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Exploring reasons why Australian senior secondary students do not enrol in higherlevel mathematics courses

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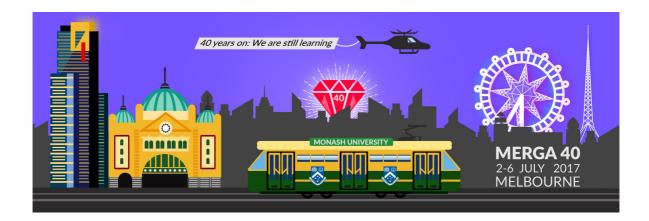
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# 40 years on: We are still learning!

Proceedings of the 40th Annual Conference of the Mathematics Education Research Group of Australasia

Edited by Ann Downton, Sharyn Livy, & Jennifer Hall



40 years on: We are still learning! Proceedings of the 40th Annual Conference of the Mathematics Education Research Group of Australasia

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## Preface

This publication is a record of the proceedings of the celebratory 40th conference of the Mathematics Education Research Group of Australasia (MERGA), which, like the inaugural MERGA conference, was held at Monash University in Clayton, Melbourne. The proceedings are made available to conference delegates on a USB and are also published on the MERGA website at www.merga.edu.au.

The theme of this 40th anniversary conference was 40 years on: We are still learning! This theme was chosen to acknowledge the significant contributions of Australasian researchers over the past 40 years, was inspired by a group of currently active researchers who attended both MERGA1 and MERGA40, and is linked to the Monash University motto, *Ancora Imparo* (We are still learning). The theme also highlights the impact and importance of our collective research for enabling new learning, innovation, and critique of mathematics education for those in our region and beyond.

MERGA40 conference participants presented research papers, symposia, round table discussions, and short communications that covered a broad range of topics relevant to mathematics education across all countries, with a particular focus on the Australasian region. The MERGA40 conference also included a series of nine workshops focused on research-related issues and 15 Research Interest Area (RIA) discussion groups aligned with chapter themes in the most recent four-yearly review of mathematics education research in Australasia (Makar et al., 2016). All workshops and RIA discussion groups were led by MERGA members who are acknowledged in the proceedings and conference program. We thank these members for their important contribution, leadership, and generosity.

In accordance with established MERGA procedures, all research papers were blind peer-reviewed by panels of mathematics education researchers with appropriate expertise in the field. Papers were accepted for presentation only, or for both presentation and publication in the conference proceedings. Only those research papers accepted for presentation and publication are published in full in these proceedings. Symposia papers and the abstracts of all short communications and round tables were also peer-reviewed. The published proceedings include the keynote papers; the Beth Southwell Practical Implications Award paper; symposia papers; abstracts for round tables, short communications, and research papers accepted for presentation; and the titles of all workshops and Research Interest Area discussion groups.

We acknowledge, with gratitude, the efforts of the MERGA40 review panel chairs, reviewers, and the Monash editorial team, in reading and providing constructive feedback to presenters in a short timeframe. Ensuring that the published papers are of a high academic quality is an important responsibility of the MERGA community. We thank the proceedings editors, Ann Downton, Sharyn Livy, and Jennifer Hall, for their hard work and care in preparing these proceedings for publication.

#### Ann Gervasoni and Helen Forgasz

(Co-Conveners of the MERGA40 conference on behalf of the MERGA40 Monash organising committee)

#### Reference

Makar, K., Dole, S., Visnovska, J., Goos, M., Bennison, A., & Fry, K. (Eds.). (2016). Research in mathematics education in Australasia 2012–2015. Singapore: Springer.

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# Contents

PREFACE	3
MERGA40 REVIEWERS	4
KEYNOTES	
The "M" in STEM: National Perspectives	18
We are Still Learning to Integrate Affect (and Mathematics) into our Research	19
CLEMENTS-FOYSTER LECTURE	
In Search of Mathematical Structure: Looking Back, Beneath, and Beyond – 40 Years On	32
Joanne Mulligan	
INVITED PANEL: MERGA 1 TO MERGA 40	
Progressing Along a "Road Less Traveled": The History of School Mathematics Ken Clements	43
Forty Years on: Mathematical Modelling in and for Education Peter Galbraith	47
Mathematics Performance and Future Occupation: Are They (Still) Related? Gilah C Leder	51
"Does This Mean That Kindergarten Will Be a Remedial Year?" Bob Perry	55
Forty Years of Teaching Problem Solving Kaye Stacey	59
BETH SOUTHWELL PRACTICAL IMPLICATIONS AWARD	
Framing, Assessing, and Developing Children's Understanding of Time Margaret Thomas, Doug Clarke, Andrea McDonough, & Philip Clarkson	64
INVITED LECTURE	
The "M" in STEM: AMSI's Perspective Geoff Prince	75

# **RESEARCH REPORTS**

The Prevalence of the Letter as Object Misconception in Junior Secondary Student Zarina Akhtar & Vicki Steinle	s77
Developing Interactive ICT Tools for the Teaching and Learning of Vectors at A-Level	85
Khemduth Singh Angateeah, Savial Thapermall, & Ravi Jawahir	
The Modelling Process and Pre-Service Teacher Confidence Taryn Axelsen, Linda Galligan, & Geoff Woolcott	93
Re-Examining a Framework for Teacher Identity as an Embedder-of-Numeracy Anne Bennison	101
Privileging a Contextual Approach to Teaching Mathematics: A Secondary Teacher's Perspective Raymond Brown & Trevor Redmond	109
Partial Credit in Multiple-Choice Items Joan Burfitt	117
How Might the Use of Apps Influence Students' Learning Experiences? Exploring a Socio-Technological Assemblage Nigel Calder & Carol Murphy	125
Entangled Modes: Social Interaction in Collaborative Problem Solving in Mathematics	133
Investigating Teachers' Perceptions of Enabling and Extending Prompts Jill Cheeseman, Ann Downton, & Sharyn Livy	141
The Impact of a Measurement-Focused Program on Young Children's Number Learning <i>Jill Cheeseman &amp; Yianna Pullen</i>	149
Snapshots of Productive Noticing: Orchestrating Learning Experiences Using Typical Problems Ban Heng Choy & Jaguthsing Dindyal	157
The Argument from Matriculation Used by Proprietors of Victorian Secondary Schools Around 1900 Ken Clements & Nerida F. Ellerton	165
That First Step: Engaging with Mathematics and Developing Numeracy Audrey Cooke	173
"Maths Inside": A Project to Raise Interest in Mathematics Mary Coupland, Marco Angelini, Anne Prescott, Sandy Schuck, Tapan Rai, & Carmen Lee	181
Mastery Learning: Improving the Model Mary Coupland, Danica Solina, & Gregory E. Cave	189

The Interplay Between Pre-service Teachers' Intentions and Enacted Mathematical Content Knowledge in the Classroom <i>Leah Daniel</i>	197
Exploring Ways to Improve Teachers' Mathematical Knowledge for Teaching with Effective Team Planning Practices	205
Primary School Mathematics Leaders' Views of their Mathematics Leadership Role 2 Kerryn Driscoll	213
Historical Perspectives on the Purposes of School Algebra	221
Fourth-Graders' Meta-Questioning in Statistical Investigations	229
Essential Topics for Secondary Mathematics Success: What Mathematics Teachers Think	237
Hypothesis of Developmental Dyscalculia and Down Syndrome: Implications for Mathematics Education	245
Gender and VCE Mathematics Subject Enrolments 2001-2015 in Co-Educational and Single-Sex Schools	253
A Secondary Mathematics Teacher's Perceptions of her Initial Attempts at Utilising Whiteboarding in her Classes	261
The Development of Addition and Subtractions Strategies for Children in Kindergarten to Grade 6: Insights and Implications	269
Teaching Fractions for Understanding: Addressing Interrelated Concepts	277
Teachers' Understanding and Use of Mathematical Structure	285
Initial Teacher Education Students' Reasons for Using Digital Learning Objects When Teaching Mathematics	293
Peer Observation as Professional Learning about Mathematical Reasoning Sandra Herbert & Leicha A. Bragg	301
Exploring Reasons Why Australian Senior Secondary Students Do Not Enrol in Higher-Level Mathematics Courses	309
Does (Problem-Based) Practice Always Make Proficient?	317

Explicitly Connecting Mathematical Ideas: How Well Is It Done? Chris Hurst & Ray Huntley	325
Exploring Undergraduate Mathematics Students' Difficulties with the Proof of Subgroup's Closure under Operation	333
Is Mathematics Education Worthy? From Mathematics for Critical Citizenship to Productivity Growth Dan Jazby	341
Grade 10 Students' Mathematical Understanding and Retention in a Problem–Based Learning (PBL) Classroom Premanan Juakwon & Duanghathai Katwibun	349
Knowledge, Beliefs, and Innovative Curriculum Laurinda Lomas	357
Engaging Pre-Service Mathematics Teachers in Creating Spatially-Based Problems in a 3D Virtual Environment: A CAVE2TM Experience	365
Structure in the Professional Vocabulary of Middle School Mathematics Teachers in Australia <i>Carmel Mesiti &amp; David Clarke</i>	373
Using Coding to Promote Mathematical Thinking with Year 2 Students: Alignment with the Australian Curriculum Jodie Miller & Kevin Larkin	381
Online, Anytime, Anywhere: Enacting Flipped Learning in Three Different Secondary Mathematics Classes	389
Learning from our Neighbours: The Value of Knowing Their Number History	397
Generalising Fraction Structures as a Means for Engaging in Algebraic Thinking Catherine Pearn & Max Stephens	405
First-Year University Students' Difficulties with Mathematical Symbols: The Lecturer/Tutor Perspective <i>Robyn Pierce &amp; Meredith Begg</i>	413
11th Grade Students' Self-Regulated Learning in a Mathematics Problem-Based Learning (PBL) Classroom	420
Statistics Instructors' Beliefs and Misconceptions About p-values Robyn Reaburn	428
Revisiting Friedrich Froebel and his Gifts for Kindergarten: What are the Benefits for Primary Mathematics Education? Simone Reinhold, Ann Downton, & Sharyn Livy	434

Perceived Changes in Teachers' Knowledge and Practice: The Impact on Classroom Teachers from Leader Participation in Whole-School Reform of Mathematics Teaching and Learning	442
Examining the Impact of Lesson Structure when Teaching with Cognitively Demanding Tasks in the Early Primary Years James Russo & Sarah Hopkins	450
Pricing: Exploring the Intersection Between Values, Maths, Finance, and Entrepreneurship	458
Using Activity Theory to Understand a Mathematics Leader's Motivations and Use of Mathematical Knowledge for Teaching4 <i>Matt Sexton &amp; Janeen Lamb</i>	466
Exploring Critical Thinking in a Mathematics Problem-Based Learning Classroom4 Rakkor Siriwat & Duanghathai Katwibun	474
10th Grade Students' Participation in a Mathematics Problem-Based Learning Classroom	482
Mathematics Identities: From Motivations to Turning Points in Mathematics Identity Construction <sup>2</sup> Dhanya Surith	490
Using Drawings in Solving Mathematics Word Problems <sup>2</sup> Ray Teahen & Robin Averill	498
Examining Non-Traditional Pathway Preservice Teachers' Attitudes Towards Mathematics	506
Indigenous Teacher Education: When Cultural Enquiry Meets Statistical Enquiry5 Tony Trinick & Tamsin Meaney	514
Assessing the Creation of Value in a Community of Practice Linking Pre-Service and In-Service Mathematics Teachers	522
Supporting Teachers in Planning for Interactions with Students' Ideas	530
Students' Development of Statistical Literacy in the Upper Primary Years5 Jane Watson, Rosemary Callingham, & Lyn English	538
Why Teachers of Foundation Phase Mathematics Have Yet to "Take Up" Progressive Roles	546
Relating Emotions to Motivational Processes using Middle-School Students' Expressed Aspirations for Learning	554

Maths Anxiety: The Nature and Consequences of Shame in Mathematics Classrooms	62
Graphic-Rich Items within High-Stakes Tests: Indonesia National Exam (UN), PISA, and TIMSS	69
Pre-Service Teachers' and Tutors' Perceptions about the Value of Talk Moves	77
SYMPOSIA	
STEM Professional Learning: Evaluating Secondary School Teachers' and Students' Experiences	86
The STEM Teacher Enrichment Academy Approach	87
Evaluation of the First STEM Teacher Enrichment Academy	91
The Second STEM Teacher Enrichment Academy Evaluation: Teachers' and Students' Perspectives	95
Developing an Evaluation Framework for Future STEM Academies	99
Transitions in Mathematics Education	03
Transitions in Language Use in Primary School Online Mathematical Problem Solving	04
Mathematical Writing and Writing Mathematics: The Transition from Secondary to University Mathematics	08
The Valuing of Deep Learning Strategies in Mathematics by Immigrant, First- Generation, and Australia-Born Students: Transitions Between Cultural Worlds61 Abi Brooker, Marian Mahat, & Wee Tiong Seah	12
Supporting Mathematics Students with Autism Spectrum Disorders Through the Lens of Teacher and Student Values: A Research Framework for Teacher Transformation	16

The Role of Spatial Reasoning in the Early Years	625
Tom Lowrie, Tracy Logan, & Kevin Larkin	

ELPSA and Spatial Reasoning: A Design-Based Approach to Develop a "Mapping" App Kevin Larkin & Caroline Kinny-Lewis	. 629
Research Engagement and Impact in Mathematics Education	. 633
Evidencing Research Engagement and Impact	. 634
The Convoluted Nature of a Research Impact Pathway Vince Geiger	. 638
Engagement and Impact through Research Participation and Resource Development Anne Bennison & Shelley Dole	. 642
"Numeracy for Learners and Teachers": Impact on MTeach Students	. 646
Reframing Mathematical Futures: Using Learning Progressions to Support Mathematical Thinking in the Middle Years	. 650
Developing Learning Progressions to Support Mathematical Reasoning in the Middle Years: Introducing the Reframing Mathematical Futures II Project Dianne Siemon	. 651
Developing Learning Progressions to Support Mathematical Reasoning in the Middle Years: Algebraic Reasoning Lorraine Day, Max Stephens, & Marj Horne	. 655
Learning Progressions to Support Mathematical Reasoning in the Middle Years: Geometric Reasoning Marj Horne & Rebecca Seah	. 659
Developing Learning Progressions to Support Mathematical Reasoning in the Middle Years: Statistical Reasoning Jane Watson & Rosemary Callingham	. 663

# RESEARCH PRESENTATION ABSTRACTS

Challenging Teacher Perceptions: "Those Children will Struggle No Matter What You Do to Them" <i>Glenda Anthony, Roberta Hunter, &amp; Jodie Hunter</i>	668
Students' Reflections on Portfolio Assessment in Mathematics Hem Chand Dayal, Bronwen Cowie, & Salanieta Bakalevu	668
Tracing Student Teachers' Mathematical Modelling Motivation and Competencies over Time: A Design-Based Inquiry <i>Rina Durandt, Gerrie Jacobs, &amp; Geoffrey Lautenbach</i>	669
Pedagogical Architecture for Supporting Effective Numeracy Learning Vince Geiger	669

570
570
571
571
572
572
573
73
574
574
575
575
576
576
577

	Indonesian Mathematics Teachers' and Educators' Perspectives on Their Choice of Facebook Groups Sitti Patahuddin & Siti Rokhmah	. 677
	An Evaluation of Online Resources Designed to Teach Mathematics for Equal Opportunity Elena Prieto, Peter Howley, & Kathryn Holmes	. 678
	Spatial orientation ability of 11-13 year-old students: Some empirical findings Ajay Ramful, Tracy Logan, & Tom Lowrie	. 678
	Articulating Teacher Learning: The Power of Self-Study <i>Yvonne Reilly</i>	. 679
	Comprehending or Creating? On Sense-Making and Meaning-Making Thorsten Scheiner	. 679
	Assessment for Learning Techniques in the Pacific Island Context: What are Teachers' Views? Penelope Serow & Julie Clark	. 680
	On Translating Research in Mathematics Education Rudolf Straesser, Claire Margolinas, & Vince Geiger	. 680
	Junior Secondary Mathematics Teachers' Perspectives on the Transition of Year 7 into Secondary Schooling in Queensland Rebekah Strang & Kevin Larkin	.681
	Teachers' Anticipation of the Potential of Specific Suggestions for Mathematical Learning Experience Peter Sullivan, Melody McCormick, & Aylie Davidson	. 681
	Are Students' Perceptions about Mathematics Different Amongst Those Taking Different Senior Secondary Mathematics Subjects?	. 682
	He Puawaitanga Harakeke: Using technology to accelerate learning in Māori-medium learning programmes <i>Tony Trinick, Piata Allen, Bruce Taplin, &amp; Ana Pipi</i>	. 682
	Towards a Positive Approach to Teaching for Productive Disposition in Mathematics	. 683
R	OUND TABLE ABSTRACTS	
	Rethinking Mathematical Tasks Ban Heng Choy & Jaguthsing Dindyal	. 685
	Scaling Up and Sustaining Successful Interventions in Mathematics Teaching Merrilyn Goos, Robin Proffitt-White, & Anne Bennison	. 686
	Exploring Emotional Aspects of Pre-Service Mathematics Learning Environments Joanna Higgins	. 687
	Mathematics Leadership in Primary Schools Heather McMaster, Janette Bobis, & Jennifer Way	. 688

## SHORT COMMUNICATION ABSTRACTS

Use of Social Media in Preservice Mathematics Education Courses Paul Brown	690
Exploring Primary Teachers' Conceptions of Mathematical Fluency: Are We Speaking the Same Language? <i>Katherin Cartwright</i>	690
Looking Inside the Black Box of Mathematics Teacher Noticing Ban Heng Choy & Jaguthsing Dindyal	691
Improving Mathematics Curriculum Support for Indigenous Language Speaking Students Cris Edmonds-Wathen	692
The Use of Contextual Patterning Tasks with Young Pāsifika and Maori Students in New Zealand Mathematics Classrooms Jodie Hunter & Jodie Miller	693
Unidoodle Michael Jennings	694
Factors Influencing Student Selection of Senior Secondary School Mathematics Subjects	694
Practitioner Inquiry: Developing Capabilities in Mathematics Teachers	695
Teachers Choosing Mathematics Inge Koch & Janine McIntosh	695
Student Engagement in Mathematics Alexandra Laird & Peter Grootenboer	696
Testing Inquiry-Based Mathematics Competencies Dorte Moeskær Larsen	696
Students' Espoused and Enacted Theories in an Inquiry Mathematics Classroom Generosa Leach	697
Task Modification to Facilitate Creativity by Korean Prospective Mathematics Teachers	698
A Five Question Approach to the Teaching of Mathematics John Ley	699
Numeracy of Undergraduate Business School Students Chris Linsell, Brigid Casey, & Christine Smith-Han	699
Numeracy in Action in Family Shopping Experiences: A View from the Trolley Amy MacDonald, Angela Fenton, & Christina Davidson	700
A Developing Framework for Identifying Young Children's Engagement with the Spatial Features of Play Spaces <i>Catherine McCluskey &amp; Joanne Mulligan</i>	700

	Influential Factors for Effective Problem Solving Practice in Primary Mathematics Teachers	. 701
	Using Peer-Reflection to Develop Self-Regulated Learning Strategies in Year 10 Mathematics	. 701
	Exploring Mathematics Pedagogy in Collaborative Teaching Environments Bilinda Offen & Naomi Ingram	.702
	The Road to Transformative Healing of Mathematics Anxiety: A Case Study in Progress <i>Timothy Perkins</i>	. 702
	Linguistic Obstacles to Second Language Learners' Access to Mathematical Talk for Individualised Sense-Making Sally-Ann Robertson & Mellony Graven	. 703
	Interbreeding Paradigms in Research on Mathematics Knowing and Learning Thorsten Scheiner & Marcia Maria Fusaro Pinto	.703
	Fitness for Purpose of Tertiary Algebra Textbooks: An Arabic Case Study Hassnaa Shaheed	. 704
	Evaluating Learning Analytics of an Online System to Improve Teacher Education Students' Numeracy Skills Development	
	South African Vocational Engineering Students' Conceptual Understandings of Area, Surface Area, Volume, and Flow Rate Measurement: A Case Study <i>Pamela Vale</i>	. 705
	Student Errors in a Mathematical Literacy Examination and the Correlated English Language Features Pamela Vale	. 705
	Impact of Culture in Parental Control and Mathematics Achievement of their Children Daya Weerasinghe	. 706
	High-Potential Mathematics Students and Their Mathematics-Related Activities Outside School	. 706
RI	ESEARCH INTEREST AREA DISCUSSION GROUPS	. 708
W	ORKSHOP SESSIONS	.710

# Exploring Reasons Why Australian Senior Secondary Students Do Not Enrol in Higher-Level Mathematics Courses

#### <u>Gregory Hine</u> The University of Notre Dame Australia <gregory.hine@nd.edu.au>

In this research paper, I present the reasons why senior secondary students elect not to enrol in a higher mathematics course. All Year 11 and Year 12 mathematics students within Western Australian secondary schools were invited to participate in an online survey comprised chiefly of qualitative items. The key reasons espoused by students include an expressed dissatisfaction with mathematics, the opinion that there are other more viable courses of study to pursue, and that the Australian Tertiary Admissions Ranking (ATAR) can be maximised by taking a lower mathematics course. In addition, student testimony suggests that there are few incentives offered for undertaking a higher mathematics course.

Mathematics has been heralded as a critically important subject for students to undertake (McPhan, Morony, Pegg, Cooksey, & Lynch, 2008; Office of the Chief Scientist [OCS], 2014; Sullivan, 2011). This importance has been argued largely on the basis of students learning key interdisciplinary knowledge such as science, technology, and engineering (Ker, 2013), and to use this knowledge base to add intellectual value to new technologies, drive innovation and research capacities, and to help Australia compete globally (Australian Academy of Science [AAS], 2006). Furthermore, failure to produce a workforce with sufficient training in mathematics is considered a national concern for the economy of Australia and for keeping Australia as a competitor in the technological world (AAS, 2006; Hine et al., 2016; Maltas & Prescott, 2014; Rubinstein, 2009).

The importance of mathematics is also highlighted within tertiary study, where researchers suggest that university success depends on the level of mathematics studied at secondary school (Nicholas, Poladin, Mack, & Wilson, 2015; Rylands & Coady, 2009). More specifically, findings from various studies indicate that students who undertake higher-level mathematics courses at a secondary level tend to outperform their counterparts who undertake a lower-level mathematics course (Anderson, Joyce, & Hine, in press; Kajander & Lovric, 2005; Sadler & Tai, 2007). Despite this acknowledged importance, the number of students enrolling in higher-level and intermediate secondary school mathematics in Australia is declining (Barrington & Evans, 2014; Kennedy, Lyons, & Quinn, 2014; Wilson & Mack, 2014).

While most Australian universities have dispensed with subject prerequisites for degree programs (Maltas & Prescott, 2014; Nicholas et al., 2015), the phenomenon of declining enrolments is also experienced within tertiary mathematics courses (Brown, 2009; OCS, 2012). At the same time, there has been a reported increase in first-year university students lacking the appropriate mathematical background to complete courses in various disciplines (Poladian & Nicholas, 2013; Rylands & Coady, 2009; Wilson et al., 2013). Studies conducted in New South Wales and South Australia have identified why Australian students enrol in higher-level mathematics courses (Mathematical Association of New South Wales, 2014; McPhan et al., 2008), but there are few reasons proffered as to why capable students do not enrol in these courses. More recently, some researchers in Queensland have identified that capable students do not enrol in senior calculus mathematics courses due to a limited understanding of the relevance of mathematics (Easey & Gleeson, 2016) or the removal of Mathematics C (an advanced mathematics

course in Queensland) from university prerequisite lists (Jennings, 2014, 2013). Additionally, there is no research available that seeks to explain the declining student enrolments in a Western Australian context.

#### **Research Aims and Significance**

The aim of this research is to explore the perceptions of Year 11 and Year 12 Australian Tertiary Admissions Ranking (ATAR) mathematics students in Western Australian schools as to why they believe that senior secondary students do not enrol in a higher-level mathematics course. The ATAR is a percentile score that denotes an Australian student's academic ranking relative to his or her peers upon completion of secondary education. This score is used to predict a student's suitability for particular university courses and, ultimately, for university entrance. The research itself builds on the findings of a previous study (Hine, 2016) in which I investigated the perceptions of Heads of Learning Area: Mathematics (HOLAMs) as to why they felt that capable senior secondary students do not enrol in the two highest mathematics courses. HOLAMS indicated perceptions of student awareness that two mathematics courses are not needed for university entrance, there are other viable and less rigorous courses of study available, and students can maximise their ATAR score without completing those mathematics courses.

It is hoped that findings from this research project may be of particular interest to secondary and tertiary mathematics educators in Western Australia, and more broadly to mathematics educators across Australia. The overarching guiding question to be explored is: What are the factors that influence Year 11 and Year 12 ATAR students' decisions not to enrol in higher-level mathematics courses in Western Australian secondary schools? This research is a predominantly qualitative study designed to give a snapshot (Rose, 1991) of the students' perceptions regarding this phenomenon.

### Methodology

This study was interpretive in nature, and relied principally on qualitative research methods to gather and analyse data about why Year 11 and Year 12 ATAR mathematics students feel that senior secondary students do not enrol in higher-level mathematics courses. All Year 11 and Year 12 ATAR mathematics students in Western Australian secondary schools were invited to participate in the study. Participants registered their perceptions through the completion of a single anonymous, online survey comprising 12 five-point, Likert scale items (Q3) and two open qualitative questions (Q4 and Q5). The survey items were developed from the findings of a previous study (Hine, 2016) as well as from current literature (Barrington & Evans, 2014; Kennedy, Lyons, & Quinn, 2014; Wilson & Mack, 2014). The 12 Likert scale items required participants to the extent to which they felt that senior secondary students did not enrol in a higher mathematics course (1 = Strongly Disagree, 2 = Disagree, 3 = Undecided, 4 = Agree, 5 = Strongly Agree). The two open-ended questions asked participants to elaborate on their responses to the Likert scale items and to make any further comments regarding why they felt that senior secondary students did not enrol in a higher mathematics course. Additional demographic information of participants was obtained through a series of closed questions regarding gender, year level, the mathematics courses currently enrolled in (e.g., Applications, Methods, Specialist), type of school (e.g., secondary 7-12), gender composition of school (e.g., co-educational), and location of school (metropolitan or regional).

### Participants

In Western Australia, there are 168 secondary schools (36 Catholic, 52 Independent, and 80 Government) offering Australian Tertiary Admissions Ranking (ATAR) mathematics courses to Year 11 and 12 students. These courses are Mathematics Applications, Mathematics Methods, and Mathematics Specialist (School Curriculum and Standards Authority, 2016). All Year 11 and Year 12 students enrolled in these purposively sampled schools were invited to participate in the research, and a total of 1,351 students from 26 schools gave their consent to participate. The demographic information of the participants is provided in Tables 1, 2, and 3.

Table 1

Summary of Participants' Demographic Data (by Gender and Year Level)

Gender	Year 11	Year 12	Total
Male	278	212	490
Female	455	406	861

Table 2

Summary of Participants' Demographic Data (by School Location and Composition)

School composition	Metropolitan	Regional	Total
Coeducational	737	113	850
Single Gender	501	0	501

#### Table 3

Summary of Participants' Demographic Data (by Mathematics Course and Gender)

Course(s)	Male	Female	Total
Applications	264	554	818
Applications and Methods	7	9	16
Methods	109	288	397
Methods and Specialist	58	62	120

### Data Analysis

Qualitative data from the 1,351 completed surveys were explored using a content analysis process. According to Berg (2007), content analysis is "a careful, detailed systematic examination and interpretation of a particular body of material in an effort to identify patterns, themes, biases and meaning" (p. 303). After the two open-ended questions had been examined for themes, patterns, and shared perspectives, I analysed the data according to a framework offered by Miles and Huberman (1994), which comprises the steps: data collection, data reduction, data display, and conclusion drawing/verification. The themes drawn from the qualitative data are displayed in Table 5. For responses to the Likert scale items, descriptive statistics (weighted mean) were used to analyse collected data.

### Findings

For the Likert scale items, the number of participants registering a scale rating (i.e., 1 -5) and the weighted mean for each question item has been included. Within Table 4, a higher weighted mean represents stronger agreement with the question item, while a lower weighted mean represents stronger disagreement. In descending order, the five question items "Other courses are more viable/more attractive", "Dissatisfaction with mathematics", "Maximise ATAR without higher maths", "Higher mathematics not scaled", and "Not needed for university entrance" registered the highest weighted means. At the same time, question items "Not offered at our school", "Gender-related issues", and a "Lack of qualified staff" received the lowest weighted means.

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43

67

39

27

Weighted

mean

3.83

3.22

3.18

3.17

3.09

2.62

2.45

2.42

2.17

1.92

1.63

1.34

#### Table 4

1	2	3	4
38	112	262	549
99	213	467	413
94	228	489	404
	38 99	38         112           99         213	99         213         467

*Responses to Likert-Scale Ouestion Items* 

Higher mathematics not scaled

Compulsory subject selections

Friends doing the same courses

Dislike the teachers

Timetabling constraints

Lack of qualified staff

Gender-related issues

Not offered at our school

Not needed for university entrance

Table 5

Summary of Extended Answer Questions (Responses to Questions 4 and 5)

Key Themes	Question 4	Question 5	Total
Dissatisfaction with mathematics	215	558	773
Other courses are more viable/more attractive	108	282	390
Higher mathematics courses are not scaled sufficiently	102	60	162
Not needed for university entrance	60	73	133
ATAR can be maximised taking a lower maths course	76	55	131
Not needed for future life or career	33	72	105
Dissatisfaction with higher mathematics teachers	52	46	98

For Questions 4 and 5, the most commonly proffered qualitative responses included a dissatisfaction with mathematics, a decision to enrol in more attractive or viable courses, and a perception that mathematics is insufficiently scaled as a Year 12 course (see Table 5). These qualitative responses (which have been summarised in Table 5 with other responses) will now be explored.

#### Dissatisfaction with Mathematics

Participants asserted that the chief reason that secondary students did not enrol in a higher mathematics was due to a dissatisfaction with mathematics. Such dissatisfaction was registered via a variety of associated themes, including a perceived discrepancy between the complexity and workload of Applications and Methods courses, an acknowledged mismatch between effort and reward, a lack of confidence to study a higher mathematics, and an expressed lack of interest or enjoyment in the subject. The most frequently expressed theme by participants was the perceived discrepancy between Mathematics Applications and Methods courses, particularly in terms of overall workload and complexity of content (Q4: 139/215, Q5: 395/558). For instance, one participant reflected on this perceived discrepancy between courses:

I was previously enrolled in Methods, however I found it extremely hard. I had never received such low scores in maths. Now being in Applications, I have noticed that the topics studied are completely unrelated to Methods. It's not necessarily that Methods students are learning a harder level of math, they are learning a completely different topic which is harder to understand. I didn't see how what we learnt applied to real life like the topics we learnt in Applications do. I think there needs to be a bit of consistency in the topics. I also found Methods stressful as we went through the topics very fast.

From those participants asserting that students' dissatisfaction with mathematics stemmed from a perceived discrepancy between Applications and Methods courses, many proposed that an "in-between" course needs to be developed and offered to students. According to those participants, such a course would contain a considerable amount of content common to both Methods and Applications courses, and pitched at a level of difficulty in between those courses.

#### Other Courses are Viable/More Attractive

The second most common assertion participants made was that secondary students tend to enrol in those courses of study that appear to be more viable or more attractive than a higher mathematics course. In particular, participant responses regarding "course viability" or "course attractiveness" were further classified into the following associated themes: Students chose a "lower" mathematics course in order to excel at it, observed that lower courses were less stressful to undertake, rationalised that undertaking a lower mathematics course translated into less time studying mathematics and more time to allocate to other ATAR courses, and decided to broaden the variety of ATAR courses studied. The most commonly occurring theme was that students felt that undertaking a lower mathematics course required them to devote less time to mathematics study and to set aside more time to successfully complete other ATAR courses (Q4: 43/108, Q5: 123/282). To illustrate, a participant stated:

I feel as though I prefer to do really well in Applications than have to struggle through Methods with only satisfactory results. It also means I can put more effort into other subjects as I am not having to spend hours and hours of my time doing maths each week.

Another participant advanced this statement, rationalising how taking a lower mathematics course translated into increased time for other courses and a higher ATAR overall:

#### RESEARCH REPORTS

I think that people don't choose higher maths because the[se subjects] are subjects that require an increased amount of time and effort. You have to weigh up whether or not doing very well in Applications is going to be better for your ATAR than just doing average in Methods. I know for me, I would love to take a higher level maths; however, I wouldn't have time with my other subjects to do as well, and higher maths [subjects] generally don't get scaled enough. So overall it would be detrimental to my ATAR.

A further concession made by many participants was that on top of the perceived extra effort and workload associated with higher mathematics courses, taking a lower mathematics course would not only increase their ATAR score but improve their chances of being accepted into their desired university degree course.

#### Higher Mathematics Courses are not Scaled Sufficiently

Several participants (Q4: 102, Q5: 60) intimated that the reason that students do not enrol in a harder mathematics course was due to insufficient scaling or incentives. For example, one participant reinforced some previous key findings by arguing "Higher mathematics courses are not scaled enough. The difference between Applications and Methods in hardness is not compensated by scaling. People are better off doing Applications in terms of time spent on the subject and difficulty". Other participants felt that by completing the Mathematics Applications course instead of Mathematics Methods, their mathematics result would be impacted greater by scaling measures. To illustrate, a participant hypothesised:

If I dropped down to Maths Applications due to the impractical scaling of the two maths subjects (Methods and Applications) I could achieve a better ATAR by getting much higher results which are only scaled down a small amount instead of getting mid-range results which scale up by a small amount. This is seen by many students [who] I know drop down in both the current Year 12 cohort and the Year 11 cohort, this is not rational as harder maths courses are not rewarded per se for their extra effort.

There were some participants who drew attention to the 10% bonus marks offered by the School Curriculum and Standards Authority (SCSA) to Year 12 students completing Mathematics Methods or Mathematics Specialist courses from 2017 onwards. One participant stated:

Especially for this year, Methods and Specialist will not be given the 10% additional bonus if it is in your top score. Those harder subjects are not scaled much so the same amount of effort required a 65 in Methods could get a 90 in Applications, allows the people who do easier maths to get a higher ATAR...please explain how that is fair at all?

All participants who voiced concerns over insufficient scaling or incentivisation of higher mathematics courses based their reasoning upon a perceived difference in difficultly between courses (e.g., Methods and Applications), a drastically different scaling method to be used for easier or more difficult courses, the maximisation of the ATAR by taking the easier mathematics course, and the incentive offered to students from 2017 onwards. Irrespective of reason, all participants expressed that scaling procedures influenced their decision not to enrol in a higher mathematics course.

### Conclusion

The purpose of this research paper was to outline reasons why Year 11 and Year 12 ATAR mathematics students in Western Australia do not enrol in higher-level mathematics courses. I identified three key findings via Likert-scale items (Table 4) and open questions (Table 5) for further consideration. First, students indicated dissatisfaction with the

perceived discrepancy in difficulty of Methods and Applications courses currently offered in Western Australian schools. Aside from the apparent "jump" in content complexity between these courses, students feel that the time and effort spent on undertaking a more difficult course (i.e., Methods) is unrewarded. At the same time, students suggested that the creation of a mathematics course whose level of difficulty lay in between Methods and Applications would assist in reducing the current discrepancy and consequently encourage more students to enrol in it.

Second, students feel that undertaking an easier mathematics course will allow additional time to focus on other ATAR courses. The themes associated with this finding suggest that students are interested in adopting a balanced approach to their studies where they can apportion a similar amount of time and effort to mathematics as their other ATAR courses for maximal reward. Additionally, there appears to be an expressed need by students to feel confident in the mathematics course they take; this confidence is brought about by choosing a course where the content can be mastered and the level of stress associated with such mastery is not atypically high compared with other ATAR courses.

Third, students believe that there is an insufficient reward offered for taking a higher mathematics course. For the most part, students nominated that the scaling procedures or a lack of incentivisation deterred them from enrolling in a more difficult course. Interestingly, at the time of data collection, neither the Year 11 nor Year 12 students involved in the study had any foreknowledge of how the scaling process in Western Australia had worked for previous Mathematics Applications, Mathematics Methods, and Mathematics Specialist student cohorts; they would become the first and second cohorts, respectively. Some Year 12 students lamented that in 2017 – when they had completed secondary schooling – they would miss out on the incentive offered by the Tertiary Institutions Service Centre (TISC) to students completing Mathematics Methods and/or Mathematics Specialist courses. Students completing either the Methods course or both Methods and Specialist courses will receive a 10 percent bonus of their final scaled score in those courses (TISC, 2016).

This study builds on the previous research conducted in Western Australia regarding student enrolments in senior secondary mathematics courses (Hine, 2016), in that it sought to engage the student voice. The findings outlined illustrate various tensions regarding students' decisions not to enrol in a higher-level mathematics course. These tensions appeared to focus more on the students' short-term goals (e.g., achieving a higher ATAR in an easier course for reduced effort and stress) rather than on the mastery of mathematical concepts required for a career or for further study. Based on these findings, future research efforts could be directed at asking the Year 11 and Year 12 participants the extent to which they feel their choice of secondary mathematics course prepared them adequately for the future (i.e., a longer-term goal). Other efforts could focus on a replica study in the next few years, especially once the bonus marks system for Methods and Specialist has been introduced.

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