# Issues involved in the empirical testing of a multivariate predictive system. 

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ISSUES INVOLVED IN THE EMPIRICAL TESTING OF A MULTIVARIATE PREDICTIVE SYSTEM
by
ROBERT T. FORSYTH
B.A., Brock University, 1973

A Thesis
Submitted to the Faculty of Graduate Studies through the Department of Psychology in Partial Fulfillment
of the Requirements for the Degree of
Master of Arts at the University of Windsor

Windsor, Ontario, Canada
1974

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## ABSTRACT

This study utilized previously collected data from two samples of 187 and 184 college students to investigate problems inherent in multivariate data analysis as well as patterns of cannabis
use. The multivariate issues considered were: the effects of the
distributions of the scores of the variables; the use of factor
scores as well as raw data in regression analysis to facilitate
"conceptual cross-validation"; effects of sequential orthogonalization
on regression equations; and the utility of criteria exhibited by
factor analyses and canonical correlations. It was found that in
the field of marijuana research, the usual criterion - frequency of
use, was not suitable both for measuremeant and inferential reasons.
Using canonical analysis two patterns of use were found -- moderate
and abnormal, which were related to social and personality predictors
respectively.

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Chapter I
Introduction

One of the major aims, if not the only aim of psychology, is useful and accurate prediction of human behaviour. The approaches used vary with the particular behaviours studied, ranging from the study of minute reflexes, to overall life patterns, carrying with them constructs from conditioned stimuli to self-concept. For behaviour of medium complexity, the social learning approach, developed by Rotter and his colleagues (eg. Rotter, 1954; Rotter, Chance \& Phares, 1972) or a similar approach may be most useful, provided that constructs are made sufficiently clear. It is the intent of this thesis to operationalize some of these constructs, to investigate methods of testing a predictive system, and to consider specific issues that pertain to this system and generally to complex multivariate data sets.

In this study the behaviour of interest is marijuana use, specifically in college students. Studies on the drug have proliferated, perhaps in keeping with greater public interest in its use and abuse in the last few years. Although much of the literature deals with the physiological and psycho-pharmacological properties of cannabis, the psychological viewpoint demands an exploration of social and personality correlates and the consequent predictions of who uses the drug, and with what effects. Recent studies by Jessor (Jessor, Jessor \& Finney; 1973) and Sadava (1974b) have had some success in this task, by viewing marijuana use as a functional behaviour, "caused" by variables both of an interpersonal (environmental) and of an intrapersonal (personality) nature, and as an ongoing process
changing over time. This conception of the problem may be traced back to Rotter's social learning framework, and a short description of this approach (based mainly on Applications of a social learning theory of personality, chapter 1, 1972) would make the later work more meaningful. Rotter's Social Learning Theory

In general, Roter's Social Learning Theory utilizes the ideas of expectancy and the empirical law of effect, as underlying constructs emphasizing the interaction of the individual and his meaningful environment. Thus, the approach is much more cognitive in nature than most other types of learning theory. Specific efforts are directed to determing the subject's perceptions of his goals and his subjective: expectancy that they will be fulfilled according to his own past experiences. Needs and goals are social in nature since they are initially fulfilled by others. Behaviour becomes available if it has led to reinforcement, either directly, or through observation and modelling. Generalization takes place, with functionally related behavious/reinforcers leading to the same goals/ satisfactions. Cognitions are more important in this theory than others since the generalization may be of symbols and their referents. The general formula used to predict behaviour is: $B P=f(E \& R V)$ where $B P$ is the probability of the behaviour, relative to other behaviours in the specific (psychological or perceived) situations; E is the expectancy or subjective probability of a particular reinforcer occurring as a result of a certain behaviour; and RV, the reinforcement value, is the relative preference for a given reward with expectancies for all rewards kept constant.

So, for instance, the potential for marijuana smoking to occur, in
college, in relation to peer approval, is a function of the expectancy of the occurance of peer approval, following marijuana smoking in college and the value of peer approval. This is a specific example, and may be expanded by including other reinforcements, both positive and negative, other expectancies etc.

Jessor's Approach
Jessor has taken Rotter's system, developed in a clinical setting, and applied it to studies on alcohol use (eg. Jessor, Carnan, \& Grossman, 1968; Jessor \& Finney, 1973). Marijuana use is thought of as "problem behaviour... considered to be purposeful, goal oriented or functional (pl, 1973)". Variables have been classified into structures and systems by Jessor: a personality system consisting of motivational instigation, belief and personal control structures; a perceived environment system with these and other behaviours ranging from closely related to "normal". His methodology consists of administering questionaires at two or more points in time, using multiple-regression techniques, and gain scores (over time), on social and personal variables to increase "accounted-for" variance. He was able to assign users and non-users to their respective groups with $73 \%$ accuracy and to achieve multiple R's of up to .39 (Jessor, et $\mathrm{a} 1,1973$ ).

## Sadava's Approach

Sadava's approach has focused in on marijuana use specifically. One major problem in marijuana research is that while ultimate clinical interest may lie in determining what leads to abuse, research has been defined in terms of use versus non-use. Even this distinction is made in different ways by various researchers. For instance the category of "light use" ranges from one to twenty experiences, and there are at least twenty-eight
labels for use patterns (Sadava, 1974a). To cut down this confusion, Sadava designed a short group of questions, with four stages of use (Sadava, 1972) with the additional stages of non-user and "Have stopped" added (Sadava 1974b). For the non-user and the four user stages this scale has Guttman-scale type properties. Continuing to refine criteria, Sadava uses the following measures; frequency of use, time span as a user, contexts of use and adverse consequences of use in a sample comprised of drug users. These measures have average intercorrelations of .23 with a maximum of . 54 (Sadava, 1974b), indicating relationships amongst criteria, and the possibility of patterns of drug use. The complex relationships between behaviour and predictors may be obscured by a poor choice of criterion. Meaningful correlate may be hidden from our investigation if the criterion is poorly defined, or if its scale properties are ignored.

Sadava's schema of variable systems may be seen in Figure 1. The major difference between the systems of Sadava and Jessor is that in the former cognitive functions are conceptualized as a set of predictors of drug use (by Sadava), and as being predicted by other systems of variables. Using his system Sadava (1974b) has found multiple $\mathrm{R}^{\prime} \mathrm{s}$ of up to .62 for variables predicting criteria measured at the same time, and multiple $R$ 's up to . 58 for longitudinal analyses with samples of drug users. Both Jessor and Sadava use longitudinal analyses, and often utilize both the scores on variables at the earlier point in time, and change scores in these variables, to predict behaviour at the second point in time.

Social Learning Theory: Applied to Complex Operations
In the analyses of both these researchers, the variables have been analysed bit by bit, using sub groups of predictor variables to predict

Simplified Non-recursive

## Social Learning Model

## Behavior

2. Cognitive Functions
(eg. fear, coping)
3. Criteria
(eg. range,
consequence consequences)


## Proximal Causes

Distal Causes
3. Personality
(eg. locus of control, trust)
each criterion, then another sub group to predict each criterion and so on. Perhaps this is due to a lack of a statistical framework, or of a notational system that would allow easy manipulation of the large number of variables and extensive data. Thus the first stage of this thesis is the expression of Sadava's and Jessor's systems in a notation that allows manipulations of variables in order to deduce and to subject to verification, hypotheses about relationships between predictors and criteria. This is a necessary step since some of the terms used (eg. 'related structures', 'covary with other kinds of problem behaviours') and also relationships between variables (eg. $\mathrm{BP}=\mathrm{F}(\mathrm{E} \& \mathrm{RV})$ ) are hard to operationalize. Furthermore, although the underlying principles assume an integrated predictive system, the tendency is to examine concepts and variables in isolation, and with less than complete thoroughness.

## Notation

Let $B_{q t n}$ be a criterion observation [section 1 of Figure 1] for individual $\mathrm{n}(\mathrm{n}=1, \ldots, \mathrm{~N})$ at time $\mathrm{t}(\mathrm{t}=1, \ldots, \mathrm{~T})$ on criterion $\mathrm{q}(\mathrm{q}=1, \ldots, \mathrm{Q})$ which after appropriate transformations (s) is in Z-score form ( $\operatorname{Exp}\left(\mathrm{B}_{\mathrm{qtn}}\right)=0$, $\left.\operatorname{Var}\left(\mathrm{B}_{\mathrm{q} \mathrm{tn}}\right)=1\right)$. Similarly, let $\mathrm{C}_{1 \mathrm{tn}}(1=1, \ldots, \mathrm{~L})$ be a normalized variable for cognitive functions [section 2 of Figure 1]; $P_{m t n}(m=1, \ldots, M)$ be a normalized variable for personality characteristics [section 3 Figure 1] ; $E_{k t n}(k=1, \ldots, K)$ be a normalized variable for perceived environmental data [section 4 Figure 1]; and $D_{s t n}(s=1, \ldots, S)$ be a normalized variable for demographic data [section 5 Figure 1].

Let $\Delta\left(\mathrm{B}_{\mathrm{q} t \mathrm{n}}\right)$ be a normalized variable corresponding to the unpredicted part (i.e., change over time-delta) of $\mathrm{B}_{\mathrm{qtn}}$ from $\mathrm{B}_{\mathrm{q} 1 \mathrm{n}}$. Similarly, $\Delta\left(\mathrm{C}_{1 \mathrm{tn}}\right)$, $\Delta\left(P_{m t n}\right), \Delta\left(E_{k t n}\right)$ and $\Delta\left(D_{s t n}\right)$.

Let $\mathrm{F}_{\mathrm{rn}}(\mathrm{B})$ be the factor score for the r 'th factor $(\mathrm{r}=1, \ldots, \mathrm{R})$. for individual $n$, taken from the $\mathrm{B}_{\mathrm{q} t \mathrm{n}}(\mathrm{D})$.

Let $\Gamma_{m t_{n}}^{\rho}(E+C)$ denote a normalized variable consisting of that covariance-free part (gamma) of $P_{m t n}$ remaining after the variance due to the E and C variable systems is partialled out, and so on for combinations of $P, E, C$ and $D$.

Let $R_{B q . E C P}$ be the multiple correlation between the fth variable of $B$ and the variables of $E, C$ and $P$.

Thus using the above notation for measurement times 1 and 2, it is hypothesized that an equation of the following general form leads to better estimations of criteria at time 2 and higher multiple R's than obtained previously:

$$
\begin{aligned}
\hat{B}_{q 2 n}= & \sum_{s=1}^{S} r_{q s} F_{s n}\left(D_{s 1 n}\right)+ \\
& \sum_{k=1}^{K} r_{q k} F_{k n}\left(\Gamma_{k \ln }^{\varepsilon}(D)+\Gamma_{k 2 n}^{\Delta E}(D)\right)+ \\
& \sum_{m=1}^{m} r_{q m} F_{m n}\left(\Gamma_{m 1 n}^{P}(D+E)+\Gamma_{m 2 n}^{\Delta P}(D+E)\right)+ \\
& \sum_{i=1}^{L} r_{q 1} F_{1 m}\left(\Gamma_{11 n}(D+E+P)+\Gamma_{12 n}(D+E+P)\right) \\
R_{B_{q} \cdot E C P D}= & R_{\hat{B} q 2 n} B_{q 2 n} .
\end{aligned}
$$

The score for the n'th person, on the q'th criterion, at time 2 , may be estimated from a linear composite comprised of the sum of the variables in each system weighted such that the predictors are orthogonal. Thus in this case, the estimated criterion score is the sum of the factor scores for demographic data weighted by first order correlation coefficients with
the criterion, plus the sum of the personality factor scores, free of covariance with demographic data, and weighted by the correlations with the criterion, plus the percieved environment factor scores similarly partialled (of both demographic and personality scores) and weighted, plus cognitive function factor scores treated in the same manner.

Problems with this Predictive System
In the present study several important limitations exist and should be noted beforehand. Firstly, the model calls for all variables to be normally distributed, zero mean, and unit variance. This condition may not be met because of several considerations in the scales involved; measures may be nominal or at best polychotomous with very discrete values found for what may or may not be underlying continuous variables; some variables may be extremely skewed, and even with transformations may not really resemble a normal distribution.

A second deviation from the model relates to the fact that the various systems of variables should include all non redundant measures in the domain of interest. This condition is not fulfilled as: (a) those measures may not at this point in time exist and (b) only a limited subset (hopefully representative) can be administered in the time permitted.

Another problem exists in that the model is linear in nature whereas either the real or theoretical variables may combine multiplicatively in the form of moderators to other variables, or in other non-linear combinations (eg. curvilinear). This must be kept as a consideration in the research, but as the non-1inear models tend to be limited operationally more or less to small numbers of variables, the present work will (hopefully) serve as a good first approximation.

Other problems exist in the nature of the instruments used and the type of behaviour studied. In the latter case, marijuana use is, of course, illegal and therefore responses to questions about its use can be seen as incriminating. King (1972) reports that anonymous and identifiable : questionnaires on this subject do not significantly differ on reported data, however this does not mean there will be no difference between actual behaviour and reported behaviour due to some fear of exposure. With respect to questionnaire studies in general, we must consider the possibilities of response styles and sets (eg. Jackson, 1967), and also false content through misconceptions on the part of the subject. The latter is more easily dealt with, in that according to the assumptions of the Rotter, Jessor and Sadava models behaviour is determined by subjective expectancies, values, etc. not merely objective facts, and distortion of this kind do not render the information invalid.

To compare the possible distortion of responses on the questionnaire, it is best to consider that the data have two different logical sequences. The first sequence is that of cognitive functions followed by perceived environment, personality and demographic data, ordered in terms of decreasing proximity to the behaviour concerned. The subjects' own perceptions will have the most weight and be least subject to cumulative response biases.

The second sequence will be that of demographic data, personality, perceived environment, and cognitive function, in decreasing order of objective verifiability, as opposed to proximal subjectivity.

## Specific Areas of Investigation

There are four specific issues that must be examined in dealing with
the model. These are: distributional properties of predictor and criterion variables; the use of raw data vs factor scores; the use of two sequences of orthoganalization, ie. starting with cognitive functions, and starting with demographic variables; and the patterns of behaviour criteria.

## Distributions of the Variables

It is extremely important that we examine the distributions of scores on the variables we use before interpreting results from statistical analyses, since we may be misled by our results if assumptions necessary to the analysis are not met, or if more useful approaches to data analysis are ignored due to a lack of information. This warning takes on more importance when the variables haven't been used extensively in other research, and/or severa1 "non-robust" (requiring stringent assumptions for use and interpretation) statistics such as stepwise regression or canonical correlation are to be used. For instance, we might have a distribution with a few extreme values at each end, being correlated with another variable that also has extreme values. If the extreme values "match", there will be a very high correlation that is not reflected at all by the other variable pairs. Another possibility is that the two variables have a parabolic relationship, or that one variable is related to the logarithm of the other. In both cases, the correlations between the variables would be very low, and the true relationships found only by a theoretical or, more likely, an empirical investigation of the univariate and bivariate frequency distributions of the variables (see Carroll, 1967). As the first part of the exploration of this model, these distributions will be examined.

## Raw Data vs Factor Scores

Since the scales for this investigation were chosen on the basis of availability, or constructed to measure a specific area, there may be both a large overlap in the domain of measurement, and a great deal of variance "superfluous" to the model. If the variables are of this nature, the use of a multiple regression technique may lead to different weights for the variable in each sample, even though the particular underlying factors don't change from sample to sample. Cooley and Lohnes (1971) point out that "chance" is an important consideration in multivariate analysis, and since we may have several variables contributing almost the same variance, chance could determine which variable is chosen (the covariance with similar variables being partialled out and consequently not appearing as significant). This process may have more importance than seems readily apparent since we will be influenced in our model building and generalization by the labels or names attached to the "significant" variables, and may draw the wrong inference about the meaning of a variable's loading on the regression equation.

One solution to this problem is to assure ourselves, prior to the dependence analysis (eg, multiple regression), that we have predictors, whose domains, empirically, do not overlap greatly. This may be achieved by orthogonalization of our predictors. We may also collapse the number of variables into a smaller number of factors. Using this method, we may substantiate the findings of analyses of raw data, and more easily infer from the measured variable the underlying trait or cause.

## Sequence of Data Entry

When orthogonalizing the data sequentially, the first variables may
retain greater meaningful variance than later variables because of the method itself. The last variables will, most likely, have little or no correlation with the criterion, whereas the corresponding original variable may, in reality, be highly related to the criteria. Ideally every variable should have equal chance to covary with criteria, but this leads to an enormous number of analyses to include each sequential combination. Given these circumstances, together with the theoretical reasons discussed previously for the different types of response sets and kinds of verifiability two sequences of orthogonal predictors will be used: Functions-in which the function variables are entered first (the sequence of proximity); and Demo. - in which the demographic variables are entered first (the objective verifiability order). These sets will be examined to determine what differences exist due to ordering effects.

Criteria Patterns
Considering Sadava's findings (1974b) concerning the relationships between criteria, and the different predictors useful in each case, it is important to look at the criteria carefully, to examine specifically their inter-relationships (eg. by factor analysis), and to find out whether different sets of predictors predict different patterns of criteria (using canonical correlation). Using this information we can evaluate the criteria as to their reliability and usefulness. In addition, a methodology becomes available to ascertain predictive systems for genuine, multidimension: patterns of use.

## Chapter II

Method
Subjects
The ruestionnaires were filled out by first and second year students enrolled full-time at Brock University, St. Catharines, Ont. In the 1972-73 academic year. Four hundred and eighty Ss completed questionaires in Nov. 1972; and of these 371 filled out the questionnaire in Mar. 1973. The ages of the Ss ranged from 16 to 74 but most were under 26. Fifty-five per cent of those responding twice were female.

The group (371) was split into two samples randomly, Sample 1 was 187 Ss and Sample 2 was 184. Scores were standardized within samples, but all other estimated parameters. (e.g. correlations, factor loadings, etc.) were obtained from Sample 1 and applied to Sample 2.

## Questionnaire

Table 1 lists the scales used, number of items, format and source, if other than Sadava ( $1972,1973,1974 \mathrm{~b}$ ). This table is organized by variable systems, i.e. behaviour, cognitive functions, perceived environment, personality, and demographic data, and excludes some scales not used in the present study.

Major Statistics
Univariate and Bivariate Distributions
Descriptive statistics and frequency distributions were found for each scale, using data before standardization. Scattergrams were constructed for ten predictor variables (standardized) with each of the four criterion variables, to give an indication of the types of

TABLE 1
Variables Used

| System/ Variable | Number of Items | Item Format | Source** |
| :---: | :---: | :---: | :---: |
| Criteria |  |  |  |
| System |  |  | ...... |
| Consequences | 17 | 3 point scale |  |
| Range | 19 | yes/no |  |
| Time Span | 1 | "how long ago" |  |
| Frequency | 1 | 非 of occasions |  |
| Cognitive |  |  |  |
| Functions | .......... |  | ...... |
| Total Positive | 14 | 3 point scale |  |
| Instruemental | 6 | 3 point scale |  |
| Coping | 6 | 3 point scale |  |
| Total Negative | 10 | 3 point scale |  |
| Ideological | 4 | 3 point scale |  |
| Fear | 6 | 3 point scale |  |
| Percieved |  |  |  |
| Environment |  | . | . |
| Social Support | 10 | 4 point scale |  |
| Social Sanct'n | 6 | 3 point scale |  |
| Availability | 2 | 5 point scale |  |
| Parental Model | 16 | 4 point scale |  |
| Sibling Model | 5 | 4 point scale |  |
| Personality | .......... | ......... | ...... |
| Peer Confor'y | 10 | 3 point scale | Lin (1972) |
| Peer Indep. | 10 | 3 point scale | Lin(1972) |
| Peer Anticon'y | 10 | 3 point scale | $\operatorname{Lin}(1972)$ |
| Family Con'y | 10 | 3 point scale | Lin(1972) |
| Family Indep. | 10 | 3 point scale | Lin(1972) |
| Family Anti. | 10 | 3 point scale | $\operatorname{Lin}(1972)$ |
| To1. Drug Use* |  | 10 point scale |  |
| Att. To Devian | 15 | 10 point scale |  |
| Total Risk |  | 9 point scale | Jackson(1972) |
| Physical Risk | 2 | 9 point scale | Jackson (1972) |
| Financial Risk | 2 | 9 point scale | Jackson(1972) |
| Social Risk | - 2 | 9 point scale | Jackson (1972) |
| Ethical Risk | 2 | 9 point scale | Jackson (1972) |

Table 2 continued

| System/ Variable | Number of Items | Item Format | Source** |
| :---: | :---: | :---: | :---: |
| IE Locus of Con | 23 | Forced Choice | Rotter (1966) |
| IE personal | 9 | Forced Choice | Mirels (196) |
| IE political | 4 | Forced Choice | Mirels (196) |
| Trust | 25 | 5 point scale | Rotter (1966) |
| Personal Trust | 6 | 5 point scale |  |
| Political Trust | 8 | 5 point scale |  |
| Interper'1 Al'n | 10 | 5 point scale | Keniston(unp) |
| Social Alien'n | 5 | 5 point scale | Keniston(unp) |
| Moral Judge.* | 35 | mixed |  |
| Religiousity* | 3 | mixed |  |
| Delay Grat'n | 4 | 5 point scale | Stumphauser (1972) |
| Time Pers've | 5 | number of months | Shybut (1968) |
| Demographic |  | -•••••• | -•••• |
| Sex * | 1 |  |  |
| Age \% | 1 |  |  |
| Social Econ.* | 1 |  |  |
| Yr in College* | 1 |  |  |
| Poli. Orien'n* | 1 |  |  |
| Residence* | 1 |  |  |
| Reference Gr.* | 1 |  |  |
| Height * | 1 |  |  |
| Weight * | 1 |  |  |
| Self Des. Obs. ${ }^{*}$ | 1 |  |  |
| Exp. GPA * | 1 |  |  |
| GPA Difference* | 1 |  | - |

*Not repeated Spring, 1973
** If other than Sadava
bivariate distributions present in the data.

## Orthogonalization of Data

Delta and gamma scores. In order to arrive at a set of mutually independent predictors several types of transformation are needed. First, we must get an estimate of change-over-time scores. Given two sets of scores on the same variable, from the same subjects, we can paxtial out of the later score, the variance accounted for by the score taken at a point earlier in time (e.g. Jessor et a1, 1973). Thus, starting with two related scores, we obtain a base score, and an independent estimate of change, a delta ( $\Delta$ ) score. Delta is estimated by Ferguson's formula $\Delta=\left(Z_{1}-r_{12} Z_{2}\right) / \sqrt{1-r_{12}^{2}} \quad(1971, p$. 387) where $Z_{1}$ is the score at the first point in time, $Z_{2}$ is the same subjects' score at second point in time, and r12 is the correlation between $Z_{1}$ and $Z_{2}$ over all subjects.

A generalization of the above formula estimates a score that is Independent of more than one variable (this may be done across time, as for, or with other scores from a larger test battery). If we wish an estimate of this covariance-free score, a gamma ( $\Gamma$ ) score, we may use the following formula: $\Gamma_{1.23 \ldots n}=\left(Z_{1}-\sum_{m=2}^{n} r_{m} Z_{m}\right) / \sqrt{1-\sum_{1 m}^{2}} r_{1 m}$ [see appendix A for proof], where $Z_{1}$ is our variable of interest, $Z_{2}, \ldots, Z_{n}$ are the covariates, $r_{1 m}$ is the correlation between the $Z_{1}$ scores for $Z_{m}(m=2, \ldots, n)$ over all subjects. These scores will have $E(\Gamma)=0, \operatorname{VAR}(\Gamma)=1$ and will tend to a normal distribution.

Principal components. The third type of transformation needed is a principal components factor analysis, producing appropriate
factor scores. Since we are interested in linear composites with the characteristics of mutual independence, interpretability and completeness, the proper procedures for this factor analysis are: the use of unities in the main diagonal; an adaptation of the scree test (see Cattell, 1952, for a discussion of this criterion) to determine the number of factors retained; and a varimax rotation of those factors.

We must use unities in the diagonal instead of estimates of communality since our data are not being used to infer underlying structure, but rather, are being described by the factor scores. The question of establishing the number of variables to be rotated is more complex. It may be resolved by considering the nature of the factor structure and the communality of a variable. We may regard communality as the square of a variable's multiple correlation with all the extracted factors. Thus, if each variable has a high communality after a certain number of factors has been extracted, we may assume that each of the common and unique factors has been obtained. For example, if after five factors are extracted, the communality of a variable is .78 , there remains to be accounted for, only $22 \%$ of the original variable's variance in all the remaining factors.

We can always (with unities in the diagonal) account for a11 of the variance by taking as many factors as variables, but we most like1y will have "error" factors, due to faulty measurement, discrete scale values etcetera. A procedure that tends to eliminate these factors is Catte11's scree test (Cattell, 1952). A sharp drop-in eigenvalues after relatively high eigenvalues means the following eigenvalues may be neglected. The original argument by cattell
recommended both a scree test, and a minium eigenvalue over 1.0 , however, since we are using principal components, the later requirement may be dropped, and the requirement of high communalities added.

The varimax method of rotation is used so that each factor can be most easily identified as related to a few (and if possible only one) variables. Varimax simplifies factors, as opposed to variables (Mulaik, p.259, 1972), and this means that the "output" of our transformation will tend to be more easily interpretable than if we used either a variable-simplifying or both factor and variable simplifying rotation.

## Stepwise Multiple Regression

This technique (SMR) is really a combination of regression and factor analysis (Mulaik, p.412, 1972). The first step is to correlate the criterion with the criterion as the variable in the regression equation. The factor collinear with this variable is extracted from the predictor matrix, and a residual correlation matrix is obtained. Then the variables (or factors since this factor analysis method -that of Cholasky [Mulaik p.412] maintains a correspondence between factors and variables), remaining are correlated with the predictor, the corresponding factor extracted, leaving a residual matrix, and so on. At each step a variable is added to (in occasional circumstances removed from) the regression equation, and the multiple correlation is increased.

This process of adding (and/or removing) variables can continue until all the variables are in the equation, however, as with other factor analytic procedures, later factors (i.e. variables in Cholesky method) miy be unique or error torms. Since we are daling also with
regression, the unique factors that do not correlate with the criterion, may be, for practical purposes, considered error. Either error may increase the multiple correlation, but to such a small extent that, given the probability of measurement error, the predictive utility of the equation is diminished. Cooley and Lohnes (p.56-57, 1971) point out that SMR can capitalize on chance to a large extent, and care must be taken to replicate this procedure on another sample(s). The replicated $R$ may shrink appreciably if too many variables are allowed in the original equation. For our purposes, we may use an $E$ ratio (or an equivalent $t$ test) to determine whether a variable should be added to the equation. This F ratio is computed as the square of the ratio of regression coefficient and its standard error (SPSS, 1970). Orthogonal Predictor Variables

If the correlation matrix of predictor variables is an identity matrix (i.e. the variables are correlated), the regression equation weights may be obtained directly from simple correlations with the criterion (Mulaik, p.404, 1972). Furthermore, the square of the multiple correlation is the sum of the squares of the simple correlation with the criterion. If we have orthogonal predictor variables, the order of entry of these variables into a stepwise MR is the same as the rank order of the absolute values of the correlation coefficients, and the SMR is not necessary. In practice, a SMR can be useful in these circumstances since the correlation with real data probably will not be an exact identity matrix. Even if our regression weights are from a non-orthogonal group of predictors, Cooley and Lohnes (p.56, 1971) point out that sample predictor-criterion correlation
coefficients of the first order may yield better predictive utility than regression weights from more "sophisticated" processes.

## Canonical Corrclation

Stepwise Multiple Regression may be considered a special case of canonical correlation. The problem of canonical correlation $1 s$ to find relationshi ps between a set of predictor varlables and a set of criterion variables (in SMR we have a set of one criterion variable). In general, we ask if there is a combination of predictors $X$ (a pattern) that has a high correlation with a combination or pattern of criterion $Y$ variables. To do this we find a set of weights for the predictors such that the composite variable $\left(W_{1}\right)$ is maximally correlated to a composite variable $Y_{1}$ made up of a weighted combination of the' $Y$ variables. A factor corresponding to $W_{1}$ is extracted from $X$ which leaves the residuals $X_{r}$ unrelated to $W_{1}$, in the same manner as the residual matrix is found in SMR. The composite $V_{2}$ is treatedin the same way to produce a residual matrix $Y_{r}$. This process is repeated producing (usually) $\underline{m}$ set of weights, where $\underline{m}$ is the number of variables in the smaller of the predictor and criteria groups (see Van de Geer, 1971). We must then evaluate the sets of weights called canonical variates to find which are significant. The canonical correlation coefficient $R_{c}$ can easily be misinterpreted. It is not the correlation or overlap between $X$ and $Y$ but between the linear composites $W$ and $V$. To evaluate the "overlap" or shared variance of the two sets, we may use a statistic $R_{d}$, a redundancy coefficient discussed by Stewart and Love (1968). For each canonical correlation there are two redundancy coefficients, one for the $X$ variables given the composite $V$ from the $Y$ variables (i.e. $R_{d x}$ ) and one for the $Y$
variables given the composite $W$ from the $X$ variables (i.e. $R_{d y}$ ). $R_{d x}$ is calculated as the proportion of variance extracted by the factor ( $W_{n}$ ) times the proportion of shared variance $\left(R_{c n}\right)$ between the factor and corresponding canonical factor of the other battery (Cooley and Lohnes, p. 170, 1972). Thus we square the weights of the $X$ variables, divide by the number of $X$ variables, and multiply by the canonical correl ation The canonical correlation analysis can be useful in exploring criterion patterns however it should be used in conjunction with other measures such as the multiple correlation of each criterion (Cooley and Lohncs, p.176, 1972), chiefly because of the complexity of the procedure, and the possible misinterpretation of results.

## Summary of Programmes and Formulae

1. Univariate Distributions - SPSS (1970), subroutine CODEBOOK
2. Bivariate Distributions - BASIS (1971), subroutine Plot.
3. Delta Score $-Z 1 Z 2=\left(Z_{1}-r_{12} Z_{2}\right) / 1-r_{12}^{2}$. A Fortran programme was written and an example given in Appendix B.
4. Gamma Scores: $=\left(Z_{1}-\left(r_{1 m} Z_{m}\right)\right) / 1-r_{1 m}{ }^{2}$. This was done by a Fortran programme in Appendix B.
5. Principal Components Analysis: Both SPSS (1970), subroutine FACTOR, and SSP factor analysis (1970: p.429) were used, with several sets of data run on both to ensure accuracy (identical results to fifth significant digit).
6. Correlation Coefficients. SPSS (1970), subroutine PEARSON CORR was used and compared to SSP subroutine CORRE.
7. Stepwise Mutiple Regression: SPSS (1970), subroutine REGRESSION, and SSP programme for stepwise multiple regression (p. 419) were used and compared.
8. Canonical Correlation: SPSS (1970), subroutine CAN CORR was used, there were no suitable programmes for comparison.

## Results

## Univariate Distributions

The raw data may be grouped in sets of variables with common forms of frequency distribution. These distributions seem to approximate: the normal, truncated normal, superimposed two population normal, the Poisson, the rectangular and the dichotomous or binomial distributions. Table 2 gives examples of variables from each group, descriptive statistics and type of distribution.

## Bivariate Distributions and Correlations

Selected pairs of standardized variables were plotted to check for usual bivariate distributions. None of the distributions seemed curvilinear (e.g. U shaped). The scattergrams including Range seemed to indicate that extreme values (for Range) were depressing the correlations, and suggested that correlation with Log (Range) might be considerably higher. Scattergrams are included as Figure 2.

Correlations matrices between the criteria and each of the predictor variables may be found in Appendix C. There is a matrix for each of the Raw, Functions and Demo. modes of analysis for Sample 1 and for Sample 2. Transforms

The resulting variables, processed in either direction, i.e. partialli:g out covariance of functions from social, of functions and social from personality etc; and partialling out covariance of demographic from personality variables etc., were relatively easily identified, having

## TABLE

Univariate Distributions

| Variable** | Central Moments * |  |  |  | Range | Quartile | Type of Distribution |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Mean | Variance | Skewness | Kurtosis |  |  |  |
| Frequency | 17.976 | 6095.527 | 10.940 | 133.106 | 999 | 0/0/10 | Poisson/ |
| Time Span | 19.505 | 648.855 | 1.365 | 1.860 | 144 | 0/4/36 | Dichotomous <br> Poisson |
| Range | 3.585 | 13.238 | 2.725 | 12.793 | 33 | 1/2/5 | Poisson |
| Consequen. | 31.118 | 116.599 | 0.400 | -1.095 | 34 | 22/30/41 | Rectangular |
| Social Supp | 19.865 | 36.436 | 0.406 | -0.572 | 28 | 15/20/24 | Bimodal Nor. |
| Avail. | 8.435 | 2.436 | -1.382 | 2.536 | 8 | 8/9/10 | Trunc. Nor. |
| Sib. Model | 7.557 | 5.433 | 1.675 | 4.733 | 15 | 6/7/9 | Trunc. Nor. |
| Total Pos. | 22.862 | 27.451 | 0.491 | 0.156 | 28 | 19/22/26 | Trunc. Nor. |
| Ideo. Neg. | 6.470 | 3.432 | 0.799 | 0.159 | 8 | 5/6/8 | Trunc. Nor. |
| Fam. Conf. | 22.849 | 6.501 | 0.053 | 0.079 | 15 | 21/23/25 | Normal |
| Att. To Dev. | 36.891 | 81.661 | 0.069 | 0.472 | 58 | 31/37/43 | Normal |
| Total Risk | 38.192 | 89.906 | 0.052 | 0.010 | 54 | 32/38/44 | Normal |
| I.E. | 10.593 | 24.697 | -0.014 | -0.585 | 22 | 7/11/14 | Normal |
| Exp. GPA | 73.843 | 42.218 | 0.511 | 1.014 | 41 | 70/75/80 | Disc. Nor. |
| S. D. Obes. | 3.114 | 0.530 | -0.047 | 0.370 | 4 | 3/3/4 | Normal |
| Sex | 1.445 | 0.248 | 0.220 | -1.952 | 1 | 1/1/2 | Dichotomous |

* Based on 371 observations
** Spring variables except Att. to Dev.







Frequency
high loadings on principal components analyses. Table 3 includes rotated factor loadings, communalities, and lists new variable names for the two modes of factoring.

## Factor Analysis of Behaviour

In both Samples 1 and 2, frequency is unrelated to the other criteria, with time and range loading together. Table 4 presents rotated loadings and eigenvalues .

Stepwise Multiple Regression Analysis
A total of 24 SMR's were calculated. Tables 5 through 10 present the variables with significant Beta weights, the cumulative variance in thousandths and the final multiple correlation coefficient. Table 11 presents a $2 \times 3 \times 4$ breakdown of these Multiple correlations, and average correlations (using Fisher's $Z$ transformation) for each classification.

## Canonical Correlations

Five canonical correlations were performed, results for canonical correlation with raw data were not obtained due to the size of the $r$ matrix and the programmes available. One of the canonical correlations was meaningless due to a singular matrix resulting in a canonical correlation greater than 1.0 . Table 12 gives the significant canonical correlations, loadings variables with loadings for each of the four meaningful analyses.

TABLE 3

Functions and Demo. Factors

| Original Variable |  | Functions Factors |  |  |  | Demo. Factors |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Name | \# | Name | \# | Loading | Comm. | Name | \# | toading | Comm. |
| Tot Pos Func | 5 | Pos Func | 7 | . 99 | . 99 | Pos Func | 47 | . 99 | . 99 |
| Inst Pos Func | 6 | Pos Func | 7 | . 89 | . 80 | Pos Func | 47 | . 88 | . 78 |
| Cope Pos Func | 7 | Pos Func | 7 | . 87 | . 80 | Pos Func | 47 | . 88 | . 78 |
| Tot neg Func | 8 | Neg Func | 5 | . 99 | . 99 | Neg Func | 44 | . 99 | . 99 |
| Ideo Neg Func | 9 | Neg Func | 5 | . 89 | . 77 | Neg Func | 44 | . 85 | . 74 |
| Fear Neg Func | 10 | Neg Func | 5 | . 94 | . 77 | Neg Func | 44 | . 91 | . 84 |
| $\triangle$ Tot Pos | 11 | $\triangle$ Pos | 8 | . 99 | . 99 | $\triangle$ Pos | 45 | . 99 | . 99 |
| AInst Pos | 12 | $\triangle$ Pos | 8 | . 87 | . 80 | $\triangle$ Pos | 45 | . 86 | . 76 |
| ACope Pos | 13 | $\triangle$ Pos | 8 | . 86 | . 88 | $\triangle$ Pos | 45 | . 87 | . 78 |
| $\triangle$ Tot Neg | 14 | $\triangle \mathrm{Neg}$ | 6 | . 98 | . 99 | $\triangle \mathrm{Neg}$ | 46 | . 98 | . 99 |
| AIdeo Neg | 15 | ANeg | 6 | . 86 | . 76 | $\triangle \mathrm{Neg}$ | 46 | . 83 | . 70 |
| $\triangle$ Fear Neg | 16 | $\triangle \mathrm{Neg}$ | 6 | . 89 | . 83 | $\triangle \mathrm{Neg}$ | 46 | . 86 | . 81 |
| Soc supp | 17 | Soc Sanc | 9 | . 58 | . 83 | Soc Clim | 37 | . 84 | . 78 |
| Soc Sanc | 18 | Soc Sanc | 9 | . 94 | . 92 | Soc Clim | 37 | . 82 | . 70 |
| Avail'y | 19 | Avail | 15 | . 95 | . 95 | $\triangle$ Soc Supp | 38 | . 64 | . 74 |
| Par Model | 20 | Par Mod | 13 | . 95 | . 92 | Par Mod | 41 | . 95 | . 93 |
| Sib Model | 21 | Sib Mod | 10 | . 81 | . 87 | Sib Mod | 39 | . 78 | . 81 |
| $\triangle$ Soc Supp | 22 | ASoc Supp | 14 | . 96 | . 96 | $\triangle$ Soc Supp | 38 | . 85 | . 84 |
| $\triangle$ Soc Sanc | 23 | $\triangle$ Soc Sanc | 12 | . 98 | . 98 | $\triangle$ Soc Sanc | 40 | . 97 | . 95 |
| A Avail'y | 24 | $\Delta$ Avail | 16 | . 99 | . 99 | $\triangle$ Avail | 42 | . 97 | . 96 |
| 4. Par Mod | 25 | $\triangle$ Par Mod | 11 | . 97 | . 97 | $\bigcirc$ Par Mod | 43 | . 97 | . 99 |
| $\angle \mathrm{Sib}$ Mod | 26 | Sib Mod | 10 | -. 77 | . 86 | Sib Mod | 39 | -. 74 | . 79 |


Cont ${ }^{\prime} \mathrm{d}$

| Cont ${ }^{\text {d }}$ d |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Name | \# | Name | \# | Loading | Comm. | Name | \# | Loading | Comm. |
| aPeer Conf | 52 | $\Delta$ Conf | 23 | . 83 | . 82 |  |  |  |  |
| $\Delta$ Peer Indep | 53 | $\triangle$ Indep | 28 | . 68 | . 84 |  |  |  |  |
| $\Delta$ Peer Anti | 54 |  |  |  |  | $\Delta$ Fam Indep | 24 | . 51 | . 89 |
| AFam Conf | 55 | $\triangle \operatorname{Conf}$ | 23 | . 76 | . 82 | $\triangle \mathrm{Conf}$ | 17 | . 94 | . 93 |
| $\triangle$ Fam Indep | 56 | $\Delta$ Indep | 28 | . 92 | . 90 | $\Delta$ Fam Indep | 24 | . 90 | . 91 |
| $\triangle \mathrm{Fam}$ Anti | 57 | $\Delta$ Non-conf | 33 | . 87 | . 88 |  |  |  |  |
| dAtt Tow Dev | 58 | $\triangle$ Att Tow Dev | 35 | . 98 | . 99 | satt Tow Dev | 16 | . 94 | . 95 |
| 4Tot Risk | 59 |  |  |  |  |  |  |  |  |
| $\Delta$ Phys Risk | 60 | $\Delta$ Phys Risk | 29 | . 96 | . 95 |  |  |  |  |
| $\Delta$ Fin Risk | 61 | $\Delta \mathrm{Fin}$ Risk | 32 | . 94 | . 94 |  |  |  |  |
| $\Delta$ Soc Risk | 62 |  |  |  |  | $\Delta$ Soc Risk | 28 | . 96 | . 98 |
| AEth Risk | 63 | $\triangle$ Soc Risk | 34 | . 86 | . 88 | AEth Risk | 34 | . 94 | . 96 |
| $\Delta$ Total I-E | 64 | $\Delta I-E$ Pers | 19 | . 93 | . 91 |  |  |  |  |
| $\triangle I-E$ Pers | 65 | $\Delta I-E$ Pers | 19 | . 94 | . 92 | $\Delta I-E$ | 15 | . 65 | . 91 |
| AI-E Poli | . 66 |  |  |  |  | $\Delta I-E$ | 15 | . 89 | . 93 |
| ATotal Tr | -67 | $\triangle$ Poli Tr | 18 | . 92 | . 91 |  |  |  |  |
| $\Delta \mathrm{Tr}$ Pers | 68 |  |  |  |  | $\triangle$ Pers Tr | 26 | . 95 | . 96 |
| $\triangle \mathrm{Tr}$ Poli | 69 | $\triangle$ Poli Tr | 18 | . 92 | . 90 | $\triangle$ Poli Tr | 30 | . 98 | . 99 |
| AIP Alien | 70 | $\triangle$ Alien | 25 | . 74 | . 76 |  |  |  |  |
| ASoc Alien | 71 | $\Delta$ Alien | 25 | . 87 | . 83. | $\Delta$ Soc Alien | 25 | . 98 | . 98 |
| ADel Grat | 72 |  |  |  |  | $\triangle$ Del Grat | 19 | . 97 | . 97 |
| $\triangle$ Time Pers | 73 | $\Delta$ Time Pers | 31 | . 97 | . 96 | ATime Pers | 18 | .96 | . 97 |

Cont'd

| Cont'd |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Name | \# | Name | 非 | Loading | Comm. | Name | 非 | Loadin | Comm. |
| Sex | 74 | Size | 36 | . 87 | . 82 | Size | 5 | . 87 | . 82 |
| Age | 75 | Age | 42 | . 99 | . 99 | Age | 10 | . 99 | . 99 |
| Soc. Ec. St | 76 | SES | 44 | . 99 | . 99 | SES | 11 | . 99 | . 99 |
| Yr in Coll | 77 | Yr in Coll | 43 | . 99 | . 99 | Yr in Coll | 7 | . 98 | . 99 |
| Poli Orien | 78 | Poli Orien | 41 | . 98 | . 99 | Poli Aff | - 14 | . 99 | . 99 |
| Residence | 79 | Res | 39 | . 99 | . 99 | Res | 9 | . 99 | . 99 |
| Ref Group | 80 | Ref Gr | 40 | . 99 | . 99 | Ref Gr | 12 | . 99 | . 99 |
| Height | 81 | Size | 36 | . 81 | . 91 | Size | 5 | . 92 | . 88 |
| Weight | 82 | Size | 36 | .91 | . 86 | Size | 5 | . 88 | . 93 |
| Self D Obs | 83 | SDO | 38 | . 98 | . 96 | SDO | 6 | . 98 | . 97 |
| Exp GPA | 84 | Exp GPA | 45 | . 98 | . 99 | Exp GPA | 8 | . 98 | . 99 |
| Grade Diff | 85 | Gr Diff | 37 | . 97 | . 99 | Gr Diff | 13 | . 97 | . 99 |

[^0]TABLE 4
Factor Loadings of Criteria
(Varimax Rotation)

| Sample | Factor | Criterion |  |  |  | Initial <br> Eigenvalue |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Conseq. | Range | Time | Freq. |  |
| One | 1 | -. 214 | . 398 | . 900 | . 090 | 2.284 |
|  | 2 | -. 016 | . 293 | . 101 | . 975 | 0.968 |
|  | 3 | . 966 | -. 192 | -. 258 | -. 014 | 0.522 |
|  | 4 | -. 147 | . 848 | . 336 | . 202 | 0.226 |
| Two | 1 | -. 106 | . 936 | .347 | . 109 | 2.076 |
|  | 2 | -. 060 | . 124 | . 130 | . 987 | 0.870 |
|  | 3 | . 974 | -. 113 | -. 232 | -. 058 | 0.727 |
|  | 4 | -. 189 | . 309 | . 900 | . 105 | 0.327 |
| One * | 1 | $-.165$ | . 915 | . 391 | not <br> included | 2.089 |
|  | 2 | . 964 | -. 180 | -. 252 |  | 0.643 |
|  | 3 | . 209 | -. 360 | -. 885 |  | 0.268 |

Freq. excluded from analysis

Stepwise Multiple Regression
Raw Data Sample 1

*Variables with negative loadings
**All variables load significantly (p<.05)

Stepwise Multiple Regression
Raw Data Sample 2


* Variables with negative loadings
** All variables load significantly

TABLE 8
Stepwise Multiple Regression
Functions Sample 2


Stepwise Multiple Regression
Demo Sample 1

**All Variables load significantly ( $\mathrm{p}<.05$ )
*Variables with negative loading.

Stepwise Multiple Regression

Demo. Sample 2

|  | Criterion Variable |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Frequency | Time Span |  |  | Consequences |  |
| Predictor Variable** in order of entry with Cumulative Variance | ATime Persp $(067) *$ <br> Soc Clim $(094)$ | Soc Clim $(145)$ <br> Poli Aff'n $(304)$ <br> Size $(381)$ <br> SSoc Alien $(407)$ <br> Del Grat $(434)$ <br> ASoc Supp $(461)$ <br> Yr in Coll $(482)$ <br> Sib Mod $(505)$ <br> $\Delta I . E$ $(518)$ | Soc Clim <br> Pol Aff'n <br> Size <br> $\Delta$ Del Grat <br> $\Delta$ Poli Tr <br> Relig'y <br> Ref Grp <br> $\Delta E t h$ Rk | $\begin{aligned} & (144) \\ & (253) \\ & (295) \\ & (326) * \\ & (355) * \\ & (379) \\ & (395) \\ & (409) \end{aligned}$ | Poli Aff'n $(121) \star$ <br> Soc Clim $(170) \star$ <br> Residence $(209) \star$ <br> Poli Tr $(250)$ <br> $\Delta I E$ $(275) \star$ <br> Size $(309) \star$ <br> $\Delta$ Soc Sanc $(355) \star$ <br> Relig $(357) \star$ <br> Time Persp $((380) \star$ <br> Neg Func $(401)$ <br> Soc Al'n $(421) \star$ <br> Yr in Coll $(437) \star$ <br> Self D Ob $(451)$ | - |
| Multiple Correlation | . 307 | . 720 | . 640 |  | . 672 |  |

** All variables load significantly ( $p<.05$ )

* Variables with negative loading

TABLE 11
Summary of Multiple Correlations

|  |  | Mode of analysis |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Sample | Criterion | Raw | Functions | Demo. | Total ** |
| One | Conseq. | . 744 (11)* | . 673 ( 8) | . 697 (14) | . 705 |
|  | Range | . 781 ( 9) | . 743 (10) | . 726 (13) | . 750 |
|  | Time Span | . 778 (10) | . 771 (11) | . 741 (12) | . 765 |
|  | Freq. | . 426 ( 4) | . 272 ( 2) | . 448 ( 7) | . 384 |
| Two | Conseq. | . 674 (9) | . 652 ( 8) | . 672 (13) | . 666 |
|  | Range | . 711 ( 8) | . 653 (7) | .640 (8) | . 669 |
|  | Time Span | . 780 ( 7) | . 769 (12) | . 720 (9) | . 758 |
|  | Freq. | . 521 ( 7) | . 214 ( 2) | . 307 ( 2) | . 354 |
| Total ** | Conseq. | . 708 | . 664 | . 713 | . 686 |
|  | Range | . 747 | . 701 | . 684 | . 712 |
|  | Time Span | . 779 | . 770 | . 758 | . 761 |
|  | Freq. | . 457 | . 244 | . 380 | . 370 |

* Averages over modes/samples (using Fisher's Z)
** Indicates number of variables with significant loadings

Canonical Correlations

|  | Mode of Analysis |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Functions 1 |  | Demo 1 |  | Demo 2 | Demo 1 |  |  |
|  | 1 | 2 | 1 | 2 | 1 | 1 | 2 | 3 |
| Canonical** Correlation | . 876 | . 591 | . 860 | . 656 | . 855 | . 854 | . 641 | . 546 |
| Coefficient of Redundancy ( Rdx ) | . 088 | . 171 | . 094 | . 197 | . 096 | . 101 | . 237 | . 151 |
| Conseq. <br> Range <br> Time Span <br> Frequency | $\begin{array}{r} -0.382 \\ 0.364 \\ 0.419 \\ 0.080 \end{array}$ | $\begin{array}{r} 1.010 \\ 0.895 \\ 0.138 \\ -0.366 \end{array}$ | $\begin{array}{r} -0.560 \\ 0.282 \\ 0.290 \\ 0.173 \end{array}$ | $\begin{array}{r} 0.965 \\ 0.403 \\ 0.777 \\ -0.360 \end{array}$ | $\begin{array}{r} -0.475 \\ 0.281 \\ 0.475 \\ 0.042 \end{array}$ | $\begin{array}{r} -0.522 \\ 0.398 \\ 0.292 \\ \text { not } \end{array}$ | $\begin{gathered} 1.024 \\ 0.213 \\ 0.802 \\ \text { included } \end{gathered}$ | $\begin{aligned} & 0.082 \\ & 1.378 \\ & 1.266 \end{aligned}$ |
| Predictors | Neg Func $\Delta \mathrm{Neg}$ * Soc Sanc Avail | $\Delta$ Neg Func <br> $\Delta$ Time Per | Size <br> $\Delta$ Soc Rk* <br> $\Delta$ Pol Tr* <br> Soc Clim | Age <br> $\triangle \mathrm{A} . \mathrm{T} . \mathrm{D}$. $\Delta$ TimePer* Anticon* ASoc Al* Soc Rk Fam Ind Pol Tr* $\Delta E t h$ Rk* IE Pol* Relig* Soc Clim | Size <br> Pol Or <br> Pol Tr* <br> Soc Clim | Size <br> Pol Or <br> Soc Rk* <br> APOI Tr* <br> Soc Clim | Age ATime Per* ADe1 Gr** Anticon* Time Per* ASoc A1* Soc Rk Fam Ind Pol Tr* Del Gr Relig* AEth Rk* IE Pol | ADel Gr* Soc Rk $\Delta$ Per Tr Fam Ind Pol Tr* De1 Gr* $\Delta E t h$ Rk |

Chapter IV
Discussion

- 

Several importamt issues must be considered in testing a predictive system. The first point is the investigation of the nature of the distributions of scores for the variables, the effects of these distributions on results, and the possibilities of reformulating measures or transforming distributions to eliminate undesirable characteristics. Then, the effect of error components, and covariance of chosen predictors is examined by means of raw score-factor score comparisons with reference to stability of results and interpretation of regression weights. The importance of different sequences of data entry should be considered. And finally, consideration will be given to patterns existing within the criteria, and in the relationships between predictors and criteria patterns. Discussion of each of these issues follows, concluding with a general overview and discussion of implications for multivariate research.

## Distributional Properties of the Variables.

The universal and bivariate frequencies of the data seem to deviate from normal, and bivariate normal distributions. Descriptive statistics for 15 of the variables appeared in Table 2 . This sample represents the kinds of distributions found, and includes each of the variable systems. An examination of these fifteen varialbes represents a consideration of the problems in the complete set of 85 variables. First the variables will be considered individually, with the empirical distribution arising from both scaling properties, and the properties
of the underlying "real" distributions.
Criteria
Frequency. This one item scale requires the subject to state the number of times he (she) has used marijuana in the last six months. The answers range from '0' (marijuana not used) to '999', and the distribution has very high skewness (a measure of symmetry, high positive meaning a long tail to the right, high negative a long tail to the left), and a very high kurtosis ( a positve kurtosis means the distribution is more peaked than the normal curve). An examination of the histogram for frequency shows that approximately $55 \%$ of the respondents gave an answer of ' 0 '. Three possibilities exist as to the nature of the distribution: a dichotomy with unequal intervals; a poisson distribution; or a log-normal distribution. The log-normal is properly a distribution for a continuous variable, but may be approximated for a discrete variable. It is a distribution in which the logarithm of the variable is distributed normally, and results from either a particular process occurring to the "true score" or as a result of error variance being related to the value of the true score (the error variance of a normal variable is unrelated to the true score). The distribution may not take on the true value of ' 0 ' ( $\log (0)$ is undefined), and since the probability of ' 0 ' is so high, the addition of a constant in this case may be more distortion than transformation.
$\Lambda$ poisson distribution occurs when we have "rare occurrences events in a fixed time interval (Tsokos, p.113, 1972)". Since it seems strange that an event that has low probability could occur 100, 200 or 999 timen, as with froquency we must consider what these numbers mean.

First of all over the six month period, the respondent answering ' 100 ' has smoked every second day, the respondant answering ' 400 ' has smoked twice a day, etc. Also we must consider the implications of the number given as to probable error involved. Most likely those responding ' 0 ' will give an exact (true) report, but those responding with '5' may be including the interval 3,7 , and with ${ }^{\prime} 200^{\prime}$ may be including 180,220 etc. This is similar to psycho-physical problems (e.g. JND's) where the error is proportional to the magnitude of the true score. The differences between answers of ' $1^{\prime}$ and ${ }^{\prime} 100^{\prime}$ and between ' $101^{\prime}$ and ' $200^{\prime}$ cannot be considered as equal intervals. Perhaps the most important interval is that between ' 0 ' and ' 1 '. In other research (see Sadava, 1974b), the investigators often treat frequency as a dichotomous criterion 0 and 1 , a11 those answering ' 1 ' or more being grouped together and predictors analyzed by point-biserial correlation or analysis of variance. Upon reanalyzin the present data, classifying frequency as 0 or 1 , the multiple correlation with the predictors rose to .767 (as opposed to a high of .521 with raw data, for sample $1_{\text {; }}^{\text {; }}$ where a continuous distribution was assumed).

One approach to the frequency criterion would be to first analyze assuming a dichotomy and then reanalyze assuming a continuous distribution. An investigation of the portion of the curve including all those answering ' 1 ' or more may allow us to transform answers by taking log(x) or to rescale by intervals and a poisson approximation, resulting in either case in a more normal distribution.

Time Span. Although this criterion does not have the extremities of Frequency ( $\operatorname{Pr}\left['^{\prime} 0^{\prime}\right]<.5$ lower kurtosis and skewness), it is by no means normal. In theory, this measure, i.e. how many persons started smoking marijuana in a given month, should take on a poisson distribution, however in practice the person's score is complicated by errors that most likely are proportional to the 'true' answer. The most direct way of transforming this variable would be to add a very small constant (e.g. . 001 ) to avoid zeros and then take $\log (x)$, this at least would reduce skewedness.

Range. This variable is scored by adding up the number of drugs taken by the individual. The responses are not independent, as in a personality scale, but rather strongly interrelated. In a personality scale, each item is assumed to have constant probability of being endorsed, due to the underlying trait measured. With the Range scale, it is likely that endorsement of one drug in a group (e.g. opium, heroin, morphine) implies a large probability of endorsing the other drugs outside the group (e.g. tranquilizers). Instead of 19 separate questions, we may be asking about 5 or 6 categories of drugs, and assigning different weights to these categories rather arbitrarily (as above-a score of 3 for opium derivatives vs a score of 1 for tranquilizers). It we refine the scale to give equal weights to drug categories, we would most likely find a different distribution. This new variable might have the properties of a Guttman scale (if the theories about "progression to harder drugs" were true), or that of a poisson distribution. In either case, the addition of a small constant, and the use of a $\log (x)$ transform would probably make the Range variable approximate a normal distribution.

Consequences. This variable has a much different form than those above, being relatively symetric (skewness $=0.400$ ) and flat rather than peaked (the kurtosis is negative). In general however this distribution (labelled rectangular) is a close enough approximation of the Gaussian (or normal) to be used in most statistics. In Carroll's (1961) review of the effects of marginal distributions on correlations, the quality that most often gives rise to problems is that of skewness combined with peakness. The rectangular (as opposed to tapering tails as in the normal) nature of this distribution may be due to extreme scores of a response set. There are 17 three point items all keyed, and worded, in the same direction. The subjects may be responding habitually to a particular key ('often' or 'never') and more discrimination may be afforded by a reversal of keying or wording, or an extension from three point items to five or seven (see below for comments on the personality scales).

## Perceived Environment

Social support. This scale more closely approximates normal than any of the preceding, but appears to have two modes. This may be a result of chance, or perhaps there are two reponse patterns-that of users and that of non-users. A discriminant analysis would provide more evidence on this point. For our purpose this distribution may be considered normal.

Availability. This scale and those of sibling model, total positive functions and ideological negative functions all appear to be normal, with one tail truncated. The loss of symmetry caused by
this truncation is a more serious problem than the apparent bi-modality of social support, but the trunctation can be corrected. The score distribution of Availability is negatively skewed and probably results from the common milieu of the subjects. In a less resrticted sample, we most likely would find more subjects at the lower level of the scale. A second approach to approximating nomality could be the extension of this scale from the 3 items to 10 or 15 , adding questions of a higher "difficulty" level (e.g. have you had a pond of marijuana (or more) in your possession at any given time).

Sibling model. As with Availability more items (and more difficult items) should be added.

Cognitive Functions
Total positive functions and ideological negative functions. These two scales are similar in construction except that the former has 14 items and the latter 6 items. The Ideological scale has a higher skewness (. 799 vs .491 ) and this may be a direct result of there being a fewer items. This comparison suggests to us that the number (and difficulty level) be increased, at least for the ideological scale. Personality Scales

Value family conformity, attitude towards deviance, total risk and locus of control (I-E). Of all the scales used in this study the personality scales (not just the four cited), in general, may be most closely described as normal. This would seem to result from both the theoretical underlying distributions involved (as opposed to time span for example), and the scaling strategies involved (as opposed to

IdRological negative functions). The personality traits are usually assumed to be normally distributed in the general population, and the underlying traits are continuous (not dichotomous or discrete). This follows from a psychological assumption that there are many contributing causes for the trait, and the mathematical principle that the sum of a number of independent, small, random variables has a distribution that is approximately Gaussian (normal). This latter principle is used again in the scale construction, by utilizing either a large number of questions, or a wide range of valuse for each question (or both). The four scales in Table 2 all follow this strategy: Value Family Conformity has 10 items, each a three point scale; Attitude Towards Deviance had 15 ten point items; Total Risk has 8 nine point items; and Locus of Control (IE) has 23 two point items.

Demographic Variables
Expected grade point average. This scale has normal properties with a minor perperbation. Numbers ending in ' 0 ' or ' 5 ' (e.g. 65, 80, 85) seem to include most of the marks otherwise found in the surrounding interval. We may assume that ' 65 ' implies the range from '63' to '67'. (The practice may result from prior experiences with rounded marks). In our interpretation of regression weights etc., connected with Expected GPA, we may have to consider this, but there should be no major problem.

Self description: obesity. Although only a single five point item, this scale appears to be normal. This may result from connection to physical characteristics (weight, height) which are normally distributed, or may be due to chance.

Sex. This variable, at least for the purpose of this study has a dichotomous distribution. We must be careful when interpreting the meaning of any regression weights or other statistics. Furthermore, the combination $n f$ this scale with another whose distribution is markedly non-normal may result in strange values.

## Bivariate Distributions

Although only a few scattergrams were produced (out of thousands possible), some of the results were supportive of the consideration above. Range consistently showed that a transformation could have increased correlation. The plot of consequences and age showed that several extremely high values of age combined with high values for consequences to change the correlation. Because of the vast majority of the subjects were 26 or under, the older subjects may have had disproportionate effects on findings. (This may also have occured with Frequency, Time and Range.) The use of scattergrams should be extended (both in this study and mutlivariate analyses in general), and used to substantiate hypotheses about univariate distribution.

Raw Data Versus Factor Scores
The issue we are concerned with is cross-validation, both in the classic statistical sense, across samples, and in a more abstract conceptual sense, i.e. what the label of a reliable variable means. First of all, if the stepwise mutliple regressions performed on frequency are excluded (as previously mentioned, its underlying scale may be unsuitable for this analysis, and as will be pointed out below, it is unrelated to other criteria), the range of multiple R's over two three criteria and three modes of analysis, is remarkably small-the
lowest is . 640 and the highest . 781 (variance-accounted for is between $40 \%$ and $60 \%$ ).

The parameters for Sample 2 were calculated on Sample 1, yet the differences between $R^{\prime} s$ is not great (see Table 11). Without statistical tests (for which we assume, rather tenuously, a multivariate normal distribution), it is safe to say that we have not captilized on chance (we have used large samples and demonstrated a reasonable replication, Lowest variance accounted for is per cent) even though the correlation for Sample 1 are slight;y higher than those of Sample 2. That is, multivariate cross validations (Cooley and Lohnes, 1971), have been demonstrated.

The multiple correlations for the raw data are higher than for either of the factor data sets, however the difference is not great (the largest difference is. .070), and the functions (and demo) have slightly greater stability in individual variable entry into the regression equation. On the average, three variables are replicated from sample one to two, but with raw data, but 5.3 variables are replicated with the factor scores. This is to be expected since there are about half as many with Functions and Demo as there are with the raw data, and these variables are "boiled down" through a process that tends to eliminate unique or error variance.

Both the raw score and the factor score approaches have advantages, but the greatest advantage is gained in using both of them. The analyses for consequences should serve as an example. If we look for raw score variables that are significantly loaded for both Samples 1 and 2,
we find only social support and $\boldsymbol{\Delta}$ Social sanctions. Social support appears in the Functions and Demo. analyses (as the social sanctions and social climate factors respectively). Social Sanctions also appear on all of the analyses. We have gained more confidence in these variables since they might have been eliminated by the errors of proximity and verifiability discussed earlier. Availability appears in in Raw data, Sample 1, both Function analyses, and as social climate in Demo analyses; social sanctions appear in five of the analyses. Now it is clear that the variable complex: social support, social sanctions, availability and social support is of great importance to the consequences criterion. The labels may merge in the factor score analyses, but it is clear that this complex represents a major correlate. Further investigation would seem worthwhile. The variables negative Functions and $\Delta$ Negative Functions (or their subscale-fear negative function) appear four times each in the six analyses and similarly indicate that this complex of variables is of importance. In contrast, $\Delta$ personal trust is the fourth variable to enter the first raw data sample equation, but
is not replicated in raw or factor score equations. It would appear that this may have been as a result of covariance with those variables, rather than being a significant predictor.

The above discussion is brief, and could be continued for the other criteria, but should be sufficient to show the importance of a simultaneous raw score/factor score approach.

## Sequence of Data Entry

It is now appropriate to focus on the comparison of the Functions (sequence of proximity) and Demo (objective verifiability order) analyses. The averages (over samples) multiple R's of the two methods for each of the criteria are very close, and differences are more parsimoneously attributable to chance than one method's being more effective in capturing variance than the other. The two modes of analysis have different sets of individual factors included as having significant beta weights in each analysis. Whereas the function factors, contribute greatly to the multiple R's in Function mode of analysis (e.g. $42 \%$ of the variance accounted for, Function Data, Sample 1,

Time Span), they contribute almost nothing in the Demo.
analyses. Only with consequences as the criterion do these factors
appear at all. The reverse is true of demographic factors in Functions analysis (age appears with time span but may be redundant with the criterion rather than an independent correlate). However social factors appear prominently in all analyses (e.g. over $40 \%$ of the accounted-forvariance in each of Functions and Demo data, Sample 1, Range), and although not as powerful, the personality factors also enter significantly in each analysis.

Although these results need more exploration, the signs are clear that sequential data entry may influence our interpretation of results, if not the results themselves.

## Criteria Patterns

Of the criteria, Frequency was the least predictable by Stepwise Multiple $R$ 's (average $R$ is . 370 for frequency and ranges from . 686 to . 761 for the other criteria). Also its distributional properties deviate much farther from normality than those of Time Span, Range, and Consequences. In the Factor analyses of the criteria, each of the
loads highly on a separate component. Finally, Frequency has no high beta weights on any of the canonical variates. It would seem that, in general, Frequency, as measured in this study at least, is not a constituent of the overall criteria set. This may be because of the dual nature of the Frequency score distribution (dichotomous-Poisson), rendering it unsuitable for these kinds of analyses. This could be investigated by transforming it into a dichotomy and analysing; then, excluding non-users, transforming the Frequency score distribution into an approximately normal distribution and running the analysis again. The results from this might indicate a five criteria set (e.g. Consequences, Range, Time Span, Use vs. Non-use and User Frequency). Alternatively, Frequency may just be a poor criterion; but, as indicated by Sadava (1974a), this is usually the sole continuous criterion in marijuana research. Further, since the practical aim of much of the research is to treat abusers (i.e. those with high consequences) of marijuana, or conceptualize marijuana as an example of the broader range of drugs, the absence of investigation into the criterion domain may be particularly
unfortunate. Given the results of the present criteria factor analysis,
and the canonical correlation analysis, the inferential links from
predictors (of marijuana smoking) to frequency, to the "real" interest may be very weak.

## Canonical correlation analysis

In considering the results of this analysis, first a further explanation of the coefficient of redundancy $\left(R_{d x}\right)$. As Stewart and Love (1968) point out, canonical correlations are not correlations between two sets of variables, but between two linear functions of those variables. The square of the canonical correlation cannot be interpreted as $r^{2}$ for simple correlation, or $R^{2}$ in multiple correlation: $R_{d x}$ (or $R_{d y}$ ) is the quantity used to indicate the relationship between the sets of variables. This tells us the proportion of the variance of the criteria shared with the predictors. Thus the second canonical variate of Demo data, Sample 1 has twice the predictive power of the first variate, even though the first canonical correlation is higher. The loadings of the criteria indicate two patterns of marijuana use (The second canonical variate of Demo., sample two, corresponds to the other second variates, but was not statistically significant).

These might be characterized as the "normal" (i.e. low consequences associated with higher range and time span) and "abuser" (high perceived consequences associated with a long time span and low frequency of use) patterns. The abuser pattern is associated with personality variables, while the normal pattern seems to be associated with social and environmental predictors. In the case of the second variate, it would be very difficult to draw inferences on the causality sequence. To do this would require some form of path analysis, or a set of canonical correlation analyses utilizing $\Delta$ predictor scores and $\Delta$ criterion scores (see Blalock, 1971, for a set of readings on problems with causal models). At this point in the research, it seems clear that patterns in the criteria exist, and that these may result from or result in different variable complexes. Multivariate Prediction with Conceptual Systems

A consistent finding in this investigation has been the system of variable sets at work. The original model (Figure 1) included five variable systems: behaviour, cognitive function, personality, perceived

those with unknown domains, and a reconstruction of the variables as
orthogonal factors would probably improve reliability (Jesorr, Jessor \& Finney, 1973, pp. 6-8).

The empirical testing of a multivariate system mus $t$ be very
carefully done. The consideration of score distributions is often
never made, although this inattention may alone invalidate or compromise later findings. Similarly multiple regression replication must be more thoroughly done since useful predictors may be excluded or unreliable ones included. Finally, criteria patterns and the links between the measurement of a behaviour and its "real life" correspondant(s) must be examined conceptually and empirically.

The above work did not attempt to examine the results in context of Sadava's system or to relate them to the literature on marijuana research specifically, or deviant behaviour in general. The focus was on issues common to multivariate systems, and to problems often ignored for some reason or another. It is the consideration of these problems, and their solution, that will allow the construction of useful predictive systems, and their meaningful empirical testing.

The results of this thesis may be divided in two parts:
those findings with regards to the content matter, cannabis use; and those related to data analysis and methodology.

The most intriguing and suggestive of the content findings
is the type of predictor and criterion patterns found in the canonical analysis. Several implications point to the potential in replication with different measures and samples. First, consider the two criteria patterns that seem to emerge: that of a moderate or "social smoker" which may parrellel the social drinker in alcohol use; and the "abusive" pattern which includes high adverse consequences of use. If these are "true" patterns they are important in considering the treatment of marijuana problems users and for the attitudes towards marijuana itself. Further, comparisons between patterns for marijuana and alcohol abuse, may clarify the origins of and meaning of "drug abuse".

On the other side of the canonical analysis, the predictor patterns may not only help us to understand drug abuse but may help us visualize the importance of (and the utility of) the differences between situational and intrapersonal factors in psychology. It would seem that there are at least two components in the predictor set: one comprised of social-environmental variables (e.g. peer and family relationships, political orientation size etc.) which is related to the variance in normal behaviour, and a component of
personal variables (e.g. time perspective, conformity issues, etc.)
related more to the "extremes" of behaviour. A thorough investigation
of these kinds of relationships can point out what each approach
can do and how to implement a situational-personality system in
psychology.

A second finding in the content area is much more specific
but, if typical of marijuana research, of some importance. As
pointed out by Sadava (1974a) the criterion used most often in
marijuana research is frequency of use. This variable is used in
a variety of forms: dichotomous (use - not use); ordinal group

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scale (e.g. 0, 1 - 6, 7 - 15, etc.) and continuous interval
(implicit in the use of Pearson product moment correlation coefficient
or variants thereof). This study found that there were two major
drawbacks to the "frequency of use" criterion. First, the scale
and underlying distribution ssverely limit available statistics
and restrict interpretations of findings with respect to this
variable. Secondly, this variable seems to have little empirical
relationship to other criteria of drug use, and more seriously may
not be suitable as a criterion to be linked with drug abuse or
problem behaviour - the aim of much drug research. These
findings cast doubt on the results of previous research and on
the generalization of findings to the problem area.
    The methodology and data analysis issues raised by this
thesis are important when considering the task of analyzing and
interpreting the large data arrays generated in multivariate
studies. Four problem areas were pointed out: frequency distri-
```

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butions, patterns of variables, raw data vs. factor scores and
sequential variable entry. Warnings about the effects of the
first two problems are always given when introducing the student
to statistics, however, judging from the apparent lack of attention
to these problems in non-medical drug use research these warnings
may not be needed in practice. Although this thesis has not covered
any new points with regards to the topics of frequency distributions
and variable patterns, the results at least give a good example of
the effects of focused consideration on the two areas.
    The issues of type of data (raw vs. factor scores) and
orthogonalization have received much less attention in the literature
and the present thesis attempted to compare procedures and exemplify
their use. Raw data scores alone, and factor scores alone, have
been used in data analysis previously but this study shows the utility
of considering both and cross-checking results. Quite often the
name assigned to a factor, variable, or "cause" with influence
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greatly interpretation and future research directions. If a result
is obtained by "chance" (and as noted by Cooley & Lohnes, 1971,
multivariate analysis often capitalizes on "chance"), succeeding
research may be ambiguous, or interpretations forced by the historical
"momentum". Although the statistical results may be verified by
cross-validation techniques, interpretations are still based upon
a single source. However, the concurrent use of factor and raw
scores may provide "conceptual cross-validation". This means that
one set of variables (factors) is mapped onto a set of factors
(variables) formed in a different manner, and both are checked
against the criterion (criteria). Hopefully this will establish more
clearly just what it is that predicts (explains) the variance of the
criteria.
    Finally the utility of partitioning the predictor variables
so that orthogonalization takes place in different sequences was
demonstrated. Almost all techniques for orthogonalization (factor
analysis) must extract components sequentially and it is important to
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know whether the results are relatively invariant or whether the
technique determines the results. Since we used two opposite
sequences of entry, the common results may be more trustworthy,
and our subsequent interpretations may be more valid.
    With increased use of multivariate analyses in the social
sciences, the potential pitfalls must be avoided, and guidelines for
meaningful interpretation drawn up. This thesis has attempted to
explore some problem areas in multivariate analyses and to highlight
potentially useful procedures.
```


## APPENDIX A

Proof For Gamma $(\underset{y i}{(1)})$

Let $Z_{i}(i=1, \ldots, m)$ be a series of independent, normally distributed variables with $\operatorname{Exp}\left(Z_{i}\right)=0, \operatorname{Var}\left(Z_{i}\right)=1$. T, et $Z_{y}$ be another normally distributed variable $\operatorname{Exp}\left(Z_{y}\right)=0, \operatorname{Var}\left(Z_{y}\right)=1$. Then $Z_{y}$, the predictable part of $Z_{y}^{y}$ from $Z_{i}$ equals $\sum_{i=1}^{m} \beta_{i} Z_{i}$.

But $\beta_{i}=r_{i}$ for orthogonal predictors (Mulaik,1972, p.404-405), then $Z_{y}=\sum_{i=1}^{m} r_{y i} z_{i} \cdot \operatorname{Let} \Gamma_{y i}\left(\operatorname{Exp}\left(\Gamma_{y i}\right)=0, \operatorname{Var}\left(\Gamma_{y i}\right)=1\right)$ be some variable, and $\alpha$ some constant such that :

$$
\begin{aligned}
& Z_{y}=\alpha \Gamma_{y i}+\sum_{i=1}^{m} r_{y i} Z_{i}, \\
& \Gamma_{y i} \text { indecent of } Z_{i} . \text { Then } \operatorname{Var}\left(Z_{y}\right)=\operatorname{Var}\left(\alpha \Gamma_{y i}\right)+\sum_{i=1}^{m}\left(\operatorname{Var}\left(r_{y i} Z_{i}\right)\right), \\
& 1=\alpha^{2}+\sum_{i=1}^{m} r_{y i}^{2}, \\
& \alpha\left.=\sqrt{1-\sum_{i=1}^{m} r_{y i}{ }^{2}}\right) \\
& \Gamma_{y i}=\frac{Z_{y}-\sum r_{y i} Z_{i}}{\sqrt{1-\sum r_{y i}^{2}}} \\
& \text { Therefore: }
\end{aligned}
$$

## APPENDIX B

## Delta Score Programme

```
        DIMENSION XDAT(35),YOAT(35),RXY(35),XYDEN(35),DELTA(35)
    50 FORMAT(8F10.4)
    500 FOFMATI5F7.3/28X,6F7.3,/8F7.3,7X,F7.3/10F7.3/F7.3,14X,2F7.3,21X,
        22F7.3/3F7.3,28X,3F7.3/2(10F7.3/),5F7.3,40X,13)
    700 FJRM4T(5F7.3,40X,13,'91'/SF7.3,33X,I3,'92'/10F7.3,5X,I3,'931/
        11OF7.3,5X,13,'94'/2F7.3,50X,13,8X,13,'95')
        RECD(5,50)(RXY(K),K=1,33)
        ว) 300 N=1,33
        XYCEN(N)=1./SQRT(1.-RXY(N)*RXY(N))
    300 CJNTINUE
        00 400 M=1,187
        REAO(5,500)(XDAT(N),N=1,33),(YDAT (N),N=1,33),NUM
        J 100 N=1,33
        IF(XUAT(N).LT.-20..CR.YDAT(N).LT.-20.1 GO TO 99
        DELTA(N)=(YUAT(N)-RXY(N)*XDAT(N))*XYUEN(N)
        G) TO 100
    970ELTA(N)=-99.
    100 ここNTINUF
        W2ITE(7,700)(DELTA(N),N=1,5),NUM, (DELTA(N),N=6,11),NUM,(DELTA(N):
        2V=12,21),NUM,(NELTA(N),N=22,31),NUM, (DELTA(N),N=32,33),M,NUM
    400 OUNTINUE
        .TOP
    ENU
```


## Gamma Score Programme



## Appendix C



Raw Data, Sample


## Raw Data, Sample 2

## CORRELATIONS





|  | Freq. <br> VAR 001 | $\begin{gathered} \text { Time } \\ \text { VAR } 002 \end{gathered}$ | Range VAROO3 | Cons. <br> VAROO4 |
| :---: | :---: | :---: | :---: | :---: |
| VAR001 | 1.00000 | c. 28003 | 0.26321 | -0.15418 |
| VAR002 | 0.28003 | 1.00000 | 0.62854 | -0.44206 |
| VAR003 | 0.26321 | 0.62854 | 1.00000 | -0.26488 |
| VAR004 | -0.15418 | -0.44206 | -0.26488 | 1.00000 |
| VAR005 | -0.14855 | -0.41287 | -0.31759 | 0.38669 |
| VAROOG | -0.13211 | -0.18294 | -0.16946 | 0.131941 |
| VAR007 | -0.01255 | -0.07325 | -0.02633 | 0.03133 |
| VAROO 8 | 0.14063 | 0.09244 | 0.14057 | 0.12987 |
| VAR009 | 0.13678 | 0.33229 | 0.34221 | -0.23222 |
| VAR010 | 0.01523 | 0.27899 | 0.15847 | -0.04740 |
| VARO11 | -0.05134 | 0.08402 | 0.06888 | -0.05310 |
| VARO12 | 0.11156 | 0.18417 | 0.10105 | -0.31537 |
| VAR013 | -0.11007 | 0.65270 | 0.07966 | -0.09076 |
| VAR014 | -0.05119 | 0.04021 | -0.00366 | 0.01937 |
| VAR 015 | 0.09523 | 0.19352 | 0.18137 | -0.16562 |
| VAR016 | 0.03840 | 0.04023 | 0.09353 | 0.08169 |
| VAR017 | -0.06583 | -0.13788 | -0.06242 | 0.02876 |
| VAR018 | -0.09332 | -0.12187 | -0.03149 | 0.04863 |
| VAR 019 | -0.04642 | -0.13880 | 0.02818 | 0.05059 |
| VAR020 | -0.04831 | -0.09354 | -0.08934 | 0.06698 |
| VAR021 | -0.08240 | 0.10880 | 0.04351 | -0.02558 |
| VAR022 | -0.02743 | -0.15206 | -0.03686 | 0.09202 |
| VAR023 | -0.12569 | 0.03850 | 0.01765 | -0.08624 |
| VAR024 | 0.11070 | 0.01322 | -0.03318 | -0.10762 |
| VAR025 | 0.00097 | -0.00796 | -0.23405 | 0.02198 |
| VAR026 | -0.04971 | -0.04823 | -0.04885 | 0.11334 |
| VAR027 | 0.11205 | -0.03745 | -0.02757 | 0.00152 |
| VAR028 | 0.02045 | 0.13063 | 0.05201 | -0.10017 |
| VAR 029 | 0.05722 | 0.09226 | 0.05753 | 0.00564 |
| VAR030 | 0.02096 | 0.01374 | -0.08174 | -0.04740 |
| VAR031 | 0.11752 | -0.01713 | 0.03400 | -0.05674 |
| VAR032 | 0.02045 | 0.13063 | 0.05201 | -0.10017 |
| VAR033 | -0.08999 | -0.12608 | -0.13512 | -0.05682 |
| VAR034 | 0.05406 | 0.16017 | 0.11397 | 0.08375 |
| VAR035 | 0.01245 | 0.15330 | 0.17705 | -0.20506 |
| VAR036 | -0.02196 | 0.07990 | 0.06207 | -0.09379 |
| VAR037 | 0.01242 | 0.02223 | 0.05453 | -0.02149 |
| VAR038 | 0.02580 | 0.01837 | -0.02426 | 0.09587 |
| VAR039 | 0.02534 | -0.05329 | 0.01509 | -0.10864 |
| VAR040 | 0.01266 | 0.01448 | 0.05838 | 0.10423 |
| VAR041 | 0.03239 | 0.11118 | 0.02314 | -0.09154 |
| - VAR042 | 0.06922 | 0.12605 | 0.05772 | 0.05320 |
| VAR04 3 | -0.03796 | -0.02856 | -0.01374 | -0.09330 |
| VARO4 4 | -0.07238 | -0.00104 | -0.06642 | -0.07239 |
| VAR045 | -0.04677 | 0.06581 | 0.03402 | -0.00439 |



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Demo. Factors, Sample 2

|  |  | Freq. <br> VAR 001 | Time <br> VAROO2 | Range <br> VAR003 | Cons. VAROO4 |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | VAR001 | 1.00000 | 0.27443 | 0.26321 | -0.14785 |
|  | VAR002 | 0.27443 | 1.00000 | 0.64483 | -0.4'039 |
|  | VAR003 | 0.26321 | 0.64483 | 1.00000 | -0.27486 |
|  | VAR004 | -0.14785 | -0.44039 | -0.27486 | 1.00000 |
|  | VAR005 | 0.11122 | 0.28282 | 0.20975 | -0.15423 |
|  | VAR006 | 0.00234 | -0.03956 | -0.02685 | 0.13053 |
|  | VAR007 | -0.05253 | 0.14347 | 0.13516 | -0.20280 |
|  | VAR008 | -0.00426 | 0.02284 | 0.04226 | 0.01883 |
|  | VAR009 | 0.02486 | 0.04275 | 0.08938 | $-0.17852$ |
|  | VARO10 | 0.00763 | C. 06850 | -0.02984 | 0.08625 |
|  | VAR011 | -0.08946 | -0.02490 | -0.11290 | -0.12572 |
|  | VAR012 | 0.07318 | 0.07703 | 0.06678 | 0.00574 |
|  | VAR013 | 0.04274 | 0.00865 | 0.08455 | 0.07730 |
|  | VAR 014 | 0.14153 | 0.38063 | 0.31208 | -0.34728 |
|  | VARO15 | 0.12358 | 0.04976 | 0.03508 | -0.15380 |
|  | VAR016 | -0.02727 | -0.03072 | -0.00006 | 0.04871 |
|  | VAR 017 | -0.01400 | -0.07811 | -0.05805 | -0.12879 |
|  | VAR018 | -0.25966 | -0.07731 | -0.02014 | 0.07123 |
|  | VAR019 | -0.00792 | -0.02702 | -0.11947 | 0.06287 |
|  | VAR020 | 0.13887 | 0.01995 | 0.01563 | -0.04799 |
|  | VAR021 | -0.02608 | 0.01210 | -0.06541 | -0.03336 |
|  | VAR022 | -0.04647 | -0.05557 | -0.01223 | 0.06490 |
|  | VAR023 | -0.11565 | -0.01106 | -0.10785 | -0.08834 |
|  | VAR024 | 0.07522 | 0.07396 | 0.02463 | 0.04612 |
|  | VAR025 | 0.02097 | 0.10395 | -0.01369 | -0.12568 |
|  | VAR026 | -0.02388 | 0.02046 | -0.05411 | -0.03545 |
|  | VAR027 | -0.05991 | -0.04219 | 0.01728 | 0.03901 |
|  | VAR028 | -0.13344 | -0.09201 | -0.09793 | 0.05431 |
|  | VAR029 | -0.10034 | -0.02049 | -0.03929 | -0.04745 |
|  | VAR030 | -0.03461 | -0.09861 | -0.18079 | 0.00678 |
|  | VAR031 | -0.00221 | -0.08691 | 0.00460 | 0.12752 |
|  | VAR032 | 0.00938 | 0.20090 | 0.20715 | -0.17465 |
|  | VAR033 | -0.00794 | 0.08124 | 0.13933 | -0.12503 |
|  | VAR034 | -0.02833 | -0.01079 | 0.04332 | 0.00827 |
|  | VAR035 | -0.05627 | -0.10089 | -0.10386 | -0.01482 |
|  | VAR036 | 0.01694 | 0.07796 | 0.08253 | -0.00531 |
|  | VAR 037 | 0.15675 | C. 38100 | 0.38002 | -0.20629 |
|  | VAR038 | -0.05547 | 0.04151 | -0.02657 | 0.02091 |
|  | VAR039 | 0.06213 | 0.21437 | 0.15566 | 0.01784 |
|  | VAR 040 | 0.08805 | 0.07861 | 0.07557 | -0.11753 |
|  | VAR041 | -0.03145 | 0.06484 | 0.10331 | 0.01184 |
|  | VAR 042 | -0.00904 | -0.00934 | -0.04122 | 0.06873 |
|  | VAR043 | -0.06197 | 0.08787 | 0.07726 | -0.03944 |
|  | VAR 044 | 0.00351 | -0.05133 | -0.04724 | 0.12675 |
|  | VAR045 | 0.00321 | -0.01064 | 0.03339 | 0.05894 |
|  | VAR 046 | 0.05590 | 0.01127 | 0.00020 | 0.04778 |
|  | VAR047 | 0.01358 | 0.07259 | 0.03016 | 0.04284 |
|  |  |  |  |  | ,04284 |

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[^0]:    Note : All loadings after varimax rotation and based on Sample 1

