & 16 & \(0.1325 E\) & 01 & \(0.1710 E\) & 05 & \(0.6187 E\) & 00 \\
749 & \(0.2076 E\) & 06 & \(0.5219 E\) & 16 & \(0.1325 E\) & 01 & \(0.1710 E\) & 05 & \(0.6187 E\) & 00 \\
750 & \(0.2874 E\) & 06 & \(0.1984 E\) & 17 & \(0.1325 E\) & 01 & \(0.1710 E\) & 05 & \(0.4925 E\) & 00 \\
751 & \(0.2555 E\) & 06 & \(0.1509 E\) & 17 & \(0.1325 E\) & 01 & \(0.1710 E\) & 05 & \(0.4925 E\) & 00 \\
752 & \(0.2315 E\) & 06 & \(0.1131 E\) & 17 & \(0.1325 E\) & 01 & \(0.1710 E\) & 05 & \(0.4925 E\) & 00 \\
753 & \(0.1996 E\) & 06 & \(0.5864 E\) & 16 & \(0.1325 E\) & 01 & \(0.1710 E\) & 05 & \(0.4925 E\) & 00 \\
754 & \(0.1836 E\) & 06 & \(0.4191 E\) & 16 & \(0.1325 E\) & 01 & \(0.1710 E\) & 05 & \(0.4925 E\) & 00 \\
755 & \(0.4646 E\) & 06 & \(0.4959 E\) & 17 & \(0.1116 E\) & 01 & \(0.2031 E\) & 05 & \(0.9116 E\) & 00
\end{tabular}
\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|}
\hline Obsv & F1 & & \(F 2\) & & F3 & & F4 & & F5 \\
\hline 701 & \(0.4172 E\) & 06 & \(0.3526 E\) & 17 & 0.1116 E & 01 & \(0.2031 E\) & 05 & 0.3474E 00 \\
\hline 762 & \(0.3887 E\) & 06 & 0.2644 E & 17 & 0.1116 E & 01 & 0.2031 E & 05 & 0.8474 E 00 \\
\hline 763 & 0.3413 E & 06 & \(0.1371 E\) & 17 & 0.1116 E & 01 & 0.2031 E & 05 & 0.8474E 00 \\
\hline 764 & \(0.3224 E\) & 06 & \(0.9793 E\) & 16 & \(0.1116 E\) & \[
01
\] & 0.2031 E & 05 & 0.8474 E 00 \\
\hline 765 & \(0.4266 E\) & 06 & 0.3932 E & 17 & 0.1116 E & 01 & 0.2031E & 05 & \(0.7105 E 00\) \\
\hline 766 & \(0.3982 E\) & 06 & \(0.2991 E\) & 17 & 0.1116 E & 01 & \(0.2031 E\) & 05 & 0.7105E 00 \\
\hline 767 & 0.3603 E & 06 & \(0.2243 E\) & 17 & 0.1116 E & 01 & \(0.2031 E\) & 05 & 0.7105 E 00 \\
\hline 768 & \(0.3034 E\) & 06 & 0.1163 E & 17 & 0.1116 E & 01 & 0.2031 E & 05 & 0.7105E 00 \\
\hline 769 & 0.2844 E & 06 & 0.8308E & 16 & 0.1116 E & 01 & \(0.2031 E\) & 05 & 0.7105E OD \\
\hline 770 & 0.4077 E & 06 & \(0.3768 E\) & 17 & 0.1116 E & 01 & \(0.2031 E\) & 05 & 0.678. 00 \\
\hline 771 & 0.3840E & 06 & 0.2866E & 17 & 0.1116 E & 01 & 0.2031 E & 05 & 0.6789 E 00 \\
\hline 772 & 0.3508E & 06 & \(0.2150 E\) & 17 & 0.1116 E & 01 & \(0.2031 E\) & 05 & 0.6789 Co \\
\hline 773 & 0.2939E 0 & 06 & 0.1115E & 17 & 0.1116 E & 01 & 0.2031 E & 05 & 0.6739 E 0 \\
\hline 774 & \(0.2655 E\) & 06 & 0.7958 E & 16 & 0.1116 E & 01 & 0.2031 E & 05 & 0.6789E 00 \\
\hline 775 & 0.3698E & 06 & 0.3208E & 17 & 0.1116 E & 01 & \(0.2031 E\) & 05 & 0.5726E 00 \\
\hline 776 & 0.3413 E & 06 & 0.2439E & 17 & \(0.1116 E\) & 01 & 0.2031 E & 05 & \(0.5726 E 00\) \\
\hline 777 & 0.3129 E & 06 & 0.1830 E & 17 & \(0.1116 E\) & 01 & 0.2031 E & 05 & \(0.5726 E 00\) \\
\hline 778 & 0.2655E 0 & 06 & 0.9490 E & 16 & 0.1116 E & 01 & 0.2031 E & 05 & \(0.5726 E 00\) \\
\hline 779 & \(0.2465 E\) O & 06 & 0.6775 E & 16 & 0.1116 E & 01 & \(0.2031 E\) & 05 & 0.5726E 00 \\
\hline 780 & 0.3413 O & 06 & 0.2773 E & 17 & 0.1116 E & 01 & \(0.2031 E\) & 05 & 0.4916 O \\
\hline
\end{tabular}

F3
F4 F5

781
782
783
\(784 \quad 0.2086 E 06\) \(0.5269 E 06\) \(0.5050 E 06\) 0.4830 E 06
0.4172 E 06
\(0.3952 E 06\)
\(0.5160 E 06\)
\(0.4940 E 06\)
\(0.4721 E 06\)
\(0.4062 E 06\)
0.3842 E 06
\(0.5050 E 06\)
\(0.4830 E 06\)
\(0.4501 E 06\)
\(0.3733 E 06\)
\(0.3513 E 06\)
\(0.4830 E 06\)
\begin{tabular}{|c|c|c|c|c|c|c|c|}
\hline \(0.2109 E\) & 17 & \(0.1116 E\) & 01 & \(0.2031 E\) & 05 & \(0.4916 E\) & 00 \\
\hline \(0.1582 E\) & 17 & \(0.1116 E\) & 01 & \(0.2031 E\) & 05 & 0.4916 E & 00 \\
\hline \(0.8204 E\) & 16 & 0.1115 E & 01 & \(0.2031 E\) & 05 & \(0.4916 E\) & 00 \\
\hline 0.5857E & 16 & \(0.1116 E\) & 01 & \(0.2031 E\) & 05 & \(0.4916 E\) & 00 \\
\hline 0.6647E & 17 & O.9636E & 00 & \(0.2352 E\) & 05 & 0.9236E & 00 \\
\hline 0.5055E & 17 & 0.9636E & 00 & \(0.2352 E\) & 05 & \(0.7236 E\) & 00 \\
\hline \(0.3792 E\) & 17 & \(0.9636 E\) & 00 & \(0.2352 E\) & 05 & \(0.9236 E\) & 00 \\
\hline \(0.1966 E\) & 17 & \(0.9636 E\) & 00 & \(0.2352 E\) & 05 & \(0.9236 E\) & 00 \\
\hline 0.1405E & 17 & 0.9636 E & 00 & \(0.2352 E\) & 05 & \(0.9236 E\) & 00 \\
\hline \(0.6281 E\) & 17 & 0.9636E & 00 & 0.2352E & 05 & 0.8682E & 00 \\
\hline \(0.4778 E\) & 17 & 0.9636E & 00 & \(0.2352 E\) & 05 & 0.8682E & 00 \\
\hline 0.3583 E & 17 & 0.9636E & 00 & \(0.2352 E\) & 05 & . \(0.8682 E\) & 00 \\
\hline O. 1858 E & 17 & 0.9636E & 00 & \(0.2352 E\) & 05 & 0.8682E & 00 \\
\hline \(0.1327 E\) & 17 & 0.9636E & 00 & 0.2352E & 05 & 0.85825 & 00 \\
\hline 0.5509 E & 17 & 0.9636E & 00 & 0.2352E & 05 & \(0.7527 E\) & 00 \\
\hline \(0.4190 E\) & 17 & 0.9636E & 00 & 0.2352E & 05 & 0.7527E & 00 \\
\hline 0.3142E & 17 & 0.9636E & 00 & \(0.2352 E\) & 05 & \(0.7527 E\) & 00 \\
\hline \(0.1629 E\) & 17 & \(0.9636 E\) & 00 & O.2352E & 05 & 0.7527E & 00 \\
\hline \(0.1164 E\) & 17 & \(0.9636 E\) & 00 & 0.2352E & 05 & 0.7527E & 00 \\
\hline \(0.5305 E\) & 17 & 0.9636E & 00 & \(0.2352 E\) & 05 & \(0.7227 E\) & 00 \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|}
\hline Obsv & F1 & F2 & & F3 & & F4 & & F5 & \\
\hline 801 & 0.4611 E 06 & \(0.4035 E\) & 17 & \(0.9636 E\) & 00 & 0.2352 E & 05 & \(0.7227 E\) & 00 \\
\hline 802 & 0.4281E 06 & \(0.3026 E\) & 17 & 0.9636E & 00 & \(0.2352 E\) & 05 & 0.7227E & 00 \\
\hline 803 & 0.3513 E 06 & 0.1569E & 17 & 0.9636E & 00 & \(0.2352 E\) & 05 & 0.7227E & 00 \\
\hline 804 & \(0.3293 E 06\) & \(0.1121 E\) & 17 & 0. 9636E & 00 & 0.2352E & 05 & 0.7227E & 00 \\
\hline 805 & 0.4501E 06 & \(0.4674 E\) & 17 & 0. 9636 E & 00 & \(0.2352 E\) & 05 & 0.6309E & 00 \\
\hline 806 & 0.4281E 06 & \(0.3554 E\) & 17 & \(0.9636 E\) & 00. & 0.2352E & 05 & \(0.6309 E\) & 00 \\
\hline 807 & 0.3952 E 06 & \(0.2666 E\) & 17 & 0.9636E & 00 & 0.2352E & 05 & \(0.6309[\) & 00 \\
\hline 808 & 0.3293E 06 & \(0.1383 E\) & 17 & 0.9636E & 00 & 0.2352E & 05 & \(0.6309 E\) & 00 \\
\hline 809 & 0.3074E 06 & 0.9871 E & 16 & 0.9636E & 00 & 0.2352 E & 05 & 0.6309 E & 00 \\
\hline 810 & 0.4281 E 06 & \(0.4185 E\) & 17 & \(0.9636 E\) & 00 & \(0.2352 E\) & 05 & \(0.5609 E\) & 00 \\
\hline 811 & 0.3952E 06 & 0.3183 E & 17 & 0.9636E & 00 & 0.2352E & 05 & 0.5609E & 00 \\
\hline 812 & 0.3733E 06 & \(0.2387 E\) & 17 & \(0.9636 E\) & 00 & \(0.2352 E\) & 05 & 0.5609E & 00 \\
\hline 813 & 0.3074 E & 0.1238E & 17 & 0.9636E & 00 & 0.2352E & 05 & 0.5609E & 00 \\
\hline 814 & 0.2854E 06 & 0.8842 E & 16 & 0.9636E & 00 & 0.2352E & 05 & \(0.5609 E\) & 00 \\
\hline 815 & 0.4007 O & \(0.3694 E 1\) & 17 & 0.9636E & 00 & 0.2352E & 05 & \(0.4913 E\) & 00 \\
\hline 816 & \(0.3733 E 06\) & \(0.2810{ }^{1}\) & 17 & 0.9636E & 00 & 0.2352E & 05 & 0.4918 E & 00 \\
\hline 817 & \(0.3513 E 06\) & 0.2108 E & 17 & 0.9636E & 00 & 0.2352E & 05 & 0.4918 E & 00 \\
\hline 818 & 0.2854E 06 & 0.1092E 1 & 17 & \(0.9636 E\) & 00 & 0.2352E & 05 & 0.4918 E & 00 \\
\hline 819 & \(0.2635 E 06\) & 0.7801E 1 & 16 & 0.9636E & 00 & 0.2352E & 05 & 0.4918 F & 00 \\
\hline
\end{tabular}

\section*{APPENDIX H}

NOMENCLATURE
\begin{tabular}{|c|c|}
\hline A & Area of cross section, \(\mathrm{m}^{2}\) \\
\hline \(B_{s}\) & Equation constant \\
\hline \(c_{d}\) & Drag coefficient \\
\hline \(c \& m\) & Correlation constants \\
\hline D & Diameter of tank, m \\
\hline d & Particle size or sphere diameter, m \\
\hline \(\mathrm{d}_{s}\) & Particle mean size, m \\
\hline \[
\frac{d u}{d y}
\] & Velocity gradient at a depth \(y\), \(\sec ^{-1}\) \\
\hline \(\frac{d u}{d x}\) & Rate of shear or velocity gradient, \(\mathrm{sec}^{-1}\) \\
\hline \(\mathrm{d}_{75}\) & Size for which 75\% of the bed material is finer, mm \\
\hline £ & Darcy-Weisbach fricion factor \\
\hline F & Shear force, N \\
\hline \(\mathrm{F}_{1}\) & Velocity factor \\
\hline \(\mathrm{F}_{2}\) & Power factor \\
\hline \(\mathrm{F}_{3}\) & Width factor \\
\hline \(\mathrm{F}_{4}\) & Depth factor \\
\hline \(\mathrm{F}_{5}\) & Submergence factor \\
\hline \(g\) & Acceleration due to gravity, \(\mathrm{m} / \mathrm{s}^{2}\) \\
\hline h & Depth of the water above the diffuser (submergence), m \\
\hline
\end{tabular}
\begin{tabular}{|c|c|}
\hline \(\mathrm{h}_{\mathrm{E}}\) & Head loss, m \\
\hline H & Liquid depth, m \\
\hline k & An empirical constant \\
\hline \(\mathrm{k}_{1}\) & A constant with dimensions of viscosity \\
\hline \(\mathrm{k}_{\mathrm{s}}\) & Roughness height, m \\
\hline L & Length of channel reach, m \\
\hline \(L_{1}\) & Tank length, m \\
\hline m & Constant \\
\hline M & Torque, dynes - cm \\
\hline n & A dimensionless constant with a value less than one \\
\hline P & Rate of power consumption, kw \\
\hline \(\mathrm{P}_{1}\) & Absolute inlet pressure, atmosphere \\
\hline \(\mathrm{P}_{2}\) & Absolute Outlet pressure, atmosphere \\
\hline \(\mathrm{P}_{\mathrm{e}}\) & Wetted perimeter \\
\hline \(\mathrm{P}_{\text {atm }}\) & Atmospheric pressure, \(101.3 \mathrm{kN} / \mathrm{m}^{2}\) or 14.7 psia \\
\hline \(\mathrm{P}_{\text {gage }}\) & Pressure gage reading, \(\mathrm{kN} / \mathrm{m}^{2}\) or psig \\
\hline \(\mathrm{P}_{\text {rota }}\) & Pressure fqr which the rotameter was calibrated, \(101.3 \mathrm{kN} / \mathrm{m}^{2}\) or 14.7 psia \\
\hline Qal & Air flo̧w rate under atmospheric pressure and at \(20^{\circ} \mathrm{C} \mathrm{m}^{3} / \mathrm{min}\) \\
\hline \(Q_{\text {rota }}\) & Observed air flow rate (reading from rotameter), \(\mathrm{m}^{3} / \mathrm{s}\) or cfm \\
\hline \(Q_{S T P}\) & Air flow rate ynder standard conditions, \(\mathrm{m}^{3} / \mathrm{s}, 20^{\circ} \mathrm{C}\) and \(101.3 \mathrm{kN} / \mathrm{m}^{2}\) or \(\mathrm{cfm} 20^{\circ} \mathrm{C}\) and 14.7 psia \\
\hline
\end{tabular}
\begin{tabular}{|c|c|}
\hline R & Hydraulic mean radius, m \\
\hline \(\mathrm{R}_{\mathrm{b}}\) & Radius of the spindle, cm \\
\hline \(\mathrm{R}_{\mathrm{c}}\) & Radius of the container, cm \\
\hline \(\mathrm{R}_{\mathrm{e}}\) & Reynolds number \\
\hline \(\mathrm{R}_{\mathrm{g}}\) & Gas constant, 8.314J/g. mol. \\
\hline S & Slope of channel \\
\hline \(S_{f}\) & Slope ifactor \\
\hline \(\mathrm{S}_{\mathrm{s}}\) & Specific gravity of the particles or sphere \\
\hline \(t_{1}\) & Time parameter with dimensions of time, sec. \\
\hline \(\mathrm{T}_{\text {i }}\) & Inlet temperature of air \\
\hline \(t_{\text {max }}\) & Mixing time, s \\
\hline Tope & Operating temperature, \({ }^{\circ} \mathrm{K}\) \\
\hline \(\mathrm{T}_{\text {STP }}\) & Standard temperature for which the roameter was calibrated. \(293.15^{\circ} \mathrm{K}\) \\
\hline u & Point velocity at any depth \(\mathrm{y}, \mathrm{m} / \mathrm{s}\) \\
\hline \(u_{m}\) & Mean velocity, m/s \\
\hline \(u^{\prime}\) \& \(v^{\prime}\) & Components of the fluctuating velocity in \(x\) and \(y\) directions, respectively \\
\hline \(U_{*}\) & Friction or shear velocity, m/s \\
\hline \(\mathrm{U}_{*}{ }_{C}\) & Critical shear or friction velocity, m/s \\
\hline ジ & Volume of tank, \(\mathrm{m}^{3}\) \\
\hline \(\mathrm{V}_{\mathrm{c}}\) & Critical velocity to start scour of particles, m/s \\
\hline
\end{tabular}
\begin{tabular}{|c|c|}
\hline \(\mathrm{V}_{\mathrm{mc}}\) & Competent mean velocity, ,/s \\
\hline \(\mathrm{V}_{\mathbf{s}}\) & Settling or fall velocity, m/s \\
\hline \(\mathrm{V}_{\text {sur }}\) & Surface Velocity, m/sec \\
\hline v & Linear velocity at any distance r, m/s \\
\hline W & Air mass flow rate, \(\mathrm{kg} / \mathrm{s}\) \\
\hline \(W_{g}\) & Weight of a grain, kg. \\
\hline X & Distance of diffusers from the sidewall of tank, m. \\
\hline \(y\) & Distance from the bed or depth of flow, m \\
\hline \(\dot{Y}_{\mathrm{m}}\) & Depth at which the point velocity is equal mean velocity, m/s \\
\hline & \(\cdots \cdots \cdots\) \\
\hline \(\beta\) & An experimental constant \\
\hline \[
\begin{aligned}
& \gamma \text { or } \\
& \gamma_{f}
\end{aligned}
\] & Specific weight of fluid or water, \(\mathrm{N} / \mathrm{m}^{3}\) \\
\hline \(\delta\) & Thickness of laminar sub layer \\
\hline \(\kappa\) & Von Karman Universal constant, 0.4 \\
\hline \(\ell\) & Prandtl mixing length \\
\hline \(\mu\) & Fluid dynamic viscosity, H.S/m² \\
\hline \(\mu\) ' & Viscosity parameter with dimensions of viscosity, poise \\
\hline \[
\mu^{\prime}\left(\frac{d u}{d x}\right)
\] & Non-Newtonian viscosity at shear rate of \(\frac{d u}{d x}\) \\
\hline \(\mu_{p}\) & Plastic viscosity, N.S/m \({ }^{2}\) \\
\hline \(\nu\) & Kinematic viscosity, \(\mathrm{m}^{2} / \mathrm{s}\) \\
\hline \(\omega\) & Angular velocity radians/s \\
\hline
\end{tabular}
\(\theta \quad\) Angle of repose
p or
\(\rho_{\mathrm{E}}^{\mathrm{S}}\)
Fluid or water mass density, \(\mathrm{kg} / \mathrm{m}^{3}\)

Bed material mass density, \(\mathrm{kg} / \mathrm{m}^{3}\)
Shear stress at any depth, \(N / \mathrm{m}^{2}\)
\({ }^{\tau}{ }_{\ell}\)
Laminar or viscous shear stress, \(N / \dot{m}^{2}\)
Bed shear stress, \(N / \mathrm{m}^{2}\)
\({ }^{\tau}\) oc
Critical bed shear stress, \(\mathrm{N} / \mathrm{m}^{2}\)
Turbulent shear stress, \(M / \mathrm{m}^{2}\)
Yield stress, \(\mathrm{N} / \mathrm{m}^{2}\) or dynes/ cm \({ }^{2}\)
Specific weight of bed material in the fluid, \(N / \mathrm{m}^{3}\)
Specific weight of bed material, \(N / \mathrm{m}^{3}\)

\section*{Appendix I}

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[^0]:    ${ }^{1}$ Numbers in brackets are references listed in the References.

